# Complementary LHC searches for UV resonances of the $0\nu\beta\beta$ decay operators

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We investigate the quark-level effective operators related to the neutrinoless double beta  $(0\nu\beta\beta)$  decay process and their ultraviolet completions relevant to chiral enhancement effects at the hadronic level. We have classified several kinds of leptoquark models, matching to different standard model effective operators. Assuming weakly coupled new physics, we find the ongoing  $0\nu\beta\beta$  decay experiments are sensitive to new physics scale at around 2–4 TeV, which is in the reach of LHC searches. We discuss the discovery potential of such resonances in the same-sign dilepton channels at the LHC. Therefore, the direct LHC searches and indirect  $0\nu\beta\beta$  decay searches are complementary to each other in testing the UV completions of the effective operators for  $0\nu\beta\beta$  decay.

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#### I. INTRODUCTION

The origin of the tiny neutrino masses remains mysterious in particle physics. To understand this mystery, it is crucial to know the nature of neutrinos, whether the neutrinos are Majorana or Dirac fermions. Neutrinoless double beta decay  $(0\nu\beta\beta)$  in nuclei provides the most sensitive way to assess the Majorana nature of neutrinos [1]. It has been shown [2] that if the  $0\nu\beta\beta$  decay process is observed, neutrinos must have Majorana masses.

There have been lots of studies on  $0\nu\beta\beta$  decay, from the search for the signal in the standard mechanism with the exchange of three light Majorana neutrinos to the various interpretations in terms of new physics beyond the standard model (BSM); e.g., see Refs. [3,4] for review. In ultraviolet (UV) theories such as the left-right symmetric model (LRSM) [5,6], the origin of neutrino masses is explained while promising signals in  $0\nu\beta\beta$  decay and at colliders are

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Given the hierarchy between the new physics scale and the nuclei scale, the effective field theory (EFT) framework has been utilized [8,11–13] to systematically parametrize various new physics effects in the low-energy hadronic and nuclei scales, matching theories to experiments with unprecedented sensitivities.

Above the electroweak (EW) scale, the BSM physics can be systematically described by a series of higherdimensional operators in the standard model effective field theory (SMEFT), which respects the  $SU(3)_C \times SU(2)_L \times$  $U(1)_{V}$  gauge symmetry. Effective operators with odd dimensions can give rise to the lepton number violation by two units,  $\Delta L = 2$ . There is only one dim-5 (dimension 5) operator, that is the Weinberg operator [14], while the numbers of effective operators at higher dimensions blow up. The complete bases of dim-7 [15,16] and dim-9 operators [9,17] in the SMEFT have been obtained in recent years. Below the EW scale, the SM heavy fields including Higgs boson, top quark, and W and Z bosons are integrated out leading to the low-energy EFT (LEFT) with the unbroken  $SU(3)_C \times U(1)_{em}$  gauge symmetry. The complete bases of effective operators in the LEFT up to dim 9 have been achieved [18–20].

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Below the hadronic scale, the quark-lepton operators should be matched to the chiral Lagrangian at the hadronic level, and these hadronic operators are organized by chiral power counting. If the  $0\nu\beta\beta$  decay process originates from the exchange of BSM fields, the LNV interactions at low energies are described by the dim-9 quark-lepton operators in the LEFT. Among them, the operators  $O_4\bar{e}_L e_L^c$  and  $O_4\bar{e}_R e_R^c$  [cf. Eq. (2)] give rise to the long-range pion exchange at the hadronic scale with chiral enhancement [11,21]. The impact on the half-life of  $0\nu\beta\beta$  decay has been studied in detail in Refs. [8,11].

Assuming weakly coupled new physics, the future tonnescale  $0\nu\beta\beta$  experiments are typically sensitive to the new physics scale  $\Lambda$  around 1–2 TeV, which is in the reach of the searches at the Large Hadron Collider (LHC) [22,23]. However, the chiral enhancement effect would greatly enhance the  $0\nu\beta\beta$  decay rate and, thus, push the new physics scale  $\Lambda$  to 2–4 TeV. This has been investigated in the LRSM [24] due to the large mixing between the left- and right-handed W bosons, which renders the effective operators  $O_4\bar{e}_L e_L^c$  and  $O_4\bar{e}_R e_R^c$  after integrating out heavy particles below the EW scale. However, in this scenario the new physics scale characterized by the right-handed W boson mass has been severely constrained by the LHC data [25]. This motivates us to consider other kinds of UV scenarios with chiral enhancement at low energies.

The UV completions of the dim-9 quark-lepton operators responsible for  $0\nu\beta\beta$  decay have been systematically classified at tree level [26] and one-loop level [27]. With the development of the EFTs, new ways of constructing the UV completions of the effective operators in the SMEFT have been proposed [28], which have been used to obtain the complete UV resonances at tree level up to the dim-7 level [29] and the dim-8 level [30]. Following these, we find that there are certain tree-level UV completions that have not been discussed in Ref. [26].

In this work, rather than investigating all UV completions<sup>1</sup> of the dim-9 SMEFT operators for  $0\nu\beta\beta$  decay, we will focus on the UV resonances that give rise to the chiral enhancement while not severely constrained experimentally. Technically, we investigate possible "two-step" UV relations of the dim-9 quark-lepton operators, namely, from LEFT to the SMEFT and then to the UV models, and focus on the operators that lead to chiral enhancement at the hadronic scale.

We find that leptoquarks (LQs) are good candidates for the UV completions of the operators  $O_4\bar{e}_L e_L^c$  and  $O_4\bar{e}_R e_R^c$ , which are weakly constrained compared to the right-handed W boson [32] with the mass  $m_{LQ} \ge 1.8$  TeV. These UV resonances could be probed by both future tonne-scale  $0\nu\beta\beta$  decay experiments indirectly and the current and future LHC experiments directly through searching for lepton number violation, which is important to uncover the mechanisms for  $0\nu\beta\beta$  decay. Previous studies of  $\Delta L = 2$ lepton number violation induced by LQs at the LHC can be found in Refs. [22,23,33,34].

The remainder of the paper is organized as follows. In the next section, the effective operators for  $0\nu\beta\beta$  decay in the SMEFT and LEFT with chiral enhancement are studied. In Sec. III, possible UV completions of the SMEFT operators with LQs are obtained. In Sec. IV, the half-life of  $0\nu\beta\beta$  decay expressed in terms of the Wilson coefficients of the LEFT operators is given and the reach to the LNV scale is estimated. In Sec. V, LHC searches for the UV resonances are investigated. In Sec. VI, the sensitivities to the UV model in the  $0\nu\beta\beta$  decay and LHC searches are combined and discussed. We conclude in Sec. VII.

#### **II. EFFECTIVE OPERATORS FOR 0νββ DECAY**

In this work, we will study the effective operators that give rise to chirally enhanced contributions to  $0\nu\beta\beta$  decay. In the LEFT below the EW scale, the  $\Delta L = 2$  quark-lepton interactions responsible for  $0\nu\beta\beta$  decay are expressed as [8,21]

$$\mathcal{L}_{\text{LEFT}}^{(9)} \supset \frac{1}{v^5} \sum_{i=1}^8 \left( C_{iL}^{(9)} \bar{e}_L e_L^c + C_{iR}^{(9)} \bar{e}_R e_R^c \right) O_i + \cdots, \quad (1)$$

where the quark operators  $O_i$  are explicitly given in Ref. [8], v = 246 GeV, and the dots depict the terms with different lepton bilinears.

We consider the scenario where only the dim-9 operator  $O_{4X}^{(9)} \equiv O_4 \bar{e}_X e_X^c$  with X = L or *R* is generated directly after the electroweak symmetry breaking (EWSB). The quark operator is defined as [8,21]

$$O_4 = \bar{q}_L^{\alpha} \gamma_\mu \tau^+ q_L^{\alpha} \bar{q}_R^{\beta} \gamma^\mu \tau^+ q_R^{\beta}, \qquad (2)$$

where  $q_{L/R} = (u, d)_{L/R}^T$  are the left- and right-handed isospins,  $\tau^+ = (\tau_1 + i\tau_2)/2$  with  $\tau_i$  the Pauli matrices, and  $\alpha$  and  $\beta$  are color indices. Hereafter, for a chiral fermion field  $\psi$ , we use the notations  $\psi^c \equiv C\bar{\psi}^T$  and  $\bar{\psi}^c = \psi^T C$  with *C* the charge-conjugation matrix.

