# Bound-valence-quark contributions to hadron structure functions

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The conventional separation of "valence"- and "sea"-quark distributions of a hadron implicitly assumes that the quark and antiquark contributions to the sea are identical in shape, although this cannot be strictly correct due to the exclusion principle. A new separation of "bound-valence"- and -"non-valence"- quark distributions of a hadron is proposed which incorporates the Pauli principle and relates the valence component to the wave functions of the bound-state valence constituents. With this new definition, the non-valence-quark distributions correspond to structure functions which would be measured if the valence quarks of the target hadron were chargeless. The bound-valence-quark distributions are not singular at small x, thus allowing for the calculation of sum rules and expectation values which would otherwise be divergent.

## I. INTRODUCTION

Deep-inelastic lepton scattering and lepton-pair production experiments measure the light-cone longitudinal-momentum distributions  $x = (k_q^0 + k_q^z)/p_H^0 + p_H^z)$  of quarks in hadrons through the relation

$$F_2^H(x,Q^2) = \sum_q e_q^2 x G_{q/H}(x,Q^2) .$$
 (1)

 $F_2^H(x,Q^2)$  is the leading-twist structure function at the momentum-transfer scale Q. Four-momentum conservation at large  $Q^2$  then leads to the identification  $x = x_{Bj} = Q^2/2p \cdot q$ . In principle, the distribution functions  $G_{q/H}$  could be computed from the bound-state solutions of QCD.<sup>1</sup> For example, given the wave functions  $\psi_{n/H}^{(Q)}(x_i, \mathbf{k}_{\perp_i}, \lambda_i)$  in the light-cone Fock expansion of the hadronic state, one can write the distribution function in the form<sup>2</sup>

$$G_{q/H}(x,Q^2) = \sum_{n,\lambda_i} \int \prod_i \frac{dx_i d^2 k_{\perp_i}}{16\pi^3} |\psi_{n/H}^{(Q)}(x_i,\mathbf{k}_{\perp_i},\lambda_i)|^2$$

$$\times \sum_{b=q} \delta(x_b - x) . \tag{2}$$

Here  $x_i = k_i^+ / p_H^+ = (k_i^0 + k_i^z) / (p_H^0 + p_H^z)$  is the light-cone momentum fraction of each constituent, where  $\sum_i x_i = 1$ and  $\sum_i k_{\perp_i} = 0$  in each Fock state *n*. The sum is over all Fock components *n* and helicities  $\lambda_i$ , integrated over the unconstrained constituent momenta.

An important concept in the description of any bound state is the definition of "valence" constituents. In atomic physics the term "valence electrons" refers to the electrons beyond the closed shells which give an atom its chemical properties. Correspondingly, the term "valence quarks" refers to the quarks which give the bound-state hadron its global quantum numbers. In quantum field theory, bound states of fixed particle number do not exist; however, the expansion Eq. (2) allows a consistent definition of the valence quarks of a hadron: the valence quarks appear in each Fock state together with any number of gluons and quark-antiquark pairs; each component thus has the global quantum numbers of the hadron.

How can one identify the contribution of the valence quarks of the bound state with the phenomenological structure functions? Traditionally, the distribution function  $G_{q/H}$  has been separated into "valence" and "sea" contributions:<sup>3</sup>  $G_{q/H} = G_{q/H}^{val} + G_{q/H}^{sea}$ , where, as an operational definition, one assumes

$$G_{q/H}^{\text{sea}}(x,Q^2) = G_{\bar{q}/H}^{\text{sea}}(x,Q^2) \quad (0 < x < 1)$$
(3)

and thus  $G_{q/H}^{\text{val}}(x, Q^2) = G_{q/H}(x, Q^2) - G_{\overline{q}/H}(x, Q^2)$ . The assumption of identical quark and antiquark sea distributions is reasonable for the s and  $\overline{s}$  quarks in the proton. However, in the case of the *u*- and *d*-quark contributions to the sea, antisymmetrization of identical quarks in the higher Fock states implies nonidentical q and  $\overline{q}$  sea contributions. This is immediately apparent in the case of atomic physics, where Bethe-Heitler pair production in the field of an atom does not give symmetric electron and positron distributions since electron capture is blocked in states where an atomic electron is already present. Similarly in QCD, the  $q\bar{q}$  pairs which arise from gluon splitting as in Fig. 1(a) do not have identical quark and antiquark sea distributions; contributions from interference diagrams such as Fig. 1(b), which arise from the antisymmetrization of the higher Fock state wave functions, must be taken into account. Although the integral of the conventional valence distribution gives correct charge sum rules, such as  $\int_0^1 dx [G_{q/H}(x) - G_{\overline{q}/H}(x)]$ , it can give a misleading reading of the actual momentum distribution of the valence quarks.

