Studying effects of a second Z as tests of a unification model of electroweak and strong interactions

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The effects of a second heavier Z' gauge boson predicted in a model of unification of electroweak and strong interactions without grand unification are studied on the properties of Z. It is shown that future measurements of such effects can distinguish the model from the other extended gauge models which also have an extra Z'.

The advent of new experimental capabilities such as the Fermilab Tevatron, SLAC Linear Collider (SLC), and CERN LEP I, could provide precision tests of the predictions of the standard model. In the process, one may discover new physics. Extensions of the standard model involve the existence of new gauge vector bosons. Many authors¹⁻⁵ have studied the effects of an extra neutral gauge boson (Z'), which might manifest itself through accurate studies of e^+e^- collision around the Z peak. The mixing between Z and Z' could have important effects on the properties of Z. In an exhaustive study⁴ of such effects, the theoretical possibilities have been divided into two classes: (a) extension of the gauge group of the standard model; (b) electroweak symmetry breaking by the strong sector. The former class has been characterized by gauge invariance under $SU(2)_L \times U(1)_Y$ $\times U(1)_{\hat{Y}} \subset G$ [e.g., E_6 (Ref. 6)] and $^7 SU(2)_L \times SU(2)_R$ $\times U(1)_{B_{-L}}$. It is important to note that the new hypercharge \hat{Y} does not contribute to the charge operator of basic fermions in this class of models.

The purpose of this paper is to consider a different type of model,⁸ where \hat{Y} contributes to Q_{em} of quarks but not to Q_{em} of leptons. Such a model was considered as an attempt to unify electroweak interaction with strong interaction without putting quarks and leptons in one representation as is usually done in grand unified models. In fact \hat{Y} is responsible for the fractional electric charges of the quarks. Just as $\sin^2\theta_W$ determines the unification condition for electroweak interaction a new parameter $\sin^2\beta$ determines the unification condition of electroweak interaction with strong interaction. The unification scale in this model⁸ could be quite low.

The $SU(2)_L \otimes U(1)_Y \otimes U(1)_{Y'}$ content of the model gives rise to the Lagrangian⁸

$$L_{\rm ew} = e J_{\mu}^{\rm em} A_{\mu} + \frac{g}{\sqrt{2}} J_{L\mu}^{+} W_{\mu}^{-} + \text{H.c.}$$
$$+ \frac{g}{\cos\theta_{W}} J_{\mu}^{Z_{0}} Z_{0\mu} + \frac{g \tan\theta_{W}}{\sin\beta\cos\beta} J_{\mu}^{Z'_{0}} Z'_{0\mu} , \qquad (1a)$$

where

$$J_{\mu}^{Z_{0}} = J_{3L\mu} - \sin^{2}\theta_{W}J_{\mu}^{em} ,$$

$$J_{\mu}^{Z_{0}'} = \sin^{2}\beta (J_{\mu}^{Z_{0}} - \cos^{2}\theta_{W}J_{\mu}^{em}) + J_{\mu}^{C} ,$$
(1b)

with

$$J_{\mu}^{C}(l) = 0$$
, (1c)

while

$$J^{C}_{\mu}(q) = -\frac{1}{3}(\overline{u}_{n}i\gamma_{\mu}u_{n} + \overline{d}_{n}i\gamma_{\mu}d_{n}) .$$
 (1d)

Here Z_0 is the Z boson of the standard model and satisfies

$$\rho_{\rm SB} = \frac{M_W^2}{\cos^2\theta_W M_{Z_0}^2} = 1 \tag{2}$$

and $J_{\mu}^{Z_0}$ is the corresponding current. Note that Z_0 and Z'_0 are not physical particles, which we define as

$$Z = \cos \xi_0 Z_0 + \sin \xi_0 Z'_0 ,$$

$$Z' = -\sin \xi_0 Z_0 + \cos \xi_0 Z'_0 .$$
(3a)

After diagonalizing of the matrix

$$\begin{bmatrix} M_{Z_0}^2 & M_{Z_0Z_0'}^2 \\ M_{Z_0Z_0'}^2 & M_{Z_0'}^2 \end{bmatrix},$$
(3b)

where in the model

$$M_{Z_0 Z_0'}^2 = \sin \theta_W \tan \beta M_{Z_0}^2 , \qquad (4)$$

we obtain

$$\tan^2 \xi_0 = \frac{\gamma \lambda}{1 - \gamma}, \quad M_{Z_0 Z_0'}^2 = -\cos \xi_0 \sin \xi_0 (M_{Z'}^2 - M_Z^2) , \quad (5)$$

with

$$\lambda = \left[1 - \frac{M_Z^2}{M_{Z_0}^2} \right], \quad \gamma = \frac{M_{Z_0}^2}{M_{Z'}^2}$$
(6)

and

$$M_{Z'}^{2} = M_{Z_{0}}^{2} \left[1 + \frac{1}{\lambda} \sin^{2} \theta_{W} \tan^{2} \beta \right] ,$$

$$M_{Z} < M_{Z_{0}} < M_{Z'} .$$
(7)

