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# Charged-hyperon production by 400-GeV protons

T. R. Cardello,\* P. S. Cooper, L. J. Teig, J. L. Thron,<sup>†</sup> and Y. Wah<sup>‡</sup> Yale University, New Haven, Connecticut 06520

C. Ankenbrandt, J. P. Berge, A. E. Brenner, J. Butler, K. Doroba,<sup>§</sup> J. E. Elias, J. Lach, P. Laurikainen,<sup>\*\*</sup> J. MacLachlan, and J. Marriner Fermi National Accelerator Laboratory, Batavia, Illinois 60510

> E. W. Anderson, A. Breakstone,<sup>††</sup> and E. I. Rosenberg Iowa State University, Ames, Iowa 50011

> > E. McCliment

University of Iowa, Iowa City, Iowa 52242 (Received 26 November 1984)

Differential production cross sections have been measured for  $\Sigma^-$ ,  $\Xi^-$ ,  $\Omega^-$ ,  $\Sigma^+$ ,  $\overline{\Sigma}^+$ , and  $\overline{\Xi}^+$  relative to pion production at several  $x_F$  and  $P_T$  with  $0.24 \leq x_F \leq 0.90$  and  $P_T \leq 2$  GeV using 400-GeV protons incident on a Cu target. The data can be described by the function  $A(1-x_F)^n e^{-BP_T}$ , where A and n depend only on the hyperon type, and B is quadratic in  $x_F$ , and also depends on hyperon type. Comparison with previous experiments supports scaling in  $x_F$  over the range 200-400 GeV/c.

#### I. INTRODUCTION

We report here measurements of charged-hyperon and -antihyperon production over a broad range of Feynman x ( $x_F$ ) and transverse momentum ( $P_T$ ). The measurements were made in the Fermilab Proton Center chargedhyperon beam<sup>1</sup> using 400-GeV protons incident on a copper target. A narrow-band charged-hyperon beam was tuned to momenta in the range of 100-360 GeV/c, enabling us to explore the kinematic range  $0.24 \le x_F \le 0.90$ and  $P_T \le 2$  GeV/c. In this kinematic region, we describe the ratios of hyperon to pion production by the functional form

$$A (1 - x_F)^n e^{-B(x_F)P_T} , (1)$$

where A, n, and B depend on the hyperon type and B is a quadratic function of  $x_F$ .

In Sec. II of this paper, we describe the apparatus and trigger requirements for the various event topologies. Section III outlines the data reduction and analysis. Section IV describes the parametrization of the differential cross sections and compares our results with other, lowerenergy, measurements of hyperon production.

#### **II. APPARATUS AND TRIGGER LOGIC**

A plan view of the detector is shown in Fig. 1. A 400-GeV/c incident beam of between  $10^9$  and  $10^{12}$  protons per 1-sec pulse was incident on a  $14.8 \times 0.2 \times 0.2$ -cm<sup>3</sup> copper target. The primary beam had an angular divergence of 0.33-mrad full width at half maximum (FWHM), and a spot size of less than 1-mm FWHM at the target. The charged secondary beam was defined by a curved tungsten channel with a radius of curvature of 350 m, turning the secondary beam through 21 mrad. The rectangular aperture of the channel which was varied along its length was

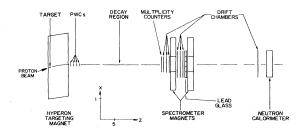


FIG. 1. Plan view of the experimental arrangement. Note the scales, different in x and z, are indicated in meters.

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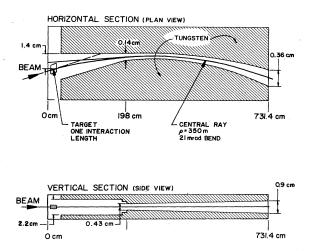


FIG. 2. Momentum-selecting channel. (Not to scale.) The noninteracting beam is dumped in the enlarged upstream section of the channel.

 $0.36 \times 0.9 \text{ cm}^2$  at its downstream end. At its upstream end, the channel also served as a dump for the noninteracting primary beam. Both the target and channel were inside the field region of a 7.3-m magnet, the hyperon magnet. The channel and target are shown in Fig. 2. The resulting secondary beam had a full width momentum spread of  $\Delta p / p = \pm 7\%$  and a solid angle of 0.64  $\mu$ sr. The momentum of the secondary beam, and thus its production  $x_F$ , was varied by changing the field in the dump magnet. The transverse momentum of the secondaries was varied by changing the angle of the incident proton beam relative to that defined by the channel, using an angle-varying bend magnet system.

Particles exiting the channel were required to be detected in a three-scintillation-counter beam telescope (B1, B2, B3). Particles outside the region defined by the channel were rejected by an additional pair of scintillators (VH1 and VH2). The locations of these counters are shown in Fig. 3.

High-resolution proportional wire chambers<sup>2</sup> (PWC's) were used to measure the trajectories of the secondary

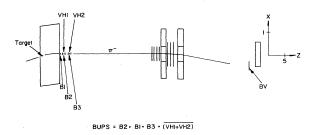


FIG. 3. Plan view of the apparatus defining the nondecaying trajectory. The scale is given in meters. Trigger scintillation counters B1, B2, and B3 and also halo veto counters VH1 and VH2 just downstream of B2 and B3, respectively, defined an incident particle. Beam veto (BV) identified a noninteracting, nondecaying particle. For the beam-upstream (BUPS) trigger, only the upstream scintillators are used. The nondecaying beam beam profile is shown downstream.

