

Parity determination for the new generation of heavy neutral mesons

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We consider how best to experimentally determine the parity quantum number of a new heavy neutral meson, including the possibility of exotic J^{PC} . Multiquark and gluon bound states can have exotic J^{PC} quantum numbers forbidden to the nonrelativistic $q\bar{q}$ system. If only the existence of easily identifiable two-body hadronic modes is known, it is not possible to establish the parity so an "exotic" meson, $J > 0$, could be misidentified as a "normal" meson. Direction-linear-polarization coefficients, which would identify the parity, are also found to be small for $e\bar{e} \rightarrow 1^{--} \rightarrow 1^{\pm+} \gamma, 0^{\pm+} \gamma$ with the high-energy photon externally converting into an $e\bar{e}$ pair. However, important parity tests do exist, independent of the polarization state of the decaying particle, which can be used to settle the confusion. These are listed in Sec. III of this paper.

I. DIFFICULTIES IN ESTABLISHING PARITIES BY EXISTENCE OF HADRONIC DECAY MODES

The rich structure of states in the psion family suggests a whole new generation of heavy neutral mesons, made presumably out of a new heavy-quark-antiquark pair, and possibly of gluon and/or multiquark bound states. These new heavy mesons are generally expected to be ordinary isotopic-spin singlets, with J^{PC} quantum numbers being those allowed for a nonrelativistic $q\bar{q}$ system, viz., $0^+, 0^-, 1^+, 1^-, 2^+, 2^-, \dots$. Mesons with J^{PC} that are not found in a nonrelativistic $q\bar{q}$ system are, by definition, exotic. Their quantum numbers are given by $0^-, 0^+, 1^-, 2^-, \dots$. Among the well-known low-energy resonances, no exotic mesons have to have been confirmed. The treatment of parity determination given below applies, of course, both to new generations of heavy neutral mesons in a nonrelativistic $q\bar{q}$ system and also to the general case which includes exotic J^{PC} mesons.

Among the recently discovered new heavy mesons, it is reasonable to expect, based on ideas of quantum chromodynamics and the bag model, the formation of multiquark-antiquark states such as the baryonium ($qq\bar{q}\bar{q}$) and higher multiquark states ($qqq\bar{q}\bar{q}$, etc.).¹ These multiquark states will in general have J^{PC} quantum numbers that include those forbidden to the nonrelativistic $q\bar{q}$ system. Thus "exotic" mesons are likely to exist, as a corollary to any discovery of baryonium states,² and should be experimentally looked for and distinguished from the "normal" mesons. Similarly, gluon bound states³ have exotic J^{PC} [see Eq. (2) below].

Exotic mesons, assuming they can be found, can also be interpreted⁴ as a signal for relativistic

bound-state $q\bar{q}$ systems.

In this paper we address ourselves to the question of how one can decide experimentally that a given new heavy neutral mesons is "exotic." Apart from the exception of a spin-0 exotic meson, for it has odd charge-conjugation quantum number, we can point out some "confusion" theorems. They emphasize the fact that without a determination of its intrinsic parity an exotic meson could be easily misidentified as a "normal" meson. So then in part II of this paper, because of the potential application in $e\bar{e}$ colliding beam processes, we discuss parity determination by γ cascade. The direction-linear-polarization coefficients are found to be small for $e\bar{e} \rightarrow 1^{--} \rightarrow 1^{\pm+} \gamma, 0^{\pm+} \gamma$ with the photon converting externally. In part III of our paper we give a list of important parity tests that can be made to settle the confusion.

To keep our discussion simple and for convenience in reference to experiments, we shall limit our attention to the easily identifiable two-body decay modes⁵ $P\bar{P}$, $V\bar{V}$, $B\bar{B}$, PV and list the allowed J^{PC} quantum numbers if a given heavy neutral isotopic-spin-singlet meson has been seen in that channel: (exotic J^{PC} quantum numbers are underlined)

$$\begin{aligned}
 P\bar{P} \text{ seen: } J^{PC} &= 0^{++}, 1^{--}, 2^{++}, \dots, \\
 P\bar{P} \text{ absent: } J^{PC} &= \underline{0^{+-}}, \underline{1^{-+}}, \underline{2^{+-}}, \dots; \underline{0^{--}}; \\
 &0^{+-}; 1^{+-}, 2^{+-}, \dots, \quad (1)
 \end{aligned}$$

$$\begin{aligned}
 V\bar{V} \text{ seen: } J^{PC} &= 0^{++}; 1^{+-}, 2^{+-}, \dots; 0^{--}; 1^{--}, 2^{--}, \dots; \\
 &\underline{1^{+-}}, \underline{2^{+-}}, \dots, \\
 V\bar{V} \text{ absent: } J^{PC} &= \underline{0^{--}}, \underline{0^{+-}}, \quad (2)
 \end{aligned}$$

