

Brief Reports

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Higgs-boson production in $p\bar{p}$ collisions at collider energies

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We show that the contribution of gluon fusion to Higgs-boson production in proton-antiproton collisions is much smaller than what has been predicted before for large Higgs-boson masses.

The $p\bar{p}$ colliders at CERN ($\sqrt{s} = 540$ GeV) and at Fermilab ($\sqrt{s} = 2$ TeV) will open another possibility for the production of the Higgs boson, which is an essential ingredient of the Weinberg-Salam model.¹

The most important contribution for the Higgs-boson production in $p\bar{p}$ collisions comes from gluon fusion, via a quark loop (Fig. 1). This process was suggested by Georgi, Glashow, Machacek, and Nanopoulos² in the study of proton-proton collisions.

However, as we will show, their estimate is overoptimistic, especially in the case of heavy Higgs bosons.

The rapidity distribution for the process of Fig. 1, in the framework of Drell-Yan mechanism,³ at $y = 0$ is given by

$$\frac{d\sigma}{dy} \Big|_{y=0} = \frac{\sqrt{2}G_F\alpha_s^2}{576\pi} N^2(\beta) \tau G^2(\sqrt{\tau}) \quad (1)$$

where $G(x)$ is the gluon distribution function in the proton (antiproton), evaluated at $\sqrt{\tau} = M_H/\sqrt{s}$, $N^2(\beta)$ is defined by

$$N^2(\beta) = \left| 3 \sum_q I_q(\beta) \right|^2 = \left| 3 \sum_q \int_0^1 dx \int_0^{1-x} dy \frac{(1-4xy)}{(1-xy/\beta)} \right|^2 \quad (2)$$

and β is the ratio

$$\beta = \frac{m_q^2}{M_H^2} \quad (3)$$

The summation in (2) is done over all flavors of quarks running in the fermion loop.

The integral that appears in (2) can be evaluated, and for $\beta < \frac{1}{4}$ it has a real and an imaginary part:

$$I_q(\beta) = 2\beta - (1-4\beta)\beta \left[\int_0^{1/x_+} dx \frac{\ln|1-x|}{x} + \int_0^{1/x_-} dx \frac{\ln|1-x|}{x} \right] - i\pi(1-4\beta)\beta \ln \left[\frac{1+\sqrt{1-4\beta}}{1-\sqrt{1-4\beta}} \right], \quad \beta < \frac{1}{4} \quad (4)$$

where x_{\pm} are the roots of

$$(1-x) = \frac{\beta}{x} \quad ,$$

and the integrals involving logarithms must be calculated numerically. Otherwise, for $\beta \geq \frac{1}{4}$, $I_q(\beta)$ has only a real part that can be expressed by the summation

$$I_q(\beta) = 2\beta + (1-4\beta)\beta \sum_{n=1}^{\infty} \frac{[(n-1)!]^2}{(2n)!\beta^n}, \quad (5)$$

$$\beta \geq \frac{1}{4} \quad .$$

Figure 2 shows the behavior of $\text{Re}[I_q(\beta)]$,

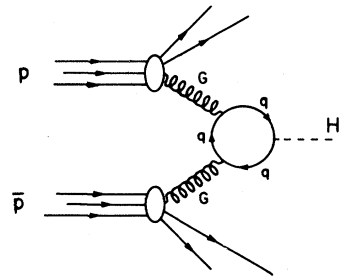


FIG. 1. Dominant contribution to $p + \bar{p} \rightarrow H + x$.

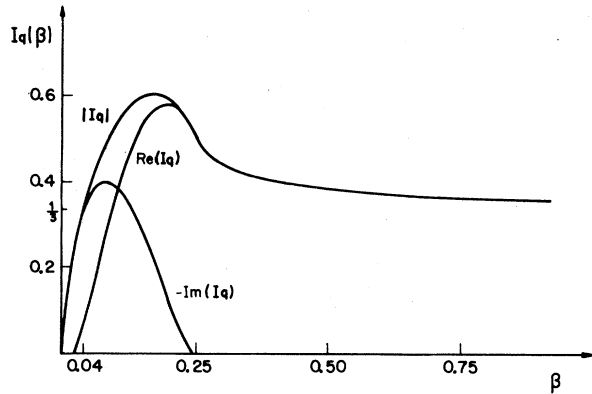


FIG. 2. Real and imaginary part of the integral $I_q(\beta)$.