The operator  $O_{4X}^{(9)}$  would mix with  $O_{5X}^{(9)} \equiv O_5 \bar{e}_X e_X^c$  due to the QCD renormalization group evolution (RGE), where the quark operator

$$O_5 = \bar{q}_L^{\alpha} \gamma_\mu \tau^+ q_L^{\beta} \bar{q}_R^{\beta} \gamma^\mu \tau^+ q_R^{\alpha}.$$
(3)

The corresponding RGE of the Wilson coefficients is [8,35,36]

<sup>&</sup>lt;sup>1</sup>Although we use the terminologies "UV completion" and "UV model," the models we discuss might be embedded into more fundamental UV theories; see Ref. [31], for example, for the related topic. In this sense, they are actually simplified models.

$$\frac{d}{d\ln\mu} \begin{pmatrix} C_{4X}^{(9)} \\ C_{5X}^{(9)} \end{pmatrix} = \frac{\alpha_s}{2\pi} \begin{pmatrix} 1 & 0 \\ -3 & -8 \end{pmatrix} \begin{pmatrix} C_{4X}^{(9)} \\ C_{5X}^{(9)} \end{pmatrix}, \quad (4)$$

where  $\alpha_s$  is the strong coupling. From the scale  $m_W = 80.4$  GeV to the hadronic scale  $\Lambda_H = 2$  GeV, we obtain

$$\begin{pmatrix} C_{4X}^{(9)}(\Lambda_H) \\ C_{5X}^{(9)}(\Lambda_H) \end{pmatrix} = \begin{pmatrix} 0.90 & 0 \\ 0.45 & 2.3 \end{pmatrix} \begin{pmatrix} C_{4X}^{(9)}(m_W) \\ C_{5X}^{(9)}(m_W) \end{pmatrix}.$$
(5)

Both the quark-lepton operators  $O_{4X}^{(9)}$  and  $O_{5X}^{(9)}$  can be mapped to the  $\Delta L = 2$  hadron-lepton operators at the hadronic scale with chiral enhancement in chiral effective field theory; see Refs. [8,11,21] for details. From Eq. (5), we can see that a nonzero  $C_{5X}^{(9)}$  is induced at the hadronic scale, although it is vanishing at the scale  $\mu = m_W$ . The half-life of  $0\nu\beta\beta$  decay including  $C_{4X}^{(9)}$  and  $C_{5X}^{(9)}$  will be given in Sec. IV.

Above the EW scale, effective operators in the SMEFT are written as

$$\mathcal{L}_{\text{SMEFT}}^{(d)} = \sum_{i} \frac{\mathcal{C}_{i}^{(d)}}{\Lambda^{d-4}} \mathcal{O}_{i}^{(d)}, \tag{6}$$

where  $C_i^{(d)}$  are the Wilson coefficients and  $\Lambda$  is the UV scale. In order to generate  $\Delta L = 2$  lepton number violation, the mass dimension *d* should be an odd number. For d = 5, the Weinberg operator [14] arises, which is irrelevant to  $O_{4X}^{(9)}$ . For d = 7, 9, the complete bases of operators have been obtained in Refs. [9,15–17].

At the dim-7 level [15,16], there is only one SMEFT operator that is related to  $O_{4X}^{(9)}$  [13]:

$$\mathcal{O}_{\bar{d}uLLD}^{(7)} = \epsilon^{ij} (\bar{d}_R \gamma^\mu u_R) (\bar{L}_i^c i D_\mu L_j), \tag{7}$$

where  $L = (\nu_e, e)_L^T$  is the SM lepton doublet with the flavor index omitted,  $D_\mu$  is the covariant derivative,  $\epsilon \equiv i\tau_2$  is the antisymmetric tensor with  $\tau_2$  the second Pauli matrix, and  $D_\mu L_j \equiv (D_\mu L)_j$ .

At the dim-9 level, there are four relevant SMEFT operators [13], which are expressed as [9]

$$\mathcal{O}_{1}^{(9)} = \epsilon^{ij} (\bar{d}_{R} \gamma^{\mu} e_{R}) (\bar{u}_{R}^{c} e_{R}) H_{j} D_{\mu} H_{i},$$

$$\mathcal{O}_{2}^{(9)} = \epsilon^{ik} (\bar{d}_{R} L_{j}) (\bar{L}_{i}^{c} \gamma^{\mu} u_{R}) H^{\dagger j} D_{\mu} H_{k},$$

$$\mathcal{O}_{3}^{(9)} = \epsilon^{ij} (\bar{d}_{R} \gamma^{\mu} u_{R}) (\bar{L}_{i}^{c} D_{\mu} L_{j}) H_{k} H^{\dagger k},$$

$$\mathcal{O}_{4}^{(9)} = \epsilon^{ik} (\bar{u}_{R}^{\alpha} Q_{j}^{\beta}) (\bar{L}^{j} d_{R}^{\alpha}) (\bar{L}_{i} Q_{k}^{\beta c}).$$
(8)

Here,  $D_{\mu}H_i \equiv (D_{\mu}H)_i$  and  $H^{\dagger j} \equiv (H^{\dagger})^j$  are used for brevity, and Q is the left-handed quark doublet with  $\alpha$  and  $\beta$  the color indices.

Notice that the quark and lepton fields are contracted with each other in the operators  $\mathcal{O}_1^{(9)}$ ,  $\mathcal{O}_2^{(9)}$ , and  $\mathcal{O}_4^{(9)}$ . In order to match with  $\mathcal{O}_{4X}^{(9)}$ , we use the Fierz relations derived in Ref. [16] and express them as

$$\mathcal{O}_1^{(9)} = -\frac{1}{2}\epsilon^{ij}(\bar{d}_R\gamma^\mu u_R)(\bar{e}_R^c e_R)H_j D_\mu H_i, \qquad (9)$$

$$\mathcal{O}_{2}^{(9)} = -\epsilon^{ik} (\bar{d}_{R}L_{i}) (\bar{L}_{j}^{c} \gamma^{\mu} u_{R}) H^{\dagger j} D_{\mu} H_{k} - \epsilon^{ik} (\bar{L}_{i}^{c}L_{j}) (\bar{d}_{R} \gamma^{\mu} u_{R}) H^{\dagger j} D_{\mu} H_{k}, \qquad (10)$$

$$\mathcal{O}_{4}^{(9)} = -\frac{1}{2} \epsilon^{ik} (\bar{u}_{R}^{\alpha} \gamma^{\mu} d_{R}^{\alpha}) (\bar{L}^{j} \gamma_{\mu} Q_{j}^{\beta}) (\bar{L}_{i} Q_{k}^{\beta c})$$

$$= \frac{1}{2} \epsilon^{ik} (\bar{u}_{R}^{\alpha} \gamma^{\mu} d_{R}^{\alpha}) (\bar{L}_{i} \gamma_{\mu} Q_{j}^{\beta}) (\bar{L}^{j} Q_{k}^{\beta c})$$

$$+ \frac{1}{2} \epsilon^{ik} (\bar{u}_{R}^{\alpha} \gamma^{\mu} d_{R}^{\alpha}) (\bar{Q}_{k}^{\beta} \gamma_{\mu} Q_{j}^{\beta}) (\bar{L}_{i} L^{jc}).$$
(11)

The isospin indices i = j are further required in Eqs. (10) and (11), so that  $\mathcal{O}_2^{(9)}$  and  $\mathcal{O}_4^{(9)}$  can be converted into the operators with separate quark and lepton bilinears. As a result, we can obtain that the Wilson coefficients of the SMEFT operators in Eqs. (7) and (8) remain the same above the EW scale since the vector quark current does not evolve in QCD [8].