The standard definition also has the difficulty that the derived valence-quark distributions are apparently singu-



FIG. 1. Structure function contributions from the threequark plus one pair Fock state of the proton. The  $d\bar{d}$  pair in diagram (a) contributes to the sea distribution, but diagram (b) due to antisymmetrization of the *d* quarks cannot be separated uniquely into "valence" vs "sea" parts.

lar in the limit  $x \rightarrow 0$ . For example, standard phenomenology indicates that the valence up-quark distribution in the proton behaves as  $G_{u/p}^{\text{val}} \sim x^{-\alpha_R}$  for small  $x^{3,4}$  where  $\alpha_R \approx 0.5.^5$  This implies that quantities that depend on the  $\langle 1/x \rangle$  moment of the valence distribution diverge. This is the case for the "sigma term" in current algebra and the J=0 fixed pole in Compton scattering.<sup>6</sup> Furthermore, it has been shown<sup>7</sup> that the change in mass of the proton when the quark mass is varied in the light-cone Hamiltonian is given by an extension of the Feynman-Hellman theorem:

$$\frac{\partial M_p^2}{\partial m_q^2(Q^2)} = \int_0^1 \frac{dx}{x} G_{q/p}(x, Q^2) .$$
(4)

In principle, this formula allows one to compute the contribution to the proton-neutron mass difference due to the difference of up- and down-quark masses. However, again, with the standard definition of the valence-quark distribution, the integration is undefined at low x. Even more seriously, the expectation value of the light-cone kinetic energy operator

$$\int_{0}^{1} dx \frac{\langle k_{\perp}^{2} \rangle + m^{2}}{x} G_{q/p}(x, Q)$$
(5)

is infinite for valence quarks if one uses the traditional definition. There is no apparent way of associating this divergence of the kinetic energy operator with renormalization.<sup>8</sup> Notice that a divergence at x=0 is an ultraviolet infinity for a massive quark, since it implies  $k^+=k^0+k^z=0$ ; i.e.,  $k^z\to -\infty$ . A bound-state wave function would not be expected to have support for arbitrarily large momentum components.

Part of the difficulty with identifying bound-state contributions to the proton structure functions is that many physical processes contribute to the deep-inelastic lepton-proton cross section: From the perspective of the laboratory or center-of-mass frame, the virtual photon can scatter out a bound-state quark as in the atomicphysics photoelectric process, or the photon can first make a  $q\bar{q}$  pair, either of which can interact in the target. As we emphasize here, in such pair-production processes, one must take into account the Pauli principle which forbids creation of a quark in the same state as one already present in the bound-state wave function. Thus the lepton interacts with quarks which are both *intrinsic* to the proton's bound-state structure, and with quarks which are *extrinsic*, i.e., created in the electron-proton collision itself. Note that such extrinsic processes would occur in electroproduction even if the valence quarks had no charge. Thus much of the phenomena observed in electroproduction at small values of x, such as Regge behavior, sea distributions associated with photon-gluon fusion processes, and shadowing in nuclear structure functions should be identified with the extrinsic interactions, rather than processes directly connected with the proton's bound-state structure.

In this paper we propose a definition of "boundvalence-quark" distribution functions that correctly isolates the contribution of the valence constituents which give the hadron its flavor and other global quantum numbers. In this new separation,  $G_{q/p}(x,Q^2) = G_{q/p}^{BV}(x,Q^2)$  $+G_{q/p}^{NV}(x,Q^2)$ , non-valence-quark distributions are identified with the structure functions which would be measured if the valence quarks of the target hadron had zero electroweak charge. We shall prove that with this new definition the bound-valence-quark distributions  $G_{q/p}^{BV}(x,Q^2)$  vanish at  $x \rightarrow 0$ , as expected for a boundstate constituent.

