

Evidence for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ at Belle

C.-Y. Chang¹, M.-Z. Wang², I. Adachi³, H. Aihara⁴, S. Al Said⁵, D. M. Asner⁶, H. Atmacan⁷, T. Aushev⁸, R. Ayad⁹, V. Babu¹⁰, Sw. Banerjee¹¹, M. Bauer¹², P. Behera¹³, K. Belous¹⁴, J. Bennett¹⁵, F. Bernlochner¹⁶, M. Bessner¹⁷, T. Bilka¹⁸, D. Biswas¹⁹, A. Bobrov²⁰, D. Bodrov²¹, G. Bonvicini²², J. Borah²³, A. Bozek²⁴, M. Bračko²⁵, P. Branchini²⁶, T. E. Browder²⁷, A. Budano²⁸, M. Campajola²⁹, L. Cao³⁰, D. Červenkov³¹, M.-C. Chang³², B. G. Cheon³³, K. Chilikin³⁴, H. E. Cho³⁵, K. Cho³⁶, S.-J. Cho³⁷, S.-K. Choi³⁸, Y. Choi³⁹, S. Choudhury⁴⁰, D. Cinabro⁴¹, S. Das⁴², G. De Nardo⁴³, G. De Pietro⁴⁴, R. Dhamija⁴⁵, F. Di Capua⁴⁶, Z. Doležal⁴⁷, T. V. Dong⁴⁸, S. Dubey⁴⁹, P. Ecker⁵⁰, T. Ferber⁵¹, D. Ferlewicz⁵², B. G. Fulsom⁵³, V. Gaur⁵⁴, A. Garmash⁵⁵, A. Giri⁵⁶, P. Goldenzweig⁵⁷, E. Graziani⁵⁸, T. Gu⁵⁹, Y. Guan⁶⁰, K. Gudkova⁶¹, C. Hadjivasiliou⁶², S. Halder⁶³, T. Hara⁶⁴, K. Hayasaka⁶⁵, H. Hayashii⁶⁶, S. Hazra⁶⁷, M. T. Hedges⁶⁸, D. Herrmann⁶⁹, W.-S. Hou⁷⁰, C.-L. Hsu⁷¹, K. Inami⁷², N. Ipsita⁷³, A. Ishikawa⁷⁴, R. Itoh⁷⁵, M. Iwasaki⁷⁶, Y. Iwasaki⁷⁷, W. W. Jacobs⁷⁸, S. Jia⁷⁹, Y. Jin⁸⁰, K. K. Joo⁸¹, A. B. Kaliyar⁸², T. Kawasaki⁸³, C. Kiesling⁸⁴, C. H. Kim⁸⁵, D. Y. Kim⁸⁶, K.-H. Kim⁸⁷, Y.-K. Kim⁸⁸, K. Kinoshita⁸⁹, P. Kodyš⁹⁰, T. Konno⁹¹, A. Korobov⁹², S. Korpar⁹³, E. Kovalenko⁹⁴, P. Križan⁹⁵, P. Krokovny⁹⁶, T. Kuhr⁹⁷, M. Kumar⁹⁸, K. Kumara⁹⁹, A. Kuzmin¹⁰⁰, Y.-J. Kwon¹⁰¹, Y.-T. Lai¹⁰², T. Lam¹⁰³, M. Laurenza¹⁰⁴, S. C. Lee¹⁰⁵, D. Levit¹⁰⁶, L. K. Li¹⁰⁷, L. Li Gioi¹⁰⁸, J. Libby¹⁰⁹, K. Lieret¹¹⁰, Y.-R. Lin¹¹¹, D. Liventsev¹¹², Y. Ma¹¹³, M. Masuda¹¹⁴, D. Matvienko¹¹⁵, S. K. Maurya¹¹⁶, F. Meier¹¹⁷, M. Merola¹¹⁸, F. Metzner¹¹⁹, R. Mizuk¹²⁰, R. Mussa¹²¹, I. Nakamura¹²², M. Nakao¹²³, A. Natochii¹²⁴, L. Nayak¹²⁵, N. K. Nisar¹²⁶, S. Nishida¹²⁷, K. Ogawa¹²⁸, S. Ogawa¹²⁹, H. Ono¹³⁰, P. Oskin¹³¹, P. Pakhlov¹³², G. Pakhlova¹³³, S. Pardi¹³⁴, J. Park¹³⁵, S.-H. Park¹³⁶, A. Passeri¹³⁷, S. Patra¹³⁸, S. Paul¹³⁹, T. K. Pedlar¹⁴⁰, R. Pestotnik¹⁴¹, L. E. Piilonen¹⁴², T. Podobnik¹⁴³, E. Prencipe¹⁴⁴, M. T. Prim¹⁴⁵, N. Rout¹⁴⁶, G. Russo¹⁴⁷, S. Sandilya¹⁴⁸, A. Sangal¹⁴⁹, L. Santelj¹⁵⁰, V. Savinov¹⁵¹, G. Schnell¹⁵², C. Schwanda¹⁵³, Y. Seino¹⁵⁴, K. Senyo¹⁵⁵, M. E. Seviour¹⁵⁶, W. Shan¹⁵⁷, M. Shapkin¹⁵⁸, C. Sharma¹⁵⁹, J.-G. Shiu¹⁶⁰, J. B. Singh¹⁶¹, A. Sokolov¹⁶², E. Solovieva¹⁶³, M. Starič¹⁶⁴, J. F. Strube¹⁶⁵, M. Sumihama¹⁶⁶, W. Sutcliffe¹⁶⁷, M. Takizawa¹⁶⁸, K. Tanida¹⁶⁹, F. Tenchini¹⁷⁰, R. Tiwary¹⁷¹, K. Trabelsi¹⁷², M. Uchida¹⁷³, Y. Unno¹⁷⁴, S. Uno¹⁷⁵, Y. Usov¹⁷⁶, S. E. Vahsen¹⁷⁷, G. Varner¹⁷⁸, K. E. Varvell¹⁷⁹, D. Wang¹⁸⁰, E. Wang¹⁸¹, S. Watanuki¹⁸², O. Werbycka¹⁸³, E. Won¹⁸⁴, B. D. Yabsley¹⁸⁵, W. Yan¹⁸⁶, S. B. Yang¹⁸⁷, J. H. Yin¹⁸⁸, C. Z. Yuan¹⁸⁹, L. Yuan¹⁹⁰, Y. Yusa¹⁹¹, Z. P. Zhang¹⁹², V. Zhilich¹⁹³, and V. Zhukova¹⁹⁴