$-\text{Im}[I_q(\beta)]$, and $|I_q(\beta)|$ as a function of β , and Fig. 3 gives $N^2(\beta)$ as a function of the Higgs-boson mass (M_H). We have used for the Higgs-boson mass values in the range

$$6.5 < M_H < 300 \text{ GeV} ,$$

in agreement with lower and upper bounds that have been established by Weinberg⁴ and Veltman.⁵ For the current-algebra masses of the quarks, we have assumed the following values⁶:

$$\begin{aligned} m_u &= 3.0 \text{ MeV}, & m_c &= 1.3 \text{ GeV} , \\ m_d &= 6.3 \text{ MeV}, & m_b &= 5.0 \text{ GeV} , \\ m_s &= 150 \text{ MeV}, & m_t &= 18 \text{ GeV} . \end{aligned}$$

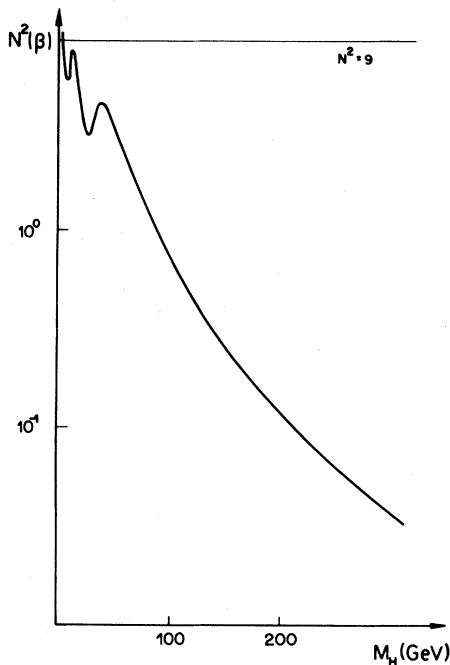


FIG. 3. $N^2(\beta)$ as a function of the Higgs-boson mass.

The mass of the hypothetical top quark is quite arbitrary, but it does not alter our results in a significant way.

The graph of $|I_q(\beta)|$ (Fig. 2) exhibits a maximum at $\beta \cong 0.16$ and tends asymptotically to $\frac{1}{3}$ as β tends to infinity. For $\beta \geq 0.04$, $I_q(\beta)$ is always larger than $\frac{1}{3}$. On the other hand, $N^2(\beta)$ (Fig. 3) has a maximum for all values of the Higgs-boson mass satisfying $M_H \cong 2.5m_q$ and decreases as M_H increases.

In the evaluation of Georgi, Glashow, Machacek, and Nanopoulos, they took into account only quarks with masses satisfying the condition

$$\beta \equiv \frac{m_q^2}{M_H^2} \geq \frac{1}{25} ,$$

and they assumed that the integral $I_q(\beta)$ contributes with approximately $\frac{1}{3}$ for each heavy flavor (c, b, t) running in the loop, and accordingly $N^2 \cong 9$, independently of the Higgs-boson mass. However, this approximation is valid only if $M_H \leq 5m_c = 6.5 \text{ GeV}$, which is the lower bound for the Higgs-boson mass. Then, this procedure is not acceptable in the case of a heavy Higgs boson (or small values of β), as we can see from Fig. 3. For example, when $M_H \cong 100 \text{ GeV}$, we have $N^2(\beta) \cong 0.78$, which is more than an order of magnitude smaller than what would be expected by the estimate of Georgi *et al.* If we consider a Higgs boson as heavy as 300 GeV, the value of $N^2(\beta)$ falls to 3.8×10^{-2} , and the respective cross section is only 0.4% of what would be expected by them.