## II. CONSTRUCTION OF BOUND-VALENCE-QUARK DISTRIBUTIONS

In order to construct the bound-valence-quark distribution, we imagine a gedanken QCD where, in addition to the usual set of quarks  $\{q\} = \{u, d, s, c, b, t\}$ , there is another set  $\{q_0\} = \{u_0, d_0, s_0, c_0, b_0, t_0\}$  with the same spin, masses, flavor, color, and other quantum numbers, except that their electromagnetic charges are zero.

Let us now consider replacing the target proton p in the lepton-proton-scattering experiment by a chargeless proton  $p_0$  which has valence quarks  $q_0$  of zero electromagnetic charge. In this extended QCD the higher Fock wave functions of the proton p and the chargeless proton  $p_0$  both contain  $q\bar{q}$  and  $q_0\bar{q}_0$  pairs. As far as the strong QCD interactions are concerned, the physical proton and the gedanken chargeless proton are equivalent.

We define the bound-valence-structure function of the proton from the difference between scattering on the physical proton minus the scattering on the chargeless proton, in analogy to an "empty target" subtraction:

$$F_i^{\rm BV}(x,Q^2) \equiv F_i^p(x,Q^2) - F_i^{p_0}(x,Q^2) .$$
(6)

The nonvalence distribution is thus  $F_i^{NV}(x,Q^2)$ = $F_i^{p_0}(x,Q^2)$ . The  $F_i(x,Q^2)$  (i=1,2) are the leadingtwist structure functions, with  $F_{2H}^{BV}(x,Q^2)$ =  $\sum_q e_q^2 x G_{q/H}^{BV}(x,Q^2)$ , etc. The situation just described is similar to the atomic-physics case, where, in order to correctly define photon scattering from a bound electron, one must subtract the cross section on the nucleus alone, without that bound electron present.<sup>9</sup> Physically the nucleus can scatter photons through virtual pair production, and this contribution has to be subtracted from the total cross section. In QCD we cannot construct protons without the valence quarks; thus we need to consider hadrons with chargeless valence constituents.<sup>10</sup>

Notice that the cross section measured in deepinelastic lepton scattering on  $p_0$  is not zero. This is because the incident photon (or vector boson) creates virtual  $q\bar{q}$  pairs which scatter strongly in the gluonic field of the chargeless proton target. In fact at small x the inelastic cross section is dominated by J=1 gluon-exchange contributions, and thus the structure functions of the physical and chargeless protons become equal:

$$\lim_{x \to 0} \left[ F_i^p(x, Q^2) - F_i^{p_0}(x, Q^2) \right] = 0 .$$
(7)

Remarkably, as shown in Sec. IV, the bound-valencequark distribution function  $G_{q/H}^{BV}$  vanishes at  $x \to 0$ ; it has neither Pomeron  $x^{-1}$  nor Reggeon  $x^{-\alpha_R}$  contributions.

Although the gedanken subtraction is impossible in the real world, we will show that, nevertheless, the bound-valence distribution can be analytically constrained at small  $x_{bj}$ . This opens up the opportunity to extend present phenomenology and relate measured distributions to true bound-state wave functions.

In the following sections we will analyze both the atomic and hadronic cases, paying particular attention to the high-energy regime.

### **III. ATOMIC CASE**

Since it contains the essential features relevant for our discussion, we will first analyze photon scattering from an atomic target. This problem contains an interesting paradox which was first resolved by Goldberger and Low in 1968.<sup>9</sup> Here we give a simple, but explicit, derivation of the main result.

The Kramers-Kronig dispersion relation relates the forward Compton amplitude to the total photoabsorptive cross section<sup>11</sup>

$$f(k) - f(0) = \frac{k^2}{2\pi^2} \int_0^\infty dk' \frac{\sigma(k')}{k'^2 - k^2 - i\epsilon} , \qquad (8)$$

where k is the photon energy. One should be able to apply this formula to scattering on a bound electron  $(e_b)$  in an atom. However, there is an apparent contradiction. On the one hand, one can explicitly compute the highenergy  $\gamma e_b \rightarrow \gamma e_b$  forward amplitude: it tends to a constant value at  $k \rightarrow \infty$ , the electron Thomson term,  $f(k) \rightarrow -e^2/m_b^e$ , where  $m_b^e$  is the effective electron mass corrected for atomic binding.<sup>12</sup> One the other hand, the  $O(e^2)$  cross section for the photoelectric effect  $\gamma e_b \rightarrow e'$  behaves as  $\sigma_{\text{photo}} \sim 1/k$  at high energies. But then the dispersion integral in Eq. (8) predicts logarithmic behavior for f(k) at high energy in contradiction to the explicit calculation. Evidently other contributions to the inelastic cross section cannot resolve this conflict.