(Belle Collaboration)



(Received 31 May 2023; accepted 25 August 2023; published 22 September 2023)

We search for the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ decay with $\bar{\Sigma}^0 \rightarrow \bar{\Lambda}\gamma$, where the γ is not measured, using a data sample corresponding to an integrated luminosity of 711 fb^{-1} which contains $772 \times 10^6 B\bar{B}$ pairs, collected around the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy e^+e^- collider. We measure for the first time the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ branching fraction to be $\mathcal{B}(B^0 \rightarrow p\bar{\Sigma}^0\pi^-) = (1.17_{-0.40}^{+0.43}(\text{stat}) \pm 0.07(\text{syst})) \times 10^{-6}$ with a significance of 3.0σ . We simultaneously measure the branching fraction for the related channel $B^0 \rightarrow p\bar{\Lambda}\pi^-$ with much improved precision.

DOI: [10.1103/PhysRevD.108.052011](https://doi.org/10.1103/PhysRevD.108.052011)

Since the first observation of the rare baryonic B decay $B^+ \rightarrow p\bar{p}K^+$ [1], many other such decay modes, together with their puzzling features, have been found which are summarized in Sec. 17.12 of Ref. [2]. One unexpected feature is the observation of an asymmetry in the angular distribution in $B^0 \rightarrow p\bar{\Lambda}\pi^-$ [3]. This indicates that the proton tends to move faster than the accompanying $\bar{\Lambda}$ in

the B meson rest frame, which contradicts the intuitive $b \rightarrow sg$ picture [4] of the $B^0 \rightarrow p\bar{\Lambda}\pi^-$ decay which is shown in Fig. 1. Factorization approaches and QCD counting rules [5,6] predict that the branching fraction (\mathcal{B}) of $B^0 \rightarrow p\bar{\Lambda}\pi^-$ is much smaller than that of $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$, and is an order of magnitude smaller than the current measured branching fraction of $(3.23_{-0.29}^{+0.33} \pm 0.29) \times 10^{-6}$ [3]. A similar approach with modifying the axial-vector and pseudoscalar operators [7] predicts $\mathcal{B}(B^0 \rightarrow p\bar{\Lambda}\pi^-)$ and $\mathcal{B}(B^0 \rightarrow p\bar{\Sigma}^0\pi^-) \sim 1.6 \times 10^{-6}$. Thus, it is promising to observe $\mathcal{B}(B^0 \rightarrow p\bar{\Sigma}^0\pi^-)$ using the full $\Upsilon(4S)$ dataset collected by the Belle experiment. Another important aspect for this study is the large B sample

Published by the American Physical Society under the terms of the [Creative Commons Attribution 4.0 International license](https://creativecommons.org/licenses/by/4.0/). Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP³.

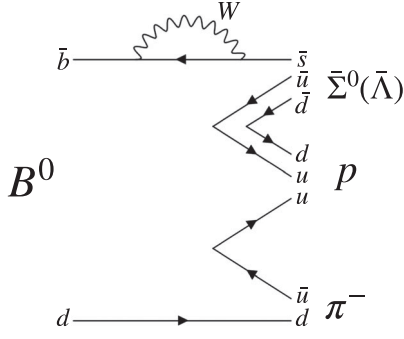


FIG. 1. A possible $b \rightarrow sg$ penguin diagram for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ and $B^0 \rightarrow p\bar{\Lambda}\pi^-$.

accumulated by the LHCb experiment, where branching fraction measurements of rare baryonic B decays such as $B_s^0 \rightarrow p\bar{\Lambda}K^-$ [8] utilize $\mathcal{B}(B^0 \rightarrow p\bar{\Lambda}\pi^-)$ for the normalization. These measurements will hence profit from a more precise measurement of $\mathcal{B}(B^0 \rightarrow p\bar{\Lambda}\pi^-)$. In addition, the systematic uncertainty due to the contamination of $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ can be better constrained if $\mathcal{B}(B^0 \rightarrow p\bar{\Sigma}^0\pi^-)$ is known.

We study the decay $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ based on a data sample that corresponds to an integrated luminosity of 711 fb^{-1} and contains 772×10^6 $B\bar{B}$ pairs. The whole data sample is collected with the Belle detector at the KEKB asymmetric-energy e^+e^- collider [9,10] using an e^+ energy of 3.5 GeV and an e^- energy of 8 GeV. The Belle detector [11,12] is a large-solid-angle magnetic spectrometer which includes a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of 44 aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field, and an iron flux-return located outside of the coil, which is instrumented to detect K_L mesons and identify muons (KLM). The details of each subdetector are described in Ref. [11].