After the EWSB, the Wilson coefficients of the SMEFT operators are matched to  $C_{4X}^{(9)}$ . The matching conditions at the scale  $\mu = m_W$  are [13]

$$C_{4R}^{(9)}(m_W) = \frac{i}{2} V_{ud} \frac{v^5}{\Lambda^5} C_1^{(9)*}, \qquad (12)$$

$$C_{4L}^{(9)}(m_W) = \frac{i}{2} V_{ud} \frac{v^5}{\Lambda^5} (\mathcal{C}_2^{(9)*} + 2\mathcal{C}_3^{(9)*}) + \frac{1}{4} \frac{v^5}{\Lambda^5} \mathcal{C}_4^{(9)} - 2V_{ud} \frac{v^3}{\Lambda^3} \mathcal{C}_{duLLD}^{(7)*}, \quad (13)$$

where  $V_{ud} = 0.974$  denotes the quark mixing in the SM. We can see that the contributions of the dim-9 SMEFT operators in Eq. (8) to the Wilson coefficients of the LEFT operators  $\mathcal{O}_{4X}^{(9)} X = L$ , *R* are proportional to  $v^5/\Lambda^5$ ,<sup>2</sup> while that of the dim-7 operator in Eq. (7) is proportional to  $v^3/\Lambda^3$ .

#### **III. UV COMPLETION**

In this section, we will investigate possible UV completions of the SMEFT operators discussed in Sec. II. It is noted that there is no tree-level UV completion of the dim-7

<sup>&</sup>lt;sup>2</sup>The contribution of  $\mathcal{O}_4^{(9)}$  is comparable to the other three dim-9 SMEFT operators, since for the latter both Higgs fields develop the vacuum expectation values that cancel  $m_W^2$  in the propagator in the matching.

TABLE I. The new fields with the corresponding quantum numbers (X, Y, Z) under the  $SU(3)_C$ ,  $SU(2)_L$ , and  $U(1)_Y$  gauge groups are shown. We label the masses of scalar LQs:  $\tilde{R}_2$ ,  $\bar{S}_1$ , and  $S_1$ ; vector LQs:  $U_1$  and  $\tilde{V}_2$ ; vectorlike fermions:  $\Psi = (\Psi_L, \Psi_R)$ ,  $E' = (E'_L, E'_R)$ , and  $d' = (d'_L, d'_R)$ ; and singlet scalar: S as  $m_R, m_{\tilde{S}_1}, m_{S_1}, m_U$ ,  $m_V, m_\Psi, m_{E'}, m_{d'}$ , and  $m_S$ , respectively. The vectorlike fermions are introduced to make the models anomaly-free. We follow the notations of Ref. [38] for LQs; see also Ref. [39].

Operator	Leptoq	uark(s)	Vectorlike fermions	Singlet scalar
$\mathcal{O}_1^{(9)}$	$\tilde{R}_2 \in (3, 2, 1/6)$	$U_1 \in (3, 1, 2/3)$	$\Psi_{L,R} \in (1, 2, -1/2)$	
$\mathcal{O}_2^{(9)}$	$\bar{S}_1 \in (\bar{3}, 1, -2/3)$	$\tilde{V}_2 \in (\bar{3}, 2 - 1/6)$	$E'_{L,R} \in (1, 1, -1)$	••••
$\mathcal{O}_{3}^{(9)}$	$\tilde{R}_2 \in (3, 2, 1/6)$		$\Psi_{L,R} \in (1, 2 - 1/2)$	$S \in (1, 1, 0)$
$\mathcal{O}_{4}^{(9)}$	$\tilde{R}_2 \in (3, 2, 1/6)$	$S_1 \in (\bar{3}, 1, 1/3)$	$\Psi_{L,R} \in (1, 2 - 1/2)$	
$O_{\overline{d}uLLD}^{(7)}$	$\tilde{V}_2\!\in\!(\bar{3},2-1/6)$		$\Psi_{L,R} \in (1, 2, -1/2), \ d'_{L,R} \in (3, 1, -1/3)$	$S\!\in\!(1,1,0)$

SMEFT operator  $\mathcal{O}_{\overline{d}uLLD}^{(7)}$  [28]. The Wilson coefficient  $\mathcal{C}_{\overline{d}uLLD}^{(7)}$  obtained by integrating out heavy fields at oneloop level is suppressed by the loop factor  $1/(16\pi^2)$ ; thus, it is expected to be comparable to the Wilson coefficients of the dim-9 SMEFT operators  $\mathcal{O}_i^{(9)}$  (i = 1, ..., 4) if they are obtained at tree level in UV models with the LNV scale  $\Lambda \sim 4\pi v$ .

Moreover, the dim-9 SMEFT operator  $\mathcal{O}_1^{(9)}$  can be realized in the LRSM from the exchange of both leftand right-handed W bosons [8,11,24]. As mentioned in Sec. I, such contribution is suppressed by the right-handed W boson mass. Besides,  $\mathcal{O}_4^{(9)}$  could originate from the exchange of charged scalars, which was considered in the LRSM [37]. This is easily verified if one converts  $\mathcal{O}_4^{(9)}$  into the following SMEFT operator in the basis of Ref. [17]:

$$\mathcal{O}_{dQQuLL2}^{(9)} = \epsilon^{ij} (\bar{d}^{\alpha} Q_i^{\beta}) (\bar{Q}^{\beta} u^{\alpha}) (\bar{L}^c L_j)$$
(14)

using the Fierz identities. However, such a physical scenario is severely constrained by the charged lepton-flavor-violating searches [7,24].

In the following, we will study possible UV completions with the LQs that are weakly constrained. In Table I, the new fields we introduce are listed, and their interactions with the SM fields are given for each case.

#### A. Dim-9 SMEFT operator: $\mathcal{O}_1^{(9)}$

First, we consider a UV model with the following interactions as the explicit completion of  $\mathcal{O}_1^{(9)}$ :

$$\mathcal{L} \supset \lambda_{ed}(\bar{d}_R \gamma_\mu e_R) U_1^\mu + \lambda_{u\Psi} \tilde{R}_2^* \bar{u}_R^c \Psi_R + \lambda_{DH} U_1^{\mu\dagger} \tilde{R}_2 \epsilon(iD_\mu H) + f_{\Psi e} \bar{\Psi}_L H e_R + \text{H.c.}, \quad (15)$$

where "H.c." represents the Hermitian conjugate terms. A scalar LQ field  $\tilde{R}_2$ , a vector LQ field  $U_1$ , and vectorlike fermions  $\Psi_L$  and  $\Psi_R$  with opposite chirality are introduced with the quantum number being specified in Table I. The vectorlike fermion doublets are expressed as

$$\Psi_L = \binom{N_L}{E_L}, \qquad \Psi_R = \binom{N_R}{E_R}. \tag{16}$$

The kinetic and mass terms are omitted here, and discussion on the mixing of lepton fields is given in Appendix A.

After integrating out the heavy fields  $U_1$ ,  $\tilde{R}_2$ , and  $\Psi = (\Psi_L, \Psi_R)$  at tree level, we obtain the dim-9 SMEFT operator  $\mathcal{O}_1^{(9)}$  (cf. Fig. 1) with the Wilson coefficient

$$\frac{C_1^{(9)}}{\Lambda^5} = i \frac{\lambda_{ed} \lambda_{u\Psi} \lambda_{DH} f_{\Psi e}}{m_U^2 m_R^2 m_{\Psi}},$$
(17)

where  $m_U$ ,  $m_R$ , and  $m_{\Psi}$  denote the masses of  $U_1$ ,  $\tilde{R}_2$ , and  $\Psi$ , respectively.