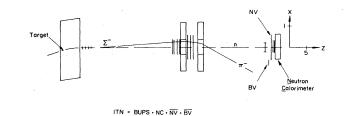


FIG. 4. The 1TN trigger type is defined by a BUPS trigger and a neutral particle hitting the neutron calorimeter (NC), preceded by a neutral veto (NV), and the nondecaying beam veto (BV). The most downstream magnet steers charged decay products away from the neutron counter and beam veto. Decayproduct profiles are shown downstream. Trigger 1TN is sensitive to decay modes (1), (2), and (3) in Table I. Scale is shown in meters.

particles. Positions were measured to better than 30  $\mu$ m (rms) and the angles of the tracks were measured to within 50  $\mu$ rad (rms). This information, when combined with the assumption that the particles originated in the target, resulted in a 0.7% (rms) momentum determination.

Downstream of the PWC's was an evacuated decay region 23 m long (10 m long for the 100-GeV/c data) followed by a drift-chamber spectrometer. A four-section scintillator multiplicity counter (M) immediately upstream of this spectrometer served to identify events with more than one charged decay product. Using the magnetic drift-chamber spectrometer with a  $P_T$  of 0.84 GeV/c, the positions, angles, and momenta of particles exiting the decay region were measured (rms) to within 150  $\mu$ m, 100  $\mu$ rad, and 1%, respectively.

Immediately downstream of this spectrometer, another magnet was used to provide additional momentum separation of the tracks. These tracks were further identified by the downstream trigger elements shown in Figs. 4 and 5. Two additional scintillators identified high-momentum stable tracks (BV) and protons (P) consistent with  $\Lambda$  decay. Events with a neutron decay were identified by an iron-scintillator calorimeter (NC) preceded by a scintillation counter (NV). The NC is composed of close packed alternating iron and plastic scintillator plates of dimensions 69.8×91.4 cm<sup>2</sup>. The nine scintillators were each 0.64 cm thick and the nine iron plates were each 5.1 cm in

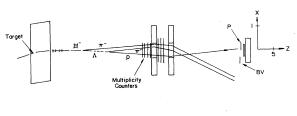




FIG. 5. The three-particle trigger type 3T is defined by a BUPS and two or more of the multiplicity counters and P and not BV. Trigger 3T is sensitive to decay modes (4), (5), and (6) in Table I. Decay-product profiles are shown downstream. Scale is shown in meters.

thickness. All of the scintillators were joined together on each of two opposite edges with light pipes, each of which was viewed by a single Philips 56 DVP 2-in. phototube.

The events of interest fell into three classes. The broadest class was defined as a simple straight track in the high-resolution PWC's, and required hits in B1, B2, and B3 and no hits in VH1 and VH2. The topology of these "beam upstream" (BUPS) triggers is shown in Fig. 3.

The second class of events was designed to include candidates for the decays

$$\Sigma^- \rightarrow n + \pi^-$$

and

These events required an upstream beam particle (BUPS), no downstream beam particle ( $\overline{BV}$ ), and the detection of a neutral particle ( $NC \cdot \overline{NV}$ ). The topology of these "one track plus a neutral" (1TN) event is shown in Fig. 4. In the final data sample, we required both a single charged nonbeam particle and a reconstructed vertex for an event to fall into this class.

The third class of events corresponded to a sequential decay, with two charged particles associated with the secondary vertex and one charged particle associated with the primary vertex. Events in this class were candidates for the decays

 $+\pi$ 

$$\Omega^- \to K^- + \Lambda$$

$$\downarrow_{\to p}$$

and

$$\begin{array}{c} \Xi^- \to \pi^- + \Lambda \\ \vdots \\ p + \pi^- \end{array}$$

For an event of this class, we required an upstream beam particle (BUPS), signals from at least two quadrants

TABLE I. Hyperons and decay modes studied. Antihyperons and their decay products are studied for all modes except (1) and (6).

	Decay	Branching ratio
(1)	$\Sigma^+ \rightarrow n + \pi^+$	0.48
(2)	$\Sigma^- \rightarrow n + \pi^-$	1.00
(3)	$\Xi^- \rightarrow \Lambda + \pi^- \\ \downarrow, n + \pi^0$	1.00 0.35
(4)	$\Xi^- \rightarrow \Lambda + \pi^-$ $\downarrow p + \pi^-$	1.00 0.64
(5)	$\begin{array}{c} \Omega^- \rightarrow \Lambda + K^- \\ \  \  \  \  \  \  \  \  \  \  \  \  \$	0.68 0.64
(6)	$\Omega^{-} \rightarrow \Xi^{0} + \pi^{-} \\ \downarrow \Lambda + \pi^{0} \\ \downarrow p + \pi^{-}$	0.23 1.00 0.64

of the multiplicity counter (M2), a proton signal (P) and no downstream stable beam particle  $(\overline{BV})$ . The topology of these three track events (3T) is shown in Fig. 5.

A summary of the hyperon decay modes which were studied is given in Table I.

The geometrical acceptance of the apparatus for decays within the decay region of our detector was 100%, except for the shorter decay region used at 100 GeV/c. Here the acceptance fell to 90%. Triggering efficiency for  $\Sigma^-$  and  $\Xi^-$  (1TN events) decaying within the decay region was 77%. The short length of the neutron calorimeter was the primary cause of the trigger inefficiency. The 3T events,  $\Omega^-$  and  $\Xi^-$ , which decayed in the decay region had a smaller triggering efficiency of 60%. For these 3T events, the primary loss of triggers was due to  $\Lambda$  decays downstream of the multiplicity counter.

