Shape of CMB lensing in the early dark energy cosmology

Gen Ye[®], ^{1,*} Jun-Qian Jiang[®], ^{2,†} and Yun-Song Piao^{2,3,4,5,‡}

¹Institute Lorentz, Leiden University, P.O. Box 9506, Leiden 2300 RA, The Netherlands
²School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China
³School of Fundamental Physics and Mathematical Sciences, Hangzhou Institute for Advanced Study,
UCAS, Hangzhou 310024, China

⁴International Center for Theoretical Physics Asia-Pacific, Beijing/Hangzhou 100190, China ⁵Institute of Theoretical Physics, Chinese Academy of Sciences, P.O. Box 2735, Beijing 100190, China

(Received 19 June 2023; accepted 31 August 2023; published 12 September 2023)

Recently, the cosmological tensions, H_0 and S_8 in particular, have inspired modification of both pre- and postrecombination physics simultaneously. Early dark energy is a promising pre-recombination solution of the H_0 tension, known to be compatible with the cosmic microwave background (CMB). However, the compatibility of early dark energy, as well as general early resolutions, with the CMB is no longer obvious if the late Universe is also modified. Aside from cosmological parameters, the main channel through which late Universe physics affects CMB observables is gravitational lensing. We employed a new method of sampling functions using the Gaussian Process in the Monte Carlo Markov Chain analysis to constrain the shape of the CMB lensing potential. We obtained the early Universe (CMB) only constraints on the full shape of the CMB lensing potential, with the late-time Universe being marginalized over. It is found that CMB data prefers a lensing potential shape that is Λ CDM-like at $80 \lesssim L \lesssim 400$ but with enhanced amplitude beyond this range. The obtained shape constraints can serve as a CMB-compatibility guideline for both late and early Universe model building that modifies the lensing potential.

DOI: 10.1103/PhysRevD.108.063512

I. INTRODUCTION

One of the most important parameters in cosmology is the Hubble constant H_0 , which characterizes the expansion rate of our current Universe. It can be measured directly through the distance-redshift relation. Using the state-of-art Cepheid calibrated distance ladder approach, the SH0ES group reports $H_0 = 73.04 \pm 1.04$ km/s/Mpc [1]. On the other hand, in a given cosmological model H_0 calibrates the distance to the last scattering surface and can be derived from precise cosmic microwave background (CMB) measurements. The Planck satellite results yield $H_0 = 67.37 \pm$ 0.54 km/s/Mpc assuming ΛCDM [2], also confirmed by more recent ground CMB experiments [3,4]. The $> 4\sigma$ tension, usually dubbed the Hubble tension, between the locally measured H_0 and the CMB derived ones is one of the most significant challenges faced by current cosmology, which might be a hint of new physics beyond Λ CDM [5,6].

Among the plethora of models proposed to alleviate the Hubble tension, see, e.g., [7,8] for thorough reviews, a promising class of solutions is to introduce beyond Λ CDM modifications to the pre and near recombination evolution (early resolution), such as early dark energy (EDE) [9–24], see, e.g., [25,26] for recent reviews, early modified gravity [27–30], neutrino self-interaction [31,32], nonstandard recombination process [33–36], and modified physical constants at early times [37].

On the other hand, there is another possible tension between large scale structure (LSS) and CMB observations, characterized by $S_8 = \sigma_8 (\Omega_m/0.3)^{0.5}$, where σ_8 is the root-mean-square amplitude of the matter fluctuation in spheres of radius $8h^{-1}$ Mpc today. Planck CMB measurement reports $S_8 = 0.834 \pm 0.016$ with Λ CDM [2] while weak lensing measurements find lower values. The 3×2 pt analysis from KiDS-1000 obtains $S_8 = 0.766^{+0.020}_{-0.014}$ [38] and DES-Y3 obtains $0.779^{+0.014}_{-0.015}$ [39]. The most recent DES-Y3 + KiDS-1000 result, however, gives $S_8 = 0.790^{+0.018}_{-0.014}$ which is compatible with Planck at 1.7σ [40]. Many models that modify the evolution of the late Universe have been proposed to resolve this tension, see, e.g., [8,41] for recent reviews.

The S_8 tension not only affects the Λ CDM model, but also becomes a concern for EDE [42–44]. This tension is usually exacerbated in these early resolutions as a consequence of increased total matter energy density [45–48]. Recently there has been increasing interest in reconciling EDE with LSS by paring it with other possible mechanisms to alleviate the S_8 tension, many of which are nonnegligible in the post-recombination Universe, such as

ye@lorentz.leidenuniv.nl

[†]jiangjq2000@gmail.com

[‡]yspiao@ucas.ac.cn

axion dark matter [49,50], decaying dark matter [51], neutrino mass [52,53] and dynamics of the dark sector [20,52,54–58]. An immediate question follows is what information about EDE we could extract from the early Universe observations, i.e., CMB, independent of possible modification to the evolution of the Universe after recombination. Inversely, such constraints provide guidelines on how late modification should behave to maintain compatibility with CMB observations.

On the background level, many late time modifications can be marginalized by a time dependent dark fluid equation of state w(z) and it has been shown in both Λ CDM [2] and EDE [54,58] that a Λ CDM-like, i.e., $w \simeq -1$, post-recombination Universe is preferred. On the perturbation level, late time physics imprints itself in the CMB observation mainly through the late integrated Sachs-Wolfe (ISW) effect, scattering of CMB photon by the free electrons from reionization and gravitational lensing. It has been suggested that the CMB lensing information can be marginalized by, e.g., parametrization [59–64] and interpolation [65] in Λ CDM. In this paper, we employ a new method of sampling free functions in the Monte Carlo Markov Chain (MCMC) analysis. We draw our functions directly from a Gaussian process (GP) which is able to explore a wide range of function shapes while also requiring fewer parameters than the interpolation method. Using the new method, we build the CMB-only constraints on the shape of lensing in the EDE models, marginalizing over the late Universe evolution, see Fig. 1. We found that CMB data is most constraining on the shape of lensing in the multiple range $80 \lesssim L \lesssim 400$, where the constraints is compatible with Λ CDM prediction. Beyond this region, shape constraints deviate from Λ CDM prediction and seem to prefer higher amplitudes of the lensing potential spectrum on both low and high L parts, related to the possible preference for excess lensing-like smoothing in Planck CMB spectra (lensing anomaly) [2]. Due to the lensing B-mode, CMB B-mode data from BICEP/Keck [66] contributes non-trivial constraining power on the L > 400 tail of the lensing spectrum, see also Ref. [67]. Our results show that inclusion of the B-mode does not remove the preference for a higher lensing potential on the high-L tail, see Fig. 2.

