

## Charged Higgs bosons, charged hyperpions, and the nonleptonic decays of heavy-flavored mesons

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We find that the existence of charged Higgs bosons  $H^\pm$  or charged hyperpions  $P^\pm$  may enhance the nonleptonic decays of the pseudoscalar  $t$ -flavored mesons  $T_q$ . This, in turn, would induce a difference in the average kaon multiplicities expected for two-jet events in  $T_b$  and  $T_b^*$  decays and therefore provide a possible way to discriminate between  $T_b$  and  $T_b^*$  production in  $e^+e^-$  annihilation.

### I. INTRODUCTION

It was recently pointed out<sup>1</sup> that the weak interactions are expected to dominate the decays of the heavy-flavored mesons  $T_q$  and  $T_q^*$ , which are composed of the hypothetical heavy  $t$  quark and light quark  $q$ . This result arises from the estimates that the vector  $T_q^*$  and pseudoscalar  $T_q$  states are separated by less than a pion mass, the strong decay  $T_q^* \rightarrow T_q \pi$  is then kinematically forbidden, and the electromagnetic transition  $T_q^* \rightarrow T_q \gamma$  is strongly suppressed, yielding widths of just few eV. On the other hand, in the valence-quark approximation, the weak hadronic total decay rate is simply given by the  $t$ -quark cascade transition  $t \rightarrow b \sum (q\bar{q}' + l\nu)$ , the light quark  $q$  acting as spectator, which yields widths of order a few keV (Ref. 1). Corrections to this approximation are given by nonspectator contributions, which are in general negligible except for the  $T_q^*$  mesons, where the annihilation of the  $t\bar{q}$  system in the  $s$  channel through the exchange of a  $W$  boson gives a sizable contribution.<sup>2</sup> In the scenario outlined above, the final states in  $e^+e^- \rightarrow T_q \bar{T}_q$ ,  $T_q^* \bar{T}_q^*$  would be essentially identical to those in the  $e^+e^- \rightarrow t\bar{t}$  continuum above threshold, and it would be very difficult to discriminate between  $T_q$  and  $T_q^*$  production.

In the present note we study the effect of charged Higgs bosons  $H^\pm$  and charged pseudo-Goldstone bosons  $P^\pm$  (hyperpions) on the nonleptonic decays of the  $T_q^*$  and  $T_q$  mesons. These particles are predicted in most extensions of the standard electroweak model,<sup>3</sup> in all its supersymmetric versions, and in the extended hypercolor (EHC) models.<sup>4</sup> If these particles exist with mass lower than the mass of the  $t$  quark and their coupling to fermions is proportional to the mass of the heaviest fermion available, it is known<sup>2,5,6</sup> that the decay of the  $t$  quark will be dominated by the production of real  $H^\pm$  ( $P^\pm$ ). In this case, both  $T_q$  and  $T_q^*$  mesons will decay predominantly into  $H^\pm$  ( $P^\pm$ ) +  $X$ , the final states in  $e^+e^- \rightarrow T_q \bar{T}_q$ ,  $T_q^* \bar{T}_q^*$  will be again identical to those in  $e^+e^- \rightarrow t\bar{t}$  continuum above threshold, and it would be also very difficult to distinguish between  $T_q$  and  $T_q^*$  production.

In a previous note,<sup>7</sup> one of us studied the purely leptonic decays of the  $T_q$  and  $T_q^*$  mesons in the framework of some models which predict  $H^\pm$  ( $P^\pm$ ) particles. It was pointed out that since only "light" leptons can be produced in these decays, helicity suppression is active, and the leptonic  $T_q^*$ -

meson decays then will proceed via weak annihilation into  $W^\pm$ , while the leptonic  $T_q$ -meson decays will proceed through  $H^\pm$  ( $P^\pm$ ) annihilation. Even though it was found that some of the leptonic decays of the  $T_b$  meson could be comparable to the leptonic  $T_b^*$  decays, a measurement of these decay modes would not discriminate between  $T_b$  and  $T_b^*$  production. In the present note we will find that if  $H^\pm$  ( $P^\pm$ ) exists with  $m_H < m_t$ , they will induce measurable effects in the nonleptonic decays of  $T_b^*$  and  $T_b$  mesons. Although these effects are expected to be too small to be used as an evidence for the existence of  $H^\pm$  ( $P^\pm$ ), they can be used to discriminate between  $T_b$  and  $T_b^*$  production. In particular, we have found that the presence of  $H^\pm$  ( $P^\pm$ ) may enhance some of the nonleptonic annihilation decays of the  $T_b$  meson. This in turn will induce that the average kaon multiplicity expected for two-jet events in  $T_b$  decay is slightly greater than the one expected for two-jet events in  $T_b^*$  decays. The production of either  $T_b$  or  $T_b^*$  is expected to have a very small cross section in almost any reaction, except, perhaps, in the case<sup>1,2</sup> that a  $t$ -quarkonium state decays by a spectator mechanism into  $(t\bar{t}) \rightarrow (t\bar{b}) + W^-$  virtual ( $H^-$  real), where the  $(t\bar{b})$  system will fuse to form a  $T_b$  state 26% of the time and a  $T_b^*$  state 74% of the time. Therefore, if the production of  $T_b$  and  $T_b^*$  is experimentally feasible in this way, one could distinguish between  $T_b$  and  $T_b^*$  production by studying the average kaon multiplicities in events like  $e^+e^- \rightarrow$  two jets +  $l\nu$  (large  $p_T$ ).