In the notation of Ref. 4, which we shall closely follow in studying the consequences of Z',

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	$m_t = 100 \text{ GeV}$	$m_i = 200 \text{ GeV}$
A_{v}	2.01	2.03
A_{v} A_{e}	1.18	1.23
A_{u}	5.69	5.77
A_d	6.55	6.59
B_{v}	4.01	4.05
B_e	1.63	1.54
B_u	$-\left[10.18+\frac{3.14}{\sin^2\beta}\right]$	$-\left[10.39+\frac{3.26}{\sin^2\beta}\right]$
B_d	$\left[4.82 + \frac{5.74}{\sin^2\beta}\right]$	$\left[4.86+\frac{5.84}{\sin^2\beta}\right]$
$\delta \Gamma_{v}$ (MeV)	-2.79	-1.25
$\delta \Gamma_e$ (MeV)	-0.63	-0.19
Γ_{v}^{0} (MeV)	166	167
Γ_l^0 (MeV)	83.3	84.3
Γ_{h}^{0} (MeV)	1733	1754

TABLE I. The coefficients A_f, B_f , deviations of leptonic widths $\delta \Gamma_l$, and the widths Γ_f^0 in the standard model.

$$\lambda = \frac{\Delta \rho_M}{\rho_M}, \quad \Delta \rho_M = \rho_M - 1 \ . \tag{8}$$

The model gives rise to the following effective lowenergy Lagrangian⁸ in the neutral sector (apart from electromagnetic term)

$$L_{\rm eff} = \frac{g^2}{M_{Z_0}^2 \cos^2 \theta_W} (J_{\mu}^{Z_0} J_{\mu}^{Z_0} + A^2 \cos^4 \theta_W J_{\mu}^D J_{\mu}^D) , \qquad (9a)$$

where

$$A^{2} = (1-\lambda)^{-1}\lambda(1-\gamma)$$
(9b)

and

$$J^{D}_{\mu} = J^{\rm em}_{\mu} - \frac{1}{\sin^2 \beta \cos^2 \theta_W} J^{C}_{\mu} .$$
 (10)

Note that $J^D_{\mu}(\nu) = 0$ so that there is no contribution of the additional term in Eq. (9a) to ν -q and ν -e scattering. J^D_{μ} being a pure vector, there is also no contribution to the asymmetry parameter in e-q scattering. Thus the low-energy predictions of the model are exactly the same as in

TABLE II. The deviations of hadronic width and the lower limits on $M_{Z'}$.

	m	h = 100 G	eV	$m_t = 200 \text{ GeV}$		
$\sin^2\beta$	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$
<i>M_{Z'}</i> (GeV)	257	301	351	368	436	513
$\delta\Gamma_h$ (MeV)	5.5	14.8	21.0	2.6	6.7	11.0

the standard model irrespective of the masses of Z and Z'.

In order to study the effect of Z' on Z properties, we extract from Eqs. (1), on using Eq. (3a), the Z couplings:

$$\frac{g}{\cos\theta_{W}}\cos\xi_{0}\left[J_{\mu}^{Z_{0}}+\sin\theta_{W}\tan\xi_{0}\tan\beta\right] \times \left[J_{\mu}^{Z_{0}}-\cos^{2}\theta_{W}J_{\mu}^{em}+\frac{1}{\sin^{2}\beta}J_{\mu}^{C}\right].$$
(11)

Now using Eqs. (4), (5), and (6),

$$\sin\theta_{W}\tan\xi_{0}\tan\beta = -\sin^{2}\varepsilon_{0}\left[\frac{M_{Z'}^{2}}{M_{Z_{0}}^{2}} - \frac{M_{Z}^{2}}{M_{Z_{0}}^{2}}\right] = -\lambda , \quad (12)$$

independent of the sign of ξ_0 . Thus, the Z couplings are given by

$$\frac{g}{\cos\theta_{W}}\cos\xi_{0}\left[J_{\mu}^{Z_{0}}-\lambda\left[J_{\mu}^{Z_{0}}-\cos^{2}\theta_{W}J_{\mu}^{em}+\frac{1}{\sin^{2}\beta}J_{\mu}^{C}\right]\right].$$
(13)

Therefore, to first order in λ or $\Delta \rho_M$ and $\cos^2 \xi_0 \simeq 1$,

$$\delta\Gamma_f = \frac{G_F M_Z^3}{24\sqrt{2}\pi} \Delta\rho_M (A_f - B_f) , \qquad (14a)$$

where⁴

TABLE III. The deviations of Γ_f (MeV) for U(1) (arising from E₆) and LR models.