In Sec. II we describe our sampling method and datasets. Section III reports the cosmological models studied and the corresponding results. We conclude in Sec. IV and group large plots and auxiliary details in the Appendixes.

II. METHODS AND DATASETS

In this paper we are interested mainly in the linear multiple range L < 3000 and reionization effects can be well captured by an effective optical depth $\tau_{\rm reion}$. In the high-l CMB data, there is a degeneracy between $\tau_{\rm reion}$ and the primordial scalar power spectrum amplitude A_s as $A_s e^{-2\tau_{\rm reion}}$. This degeneracy can be broken by the low-l E polarization data as well as lensing [69]. Reionization happens at very high redshift $z \gtrsim 6.5$ [70], on which late time dynamics relevant to LSS generally has marginal effect. Therefore, aside from cosmological parameters, the main interface between the free streaming CMB photons after

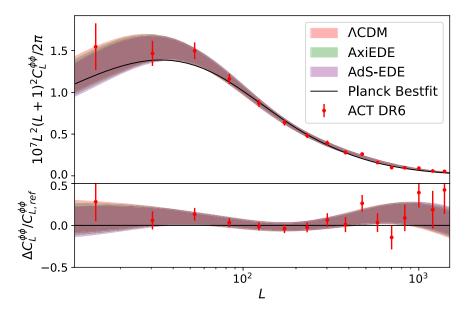


FIG. 1. Constraints on lensing spectra shape using the Planck CMB temperature and polarization data as well as Planck + ACT DR6 lensing measurement in the Λ CDM and EDE models. Shaded areas represent the 95% distribution of the lensing spectra. Solid black lines are the reference Λ CDM model from Planck2018 baseline bestfit [2]. Points with error bars are ACT DR6 [68] lensing bandpower in the extended multiple range. Following Ref. [68], only lensing data in the multiple range 40 < L < 1300 is used in the shape constraint, thus the left most two ACT data points do not contribute to the shape constraints. The derived shape constraints contain both information from the Planck + ACT lensing potential reconstruction and the lensed CMB temperature and polarization spectra.

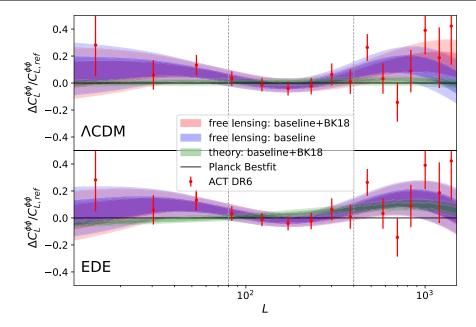


FIG. 2. Comparison between the baseline and baseline + BK18 68% and 95% constraints on free lensing shape in Λ CDM and AdS-EDE. The result for AxiEDE is similar to AdS-EDE, thus constraints are only plotted for one EDE model to simplify presentation. The reference model is the Λ CDM model from Planck2018 baseline bestfit [2]. Green constraints are produced by theory derived lensing potential. Dashed gray vertical lines indicate the multiple range 80 < L < 400.

recombination and possible post-recombination modifications relevant to LSS is the late ISW effect and gravitational lensing. The late ISW effect receives constraints from low-l TT spectrum where data is plagued by cosmic variance. Appendix B shows that it has marginal constraining power on details of the late-time physics by marginalizing over the overall strength $A_{\rm LISW}$ of the late ISW effect. Therefore, we assume standard late ISW contribution ($A_{\rm LISW}=1$) and only focus on the CMB lensing spectrum in this paper.

Instead of the theory lensing power spectrum $C_{L,\text{th}}^{\phi\phi}$ predicted by a model that describes the full post-recombination evolution, we use

$$C_L^{\phi\phi} = A(L)C_{L,\text{th}}^{\phi\phi} \tag{1}$$

to calculate the lensed temperature and polarization power spectra and fit to CMB data, where A(L) is a free function to be sampled from a GP, which can be thought of as a Gaussian distribution of functions $f(x) \sim \text{GP}[\bar{f}(x), K]$ with \bar{f} the mean function and K the kernel function ("covariant matrix"). We use the standard square exponential kernel $K(x_1, x_2) = \sigma^2 \exp(-\frac{|x_1 - x_2|^2}{2l^2})$, with correlation length l characterizing the smoothness of the function samples and σ being the uncertainty amplitude parameter with respect to the mean.

We use the Monte Carlo Markov Chain (MCMC) method to sample the parameter space. One problem is that the GP sampling process is purely random and receives no "guidance" from any MCMC likelihoods (data) thus

will severely affect convergence speed. To remedy this, we introduce a few nodes $\{X_i, A_i\}_{i \in I}$ where $X_i \equiv \log_{10} L_i$ are fixed multiple positions in log space and $A_i = A(L_i)$ are amplitudes at L_i , which are varied in the MCMC analysis. A(L) is then drawn from a conditional GP under the condition that the sampled function passes through these specified nodes. Formally, on any given finite set of multiples $\{L\}$ we define $X_L = \{\log_{10} L\}$, then the GP reduces to a conditional multivariate Gaussian distribution

$$A(L) \sim \mathcal{N}(\bar{A}(L), \Sigma)$$
 (2)

with

$$\bar{A}(L) = K(X_L, \mathsf{X}_i) K^{-1}(\mathsf{X}_i, \mathsf{X}_j) \mathsf{A}_j \tag{3}$$

$$\Sigma_{L_1L_2} = K(X_{L_1}, X_{L_2}) - K(X_{L_1}, \mathsf{X}_i) K^{-1}(\mathsf{X}_i, \mathsf{X}_j) K(\mathsf{X}_j, X_{L_2}), \tag{4}$$

where common subscripts are summed over. On one hand, nodes do not bias our function sampling because the amplitudes A_i are free to vary in the MCMC analysis. On the other hand, nodes aid convergence by shaping the mean function to the data-constrained direction. Moreover, unlike the standard interpolation method, GP still provides sufficient freedom for A(L) to vary even one fixes the nodes and amplitudes, which allows us to use much fewer nodes than standard interpolation. In principle, a large number of Gaussian realizations of A(L) is needed for the same cosmology to sample the function space as much as possible.