### II. NONLEPTONIC ANNIHILATION DECAYS

A simple analysis of the mass dependence of QCD effects in  $t$ -quark decays indicates that one can safely neglect strong effects and use simple  $W$ -exchange diagrams.<sup>2,8</sup> Consequently, the spectator model for  $T$ -meson decays is well justified and only the vector meson  $T_b^*$  may have a sizeable nonspectator component through annihilation via  $W$  exchange.<sup>2</sup> We will assume that the heavy  $t$  quark exists with  $m_t < M_W$  in the context of the three-generation extension of the standard model.<sup>9</sup> For simplicity, we assume that nature uses either elementary Higgs fields or the hypercolor scheme but not both, and that the  $H^\pm$  ( $P^\pm$ )-fermion couplings can be parametrized as

$$L_{\text{eff}} = i(\sqrt{2}G_F)^{1/2}H^+ \{ \bar{u} [C_1 U_{KM} M_d (1 + \gamma_5) + C_2 M_u U_{KM} (1 - \gamma_5)] d + C_3 M_e \bar{\nu} (1 + \gamma_5) e \} + \text{H.c.} , \quad (2.1)$$

where the symbols  $u$ ,  $d$ ,  $\nu$ , and  $e$  refer to the conventional type of fermions of charges  $2/3$ ,  $-1/3$ ,  $0$ , and  $-1$ , respectively,  $M_{u,d,e}$  are the corresponding diagonalized mass matrices, and  $U_{KM}$  is the conventional Kobayashi-Maskawa matrix.<sup>9</sup> The coefficients  $C_i$  in Eq. (2.1) are rather model dependent. They are of order unity in some "monophagic" hypercolor models,<sup>6</sup> and for the standard model with two Higgs doublets,  $C_i = \eta_1/\eta_2$ ,  $\eta_2/\eta_1$ , or  $1$ , where  $\eta_1$  and  $\eta_2$  are the respective Higgs-field vacuum expectation values.<sup>10</sup>

We are going to take separately the two possibilities that  $H^\pm$  ( $P^\pm$ ) exists with either  $m_H > m_t$  or  $m_H < m_t$ . In the first case, the decay widths of both  $T_q^*$  and  $T_q$  mesons are determined mainly by the spectator diagram shown in Fig. 1(a), and it is given by

$$\Gamma_S(t \rightarrow b \sum (q\bar{q}' + l\nu)) \cong \frac{3G_F^2 m_t^5}{64\pi^3} \left( 1 + \frac{192C_2^2 m_t^2 (C_1^2 U_{cb}^2 m_b^2 + C_2^2 U_{cs}^2 m_c^2 + C_3^2 m_\tau^2)}{206m_H^4} \right) , \quad (2.2)$$

where the second term in the large parentheses is the  $H^\pm$ -exchange contribution and in general is negligible. In the second case, if  $m_H < m_t$ , the decay widths of both  $T_q^*$  and  $T_q$  are now determined by the diagram shown in Fig. 1(b) for the creation of a real  $H^\pm$ :

$$\Gamma_H(t \rightarrow bH^+) \cong \frac{\sqrt{2}G_F C_2^2 U_{tb}^2 m_t^3}{16\pi} . \quad (2.3)$$

