

Probing compressed mass spectra in the type-II seesaw model at the LHC

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Despite a great deal of effort in searching for the tripletlike Higgses in the type-II seesaw model, evidence for their production is yet to be found at the LHC. As such, one might be in the balance regarding this model's relevance at the electroweak scale. In this work, we peruse a scenario, akin to compressed mass spectra in supersymmetry, which might have eluded the experimental searches thus far. We perform a multivariate analysis to distinguish signals with a pair of same-sign leptons with low invariant mass from the Standard Model processes, including those accruing from *fake* leptons and electron charge misidentification, and find that a significant part of the hitherto unconstrained parameter space could be probed with the already collected run 2 13 TeV LHC and future HL-LHC data.

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I. INTRODUCTION

The type-II seesaw model [1–6], extending the Standard Model (SM) with an $SU(2)_L$ triplet scalar field with hypercharge $Y = 1$, offers a tenable explanation for the observed neutrino masses and mixings; as such, it is arguably the most widely studied neutrino mass model [7–70]. This model accommodates, in addition to the 125 GeV Higgs, several other physical states: doubly charged scalar ($H^{\pm\pm}$), singly charged scalar (H^\pm), and CP -even and CP -odd neutral scalars (H^0 and A^0). The phenomenology of these states, particularly $H^{\pm\pm}$, has been studied extensively at the Large Hadron Collider (LHC) [7–47], electron colliders [48–56], muon colliders [57–60], and electron-proton colliders [61,62]; see Refs. [44,63,64] for comprehensive reviews. Experimental collaborations have performed several searches for $H^{\pm\pm}$ [71–82], and nonobservations of any significant excess over the SM expectations have led to stringent limits on them. While the ATLAS Collaboration has set a lower limit of 1020 GeV for $H^{\pm\pm}$ decaying into $\ell^\pm\ell^\pm$ (with $\ell = e, \mu$) [82], the CMS Collaboration has set a lower limit of 535 GeV for those decaying into $\tau^\pm\tau^\pm$ [76]. For $H^{\pm\pm}$ decaying into $W^\pm W^\pm$,

the ATLAS Collaboration has excluded them within the mass range 200–350 GeV [81].

Recently, Ref. [44] has estimated exclusion limits on $m_{H^{\pm\pm}}$ for a vast model parameter space, characterized by the mass splitting $\Delta m = m_{H^{\pm\pm}} - m_{H^\pm}$ and the triplet vacuum expectation value (VEV) v_t , by recasting several searches performed by the CMS and ATLAS Collaborations.¹ The regions corresponding to $\Delta m = 0$ and $\Delta m < 0$, being dominated with the so-called “golden decays” of $H^{\pm\pm}$ to $\ell^\pm\ell^\pm$ and $W^\pm W^\pm$, are highly constrained by the LHC searches, as such $H^{\pm\pm}$ up to 1115 (420) GeV masses are excluded for small (large) v_t . On the other hand, a significantly large part of the model parameter space characterized by $\Delta m \sim \mathcal{O}(10)$ GeV and $v_t \sim \mathcal{O}(10^{-7})$ – $\mathcal{O}(10^{-3})$ is largely unconstrained by the existing LHC searches. A detailed analysis for probing this region at future e^-e^+ colliders has been performed in Ref. [55]. This region is dominated by the exclusive decays to one or more off-shell W^\pm bosons and H^0/A^0 . While the latter decays to $\nu\nu$ for $v_t \leq \mathcal{O}(10^{-4})$ and to $b\bar{b}, t\bar{t}, ZZ, Zh, hh$ for $v_t \geq \mathcal{O}(10^{-4})$, the former results in leptons and jets with relatively low transverse momentum (p_T), termed as soft leptons and soft jets.

The present work concerns part of the above-mentioned unconstrained region where H^0/A^0 exclusively decays to $\nu\nu$. Therefore, the resulting final state is populated with soft leptons and jets and low missing transverse momentum

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¹For $H^{\pm\pm}$ decaying into $W^\pm W^\pm$, Ref. [44] estimates an improved exclusion range of 200–400 GeV compared to 200–350 GeV obtained by the ATLAS Collaboration in Ref. [81].

(p_T^{miss}). Typically, these are beset with oversized background contributions from quantum chromodynamics (QCD) multijet, multitop, and Drell-Yan processes and, thus, are not highly sensitive to new physics searches. Such signals, akin to those appearing in compressed mass spectra in supersymmetry, in principle, can be distinguished from the SM background by requiring either a jet with large p_T from initial state radiation that leads to a high boost of the decaying particle pair and, thus, large p_T^{miss} [83,84] or two or more soft leptons along with large p_T^{miss} [85,86]. However, as it turns out, the requirement of an energetic jet or large p_T^{miss} exceedingly reduces the signal rate, thereby making such searches insensitive to the present model [44]. Keeping this in mind, we relax the aforementioned requirement to retain signal acceptance and require only a pair of same-sign leptons with low invariant mass. We perform a multivariate analysis to distinguish such characteristic signal from the SM background, including those arising from *fake* leptons and electron charge misidentification.

The rest of this work is structured as follows. We briefly outline the type-II seesaw model in Sec. II, followed by a detailed collider analysis in Sec. III and a summary in Sec. IV.