	$\theta_2 = 0$				$\theta_2 = -90$				L	R
ξ0	0.04	-0.04	0.02	-0.02	0.04	-0.04	0.02	-0.02	0.02	-0.02
δΓν	0.67	4.97	1.74	3.90	11.2	-5.51	6.99	-1.34	4.96	0.68
$\delta \Gamma_l$	0.79	2.52	1.22	2.08	-2.76	6.07	-0.56	3.86	-0.75	4.06
$\delta \Gamma_h$	39.5	47.4	41.5	45.5	31.3	55.6	37.4	49.6	29.9	57.1
$\delta \Gamma_T$	43.8	69.8	50.3	63.3	56.3	57.3	56.6	57.0	42.4	71.3

$$A_{f} = 4N_{c}^{f}\rho_{f} \left[(T_{3L}^{f} - 2\sin^{2}\theta_{f}Q_{em})^{2} + (T_{3L}^{f})^{2} + 4\frac{\sin^{2}\theta_{f}\cos^{2}\theta_{f}}{\cos^{2}\theta_{f}}Q_{em}(T_{3L}^{f} - 2\sin^{2}\theta_{f}Q_{em}) \right]$$
(14b)

and, in our case,

$$B_{f} = 8N_{c}^{f}\rho_{f} \left[(T_{3L}^{f} - 2\sin^{2}\theta_{f}Q_{em}) \left[T_{3L}^{f} - 2Q_{em} - \frac{2}{3\sin^{2}\beta} \delta_{fq} \right] + (T_{3L}^{f})^{2} \right].$$
(14c)

Here $N_c^f = 1$ or $3(1 + \alpha_s/\pi) \simeq 3(1 + 0.04)$ for f = lepton (l)or quark (q), $\delta_{fq} = 0$ for f = l and = 1 for f = q. $\sin^2\theta_f$ has been defined in Ref. 4 and is essentially $\sin^2\theta_W$ with radiative corrections included while $\rho_f = 1/(1 - \Delta \rho_T)$, $\Delta \rho_T \simeq 3G_F m_t^2 / 8\sqrt{2}\pi^2$.

For the evaluation of A_f and B_f , we use the bound⁴

$$\Delta \rho_M < 0.020 - 0.002 (m_t / 80 \text{ GeV})^2 \tag{15}$$

obtained from the ratio M_W/M_Z as obtained from the Collider Detector at Fermilab⁹ (CDF) and UA2 (Ref. 10) Collaborations data and $M_Z = 91.10 \pm 0.06$ GeV determined by combining the SLC (Ref. 11) and LEP 1 (Ref. 12) results. Thus we shall use⁴

$$m_{t} = 100 \text{ GeV}, 200 \text{ GeV},$$

$$\sin^{2}\theta_{f} = 0.234, 0.230,$$

$$\Delta\rho_{M} = 1.69 \times 10^{-2}, 7.5 \times 10^{-3},$$

$$\Delta\rho_{f} = 3.14 \times 10^{-3}, 1.26 \times 10^{-2}.$$
(16)

Equation (7) gives

$$M_{Z'}^2 \simeq M_Z^2 [1 + (\Delta \rho_M)^{-1} \sin^2 \theta_f \tan^2 \beta]$$
, (17a)

so that Eqs. (16) give the following lower bounds on $M_{Z'}$ for $m_t = 100$ and 200 GeV, respectively:

$$M_{Z'}^2 \ge M_Z^2 (1+13.85 \tan^2 \beta)$$
, (17b)

$$M_{Z'}^2 \ge M_Z^2 (1+30.67 \tan^2 \beta)$$
 (17c)