## **III. DATA REDUCTION AND ANALYSIS**

The raw distribution of hits in the PWC's and drift chambers along with the trigger information was recorded on magnetic tape by a PDP 11/45 data-acquisition computer. Off-line a least-squares multitrack reconstruction algorithm was then applied to the data. Decay vertices were calculated from the fitted tracks and the differing decay hypotheses were imposed to calculate effective mass combinations. The events were then required to fall into one of the three classes (BUPS, 1TN, 3T) described previously. The various components of the secondary beam were identified as follows.

A.  $\pi^{\pm}$ 

The charged-pion signals were obtained from the nondecaying particles recorded with the BUPS trigger. To ensure that these beam particles did not decay, the momentum of these tracks as measured independently by the PWC's and the drift-chamber spectrometer were compared. Figure 6 shows a plot of the residuals variable

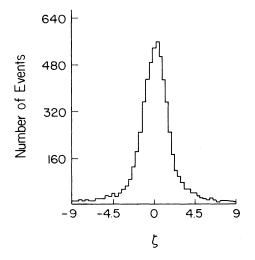


FIG. 6. A histogram of the residuals ( $\zeta$ ), representing the difference in momentum measured in the PWC's and in the drift-chamber spectrometer, relative to the rms resolution of the momentum measurements for nondecaying beam particles.

TABLE II. Cuts and tolerances applied to the data. The cut number code is as follows: (1) Minimum  $P_T$  of meson from bean vertex, (2) minimum vertex z, (3) maximum vertex z, (4) number of standard deviations in fit integration limits, (5) reject events within this tolerance of  $K^+$  mass, (6) maximum momentum nonconservation of decays, and (7) minimum mass calculated using  $\Lambda \pi^-$  hypothesis.

Cut	1T negati	ive beam	1T positive beam		3T only		
No.	<160 GeV	>160 GeV	<160 GeV	>160  GeV	<160 GeV	>160 GeV	
1	0.0188 GeV	0.028 GeV	· 0.032 GeV	0.032 GeV	0.0188 GeV	0.0188 GeV	
2	361.2 cm	450.0 cm	261.2 cm	311.2 cm	261.2 cm	261.2 cm	
3	1337.8 cm	2602.8 cm	1187.8 cm	2452.2 cm	1187.8 cm	2602.8 cm	
4	4	4	8	8	4	4	
5			0.02 GeV				
6					0.02	0.02	
7					1.341 GeV	1.341 GeV	

(2)

$$\zeta = rac{\sum \Delta_i}{\delta \Delta_i}$$
 ,

where  $\Delta_i$  is the difference in the *i*th component of the momentum vector as measured by the PWC's and the drift-chamber spectrometer and  $\delta \Delta_i$  is the rms resolution in  $\Delta_i$ . By demanding that  $\zeta$  lie within 4 standard deviations (4 $\sigma$ ) of the mean of this distribution we identify particles that do not decay within the decay volume of the apparatus. The known production cross sections<sup>3</sup> can then be used to infer the number of charged pions within this sample. All of our subsequent particle yields are given relative to pion production. Thus, the uncertainties in the pion-production cross sections introduce a systematic error in our results on hyperon production.

All of the hyperon-event candidates were identified by requiring at least one reconstructed vertex. In addition to the probability requirements imposed during track and vertex reconstruction, several additional requirements were imposed. (1) Nondecaying beam particles were eliminated by imposing a minimum transverse momentum requirement on the charged decay meson. This requirement also improved the decay vertex resolution. (2) All reconstructed vertices were required to lie within the vacuum decay region. This requirement reduced the background due to particle interactions. (3) For each hyperon an appropriately restricted mass<sup>4</sup> region was studied. (4) For the 100-GeV data, 1TN class events which had a fit consistent with the hypothesis

$$\begin{array}{c} K^{\pm} \rightarrow \pi^{0} + \pi^{\pm} \\ & \downarrow \qquad \gamma + \gamma \end{array}$$

were eliminated. At this energy,  $K^{\pm}$  is a source of background to the  $\Sigma^+$  and  $\Sigma^-$  signals and must be eliminated. Table II summarizes these criteria and others to be described below.

## B. $\Sigma^-$ , $\Xi^-$ , and $\overline{\Xi}^+$

The  $\Sigma^-$ ,  $\Xi^-$ , and  $\overline{\Xi}^+$  signals were obtained from events in the 1TN class, assuming the decays

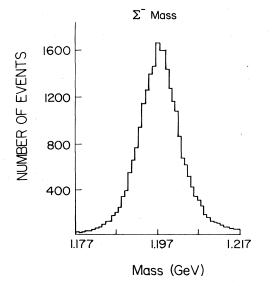


FIG. 7. The measured  $\Sigma^-$  mass distributions. In this distribution, there are 24471 entries. Of these after subtracting background, there are  $24294\pm191 \Sigma^-$  events.

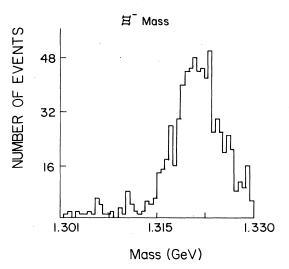


FIG. 8. The measured  $\Xi^-$  mass distribution. The range of this histogram was chosen to minimize the background from the  $\Sigma^-$ . There are 709 entries in this histogram, of which  $642\pm35$  are  $\Xi^-$  events.