$$\begin{aligned} \overline{B\overline{B}} \text{ seen: } J^{PC} &= 0^{++}; 1^{++}, 2^{++}, \dots; 0^{+-}, 1^{+-}, \dots, \\ \overline{B\overline{B}} \text{ absent: } J^{PC} &= \underline{0}^{-+}; \underline{0}^{-+}, \underline{1}^{-+}, \dots, \end{aligned} \quad (3)$$

and

$$\begin{aligned} PV \text{ seen: } J^{PC} &= \underline{0}^{-+}; 1^{-+}, 2^{-+}, \dots; 1^{+-}, \underline{2}^{+-}, 3^{+-}; \dots, \\ PV \text{ absent: } J^{PC} &= \underline{0}^{++}; 0^{++}, 1^{++}, \dots; 0^{+-}, \underline{1}^{+-}, 2^{+-}; \dots \end{aligned} \quad (4)$$

In Eq. (4) G parity (i.e., isotopic spin and charge conjugation) has been used, e.g., $0^{+}(I=0) + 0^{+}(I=1) + 1^{-}(I=1)$. For PV modes involving strange particles, $SU(3)$ has been assumed to be good in the hadronic decay.

Inspection of this list⁶ easily shows the following: The presence or absence of any set of these modes cannot be used to establish an exotic spin- J meson with $J > 0$, but only that the observation of the $\overline{B\overline{B}}$ mode can be used to exclude it. Such an exotic meson can appear in the $\overline{V\overline{V}}$ channel and if J is even, it can appear in the PV channel. For $J=0$ meson, observation of a PV decay mode would directly establish its exoticity, whereas observation of $\overline{P\overline{P}}$, $\overline{V\overline{V}}$, $\overline{B\overline{B}}$ modes would imply that its J^{PC} quantum number is not exotic. 0^{+-} , however, cannot be established directly through these hadronic modes.

Both 0^{+-} and 0^{--} exotic mesons have negative charge conjugation, and with 0 spin might, on dynamical grounds, be expected to be among the lowest-lying exotic states of a new generation of heavy neutral mesons. Thus the above list very clearly emphasizes the simplicity and importance of a search via a γ cascade chain for a spin-0, isosinglet, neutral meson state with negative C .

If $SU(3)$ is not assumed to be good for the hadronic PV decay channel of the heavy neutral $SU(3)$ -singlet meson, only $J^P = 0^+$ is forbidden for the PV mode involving strange particles.

II. PARITY DETERMINATION BY γ CASCADES

Because it is necessary to measure a small direction-polarization correlation of a linearly polarized photon having an energy of the order of a hundred MeV, we find that it would be difficult, though in principle possible, to determine relative parities of states in a new generation of heavy neutral mesons by study of γ cascades. The alignment of an initial 1^{--} state, such as the ψ' , is a consequence of its formation by $e\overline{e}$ colliding beams.

This technique for measuring the relative parity has been used extensively, of course, in nuclear physics⁷ so we will only briefly review what it is necessary to measure in the relativistic case.⁸

To show the confusion theorem that exists even

for relativistic systems, unless there is a measurement of the dependence of the decay distribution on the linear polarization of the photon, we recall Zwanziger's decomposition of three- and four-particle scattering amplitudes involving massless particles into a minimum number of linearly independent invariant amplitudes that are free of kinematic singularities.⁹ For the electromagnetic vertex function, gauge invariance and Lorentz invariance imply the invariant decay amplitudes for a right circularly polarized photon and those for a left circularly polarized photon are related by (suppressing angular momentum indices)

$$A_+ = \eta A_- ,$$

where η is the relative parity of the other two particles. Because of this simple proportionality⁹ which involves the relative parity, there is a confusion about the relative parity unless there is a direction-polarization correlation measurement. To be able to eliminate the confusion, such a measurement must involve linear, not circular, photon polarization.