We use Monte Carlo (MC) samples to study the selection criteria for signal reconstruction. The MC samples are generated by the EvtGen package [13] and the response of the Belle detector is simulated by the GEANT3 package [14]. In the signal MC sample, one of the B^0 or \bar{B}^0 mesons in the $B^0\bar{B}^0$ pair decays to our signal channel, and the other one decays randomly according to the known or estimated branching fractions. We generate signal MC samples using two decay models: a threshold-enhancement (TE) model, where the baryon-antibaryon pair in the final state is generated near its kinematic threshold, and a phase-space model, where the final-state particles from the decay are distributed uniformly in phase space. In the TE model, we define hypothetical particles with nominal mass values of 2.05 and 2.18 GeV/c^2 , and a width of 0.3 GeV/c^2 , which

decay to $p\bar{\Lambda}$ and $p\bar{\Sigma}^0$, respectively. In our analysis, we assume the signal events to follow the TE model. The classification of signal and background events is optimized using signal MC samples where we assumed a $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ branching fraction of 1.9×10^{-6} , which is half the value of the previously measured upper limit [15]. To study the background, we use MC samples that include generic B decays (both B mesons are collection of $b \rightarrow c$ process only, with known or estimated branching fractions), continuum background ($e^+e^- \rightarrow q\bar{q}$ with $q = u, d, s, c$), and rare B decays ($b \rightarrow u, d, s$).

The charged-track selection criteria are based on the information obtained from the tracking system (SVD and CDC). We use information from the CDC, ACC, and TOF to form hadron particle identification (ID) [16] likelihood values \mathcal{L}_i calculated for each particle hypothesis i —with $i = \pi, K$, and p . For lepton (e, μ) particle ID, the information from the KLM is used to calculate muon ID likelihood value \mathcal{L}_μ , and the information from the CDC, ACC and ECL is utilized to form electron ID likelihood value \mathcal{L}_e . We first reject highly electronlike ($\mathcal{L}_e \geq 0.95$) and muonlike ($\mathcal{L}_\mu \geq 0.95$) tracks. To select protonlike tracks, we require $\mathcal{L}_p/(\mathcal{L}_p + \mathcal{L}_K) > 0.6$ and $\mathcal{L}_p/(\mathcal{L}_p + \mathcal{L}_\pi) > 0.6$ which has 92.4% selection efficiency. To select π -like tracks, we require $\mathcal{L}_K/(\mathcal{L}_\pi + \mathcal{L}_K) < 0.4$ which has 92.1% selection efficiency. We constrain the distance of closest approach of a charged track and the interaction point (IP) along the e^+ beam direction (dz) and in the plane transverse to it (dr). For protons (pions), which do not originate from a Λ decay, we require $|dr| < 0.3(0.3)$ cm and $|dz| < 2(4)$ cm.

The Λ is reconstructed by combining a p track and a π track. We select Λ candidates by applying Λ -momentum-dependent constraints on four kinematic variables: the distance between the two daughter tracks at their interception position along the e^+ beam direction; the smaller of the proton dr and pion dr ; the angle between the vector from the primary to the secondary vertex and the momentum vector of the Λ ; and the flight-path length of the Λ candidate. The invariant mass of the Λ candidates is required to be in the range from 1.111 to 1.121 GeV/c^2 , which corresponds approximately to the $\pm 3\sigma_{m_\Lambda}$ interval with σ_{m_Λ} being the Λ mass resolution. The daughter proton of the Λ candidate is required to have $\mathcal{L}_p/(\mathcal{L}_p + \mathcal{L}_K) > 0.6$ and $\mathcal{L}_p/(\mathcal{L}_p + \mathcal{L}_\pi) > 0.6$ in order to reduce combinatorial background. But we do not impose any additional criteria on pions.

The B signal candidates are reconstructed by combining the 4-momenta of $p, \bar{\Lambda}$ and π^- candidates including their charged-conjugate states. Soft photon candidates from $\bar{\Sigma}^0 \rightarrow \bar{\Lambda}\gamma$ are not included in the signal B reconstruction, since this would lead to excessive background. For each B candidate, a kinematic fit is performed, which constrains the 4-momenta of all final-state particles to originate from a

common vertex. Only B candidates where this fit converges are selected.

We also measure $B^0 \rightarrow p\bar{\Lambda}\pi^-$ simultaneously to obtain a more precise branching fraction and validate the analysis procedure for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$. To disentangle the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ contribution from the $B^0 \rightarrow p\bar{\Lambda}\pi^-$ contribution and the background contributions, we use the distribution of two kinematic variables defined in the e^+e^- center-of-momentum (c.m.) frame: the beam-energy-constrained mass $M_{bc} = \sqrt{E_{\text{beam}}^2/c^4 - p_B^2/c^2}$, and the energy difference $\Delta E = E_{\text{beam}} - E_B$, where E_{beam} is the beam energy and p_B , E_B are the momentum and the energy of the B meson candidate, respectively. We require our signal candidates to lie within $\Delta E \in (-0.14, 0.20)$ GeV, which effectively reduces the contributions from possible rare channels and other excited states like $B^0 \rightarrow p\bar{\Lambda}(1405)\pi^-$ and $B^0 \rightarrow p\bar{\Sigma}^0(1385)\pi^-$, such that they are insignificant compared to signals in MC simulation, and $M_{bc} \in (5.23, 5.30)$ GeV/ c^2 .

