

## Effects of exotic composite bosons in $e^+e^-$ scattering at 50–100 GeV

Keiichi Akama

*Department of Physics, Saitama Medical College, Kawakado, Moroyama, Saitama 350-04, Japan*

Takashi Hattori

*Department of Physics, Kanagawa Dental College, Inaokacho, Yokosuka, Kanagawa 238, Japan*

Masaki Yasuè

*Institute for Nuclear Study, University of Tokyo, Midori-cho, Tanashi, Tokyo 188, Japan*

(Received 6 February 1990)

We show that some of the neutral exotics in the composite model decouple from neutrinos at low energies, and can be as light as the mass scale of the weak interactions, offering the possibility of detecting sizable effects in  $e^+e^-$  scattering at 50–100 GeV.

Regularities in the quark-lepton spectra seem to suggest a further fundamental layer of matter, the subquark (or preon).<sup>1–3</sup> For example, the proliferation of color triplets and weak isodoublets may indicate the subquarks  $c$  and  $w$ , the common carriers of the color and the weak isospin, respectively. In this picture, weak bosons, Higgs-boson scalars, and even the photon and gluon could also be composite.<sup>2</sup> The composite models predict various new phenomena at energies as high as the compositeness scale. New exotic and excited states should appear,<sup>4</sup> the scattering cross sections should deviate from their standard-model values due to their size effects,<sup>5</sup> and subquarks should develop jets consisting of quarks, leptons, and intermediate bosons.<sup>6</sup> From the argument of unnaturalness in the mass renormalization of the Higgs-boson sector in the standard model, the scale of new physics cannot be much beyond the TeV region.<sup>7</sup> If compositeness is responsible for avoiding unnaturalness, the above-mentioned phenomena would be observed in this region. In particular, we expect that the ground states of the neutral exotics can be observed at comparatively low energies. In this paper we examine the possibilities of observing their effects in the energy regions of the experiments with the  $e^+e^-$  colliders such as TRISTAN at KEK, the SLAC Linear Collider (SLC), and LEP at CERN.

The neutral exotics should exhibit their effects also in  $p\bar{p}$  scattering, neutrino scattering, the anomalous magnetic moments of leptons, and the  $Z$ -boson mass deviation via mixing. Among them, neutrino scattering places the most severe restriction on their masses—larger than a few hundred GeV. Accordingly, they cannot affect  $e^+e^-$  scattering at 50–100 GeV so much, as long as they couple to neutrinos. The same restriction arises for the extra  $Z$  boson(s) in the grand unified and superstring-inspired models.<sup>8</sup> However, some of the neutral exotics in the composite models may decouple from neutrinos at low energies and are free from the restriction. We consider, as examples, (i) the “color-singlet gluon,” the vector boson made of  $c$  and  $\bar{c}$ , where  $c$  is the subquark carrying the

three colors and (ii) the heavy (excited) photon, which couples to matters with the strength proportional to their electric charges. For the purpose of comparison we also examine the effects of (iii) the “leptonic gluon,”<sup>9</sup> the vector boson made of  $c_l$  and  $\bar{c}_l$ , where  $c_l$  is the subquark carrying leptonic color, although this particle does couple to neutrinos.

Let us denote the exotic vector boson by  $V_\mu$ . It is mixed with the photon  $\tilde{A}_\mu$  (tilded because it is yet to be diagonalized to form the physical photon) and the neutral component of  $W_\mu^3$  of the weak boson through

$$\mathcal{L}_{\text{mix}} = -\frac{1}{2}\lambda\tilde{A}_{\mu\nu}W^{3\mu\nu} - \frac{1}{2}\lambda'\tilde{A}_{\mu\nu}V^{\mu\nu} - \frac{1}{2}\lambda''W_{\mu\nu}^3V^{\mu\nu} + \Delta M^2W_\mu V^\mu, \quad (1)$$

where  $B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu$  for the vector field  $B_\mu$  in general;  $\lambda$ ,  $\lambda'$ , and  $\lambda''$  are the current mixing parameters and  $\Delta M$  is the mass mixing parameter. These bosons couple to matters through

$$\mathcal{L}_{\text{int}} = eJ_\mu^{\text{em}}\tilde{A}^\mu + gJ_\mu^3W^{3\mu} + g_VJ_\mu^V V^\mu, \quad (2)$$

where  $e$  is the electromagnetic coupling constant,  $g$  is the weak coupling constant,  $g_V$  is the coupling constant of  $V_\mu$ ,  $J_\mu^{\text{em}}$  is the electromagnetic current,  $J_\mu^3$  is the neutral component of the weak-isospin current, and  $J_\mu^V$  is the current of  $V_\mu$ . As Hung and Sakurai pointed out, if and only if

$$\lambda = e/g, \quad (3)$$

then the known sector of the photon and weak bosons exactly coincides with that in the standard model,<sup>10</sup> and the model is phenomenologically acceptable.