The results of A_f , B_f , $\delta\Gamma_l$ (which are independent of $\sin^2\beta$), and

$$\Gamma_f^0 = \frac{G_F M_Z^3}{24\sqrt{2}\pi} C_f^0 , \qquad (18a)$$

with

$$C_f^0 = 4N_c^f \rho_f [(T_{3L} - 2\sin^2\theta_f Q_{\rm em})^2 + (T_{3L}^f)^2],$$
 (18b)

are summarized in Table I. From Table I, we have for $m_t = 100$ and 200 GeV, respectively,

$$\frac{\delta\Gamma_{h}}{\Gamma_{h}^{0}} = \frac{2\delta\Gamma_{u} + 3\delta\Gamma_{d}}{2\Gamma_{u}^{0} + 3\Gamma_{d}^{0}}$$
$$= \begin{cases} (2.97 - 0.88/\sin^{2}\beta) \times 10^{-2}, & (19a)\\ (1.32 - 0.39/\sin^{2}\beta) \times 10^{-2}. & (19b) \end{cases}$$

TABLE IV. The deviations of total width.						
	$m_t = 100 \text{ GeV}$			$m_t = 200 \text{ GeV}$		
sin ² β	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$
$\frac{\delta\Gamma_T}{\Delta=0} (\text{MeV})$	-4.62	4.84	10.7	-1.69	2.55	6.88
$\delta \Gamma_T (\text{MeV})$ $\Delta = 0.1$	12.0	21.4	27.3	15.0	19.3	23.6
$\delta \Gamma_T (\text{MeV})$ $\Delta = 0.2$	28.6	38.0	60.5	31.7	52.7	57.0

TABLE V. The values of \mathcal{A}_f in the standard model and the coefficients α_f and β_f .

	$m_t = 100 \text{ GeV}$	$m_t = 200 \text{ GeV}$	
\mathcal{A}_{l}	-0.127	-0.159	
${\mathcal A}_l \ {\mathcal A}_c$	-0.659	-0.673	
\mathcal{A}_{b}	-0.934	-0.935	
α_l	-2.66	-2.57	
α_c	-1.18	-1.13	
α_d	-0.22	-0.21	
$\boldsymbol{\beta}_l$	-6.05	-6.04	
β_c	$-\left[2.69+\frac{1.75}{\sin^2\beta}\right]$	$-\left(2.64+\frac{1.72}{\sin^2\beta}\right)$	
β_d	$-\left[0.50-\frac{0.65}{\sin^2\beta}\right]$	$-\left[0.49-\frac{0.63}{\sin^2\beta}\right]$	

For some typical values of $\sin^2\beta$, the results for lower limits of $M_{Z'}$ and $\delta\Gamma_h$ are summarized in Table II.

Very small and negative deviations (-0.2 to -0.6 MeV) for the leptonic width and positive and relatively large (3 to 21 MeV) deviations for the hadronic width are the distinguishing features of the model. This is brought out by comparison with extra U(1) models (arising from E_6), for which we consider two representative cases which correspond in the notation of Ref. 4 to $\theta_2=0$ (which occurs in many superstring models and is called the η model in the literature) an $\theta_2 = -90$. For these cases the deviation of widths for $\xi_0 = \pm 0.04$ and $\xi_0 = \pm 0.02$ and $m_t = 100$ GeV (as calculated from the relevant formulas of Ref. 4) are summarized in Table III. In the same table we also give the corresponding values for the left-right (*LR*) models for $\xi_0 = \pm 0.02$ and $m_t = 100$ GeV.

As far as the total width Γ_T is concerned, it depends on what one should use for N_v , the number of lightneutrino generations. Defining an "effective" value of N_v as $N_v = 3 + \Delta$, we have

$$\delta\Gamma_T = 3\delta\Gamma_v + 3\delta\Gamma_e + 2\delta\Gamma_u + 3\delta\Gamma_d + \Delta\Gamma_v^0 , \qquad (20)$$

so that we have from Table I and Eqs. (19) for $m_t = 100$ and 200 GeV, respectively,

$$\delta\Gamma_T = \frac{1}{2}\Gamma_{\nu}^0 \left[1.69 \times 10^{-2} \left[29.66 - \frac{10.92}{\sin^2\beta} \right] + 2\Delta \right] , \quad (21a)$$

$$\delta\Gamma_T = \frac{1}{2}\Gamma_v^0 \left[0.75 \times 10^{-2} \left[30.16 - \frac{10.87}{\sin^2\beta} \right] + 2\Delta \right] . \quad (21b)$$

