

## Difficulty of $V(e)V(q) + A(e)A(q)$ neutral currents in $SU(2) \times U(1) \times U(1)$ theory

Kyungsik Kang

*Department of Physics, Brown University, Providence, Rhode Island 02912*

Jihn E. Kim

*Department of Physics, University of Pennsylvania, Philadelphia, Pennsylvania 19174*

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It is shown that the condition of no Adler-Bell-Jackiw anomalies in the  $SU(2) \times U(1) \times U(1)'$  gauge theory having vector-type  $C_\mu$  coupling and the right-handed fermions all in the singlet representations excludes the possibility that the neutral-current interaction of the leptons and hadrons is of the form  $VV + AA$ .

The original Weinberg-Salam (WS) model<sup>1</sup> of gauge theories has successfully predicted the existence of neutrino related hadronic neutral currents as confirmed by CERN, Fermilab, and Brookhaven experiments.<sup>2</sup> However, the need for extending the gauge groups and fermion representations was often motivated by new experimental discoveries.<sup>3</sup>

The proliferation of quarks and leptons began with the so-called "high- $\gamma$  anomaly". A right-handed quark doublet was introduced. Since the high- $\gamma$  anomaly has not been confirmed by more recent experiment,<sup>4</sup> this motivation for the introduction of the right-handed doublets in  $SU(2) \times U(1)$  theory is no longer operative. Hence the WS theory seems to describe all neutrino-hadron experiments.<sup>5</sup> However, a problem still remains: Is there parity violation in atomic physics? The first-generation experiments on this have brought conflicting results. The Washington (Seattle) group<sup>6</sup> did not see the effect, but the Novosibirsk group<sup>7</sup> saw the effect agreeing with the WS predictions. The first<sup>8</sup> of the second-generation experiments again by the Washington group confirmed their earlier result. Therefore, it is fair to say that the parity-violation problem in atomic physics is not settled yet.

Nevertheless, we may ask if it is possible to have no parity violation in atomic physics when the right-handed fermions are all assigned in the singlet representations. Of course it is not possible in  $SU(2) \times U(1)$  theory. But is it still the case if there exist more neutral gauge bosons? We would like to answer this with the previously considered  $SU(2) \times U(1) \times U(1)'$  model.<sup>9</sup> [The method may easily be extended to any number of  $U(1)$  factors. In principle, some of these  $U(1)$  factors can be remnants of, e.g., the superunified gauge group or any simple flavor group whose rank is larger than 2.]

In this theory, we have two massive neutral vector bosons. Hence one may think<sup>10</sup> that it is al-

ways possible to have the  $VV + AA$  form of neutral currents, and the parity is conserved by the electron-related neutral currents but apparently violated by the neutrino-related neutral-current experiments because of the left-handed (right-handed) laboratory  $\nu(\bar{\nu})$ . Our results show that it is not the case. The main reason is the constraint coming from no triangle anomalies which is often overlooked in phenomenological application<sup>9</sup> of gauge models. In an  $SU(2) \times U(1) \times U(1)'$  gauge theory, the charge can be defined by the formula  $Q = T_3 + (Y + C)/2$  where  $Y$  and  $C$  are two different weak hypercharges. But we can always redefine the gauge fields such that only one of the hypercharges appear in the charge relation

$$Q = T_3 + \frac{1}{2} Y. \quad (1)$$

We will use this convention, because it gives simpler expressions for the triangle anomaly. There are gauge fields  $A_\mu^i$  ( $i = 1, 2, 3$ ),  $B_\mu$ , and  $C_\mu$ . Fermions are grouped into "V-A" doublets and "V+A" singlets as in the WS model,

$$L_e = \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \quad \nu_{eR}, e_R; \text{ etc.} \quad (2)$$

$$L_d = \begin{pmatrix} u' \\ d \end{pmatrix}_L, \quad u_R, d_R; \text{ etc.}$$

We choose to work with the minimal scalar multiplets, one doublet and another singlet,

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \quad \phi' = (\phi'_0). \quad (3)$$