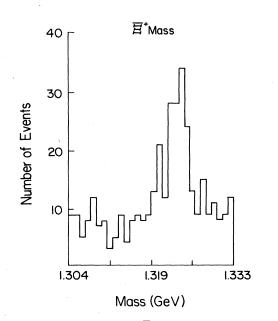


FIG. 9. A histogram of the  $\overline{\Xi}^+$  mass. In this distribution, there are 359 entries. Of these,  $136\pm30$  are estimated to be  $\overline{\Xi}^+$  over a background of  $223\pm24$  events.

$$\begin{split} \Sigma^{-} &\to n + \pi^{-} , \\ \Xi^{-} &\to \Lambda + \pi^{-} \\ & & \downarrow \rightarrow n + \pi^{0} , \\ \overline{\Xi}^{+} &\to \overline{\Lambda} + \pi^{+} \\ & & \downarrow \rightarrow \overline{n} + \pi^{0} . \end{split}$$

The appropriate two-body effective-mass distributions are shown in Figs. 7–9. In each case, the mass distribu-

TABLE III. Decay modes and fit functions. The  $a_i$  are the fitted parameters. m is the hyperon mass assuming the stated decay mode. Antiparticles are treated in the same manner as particles unless explicitly stated.

Decay mode	Fitted function	
$\Sigma^- \rightarrow n + \pi^-$	F'	
$\Xi^- \rightarrow \Lambda + \pi^-$		
$  n + \pi^{0} $	F ·	
$\Xi^- \rightarrow \Lambda + \pi^-$		
	F	
$\Omega^- \rightarrow \Lambda + K^-$	•	
	None	
$\Sigma^+ \rightarrow n + \pi^+$	F+G	
$\overline{\Sigma}^+ \rightarrow \overline{n} + \pi^+$	F+G	

Functions

$$F = a_1 + a_2 m + \frac{a_3}{a_4 \sqrt{2\pi}} \exp[-(m - a_5)^2 / 2a_4^2]$$
  

$$F' = F + \frac{a_6}{2a_4 \sqrt{2\pi}} \exp[-(m - a_5)^2 / 8a_4^2]$$
  

$$G = \frac{a_6}{a_4 \sqrt{2\pi}} \exp[-(m - a_5 - \delta)^2 / 2a_4^2]$$
  

$$\delta = \overline{\Sigma}^+ - \Sigma^+ \text{ mass difference}$$

tion was fit to a Gaussian peak plus a linear background term. The background arises from misidentified events and from interactions in and downstream of the channel. Table III summarizes these fitting functions. The number of hyperons was defined as those events within  $4\sigma$  of the mean effective mass of the peak less the integral of the background term over this mass region.

## C. $\Sigma^+$ and $\overline{\Sigma}^+$

The 1TN class of events is also a source of candidates for the decays

$$\Sigma^+ \rightarrow n + \pi^+$$
,  
 $\overline{\Sigma}^+ \rightarrow \overline{n} + \pi^+$ .

The  $\pi^+$  + (neutrals) effective mass at  $x_F = 0.27$  is plotted in Fig. 10. Since the  $\Sigma^+ - \overline{\Sigma}^+$  mass difference (8 MeV) is less than twice our effective-mass resolution (4.5 MeV), we fit this data to two Gaussian peaks plus a linear background term. The Gaussians were constrained to have the same width and a fixed separation of 8 MeV. The total number of  $\Sigma^+$  and  $\overline{\Sigma}^+$  was defined as the total number of events in the plot less the integral of the background term. The relative number of  $\Sigma^+/\overline{\Sigma}^+$  was defined as the ratio of the amplitudes of the fitted Gaussians.

A further test of the two-peak hypothesis for the  $\pi^+$  + (neutral) effective-mass plot is based on the  $\Sigma^+/\overline{\Sigma}^+$  lifetime difference. Requiring the decay vertex to lie in the upstream half of the decay region enhances the  $\Sigma^+$  signal; requiring vertices in the downstream half enhances the  $\overline{\Sigma}^+$  signal. Figure 11 superimposes the  $\pi^+$  + (neutral) effective-mass plots for these two requirements. The plots are normalized to the same number of events and show the anticipated mass shift.

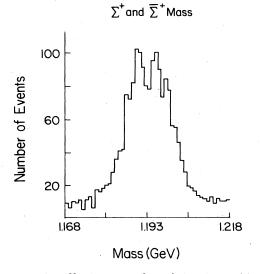
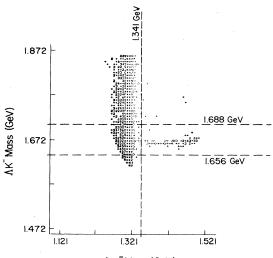


FIG. 10 The effective mass for  $\pi^+$  + (neutrals) at 100-GeV/c incident momentum and  $x_F=0.27$ . These represent the  $\Sigma^+$  and  $\overline{\Sigma}^+$  sample plus background. Shown are 1895 entries with 1.0-MeV bin width. The fits described in the text result in  $703\pm50 \Sigma^+$ ,  $643\pm50 \overline{\Sigma}^+$ , and  $549\pm33$  background events.