The mixing parameters, the coupling constants, and the form of  $J_\mu^V$  should be determined by the dynamics of the subquarks. People considered two complementary types of dynamics: that of the Nambu–Jona-Lasinio–Bjorken type<sup>11,12</sup> and that with fundamental gauge interactions.<sup>13,14</sup> The former is perturbatively solvable for composite states, though it requires an explicit

momentum cutoff, and is not renormalizable. On the other hand, the latter is renormalizable and confining under appropriate conditions, while it is in general difficult to get explicit solutions for composite states. The latter, however, also includes cases where we can explicitly determine the composite spectrum<sup>14</sup> by virtue of complementarity between the Higgs phase and the confining phase.<sup>15</sup> To see the consequences of these dynamical models, we actually examined the following typical ones: (a) a model of the Nambu–Jona-Lasinio type and (b) an  $SU(2)_L \times U(1) \times U(1)'$  gauge model, which are the straightforward extensions of the models in Refs. 16 and 17, respectively. The procedures illustrated in Refs. 16 and 17 lead to the following results. The relation (3) is safely satisfied, and

$$\lambda' = eQ_{c_l}/g_V, \quad \lambda'' = 0, \quad J_\mu^V = J_\mu^l \quad \text{for } V_\mu = \text{leptonic gluon}, \quad (4a)$$

$$\lambda' = eQ_c/g_V, \quad \lambda'' = 0, \quad J_\mu^V = J_\mu^q \quad \text{for } V_\mu = \text{color-singlet gluon}, \quad (4b)$$

$$\lambda' = e/g_V, \quad \lambda'' = g_V/g, \quad J_\mu^V = J_\mu^{\text{em}} \quad \text{for } V_\mu = \text{heavy photon}, \quad (4c)$$

and  $\Delta M^2 = 0$  for each case, where  $Q_{c_l} = -\frac{1}{2}$  and  $Q_c = \frac{1}{6}$  are the electric charge of the subquark  $c$  and  $c_l$ , respectively, and  $J_\mu^l$ ,  $J_\mu^q$ , and  $J_\mu^{\text{em}}$  are, respectively, the lepton number current, the quark number current, and the electromagnetic current of quarks and leptons. The heavy photon is equivalent to the boson  $V'_\mu$  that couples to the weak hypercharge current  $J_\mu^Y$ , whose interactions are described by

$$\mathcal{L}'_{\text{int}} = eJ_\mu^{\text{em}} \tilde{A}^\mu + gJ_\mu^3 W'^{3\mu} + g'_V J_\mu^Y V'^\mu, \quad (2')$$

and  $\mathcal{L}_{\text{mix}}$  in (1) with

$$\begin{aligned} \lambda &= e/g, \quad \lambda' = e/g'_V, \\ \lambda'' &= 0, \\ \Delta M^2 &= g'_V M_W^2/g, \end{aligned} \quad (4')$$

where  $M_W$  is the mass of the  $W$  boson. The equivalence is established by the transformation

$$\begin{aligned} \mathcal{L}_{\text{int}} &= eJ_\mu^{\text{em}} A^\mu + [(gJ_\mu^3 - e\lambda J_\mu^{\text{em}})\cos\phi/M_W - (g_V J_\mu^Y - e\lambda' J_\mu^{\text{em}})\sin\phi/M_V] M_Z Z^\mu \\ &\quad + [(gJ_\mu^3 - e\lambda J_\mu^{\text{em}})\sin\phi/M_W + (g_V J_\mu^Y - e\lambda' J_\mu^{\text{em}})\cos\phi/M_V] M_X X^\mu \end{aligned} \quad (12)$$

with  $\lambda$ 's and  $J_\mu^V$  given by (4a)–(4c).

The mixing parameters  $\lambda$ 's are written in terms of the coupling constants,  $e$ ,  $g$ , and  $g_V$  as in (4a)–(4c). Among them,  $e$  is precisely determined by experiments. We use the value such that  $\alpha = e^2/4\pi = (1/137.036)(1 - \Delta r)$ , where  $\Delta r = 0.058$  is the radiative correction with the top-quark mass  $m_t = 100$  GeV and the Higgs-boson mass  $M_H = 100$  GeV (Ref. 19). The coupling constant  $g$  is related to  $M_W$  by  $g = (4\sqrt{2} G_F)^{1/2} M_W$ , where the Fermi coupling constant  $G_F$  is precisely determined by  $\beta$  decay

$$gW'_\mu{}^3 = gW_\mu^3 - g_V V_\mu, \quad g'_V V'_\mu = g_V V_\mu, \quad (5)$$

with  $(g'_V)^{-2} = (g_V)^{-2} + g^{-2}$ . Further details of these models will appear in a separate paper.<sup>18</sup> It is remarkable that the originally different dynamical models (a) and (b) lead to the same results (4a)–(4c). The fact that  $\lambda'$  has the form  $e/g_V \times$  (subquark charge) can be taken as a general consequence of the dynamics which respects relation (3). Thus, we expect that relations (4a)–(4c) hold in a fairly wide class of dynamical composite models. In the following we investigate the phenomenological consequences of these relations.