On the other hand, to perform the MCMC analysis over cosmological parameters, we cannot afford too much time at each cosmological step (i.e., the same cosmological parameters). As a compromise, in one cosmological step we oversample 2 sets of node amplitudes $\{A_i\}$ and test over 4 random samples of A(L) for each set of $\{A_i\}$, thus in total 8 realizations of A(L) are sampled in each cosmological step. Each sampled realization of A(L) is treated as a separate MCMC step with its acceptance into the chain depending on the usual MCMC criteria [71]. Increasing the oversampling number without heavily impacting the convergence speed has little effect on the final constraints. The MCMC sampling is performed using MontePython-3.5 [59,72], modified to implement the GP sampling method described above [73]. Cosmological background and perturbations are calculated using CLASS [74,75], modified to include the EDE models and recomputation of lensing [76]. The modification exposed the lensing module of CLASS so that it supports redoing the lensing computation only given input vector $A(L), L=2,3,...,L_{\max}$ with $A(0)=L_{\max}$ if cosmology keeps unchanged. For speed reasons, the actual vector drawn from GP is the values of A(L) evaluated at 40~L's log-evenly distributed in the multiple range $10 \le L \le 1500$, which is then interpolated to the full A(L). The corresponding values of $C_{L,\text{th}}^{\phi\phi}$ and A(L) at the 40~L's are output into the chain for every step, and posterior distributions of the product (1) of them will be later presented as the lensing shape constraint. Our baseline datasets include:

- (i) CMB T/E: CamSpec High-ℓ TTTEEE CMB likelihood [77] derived from the Planck PR4 NPIPE data [78]. Low-ℓ CMB TT (PR3) and EE (PR4) data from Planck [78,79].
- (ii) Lensing: The combined likelihood of ACT DR6 lensing and Planck NPIPE lensing with extended range (40 < L < 1300) [68,80,81].

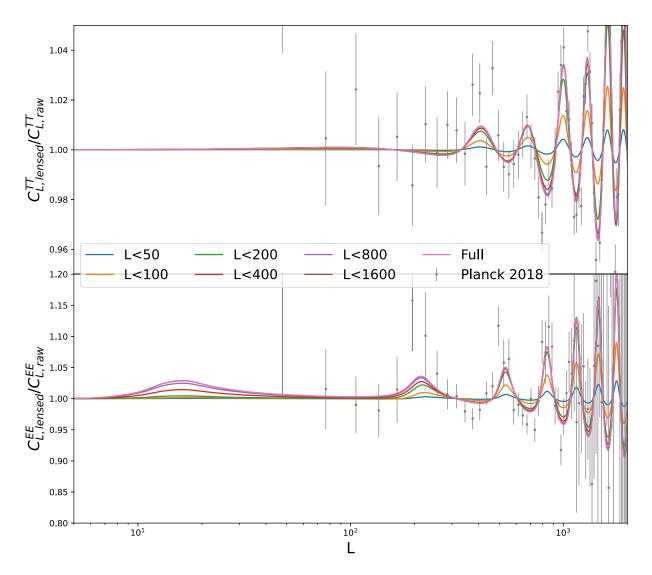


FIG. 3. Comparison between the lensed and raw TT and EE spectra. Different line color indicates that the corresponding lensed spectra is produced with the L < # section of $C_L^{\phi\phi}$ (others set to zero). Points with error bars are binned power spectra of Planck 2018 [2].

With explicit mentioning, we will also use the BICEP/Keck 2018 data (BK18) [66] of CMB B-mode polarization and the local measurement of $H_0 = 73.04 \pm 1.04$ km/s/Mpc [1] as a Gaussian prior (R21).

III. MODELS AND RESULTS

For ACDM we sample over the standard six cosmological parameters $\{\omega_{\rm cdm}, \omega_b, H_0, \ln 10^{10} A_s, n_s, \tau_{\rm reion}\}$. In the typical EDE scenario, a scalar field is initially frozen due to the Hubble friction at some initial position with nonvanishing potential energy. As the Universe cools, the scalar field thaws and starts rolling when the Hubble parameter drops below some critical value and the Hubble friction is no longer able to freeze the field. For specific EDE models we study the n=3 axion-like EDE (AxiEDE) [9] and AdS-EDE with a fixed AdS depth $\alpha_{ads} = 3.79 \times 10^{-4}$ [16,82]. EDE is characterized by two additional model parameters $\{z_c, f_{ede}\}$ where z_c is the redshift at which the EDE field starts rolling and f_{ede} its energy fraction at z_c . In AxiEDE we vary one more parameter Θ_i describing the initial phase of the field. See corresponding EDE papers for details. All AxiEDE analysis presented in this paper further includes the R21 H_0 prior in addition to our baseline dataset to achieve nontrivial EDE energy fraction [83,84]. Without such a prior, the AxiEDE model biases toward ACDM and does not represent the EDE cosmology. AdS-EDE does not suffer this problem partially due to the existence of V < 0 (AdS), which removes the Λ CDM (f_{ede}) best fit point from this model because too small $f_{\rm ede}$ will result in the field being confined in the disastrous AdS region and collapse the Universe before today.

We vary amplitudes $\{\ln A_1, \ln A_2, \ln A_3\}$ with flat priors at three nodes $L \in [50, 200, 800]$ log-evenly distributed in the lensing data multiple range. Considering that the characteristic shape of the lensing power spectrum $L^2(L+1)^2C_L^{\phi\phi}/2\pi$ is a peak, the three nodes are selected such that the first one near the peak, the second tunes the most constrained amplitude at the intermediate scales and the last anchors the high-L tail [85]. Because the typical relative variance of the lensing data used is $\lesssim 10\%$, we fix the kernel function parameter to $\sigma=0.1$. We also set the correlation length parameter l=1.0 which is small enough to capture the main features while also maintains acceptable convergence speed. See Appendix C for details.

Figure 1 plots our main results of the lensing shape constraints in the baseline dataset for ΛCDM and EDE, see Appendix A for details of the MCMC analysis. Width of the shaded area at a given multiple indicates the constraining power of data on lensing potential. One also notes that the constraint are very similar between AxiEDE and AdS-EDE in Fig. 1, which turns out to be general for lensing shape constraint. Therefore, to simplify presentation, we only present the AdS-EDE result hereafter unless explicitly specified. The most constrained range is roughly

 $80 \lesssim L \lesssim 400$, in accordance with the ACT + Planck bandpower bins. The constrained bands in this region distribute approximately evenly around A(L)=1, which requires that any model describing the late Universe that is compatible with data to predict lensing potential close to the concordance model in this multiple range. This can also be seen from the theory results (green) in Fig. 2, while EDE and Λ CDM constraints are generally different in the high and low L tail (mainly due to the significantly different prediction on n_s in EDE [86–89]), they overlap with each other in $80 \lesssim L \lesssim 400$. This observation agrees with the finding of Refs. [68,90] that lensing reconstruction is compatible with $A_{\rm lens}=1$ when marginalizing over a single $A_{\rm lens}$.