We proceed to construct neutral-current interactions of the form  $V(e)V(q) + A(e)A(q)$  while maintaining the renormalizability of the theory, in particular requiring the absence of triangle anomalies.<sup>11</sup> Since this constraint is independent of the detailed mass matrix of the gauge bosons, we choose any independent set of gauge fields, say

$$A_\mu^i (i=1, 2, 3), A_\mu (\equiv \text{photon}), C_\mu \quad (4)$$

and require at the outset that there be no triangle anomalies. In general, the photon field  $A_\mu$  is a linear combination of primordial fields  $A_\mu^3, B_\mu,$  and  $C_\mu$ . The gauge fields in (4) are associated with the matrices,

$$T_i (i=1, 2, 3), Q, C. \quad (5)$$

Note that the use of relation (1) leaves the gauge boson  $C_\mu$  couplings completely arbitrary. Were  $Q = T_3 + (Y+C)/2$  used,  $Y$  or  $C$  would be arbitrary though  $(Y+C)$  is not. The merit of using (1) here lies in that the triangle graphs involving  $A_\mu^i$  and  $A_\mu$  ( $\equiv$  photon) do not cause anomaly in the case of equal number of "V-A" leptons ( $Q=0, -1$ ) and color-tripled quark doublets ( $Q = \frac{2}{3}, -\frac{1}{3}$ ). This is because<sup>12</sup>

$$\text{Tr}QT^2 = 0, \quad (6)$$

or equivalently  $\text{Tr}Q=0$  is satisfied in this case. Extending the argument of vanishing  $d_{abc}$  terms to include  $C_\mu$ , we find the following constraints:

$$\text{Tr}CT^2 = 0, \quad (7)$$

$$\text{Tr}QC^2 = 0, \quad (8)$$

$$\text{Tr}CQ^2 = 0, \quad (9)$$

$$\text{Tr}T_3QC = 0, \quad (10)$$

$$\text{Tr}C^3 = 0. \quad (11)$$

The "V-A" fermions contribute to (6)-(11) positively whereas the "V+A" fermions contribute negatively. Further, (8), (9), and (11) get contributions from the singlets.

To be more general a right-handed neutrino is introduced, thus making it massive in principle. Treating the three lepton families ( $\nu_e, e$ ), ( $\nu_\mu, \mu$ ), and ( $\nu_\tau, \tau$ ) and the three quark families ( $u, d$ ), ( $c, s$ ), and ( $t, b$ ) symmetrically, we have eight c

TABLE I. Eigenvalues of  $Y$  and  $C$ .

	$Y$	$C$
$L_e$	-1	$(\alpha, -1 + 2\alpha)$
$\nu_R$	0	$\alpha$
$e_R$	-2	$-1 + 2\alpha$
$L_d$	$\frac{1}{3}$	$(\frac{2}{3} - \alpha, -\frac{1}{3})$
$u_R$	$\frac{4}{3}$	$\frac{2}{3} - \alpha$
$d_R$	$-\frac{2}{3}$	$-\frac{1}{3}$
$\phi$	1	$(c_+, c_0)$
$\phi'$	0	$c'$

parameters,  $c_\nu^L, c_e^L, c_u^L, c_d^L, c_\nu^R, c_e^R, c_u^R,$  and  $c_d^R$ . Five of these can be removed from the relations (7)-(11), thus leaving three unknown  $c$ 's. However, if the  $C_\mu$  coupling is vector, i.e.,  $c_\nu^L = c_\nu^R, c_e^L = c_e^R,$  etc., then only (7) and (10) give nontrivial results for four remaining  $c$  parameters, leaving only two unknown  $c$ 's. We will study this simple case of vector  $C_\mu$  coupling in the following. As far as fermions are concerned one of these parameters can be absorbed into the redefinition of the gauge coupling  $g''$ . We then find for the vector-type  $C_\mu$  couplings that

$$\begin{aligned} c_\nu &= \alpha, \\ c_e &= -1 + 2\alpha, \\ c_u &= \frac{2}{3} - \alpha, \\ c_d &= -\frac{1}{3}. \end{aligned} \quad (12)$$