This problem was solved<sup>9</sup> by carefully defining what one means by scattering on a bound-state electron. For both the elastic Compton amplitude and the inelastic cross section one must subtract the contribution in which the photon scatters off the Coulomb field of the nucleus (empty target subtraction). Thus  $\sigma(k)$  in Eq. (8) is really the difference between the total atomic cross section  $\sigma_{atom}(k)$  and the nuclear cross section  $\sigma_{nucleus}(k)$ , which is dominated by pair production. We will present a simple proof that the high-energy behavior  $\sim 1/k$  of the cross sections exactly cancels in this difference, which is a necessary condition for a consistent dispersion relation.

The total cross section for photon scattering on the atom is dominated by two main terms: the photoelectric contribution and  $e^+e^-$  pair production, with the produced electron going into a different state than the electron already present in the atom.<sup>13</sup> On the other hand, in the subtraction, pair production in the field of the nucleus is not restricted by the Pauli principle; this cross section contains a contribution where the produced electron goes into the same state as the bound-state electron of the atom, plus other terms in which it goes into different states. These last contributions cancel in the difference  $\sigma_{\rm atom} - \sigma_{\rm nucleus}$ . Thus the bound-state electron photoabsorption cross section is the difference between the photoelectric cross section on the atom and the pairproduction capture cross section on the nucleus, where the produced electron is captured in the same state as the original bound-state electron:  $\sigma_{e_b} = \sigma_{\text{photoelectric}} - \sigma_{\text{capture}}$ . This is depicted graphically in Fig. 2.

We next note that the squared amplitude for the capture process  $\gamma Z \rightarrow e^+$  atom is equal, by charge conjugation, to the squared amplitude for  $\gamma \overline{Z} \rightarrow e^-$  atom. (See Fig. 3.) Furthermore, by crossing symmetry, the (helicity-summed) squared amplitude for this last process is equal to the (helicity-summed) squared amplitude for  $\gamma \operatorname{atom} \rightarrow e^- Z$ , with  $p_Z$  and  $(-p_{\operatorname{atom}})$  interchanged. This is equivalent to the interchange of the Mandelstam variables  $s = (p_{\gamma} + p_Z)^2$  and  $u = (p_{\gamma} - p_{\operatorname{atom}})^2$ . Thus at high photon energies (where  $s \simeq -u$ ), the two cross sections  $\sigma_{\operatorname{photoelectric}}$  and  $\sigma_{\operatorname{capture}}$  of Fig. 2 cancel, consistent with the Kramers-Kronig relation. In Regge language, the imaginary part of the J=0 Compton amplitude is zero.

The proof we have presented implicitly assumes the equality of the flux factors for the photoelectric process on the atom and the capture process on the nucleus. This is normally a good approximation since the atomic and nuclear masses are almost identical for  $M_Z \gg m_e$ . How-



FIG. 2. The bound-electron photoabsorption cross section  $\sigma_{\gamma e_b}$  is defined as the difference of  $\gamma$ -atom and  $\gamma$ -nucleus cross sections. This can also be expressed as the difference between the atomic "photoelectric" cross section and the pairproduction "capture" cross section on the nucleus, but with the produced electron going into the same atomic state as the original bound-state electron.



FIG. 3. The helicity-summed squared amplitude for the process  $\gamma Z \rightarrow e^+$  atom is equal, by charge conjugation, to the helicity-summed squared amplitude for  $\gamma \overline{Z} \rightarrow e^-$  atom, up to a phase. This is also equal by crossing to the helicity-summed squared amplitude for the process  $\gamma \operatorname{atom} \rightarrow e^- Z$ , but with s and u interchanged.

ever, for finite mass systems such as muonic atoms, the mass of the nucleus and atom are unequal, and the cross sections do not cancel at high energy. The difficulty in this case is that the nucleus does not provide the correct "empty target" subtraction.

