

Decay of the Higgs boson into heavy-quarkonium states

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The exclusive production of a pair of heavy-quarkonium states $V (= \psi/J, Y, \zeta, \dots)$ from the decay of the Higgs boson in the standard model is studied in the approximation of zero binding energy. The branching fractions could only be as large as 10^{-5} around the kinematic thresholds. The alternative process $H \rightarrow V\gamma$ is also studied and found to have branching fractions usually less than 10^{-3} .

In the standard model,¹ a neutral Higgs boson remains in the spectrum of physical particles after the spontaneous breakdown of the gauge symmetry. The unknown mass m_H of the Higgs boson can fall into a range from 300 MeV to 1 TeV without endangering the theory or contradicting present experimental limits.² Searching for the Higgs boson is important in understanding the symmetry-breaking mechanism. The search for the Higgs boson would be a goal of high priority in future high-energy accelerators. However, the experimental difficulty lies in the absence of techniques for tagging the heavy particles which are the dominant decay products.^{3,4}

In this paper we study the Higgs-boson decays into heavy vector quarkonium states $V (= \psi/J, Y$, and the presumed t -quarkonium ζ), namely, the processes $H \rightarrow VV$ and also $H \rightarrow V\gamma$. These produced quarkonia could easily be identified via their subsequent decays into lepton pairs. The rates are usually suppressed by the binding effects.

Firstly, we calculate the partial width for $\Gamma(H \rightarrow VV)$. Figure 1 illustrates the lowest-order diagrams for the process $H \rightarrow VV$. Within the zero-binding-energy approximation,⁵ $m_Q = \frac{1}{2}m_V$, the momenta of the heavy quark Q and the heavy antiquark \bar{Q} are equal. The amplitude T for producing a pair of V of the momenta p and p' and polarizations e and e'

is given as

$$T = \frac{4}{3} (128\alpha_S \pi \phi_0^2 / m_H^4) (\sqrt{2} G_F m_Q^2)^{1/2} \times [2p \cdot e' e \cdot p' - (m_H^2 - 2m_V^2) e \cdot e'] \quad (1)$$

Here the factor $\frac{4}{3}$ comes from the color factor. The wave functions at the origin are measured through the leptonic decay width Γ_{ee} :

$$\phi_0^2 = m_V^2 \Gamma_{ee} / 16\pi \alpha^2 e_Q^2 \quad (2)$$

The values of ϕ_0^2 for ψ/J and Y are, therefore,

$$\begin{aligned} \phi_0^2(\psi/J) &= 0.04 \text{ GeV}^3, \\ \phi_0^2(Y) &= 0.4 \text{ GeV}^3, \end{aligned} \quad (3)$$

respectively. We also set the strong coupling constant $\alpha_S = 0.3$ in our calculations. For the $\zeta(\bar{t}t)$ production, we assume $m_\zeta = 40 \text{ GeV}$ and approximate the wave-function value ϕ_0^2 from the calculation based on a Coulomb-type binding potential

$$\phi_0^2 = \alpha_S^3 m_V^3 / 27\pi \quad (4)$$

The partial decay width $\Gamma(H \rightarrow VV)$ is

$$\Gamma(H \rightarrow VV) = \frac{1}{2} \frac{1}{2m_H} \frac{1}{8\pi} \sum_{\text{spins}} |T|^2 \left(1 - \frac{4m_V^2}{m_H^2}\right)^{1/2} \quad (5)$$

$$= \frac{2^{14} \pi \alpha_S^2 \sqrt{2} G_F m_Q^2 m_H}{9} \left(\frac{\phi_0^2}{m_H^3}\right)^2 \left(1 - \frac{4m_V^2}{m_H^2} + \frac{6m_V^4}{m_H^4}\right) \left(1 - \frac{4m_V^2}{m_H^2}\right)^{1/2} \quad (6)$$

The nature of identical particles in the final state gives rise to the first factor $\frac{1}{2}$ in Eq. (5). In comparison to the dominant decay channel $H \rightarrow Q\bar{Q}$,

$$\Gamma(H \rightarrow Q\bar{Q}) = 3(\sqrt{2} G_F m_Q^2 m_H / 8\pi) (1 - m_V^2 / m_H^2)^{3/2}, \quad (7)$$

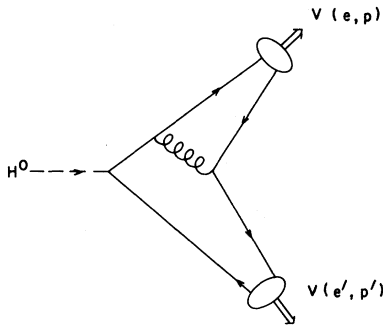


FIG. 1. Lowest-order QCD diagrams for $H \rightarrow VV$. Three other similar diagrams are not shown.