If all of the couplings in Eq. (15) are nonvanishing,  $\lambda_{ed}\lambda_{u\Psi}\lambda_{DH}f_{\Psi e} \neq 0$ , there is  $\Delta L = 2$  lepton number violation, and vice versa. To see it, following Ref. [23] we consider a fictitious lepton number  $U(1)_L$  under which the fields are charged and the couplings are treated as spurions to make the Lagrangian in Eq. (15) invariant. Let  $q(U_1) = r$ ,  $q(\tilde{R}_2) = s$ , and  $q(\Psi) = t$ ; we have  $q(\lambda_{ed}) = -(r+1)$ ,  $q(\lambda_{u\Psi}) = s - t$ ,  $q(\lambda_{DH}) = r - s$ , and  $q(f_{\Psi e}) = t - 1$ , which implies that  $q(\lambda_{ed}\lambda_{u\Psi}\lambda_{DH}f_{\Psi e}) = -2$ .

## **B.** Dim-9 SMEFT operator: $\mathcal{O}_2^{(9)}$

Then we introduce a UV model as an explicit completion of  $\mathcal{O}_2^{(9)}$  with the interactions as follows:

$$\mathcal{L} \supset f_{LE}(\bar{L}E_{R}')H + \lambda_{DH}(iD_{\mu}H)^{\dagger}\tilde{V}_{2}^{\mu}\bar{S}_{1}^{*} + \lambda_{Ed}(\bar{E}_{L}'d_{R})\bar{S}_{1} + \lambda_{Lu}(\bar{L}\gamma_{\mu}u_{R}^{c})\epsilon\tilde{V}_{2}^{\mu\dagger} + \text{H.c.}, \quad (18)$$

FIG. 1. Feynman diagram for the UV completion of  $\mathcal{O}_1^{(9)}$ .



FIG. 2. Feynman diagram for the UV completion of  $\mathcal{O}_2^{(9)}$ .

where the new fields we introduce are vectorlike fermions  $E'_L$  and  $E'_R$ , a scalar LQ  $\bar{S}_1$ , and a vector LQ  $\tilde{V}_2$ , which are specified in Table I.

After integrating out the heavy fields at tree level (cf. Fig. 2.), we can obtain the operator  $\mathcal{O}_2^{(9)}$  with the Wilson coefficient

$$\frac{\mathcal{C}_2^{(9)*}}{\Lambda^5} = -i \frac{f_{LE} \lambda_{Ed} \lambda_{DH} \lambda_{Lu}}{m_{E'} m_{\tilde{\varsigma}_{*}}^2 m_V^2}.$$
(19)

The condition  $f_{LE}\lambda_{Ed}\lambda_{DH}\lambda_{Lu} \neq 0$  implies lepton number violation as the case of  $\mathcal{O}_1^{(9)}$ .

## C. Dim-9 SMEFT operator: $\mathcal{O}_3^{(9)}$

The operators  $\mathcal{O}_1^{(9)}$  and  $\mathcal{O}_2^{(9)}$  involve the covariant derivative on the Higgs doublet  $D_{\mu}H$ , which can be generated directly after integrating out the heavy fields. The situation of the operator  $\mathcal{O}_3^{(9)}$  is different, as the mass dimension of  $D_{\mu}L$  is 5/2, so that it can emerge only from the kinematic terms of fermions.

An example UV completion of  $\mathcal{O}_3^{(9)}$  is given as follows:

$$\mathcal{L} \supset \lambda_{Ld}(\bar{L}d_R)\epsilon \tilde{R}_2^* + \lambda_{u\Psi}(\bar{\Psi}_R u_R^c) \tilde{R}_2 + f_{L\Psi}(\bar{L}\Psi_R)S + \mu(H^{\dagger}H)S^*, \qquad (20)$$

where a scalar LQ  $\tilde{R}_2$ , vectorlike fermions  $\Psi$ , and a real singlet scalar *S* are introduced, which are listed in Table I.

After integrating out the heavy fields at tree level (cf. Fig. 3), we can obtain the following effective interactions:

$$\mathcal{L}_{\text{eff}} \supset -\frac{\lambda_{Ld}\lambda_{u}\Psi f_{L}\Psi\mu}{m_{R_{2}}^{2}m_{\Psi}^{2}m_{S}^{2}}\epsilon_{ij}[(\bar{L}^{i}d_{R})(\bar{L}^{j}\gamma_{\mu}iD^{\mu}u_{R}^{c})(H^{\dagger}H) + (\bar{L}^{i}iD^{\mu}d_{R})(\bar{L}^{j}\gamma_{\mu}u_{R}^{c})(H^{\dagger}H) + (iD^{\mu}\bar{L}^{i}d_{R})(\bar{L}^{j}\gamma_{\mu}u_{R}^{c})(H^{\dagger}H)].$$
(21)

The covariant derivatives of the SM fields in Eq. (21) are tracked from the kinematic terms of the vectorlike fermions  $\Psi$ . The details are given in Appendix B. Since the covariant derivatives  $D^{\mu}u_{R}^{c}$  and  $D^{\mu}d_{R}$  do not involve the W boson and



FIG. 3. Feynman diagram for the UV completion of  $\mathcal{O}_3^{(9)}$ . The red dot labels the insertion of the covariant derivative.

would not generate  $0\nu\beta\beta$  decay at lower energies, only the third term is relevant. We label it as  $\mathcal{O}_3^{(9)\prime}$  with the coefficient

$$\frac{C_3^{(9)\prime}}{\Lambda^5} = -\frac{\lambda_{Ld}\lambda_u \Psi f_L \Psi \mu}{m_R^2 m_\Psi^2 m_S^2}.$$
(22)

Using the Fierz relations derived in Ref. [16], we can convert  $\mathcal{O}_3^{(9)\prime}$  into  $\mathcal{O}_3^{(9)}$ :

$$\mathcal{O}_3^{(9)\prime} = -i\mathcal{O}_3^{(9)\dagger} + \epsilon_{ij}(\bar{u}_R\gamma_\mu iD^\mu L^{ic})(\bar{L}^j d_R)(H^\dagger H).$$
(23)

Thus, the Wilson coefficient<sup>3</sup>

$$\frac{C_3^{(9)\prime}}{\Lambda^5} = i \frac{C_3^{(9)*}}{\Lambda^5}.$$
 (25)

Similarly, the condition of lepton number violation is  $\lambda_{Ld}\lambda_{u}\Psi f_{L}\Psi \mu \neq 0.$ 

## D. Dim-9 SMEFT operator: $\mathcal{O}_4^{(9)}$

Besides the LRSM mentioned before, the six-fermion operator  $\mathcal{O}_4^{(9)}$  can also be realized in the following UV model:

$$\mathcal{L} \supset \lambda_{Ld}(\bar{L}d_R)\epsilon \tilde{R}_2^* + \lambda_{u\Psi}(\bar{\Psi}_R u_R^c)\tilde{R}_2 + f_{\Psi S} S_1(\bar{Q}^c \epsilon \Psi_L) + f_{LQ}(\bar{L}\epsilon Q^c)S_1^* + \text{H.c.}, \quad (26)$$

where two scalar leptoquarks  $\tilde{R}_2$  and  $S_1$  and vectorlike fermions  $\Psi_L$  and  $\Psi_R$  with opposite chirality are introduced with the quantum number being specified in Table I. A similar model was introduced in Table 8 in Ref. [26] as the UV completion of the LEFT operator  $O_{4I}^{(9)}$ .

$$C_{4L}^{(9)}(m_W) = \frac{1}{2} V_{ud} \frac{v^5}{\Lambda^5} C_3^{(9)\prime}(m_W).$$
(24)

<sup>&</sup>lt;sup>3</sup>It is noted that in Eq. (23) the second term, which is redundant by using the equation of motion, also contributes to the Wilson coefficient of the LEFT operator  $O_{4L}^{(9)}$ . Thus, the matching condition at the scale  $\mu = m_W$  is



FIG. 4. Feynman diagram for UV completion of  $\mathcal{O}_4^{(9)}$ .

After integrating out the heavy fields at the tree level (cf. Fig. 4), we have

$$\mathcal{C}_4^{(9)} = -\frac{\lambda_{Ld}\lambda_u\Psi f_{\Psi S}f_{LQ}}{m_R^2 m_\Psi m_{S_1}^2},\tag{27}$$

and the condition for lepton number is  $\lambda_{Ld}\lambda_{u\Psi}f_{\Psi S}f_{LQ} \neq 0$ .