Assuming a photon energy of the order of a hundred MeV, we consider measurement of photon linear polarization by pair production. Indeed, the absolute rate is small for a high-energy γ to convert into $e\overline{e}$ in the presence of the external high- Z nucleus; however, it is still worthwhile to calculate the range of allowed values for the resulting correlation coefficients. We follow the Maximon-Olsen treatment of γ linear-polarization measurement by pair production^{10,11} and obtain the range of allowed values for the correlation coefficients in the two simplest cases

$$e\overline{e} \rightarrow 1^{--} \rightarrow 1^{++}\gamma$$

and

$$e\overline{e} \rightarrow 1^{--} \rightarrow 0^{++}\gamma .$$

We consider $e\overline{e} \rightarrow 1^{--} \rightarrow 1^{++}\gamma$ for the case in which the photon and $e\overline{e}$ pair are nearly coplanar. In the 1^{--} rest frame with the γ momentum chosen along the z axis, the resulting direction-polarization distribution $W(\theta, \chi)$ is a function of the polar angle θ of the initial electron beam and of the opening angle χ measured from the initial electron beam to the conversion-produced final-positron momentum direction. For 1^{++} we find

$$\begin{aligned} W(\theta, \chi) &= 1 - \left(\frac{1}{2} - \frac{a}{b} \right) \sin^2 \theta \\ &\quad + \frac{1}{2} \left(1 + 2 \frac{M}{N} \right)^{-1} \sin^2 \theta \cos 2\chi \end{aligned} \quad (5)$$

with $a, b \geq 0$, and for 1^{--}

$$W(\theta, \chi) = 1 - \left(\frac{1}{2} - \frac{c}{d} \right) \sin^2 \theta - \frac{1}{2} \left(1 + 2 \frac{M}{N} \right)^{-1} \sin^2 \theta \cos 2\chi \quad (6)$$

with $c, d \geq 0$, where the quantities M and N describe the density matrix for the γ conversion into $e\bar{e}$ in the case of complete screening, which is what is appropriate for a high- Z nucleus. These quantities, M and N , are given explicitly in the Appendix and are functions of the photon energy k , the final positron energy ϵ_1 , the final electron energy ϵ_2 , and a parameter α which is needed to analyze correctly^{10,11} the conversion density matrix.

This parameter $\alpha = \Delta\phi/\beta$, where $\beta^{-1} = 111/Z^{1/3}$ is the screening radius of the atom in Compton wavelengths. In terms of α the conversion density matrix is found to be

$$\rho_{ij} = \begin{pmatrix} M + N \cos^2 \phi_1 & L \sin 2\phi_1 \\ L \sin 2\phi_1 & M + N \sin^2 \phi_1 \end{pmatrix}, \quad (7)$$

where $L = \frac{1}{2}N$. This, indeed, gives $\det \rho$ independent of ϕ_1 . The positron azimuthal angle ϕ_1 is measured from the direction of the photon polarization vector to the positron momentum. The elements of this conversion density matrix have been integrated over the polar angles θ_1 (and θ_2) between the momentum of the photon and that of the conversion produced positron (and electron), and have also been integrated over a small range of the azimuthal angle ϕ ,

$$\pi - \Delta\phi \leq \phi = \phi_1 - \phi_2 \leq \pi + \Delta\phi, \quad \Delta\phi \ll 1,$$

between the $e\bar{e}$ pair which is nearly coplanar with the converting photon. This latter integration is essential^{10,11} since any experiment will average over a small range of ϕ close to π and the elements of the conversion density matrix are very sensitive to ϕ near π .

If data with associated acceptances existed, the full direction-polarization distribution $W(\theta, \chi)$ given above would probably be the quantity to use for making a maximum-likelihood fit by letting a/b (similarly c/d) be a free non-negative parameter. However, to assess the possible magnitude of this parity signature, it is simpler to integrate over the angle θ and consider the case of an equal-energy pair, $\epsilon_1 = \epsilon_2 = k/2$; so then for 1^{**}

$$W(\chi) = 1 + \frac{1}{2} \left(1 + \frac{a}{b} \right)^{-1} \left(\frac{R-1}{R+1} \right) \cos 2\chi \quad (8)$$

and for 1^{*-}

$$W(\chi) = 1 - \frac{1}{2} \left(1 + \frac{c}{d} \right)^{-1} \left(\frac{R-1}{R+1} \right) \cos 2\chi, \quad (9)$$

where N/M has been replaced by $R = 1 + N/M$,

$R \geq 0$.

A plot of R versus α is given in Ref. 11 in Fig. 4. In the α range of interest, R increases monotonically with α with a flattening trend for larger α . In particular, for $\alpha = 0$, $R = 0.5$ but this point is $\Delta\phi = 0$, and so it is not relevant to experiment as we discussed above; near $\alpha \approx 1$, $R = 1$, so here the $W(\chi) = 1$ for both 1^{**} and 1^{*-} ; and then at $\alpha = 8$, $R \approx 1.316$. Assuming, then, a favorable value of $\alpha = 8$ (but still $\Delta\phi \ll 1$), we find for 1^{**}

$$W(\chi) = 1 + \left(1 + \frac{a}{b} \right)^{-1} (0.0682) \cos 2\chi \quad (10)$$

with $a, b \geq 0$, and for 1^{*-}

$$W(\chi) = 1 - \left(1 + \frac{c}{d} \right)^{-1} (0.0682) \cos 2\chi \quad (11)$$

with $c, d \geq 0$. So, the direction-polarization coefficient cannot be large in this case.