The current mixings in (4a)–(4c) are diagonalized by the following transformation that yields the physical photon  $A_\mu$ ,  $Z$  boson  $Z_\mu$ , and extra vector boson  $X_\mu$ :

$$\begin{pmatrix} A_\mu \\ Z_\mu \\ X_\mu \end{pmatrix} = \begin{pmatrix} 1 & \lambda & \lambda' \\ 0 & M_W \cos\phi/M_Z & -M_V \sin\phi/M_Z \\ 0 & M_W \sin\phi/M_X & M_V \cos\phi/M_X \end{pmatrix} \begin{pmatrix} \tilde{A}_\mu \\ \tilde{W}_\mu^3 \\ V_\mu \end{pmatrix}, \quad (6)$$

where  $M_V$  is the mass of  $V_\mu$  before the diagonalization,  $M_Z$  and  $M_X$  are the diagonalized masses of  $Z_\mu$  and  $X_\mu$ , respectively, and  $\phi$  is the mixing angle defined by

$$\sin 2\phi = \frac{2M_X M_Z (\lambda\lambda' - \lambda'')}{(M_X^2 - M_Z^2)\sqrt{\Delta}} \quad (7)$$

with

$$\Delta = 1 - \lambda^2 - \lambda'^2 - \lambda''^2 + 2\lambda\lambda'\lambda'' \quad (8)$$

The masses  $M_W$ ,  $M_V$ ,  $M_Z$ , and  $M_X$  are related to each other by

$$M_W^2 M_V^2 = M_Z^2 M_X^2 \Delta, \quad (9)$$

$$(1 - \lambda'^2)M_W^2 + (1 - \lambda^2)M_V^2 = (M_Z^2 + M_X^2)\Delta. \quad (10)$$

Eliminating  $M_V$  we obtain the following relation among the observable masses:

$$\begin{aligned} [1 - (1 - \lambda^2)M_Z^2/M_W^2][1 - (1 - \lambda^2)M_X^2/M_W^2] \\ = -(\lambda'' - \lambda\lambda')^2/\Delta. \end{aligned} \quad (11)$$

The interaction Lagrangian becomes

experiments. Thus, for a given set of  $M_{W,Z,X}$ , we can fix  $g_V$  by (11) and can calculate any physical quantities in terms of them. We show, by the solid lines in Fig. 1, the bounds<sup>20</sup> on  $M_X$  and  $g_V$  (or  $g'_V$ ) from the constraint (11) with the averaged experimental values<sup>21–23</sup>

$$M_W = (80.0 \pm 0.56) \text{ GeV}, \quad (13)$$

$$M_Z = (91.09 \pm 0.06) \text{ GeV}.$$

The solid lines in Fig. 2 show the bounds from the same conditions on  $R(60 \text{ GeV})$ ,  $R(M_Z)$ , and  $\Gamma_Z$ , where  $R(E) = \sigma(e\bar{e} \rightarrow \text{hadrons}) / \sigma(e\bar{e} \rightarrow \mu\bar{\mu})_{\text{QED}}$  at the c.m. energy  $E$  and  $\Gamma_Z$  is the decay width of the  $Z$ . Then we examine the following physical quantities, and compare

$$\sin^2\theta_W = \begin{cases} \frac{e^2}{g^2} \left[ 1 + 2Q_{c_l} \frac{M_W^2}{M_V^2} \right] & (\text{leptonic gluon, } \nu p, \bar{\nu} p), \\ \frac{e^2}{g^2} \left[ 1 + 2 \left[ Q_{c_l} + \frac{g_V^2}{e^2} \right] \frac{M_W^2}{M_V^2} \right] & (\text{leptonic gluon, } \nu e, \bar{\nu} e), \\ \frac{e^2}{g^2} & (\text{singlet gluon, heavy photon}). \end{cases} \quad (14)$$

Note that the singlet gluon and the heavy photon decouple from neutrinos at low energies, and suffer from no restriction from them. As the experimental value we use, following Costa *et al.*,<sup>24</sup>  $\sin^2\theta_W = 0.2283 \pm 0.0048$  ( $0.2271 \pm 0.0143$ ) from  $\nu p$  and  $\bar{\nu} p$  ( $\nu e$  and  $\bar{\nu} e$ ) scatterings.

(ii) *The compositeness scale  $\Lambda_c$  (Ref. 25) from Bhabha scattering.* The scale  $\Lambda_c$  is written in the present model as

$$\Lambda_c^2 = 2\pi M_V^2 / (g_V N_e - eQ_e \lambda')^2, \quad (15)$$

where  $Q_\psi$  ( $\psi = e, q$ , etc.) is the electric charge of the fermion  $\psi$ , and  $N_\psi$  is the lepton number of  $\psi$  for  $V_\mu =$  leptonic gluon, the quark number of  $\psi$  for  $V_\mu =$  singlet gluon, and the electric charge of  $\psi$  for  $V_\mu =$  heavy photon. The experimental bound is<sup>26</sup>  $\Lambda_c > 7.1 \text{ TeV}$  for current  $\times$  current interactions with the vector coupling.

(iii) *The compositeness scale  $\Lambda_c$  from  $p\bar{p} \rightarrow J + \text{anything}$  ( $J$  denotes a jet).* The scale  $\Lambda_c$  is written as

$$\Lambda_c^2 = 2\pi M_V^2 \sum_q Q_q^2 / \sum_q Q_q^2 (g_V N_q - eQ_q \lambda')^2, \quad (16)$$

where the summation is carried over the valence quarks  $u_v$  and  $d_v$ , and simple proportionality of their distribution functions is assumed. The experimental bound is<sup>27</sup>  $\Lambda_c > 700 \text{ GeV}$ , which is derived by assuming current  $\times$  current interactions with the left-handed coupling. This is the only case analyzed by the authors of Ref. 27, and we use this value, though the coupling in the present model is vectorlike. It would be rather safe, because a crude estimate indicates that the value of  $\Lambda_c$  is larger for the vector coupling.