Using the background MC samples described above, we find that the dominant source of background comes from $q\bar{q}$ continuum background. In contrast to $b \rightarrow c$ and $b \rightarrow u, d, s$ decays of B mesons, continuum background can be distinguished well from signal events by its shape variables. To classify signal and background events, we use a multivariate analysis package named NEUROBAYES [17], which is based on neural networks. The training samples are generated using a signal MC sample and a background sample obtained from real data in a sideband region defined by $\Delta E > 0.1$ GeV. The neural network was trained using the following 29 input variables: 20 modified Fox-Wolfram moments [18,19]; the cosine of polar angle of the B daughters with respect to the beam axis; the cosine of the angle between the reconstructed B flight direction in the beam axis; the sphericity of the event calculated in the c.m. frame [20]; the longitudinal distance between the vertices of signal B candidate and the accompanying \bar{B} ; the quality variable given by the flavor tagging used to judge how likely a B candidate is a B meson [21]; as well as the missing mass and missing energy of the event obtained from the deviation between the reconstructed and expected four momentum of the accompanying \bar{B} . The output discriminant of NEUROBAYES varies from -1 to $+1$, where a value close to $+1$ corresponds to a signal-like event, whereas -1 corresponds to a background-like event. We determine the threshold on the NEUROBAYES output by optimizing the figure-of-merit (FOM) given as

$$\text{FOM} = \frac{N_{\text{sig}}}{\sqrt{N_{\text{sig}} + N_{\text{bkg}}}}, \quad (1)$$

where N_{sig} is the number of signal events estimated from the signal efficiency and assumed branching fraction in the MC simulation, and N_{bkg} is the number of background events obtained from the $q\bar{q}$ continuum background MC

scaled to the full Belle luminosity in the signal region $\Delta E \in (-0.14, 0.00)$ GeV and $M_{bc} \in (5.26, 5.30)$ GeV/ c^2 and calibrated by a scaling from ΔE sidebands in data into ΔE signal region.

To remove the background from $B^0 \rightarrow p\bar{\Lambda}_c^-$ without a major loss of reconstruction efficiency, we veto events within $M_{\Lambda_c} \in (2.15, 2.30)$ GeV/ c^2 , which corresponds approximately to the $\pm 2\sigma_{m_{\Lambda_c}}$ interval around the Λ_c^- nominal mass with $\sigma_{m_{\Lambda_c}}$ being the Λ_c^- mass resolution.

For events with multiple signal candidates, we select the candidate with the smallest vertex χ^2 from the B vertex fit by using p , π tracks and Λ vertex reconstructed with p, π tracks of Λ candidates. MC studies show that this selects the true candidate in 99.3% of the events with more than one candidate. In the real data, 3.66% of events have multiple B candidates with an average multiplicity of 1.04.

To extract the signal yields, we perform a two-dimensional (2D) extended unbinned maximum likelihood fit to the $(\Delta E, M_{bc})$ distribution. The likelihood function is given by

$$\begin{aligned} \mathcal{L} = & \frac{e^{-(N_{s1}+N_{s2}+N_b)}}{N!} \prod_{i=1}^N [N_{s1}P_{s1}(M_{bc}^i, \Delta E^i) \\ & + N_{s2}P_{s2}(M_{bc}^i, \Delta E^i) + N_bP_b(M_{bc}^i, \Delta E^i) \\ & + N_{cb}P_{cb}(M_{bc}^i, \Delta E^i)], \end{aligned} \quad (2)$$

where i denotes the i th event and N is number of measured events. N_{s1} , N_{s2} , N_b and N_{cb} are the yields for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$, $B^0 \rightarrow p\bar{\Lambda}\pi^-$, background and combinatorial background of $B^0 \rightarrow p\bar{\Lambda}\pi^-$, respectively. P_{s1} , P_{s2} , P_b , and P_{cb} represent the probability density functions (PDFs) for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$, $B^0 \rightarrow p\bar{\Lambda}\pi^-$, background and combinatorial background of $B^0 \rightarrow p\bar{\Lambda}\pi^-$, respectively.

The following PDF shapes are obtained from MC simulation. We model P_{s1} using a 2D binned PDF obtained from MC simulation. For the $B^0 \rightarrow p\bar{\Lambda}\pi^-$ channel, we use a double Gaussian with a common mean to model the M_{bc} distribution and a triple Gaussian with a common mean to model the ΔE distribution. Because the ΔE and M_{bc} distributions of the $q\bar{q}$ continuum background and the other B backgrounds are similar, we combine these components and use an ARGUS function [22] to describe M_{bc} and a second-order polynomial to describe ΔE . To model the combinatorial background caused by $B^0 \rightarrow p\bar{\Lambda}\pi^-$, we use a 2D nonparametric PDF using Kernel Estimation [23] obtained from MC simulation. The free parameters in the fit are yields of the four components and the shape parameter of the ARGUS function.

Figure 2 shows projections of the fit of Eq. (2) to data. We obtain signal yields of $N_{s1} = 50_{-17}^{+18}$ with a significance of 3.0σ including the relevant systematic uncertainty and $N_{s2} = 216 \pm 17$. The value of the significance is defined