we obtain the branching ratio

$$\frac{\Gamma(H \rightarrow VV)}{\Gamma(H \rightarrow Q\bar{Q})} = \frac{2^{17}\pi^2\alpha_S^2\phi_0^4}{27m_H^6} \left(1 - \frac{4m_V^2}{m_H^2} + \frac{6m_V^4}{m_H^4} \right) \times \frac{(1 - 4m_V^2/m_H^2)^{1/2}}{(1 - m_V^2/m_H^2)^{3/2}}. \quad (8)$$

Our results are shown in Fig. 2. The branching fractions could only be as large as 10^{-5} around the kinematic thresholds. They might be too rare for detection even though their identifications are simpler than other dominant channels.

Now we study another process, $H \rightarrow V\gamma$, the inverse Wilczek⁶ mechanism. The rate is bigger than the previous one as only one binding vertex $VQ\bar{Q}$ is involved. The amplitude is

$$T = \sqrt{3}4e_Q e (G_F m_Q \phi_0^2 / \sqrt{2})^{1/2} (m_H^2 - m_V^2)^{-1} \times [2p_\gamma \cdot e_V p_V \cdot e_\gamma - (m_H^2 - m_V^2) e_\gamma \cdot e_V]. \quad (9)$$

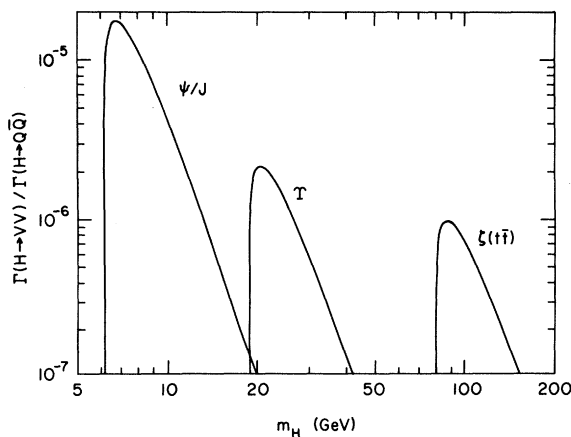


FIG. 2. Ratio of $\Gamma(H \rightarrow VV)$ to $\Gamma(H \rightarrow Q\bar{Q})$ vs m_H for the cases $V = \psi/J$, Y , or ζ , assuming $m_\zeta = 40$ GeV.

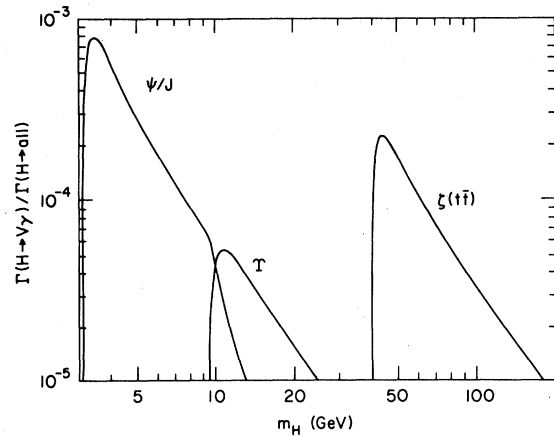


FIG. 3. Branching fraction of $H \rightarrow V\gamma$ vs m_H for the cases $V = \psi/J$, Y , and ζ , assuming $m_\zeta = 40$ GeV.

Here e_γ and e_V are the polarizations and p_γ and p_V are the momenta of γ and V , respectively. The partial width is

$$\Gamma(H \rightarrow V\gamma) = 6\sqrt{2}G_F m_V \alpha e_Q^2 (m_H^2 - m_V^2) (\phi_0^2/m_H^3). \quad (10)$$

Figure 3 illustrates the branching fractions versus m_H for the cases $V = \psi/J$, Y , or the hypothetical t -quarkonium of mass $m_\zeta = 40$ GeV. The branching fractions lie in a range below 10^{-3} . It should be noticed that the zero-binding approximation fails for the soft-photon emission when $m_H \approx m_V$, and the results are overestimated.

Our conclusion is that the quarkonia are produced quite rarely from the decay of the Higgs boson. They can only be observed in a copious source of the Higgs bosons.

Note added. The decay of the Higgs boson into quarkonium states has been studied previously by M. Bander and A. Soni [Phys. Lett. **82B**, 411 (1979)]. Their approach to the process $H \rightarrow VV$ is different from ours. They do not include the gluon line in Fig. 1 so that the quark lines cannot all be maintained on shell. This requires knowledge of the off-shell behavior of the form factor, which is not well understood at the present time. By taking a rather mild form factor, they obtain a much larger branching fraction $B(H \rightarrow VV)$ than ours, which we believe, is based on better known parameters.

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