## Comments and Addenda

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## Possible existence of a second minimum in elastic pp scattering

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Comparing new elastic pp data at 200 and 1500 GeV, it is suggested that at higher energies  $d\sigma/dt$  "caves in" at an intermediate  $t$  value. Comparison with predictions of a geometrical picture leads to the speculation of the existence of a second minimum and a third maximum in the elastic differential cross section.

Recently there have been published $1,2$  new data for high-  $|t|$ , high-energy (1500 and 200 GeV) elastic *bb* scattering. These data are sketched in Fig. 1 together with older data<sup>3,4</sup> for lower  $|t|$ values at similar energies (1500 and 280 GeV). The average slope parameter  $b = (d/dt) \ln(d\sigma/dt)$ in the lower- and higher-  $\left| t \right|$  regions is tabulate in Table I. It has been observed<sup>1,2</sup> that the slope parameter is smaller at higher  $|t|$  values. An additional characteristic that we now want to emphasize is that the slope parameter increases (from a high value) with increasing energy for the



FIG. 1. pp elastic differential cross section at 200, 280, and 1500 GeV equivalent laboratory energies. Low- $|t|$  data are taken from Refs. 3, 4, and 12, and high- $|t|$  data from Refs. 1 and 2. The dashed curve indicates the conjectured (schematic) shape for  $pp$  differential cross section at ultrahigh energies much above the ISR range. Error bars that are small are omitted.

lower-  $\left| t \right|$  region, and  $decreases$  (from a low value) with increasing energy for the higher-  $|t|$ region. If this trend continues into higher energies, the  $ln(d\sigma/dt)$  vs  $|t|$  curve must "cave in" in the  $|t| \approx 4$  to 6 GeV<sup>2</sup> region (portions a and b of the dashed curve in Fig. 1). Now it is rather difficult to imagine that at these higher energies the slope parameter remains <0.8 GeV<sup>2</sup> for  $|t|$ larger than 10 GeV<sup>2</sup> (cf., the experimental curve in this region for 200 GeV). Hence we suggest the schematic shape of the portion c of the dashed curve of Fig. 1. Putting the three pieces of the dashed curve together, we suggest the development of a shoulder, or even a (second) minimum and a (third) maximum in the region  $|t| \approx 4$  to 7 GeV' at energies higher than 1500 GeV.

The suggestion above is based purely on the trend of change of the experimental slope parameter with energy. It is interesting to compare this suggestion-with the calculations based on a very simple geometrical picture<sup>5</sup> of hadron collisions. The calculation involves no adjustable parameters; the input is the experimental total cross section  $\sigma_T$  and the form factor  $G_{\mu}$  for the proton. Before discussing the calculation it is perhaps appropri-

TABLE I. Average slope parameter  $b = (d/dt) \ln(d\sigma/dt)$ (in GeV<sup>-2</sup>) in the low- $|t|$  and high- $|t|$  regions for 200-280-GeV and  $1500$ -GeV elastic  $pp$  scattering.

$p_L$ (GeV/c)	$3 <  t  < 6 \text{ GeV}^2$	$7 <  t  < 10 \text{ GeV}^2$
$200 - 280$	1.4	1.05
1500	1.8	0.8

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ate to point out that this geometrical picture has had impressive success: (i) It produced excellent agreement<sup>6</sup> with the high-energy  $pp$  differential cross section, down to details in the  $|t| < 1.2$  GeV<sup>2</sup> region. (ii) It predicted<sup>7,8</sup> the existence of a (first) minimum and a (second) maximum at higher  $|t|$ values, which were later found in CERN ISR experiments. The agreement of the calculation' with experimental data around the first minimum and the second maximum is very good. (iii) Since  $\sigma_{\tau}$  increases with increasing energy, the calculation predicts<sup>9</sup> a shift of the position of the first minimum with energy and a concurrent rise of the second maximum. These characteristics were later found to be in agreement with experiments.<sup>4</sup> However, the picture also predicts<sup>7,8</sup> a second minimum and a third maximum which have $10$  so far not been experimentally verified.

We have redone the computation for the  $pp$  differential cross section, using the same parametrization for form factor  $G_{\mu}$  as in Fig. 1 of Ref. 7, but using a total cross section of  $\sigma_T = 42.5$  mb. The result is exhibited as curve A in Fig. 2. Also exhibited, as curve B, is the same calculation, but with a dipole form factor  $G_M/\mu = (1 + |t|/0.71)^{-2}$ and with  $\sigma_T = 42.5$  mb. Both curves exhibit a second minimum and a third maximum, qualitatively in agreement with the calculations<sup>7,8</sup> of 1968, as they should be, since in the input only the total cross section has been changed.

Comparing curves A and B with the dashed speculative curve of Fig. 1 we wonder whether at superhigh energies the  $d\sigma/dt$  curve may indeed exhibit a second minimum and a third maximum. The four curves, (a) 200 GeV data, (b) 1500 GeV data, (c) dashed curve of Fig. 1, and (d) the curve A (or B), seem to represent a possible trend of development of the  $d\sigma/dt$  curve as the energy increases. Whether this is true is of course best tested with future accelerators Such as Isabelle. We suggest a preliminary test in measuring the energy dependence of  $d\sigma/dt$  at fixed  $t$ , for  $|t\,|=4$ to  $9 \text{ GeV}^2$ , within the ISR energy range of 280 to



FIG. 2. Experimental  $pp$  differential cross section curve at 1500 GeV equivalent laboratory energy. Curves A and B are results of calculations described in the text.

2000 GeV. A comparison of these dependences at different  $t$  may indicate whether there is the beginning of the "cave-in" phenomenon referred to earlier.

If the  $d\sigma/dt$  curve at superhigh energies does exhibit qualitative features like those of curves <sup>A</sup> and B, it would be easy to understand why, in the  $7<|t|<10$  GeV<sup>2</sup> region, the differential cross sections of existing data do not<sup>11</sup> smoothly decrease with increasing energy: As is the case with the second maximum, the high-  $\left| t \right|$  side of the third maximum, i.e., the region  $7 < |t| < 10$  GeV<sup>2</sup>, is approached by the  $d\sigma/dt$  curve at a lower energy than the region near the preceding minimum,  $\left| t \right|$  $=4-5 \text{ GeV}^2$  (cf. the 100 GeV curve in Ref. 12). Thus it is quite natural that the  $d\sigma/dt$  settles down to a "limiting" value quite rapidly in the  $7\!<\!|t|\!<\!10\,\,{\rm GeV}^2$  region

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