In order to verify the sensitivity of the cross section on possible parametrizations of the gluon distribution function,⁷ we consider, besides the standard distribution

$$G_2(x) = 3.30 \frac{(1-x)^5}{x} , \quad (6)$$

an alternative broad distribution

$$G_1(x) = 1.10 \frac{(1+9x)(1-4x)^4}{x} , \quad (7)$$

and a narrow one

$$G_3(x) = 0.74 \frac{(1-x)^5}{x^{3/2}} . \quad (8)$$

The rapidity distributions at $y=0$ for the process of gluon fusion versus M_H , at the energies of 540 and 2000 GeV, are shown in Figs. 4 and 5, for each gluon distribution function.

If we consider the luminosity of the CERN and Fermilab $p-\bar{p}$ colliders,

$$L \cong 10^{30} \text{ cm}^{-2} \text{ sec}^{-1} \cong 8.6 \times 10^{-2} \text{ pb}^{-1}(\text{day})^{-1} ,$$

we can see that if we want to have at least one event per day, only a Higgs boson with mass less than $\sim 20 \text{ GeV}$ may be observable in the case of the standard

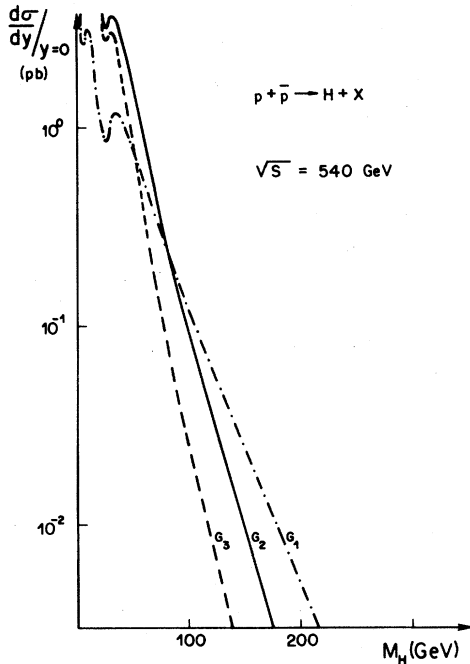


FIG. 4. Cross section for gluon fusion at $\sqrt{s} = 540$ GeV vs the Higgs-boson mass. G_1 , G_2 , and G_3 are given by Eqs. (6), (7), and (8).

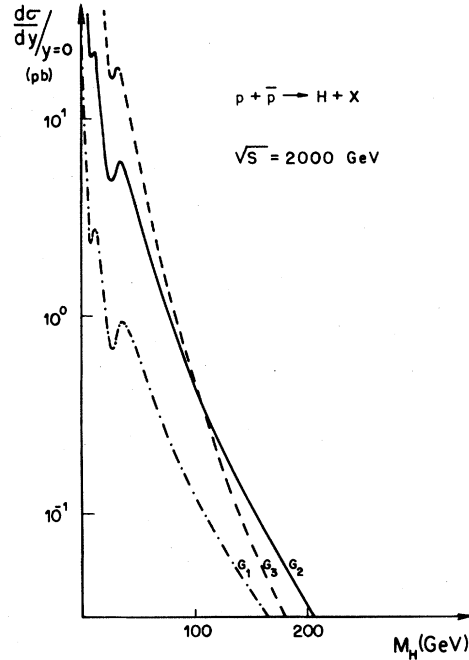


FIG. 5. Cross section for gluon fusion at $\sqrt{s} = 2000$ GeV vs the Higgs-boson mass. G_1 , G_2 , and G_3 are given by Eqs. (6), (7), and (8).

gluon distribution function (the other two distributions do not alter this value in a significant way).

If we take into consideration the poor signature of this process,⁸ besides the smallness of the cross section, we can therefore conclude that the possibilities of detection of the Higgs boson in the future generation of $p\text{-}\bar{p}$ colliders are very remote.

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