If the neutrino appears only as a member of the left-handed doublet and yet the  $C_\mu$  coupling is of vector type, we must have  $\alpha=0$ . In this case the eigenvalues of  $C$  are simply given by the respective electric charges. For completeness we give the eigenvalues of  $Y$  and  $C$  in Table I. Hence the gauge-invariant Lagrangian is

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4}(\partial_\mu \vec{A}_\nu - \partial_\nu \vec{A}_\mu + g\vec{A}_\mu \times \vec{A}_\nu)^2 - \frac{1}{4}(\partial_\mu B_\nu - \partial_\nu B_\mu)^2 - \frac{1}{4}(\partial_\mu C_\nu - \partial_\nu C_\mu)^2 \\ & - \bar{L}_e \gamma_\mu \left[ \partial_\mu - ig \frac{1}{2} \vec{\tau} \cdot \vec{A}_\mu + \frac{1}{2} ig' B_\mu - \frac{1}{2} ig'' \begin{pmatrix} \alpha & 0 \\ 0 & -1 + 2\alpha \end{pmatrix} C_\mu \right] L_e \\ & - \bar{e}_R \gamma_\mu (\partial_\mu + ig' B_\mu + \frac{1}{2} ig'' (1 - 2\alpha) C_\mu) e_R - \bar{\nu}_{eR} \gamma_\mu (\partial_\mu - \frac{1}{2} ig'' \alpha C_\mu) \nu_{eR} \\ & + (\mu\text{-family terms}) + (\tau\text{-family terms}) - \bar{L}_d \gamma_\mu \left[ \partial_\mu - \frac{1}{2} ig \vec{\tau} \cdot \vec{A}_\mu - \frac{1}{6} ig' B_\mu - \frac{1}{2} ig'' \begin{pmatrix} \frac{2}{3} - \alpha & 0 \\ 0 & \frac{1}{3} \end{pmatrix} C_\mu \right] L_d \\ & - \bar{u}_R \gamma_\mu [\partial_\mu - \frac{1}{3} ig' B_\mu - \frac{1}{2} ig'' (\frac{2}{3} - \alpha) C_\mu] u_R - \bar{d}_R \gamma_\mu (\partial_\mu + \frac{1}{3} ig' B_\mu + \frac{1}{6} ig'' C_\mu) d_R \\ & + (s\text{-family terms}) + (b\text{-family terms}) + (\text{Yukawa-coupling terms}) \\ & - \left| \partial_\mu \phi - \frac{1}{2} ig \vec{\tau} \cdot \vec{A}_\mu - \frac{1}{2} ig' B_\mu \phi - \frac{1}{2} ig'' \begin{pmatrix} c_+ & 0 \\ 0 & c_0 \end{pmatrix} C_\mu \phi \right|^2 - \left| \partial_\mu \phi' - \frac{1}{2} ig'' c' C_\mu \phi' \right|^2 - V(\phi, \phi'), \end{aligned} \quad (13)$$

where the Yukawa-coupling terms generate fermion masses as usual through spontaneous symmetry breaking and  $V$  is the usual Higgs potential having minima at  $\langle\phi^0\rangle=v/\sqrt{2}$  and  $\langle\phi^{\pm}\rangle=v'/\sqrt{2}$ . While the charged vector bosons  $W_{\mu}^{\pm}=(A_{\mu}^1\mp iA_{\mu}^2)/\sqrt{2}$  have the mass

$$M_W = \frac{1}{2}g'v, \quad (14)$$

those of the physical neutral gauge bosons  $A_{\mu}$ ,  $Z_{\mu}$ , and  $X_{\mu}$  are governed by

$$\frac{1}{2}(M_Z^2 Z_{\mu}^2 + M_X^2 X_{\mu}^2) + 0 \times A_{\mu}^2$$

$$\begin{bmatrix} \sin\theta, & -\cos\theta \cos\psi, & -\cos\theta \sin\psi \\ \cos\theta \sin\zeta, & \sin\theta \cos\psi \sin\zeta & \sin\theta \sin\psi \sin\zeta \\ & +\sin\psi \cos\zeta, & -\cos\psi \cos\zeta \\ -\cos\theta \cos\zeta, & -\sin\theta \cos\psi \cos\zeta & -\sin\theta \sin\psi \cos\zeta \\ & +\sin\psi \sin\zeta, & -\cos\psi \sin\zeta \end{bmatrix}. \quad (17)$$