The nonleptonic decays of the charged mesons  $T_q^*$  and  $T_q$  will have characteristic three- or two-jet events depending if they arise through spectator [Fig. 1(a)] or annihilation [Fig. 1(c)] diagrams, respectively. In the last case, since only "light" quarks can be produced, helicity suppression is active, the exchange of  $H^\pm$  ( $P^\pm$ ) is helicity suppressed for the vector state, and  $T_{q_1}^* \rightarrow q_2\bar{q}_3$  is determined only by  $W^\pm$

exchange:

$$\Gamma_a(T_{q_1}^* \rightarrow q_2\bar{q}_3) \cong \frac{G_F^2 f_V^2 U_{t1}^2 U_{23}^2 M_T^3}{4\pi (1 - M_T^2/M_W^2)^2} , \quad (2.4)$$

where  $M_t \cong m_t + m_{q_1}$  and  $f_V(T_q^*)$  is proportional to the  $T_q^*$  wave function at the origin. Simple potential-model calculations indicate<sup>1</sup> that  $f_V(T_b^*) \cong 700$  MeV,  $f_V(T_s^*) \cong 90$  MeV, and  $f_V(T_d^*) \cong 70$  MeV. On the other hand, the exchange of  $W^\pm$  is helicity suppressed for the pseudoscalar state and  $T_{q_1} \rightarrow q_2\bar{q}_3$  is determined only by  $H^\pm$  exchange:

$$\begin{aligned} \Gamma_a(T_{q_1} \rightarrow q_2\bar{q}_3) \\ \cong \frac{3G_F^2 f_V^2 U_{t1}^2 U_{23}^2 M_T^3 (C_1 m_1 - C_2 m_t)^2 (C_1^2 m_4^2 + C_2^2 m_3^2)}{8\pi (M_T^2 - m_H^2)^2} , \end{aligned} \quad (2.5)$$

where  $f_V(T_q) \cong f_V(T_q^*)$ .

A simple comparison of Eq. (2.2)–(2.5) shows that the annihilation branching ratios for  $T_q^*$  and  $T_q$  are negligible except in the case that  $m_H > m_t$  for  $T_q^*$ , and for the  $T_q$  meson in the case that  $M_T \sim m_H$ , where we would have a resonancelike phenomenon. In spite of this, there is the interesting possibility that for some channels the  $T_b$  and  $T_b^*$  annihilation widths might be comparable if  $m_H < m_t$ . In particular, we expect the most striking effects in the decay channels  $T_b, T_b^* \rightarrow c\bar{s}, c\bar{b}$ . If we take as a maximal choice  $C_2 \cong 10$  and the experimental bound<sup>11</sup>  $m_H \geq 15$  GeV, then from Eqs. (2.4) and (2.5) it follows that<sup>12</sup>  $\Gamma(T_b \rightarrow c\bar{s})/\Gamma(T_b^* \rightarrow c\bar{s}) \sim 65$  if  $m_t = 25$  GeV,  $m_H = 15$  GeV; and  $\Gamma(T_b \rightarrow c\bar{s})/\Gamma(T_b^* \rightarrow c\bar{s}) \sim 15$  if  $m_t = 40$  GeV,  $m_H = 25$  GeV. We obtain similar results in the case  $\Gamma(T_b \rightarrow c\bar{b})/\Gamma(T_b^* \rightarrow c\bar{b})$ .

### III. KAON MULTIPLICITIES

In this section we explore the possibility that the nonleptonic annihilation channels of  $T_b$  could be comparable to those of the vector meson  $T_b^*$ . As far as the purely leptonic channels are concerned, it was pointed out<sup>1,7</sup> that the most striking signatures in the production of  $T_b$  and  $T_b^*$  are expected in the leptonic and semi-inclusive decays  $T_b, T_b^* \rightarrow l\nu$ , (large  $p_T$ )  $l\nu$  + few soft hadrons. We now study the average kaon multiplicities expected for two- and three-jet events in  $T_b$  and  $T_b^*$  decays as a possible way of distinguishing between  $T_b$  and  $T_b^*$  production.

It was pointed out by Bigi and Krasemann<sup>1</sup> that the annihilation decays of  $T_b^*$  should differ from cascade decays in