(iv)  $\sigma(p\bar{p} \rightarrow X + \text{anything}) B(X \rightarrow JJ)$ . The experimental bound is given in Fig. 3 of Ref. 28 for  $160 < M_X < 400 \text{ GeV}$ . In evaluating  $\sigma(p\bar{p} \rightarrow X + \text{anything})$  in our model we use the parton distribution functions of the set I in Ref. 29.

(v)  $\sigma(p\bar{p} \rightarrow X + \text{anything}) B(X \rightarrow e\bar{e})$ . The experimental bound is 1 pb (Ref. 30). In evaluating  $\sigma(p\bar{p} \rightarrow X + \text{anything})$  in our model we again use the parton distribution functions of the set I in Ref. 29.

(vi) We have also examined the constraints from the

them with the presently known experimental results (Figs. 1 and 2).

(i) *The Weinberg angle  $\theta_W$  from neutrino scattering.* The angle  $\theta_W$  determined by assuming the standard model is related to the quantities of the present model as

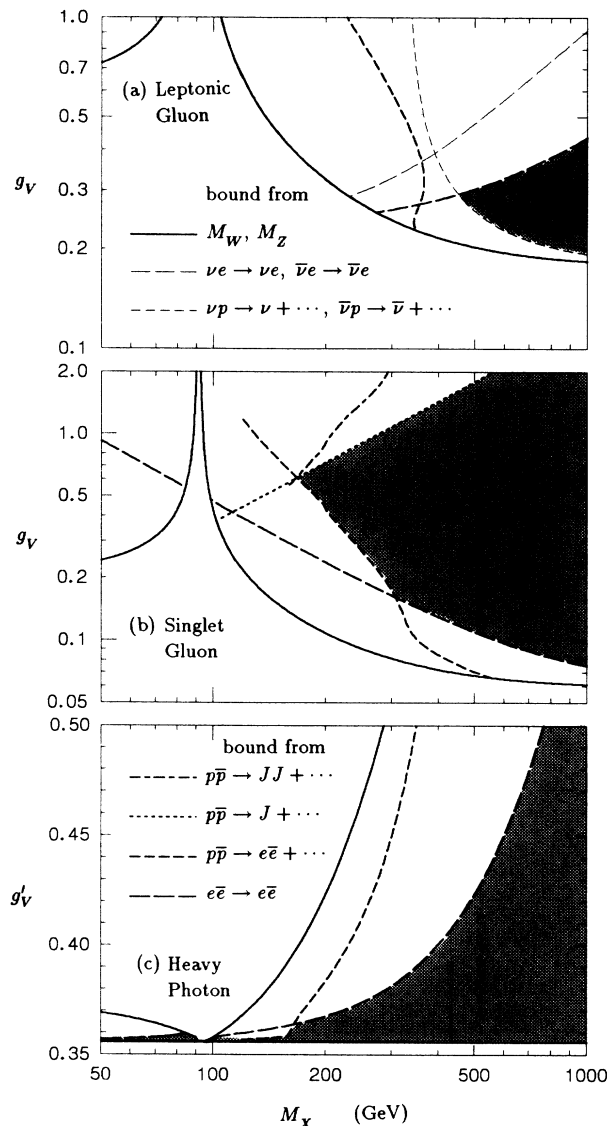


FIG. 1. The experimental bounds on  $g_V$  (or  $g'_V$ ) vs  $M_X$  for (a) leptonic gluon, (b) color-singlet gluon, and (c) heavy photon. The allowed regions are indicated by the shaded area. Each curve corresponds to the bound indicated in (a) and (c).

anomalous magnetic moments of the electron and muon, deep-inelastic lepton nucleon scattering, and parity violations in atoms. They are less restrictive than the above bounds because of their larger experimental errors.

The experimental bounds in (i)–(v), when combined with the ranges of the weak-boson masses in (13), give the bounds on  $M_X$  and  $g_V$  (or  $g'_V$ ) shown in Fig. 1, and those on  $R(60 \text{ GeV})$ ,  $R(M_Z)$ , and  $\Gamma_Z$  shown in Fig. 2. The shaded regions are finally left allowed.

Since the mixing parameter  $\lambda'$  is proportional to  $1/g_V$ , a value of  $g_V$  too small causes mixing that is too large and is forbidden. When we have an experimental bound on a quantity concerning  $X\psi\bar{\psi}$  vertex ( $\psi=q, \nu, e$ ),  $g_V$  is bounded from above if  $V$  ( $X$  before mixing) directly couples to the  $\psi\bar{\psi}$  channel, while  $g_V$  is bounded from below if  $X$  cou-

ples to the  $\psi\bar{\psi}$  channel through mixing. Since neutrinos have a vanishing quark number and a vanishing electric charge, the singlet gluon and the heavy photon decouple from neutrinos at low energies, but the leptonic gluon couples to them through the lepton number. Consequently,  $\nu p$ ,  $\bar{\nu} p$ ,  $\nu e$ , and  $\bar{\nu} e$  scattering experiments place restrictions on the mass of the leptonic gluon only:  $M_X > 390 \text{ GeV}$  ( $M_X > 450 \text{ GeV}$  when combined with the bound from  $e^+e^- \rightarrow e^+e^-$ ) [Fig. 1(c)]. The leptonic gluon can hardly affect  $R(60 \text{ GeV})$ ,  $R(M_Z)$ , and  $\Gamma_Z$ . The singlet gluon is allowed in the region inside the bound from  $\Lambda_c$  in  $p\bar{p} \rightarrow J + \dots$ , that from  $\Lambda_c$  in  $e^+e^- \rightarrow e^+e^-$ , and that from  $p\bar{p} \rightarrow e^+e^- + \dots$ , which leaves the possibility of a mass as small as  $M_X > 170 \text{ GeV}$ . For the heavy photon, the allowed region lies inside the