The neutral gauge bosons couple to fermions as

$$\begin{aligned} \mathcal{L}^{NC} = & (\bar{\nu}_e, \bar{e})_L i\gamma_{\mu} \begin{pmatrix} \frac{1}{2}gA_{\mu}^3 - \frac{1}{2}g'B_{\mu} + \frac{1}{2}\alpha g''C_{\mu}, & 0 \\ 0, & -\frac{1}{2}gA_{\mu}^3 - \frac{1}{2}g'B_{\mu} + \frac{1}{2}g''(-1+2\alpha)C_{\mu} \end{pmatrix} \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L \\ & + \bar{e}_R i\gamma_{\mu} [-g'B_{\mu} - \frac{1}{2}g''(1-2\alpha)C_{\mu}] e_R + \bar{\nu}_R i\gamma_{\mu} (\frac{1}{2}g''\alpha C_{\mu}) \nu_R \\ & + (\bar{u}, \bar{d})_L i\gamma_{\mu} \begin{pmatrix} \frac{1}{2}gA_{\mu}^3 + \frac{1}{6}g'B_{\mu} + \frac{1}{2}g''(\frac{2}{3}-\alpha)C_{\mu}, & 0 \\ 0, & -\frac{1}{2}gA_{\mu}^3 + \frac{1}{6}g'B_{\mu} - \frac{1}{6}g''C_{\mu} \end{pmatrix} \begin{pmatrix} u \\ d \end{pmatrix}_L \\ & + \bar{u}_R i\gamma_{\mu} [\frac{2}{3}g'B_{\mu} + g''(\frac{1}{3}-\frac{1}{2}\alpha)C_{\mu}] u_R + \bar{d}_R i\gamma_{\mu} (-\frac{1}{3}g'B_{\mu} - \frac{1}{6}g''C_{\mu}) d_R. \end{aligned} \quad (18)$$

There are relations between  $\theta$ ,  $\psi$ ,  $\zeta$  and  $g$ ,  $g'$ ,  $g''$ ,  $c_0$ ,  $v$ , and  $c'v'$ . The electromagnetic coupling is correctly given if

$$g \sin\theta = g' \cos\theta \sin\zeta, \quad (19)$$

along with either

$$(i) \cos\zeta = 0,$$

or

$$(ii) \alpha = 0.$$

Then the case (i) gives

$$e = g \sin\theta = \frac{gg'}{(g^2 + g'^2)^{1/2}}, \quad (20)$$

while the case (ii) gives

$$e = g \sin\theta - \frac{1}{2}g'' \cos\theta \cos\zeta. \quad (21)$$

We have given in Tables II and III the respective neutral-current couplings of cases (i) and (ii) explicitly. The entries of the Tables are the coupling strength of the neutral gauge bosons,  $Z_{\mu}$  and  $X_{\mu}$ , to the respective fermion currents. For case (i)  $\sin\zeta$  is set to +1.

$$= \frac{1}{8}v^2(gA_{\mu}^3 - g'B_{\mu} - g''c_0C_{\mu})^2 + \frac{1}{8}v'^2(g''c'C_{\mu})^2. \quad (15)$$

The fields of the mass eigenstates are related to the primordial fields through

$$\begin{pmatrix} A_{\mu}^3 \\ B_{\mu} \\ C_{\mu} \end{pmatrix} = M \begin{pmatrix} A_{\mu} \\ Z_{\mu} \\ X_{\mu} \end{pmatrix}, \quad (16)$$