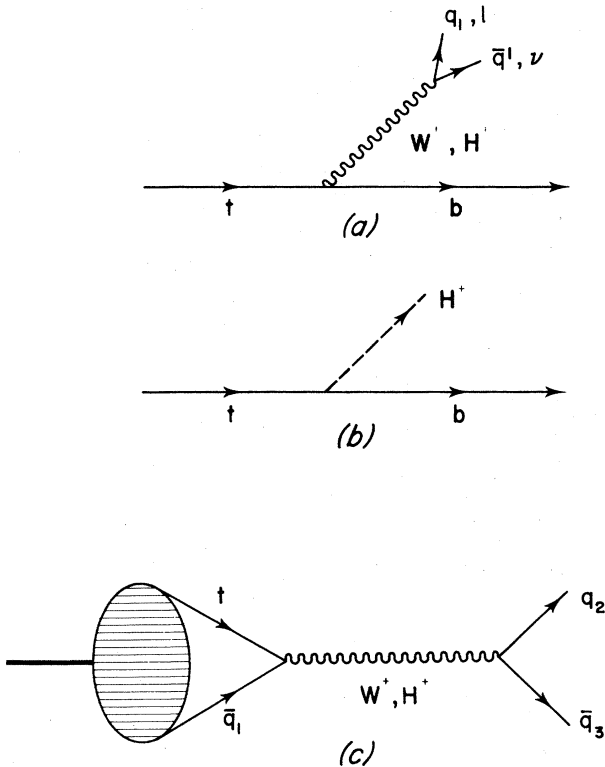


FIG. 1. Dominant Feynman diagrams involved in the weak decay of  $T$  mesons: (a) spectator diagram, (b) decay into a real  $H^\pm$ , and (c) annihilation diagram.

their flavor content. In particular, they found that, if one considers only the effect of virtual  $W$  exchanges, then the average kaon multiplicities expected in these decays differ by about one unit. In order to get this result, it is necessary to assume that in the annihilation reaction the decay proceeds via a  $W$  boson which fragments into three color doublets of  $u\bar{d}$  and  $c\bar{s}$  each and into three lepton doublets  $e\nu$ ,  $\mu\nu$ , and  $\tau\nu$ . The further development into the observed final state is assumed to be driven by only soft gluons, whose transition into  $s\bar{s}$  is suppressed. Thus the annihilation picture leads to the following chains:

$$T_b^* \rightarrow \begin{cases} u\bar{d} + 5 \text{ gluons} \\ c\bar{s} + 4 \text{ gluons} \end{cases} \rightarrow s\bar{s} + 4 \text{ gluons} + W_{\text{soft}} \quad (3.1)$$

which has to be compared with the following cascade chains:

$$\begin{aligned} T_b^*(T_b) &\rightarrow b\bar{b} + W_{\text{hard}} \rightarrow c\bar{c} + 3W_{\text{hard}} \\ &\rightarrow s\bar{s} + 2W_{\text{soft}} + 3W_{\text{hard}} \quad (3.2) \end{aligned}$$

The following crude estimates for the probabilities for a gluon turning into  $s\bar{s}$  and for the fragmentation  $W_{\text{hard}} \rightarrow c\bar{s}$ ,

$$P(g \rightarrow s\bar{s}) \sim \frac{1}{6} - \frac{1}{9} \quad (3.3)$$

$$P(W_{\text{hard}}^+ \rightarrow c\bar{s}) \sim \frac{1}{3} \quad (3.4)$$

lead to different average kaon multiplicities:<sup>1</sup>  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle \sim 0.7-0.9$  for the annihilation chains (3.1), and  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle \sim 2$  for the cascade chain (3.2). Incorporating the charged Higgs boson  $H^\pm$  ( $P^\pm$ ) into the picture, we have to add the cascade chain

$$T_b^*(T_b) \rightarrow b\bar{b} + H_{\text{hard}}^+ \rightarrow s\bar{s} + 2W_{\text{soft}} + 2W_{\text{hard}} + H_{\text{hard}} \quad (3.5)$$

and the annihilation chain:

$$T_b \rightarrow c\bar{s} + 4 \text{ gluons} \rightarrow s\bar{s} + 4 \text{ gluons} + W_{\text{soft}} \quad (3.6)$$

According to the couplings given in (2.1), the  $H^\pm$  boson will fragment essentially into three  $c\bar{s}$  color doublets and one lepton doublet  $\tau\nu$ ; then we have  $(H^+ \rightarrow c\bar{s}) \sim 3/4$ .

If we now take into account the chains (3.5) and (3.6), the average kaon multiplicities become  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle$

$= 1.1-1.3$  for the  $T_b$  annihilation mechanism, and  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle = 4.4$  for both  $T_b$  and  $T_b^*$  cascade mechanisms. Therefore, we have that including the new channels open by the possible existence of  $H^\pm$  ( $P^\pm$ ) with  $m_H < m_t$ , there is a difference of about half unit between the average kaon multiplicities expected for the two-jet events in  $T_b$  and  $T_b^*$  decays. On the other hand, if  $H^\pm$  ( $P^\pm$ ) does not exist or  $m_H > m_t$ , then the only available channels arise through chains (3.1) and (3.2) and we should expect an average kaon multiplicity of about 0.7-0.9 for the two-jet events coming from  $T_b^*$  decays.