However, we can extend the analysis to the general atomic problem by considering hypothetical atoms  $A_0$ consisting of null leptons  $l_0$  with normal electromagnetic and Coulomb interactions with the nucleus but with zero external charge. [In effect, we consider an extended QED with U(1)×U(1) gauge interactions, where the null lepton has charge (-1,0), and the normal lepton and nucleus have charges (-1,-1) and (Z,Z), respectively.] The empty target subtraction is defined as the difference between the cross section on the normal atom A = (Zl) and the cross section on the null atom  $A_0 = (Zl_0)$ . Since the mass and binding interactions of A and  $A_0$  are identical, the photoabsorption flux factors are the same in both cases.

As in the earlier proof, the matrix element for the photoelectric process on the atom A becomes equal in modulus at high energies with the matrix element for the capture process on the null atom  $A_0$ . Note that in the computation of the capture process amplitude, the presence of the spectator lepton  $l_0$  is irrelevant since it remains in the original quantum state (say, 1S): The required matrix element of the current is

$$\langle Al_0(1S)l^+|J^{\mu}|A_0\rangle = \langle Al_0(1S)l^+|\overline{\psi}_l\gamma^{\mu}\psi_lb_{l_0}^{\dagger}(1S)|Z\rangle$$
$$= \langle Al^+|J^{\mu}|Z\rangle .$$

By charge conjugation and crossing this is equal in modulus to

$$\langle Zl^{-}|J^{\mu}|A\rangle$$
,

the corresponding photoelectric matrix element with  $s \rightarrow u$ . Final-state interactions can only affect the phase at high energies. Thus we obtain cancellation of the photoelectric and capture cross sections at high energies, and verify the Kramers-Kronig dispersion relation for Compton scattering on leptons bound to finite mass nuclei.

#### **IV. REGGEON CANCELLATIONS IN QCD**

We now return to the analysis of the "bound-valencequark distributions" of the proton. According to the discussion of Sec. II, the measurement of the boundvalence-quark distribution requires an "empty target" subtraction:

$$\sigma(\gamma^* p \to X) - \sigma(\gamma^* p_0 \to X) \; .$$

Both p and  $p_0$  contain higher Fock states with arbitrary number of gluons,  $q\bar{q}$ , and  $q_0\bar{q}_0$  pairs. It is clear that the terms associated with  $J \approx 1$  Pomeron behavior due to gluon exchange cancel in the difference. In this section we shall prove that the Reggeon terms also cancel, and thus the resulting distribution of bound-valence quarks  $G_{q/p}^{BV}(x, Q^2)$  vanishes as  $x \rightarrow 0$ .

As in the atomic case, we now proceed to describe the leading contributions to the scattering of a photon from both the proton p and the state  $p_0$ . For simplicity of notation, we will consider an example which isolates just the bound-valence d-quark distribution of the proton p(uud); in this case the subtraction term is the deepinelastic cross section on the system  $p_0(uud_0)$  in which the  $d_0$  valence quark has normal QCD interactions but does not carry electric charge. The general case, corresponding to the definition of Eq. (6), where the subtraction is on the completely neutral state  $p_0(u_0u_0d_0)$ , is a simple generalization. The high  $Q^2$  virtual photoabsorption cross section on the proton (laboratory frame) contains two types of terms: contributions in which a quark in p absorbs the momentum of the virtual photon; and terms in which a  $q\bar{q}$  pair is created, but the produced q is in a different quantum state than the quarks already present in the hadron. On the other hand, the cross section for scattering of the virtual photon from the state  $p_0(uud_0)$  contains contributions that differ from the p(uud) case in two important aspects: first the virtual photon can be absorbed only by charged quarks; and in  $d\overline{d}$  pair production on the null proton  $p_0$ , the d quark can be produced in any state. Thus the difference between the cross sections off p and  $p_0$  equals a term analogous to  $\sigma_{\rm photoelectric}$  in which a d quark in p absorbs the photon momentum, minus a  $d\overline{d}$  pair-production contribution on  $p_0$  analogous to  $\sigma_{\text{capture}}$ , in which the produced d quark ends up in the same quantum state as the d quark in the original proton state p. This is shown graphically in Fig. 4.<sup>1</sup>

Reggeon behavior in the electroproduction cross section can be understood as due to the appearance of a spectrum of bound  $q\bar{q}$  states in the *t* channel. The absorptive cross section associated with *t*-channel ladder diagrams is depicted in Fig. 5(a). The summation of such diagrams leads to Reggeon behavior of the deep-inelastic structure functions at small x.<sup>15</sup> In the rest system, the virtual photon creates a  $d\bar{d}$  pair at a distance proportional to 1/x before the target. The radiation which occurs over this distance contributes to the physics of the Reggeon behavior.