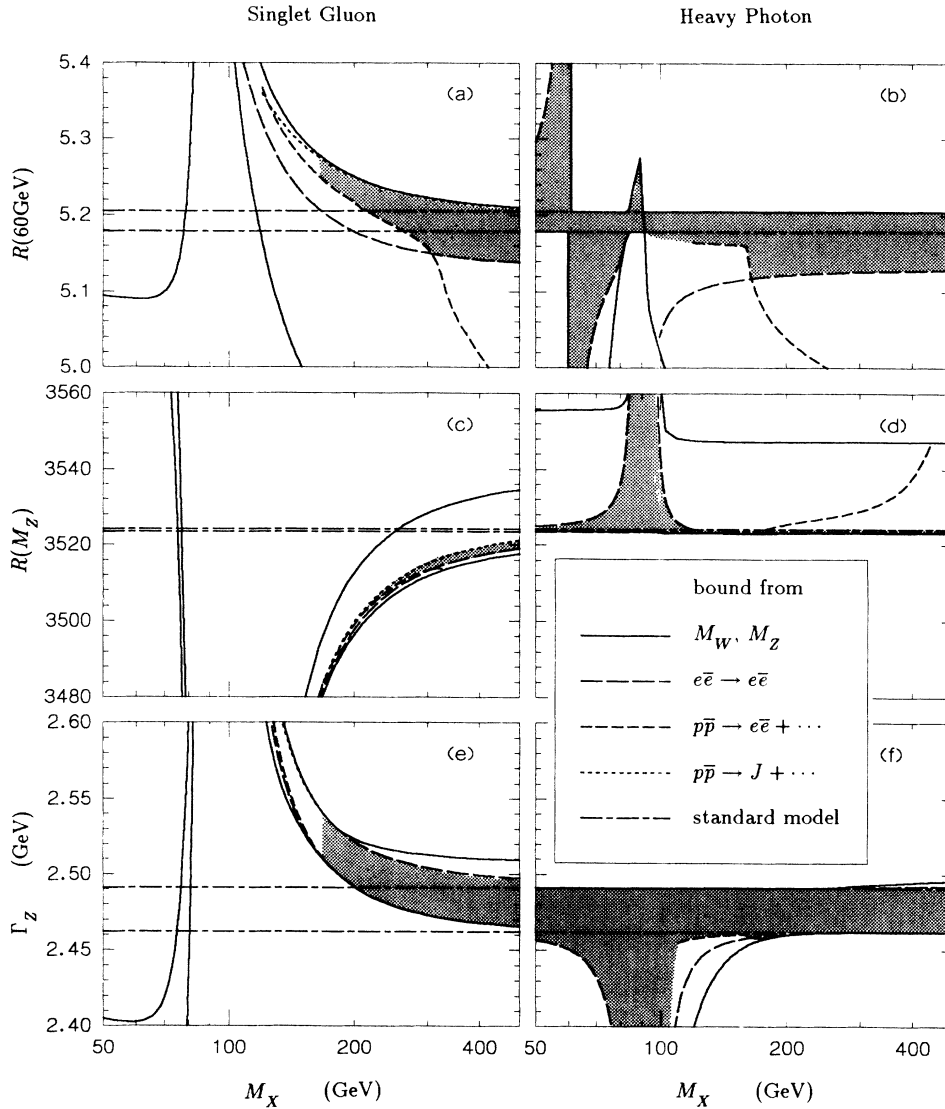


FIG. 2. The experimental bounds on  $R(60 \text{ GeV})$  [(a) and (b)],  $R(M_Z)$  [(c) and (d)], and  $\Gamma_Z$  [(e) and (f)] vs  $M_X$  for the singlet gluon [(a), (c), and (e)] and for the heavy photon [(b), (d) and (f)]. The allowed regions are indicated by the shaded area. Each curve corresponds to the bound indicated in (d) and (f).

bound from  $\Lambda_c$  in  $e^+e^- \rightarrow e^+e^-$ , that from  $p\bar{p} \rightarrow e^+e^- + \dots$ , and the kinematical bound from  $\Delta \geq 0$  with  $\Delta$  in (8), which imposes no essential lower bound on  $M_X$ . The allowed values of  $R(60 \text{ GeV})$ ,  $R(M_Z)$ , and  $\Gamma_Z$  deviate from their standard-model values. The singlet gluon with 170 to 300 GeV can increase  $R(60 \text{ GeV})$ , which possibly explains the (slight) enhancement in  $R$  at TRISTAN.<sup>31</sup> The singlet gluon (heavy photon) decreases (increases)  $R(M_Z)$ , and increases (decreases)  $\gamma_Z$ . Al-

though the larger  $R(M_Z)$  and the smaller  $\Gamma_Z$  of the heavy photon near  $M_X = M_Z$  are already ruled out by the SLC<sup>22</sup> and LEP<sup>23</sup> data, the rest regions as well as the whole regions of the singlet gluon still remain consistent within errors. More precise measurements in the near future should be able to distinguish the present model from the standard model. We hope that these predictions are examined in the forthcoming experiments at TRISTAN, SLC, and LEP.