Finally, we would like to comment on the possibility that the annihilation channels  $T_b^*$ ,  $T_b \rightarrow c\bar{b}$  might be also important. In this case we have to include two more annihilation chains:

$$\begin{aligned} T_b^*(T_b) &\rightarrow c\bar{b} + 2 \text{ gluons} \\ &\rightarrow s\bar{s} + 2 \text{ gluons} + 2W_{\text{soft}} + W_{\text{hard}} \quad (3.7) \end{aligned}$$

In this condition, the probabilities (3.3) and (3.4) have to be modified to

$$P(W_{\text{hard}}^+ \rightarrow c\bar{s} \text{ or } c\bar{b}) \sim \frac{1}{4} \quad (3.8)$$

$$P(H_{\text{hard}}^+ \rightarrow c\bar{s} \text{ or } c\bar{b}) \sim \frac{3}{7} \quad (3.9)$$

As a consequence, the total average kaon multiplicities expected for two-jet (annihilation) events become  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle \sim 0.9-1.0$  for  $T_b^*$  decays, and  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle \sim 1.2-1.3$  for  $T_b$  decays if  $m_H < m_t$ . The cascade chains (3.2) and (3.5) remain unaltered even if these new channels are opened, and their average kaon multiplicities are again given by  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle \sim 2$  if there is no  $H^\pm$ , and  $\langle N_K \rangle = \langle N_{\bar{K}} \rangle \cong 4.4$  if there is a  $H^\pm$  with  $m_H < m_t$ .

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<sup>1</sup>I. I. Y. Bigi and H. Krasemann, *Z. Phys. C* **7**, 127 (1981).

<sup>2</sup>J. P. Leveille, in *Proceedings of the Z<sup>0</sup> Physics Workshop, Ithaca, 1981*, edited by M. E. Peskin and S.-H. Henry Tye (Cornell University Report No. CLNS 81-485, 1981), p. 241.

<sup>3</sup>S. Weinberg, *Phys. Rev. Lett.* **19**, 1264 (1967); A. Salam, in *Elementary Particle Theory: Relativistic Groups and Analyticity (Nobel Symposium No. 8)*, edited by N. Svartholm (Almqvist and Wiksell, Stockholm, 1968), p. 367.

<sup>4</sup>J. Schwinger, *Phys. Rev.* **128**, 2425 (1969); R. Jackiw and K. Johnson, *Phys. Rev. D* **8**, 2386 (1973); J. M. Cornwall and R. E. Norton, *ibid.* **8**, 3338 (1973); M. A. B. Bég and A. Sirlin, *Ann. Rev. Nucl. Science* **24**, 379 (1974); S. Weinberg, *Phys. Rev. D* **19**, 1277 (1979); L. Susskind, *ibid.* **20**, 2619 (1979).

<sup>5</sup>A. Ali and M. A. B. Bég, *Phys. Lett.* **103B**, 376 (1981).

<sup>6</sup>G. Barbiellini *et al.* (exotic particles working group), DESY Report No. 81-064, 1981 (unpublished).

<sup>7</sup>M. A. Pérez, *Z. Phys. C* **18**, 113 (1983).

<sup>8</sup>B. Guberina, in *New Flavors*, proceedings of the Second Moriond

Workshop, Les Arcs, France, 1982, edited by J. Tran Thanh Van and L. Montanet (Éditions Frontières, Gif-sur-Yvette, 1982), p. 217.

<sup>9</sup>M. Kobayashi and T. Maskawa, *Prog. Theor. Phys.* **49**, 652 (1973).

<sup>10</sup>H. E. Haber, G. L. Kane and T. Sterling, *Nucl. Phys.* **B161**, 493 (1979); J. F. Donoghue and L.-F. Li, *Phys. Rev. D* **19**, 945 (1979); H. Huffer and G. Pócsik, *Z. Phys. C* **8**, 13 (1981).

<sup>11</sup>W. Bartel *et al.*, *Phys. Lett.* **114B**, 211 (1982); B. Adeva *et al.*, *Phys. Rev. Lett.* **115B**, 345 (1982); C. A. Blocker *et al.*, *Phys. Rev. Lett.* **49**, 517 (1982).

<sup>12</sup>We have taken the KM mixing angles as  $\theta_i = \theta_C$  (Cabibbo),  $i = 1, 2, 3$ , and  $\delta = 0$ , which is near to the best Sakurai's choice obtained from different constraints, see, e.g., S. G. Wojcicki, in *Particles and Fields—1981: Testing the Standard Model*, proceedings of the meeting of the APS Division of Particles and Fields, Santa Cruz, California, edited by C. A. Heusch and W. T. Kirk (AIP, New York, 1982), p. 316.