However, beyond the most constrained range $80 \lesssim L \lesssim 400$, Fig. 1 indicates a preference, general to ΛCDM and EDE, for enhanced lensing potential (compared with the concordance model) in both the low and high L tails. The enhancement in the low-L tail can be at least partially attributed to the preference for additional lensing-like smoothing in Planck data, sometimes referred to as the "lensing anomaly." Figure 3 shows how different sections of $C_L^{\phi\phi}$ contribute to the lensed T and E spectra. The oscillatory pattern in both spectra at high-L is the lensing smoothing effect, which according to Ref. [2], accounts for most of the improvement in fit for the lensing anomaly. This is also visible in Fig. 3 where the Planck data points have slightly higher amplitude than the "full" line in the oscillatory region. Figure 3 shows that L < 100 has

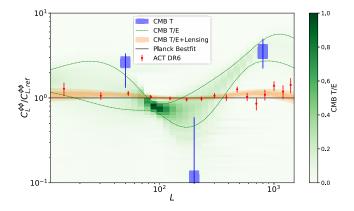


FIG. 4. Comparison between the lensing shape constraints from CMB temperature (CMB T) and E polarization (CMB T/E) and CMB T/E + lensing reconstruction. For CMB T/E + Lensing, 68% and 95% posterior bands of $C_L^{\phi\phi}$ are plotted. For CMB T/E, color shading plots the posterior density distribution of the $C_L^{\phi\phi}$ values at 40 L's log-evenly distributed in the range $10 \le L \le 1500$, with the corresponding 68% C.L. band indicated by green dotted lines. For CMB T, the second node is unconstrained from below, causing the full shape constraint to be prior dominated. Therefore, we only plot the 68% (blue rectangles) and 95% (blue lines) constraints (upper bound for the second node) of $C_L^{\phi\phi}$ at L = [50, 200, 800], corresponding to the positions of the three nodes $\{\ln A_1, \ln A_2, \ln A_3\}$.

major contribution to smoothing while the effect of L>400 is marginal. Figure 4 further compares the shape constraints from CMB temperature, polarization, and lensing reconstruction. Lensing reconstruction dominates the constraint in the most constrained region $80 \lesssim L \lesssim 400$, while lensed temperature and polarization spectra drive the preference for enhanced lensing effect on both the low and high L tails. E mode polarization data reduces the enhancement at L<100, which is consistent with the finding of Ref. [2] that the lensing anomaly becomes less obvious after inclusion of polarization spectra.

In Fig. 3, the L > 400 tail has significant contribution in the first two bumps of the E mode plot, especially the first bump is nearly exclusively contributed by $C_L^{\phi\phi}(L > 200)$.

This is due to the E to B mode conversion through CMB lensing and has already been noticed in Ref. [16]. It will thus be interesting to test if B-mode data provides additional constraints in the high-L tail and, inversely, if the preferred enhancement of $C_L^{\phi\phi}$ at high-L can change the derived bound on the tensor-to-scalar ratio r, defined as the ratio of primordial tensor power spectrum amplitude to scalar amplitude at $k=0.05~{\rm Mpc^{-1}}$. The enhancement at high L of the baseline + BK18 result (red) compared with the baseline one (blue) in Fig. 2 shows that B-mode data indeed contributes non-trivially to the lensing shape constraint in Λ CDM. On the other hand, upper bounds on r does not shift with the addition of free lensing, i.e., we obtain the same $r < 0.037~(95\%~{\rm C.L.})$ in Λ CDM

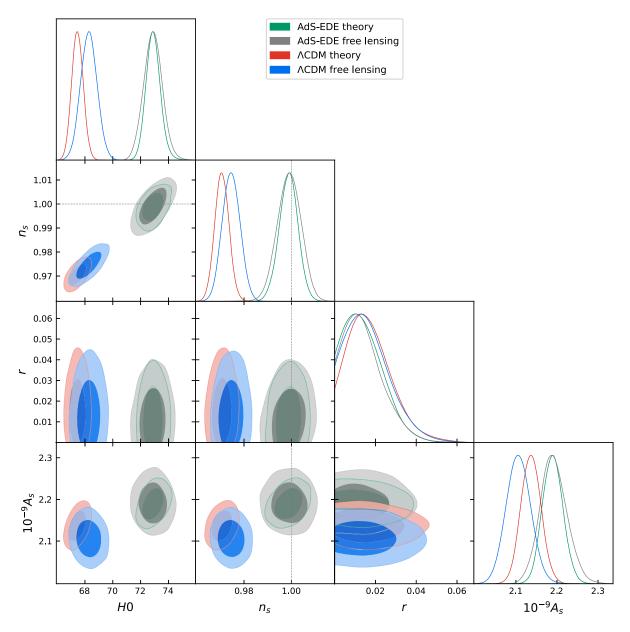


FIG. 5. 68% and 95% posterior distributions of relevant cosmological parameters in the Λ CDM and AdS-EDE models with and without free lensing. The dataset used is baseline + BK18. Dotted lines mark the position of $n_s = 1$.

and r < 0.033 (95% C.L.) in AdS-EDE with and without free lensing, see Fig. 5 for relevant cosmological parameter constraints. We attribute the slightly different bounds than Refs. [66,67,91] to the different datasets used. Another interesting point in Fig. 5 and also Appendix-A is that the AdS-EDE cosmological constraints seems to be more "robust" than Λ CDM against the addition of free lensing. This is because due to the nearly scale invariant n_s [86–89], the theoretically predicted $C_{L, \text{th}}^{\phi\phi}$ in AdS-EDE is already close to the shape constraint at the high-L tail, see Fig. 2, while in Λ CDM, some additional parameter shifts are needed to accommodate the new lensing shape when free lensing is turned on. Interestingly, including BK18 on top of the baseline dataset in Λ CDM further increases the enhancement in A(L) at high L.

IV. CONCLUSION

In this paper, we studied how CMB data alone, including temperature and polarization spectra as well as lensing reconstruction, can constrain the overall shape of the lensing potential in ACDM and EDE. We proposed a new function reconstruction method based on GP, which allowed us to marginalize over late-Universe effects such as lensing. As a consequence, the derived shape constraint does not rely on late Universe datasets such as baryon acoustic oscillation, SNIa and galaxy surveys which require assuming a specific cosmological model to bridge the early and late Universe. On the other hand, our result does depend on the early Universe model assumed, e.g. EDE. The lensing reconstruction data has relatively weak dependence on models because the reconstruction procedure mainly relies on the observed spectrum. However, as shown in Fig. 4, there is also part of the constraint coming from the smoothing of raw CMB T/E spectra. Both the smoothing effect and the raw spectra can depend on the model details of the prerecombination cosmology. It is quite interesting that AxiEDE and AdS-EDE produce very similar shape constraints in the end. We found current CMB lensing data can constrain the shape of lensing on a broad multiple range and, according to Fig. 2, the most stringent constraint is in $80 \lesssim L \lesssim 400$, where the cosmological models are required to produce ΛCDM-like lensing potential. This is a strong constraint on the possible behaviors of the late Universe during the period relevant to CMB lensing (a broad redshift range around $z \sim 2$) on these scales. On both the high and low-L tails beyond this range, the shape constraints are weaker but interestingly favor enhanced lensing compared with ACDM prediction, which we conclude is at least partially due to the preferred excess lensing-like smoothing in Planck data [92]. We found B-mode data can offer meaningful constraint on the lensing shape at L > 400 through its constraint on the lensing B-mode. Inclusion of B-mode does not remove the preference for enhanced lensing at L > 400. Despite different shapes of theoretically predicted lensing potentials, the lensing shape constraints from CMB data are very similar in EDE and Λ CDM. However, we do notice that, with free lensing, cosmological parameter constraints experience nearly no change in AdS-EDE as opposed to Λ CDM because the theory lensing potential shape in the former is closer to the data preferred shape due to its very scale invariant $n_{\rm s}$.