- <sup>1</sup>J. C. Pati and A. Salam, *Phys. Rev. D* **10**, 275 (1974); K. Matumoto, *Prog. Theor. Phys.* **52**, 1973 (1974).
- <sup>2</sup>K. Akama and H. Terazawa, INS-Report No. 257, 1976 (unpublished); H. Terazawa, Y. Chikashige, and K. Akama, *Phys. Rev. D* **15**, 480 (1977).
- <sup>3</sup>M. Yasuè, *Prog. Theor. Phys.* **59**, 534 (1978); **61**, 269 (1979); Y. Tanikawa and T. Saito, *ibid.* **59**, 563 (1978); Y. Ne'eman, *Phys. Lett.* **82B**, 69 (1979).
- <sup>4</sup>F. E. Low, *Phys. Rev. Lett.* **14**, 283 (1965); H. Terazawa, *Prog. Theor. Phys.* **37**, 204 (1967); T. Appelquist and J. D. Bjorken, *Phys. Rev. D* **4**, 3726 (1971); K. Matumoto and T. Tajima, *Prog. Theor. Phys.* **52**, 741 (1974); H. Terazawa, M. Yasuè, K. Akama, and M. Hayashi, *Phys. Lett.* **112B**, 387 (1982); M. Kuroda and D. Schildknecht, *ibid.* **121B**, 173 (1983); M. Yasuè and S. Oneda, *Phys. Rev. D* **32**, 317 (1985); **32**, 3066 (1985).
- <sup>5</sup>K. Matumoto, *Prog. Theor. Phys.* **47**, 1795 (1972); M. S. Chanowitz and S. D. Drell, *Phys. Rev. Lett.* **30**, 807 (1973); K. Akama, *Prog. Theor. Phys.* **51**, 1879 (1974); E. J. Eichten, K. D. Lane, and M. E. Peskin, *Phys. Rev. Lett.* **50**, 811 (1983).
- <sup>6</sup>K. Akama, *Prog. Theor. Phys.* **73**, 845 (1985).
- <sup>7</sup>M. A. Bég and A. Sirlin, *Annu. Rev. Nucl. Sci.* **24**, 379 (1974); S. Weinberg, *Phys. Rev. D* **19**, 1277 (1979); G. 't Hooft, in *Recent Developments in Gauge Theories*, proceedings of the Cargèse Summer Institute, Cargèse, France, 1979, edited by G. 't Hooft *et al.* (NATO Advanced Study Institutes Series B: Physics, Vol. 59) (Plenum, New York, 1980), p. 135; L. Susskind, *Phys. Rev. D* **19**, 2691 (1979).
- <sup>8</sup>V. Barger, N. G. Deshpande, and K. Whisnant, *Phys. Rev. Lett.* **56**, 30 (1986); L. S. Durkin and P. Langacker, *Phys. Lett.* **166B**, 436 (1986); U. Amaldi, A. Böhm, L. S. Durkin, P. Langacker, A. K. Mann, W. J. Marciano, A. Sirlin, and H. H. Williams, *Phys. Rev. D* **36**, 1385 (1987); G. Costa, J. Ellis, G. L. Fogli, D. V. Nanopoulos, and F. Zwirner, *Nucl. Phys.* **B297**, 244 (1988); J. Ellis, P. J. Franzini, and F. Zwirner, *Phys. Lett. B* **202**, 417 (1988).
- <sup>9</sup>K. Akama and T. Hattori, *Phys. Rev. D* **40**, 3688 (1989).
- <sup>10</sup>P. Q. Hung and J. J. Sakurai, *Nucl. Phys.* **B143**, 81 (1978).
- <sup>11</sup>Y. Nambu and G. Jona-Lasinio, *Phys. Rev.* **122**, 345 (1961); J. D. Bjorken, *Ann. Phys. (N.Y.)* **24**, 174 (1963).
- <sup>12</sup>Terazawa, Chikashige, and Akama (Ref. 2); H. Terazawa, *Phys. Rev. D* **22**, 184 (1980); M. Yasuè, *Nucl. Phys.* **B234**, 252 (1983); *Phys. Rev. D* **39**, 3458 (1989); I. Ito and M. Yasuè, *ibid.* **29**, 547 (1984); T. Kugo, S. Uehara, and T. Yanagida, *Phys. Lett.* **147B**, 321 (1984); S. Uehara and T. Yanagida, *ibid.* **165B**, 94 (1985); M. Suzuki, *Phys. Rev. D* **37**, 210 (1988); K. Akama and T. Hattori, *ibid.* **39**, 1992 (1989).