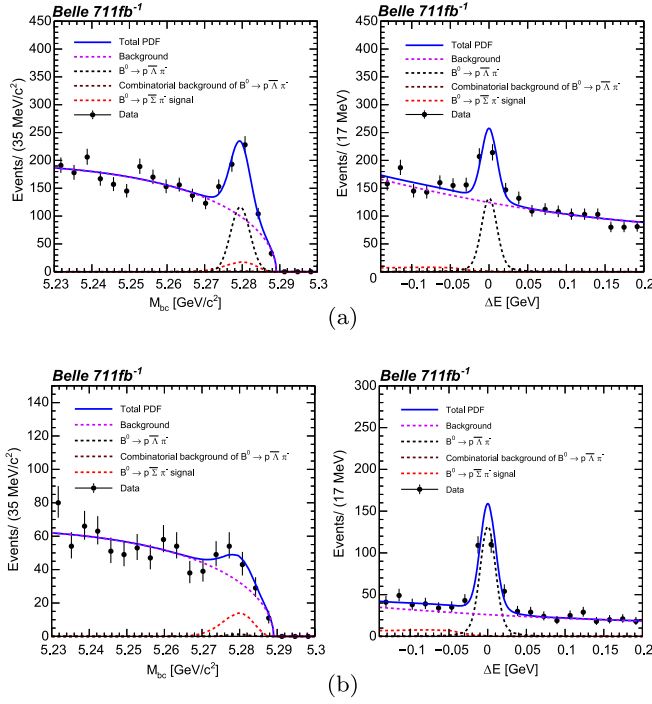


FIG. 2. Projections of the fit results on M_{bc} (left) and ΔE (right) distributions of the selected candidates (data points with error bars). Curves represent the components of the PDF in Eq. (2): $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ signal (red dashed line), combinatorial background from $B^0 \rightarrow p\bar{\Lambda}\pi^-$ (brown dashed line), $B^0 \rightarrow p\bar{\Lambda}\pi^-$ signal (black dashed line), background (purple dashed line), and total PDF (blue solid line). (a) The projected regions are the fitted regions: $\Delta E \in (-0.14, 0.2)$ GeV for the left column and $M_{bc} \in (5.23, 5.30)$ GeV/ c^2 for the right column. (b) The projected regions are $\Delta E \in (-0.14, -0.05)$ GeV for the left column and $M_{bc} \in (5.26, 5.30)$ GeV/ c^2 for the right column to enhance the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ PDF component.

by $\sqrt{-2\ln[\mathcal{L}(\theta_0)/\mathcal{L}(\hat{\theta}_0)]}$, where $\mathcal{L}(\theta_0)$ is the value of the likelihood function when the respective yield θ_0 is set to 0 and $\mathcal{L}(\hat{\theta}_0)$ when it is allowed to vary. In order to include the relevant systematic uncertainty in the significance calculation are smeared by using the uncertainty due to the PDF modeling described later. We also perform a fit in the TE region of $M_{p\bar{\Lambda}} < 2.8$ GeV/ c^2 , which is shown in Fig. 3. In this region, we obtain signal yields of $N_{s1} = 37^{+12}_{-11}$ with a significance of 3.5σ for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ and $N_{s2} = 185 \pm 15$ for $B^0 \rightarrow p\bar{\Lambda}\pi^-$. The concentration of signal events in the TE region indicates that the TE effect also exists in $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ decay. Because of the exclusion of soft photon in reconstruction of the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ channel, the ΔE distribution of that channel locates mostly in the negative ΔE region. We fit the regions of ΔE and M_{bc} at $\Delta E \in (-0.14, -0.05)$ GeV and $M_{bc} \in (5.26, 5.30)$ GeV/ c^2 to enhance the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ signal PDFs in Figs. 2 and 3.

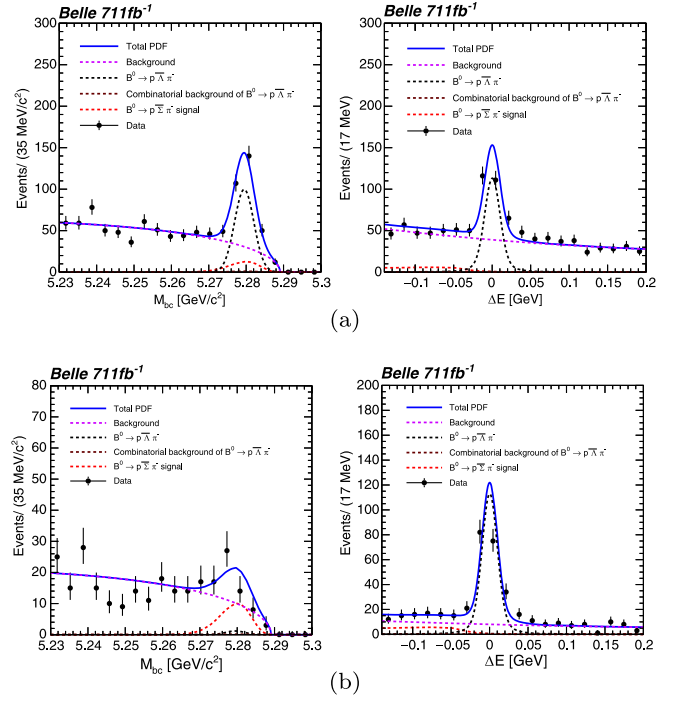


FIG. 3. The data points and curves shown are the same as those in Fig. 2, but with an additional selection $M_{p\bar{\Lambda}} < 2.8$ GeV/ c^2 applied.

The branching fraction is calculated as

$$\mathcal{B} = \frac{N_{\text{sig}}}{N_{B\bar{B}}\epsilon\mathcal{C}_{\text{PID}}\mathcal{C}_{\text{bkg}}}, \quad (3)$$

where N_{sig} is the number of signal events, $N_{B\bar{B}} = 772 \times 10^6$ is the number of $B\bar{B}$ pairs, ϵ denotes the signal efficiency obtained from signal MC samples, and \mathcal{C}_{PID} , \mathcal{C}_{bkg} are efficiency calibration factors for the particle identification and the continuum suppression obtained from data, respectively. \mathcal{C}_{PID} is calculated as $\mathcal{C}_p\text{ID}\mathcal{C}_{\pi\text{ID}}$, where $\mathcal{C}_p\text{ID}$ is the calibration factor for proton identification determined from a $\Lambda \rightarrow p\pi$ control sample, and $\mathcal{C}_{\pi\text{ID}}$ is the calibration factor for charged-pion identification determined from a large $D^{*+} \rightarrow D^0(K^-\pi^+)\pi^+$ control sample. \mathcal{C}_{bkg} is the calibration factor for the $q\bar{q}$ continuum background suppression using the neural-network classifier that is obtained using large $B^0 \rightarrow D^-\pi^+$ and $D^- \rightarrow K_S^0\pi^-$ control samples. The calibration factors are summarized in Table I.