FIG. 11. The  $\Sigma^+$  and  $\overline{\Sigma}^+$  mass histogram divided into the first and second half of the decay fiducial volume. In order to see that Fig. 10 is composed of two distinct signals, events which decay in the second half of the decay volume are removed from Fig. 10 and the result shown by the solid histogram. The  $\overline{\Sigma}^+$  signal is thereby reduced relative to the  $\Sigma^+$ . Events which decay in the first half of the decay volume are removed from Fig. 10 and the area normalized result is shown by the dashed histogram. The  $\overline{\Sigma}^+$  signal is thereby enhanced relative to the  $\Sigma^+$ .



 $\Lambda\pi$  Mass (GeV)

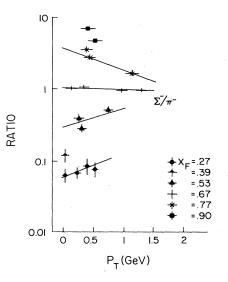
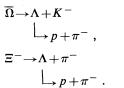


FIG. 13. The  $\Sigma^-/\pi^-$  production ratios as a function of  $P_T$  at a number of  $x_F$ . The fitted function f is also shown.

**D**. Ω<sup>-</sup>

The events in the 3T class are candidates for the decays



The  $\Lambda$  is identified using two of the tracks in the driftchamber spectrometer. The  $\Lambda K^-$  and  $\Lambda \pi^-$  mass hypotheses are then used to distinguish the  $\Omega^-$ 's from the  $\Xi^-$  background. Figure 12 is a scatter plot of the two effective-mass combinations. For both the  $\Omega^-$  and  $\Xi^$ yields, the density of nonresonant points within the

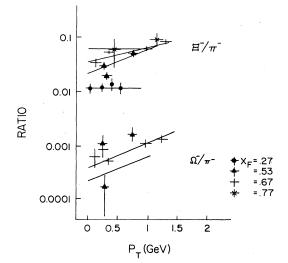


FIG. 14. The  $\Xi^-/\pi^-$  and  $\Omega^-/\pi^-$  production ratios as a function of  $P_T$ . The fitted function f as described in the text is also shown.

TABLE IV. Measured production ratios at the target. The errors listed are statistical (systematic). The asterisk denotes an average over a wide range of  $P_T$ . For the  $\Sigma^+$  for  $x_F > 0.6$  no correction has been made for contributions from  $\overline{\Sigma}^+$ .