- <sup>13</sup>Matumoto (Ref. 1); 't Hooft (Ref. 7); H. Terazawa, *Prog. Theor. Phys.* **64**, 1736 (1980); R. Casalbuoni and R. Gatto, *Phys. Lett.* **93B**, 47 (1980); J. C. Pati, *ibid.* **98B**, 40 (1981); H. Harari and N. Seiberg, *ibid.* **98B**, 269 (1981); O. W. Greenberg and J. Sucher, *ibid.* **99B**, 339 (1981).
- <sup>14</sup>L. F. Abbott and E. Farhi, *Phys. Lett.* **101B**, 69 (1981); *Nucl. Phys.* **B189**, 547 (1981); Kugo, Uehara, and Yanagida (Ref. 12); Uehara and Yanagida (Ref. 12); H. Terazawa, in *Proceedings of the 6th INS Winter Seminar on Structures and Forces in Elementary Particle Physics*, edited by H. So (INS Report No. J-170, Tokyo, 1986), p. 1; M. Yasuè, *Mod. Phys. Lett. A* **4**, 815, (1989); **A 4**, 1559, (1989); V. Višnjić, *Nuovo Cimento* **101A**, 385 (1989); C. Bilchak and D. Schildknecht, Report No. BI-TP 8/18, 1989 (unpublished).
- <sup>15</sup>t Hooft (Ref. 7); S. Dimopoulos, S. Raby, and L. Susskind, *Nucl. Phys.* **B173**, 208 (1980); T. Matsumoto, *Phys. Lett.* **97B**, 131 (1980); R. Casalbuoni and R. Gatto, *ibid.* **103B**, 113 (1981).
- <sup>16</sup>Akama and Hattori (Refs. 9 and 12).
- <sup>17</sup>Yasuè (Ref. 14).
- <sup>18</sup>K. Akama, T. Hattori, and M. Yasuè, in preparation.
- <sup>19</sup>W. J. Marciano, *Phys. Rev. D* **20**, 274 (1979).
- <sup>20</sup>All the bounds in this paper are taken up to the 95% confidence level.
- <sup>21</sup>Collider Detector at Fermilab (CDF) Collaboration, P. Sineruo, in *Proceedings of the XIVth International Symposium on Lepton and Photon Interactions*, Stanford, California, 1989, edited by M. Riordan (World Scientific, Singapore, 1990); UA2 Collaboration, K. Eggert, *ibid.*
- <sup>22</sup>Mark II Collaboration, G. S. Abrams, *Phys. Rev. Lett.* **63**, 2173 (1989).
- <sup>23</sup>L3 Collaboration, B. Adeva *et al.*, *Phys. Lett. B* **231**, 509 (1989); ALEPH Collaboration, D. Decamp *et al.*, *ibid.* **231**, 519 (1989); OPAL Collaboration, M. Z. Akrawy *et al.*, *ibid.* **231**, 530 (1989); DELPHI Collaboration, P. Aarnio *et al.*, *ibid.* **231**, 539 (1989).
- <sup>24</sup>Costa *et al.* (Ref. 8).
- <sup>25</sup>We follow the definition of  $\Lambda_c$  in Eichten, Lane, and Peskin (Ref. 5).
- <sup>26</sup>TASSO Collaboration, W. Braunschweig *et al.*, *Z. Phys. C* **37**, 171 (1988).
- <sup>27</sup>CDF Collaboration, F. Abe *et al.*, *Phys. Rev. Lett.* **62**, 613 (1989).
- <sup>28</sup>UA1 Collaboration, R. Albajar *et al.*, *Phys. Lett. B* **209**, 127 (1988).
- <sup>29</sup>E. Eichten, I. Hinchliffe, K. Lane, and C. Quigg, *Rev. Mod. Phys.* **56**, 579 (1984).
- <sup>30</sup>CDF Collaboration, S. Geer, Talk given at the 8th INFN Eloisatron Project Workshop on the Higgs Boson, Erice, Italy, 1989.
- <sup>31</sup>AMY Collaboration, T. Mori *et al.*, *Phys. Lett. B* **218**, 499 (1989).