TABLE I. Summary of efficiency calibration factors.

Source	$B^0 \rightarrow p\bar{\Lambda}\pi^-$	$B^0 \rightarrow p\bar{\Sigma}^0\pi^-$
Proton ID	0.95 ± 0.01	0.94 ± 0.01
Pion ID	0.94 ± 0.01	0.94 ± 0.01
$q\bar{q}$ continuum suppression	0.99 ± 0.02	0.99 ± 0.02
Total factor	0.88 ± 0.02	0.88 ± 0.02

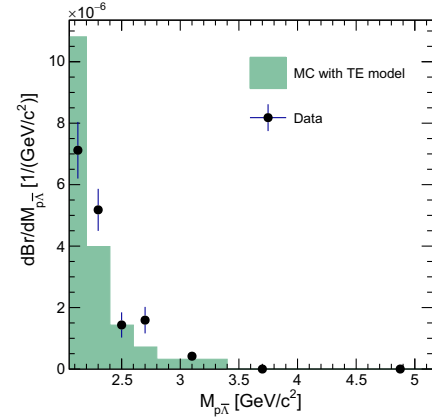
TABLE II. Systematic uncertainties.

Source	$B^0 \rightarrow p\bar{\Lambda}\pi^-$	$B^0 \rightarrow p\bar{\Sigma}^0\pi^-$
Number of $B\bar{B}$	1.4%	1.4%
Tracking	1.4%	1.4%
Proton ID	0.6%	0.6%
Pion ID	0.7%	0.7%
$\mathcal{B}(\Lambda \rightarrow p\pi^-)$	0.8%	0.8%
Λ selection	3.4%	3.4%
$q\bar{q}$ continuum suppression	2.4%	2.4%
PDF modeling	1.4%	3.3%
Total uncertainty	5.0%	5.8%

Different sources of systematic uncertainty are considered in this study. The independent uncertainties are summed in quadrature. The uncertainty on the number of $B\bar{B}$ pairs is 1.4%. The uncertainty from charged-particle tracking is 0.35% per track which is obtained from studying a sample of partially reconstructed $D^{*+} \rightarrow D^0(\pi^-\pi^+K_S^0)\pi^+$ events. The uncertainty from proton identification is 0.6% for $B^0 \rightarrow p\bar{\Lambda}\pi^-$ and $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$. The uncertainty from pion identification is 0.7% for $B^0 \rightarrow p\bar{\Lambda}\pi^-$ and $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$. The uncertainty from the Λ selection is 3.4%, which is obtained from a control sample of $B^+ \rightarrow \Lambda\bar{K}^+$ events. The uncertainty from the suppression of $q\bar{q}$ continuum background is 2.5%, which is estimated using a control sample of $B^0 \rightarrow D^-\pi^+(D^- \rightarrow K_S^0\pi^-)$ events, which have a final state that is topologically similar to $B^0 \rightarrow p\bar{\Lambda}\pi^-$. The uncertainty on the $\Lambda \rightarrow p\pi^-$ branching fraction is taken from the world average value [24]. The uncertainties due to the choice of model functions in the PDF in Eq. (2) are 1.4% for $B^0 \rightarrow p\bar{\Lambda}\pi^-$ and 3.3% for $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ obtained by shifting the fixed parameters of the $B^0 \rightarrow p\bar{\Lambda}^0\pi^-$ signal PDF P_{s2} by 1σ , by changing the bin width of the histogram used to model the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ signal PDF P_{s1} , and by changing the background PDF P_b

TABLE III. Measured partial branching fractions $\mathcal{B}(10^{-6})$ in different $M_{p\bar{\Lambda}}$ bins.

$M_{p\bar{\Lambda}}(\text{GeV}/c^2)$	$B^0 \rightarrow p\bar{\Lambda}\pi^-$	$B^0 \rightarrow p\bar{\Sigma}^0\pi^-$
<2.2	$1.04^{+0.14}_{-0.13}$	$0.27^{+0.12}_{-0.11}$
2.2–2.4	$1.04^{+0.14}_{-0.13}$	$0.24^{+0.14}_{-0.12}$
2.4–2.6	$0.29^{+0.09}_{-0.07}$	$0.13^{+0.13}_{-0.12}$
2.6–2.8	$0.32^{+0.09}_{-0.08}$	$0.12^{+0.13}_{-0.11}$
2.8–3.4	$0.25^{+0.08}_{-0.07}$	$0.29^{+0.19}_{-0.18}$
3.4–4.0	$0.11^{+0.06}_{-0.05}$	$-0.22^{+0.14}_{-0.12}$
4.0–4.6	$0.07^{+0.06}_{-0.05}$	$0.23^{+0.20}_{-0.17}$
>4.6	$0.09^{+0.09}_{-0.07}$	$0.11^{+0.20}_{-0.18}$
<2.8	$2.69^{+0.24}_{-0.21}$	$0.76^{+0.26}_{-0.23}$
Full region	$3.21^{+0.28}_{-0.25}$	$1.17^{+0.43}_{-0.40}$

FIG. 4. Differential branching fraction for $B^0 \rightarrow p\bar{\Lambda}\pi^-$ as a function of $M_{p\bar{\Lambda}}$ (data points with statistical uncertainties). The shaded histogram represents the distribution obtained from the TE MC data sample.

from second-order polynomial to third-order polynomial. The systematic uncertainties are summarized in Table II.