For $e\bar{e} \rightarrow 1^{*-} \rightarrow 0^{*+} \gamma$ the expressions given above hold, but now the coefficients are unique with $a = 0$ (for 0^{*-}) and $c = 0$ (for 0^{*+}), respectively. The direction-polarization distributions, then, have the coefficients $\pm(R-1)/(R+1)$, which equal ± 0.0682 for $\alpha = 8$.

Our purpose in this calculation was to assess very simply the possible magnitude of this parity signature. The specific choice of $\alpha = 8$ (but still $\Delta\phi \ll 1$) was made because it is not unrealistic experimentally and because it does enhance the effect, versus a smaller choice of α . Again, if actual data existed, one *might* be able to enhance the effect somewhat further by cuts in α . (Comparison with a similar proposal in Ref. 11 indicates that an effective $R \lesssim 1.5$ in this way might be possible, depending in part on the nucleus chosen, so 0.0682 *might* be replaced by a number ≤ 0.2 .)

III. PARITY DETERMINATIONS FOR THE NEW GENERATION OF HEAVY NEUTRAL MESONS

From the preceding discussion the simplest tests to establish an "exotic" J^{PC} meson, and to determine its parity, are the following.

(i) For spin 0, if C is odd, then the meson is exotic. Such states can be searched for and established via γ cascade chains. Since $0^{*-} \rightarrow PV$, observation of its PV mode would uniquely establish its parity. For 0^{*-} , however, no easily identifiable hadronic modes exist, and so, unlike for the case of even charge conjugation, $\phi\phi$ decay¹² cannot be used as a parity test. Other hadronic decay channels can couple to 0^{*-} . In the SU(3) limit, both 0^{*+} and 0^{*-} can be coupled to AV channel and $0^{*-} \rightarrow SV$, whereas $0^{*+} \rightarrow SV$ (forbidden by parity conservation). The latter mode would

probably be difficult to identify but in principle it is a definitive parity signature for 0^{--} .

(ii) For spin J , $J > 0$, the simplest test is based on the fact that both the exotic and normal J^{PC} meson can couple to $V\bar{V}$ channel, e.g., $\phi\phi$, so the parity can be determined, if such a decay mode is observed, by a study of the dependence of the decay distribution on the azimuthal angle between the two $V \rightarrow PP'$ decay planes. This method, which is independent of the polarization state of the particle, is discussed in Trueman's recent article.^{13,12} For example, consider the choice of 1^- (exotic) versus 1^{++} (normal). Then $\phi\phi \rightarrow 2K2\bar{K}$ or $K^*\bar{K}^* \rightarrow 2K2\pi$ would have a decay distribution $(1 + \frac{1}{2}\cos\phi)$ for $J^{PC} = 1^{--}$ and $(1 - \frac{1}{2}\cos\phi)$ for $J^{PC} = 1^{++}$. The azimuthal angle between two $V \rightarrow PP'$ decay planes is denoted by ϕ , and the $K^* \dots$ acceptances are $\pi/2$ in the V rest frame (for $\phi \rightarrow K^*K^-$, the angle ϕ is specified by the two K^* momenta).

Obviously, the parity of new heavy neutral mesons with J^{PC} quantum numbers as allowed by the nonrelativistic $q\bar{q}$ system can also be determined. Since $(0^{++}, 1^{--}, 2^{++}, \dots) \rightarrow P\bar{P}$ but $(0^{--}, 1^{--}, 2^{--}, \dots) \not\rightarrow P\bar{P}$, observation of $P\bar{P}$ mode will, of course, establish states of the former series. The 1^{--} has quantum numbers of the photon and so could be formed in $e\bar{e}$ colliding beams. Since mesons of both series can couple to $V\bar{V}$, the dependence of the decay distribution on the azimuthal angle of the $V \rightarrow PP'$ decay planes can again be used to establish the parity for states of either series for any spin.