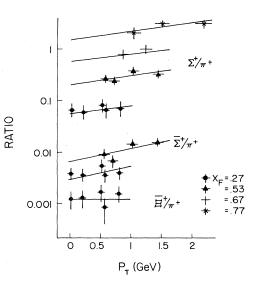
$x_F$	$P_T$ (GeV/c)	Ratio	Error	$x_F$	$P_T$ (GeV/c)	Ratio	Error
	(a	) $\Sigma^-/\pi^-$				) $\Sigma^+/\pi^+$	
$0.90 \pm 0.03$	$0.37 \pm 0.12$	7.03	0.30 (0.90)	$0.78 {\pm} 0.03$	$1.46 \pm 0.12$	3.26	0.35 (0.82)
$0.89 \pm 0.03$	$0.49 \pm 0.12$	4.68	0.20 (0.60)	$0.77 \pm 0.03$	$2.15 \pm 0.13$	3.35	0.60 (0.84)
$0.78 \pm 0.03$	$0.35 \pm 0.10$	3.50	0.16 (0.06)	$0.77 \pm 0.03$	$1.00 \pm 0.11$	2.09	0.49 (0.53)
$0.77 \pm 0.03$	$0,40 \pm 0.10$	2.71	0.14 (0.04)	$0.64 {\pm} 0.02$	$0.84 \pm 0.09$	0.78	0.16 (0.14)
0.76±0.03	$1.11 \pm 0.11$	1.62	0.11 (0.03)	$0.64 \pm 0.02$	$1.21 \pm 0.10$	1.00	0.17 (0.18)
$0.67 \pm 0.03$	$0.31 \pm 0.09$	1.05	0.025 (0.010)	$0.54 {\pm} 0.02$	$1.01 \pm 0.08$	0.371	0.040 (0.046)
$0.67 \pm 0.02$	$0.10 \pm 0.09$	1.02	0.055 (0.010)	$0.53 {\pm} 0.02$	$0.69 \pm 0.08$	0.235	0.031 (0.030)
$0.66 {\pm} 0.03$	$0.94 \pm 0.09$	0.938	0.031 (0.009)	$0.53 \pm 0.02$	$0.55 {\pm} 0.07$	0.260	0.031 (0.032)
$0.66 \pm 0.03$	$1.27 \pm 0.10$	0.946	0.047 (0.009)	$0.52 \pm 0.02$	$1.42 \pm 0.09$	0.323	0.039 (0.041)
$0.54 {\pm} 0.02$	$0.28 {\pm} 0.07$	0.284	0.032 (0.003)	$0.27 \pm 0.01$	$0.81 \pm 0.05$	0.071	0.022 (0.003)
$0.53 \pm 0.02$	$0.23 \pm 0.07$	0.387	0.027 (0.004)	$0.26 {\pm} 0.01$	$0.57 {\pm} 0.04$	0.065	0.019 (0.003)
$0.53 \pm 0.02$	$0.72 \pm 0.07$	0.510	0.027 (0.005)	$0.26 {\pm} 0.01$	$0.51 \pm 0.04$	0.081	0.023 (0.004)
$0.39 \pm 0.01$	$0.01 \pm 0.05$	0.123	0.024 (0.000)	$0.26 \pm 0.01$	$0.01 \pm 0.03$	0.065	0.014 (0.003)
$0.27 \pm 0.01$	$0.21 \pm 0.04$	0.069	0.010 (0.000)	$0.26 \pm 0.01$	$0.20 \pm 0.04$	0.059	0.017 (0.003)
$0.27 \pm 0.01$	$0.01 \pm 0.04$	0.064	0.011 (0.000)				
$0.27 \pm 0.01$	$0.37 {\pm} 0.04$	0.086	0.019 (0.000)				
$0.27 \pm 0.01$	$0.51 \pm 0.04$	0.077	0.017 (0.000)				
	(b	) $\Xi^{-}/\pi^{-}$					
$0.90 \pm 0.03$	0.37±0.12	0.0574	0.0098 (0.0074)		<b>^</b>		
$0.89 \pm 0.03$	$0.49 \pm 0.12$	0.0360	0.0058 (0.0046)				
$0.77 \pm 0.03$	$0.40 \pm 0.10$	0.060	0.032 (0.001)				
$0.76 \pm 0.03$	$1.11 \pm 0.11$	0.091	0.021 (0.001)		(e)	$\overline{\Sigma}^{+}/\pi^{+}$	
$0.68 \pm 0.03$	$0.32 \pm 0.09$	0.0531	0.0029 (0.0005)	$0.54 \pm 0.02$	$1.01 \pm 0.08$	0.0141	0.0018 (0.0017)
$0.67 \pm 0.03$	$0.10 \pm 0.09$	0.0339	0.0041 (0.0003)	$0.53 \pm 0.02$	$0.69 \pm 0.08$	0.0069	0.0018 (0.0008)
$0.67 \pm 0.03$	$0.94 \pm 0.10$	0.0616	0.0036 (0.0006)	$0.53 \pm 0.02$	$0.55 \pm 0.07$	0.0089	0.0018 (0.0011)
$0.66 \pm 0.03$	$1.27 \pm 0.10$	0.0830	0.0057 (0.0008)	$0.52 \pm 0.02$	$1.42 \pm 0.09$	0.0154	0.0024 (0.0002)
$0.54 \pm 0.02$	$0.28 \pm 0.07$	0.0196	0.0025 (0.0002)	$0.27 \pm 0.01$	$0.81 \pm 0.05$	0.0040	0.0012 (0.0002)
$0.54 \pm 0.02$	$0.23 \pm 0.07$	0.0302	0.0030 (0.0003)	$0.26 \pm 0.01$	$0.57 \pm 0.04$	0.0036	0.0010 (0.0002)
$0.53 \pm 0.02$	$0.72 \pm 0.08$	0.0501	0.0047 (0.0005)	$0.26 \pm 0.01$	$0.51 \pm 0.04$	0.0055	0.0014 (0.0002)
$0.40 \pm 0.02$	$0.01 \pm 0.05$	0.0192	0.0040 (0.0002)	$0.26 \pm 0.01$	$0.01 \pm 0.03$	0.0038	0.0007 (0.0002)
$0.28 \pm 0.01$	$0.21 \pm 0.04$	0.0120	0.0019 (0.0000)	$0.26 \pm 0.01$	$0.20 \pm 0.04$	0.0036	0.0009 (0.0002)
$0.28 \pm 0.02$	$0.37 \pm 0.04$	0.0139	0.0033 (0.0000)				
$0.28 \pm 0.01$	$0.01 \pm 0.04$	0.0113	0.0020 (0.0000)				
$0.27 \pm 0.01$	$0.01 \pm 0.04$	0.0117	0.0026 (0.0000)				
	(c)	) $\Omega^-/\pi^-$					
0.90±0.03	0.43*	0.000 56	(0.000 56)				
$0.90 \pm 0.03$ $0.77 \pm 0.03$	0.52*	0.000 30	(0.000 30)				
$0.77 \pm 0.03$ $0.67 \pm 0.03$	$1.22 \pm 0.10$	0.000 80	(0.00080) $0.00017\ (0.00001)$				
$0.67 \pm 0.03$ $0.67 \pm 0.03$	$0.95 \pm 0.10$	0.001 22	0.00017 (0.00001)				
$0.67 \pm 0.03$ $0.67 \pm 0.03$	$0.93 \pm 0.10$ $0.33 \pm 0.09$	0.001 02	0.00018(0.00001) 0.00007(0.00001)				
$0.67 \pm 0.03$ $0.67 \pm 0.03$	$0.33 \pm 0.09$ $0.10 \pm 0.09$	0.000 47	0.00007(0.00001) 0.00023(0.00001)		( <b>f</b> )	$\Xi^+/\pi^+$	
$0.67 \pm 0.03$ $0.67 \pm 0.03$	$0.10\pm0.09$ $0.24\pm0.09$	0.000 39	0.000 23 (0.000 01)	0.27±0.01	$0.81 \pm 0.05$	$= 7\pi$ 0.001 56	0.000 56 (0.000 04)
$0.67 \pm 0.03$ $0.54 \pm 0.02$			0.00018(0.00001) 0.00012(0.000002)		$0.81 \pm 0.03$ $0.57 \pm 0.04$	0.001 36	0.00038(0.00004) 0.00045(0.00004)
$0.34 \pm 0.02$ $0.54 \pm 0.02$	$0.28 \pm 0.07$ $0.23 \pm 0.07$	0.000 17 0.001 09	0.00012(0.000002) 0.00048(0.00001)	$0.26 \pm 0.01$ $0.26 \pm 0.01$	$0.37 \pm 0.04$ 0.51 ± 0.04	0.000 84	0.000 43 (0.000 04)
$0.34 \pm 0.02$ $0.54 \pm 0.02$	$0.23 \pm 0.07$ $0.73 \pm 0.08$			$0.26 \pm 0.01$ $0.26 \pm 0.01$	$0.01 \pm 0.04$ 0.01 ± 0.03	0.001 71	$0.00062\ (0.00007)$ $0.00045\ (0.00005)$
$0.34 \pm 0.02$ $0.27 \pm 0.01$	0.23*	0.001 64 0.000 35	0.00045(0.00002)	$0.26 \pm 0.01$ $0.26 \pm 0.01$	$0.01\pm0.03$ $0.20\pm0.04$	0.001 22	0.000 43 (0.000 03)
$0.27 \pm 0.01$	0.23	0.000.33	(0.00025)	0.2010.01	0.20 ±0.04	0.001 29	0.000 51 (0.000 08)