To study the $M_{p\bar{\Lambda}}$ dependence of the efficiencies and the branching fractions, we fit Eq. (2) in narrow $M_{p\bar{\Lambda}}$ bins, and obtain the partial branching fractions based on Eq. (3). The results are listed in Table III. We sum these partial branching fractions in the full $M_{p\bar{\Lambda}}$ region to obtain $\mathcal{B}(B^0 \rightarrow p\bar{\Lambda}\pi^-) = (3.21^{+0.28}_{-0.25}(\text{stat}) \pm 0.16(\text{syst})) \times 10^{-6}$ and $\mathcal{B}(B^0 \rightarrow p\bar{\Sigma}^0\pi^-) = (1.17^{+0.43}_{-0.40}(\text{stat}) \pm 0.07(\text{syst})) \times 10^{-6}$. In Fig. 4, we only show the $M_{p\bar{\Lambda}}$ dependence of $\mathcal{B}(B^0 \rightarrow p\bar{\Lambda}\pi^-)$ because the yield of $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ is insufficient to obtain precise differential branching fractions.

Using a similar approach, we study the branching fraction of $B^0 \rightarrow p\bar{\Lambda}\pi^-$ as a function of $\cos\theta_p$, where θ_p is the angle between the proton and the pion in the baryon pair rest frame. Table IV lists the partial branching fractions for $B^0 \rightarrow p\bar{\Lambda}\pi^-$ and $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ in each $\cos\theta_p$ bin. Figure 5 shows the $\cos\theta_p$ dependence of $\mathcal{B}(B^0 \rightarrow p\bar{\Lambda}\pi^-)$. Our measurement confirms the asymmetry of this distribution observed by the previous measurement [3].

In conclusion, we measure the branching fraction of $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ for the first time to be $\mathcal{B}(B^0 \rightarrow p\bar{\Sigma}^0\pi^-) = (1.17^{+0.43}_{-0.40}(\text{stat}) \pm 0.07(\text{syst})) \times 10^{-6}$ with a significance of

TABLE IV. Measured partial branching fractions $\mathcal{B}(10^{-6})$ in the TE region and different $\cos\theta_p$ bins.

$\cos\theta_p$	$B^0 \rightarrow p\bar{\Lambda}\pi^-$	$B^0 \rightarrow p\bar{\Sigma}^0\pi^-$
−1.0 to 0.6	$0.79^{+0.14}_{-0.13}$	$0.20^{+0.13}_{-0.12}$
−0.6 to 0.2	$0.70^{+0.12}_{-0.11}$	$0.23^{+0.11}_{-0.10}$
−0.2 to 0.2	$0.64^{+0.11}_{-0.10}$	$0.09^{+0.11}_{-0.10}$
0.2 to 0.6	$0.44^{+0.09}_{-0.08}$	$0.17^{+0.11}_{-0.10}$
0.6 to 1.0	$0.25^{+0.07}_{-0.06}$	$0.05^{+0.11}_{-0.10}$

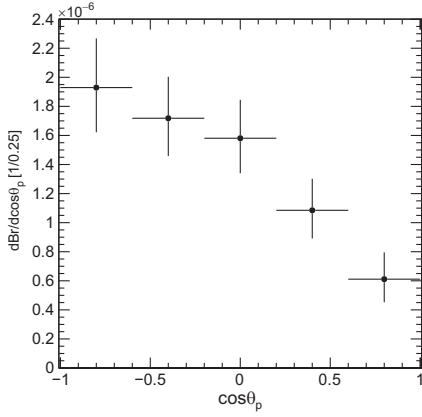


FIG. 5. Differential branching fraction for $B^0 \rightarrow p\bar{\Lambda}\pi^-$ as a function of $\cos\theta_p$ in the baryon-pair rest frame.

3.0σ . For the yield in the TE region, we obtain a slightly larger significance of 3.5σ . Both significances take into account systematic uncertainties. The $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ signal yield is concentrated in the TE region indicating that a threshold enhancement is also present in the $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ channel. For the $B^0 \rightarrow p\bar{\Lambda}\pi^-$ channel, we measure a branching fraction of $(3.21^{+0.28}_{-0.25}(\text{stat}) \pm 0.16(\text{syst})) \times 10^{-6}$ which supersedes the previous measurement [3], and the systematic uncertainty due to the normalized mode $B^0 \rightarrow p\bar{\Lambda}\pi^-$ in the LHCb rare baryonic decay measurement could be improved by 20%. We also study the differential branching fraction as a function of $M_{p\bar{\Lambda}}$ and $\cos\theta_p$, and observe an asymmetric distribution in $\cos\theta_p$. Our study also shows that $B^0 \rightarrow p\bar{\Sigma}^0\pi^-$ has a lower branching fraction than $B^0 \rightarrow p\bar{\Lambda}\pi^-$ which is in contrast to the QCD model prediction [5,6], but more close to the modified approach [7].