The constraints obtained in this paper can serve as a guideline for model building. Given a late Universe physics model, a necessary condition for such a model to be compatible with CMB is that it should respect the most stringent constraints in $80 \lesssim L \lesssim 400$ in Figs. 1 and 2. For example, a direct observation from the constrained shape is that any overall shift of the lensing potential amplitude will be difficult to reconcile with CMB lensing, such as a constant A_{lens} or positive spatial curvature [2,93–95]. This is in line with the observation that, despite the lensing anomaly, lensing reconstruction in both Planck 2018 [2] and ACT DR6 [68] supports $A_{lens} = 1$. Given the preference for enhanced lensing at L > 400 and that galaxy weak lensing surveys [38,39,96] seem to indicate reduced amplitude of matter power spectrum on small scales, we are working on generalizing the GP method presented here to the matter power spectrum and studying how combining CMB lensing with galaxy weak lensing can further constrain its shape.

ACKNOWLEDGMENTS

We acknowledge the Xmaris cluster for providing computing resources. Some figures are generated using GetDist [97]. We thank Alessandra Silvstri for useful comments and discussions. G. Y. is supported by NWO and the Dutch Ministry of Education, Culture and Science (OCW) (Grant No. VI.Vidi.192.069). Y. S. P. is supported by NSFC, No. 12075246 and the Fundamental Research Funds for the Central Universities.

APPENDIX A: MORE MCMC RESULTS

This appendix gathers some details of our baseline (i.e., CMB T/E + Lensing) MCMC analysis. Table I lists the priors for all varied model parameters. Figure 6 plots the

TABLE I. Priors for all model parameters varied in our MCMC analysis.

Parameter	Prior	Parameter	Prior
ω_b $\omega_{ m cdm}$	Uniform $(-\infty, +\infty)$ Uniform $(-\infty, +\infty)$ Uniform $(-\infty, +\infty)$	$ \frac{f_{\text{ede}}}{\ln(1+z_c)} $	Uniform(10 ⁻⁴ , 0.3) Uniform(7.5, 9.5) Uniform(0, 3.1)
$H_0 \\ \ln 10^{10} A_s \\ n_s$	Uniform $(-\infty, +\infty)$ Uniform $(-\infty, +\infty)$ Uniform $(-\infty, +\infty)$	$\Theta_i \ \ln A_{L_1} \ \ln A_{L_2}$	Uniform $(0, 3.1)$ Uniform $(-2, 2)$ Uniform $(-2, 2)$
$ au_{ m reion}$	Uniform $(0.004, +\infty)$	$\ln A_{L_3}$	Uniform $(-2,2)$

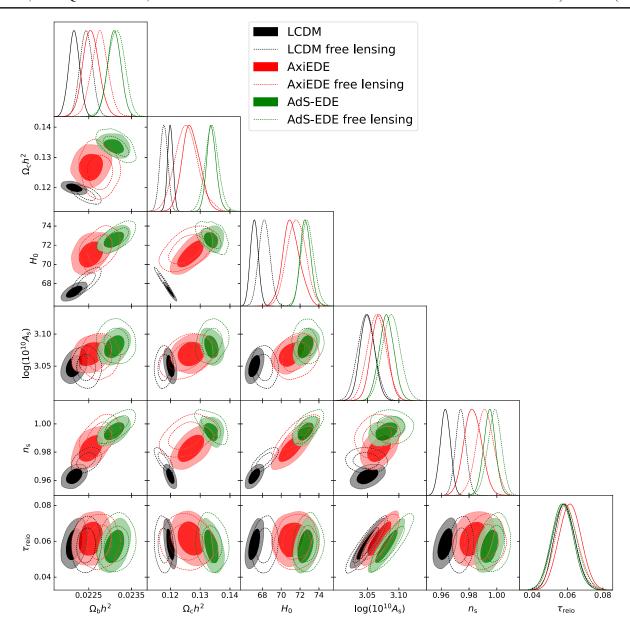


FIG. 6. 68% and 95% posterior distributions of cosmological parameters in our baseline ΛCDM, AxiEDE, and AdS-EDE models.

TABLE II. Mean and 1σ parameter constraints in our baseline Λ CDM, AxiEDE, and AdS-EDE models.

	ΛCDM		AxiEDE		AdS-EDE	
Parameters	Theory	Free lensing	Theory	Free lensing	Theory	Free lensing
$100\omega_b$	2.216 ± 0.013	2.245 ± 0.015	2.253 ± 0.020	$2.276^{+0.019}_{-0.017}$	2.309 ± 0.016	2.315 ± 0.019
$\omega_{ m cdm}$	0.1199 ± 0.0010	0.1178 ± 0.0013	$0.1256^{+0.0039}_{-0.0032}$	$0.1253^{+0.0028}_{-0.0033}$	$0.1338^{+0.0015}_{-0.0017}$	$0.1342^{+0.0021}_{-0.0023}$
H_0	67.15 ± 0.43	68.24 ± 0.59	70.7 ± 1.1	71.55 ± 0.83	$72.60^{+0.51}_{-0.59}$	72.79 ± 0.69
$\ln 10^{10} A_s$	3.050 ± 0.012	3.048 ± 0.014	$3.060^{+0.15}_{-0.18}$	$3.064^{+0.013}_{-0.016}$	3.080 ± 0.012	3.087 ± 0.014
n_s	0.9629 ± 0.0037	0.9740 ± 0.0038	$0.9793^{+0.0092}_{-0.0066}$	$0.9911^{+0.0061}_{-0.0053}$	0.9947 ± 0.0043	0.9981 ± 0.0049
$ au_{ m reion}$	0.0583 ± 0.0058	0.0577 ± 0.0066	0.0614 ± 0.0064	0.0595 ± 0.0070	0.0572 ± 0.0061	0.0583 ± 0.0065
$f_{ m ede}$	Not applicable	Not applicable	0.078 ± 0.029	0.088 ± 0.023	$0.1140^{+0.0031}_{-0.0078}$	$0.1154^{+0.0034}_{-0.0084}$
$ln(1+z_c)$	Not applicable	Not applicable	$8.289^{+0.345}_{-0.414}$	$8.312^{+0.143}_{-0.322}$	8.142 ± 0.058	$8.120^{+0.054}_{-0.061}$
Θ_i	Not applicable	Not applicable	> 2.54(95% C.L.)	$2.79^{+0.19}_{-0.09}$	Not applicable	Not applicable