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APPENDIX: EXPRESSIONS USED FOR STUDYING MEASUREMENT OF LINEAR γ POLARIZATION BY PAIR PRODUCTION

For completeness we list those expressions which we used in the calculation discussed in Sec. II. The γ conversion into $e\bar{e}$ density matrix, Eq. (7), we expressed in terms of

$$M(\alpha) = (\alpha^2 - 1)^{-2} \left\{ \frac{1}{2} k^2 (\alpha^2 - 1) [-\alpha^2 + \alpha(2\alpha^2 - 1)f(\alpha)] - 2\epsilon_1\epsilon_2 (\alpha^2 - 1) [-\alpha^2 + \alpha^3 f(\alpha)] \right\}, \quad (A1)$$

$$N(\alpha) = (\alpha^2 - 1)^{-2} \left\{ -2\epsilon_1\epsilon_2 (\alpha^2 - \frac{3}{2}) \times [\alpha^2 - \frac{1}{3}\alpha(2\alpha^2 + 1)f(\alpha)] \right\}, \quad (A2)$$

where

$$f(\alpha) = \begin{cases} \cosh^{-1}\alpha/(\alpha^2 - 1)^{1/2}, & \alpha > 1 \\ 1, & \alpha = 1 \\ \cos^{-1}\alpha/(1 - \alpha^2)^{1/2}, & \alpha < 1. \end{cases}$$

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¹See, e.g., V. Novikov *et al.*, Moscow Report No. ITEP, N65, 1979 (unpublished); R. L. Jaffe and K. Johnson, Phys. Lett. 60B, 201 (1975).

²For a review of the early experiments reporting candidates for baryonium, see L. Montanet, in *Phenomenology of Quantum Chromodynamics*, proceedings of the 13th Rencontre de Moriond, 1978, edited by J. Trân Thanh Vân (Editions Frontières, Gif-Sur-Yvette, 1978), Vol. 1. Duality arguments have been used to predict $B\bar{B}$ resonances in J. L. Rosner, Phys. Rev. Lett. 21, 950 (1968); P. G. O. Freund, R. Waltz, and J. L. Rosner, Nucl. Phys. B13, 237 (1969).

³A recent study of gluon bound states was reported by L. Okun at the Geneva Conference on High Energy Physics, 1979 (unpublished). See Ref. 1 and references therein.

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mann and M. Krammer, Phys. Lett. 70B, 457 (1977).

⁵We denote P (pseudoscalar), V (vector), S (scalar), A (axial vector), and B (a spin- $\frac{1}{2}$ baryon); all massive.

⁶These selection rules are all for free, on mass-shell state vectors. A careful distinction must be made between the bound-state, for example, $B\bar{B}$, system and the free state vector. To any finite order in perturbation theory, free $B\bar{B}$ states do not couple to exotic mesons [for proof of such decoupling theorems see Appendix to N. P. Chang and C. A. Nelson, Phys. Rev. D 19, 3336 (1979)]. In bound-state Bethe-Salpeter equations, examples of exotic states have been found, see, e.g., N. Nakanishi, Prog. Theor. Phys. Suppl. 43, 1 (1969); and M. Böhm, H. Joos, and M. Krammer, in *Proceedings of the XII Schlading Conference on Nuclear Physics*, edited by P. Urban (Springer, Berlin, 1973) [Acta Phys. Austriaca Suppl. 11, (1973)], p. 3.

⁷See, e.g., *The Electromagnetic Interaction in Nuclear Spectroscopy*, (edited by W. B. Hamilton (North-Holland,

Amsterdam, 1975); A. J. Ferguson, *Angular Correlations Methods in γ -ray Spectroscopy* (North-Holland, Amsterdam, 1965), p. 91; R. M. Steffen and K. Alder, in *Alpha-, Beta-, and Gamma-Ray Spectroscopy*, edited by K. Siegbahn (North-Holland, Amsterdam, 1966), p. 545.

⁸Spin tests for intermediate states in γ decay cascades have been studied in the general, relativistic case in P. K. Kabir and A. J. G. Hey, *Phys. Rev. D* **13**, 3161 (1976); and see G. Karl, S. Meshkov, and J. Rosner, *ibid.* **13**, 1203 (1976). In the dipole approximation, calculations of spin-test correlation functions have been reported in, e.g., G. J. Feldman and F. J. Gilman, *ibid.* **12**, 2161 (1975); and by L. S. Brown and R. Cahn, *ibid.* **13**, 1195 (1976).

⁹D. Zwanziger, in *Lectures in Theoretical Physics*, edited by W. E. Brittin and A. O. Barut (Univ. of Colorado Press, Boulder Colorado, 1965), Vol. 7A.

¹⁰That pair production may be used to determine the polarization of high-energy photons was suggested by C. N. Yang, *Phys. Rev.* **77**, 722 (1950); and by T. H. Berlin and L. Madansky, *ibid.* **78**, 623 (1950). See, G. C. Wick, *ibid.* **81**, 467 (1951).

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