A corresponding Reggeon contribution at low x also occurs in the subtraction term indicated in Fig. 5(b). In the case of the proton target, the d quark, after radiation, cannot appear in the quantum state already occupied by the d quark in the proton because of the Pauli principle. However, the corresponding contribution is allowed on the  $p_0$  target: in effect, the d quark replaces the  $d_0$  quark and is captured into a proton. The capture cross section is computed from the amplitude for  $\gamma^* p_0 \rightarrow \overline{d}^* p d_0^{1.5}$ .<sup>16</sup> As in the corresponding atomic-physics analysis, the



FIG. 4. The bound-valence-quark distribution of quark d can be calculated from the difference between (a) the cross section on the state p in which the virtual-photon momentum is absorbed by the quark d, and (b) the  $d\overline{d}$  pair-production cross section in the field of  $p_0$ , but with the produced d quark ending in the same state as the d quark in the original proton state p.

spectator  $d_0$  quark in the null target  $p_0$  is inert and cancels out from the amplitude. Thus we only need to consider effectively the (helicity-summed) squared amplitude for  $\gamma^*(uu) \rightarrow \overline{d}^*p$ . However, as illustrated in Fig. 6 this amplitude, after charge conjugation and crossing  $s \rightarrow u$ , is equal to the (helicity-summed)  $\gamma^*p \rightarrow d^*(uu)$  squared amplitude at small x. The flux factors for the proton and null proton target are equal.

If we write  $s\sigma_{\text{photoelectric}}$  as a sum of Regge terms of the form  $\beta_R |s|^{\alpha_R}$ , where  $\alpha_R > 0$ , then the subtraction of the capture cross section on the null proton will give the net virtual photoabsorption cross section as a sum of terms  $s\sigma^{\text{BV}} = \sum_R \beta_R (|s|^{\alpha_R} - |u|^{\alpha_R})$ . If we ignore mass corrections in leading twist, then  $s \simeq Q^2(1-x)/x$  and  $u \simeq -Q^2/x$ . Thus for small x every Regge term is multiplied by a factor  $K_R = (-\alpha_R)x$ . For example, for  $\alpha_R = \frac{1}{2}$ (which is the leading even charge-conjugation Reggeon contribution for nonsinglet isospin structure functions),  $F_2^{p(uud)} - F_2^{p_0(uud_0)} \sim x^{3/2}$ . The bound-valence-quark nonsinglet (I=1) distribution thus has leading behavior  $G_{q/H}^{\text{BV}} \sim x^{1/2}$  and vanishes for  $x \to 0$ . We can also understand this result from symmetry con-

We can also understand this result from symmetry considerations. We have shown from crossing symmetry  $G_{q/p}(x,Q^2) - G_{\overline{q}/p_0}(x,Q^2) \rightarrow 0$  at low x. Thus the even charge-conjugation Reggeon and Pomeron contributions decouple from the bound-valence-quark distributions.



FIG. 5. Amplitudes describing Reggeon behavior at small x (a) in electroproduction, and (b) in the subtraction term of Fig. 4(b).



FIG. 6. The helicity-summed squared amplitude for (a)  $\gamma^* p \rightarrow d^*(uu)$  is equal, by charge conjugation, to the helicitysummed squared amplitude for the process (b)  $\gamma^* \overline{p} \rightarrow \overline{d}^*(\overline{uu})$ , up to a phase. This is also equal, by crossing symmetry, to the helicity-summed squared amplitude for (c)  $\gamma^*(uu) \rightarrow \overline{d}^* p$ , with s and u interchanged. Thus at high energies the Reggeon contribution from the subtraction term of Fig. 5(b) cancels the Reggeon contribution of Fig. 5(a).

The analytic cancellation of the leading Reggeon contributions of the *s*-channel and *u*-channel contributions suggests that, given sufficiently detailed Regge fits to the data for the nonsinglet structure functions, one could construct a phenomenological model for the boundvalence-quark distributions. Eventually, lattice gauge theory or other nonperturbative methods for solving QCD, such as discretized light-cone quantization,<sup>1</sup> may provide detailed first-principles predictions for the bound-valence-quark distributions which could be compared with the phenomenological forms.