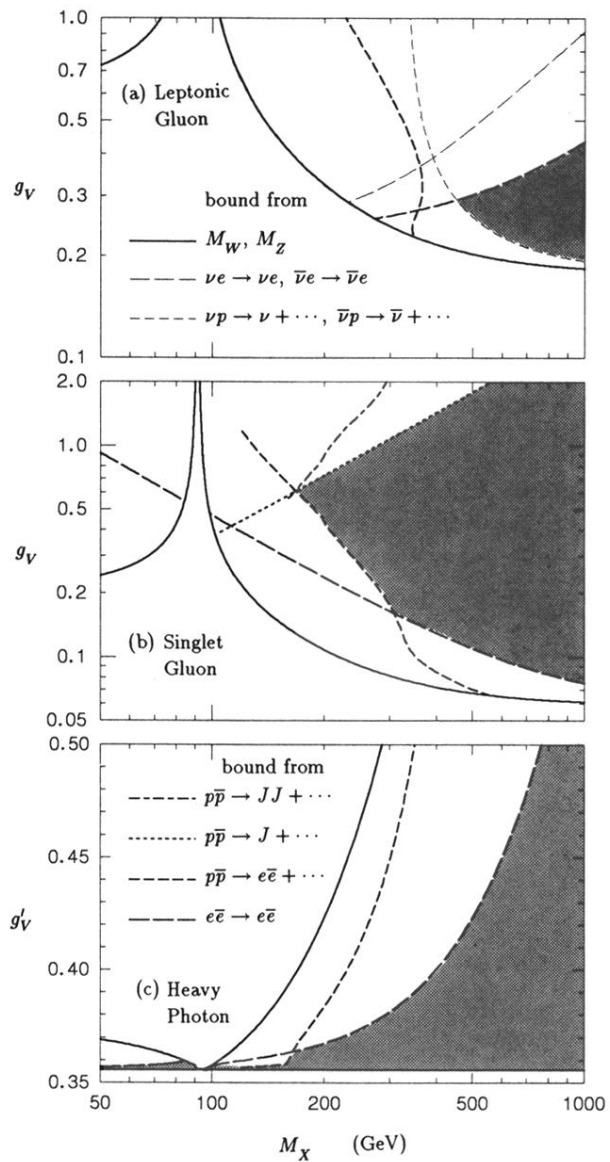


FIG. 1. The experimental bounds on  $g_\nu$  (or  $g'_\nu$ ) vs  $M_X$  for (a) leptonic gluon, (b) color-singlet gluon, and (c) heavy photon. The allowed regions are indicated by the shaded area. Each curve corresponds to the bound indicated in (a) and (c).

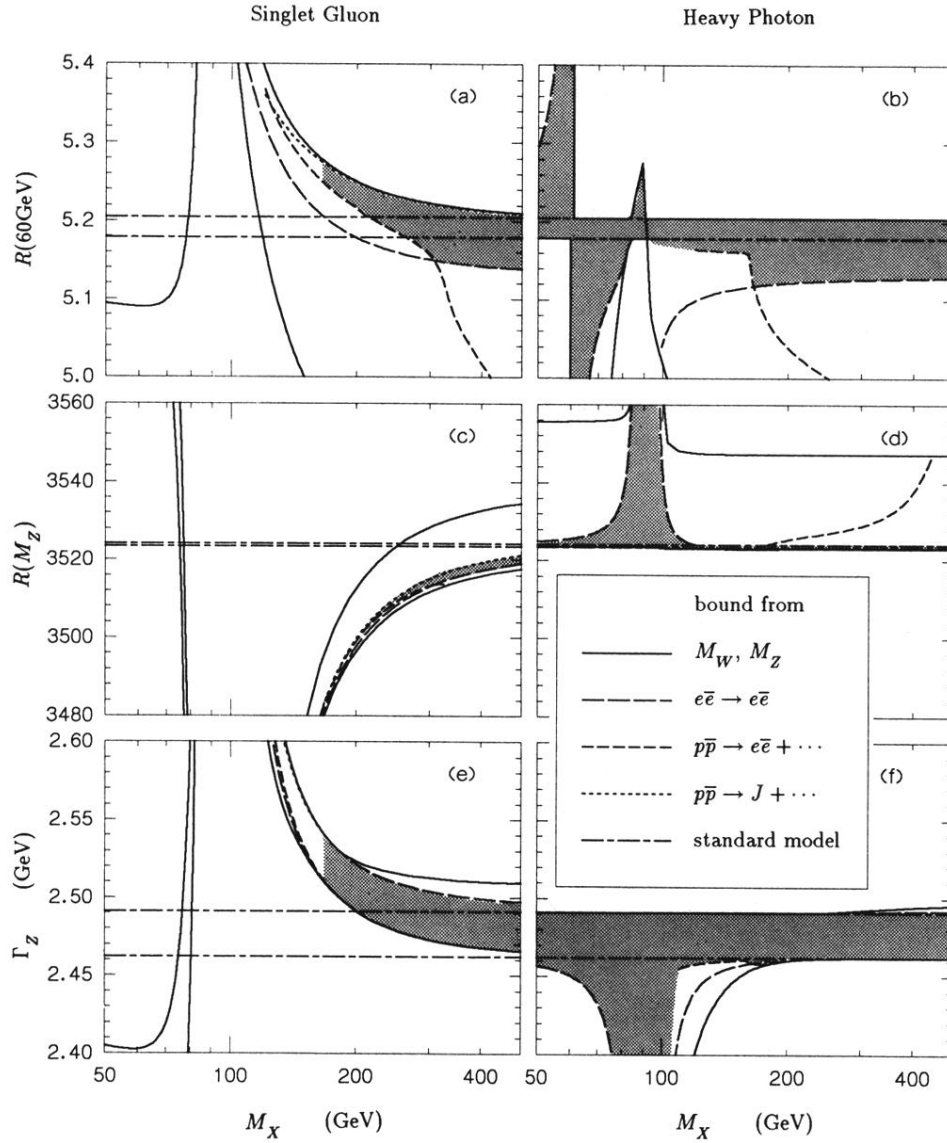


FIG. 2. The experimental bounds on  $R(60\text{ GeV})$  [(a) and (b)],  $R(M_Z)$  [(c) and (d)], and  $\Gamma_Z$  [(e) and (f)] vs  $M_X$  for the singlet gluon [(a), (c), and (e)] and for the heavy photon [(b), (d) and (f)]. The allowed regions are indicated by the shaded area. Each curve corresponds to the bound indicated in (d) and (f).