posterior distributions in our baseline Λ CDM, AxiEDE and AdS-EDE analysis. The corresponding parameter constraints are reported in Table II. Note that AxiEDE has a nonvanishing $f_{\rm ede}$ here, which is due to the inclusion of an H_0 prior (R21) on top of the baseline datasets for this specific model, as explained in Sec. III. In both Figs. 5 and 6, parameter posteriors with free lensing show some shift (not statistically significant) compared with the ones without. The shifts are

generally smaller in Fig. 5 (baseline + BK18) than in Fig. 6 (baseline), which we attribute to the additional constraining power from BK18.

APPENDIX B: IMPACT OF LATE ISW

Another possible channel through which late Universe physics can affect CMB observable is the late time ISW effect, mainly originates from the dark energy dominated

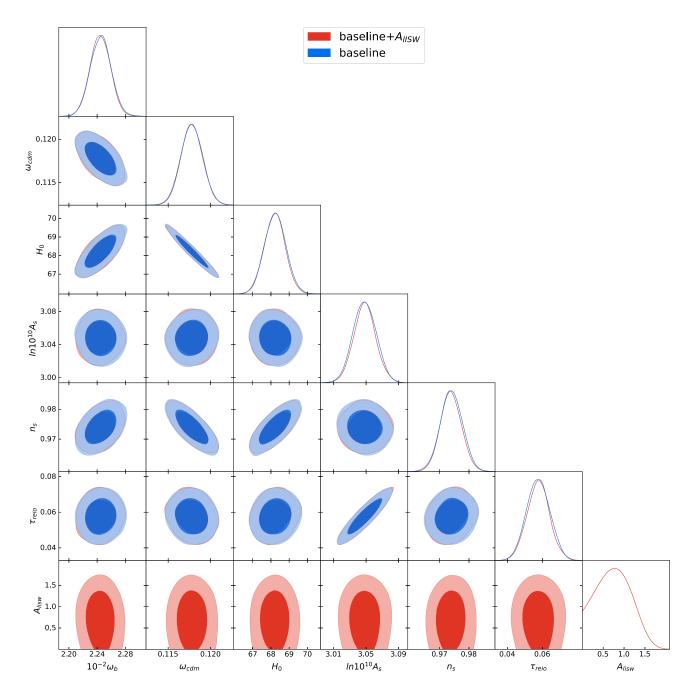


FIG. 7. 68% and 95% posterior distributions of cosmological parameters in Λ CDM with $A_{LISW} = 1$ and A_{LISW} free.

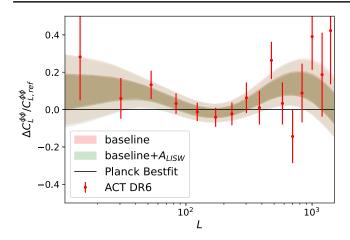


FIG. 8. Lensing shape constraints in ΛCDM with $A_{\text{LISW}}=1$ and A_{LISW} free.

era. To test the impact this effect, we rescale the late ISW (z < 120) contribution to the CMB power spectra by a free parameter $A_{\rm LISW}$ and redo our baseline analysis of Λ CDM. Figure 7 compares the cosmological parameter constraints with $A_{\rm LISW} = 1$ and $A_{\rm LISW}$ free, which shows that the constraint on $A_{\rm LISW}$ is fairly weak and does not significantly impact parameter constraints. Figure 8 further illustrates that the lensing shape constraints are also

unaffected by fixing $A_{\rm LISW}=1$. Therefore, we fix $A_{\rm LISW}=1$ in our baseline analysis to reduce number of free parameters.

APPENDIX C: IMPACT OF CORRELATION LENGTH l AND UNCERTAINTY σ

In this section, we compare the impact of different values of the GP parameters. Using the same model setups as described in Sec. III but with $l = \{0.25, 0.5, 1.0, 2.0\}, \sigma =$ 0.1 and l = 1.0, $\sigma = \{0.05, 0.1, 0.2\}$, we redo our analysis against the baseline dataset. It is clear Fig. 9 that the choice of l has nearly no effects on the parameter constraints. The left panel of Fig. 10 shows that the general shape constraint is also insensitive to the choice of l in a wide multiple range. However, too small l means the GP will tend to sample more functions with many random sharp features between two nodes and are not well constrained by data. This in practice manifests as extremely low acceptance rates and convergence speed in the MCMC analysis. We choose to fix l = 1.0 which is a good compromise between the acceptance rate and good shape constraints. The right panel of Fig. 10 shows that the main constraint at L > 40 is also stable against a change in σ . We choose to fix $\sigma = 0.1$ as it represents the typical relative error of the lensing reconstruction data.

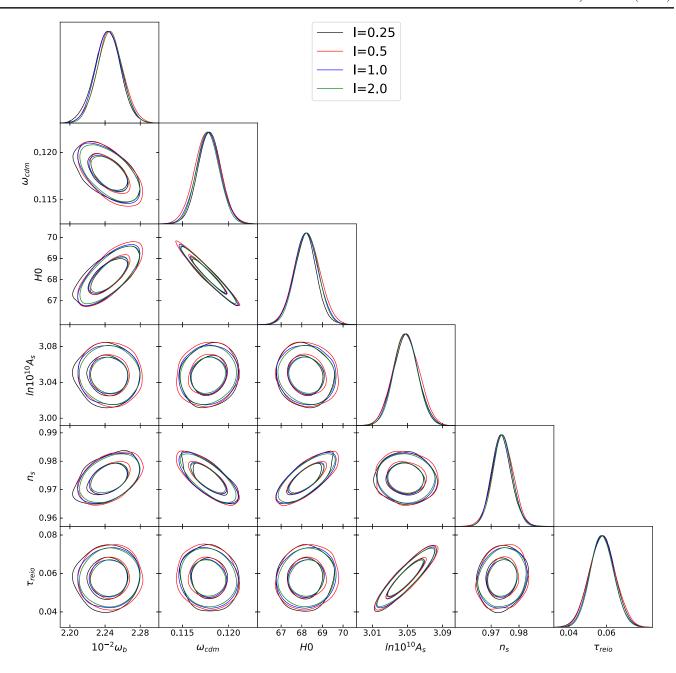
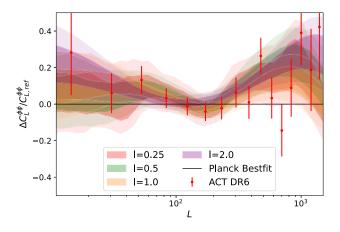


FIG. 9. 68% and 95% posterior distributions of cosmological parameters in ΛCDM with different GP parameter *l*.