### **V. CONCLUSIONS**

The observation that the deep-inelastic lepton-proton cross section is nonzero, even when the quarks in the target hadron carry no charge, implies that we should distinguish two separate contributions to deep-inelastic lepton scattering: intrinsic (bound-state) and extrinsic (nonbound) structure functions. The extrinsic contributions are created by the virtual strong interactions of the lepton itself, and are present even if the quark fields of the target are chargeless. The bound-valence-quark distributions, defined by subtracting the distributions for a gedanken "null" hadron with chargeless valence quarks, correctly isolate the valence-quark contributions intrinsic to the bound-state structure of the target. As we have shown, both the Pomeron and leading Reggeon contributions are absent in the bound-valence-quark distributions. The leading Regge contributions are thus associated with particles created by the photon-hadron scattering reaction, processes extrinsic to the bound-state physics of the target hadron itself. The bound-valence-quark distributions are in principle computable by solving the boundstate problem in QCD. Sum rules for the proton derived from properties of the hadronic wave function thus apply to the bound-valence-quark contributions. In particular, the light-cone kinetic energy of the bound-valence quarks,

$$\int_0^1 dx \frac{\langle k_\perp^2 \rangle + m^2}{x} G_{q/p}^{\text{BV}}(x, Q) , \qquad (9)$$

is finite, as expected for a bound-state wave-function contribution. The ultraviolet divergence of the kinetic energy obtained from the nonvalence distribution is associated with the production of high mass states in the electron-proton collision, rather than the distribution of the bound-state-valence quarks.

The essential reason why the new definition of the bound-valence-quark distribution differs from the conventional definition of valence distributions is the Pauli principle: the antisymmetrization of the bound-state wave function for states which contain quarks of identical flavor. As we have shown, this effect plays a dynamical role at low x, eliminating leading Regge behavior in the bound-valence-quark distributions. In the atomic-physics case, where the leading Regge behavior corresponds to  $J = \alpha_R = 0$ , the analogous application of the

Pauli principle leads to analytic consistency with the Kramers-Kronig dispersion relation for Compton scattering on a bound electron.

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- <sup>5</sup>The position  $\alpha_R$  of *J*-plane singularities in the forward virtual Compton amplitude are  $Q^2$  independent, and thus the nonsinglet Reggeon behavior  $F_2^{NS}(x,Q^2) \sim x^{1-\alpha_R}$  at  $x \to 0$  must be unaffected by QCD evolution. We thank J. Collins for conversations on this point.
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- <sup>8</sup>One can identify the ultraviolet divergences at  $x \rightarrow 0$  of Eqs. (4) and (5) for sea quarks with the renormalization of the gluon

propagator (which cancels in the proton-neutron mass difference).

- <sup>9</sup>M. L. Goldberger and F. E. Low, Phys. Rev. **176**, 1778 (1968); see also T. Erber, Ann. Phys. (N.Y.) **6**, 319 (1959).
- <sup>10</sup>Strictly speaking, the bound-valence structure function of the proton refers to a proton in the extended QCD which contains chargeless quark pairs. Since these quarks are spectators in the deep-inelastic lepton-proton cross sections, this should be a minor effect.
- <sup>11</sup>For discussion and references, see M. Damashek and F. J. Gilman, Phys. Rev. D 1, 319 (1970).
- <sup>12</sup>We neglect here the  $O(e^6)$  light-by-light scattering contributions to the forward Compton amplitude.
- <sup>13</sup>To leading order in  $\alpha$  we can ignore higher-order processes in the total cross section such as Compton scattering.
- <sup>14</sup>We neglect processes higher order in  $\alpha_{\text{QED}}$  such as pair production in the electromagnetic field of the quark *d*.
- <sup>15</sup>For a derivation of the Reggeon contribution to the leadingtwist structure functions, see P. V. Landshoff, J. C. Polkinghorne, and R. Short, Nucl. Phys. **B28**, 224 (1971), and S. J. Brodsky, F. E. Close, and J. F. Gunion, Phys. Rev. D 8, 3678 (1973).
- <sup>16</sup>As usual we neglect hadronization effects and other final-state interactions at high energies.