### E. Dim-7 SMEFT operator: $\mathcal{O}_{\bar{d}uLD}^{(7)}$

As obtained in Ref. [28], there is no tree-level UV completion of the dim-7 SMEFT operator  $O_{\bar{d}uLLD}^{(7)}$ . A possible one-loop realization is described by the following Lagrangian:

$$\mathcal{L} \supset \lambda_{Lu} (\bar{L}\gamma^{\mu} u_R^c) \epsilon \tilde{V}_{2\mu}^{\dagger} + \lambda_{\Psi d'} (\bar{\Psi}_R \gamma^{\mu} d_R') \tilde{V}_{2\mu} + f_{d'd} (\bar{d}_L' d_R) S + f_{L\Psi} (\bar{L}\Psi_R) S + \text{H.c.}, \qquad (28)$$

where we have introduced a vector LQ  $\tilde{V}_2 \in (\bar{3}, 2, -1/6)$ , vectorlike fermions  $\Psi_{L,R} \in (1, 2, -1/2)$  and  $d'_{L,R} \in (3, 1, -1/3)$ , and a real singlet scalar  $S \in (1, 1, 0)$ . The UV completion of the dim-7 SMEFT operator  $\mathcal{O}_{\bar{d}uLLD}^{(7)}$  is shown in Fig. 5. The covariant derivative is also tracked from the kinetic term of  $\Psi$  similar to the dim-9 SMEFT operator  $\mathcal{O}_3^{(9)}$ ; see more details in Appendix B.

Using the naive dimensional analysis [40–42], we can estimate the Wilson coefficient as

$$\mathcal{C}_{\bar{d}uLLD}^{(7)} \sim \frac{1}{(4\pi)^2} \lambda_{Lu} \lambda_{\Psi d'} f_{d'd} f_{L\Psi}.$$
 (29)



FIG. 5. Feynman diagram for the UV completion of  $\mathcal{O}_{duLLD}^{(7)}$ . The red dot labels the insertion of the covariant derivative.

Similarly,  $\lambda_{Lu}\lambda_{\Psi d'}f_{d'd}f_{L\Psi} \neq 0$  implies lepton number violation.

We have some general discussions on the UV models introduced. Different from the previous studies, which either match the known UV theories (such as the LRSM) with the effective operators or construct the UV models based on the topologies of the LEFT operators, our approach in two steps enables new UV completions, which have not been investigated before. Besides, in all of these UV models, the neutrino masses firstly arise at *n*-loop level with n = 2, 3, 4, which are negligible as we show in Appendix C. As we have discussed, the contributions of dim-7 and dim-9 SMEFT operators to  $0\nu\beta\beta$  decay are comparable; thus, in order to diagnose the mechanism of  $0\nu\beta\beta$  decay, we need other complementary probes and to search for the UV resonances in the UV models.

Thus, in the following sections, we will investigate the sensitivities to the mass and couplings of the UV resonances in  $0\nu\beta\beta$  decay and at the LHC. For simplicity, we will assume that all couplings are real and positive.

#### ΙΥ. Ονββ DECAY

In the EFT framework, the inverse half-life of  $0\nu\beta\beta$  decay can be expressed as [8]

$$(T_{1/2}^{0\nu})^{-1} = g_A^4 [G_{01}(|\mathcal{A}_L|^2 + |\mathcal{A}_R|^2) -2(G_{01} - G_{04}) \operatorname{Re} \mathcal{A}_L^* \mathcal{A}_R], \qquad (30)$$

and the amplitude is

$$\mathcal{A}_{X} = \frac{1}{2m_{e}v} C_{\pi\pi X}^{(9)} \sum_{i=GT,T} \left( \frac{1}{2} M_{i,sd}^{AP} + M_{i,sd}^{PP} \right), \quad (31)$$

$$C_{\pi\pi X}^{(9)} = -g_4^{\pi\pi} C_{4X}^{(9)} - g_5^{\pi\pi} C_{5X}^{(9)}, \qquad (32)$$

where X = L, R,  $g_A = 1.27$ , and the Wilson coefficients  $C_{4X}^{(9)}$  and  $C_{5X}^{(9)}$  are evaluated at  $\mu = 2$  GeV. The low-energy constants  $g_4^{\pi\pi} = -1.9 \text{ GeV}^2$  and  $g_5^{\pi\pi} = -8.0 \text{ GeV}^2$  [43]. For <sup>136</sup>Xe, the phase-space factor  $G_{01} = 1.5 \times 10^{-15} \text{ yr}^{-1}$ , and the nuclear matrix elements using the quasiparticle random-phase approximation are [8,44]

$$M_{GT,sd}^{AP} = -2.8, \qquad M_{GT,sd}^{PP} = 1.06, M_{T,sd}^{AP} = -0.92, \qquad M_{T,sd}^{PP} = 0.36.$$
(33)

It should be noted that the pion-exchange neutrino potential scales as  $1/\mathbf{q}^2$  at large  $|\mathbf{q}|$  with  $\mathbf{q}$  being the momentum transfer [8]. As a result, the amplitude of  $0\nu\beta\beta$  decay is UV divergent [45]. To absorb this divergence, the short-range *NNNee* contact interaction needs to be promoted to leading order [45,46], which is of the same



FIG. 6. Sensitivities to the LNV scale  $\Lambda$  in the  $0\nu\beta\beta$  decay experiments for the new physics couplings  $g_{\rm NP} = 0.2$  (red) or 0.5 (blue). The solid and dashed black lines correspond to limits given by KamLAND-Zen and future tonne-scale experiments, respectively.

order as nonderivative  $\pi\pi ee$  interaction [8]. In this work, we use the amplitude  $\mathcal{A}_X$  in Eq. (31) to provide an estimate of the  $0\nu\beta\beta$  decay rate.

Currently, the most stringent constraint on the  $0\nu\beta\beta$  decay is given by the KamLAND-Zen experiment,  $T_{1/2}^{0\nu} > 2.3 \times 10^{26}$  yr at 90% confidence level (CL) [47]. The future tonne-scale experiments are expected to improve the sensitivity to the half-life by about 2 orders of magnitude  $\sim 10^{28}$  yr; see Ref. [48] and references therein.

As an estimate, we consider the sensitivities to the LNV scale  $\Lambda \equiv m_R = m_U = m_{\Psi}$  assuming two benchmark values of the new physics couplings  $g_{\rm NP} \equiv \lambda_{ed} = \lambda_{u\Psi} = \lambda_{DH} = f_{\Psi}$  in the UV model for  $\mathcal{O}_1^{(9)}$  in KamLAND-Zen and future tonne-scale  $0\nu\beta\beta$  decay experiments. From Fig. 6, we find that the ongoing  $0\nu\beta\beta$  decay experiments are able to reach the LNV scale  $\Lambda \sim 2-3$  or 4–5 TeV for  $g_{\rm NP} = 0.2$  or 0.5, respectively. Given the existing constraints on the masses and couplings [32,49,50], we obtain that the sensitivities to the masses of UV resonances could be probed directly in the LHC searches.



FIG. 7. Diagrams for the cascade decays of LQs. The labels  $P_1, \ldots, P_7$  denote the possible particles in the chain, and  $\bar{P}_1$  is the antiparticle of  $P_1$ . All particles are specified in Table II.

TABLE II. The decays of LQs in UV models for the SMEFT operators  $\mathcal{O}_1^{(9)}$ ,  $\mathcal{O}_2^{(9)}$ , and  $\mathcal{O}_3^{(9)}$  in Eq. (8).