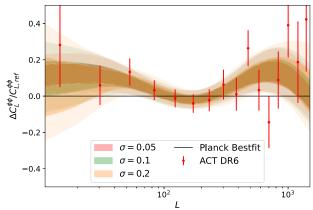


FIG. 10. Lensing shape constraints in Λ CDM with different GP parameters. Left panel: $l = \{0.25, 0.5, 1.0, 2.0\}$, $\sigma = 0.1$. Right panel: l = 1.0, $\sigma = \{0.05, 0.1, 0.2\}$.

- [1] A. G. Riess et al., Astrophys. J. Lett. 934, L7 (2022).
- [2] N. Aghanim *et al.* (Planck Collaboration), Astron. Astrophys. **641**, A6 (2020); **652**, C4(E) (2021).
- [3] S. Aiola *et al.* (ACT Collaboration), J. Cosmol. Astropart. Phys. 12 (2020) 047.
- [4] L. Balkenhol *et al.* (SPT-3G Collaboration), Phys. Rev. D 104, 083509 (2021).
- [5] L. Verde, T. Treu, and A. G. Riess, Nat. Astron. 3, 891 (2019).
- [6] P. Shah, P. Lemos, and O. Lahav, Astron. Astrophys. Rev. 29, 9 (2021).
- [7] E. Di Valentino, O. Mena, S. Pan, L. Visinelli, W. Yang, A. Melchiorri, D. F. Mota, A. G. Riess, and J. Silk, Classical Quantum Gravity 38, 153001 (2021).
- [8] L. Perivolaropoulos and F. Skara, New Astron. Rev. 95, 101659 (2022).
- [9] V. Poulin, T. L. Smith, T. Karwal, and M. Kamionkowski, Phys. Rev. Lett. 122, 221301 (2019).
- [10] P. Agrawal, F.-Y. Cyr-Racine, D. Pinner, and L. Randall, arXiv:1904.01016.
- [11] S. Alexander and E. McDonough, Phys. Lett. B 797, 134830 (2019).
- [12] M.-X. Lin, G. Benevento, W. Hu, and M. Raveri, Phys. Rev. D 100, 063542 (2019).
- [13] T. L. Smith, V. Poulin, and M. A. Amin, Phys. Rev. D 101, 063523 (2020).
- [14] F. Niedermann and M. S. Sloth, Phys. Rev. D **103**, L041303 (2021).
- [15] J. Sakstein and M. Trodden, Phys. Rev. Lett. 124, 161301 (2020)
- [16] G. Ye and Y.-S. Piao, Phys. Rev. D 101, 083507 (2020).
- [17] M. Braglia, W. T. Emond, F. Finelli, A. E. Gumrukcuoglu, and K. Koyama, Phys. Rev. D **102**, 083513 (2020).
- [18] T. Karwal, M. Raveri, B. Jain, J. Khoury, and M. Trodden, Phys. Rev. D 105, 063535 (2022).
- [19] F. Niedermann and M. S. Sloth, Phys. Rev. D **105**, 063509 (2022).

- [20] E. McDonough, M.-X. Lin, J. C. Hill, W. Hu, and S. Zhou, Phys. Rev. D 106, 043525 (2022).
- [21] E. McDonough and M. Scalisi, arXiv:2209.00011.
- [22] K. Rezazadeh, A. Ashoorioon, and D. Grin, arXiv:2208 .07631.
- [23] L. Brissenden, K. Dimopoulos, and S. Sánchez López, arXiv:2301.03572.
- [24] O. Seto and Y. Toda, Phys. Rev. D 103, 123501 (2021).
- [25] M. Kamionkowski and A. G. Riess, arXiv:2211.04492.
- [26] V. Poulin, T. L. Smith, and T. Karwal, arXiv:2302.09032.
- [27] M.-X. Lin, M. Raveri, and W. Hu, Phys. Rev. D 99, 043514 (2019).
- [28] M. Zumalacarregui, Phys. Rev. D 102, 023523 (2020).
- [29] M. Braglia, M. Ballardini, W. T. Emond, F. Finelli, A. E. Gumrukcuoglu, K. Koyama, and D. Paoletti, Phys. Rev. D 102, 023529 (2020).
- [30] G. Ballesteros, A. Notari, and F. Rompineve, J. Cosmol. Astropart. Phys. 11 (2020) 024.
- [31] N. Blinov, K. J. Kelly, G. Z. Krnjaic, and S. D. McDermott, Phys. Rev. Lett. 123, 191102 (2019).
- [32] C. D. Kreisch, F.-Y. Cyr-Racine, and O. Doré, Phys. Rev. D 101, 123505 (2020).
- [33] C.-T. Chiang and A. Slosar, arXiv:1811.03624.
- [34] K. Jedamzik and L. Pogosian, Phys. Rev. Lett. 125, 181302 (2020).
- [35] T. Sekiguchi and T. Takahashi, Phys. Rev. D 103, 083507 (2021).
- [36] L. W. H. Fung, L. Li, T. Liu, H. N. Luu, Y.-C. Qiu, and S. H. H. Tye, J. Cosmol. Astropart. Phys. 08 (2021) 057.
- [37] L. Hart and J. Chluba, Mon. Not. R. Astron. Soc. 493, 3255 (2020).
- [38] C. Heymans et al., Astron. Astrophys. 646, A140 (2021).
- [39] T. M. C. Abbott *et al.* (DES Collaboration), Phys. Rev. D 105, 023520 (2022).
- [40] T. M. C. Abbott *et al.* (Kilo-Degree Survey and Dark Energy Survey Collaborations), arXiv:2305.17173.
- [41] E. Abdalla et al., J. High Energy Astrophys. 34, 49 (2022).