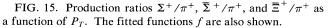
respective mass bands is assumed to be the same as that outside the bands. The  $\Omega^-$  events are defined as those with  $M_{\Lambda\pi^-} \ge 1.341$  GeV and  $1.656 \le M_{\Lambda K^-} \le 1.688$  GeV.

events classes is well understood. This enables us to combine ratios  $(\Omega^-/\Xi^-)_{3T}$  and  $(\Xi^-/\pi^-)_{1TN}$  in obtaining the relative  $\Omega^-$  to  $\pi^-$  yields.

While not used in quoting  $\Xi^-$  yields, the number of  $\Xi^-$  events obtained from the 3T class can be compared with that obtained from the 1TN class. To within the statistical accuracy of the data, the yields are identical. Thus we are confident that the relative acceptance for the two

The hyperon yields at the production target are determined from the number of hyperons observed in the various mass plots. We apply corrections for various loss mechanism: reabsorption in the target, upstream decays, trigger inefficiency, geometric acceptance, and reconstruc-





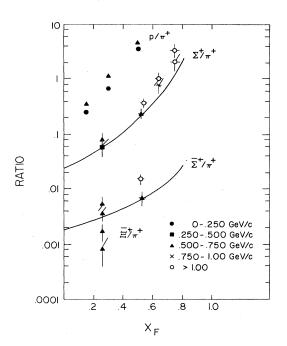
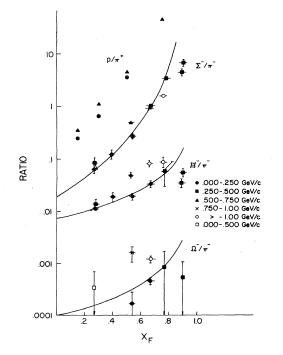


FIG. 17. The production ratios  $\Sigma^+/\pi^+$ ,  $\overline{\Sigma}^+/\pi^+$ , and  $\overline{\Xi}^+/\pi^+$  as a function of  $x_F$ . For each value of  $x_F$ , the extreme values as measured by this experiment are plotted and the  $P_T$  value of the measurement indicated. The solid lines represent the  $P_T=0$  fits of Eq. (3). Also plotted is the production ratio  $p/\pi^+$  reported in Ref. 6 corrected for target differences as described in the text.



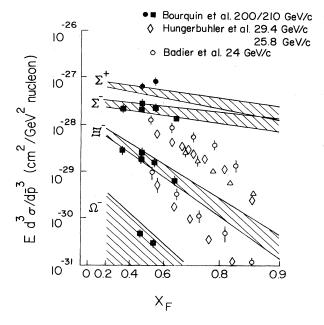


FIG. 16. The production ratios  $\Sigma^-/\pi^-$ ,  $\Xi^-/\pi^-$ , and  $\Omega^-/\pi^-$  as a function of  $x_F$ . For each value of  $x_F$ , the extreme values as measured by this experiment are plotted and the  $P_T$  value of the measurement indicated. The solid lines represent the  $P_T=0$  fits of Eq. (3). Also plotted is the production ratio  $p/\pi^+$  reported in Ref. 6 corrected for target differences as described in the text.

FIG. 18. The invariant cross section for charged-hyperon production at low  $P_T$ . This double-logarithmic plot with a natural abscissa in  $1-x_F$ , is labeled in  $x_F$ . The data of this experiment is extrapolated to  $P_T=0$  and normalized to the pion cross section as described in the text. The bands represent the  $1\sigma$  extent of this extrapolation. Also plotted are the corresponding data from Refs. 7–9.