Operator	$P_1$	$P_2$	$P_3$	$P_4$	$P_5$	$P_6$	<i>P</i> <sub>7</sub>
$\overline{\mathcal{O}_{1}^{(9)}}$	$\tilde{R}_{2}^{-1/3}$	$W^-$	$U_{1}^{2/3}$	$e^+$	d	$e^+$	ū
1	$U_1^{-2/3}$	$W^-$	$ ilde{R}_2^{+1/3}$	$e^+$	ū	$e^+$	d
$\mathcal{O}_{2}^{(9)}$	$\bar{S}_{1}^{-2/3}$	$W^-$	$\tilde{V}_{2}^{1/3}$	$e^+$	ū	$e^+$	d
2	$\tilde{V}_{2}^{-1/3}$	$W^-$	$\bar{S}_{1}^{2/3}$	$e^+$	d	$e^+$	ū
${\cal O}_{3}^{(9)}$	$\tilde{R}_2^{-2/3}$	ū	$\Psi^0$	$e^+$	$W^{-}$	$e^+$	d

#### V. LHC SEARCHES

In this section, we will study the LHC searches for the UV resonances in the models discussed in Sec. III. The LQs are mainly produced in pairs, which subsequently decay into the SM quarks, leptons, or other new particles. Because of the lepton number violation, we can achieve the same-sign dilepton (SSDL) signature with a pair of same-sign electrons and at least two jets in the final state. For previous studies of lepton number violation in the final state of muon(s) in other contexts, see Refs. [51–55].

In Fig. 7 and Table II, we show the processes  $pp \rightarrow e^{\pm}e^{\pm}jjW^{\pm}$  with *j* denoting a quark or antiquark at the parton level in the UV models for the SMEFT operators  $\mathcal{O}_1^{(9)}$ ,  $\mathcal{O}_2^{(9)}$ , and  $\mathcal{O}_3^{(9)}$ .<sup>4</sup> Interestingly, the *W* boson, which comes from the decay of heavy particles due to the covariant derivative interaction, is unique in the two-step UV completions we consider.

The pair production of LQs at the LHC is dominated by the gluon fusion  $gg \rightarrow LQ + \overline{LQ}$ . The cross section of  $pp \rightarrow LQ + \overline{LQ}$  is expressed as

$$\sigma_{\rm LQ} = K \int \frac{d\hat{s}}{s} \int_{\tau}^{1} \frac{dx}{x} f_{g/p}(x) f_{g/p}\left(\frac{\tau}{x}\right) \hat{\sigma}_{\rm LQ}, \quad (34)$$

where  $\sqrt{\hat{s}}$  is the center-of-mass (c.m.) energy of the parton subprocess,  $\sqrt{s}$  is the c.m. colliding energy,  $f_{g/p}$  denotes the parton distribution function for the gluon in a proton, and  $\tau \equiv \hat{s}/s$ . The leading-order cross sections at parton level  $\hat{\sigma}_{LO}$  is [56,57]

$$\hat{\sigma}_{LQ} = \frac{\alpha_s^2 \pi}{96\hat{s}} \left[ \beta (41 - 31\beta^2) + (18\beta^2 - \beta^4 - 17) \ln \frac{1 + \beta}{1 - \beta} \right]. \quad (35)$$

<sup>&</sup>lt;sup>4</sup>The SSDL process can also be achieved in the UV model for  $\mathcal{O}_4^{9)}$  with a different topology of the decay channels, similar to that in Ref. [23]. On the other hand, it is difficult to generate the SSDL process in the model for  $\mathcal{O}_{duLLD}^{(7)}$ .



FIG. 8. Left:  $\hat{\sigma}_{LQ}$  in arbitrary unit (arb. units) with  $\sqrt{\hat{s}} = 3$ , 5 TeV for different masses of LQ. Right:  $\sigma_{LQ}$  with  $\sqrt{s} = 13$ , 14, and 27 TeV for different masses of LQ.

Here,  $\beta \equiv \sqrt{1 - 4m_{LQ}^2/\hat{s}}$ . In Eq. (34), the *K* factor is included to parametrize the next-to-leading-order QCD corrections [39,58,59].

The partonic cross section  $\hat{\sigma}_{LQ}$  and hadronic cross section  $\sigma_{LQ}$  are illustrated in Fig. 8. In the left panel, two benchmark values of the partonic energy  $\sqrt{\hat{s}}$  are chosen. In both scenarios,  $\hat{\sigma}_{LQ}$  drops rapidly with the increase of LQ mass dubbed  $m_{LQ}$ . Besides, for  $m_{LQ} \gtrsim 1.8$  TeV, the increase of  $\sqrt{\hat{s}}$  from 3 to 5 TeV can significantly enhance the gluon-fusion subprocess of LQ pair production. In the right panel, we can see that  $\sigma_{LQ} \simeq 1.5 \times 10^{-2}$  fb at  $\sqrt{s} = 13$  TeV, while  $\sigma_{LQ}$  reaches about 2 fb at  $\sqrt{s} = 27$  TeV. From Fig. 8, we find that, in order to search for LQ with its mass around 2 TeV or heavier, it would be critical and effective to improve the colliding energy.

There have been extensive searches for the SSDL signature at the 13 TeV LHC in the benchmark models of supersymmetric particles [60,61] or heavy Majorana neutrinos [25,62–65] with null results, which can be reinterpreted as searches for the UV resonances of the  $0\nu\beta\beta$ -decay-related operators. Besides, we will consider SSDL searches at the high-luminosity LHC (HL-LHC) with  $\sqrt{s} = 14$  TeV and the proposed high-energy upgrade (HE-LHC) with  $\sqrt{s} = 27$  TeV.

As a case study, we will consider the process  $pp \rightarrow \tilde{R}_2^{1/3} \tilde{R}_2^{-1/3}$  and the decay chains in the first row in Table II, where the leptoquark  $U_1$  and W boson are on the shell. The partial decay widths are

$$\Gamma(\tilde{R}_2^{-1/3} \to U_1^{2/3} + W^-) = \frac{\beta(m_R^2, m_U^2, m_W^2)}{64\pi m_R^3 m_U^2} \lambda_{DH}^2$$
(36)

$$\times \left[ (m_R^2 - m_U^2 - m_W^2)^2 + 8m_U^2 m_W^2 \right], \quad (37)$$

where  $\beta(x, y, z) \equiv [(x - y - z)^2 - 4yz]^{1/2}$  and

$$\Gamma(\tilde{R}_2^{-1/3} \to u + e^-) = \frac{\lambda_{u\Psi}^2 \sin^2 \theta}{16\pi} m_R.$$
 (38)

The mixing angle  $\theta$  is defined as

$$\sin\theta = \frac{f_{\Psi_e}v}{\sqrt{2}m_{\Psi}},\tag{39}$$

which is convenient for the phenomenological study; see Appendix A for more discussions. In the model for  $\mathcal{O}_1^{(9)}$ ,  $U_1^{2/3}$  can decay only into  $e^+$  and d. Thus, the cross section of the signal  $pp \to e^{\pm}e^{\pm}jjW^{\mp}$  at the parton level is expressed as

$$\sigma_s = 2\sigma_{\rm LO} \times \mathcal{B}_1 \times \mathcal{B}_2,\tag{40}$$

where *j* denotes a quark or antiquark,  $\mathcal{B}_1$  and  $\mathcal{B}_2$  are the branching rations of  $\tilde{R}^{-1/3} \rightarrow U_1^{2/3} + W^-$  and  $\tilde{R}^{1/3} \rightarrow \bar{u} + e^+$ , respectively, and the *W* boson can decay hadronically or leptonically.

As an estimate, taking  $m_R = 2$  TeV and  $m_U = 1.8$  TeV, we obtain

$$\frac{\mathcal{B}_2}{\mathcal{B}_1} \simeq \left(\frac{\sin\theta}{0.05} \frac{\lambda_{u\Psi}}{\lambda_{DH}}\right)^2. \tag{41}$$

If  $\sin \theta = 0.05$ , the coupling and mass of  $\tilde{R}_2$  is  $f_{\Psi e}/m_{\Psi} \simeq 1/(3.5 \text{ TeV})$ .