Present data¹² are consistent with $\Delta \leq 0.23$. The results for various values of $\sin^2\beta$ and Δ are summarized in Table IV. The deviations from the lepton polarization and the forward-backward asymmetries of the standard model are given by⁴

$$\delta A_{\rm pol} = -\delta \mathcal{A}_l = -\Delta \rho_M (\alpha_f - \beta_f) , \qquad (22)$$

$$\delta A_{FB}^{f} = \frac{3}{4} \Delta \rho_{M} [\mathcal{A}_{e} (\alpha_{f} - \beta_{f}) + \mathcal{A}_{f} (\alpha_{e} - \beta_{e})]$$
$$+ \frac{3}{4} (\Delta \rho_{M})^{2} (\alpha_{f} - \beta_{f}) (\alpha_{e} - \beta_{e}) , \qquad (23a)$$

where

$$\alpha_f = K_f \frac{2\sin^2\theta_f \cos^2\theta_f}{\cos^2\theta_f} T_{3L}^f Q_{\rm em} , \qquad (23b)$$

$$\beta_{f} = K_{f} \left[T_{3L}^{f} (T_{3L}^{f} - 2\sin^{2}\theta_{f}Q_{em}) - T_{3L}^{f} \left[T_{3L}^{f} - 2Q_{em} - \frac{2}{3\sin^{2}\beta} \delta_{fh} \right] \right], \quad (23c)$$

$$K_f = -2 \frac{(T_{3L}^f)^2 - (T_{3L}^f - 2\sin^2\theta_f Q_{\rm em})^2}{[(T_{3L}^f)^2 + (T_{3L}^f - 2\sin^2\theta_f Q_{\rm em})^2]^2} .$$
(23d)

The values of \mathcal{A}_f and α_f as calculated in Ref. 4 as well as those of β_f are given in Table V. Using Table V and Eqs. (22) and (23), the lepton polarization and forwardbackward asymmetries deviations for $m_t = 100$ and 200 GeV are, respectively, given by

$$\delta A_{\rm pol} = \begin{cases} -0.057 , \\ -0.026 , \end{cases}$$
(24)

$$\delta A_{FB}^{l} = \frac{3}{4} (\Delta \rho_{M}) (\alpha_{l} - \beta_{l}) [2\mathcal{A}_{l} + (\Delta \rho_{M}) (\alpha_{l} - \beta_{l})] = \begin{cases} -8.45 \times 10^{-3} , \\ -5.70 \times 10^{-3} , \end{cases}$$
(25)

$$\delta A_{FB}^{c} = \begin{cases} -\left[3.077 + \frac{0.283}{\sin^{2}\beta}\right] 10^{-2}, \\ -\left[1.450 + \frac{0.154}{\sin^{2}\beta}\right] 10^{-2}, \end{cases}$$
(26)

$$\delta A_{FB}^{\alpha} = \begin{cases} -\left[4.062 - \frac{0.104}{\sin^2\beta}\right] 10^{-2} ,\\ -\left[1.85 - \frac{0.056}{\sin^2\beta}\right] 10^{-2} . \end{cases}$$
(27)

The values of δA_{FB}^c and δA_{FB}^{α} for various values of $\sin^2\beta$

TABLE VI. The values δA_{FB}^c and δA_{FB}^d for various values of $\sin^2\beta$.

	$m_t = 100 \text{ GeV}$			$m_t = 200 \text{ GeV}$		
sin² <i>β</i>	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{5}{12}$	$\frac{1}{2}$
δA_{FB}^{c}	-3.93×10^{-2}	-3.76×10^{-2}	-3.64×10^{-2}	-1.91×10^{-2}	-1.82×10^{-2}	-1.76×10^{-2}
δA_{FB}^{d}	-3.75×10^{-2}	-3.81×10^{-2}	-3.85×10^{-2}	-1.68×10^{-2}	-1.72×10^{-2}	-1.74×10^{-2}

	θ	2=0	$\theta_2 =$	= - 90
ξ ₀	0.02	-0.02	0.02	-0.02
δA_{FB}^{l}	1.54×10^{-2}	5.4×10^{-3}	4.6×10^{-3}	1.65×10^{-2}
δA_{FB}^{c}	4.43×10^{-2}	2.03×10^{-2}	1.71×10^{-2}	4.75×10^{-2}
δA_{FB}^{d}	6.02×10^{-2}	2.46×10^{-2}	2.22×10^{-2}	6.26×10^{-2}

TABLE VII. The deviations for forward-backward asymmetries for U(1) (arising from E_6) models.

are summarized in Table VI. These are not sensitive to $\sin^2\beta$. Again the predictions of Eqs. (26) and (25) and Table VI for deviations for polarization and forward-backward asymmetries are quite different from the corresponding values summarized in Table VII for $\xi_0 = \pm 0.02$ and $m_t = 100$ GeV for U(1) models exemplified by $\theta_2 = 0$ and $\theta_2 = -90$.

In conclusion, the effects of mixing between Z and Z'

bosons on various properties of Z can distinguish the model considered here from the other extended gauge models which also have an extra Z'. Further precision measurements of such effects would make such a distinction possible.

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