Ratio	<i>a</i> <sub>1</sub>	<i>a</i> <sub>2</sub>	<i>a</i> <sub>3</sub>	<i>a</i> <sub>4</sub>	<i>a</i> <sub>5</sub>	$\chi^2/\mathrm{DF}$	
$\Sigma^-/\pi^-$	0.0194 ±0.0024	$-3.60\pm0.11$	$0.45 \pm 0.84$	$-7.5\pm2.5$	10.3±2.0	19/12	
$\Xi^{-}/\Sigma^{-}$	$0.379 \pm 0.025$	$2.10 \pm 0.11$	$0.87 \pm 0.48$	$-0.8 \pm 2.0$	$-2.2\pm1.6$	12/11	
$\Xi^-/\pi^-$	$0.0077 \pm 0.0012$	$-1.33\pm0.17$	$4.6 \pm 1.1$	$-22.2\pm3.7$	$21.3 \pm 3.2$	19/11	
$\Omega^{-}/\Xi^{-}$	$0.047 \pm 0.039$	$1.42 \pm 0.77$	$-0.46\pm0.14$			10/5	
$\Omega^{-}/\Sigma^{-}$	$0.00669 \pm 0.0061$	$2.66 \pm 0.82$	$-1.15\pm0.16$			10/5	
$\Omega^-/\pi^-$	$0.0001 \pm 0.0001$	$-1.5 \pm 1.0$	$-0.94{\pm}0.17$			10/5	
$\Sigma^+/\pi^+$	$0.0245 \pm 0.0027$	$-2.88{\pm}0.16$	$-0.35 \pm 0.12$			8/11	
$\overline{\Sigma}^{+}/\pi^{+}$	$0.00187\pm0.00036$	$-1.65 \pm 0.40$	$-0.59 \pm 0.21$			8/6	
$\overline{\Sigma}^+ / \Sigma^+$	$0.0824 \pm 0.0058$	$1.13 \pm 0.20$	$-0.09\pm0.11$			6/6	
$\overline{\Xi}^+/\pi^+$	$0.00120\pm0.00037$		$-0.08 \pm 0.64$			2/3	
$\overline{\Xi}^+ / \Sigma^+$	$0.0182 \pm 0.0032$		0.0 ±0.34			2/3	
$\overline{\Xi}$ + $\overline{\Sigma}$ +	$0.318 \pm 0.056$		$0.02 \pm 0.35$			2/3	
$\Sigma^+/p$	$0.0310 \ \pm 0.0035$	$-0.38 {\pm} 0.16$	$-0.35 {\pm} 0.013$			8/11	

TABLE V. Fit results for the function  $a_1(1-x_F)^{a_2}e^{-P_T(a_3+a_4x_F+a_5x_F^2)}$ . The  $\chi^2$ /DF is the fit  $\chi^2$  per degree of freedom.

tion inefficiency. The uncertainty in the yields due to applying these corrections is less than 5%. Most of our results are expressed in terms of relative yields so that dependence on the channel acceptance is minimized. In addition, by comparing particles in the same trigger class and with similar topologies we minimize the dependence on trigger and reconstruction inefficiences. This reduces the errors on the relative yields. A summary of the yield results is given in Table IV.

#### **IV. RESULTS**

We represent our hyperon-to-pion production ratios in a conventional form<sup>5</sup> given by Eq. (1), based on first-order perturbative QCD models. We determine the function  $B(x_F)$  by fitting the data to the form  $Ce^{-BP_T}$  at each measured value of  $x_F$ . From the variation of B with  $x_F$ , we find  $B(x_F)$  can be described as a quadratic polynomial in  $x_F$  for each hyperon studied.

The ratios are then fit to the function

$$f = a_1 (1 - x_F)^{a_2} e^{-P_T (a_3 + a_4 x_F + a_5 x_F^2)} .$$
(3)

Figures 13 through 15 show the ratios measured as a function of  $P_T$  along with the fitted function f. Table V gives our fits to the parameters  $a_1$  through  $a_5$  for each measured ratio. The fits are not particularly good as can be seen from the values of the  $\chi^2/DF$ , indicating the inadequacy of the first-order QCD models to represent this production mechanism. Using these fitted parameters, the ratios are calculated at  $P_T=0$ , yielding the solid curves shown in Figs. 16 and 17. The  $P_T=0$  curves are added to help guide the eye.

Also shown in Figs. 16 and 17 are our measurements of

these production ratios. We plot only the extreme values as a function of  $x_F$  and indicate the  $P_T$  region in which these measurements are made. For comparison with nonstrange-baryon production, we have scaled the measurements<sup>6</sup> of  $p/\pi^+$  at 400 GeV/c to a beryllium target containing the same number of interaction lengths as our copper target. In all cases, we note the sharp rise of the hyperon to pion yield as a function of  $x_F$ .

To compare our data to lower-energy measurements<sup>7-9</sup> of charged-hyperon production, made at a number of different energies with different targets and mostly in the forward direction, we extrapolate our fits of the relative hyperon to pion production to  $P_T = 0$ . The absolute hyperon production cross sections are obtained by combining these extrapolations with the pion invariant cross sections as parametrized in Ref. 7. In Fig. 18, we plot the  $1\sigma$  extent of these absolute cross sections along with the lowerenergy data. In the region of overlap, our extrapolated fit well represents the measurements of Bourquin et al.<sup>7</sup> and supports  $x_F$  scaling in the energy regime 200-400 GeV/c. Neither of the high-energy experiments scales with the 20-30-GeV/c data.<sup>8,9</sup> The leading particle effect is evident in the rather slow decrease in  $E d^3 \sigma / dp^3$  as a function of  $x_F$ . It is also apparent in the change in slope when comparing  $\Xi^-$  to  $\Sigma^-$  production.

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saw, Poland.

- \*\*Present address: Department of High Energy Physics, University of Helsinki, Helsinki, Finland.
- <sup>††</sup>Present address: Department of Physics, University of Hawaii, Honolulu, HI 96822.
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Present address: 159 Islington St., Staten Island, NY 10308.

<sup>&</sup>lt;sup>†</sup>Present address: High Energy Physics Division, Argonne National Laboratory, Argonne, IL 60439.

<sup>&</sup>lt;sup>‡</sup>Present address: Enrico Fermi Institute, University of Chicago, Chicago, IL 60637.

<sup>§</sup>Present address: Institute of Physics, Warsaw University, War-

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