The main SM backgrounds of SSDL searches include prompt backgrounds WW, WZ, and ZZ, jet fake backgrounds from  $j \rightarrow e$ , and charge flip backgrounds from the misidentification of electron charge. We find that the selection criteria in the search for heavy Majorana neutrino at the LHC run 2 with the integrated luminosity of 139 fb<sup>-1</sup> in the resolved channel [25] are suitable for our signal. The signal events are generated using MadGraph5\_aMC@NLO [66], which are passed to PYTHIA8 [67] and DELPHES3 [68] for parton shower and detector simulation, respectively. A pair of same-sign electrons and at least two jets are selected if [25]

$$p_T^{e^{1(2)}} > 40(25) \text{ GeV}, \qquad |\eta_e| < 2.47,$$
  
 $p_T^j > 100 \text{ GeV}, \qquad |\eta_j| < 2.5,$  (42)

where  $p_T^{e1}$ ,  $p_T^{e2}$ , and  $p_T^j$  are the transverse momenta of the leading and subleading electrons and jets, respectively, and  $\eta_e$  and  $\eta_j$  are their pseudorapidities.

The  $m_{ee}$  and  $H_T$  distributions of the signal after the cuts in Eq. (42) are displayed in Fig. 9, where  $m_R = 2$  TeV and  $m_U = 1.8$  TeV are assumed. We can see that the signal has large  $m_{ee}$  and  $H_T$ , which is reasonable due to heavy resonances  $\tilde{R}_2$  and  $U_1$ .

In the ATLAS analysis [25], the cut invariant mass of electron pair  $m_{ee} > 400$  GeV and the scalar sum of the transverse momenta of electrons and two most energetic jets  $H_T > 400$  GeV are further imposed to reduce the SM



FIG. 9. Kinematic distributions of the signals at the LHC run 2, HL-LHC, and HE-LHC with  $\sqrt{s} = 13$ , 14, and 27 TeV, respectively, after passing the selection cuts in Eq. (42).

backgrounds. About 40 background events are left, which can be counted in the  $H_T$  distribution in Fig. 5(b) in Ref. [25], which also indicates less than one SM background event for  $H_T > 1.6$  TeV.

In order to reject most of the SM backgrounds, we require a harder cut  $H_T > 3$  TeV for the searches at the 13 TeV LHC run 2, 14 TeV HL-LHC, and 27 TeV HE-LHC. The corresponding signal selection efficiencies after passing the selection cuts and this optimized cut are  $\epsilon_s = 0.29, 0.30, \text{ and } 0.32$ , respectively. We emphasize that a more delicate analysis with a stronger cut on  $m_{ee}$  can also be used to effectively remove the small SM backgrounds with less impact on the signals.

The number of signal events after passing all cuts is

$$n_s = \sigma_s \epsilon_s \mathcal{L},\tag{43}$$

where  $\sigma_s$  is the signal cross section obtained in Eq. (40) and  $\mathcal{L}$  denotes the integrated luminosity. We obtain that  $n_s$  is smaller than 1 at the LHC run 2, implying that current SSDL searches at still weak to constrain the LNV parameters for the UV model we discuss.

The 95% CL exclusion limit in the case of no SM background is evaluated by requiring that the number of signal events  $n_s = 3$  [69,70]. In the next section, we will consider the exclusion limits that could be obtained at the HL-LHC and HE-LHC.

#### VI. RESULTS AND DISCUSSIONS

In this section, we study the complementary searches for the UV resonances in the models in  $0\nu\beta\beta$  decay and LHC. For illustration, the sensitivities on the model for  $\mathcal{O}_1^{(9)}$  will be compared. From Eqs. (17) and (39), the square root of the inverse half-life

$$(T_{1/2}^{0\nu})^{-1/2} \propto \frac{\lambda_{ed}\lambda_{DH}\lambda_{u\Psi}\sin\theta}{m_U^2 m_R^2}.$$
 (44)

The signal cross section depends on the masses via the LQ pair production and the decay branching ratios. Taking

 $m_R = 2$  TeV and  $m_U = 1.8$  TeV, we have that the square root of the signal cross section

$$\sigma_s^{1/2} \propto \frac{\lambda_{DH} \lambda_u \Psi \sin \theta}{(\sin \theta \lambda_u \Psi)^2 + (0.05 \lambda_{DH})^2}.$$
 (45)

From Eqs. (44) and (45), we can see that the signal process at the LHC is insensitive to the parameter  $\lambda_{ed}$ , while both the signal cross section and the  $0\nu\beta\beta$  decay rate are suppressed by the mixing angle  $\sin\theta$ . The dependence on  $\lambda_{u\Psi}$  and  $\lambda_{DH}$  implies that  $0\nu\beta\beta$  decay and LHC searches have different sensitivities to the parameters.

In Fig. 10, we show the combined sensitivities to the couplings  $\lambda_{u\Psi}$  and  $\lambda_{DH}$  in the KamLAND-Zen and future tonne-scale  $0\nu\beta\beta$  decay experiments as well as at the HL-LHC and HE-LHC. The red regions are excluded by the  $0\nu\beta\beta$  decay search in the KamLAND-Zen experiment at 90% CL, while the blue regions are expected to be excluded by the SSDL searches at the HL-LHC with the integrated luminosity of  $\mathcal{L} = 3$  ab<sup>-1</sup> at 95% CL. The slash shading regions in red and blue denotes those that can be further excluded in future tonne-scale  $0\nu\beta\beta$  decay experiments and HE-LHC with  $\mathcal{L} = 3$  ab<sup>-1</sup>, respectively.

We fix the masses of LQs as  $m_R = 2$  TeV and  $m_U = 1.8$  TeV and assume that  $m_{\Psi} > m_R$ . Four benchmark scenarios that satisfy the existing constraints [32,50] are considered: (a)  $\sin \theta = 0.05$ ,  $\lambda_{ed} = 0.2$ ; (b)  $\sin \theta = 0.01$ ,  $\lambda_{ed} = 0.2$ ; (c)  $\sin \theta = 0.05$ ,  $\lambda_{ed} = 0.1$ ; and (d)  $\sin \theta = 0.01$ ,  $\lambda_{ed} = 0.1$ .

In all of the scenarios, searches for the UV resonances the LQs  $\tilde{R}_2$  and  $U_1$ —in the  $0\nu\beta\beta$  decay and at the LHC are



FIG. 10. The sensitivities in the plane of  $\lambda_{u\Psi}$  and  $\lambda_{DH}$  of KamLAND-Zen (red) and tonne-scale (red slash shading)  $0\nu\beta\beta$  decay and SSDL searches at the HL-LHC (blue) and HE-LHC (blue slash shading). See the text for more details.

complementary to each other. Besides, we can see that the sensitivities of the high-energy upgrade of the LHC, i.e., HE-LHC, are much improved compared to the HL-LHC, because the cross section of LQ production increases significantly at the HE-LHC.

From Figs. 10(a) and 10(c), most of the parameter space is in the reach of HE-LHC and tonne-scale  $0\nu\beta\beta$  decay experiments if  $\sin\theta = 0.05$  or, equivalently,  $f_{\Psi e}/m_{\Psi} \simeq 1/(3.5 \text{ TeV})$ . For a larger  $m_{\Psi}$  or smaller  $f_{\Psi e}$ , both the sensitivities of LHC and  $0\nu\beta\beta$  decay experiments are reduced. In this case, the HE-LHC and tonne-scale  $0\nu\beta\beta$ experiments are crucial to probe the couplings of the LQs, as seen in Figs. 10(b) and 10(d). In the comparison of Figs. 10(a) and 10(c) as well as 10(b) and 10(d), the reaches of  $0\nu\beta\beta$  decay searches are sensitive to the coupling  $\lambda_{ed}$ ; thus, it can be constrained alongside with  $\lambda_{u\Psi}$  and  $\lambda_{DH}$ .

Finally, we comment that if the LQs have larger masses, the sensitivities of  $0\nu\beta\beta$  decay searches are less impacted compared to the LHC searches, because the cross section of LQ pair production drops rapidly with the increase of the LQ mass, as clearly shown in Fig. 8. The interplay for other choices of  $m_R$  and  $m_U$  or in the UV models for  $\mathcal{O}_2^{(9)}$  and  $\mathcal{O}_3^{(9)}$  can be studied analogously.