where  $M$  is

We now proceed to examine the possibility of having the neutral-current interactions of the  $V(e)V(q)+A(e)A(q)$  form. Consider, for example, the case where  $J_{\mu}^Z$  is a vector current and  $J_{\mu}^X$  is an axial-vector current. Then we must have from case (i) that  $\cos\psi=0$ , which results in  $1-4\sin^2\theta=0$ ,  $1-\frac{8}{3}\sin^2\theta=0$ , and  $1-\frac{4}{3}\sin^2\theta=0$  all at the same time. This is clearly impossible. The case (ii) gives  $\cos\psi + \sin\theta \sin\psi \cot\zeta = 0$ , which results  $\cos\theta \sin\psi - 3 \tan\theta (\sin\theta \sin\psi - \cos\psi \cot\zeta) = 0$ ,  $\cos\theta \sin\psi - \frac{5}{3} \tan\theta (\sin\theta \sin\psi - \cos\psi \cot\zeta) = 0$ , and  $\cos\theta \sin\psi + \frac{1}{3} \tan\theta (\sin\theta \sin\psi - \cos\psi \cot\zeta) = 0$  again all at the same time. These relations are mutually inconsistent. Similar inconsistency arises when the role of  $J_{\mu}^Z$  and  $J_{\mu}^X$  are interchanged.

Thus we have shown that the constraint of no triangle anomaly excludes the  $VV+AA$  form of the neutral-current interactions in the  $SU(2) \times U(1) \times U(1)'$  theory in which the right-handed fermions are all singlets and the  $C_{\mu}$  coupling is a vector type. We must face the parity violations in atomic physics in such models. If we relax the assumption on the vector-type  $C_{\mu}$  coupling, the analysis

TABLE II. Neutral-current couplings of case (i).

Currents	$Z_\mu$	$X_\mu$
$i\bar{\nu}\gamma_\mu\nu$	$-\frac{1}{4}g\sec\theta\cos\psi + \frac{1}{2}\alpha g''\sin\psi$	$-\frac{1}{4}g\sec\theta\sin\psi - \frac{1}{2}\alpha g''\cos\psi$
$i\bar{\nu}\gamma_\mu\gamma_5\nu$	$-\frac{1}{4}g\sec\theta\cos\psi$	$-\frac{1}{4}g\sec\theta\sin\psi$
$i\bar{e}\gamma_\mu e$	$\frac{1}{4}g\sec\theta\cos\psi - \frac{1}{2}g''(1-2\alpha)\sin\psi$	$\frac{1}{4}g\sec\theta\sin\psi(1-4\sin^2\theta)$ $+ \frac{1}{2}g''(1-2\alpha)\cos\psi$
$i\bar{e}\gamma_\mu\gamma_5e$	$\frac{1}{4}g\sec\theta\cos\psi$	$\frac{1}{4}g\sec\theta\sin\psi$
$i\bar{u}\gamma_\mu u$	$-\frac{1}{4}g\sec\theta\cos\psi(1-\frac{8}{3}\sin^2\theta)$ $+ \frac{1}{2}g''(\frac{2}{3}-\alpha)\sin\psi$	$-\frac{1}{4}g\sec\theta\sin\psi(1-\frac{8}{3}\sin^2\theta)$ $-\frac{1}{2}g''(\frac{2}{3}-\alpha)\cos\psi$
$i\bar{u}\gamma_\mu\gamma_5u$	$-\frac{1}{4}g\sec\theta\cos\psi$	$-\frac{1}{4}g\sec\theta\sin\psi$
$i\bar{d}\gamma_\mu d$	$\frac{1}{4}g\sec\theta\cos\psi(1-\frac{4}{3}\sin^2\theta)$	$\frac{1}{4}g\sec\theta\sin\psi(1-\frac{4}{3}\sin^2\theta)$
$i\bar{d}\gamma_\mu\gamma_5d$	$-\frac{1}{6}g''\sin\psi$	$+\frac{1}{6}g''\cos\psi$
	$\frac{1}{4}g\sec\theta\cos\psi$	$\frac{1}{4}g\sec\theta\sin\psi$

would require far more complexity, thus losing the simplicity of the theory.

The conclusion reached in this paper does not apply to the case in which right-handed doublets are utilized. For example, if one starts out with a larger vectorlike group<sup>13</sup> which contains  $SU(2) \times U(1) \times U(1)'$ , there would necessarily be right-handed nonsinglet fermions and there would be no triangle anomalies.