ACKNOWLEDGMENTS

This work, based on data collected using the Belle detector, which was operated until June 2010, was supported by the Ministry of Education, Culture, Sports, Science, and Technology (MEXT) of Japan, the Japan Society for the Promotion of Science (JSPS), and the Tau-Lepton Physics Research Center of Nagoya University; the Australian Research Council including Grants No. DP210101900, No. DP210102831, No. DE220100462, No. LE210100098, and No. LE230100085; Austrian Federal Ministry of Education, Science and Research (FWF) and FWF Austrian Science Fund No. P 31361-N36; National Key R&D Program of China under Contract No. 2022YFA1601903, National Natural Science

Foundation of China and Research Grants No. 11575017, No. 11761141009, No. 11705209, No. 11975076, No. 12135005, No. 12150004, No. 12161141008, and No. 12175041, and Shandong Provincial Natural Science Foundation Project ZR2022JQ02; the Ministry of Education, Youth and Sports of the Czech Republic under Contract No. LTT17020; the Czech Science Foundation Grant No. 22-18469S; Horizon 2020 ERC Advanced Grant No. 884719 and ERC Starting Grant No. 947006 “InterLeptons” (European Union); the Carl Zeiss Foundation, the Deutsche Forschungsgemeinschaft, the Excellence Cluster Universe, and the VolkswagenStiftung; the Department of Atomic Energy (Project Identification No. RTI 4002) and the Department of Science and Technology of India; the Istituto Nazionale di Fisica Nucleare of Italy; National Research Foundation (NRF) of Korea Grants No. 2016R1D1A1B02012900, No. 2018R1A2B3003643, No. 2018R1A6A1A06024970, No. RS202200197659, No. 2019R1I1A3A01058933, No. 2021R1A6A1A-03043957, No. 2021R1F1A1060423, No. 2021R1F1A-1064008, and No. 2022R1A2C1003993; Radiation Science Research Institute, Foreign Large-size Research Facility Application Supporting project, the Global Science Experimental Data Hub Center of the Korea Institute of Science and Technology Information and KREONET/GLORIAD; the Polish Ministry of Science and Higher Education and the National Science Center; the Ministry of Science and Higher Education of the Russian Federation, Agreement 14.W03.31.0026, and the HSE University Basic Research Program, Moscow; University of Tabuk Research Grants No. S-1440-0321, No. S-0256-1438, and No. S-0280-1439 (Saudi Arabia); the Slovenian Research Agency Grants No. J1-9124 and No. PI-0135; Ikerbasque, Basque Foundation for Science, Spain; the Swiss National Science Foundation; the Ministry of Education and the Ministry of Science and Technology of Taiwan; and the United States Department of Energy and the National Science Foundation. These acknowledgements are not to be interpreted as an endorsement of any statement made by any of our institutes, funding agencies, governments, or their representatives. We thank the KEKB group for the excellent operation of the accelerator; the KEK cryogenics group for the efficient operation of the solenoid; and the KEK computer group and the Pacific Northwest National Laboratory (PNNL) Environmental Molecular Sciences Laboratory (EMSL) computing group for strong computing support; and the National Institute of Informatics, and Science Information NETwork 6 (SINET6) for valuable network support.

- [1] K. Abe *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **88**, 181803 (2002).
- [2] Ed. A. Bevan, B. Golob, T. Mannel, S. Prell, and B. Yabsley (Belle Collaboration), *Eur. Phys. J. C* **74**, 3026 (2014).
- [3] M.-Z. Wang, Y.-J. Lee *et al.* (Belle Collaboration), *Phys. Rev. D* **76**, 052004 (2007).
- [4] K. Lingel, T. Skwarnicki, and J. G. Smith, *Annu. Rev. Nucl. Part. Sci.* **48**, 253 (1998).
- [5] H.-Y. Cheng and K.-C. Yang, *Phys. Rev. D* **66**, 014020 (2002).
- [6] C.-K. Chua, W.-S. Hou, and S.-Y. Tsai, *Phys. Rev. D* **66**, 054004 (2002).
- [7] C.-K. Chua and W.-S. Hou, *Eur. Phys. J. C* **29**, 27 (2003).
- [8] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **119**, 041802 (2017).
- [9] S. Kurokawa and E. Kikutani, *Nucl. Instrum. Methods Phys. Res., Sect. A* **499**, 1 (2003).
- [10] T. Abe *et al.*, *Prog. Theor. Exp. Phys.* **2013**, 03A001 (2013).
- [11] A. Abashian *et al.* (Belle Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **479**, 117 (2002).
- [12] J. Brodzicka *et al.*, *Prog. Theor. Exp. Phys.* **2012**, 04D001 (2012).
- [13] D. J. Lange, *Nucl. Instrum. Methods Phys. Res., Sect. A* **462**, 152 (2001).
- [14] R. Brun, F. Bruyant, M. Maire, A. C. McPherson, and P. Zanarini, Report No. CERN-DD-EE-84-1, 1987.
- [15] M.-Z. Wang *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **90**, 201802 (2003).
- [16] E. Nakano, *Nucl. Instrum. Methods Phys. Res., Sect. A* **494**, 402 (2002).
- [17] M. Feindt and U. Kerzel, *Nucl. Instrum. Methods Phys. Res., Sect. A* **559**, 190 (2006).
- [18] G. C. Fox and S. Wolfram, *Phys. Rev. Lett.* **41**, 1581 (1978).
- [19] K. Abe *et al.* (Belle Collaboration), *Phys. Lett. B* **511**, 151 (2001).
- [20] J. D. Bjorken and S. J. Brodsky, *Phys. Rev. D* **1**, 1416 (1970).
- [21] H. Kakuno *et al.* (Belle Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **533**, 516 (2004).
- [22] H. Albrecht *et al.* (ARGUS Collaboration), *Phys. Lett. B* **241**, 278 (1990).
- [23] K. S. Cranmer, *Comput. Phys. Commun.* **136**, 198 (2001).
- [24] R. L. Workman *et al.* (Particle Data Group), *Prog. Theor. Exp. Phys.* **2022**, 083C01 (2022).