#### VII. CONCLUSION

In this work, we have investigated the two-step UV completions of the effective operators that give rise to chirally enhanced contributions to  $0\nu\beta\beta$  decay. There are one dim-7 and four dim-9 SMEFT operators that can be matched to the  $\Delta L = 2$  quark-lepton  $O_{4X}^{(9)}$  with X = L or R. We have introduced possible UV completions for each of the relevant SMEFT operators with the LQs and studied the searches for the UV resonances at the LHC.

In order to illustrate the complementarities of  $0\nu\beta\beta$  decay and LHC searches, we study in detail the UV model for  $\mathcal{O}_1^{(9)}$ . Assuming the new physics couplings  $g_{\rm NP} = 0.2$  or 0.5 (weakly coupled), the  $0\nu\beta\beta$  decay experiments are sensitive to the LNV scale  $\Lambda \sim 2-3$  or 4–5 TeV, respectively. On the other hand, since the LQ production cross section is reduced significantly with the increase of the LQ mass, LHC run 2 is unable to constrain the related LNV parameters. We thus consider the same-sign dilepton searches for the process  $pp \rightarrow e^{\pm}e^{\pm}jjW^{\mp}$  at the highluminosity LHC and high-energy LHC with the integrated luminosities of 3 ab<sup>-1</sup>.

We obtain that the direct searches at the HL-LHC and HE-LHC and indirect searches in the KamLAND-Zen and future tonne-scale  $0\nu\beta\beta$  decay experiments are complementary to each other in testing the UV completions of the relevant SMEFT operators. Thus, possible  $0\nu\beta\beta$  decay signals from chirally enhanced mechanisms can be diagnosed with the LHC searches.

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#### **APPENDIX A: MIXING OF LEPTON FIELDS**

In this appendix, the mixing of the SM lepton and vectorlike fermion fields will be discussed. For illustration, we consider the UV model for  $\mathcal{O}_1^{(9)}$ . The mass terms of vectorlike fermions and the mixing with the SM lepton fields via the Yukawa interactions are given by

$$\mathcal{L} \supset y_e \bar{L} H e_R + f_{\Psi e} \bar{\Psi}_L H e_R + m_{\Psi} \bar{\Psi}_L \Psi_R + \text{H.c.}, \quad (A1)$$

where a mass term  $\overline{\Psi}_R L$  can be rotated away [21,71].

After the Higgs field develops a vacuum expectation value, we can obtain the mass terms of the charged leptons as follows:

$$\mathcal{L}_{m_e} = (\bar{e}_L, \quad \bar{E}_L) \mathcal{M}_e \begin{pmatrix} e_R \\ E_R \end{pmatrix}, \tag{A2}$$

where the mass matrix is given by

$$\mathcal{M}_e = \frac{1}{\sqrt{2}} \begin{pmatrix} y_e v & 0\\ f_{\Psi e} v & \sqrt{2}m_{\Psi} \end{pmatrix}.$$
 (A3)

The mass matrix  $\mathcal{M}_e$  can be diagonalized to yield mass eigenstates of charged fermions labeled by  $e'_R$  and  $E'_R$ , which are expressed as

$$e'_{R} = \cos \theta e_{R} - \sin \theta E_{R},$$
  

$$E'_{R} = \sin \theta e_{R} + \cos \theta E_{R},$$
(A4)

respectively, where we define  $\sin \theta = f_{\Psi e} v / (\sqrt{2}m_{\Psi})$ .

The interactions between the vectorlike fermions and the Higgs boson could modify the Higgs couplings [71,72], while the constraints depend on other possible heavy particles in the UV theories, the detailed study of which is beyond the scope of this work.

## APPENDIX B: SMEFT OPERATORS INVOLVING $D_{\mu}L$

As mentioned in Sec. III, the covariant derivatives of the SM fields are tracked from the kinematic terms of  $\Psi$ . In the



FIG. 11. Feynman diagram for the UV completion of  $\mathcal{O}_3^{(9)}$  with the vectorlike fermions and *W* boson being specified.



FIG. 12. Feynman diagram for the UV completion of  $\mathcal{O}_{duLLD}^{(7)}$  with the vectorlike fermions, colored fermion, and *W* boson being specified.

following, we will explain how to obtain the SMEFT operators in Eq. (21).

From the interactions in Eq. (20), we can solve the classical equation of motions (EOMs) for the heavy fields. Since there are several fields, one can first integrate one and then the others. By using the EOMs, we have

$$\Psi_{R} = -\frac{1}{m_{\Psi}^{2}} i \mathcal{D}(\lambda_{u\Psi} u_{R}^{c} \tilde{R}_{2} + f_{L\Psi} LS^{*})$$
  
$$= \frac{1}{m_{\Psi}^{2}} i \mathcal{D} \left[ -\frac{\lambda_{u\Psi} \lambda_{Ld}}{m_{R}^{2}} u_{R}^{c} (\epsilon \bar{L} d_{R}) + \frac{f_{L\Psi} \mu}{m_{S}^{2}} L(H^{\dagger} H) \right]. \quad (B1)$$

After combining the two terms on the right-hand side, we can obtain the effective interactions in Eq. (21).

In the diagrammatic approach, the SMEFT operator  $\mathcal{O}_1^{(9)}$  can be generated by integrating out the heavy fields in Fig. 11, which is more specific than Fig. 2. The components of the vectorlike fermions  $\Psi$  with mass insertion are explicitly shown, and the *W* boson is attached. Similarly, the UV completion of the dim-7 SMEFT operator  $\mathcal{O}_{duLLD}^{(7)}$  is specified in Fig. 12.

#### **APPENDIX C: NEUTRINO MASSES**

As mentioned above, the UV models for the relevant SMEFT operators give negligible contributions to the



FIG. 13. Feynman diagram of the light neutrino Majorana masses in the UV model for  $\mathcal{O}_3^{(9)}$ .



FIG. 14. Feynman diagram of the light neutrino Majorana masses in the UV model for  $\mathcal{O}_1^{(9)}$ .

neutrino masses. To see it, we draw the corresponding Feynman diagrams of the light neutrino Majorana masses and estimate their contributions.

The leading contribution to Majorana masses in the UV model for  $\mathcal{O}_3^{(9)}$  is generated at the two-loop level, while those for  $\mathcal{O}_{1,2,4}^{(9)}$  and  $\mathcal{O}_{\bar{d}uLLD}^{(7)}$  are generated at the three-loop level.

In Fig. 13, we show Feynman diagram of the light neutrino mass in the UV model for  $\mathcal{O}_3^{(9)}$ . The contribution is estimated as

$$\begin{split} m_{\nu} &\sim \frac{m_u m_d v^2 \mu}{(16\pi^2)^2} \frac{\lambda_{Ld} \lambda_u \Psi f_{L\Psi}}{m_S^2 m_R^2 m_{\Psi}^2} \Lambda_{\rm UV}^2 \\ &\approx 2.8 \times 10^{-17} \mu \left(\frac{\Lambda_{\rm UV}}{1 \text{ TeV}}\right)^2 \left(\frac{1 \text{ TeV}}{\Lambda}\right)^6. \end{split} \tag{C1}$$

Here,  $\Lambda_{\rm UV}$  is the UV cutoff  $\Lambda_{\rm UV} \sim \Lambda$ , and we have set  $\lambda_{Ld}\lambda_{u\Psi}f_{L\Psi} \equiv 1$  and  $\Lambda^6 = m_S^2 m_R^2 m_{\Psi}^2$  in the second line. We can see that  $m_{\nu}$  is negligible even for  $\mu \sim 1$  TeV.

In Fig. 14, we show Feynman diagram of the light neutrino mass in the UV model for  $\mathcal{O}_1^{(9)}$ , and those for  $\mathcal{O}_2^{(9)}$ ,  $\mathcal{O}_4^{(9)}$ , and  $\mathcal{O}_{duLLD}^{(7)}$  can be obtained analogously. In all of these cases, Majorana masses of light neutrinos generated at the three-loop level can be neglected.

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