- [42] J. C. Hill, E. McDonough, M. W. Toomey, and S. Alexander, Phys. Rev. D 102, 043507 (2020).
- [43] M. M. Ivanov, E. McDonough, J. C. Hill, M. Simonović, M. W. Toomey, S. Alexander, and M. Zaldarriaga, Phys. Rev. D 102, 103502 (2020).
- [44] G. D'Amico, L. Senatore, P. Zhang, and H. Zheng, J. Cosmol. Astropart. Phys. 05 (2021) 072.
- [45] G. Ye and Y.-S. Piao, Phys. Rev. D 102, 083523 (2020).
- [46] L. Pogosian, G.-B. Zhao, and K. Jedamzik, Astrophys. J. Lett. 904, L17 (2020).
- [47] K. Jedamzik, L. Pogosian, and G.-B. Zhao, Commun. Phys. 4, 123 (2021).
- [48] S. Vagnozzi, Phys. Rev. D 104, 063524 (2021).
- [49] I. J. Allali, M. P. Hertzberg, and F. Rompineve, Phys. Rev. D 104, L081303 (2021).
- [50] G. Ye, J. Zhang, and Y.-S. Piao, Phys. Lett. B 839, 137770 (2023).
- [51] S. J. Clark, K. Vattis, J. Fan, and S. M. Koushiappas, Phys. Rev. D 107, 083527 (2023).
- [52] A. Gómez-Valent, Z. Zheng, L. Amendola, C. Wetterich, and V. Pettorino, Phys. Rev. D 106, 103522 (2022).
- [53] A. Reeves, L. Herold, S. Vagnozzi, B. D. Sherwin, and E. G. M. Ferreira, Mon. Not. R. Astron. Soc. 520, 3688 (2023).
- [54] H. Wang and Y.-S. Piao, Phys. Lett. B 832, 137244 (2022).
- [55] S. Alexander, H. Bernardo, and M. W. Toomey, J. Cosmol. Astropart. Phys. 03 (2023) 037.
- [56] M. A. Buen-Abad, Z. Chacko, C. Kilic, G. Marques-Tavares, and T. Youn, J. High Energy Phys. 06 (2023) 012.
- [57] H. Wang and Y.-S. Piao, arXiv:2209.09685.
- [58] J. Rebouças, J. Gordon, D. H. F. de Souza, K. Zhong, V. Miranda, R. Rosenfeld, T. Eifler, and E. Krause, arXiv: 2302.07333.
- [59] B. Audren, J. Lesgourgues, K. Benabed, and S. Prunet, J. Cosmol. Astropart. Phys. 02 (2013) 001.
- [60] B. Audren, Mon. Not. R. Astron. Soc. 444, 827 (2014).
- [61] P. Motloch, W. Hu, and A. Benoit-Lévy, Phys. Rev. D 95, 043518 (2017).
- [62] P. Motloch and W. Hu, Phys. Rev. D 96, 103517 (2017).
- [63] P. Motloch and W. Hu, Phys. Rev. D 97, 103536 (2018).
- [64] P. Motloch and W. Hu, Phys. Rev. D 101, 083515 (2020).
- [65] P. Lemos and A. Lewis, Phys. Rev. D 107, 103505 (2023).
- [66] P. A. R. Ade et al. (BICEP/Keck Collaboration), Phys. Rev. Lett. 127, 151301 (2021).
- [67] G. Ye and Y.-S. Piao, Phys. Rev. D **106**, 043536 (2022).
- [68] F. J. Qu et al. (ACT Collaboration), arXiv:2304.05202.
- [69] S. Galli, K. Benabed, F. Bouchet, J.-F. Cardoso, F. Elsner, E. Hivon, A. Mangilli, S. Prunet, and B. Wandelt, Phys. Rev. D 90, 063504 (2014).
- [70] X.-H. Fan, C. L. Carilli, and B. G. Keating, Annu. Rev. Astron. Astrophys. 44, 415 (2006).
- [71] The Nth point is rejected if its χ_N^2 is larger than the previous step χ_{N-1}^2 , otherwise there is a possibility depending on $\Delta \chi^2 = \chi_{N-1}^2 \chi_N^2$ of accepting and storing it in the chain.

- [72] T. Brinckmann and J. Lesgourgues, Phys. Dark Universe 24, 100260 (2019).
- [73] Available at https://github.com/genye00/montepython-3 .5_lens.git.
- [74] J. Lesgourgues, arXiv:1104.2932.
- [75] D. Blas, J. Lesgourgues, and T. Tram, J. Cosmol. Astropart. Phys. 07 (2011) 034.
- [76] Available at https://github.com/genye00/class_multiscf.git.
- [77] E. Rosenberg, S. Gratton, and G. Efstathiou, Mon. Not. R. Astron. Soc. 517, 4620 (2022).
- [78] Y. Akrami *et al.* (Planck Collaboration), Astron. Astrophys. 643, A42 (2020).
- [79] N. Aghanim et al. (Planck Collaboration), Astron. Astrophys. 641, A5 (2020).
- [80] J. Carron, M. Mirmelstein, and A. Lewis, J. Cosmol. Astropart. Phys. 09 (2022) 039.
- [81] M. S. Madhavacheril *et al.* (ACT Collaboration), arXiv: 2304.05203.
- [82] According to Ref. [45], the existence of an AdS phase is weakly hinted. Here we focus on CMB lensing rather than specific EDE models, thus we choose to fix the AdS depth to the value in Ref. [16], which has been shown to be compatible with Planck 2018 CMB spectra and lensing reconstruction.
- [83] R. Murgia, G. F. Abellán, and V. Poulin, Phys. Rev. D 103, 063502 (2021).
- [84] T. L. Smith, V. Poulin, J. L. Bernal, K. K. Boddy, M. Kamionkowski, and R. Murgia, Phys. Rev. D 103, 123542 (2021).
- [85] We have checked that the results will not significantly depend on the selection of node positions as long as they are reasonably chosen, i.e., the intervals are large enough and contains most of the data dominated area. Also adding more nodes does not recover finer shape but affects convergence speed negatively.
- [86] G. Ye, B. Hu, and Y.-S. Piao, Phys. Rev. D 104, 063510 (2021).
- [87] J.-Q. Jiang and Y.-S. Piao, Phys. Rev. D 105, 103514 (2022).
- [88] J.-Q. Jiang, G. Ye, and Y.-S. Piao, arXiv:2210.06125.
- [89] J.-Q. Jiang, G. Ye, and Y.-S. Piao, arXiv:2303.12345.
- [90] N. Aghanim *et al.* (Planck Collaboration), Astron. Astrophys. **641**, A8 (2020).
- [91] M. Tristram et al., Phys. Rev. D 105, 083524 (2022).
- [92] Our results only indicate a similar possible preference in data. It does not confirm the lensing anomaly in any statistical sense.
- [93] W. Handley, Phys. Rev. D 103, L041301 (2021).
- [94] E. Di Valentino, A. Melchiorri, and J. Silk, Nat. Astron. 4, 196 (2019).
- [95] S. Vagnozzi, E. Di Valentino, S. Gariazzo, A. Melchiorri, O. Mena, and J. Silk, Phys. Dark Universe 33, 100851 (2021).
- [96] M. Asgari *et al.* (KiDS Collaboration), Astron. Astrophys. 645, A104 (2021).
- [97] A. Lewis, arXiv:1910.13970.