*Note added in proof.* After we submitted this paper for publication, the result of the polarized electron scattering by deuteron<sup>14</sup> was reported, which essentially rules out the neutral-current interaction of the form  $V(e)V(q) + A(e)A(q)$ .

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TABLE III. Neutral-current couplings of case (ii).

Currents	$Z_\mu$	$X_\mu$
$i\bar{\nu}\gamma_\mu\nu$	$-\frac{1}{4}g\sec\theta\cos\psi - \frac{1}{4}g\tan\theta\cot\xi\sin\psi$	$-\frac{1}{4}g\sec\theta\sin\psi + \frac{1}{4}g\tan\theta\cot\xi\cos\psi$
$i\bar{\nu}\gamma_\mu\gamma_5\nu$	$-\frac{1}{4}g\sec\theta\cos\psi - \frac{1}{4}g\tan\theta\cot\xi\sin\psi$	$-\frac{1}{4}g\sec\theta\sin\psi + \frac{1}{4}g\tan\theta\cot\xi\cos\psi$
$i\bar{e}\gamma_\mu e$	$\frac{1}{4}g\cos\theta\cos\psi - \frac{3}{4}g\tan\theta(\sin\theta\cos\psi + \sin\psi\cot\xi)$ $-\frac{1}{2}g''(-\sin\theta\cos\psi\cos\xi + \sin\psi\sin\xi)$	$\frac{1}{4}g\cos\theta\sin\psi - \frac{3}{4}g\tan\theta(\sin\theta\sin\psi - \cos\psi\cot\xi)$ $+ \frac{1}{2}g''(\sin\theta\sin\psi\cos\xi + \cos\psi\sin\xi)$
$i\bar{e}\gamma_\mu\gamma_5e$	$\frac{1}{4}g\sec\theta\cos\psi + \frac{1}{4}g\tan\theta\sin\psi\cot\xi$	$\frac{1}{4}g\sec\theta\sin\psi + \frac{1}{4}g\tan\theta\cos\psi\cot\xi$
$i\bar{u}\gamma_\mu u$	$-\frac{1}{4}g\cos\theta\cos\psi + \frac{5}{12}g\tan\theta(\sin\theta\cos\psi + \sin\psi\cot\xi)$ $+ \frac{1}{3}g''(-\sin\theta\cos\psi\cos\xi + \sin\psi\sin\xi)$	$-\frac{1}{4}g\cos\theta\sin\psi + \frac{5}{12}g\tan\theta(\sin\theta\sin\psi - \cos\psi\cot\xi)$ $-\frac{1}{3}g''(\sin\theta\sin\psi\cos\xi + \cos\psi\sin\xi)$
$i\bar{u}\gamma_\mu\gamma_5u$	$-\frac{1}{4}g\sec\theta\cos\psi - \frac{1}{4}g\tan\theta\sin\psi\cot\xi$	$-\frac{1}{4}g\sec\theta\sin\psi + \frac{1}{4}g\tan\theta\cos\psi\cot\xi$
$i\bar{d}\gamma_\mu d$	$\frac{1}{4}g\cos\theta\cos\psi - \frac{1}{12}g\tan\theta(\sin\theta\cos\psi + \sin\psi\cot\xi)$ $+ \frac{1}{6}g''(\sin\theta\cos\psi\cos\xi - \sin\psi\sin\xi)$	$\frac{1}{4}g\cos\theta\sin\psi - \frac{1}{12}g\tan\theta(\sin\theta\sin\psi - \cos\psi\cot\xi)$ $+ \frac{1}{6}g''(\sin\theta\sin\psi\cos\xi + \cos\psi\sin\xi)$
$i\bar{d}\gamma_\mu\gamma_5d$	$\frac{1}{4}g\sec\theta\cos\psi + \frac{1}{4}g\tan\theta\sin\psi\cot\xi$	$\frac{1}{4}g\sec\theta\sin\psi - \frac{1}{4}g\tan\theta\cos\psi\cot\xi$

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