II. THE HIGGS TRIPLET

In addition to the SM field content, the type-II seesaw model employs an $SU(2)_L$ triplet scalar field with $Y = 1$:

$$\Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}.$$

The scalar potential involving Δ and the SM Higgs doublet $\Phi = (\Phi^+ \ \Phi^0)^T$ is given by [67]

$$\begin{aligned} V(\Phi, \Delta) = & -m_\Phi^2 \Phi^\dagger \Phi + \frac{\lambda}{4} (\Phi^\dagger \Phi)^2 + m_\Delta^2 \text{Tr}(\Delta^\dagger \Delta) \\ & + [\mu (\Phi^T i \sigma^2 \Delta^\dagger \Phi) + \text{H.c.}] + \lambda_1 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) \\ & + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[(\Delta^\dagger \Delta)^2] + \lambda_4 \Phi^\dagger \Delta \Delta^\dagger \Phi, \end{aligned}$$

where m_Φ^2 , m_Δ^2 , and μ are the mass parameters and λ and λ_i ($i = 1, \dots, 4$) are the dimensionless quartic couplings. The neutral components Φ^0 and Δ^0 procure respective VEVs v_d and v_t such that $\sqrt{v_d^2 + 2v_t^2} = 246$ GeV. For a detailed description of the main dynamical features of the scalar potential, see Ref. [67]. After the electroweak symmetry breaking, mixing of the identically charged states results in several physical states:

- (i) Φ^0 and Δ^0 mix into two CP -even states (h and H^0) and two CP -odd states (G^0 and A^0);
- (ii) Φ^\pm and Δ^\pm mix into two mass states G^\pm and H^\pm ;
- (iii) $\Delta^{\pm\pm}$ is aligned with its mass state $H^{\pm\pm}$.

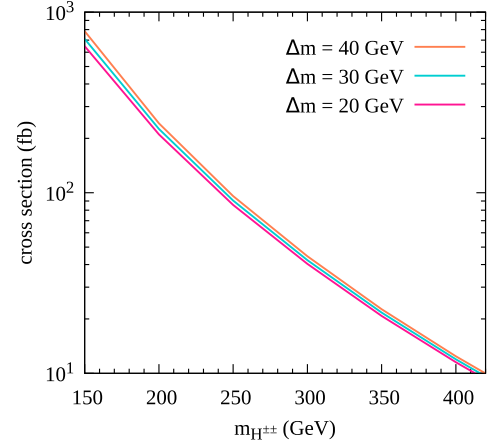


FIG. 1. LO total cross section for $pp \rightarrow H^{++}H^{--}$ and $pp \rightarrow H^{\pm\pm}H^\mp$ for $\Delta m = 20, 30,$ and 40 GeV.

G^0 and G^\pm are the *would-be* Nambu-Goldstone bosons, h is identified as the 125 GeV Higgs observed at the LHC, and the rest follows the sum rule

$$m_{H^{\pm\pm}}^2 - m_{H^\pm}^2 \approx m_{H^\pm}^2 - m_{H^0/A^0}^2 \approx -\frac{\lambda_4}{4} v_d^2.$$

The Yukawa interaction $Y_{ij}^\nu L_i^T C i \sigma^2 \Delta L_j$ (L_i stands for the SM lepton doublet, with $i \in e, \mu, \tau$, and C the charge-conjugation operator) induces masses for the neutrinos:

$$m_\nu = \sqrt{2} Y^\nu v_t.$$

The tripletlike Higgses are pair produced at the LHC via the neutral and charged current Drell-Yan mechanisms²:

$$\begin{aligned} q\bar{q} & \rightarrow \gamma^*/Z^* \rightarrow H^{++}H^{--}, H^+H^-, H^0A^0, \\ qq' & \rightarrow W^{\pm*} \rightarrow H^{\pm\pm}H^\mp, H^\pm H^0, H^\pm A^0. \end{aligned}$$

We evaluate the leading-order (LO) cross sections using the SARAH 4.14.4 [87,88] generated UFO [89] modules in MadGraph5_aMC_v2.7.3 [90,91] with the NNPDF23_LO_AS_0130_QED parton distribution function [92,93]. Figure 1 shows the LO total production cross section for $pp \rightarrow H^{++}H^{--}$ and $pp \rightarrow H^{\pm\pm}H^\mp$ at the 13 TeV LHC as a function of $m_{H^{\pm\pm}}$ for $\Delta m = 20, 30,$ and 40 GeV. For brevity, we do not include the other processes, as they do not contribute to the final state considered in Sec. III. Following the QCD corrections estimated in Ref. [94], we naively scale the LO cross section by a next-to-leading-order (NLO) K factor of 1.15.

²They are also produced via t/u -channel photon fusion as well as vector-boson fusion processes. However, such processes are rather subdominant.

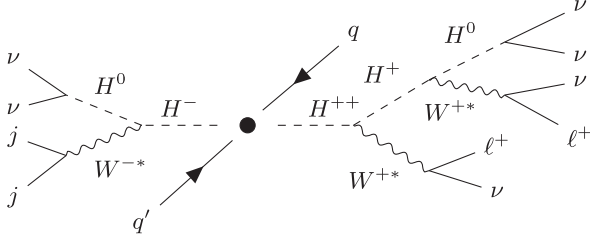


FIG. 2. Schematic diagram for $qq' \rightarrow H^{++}H^{-}$ leading to a pair of same-sign leptons and p_T^{miss} in the final state.

III. COLLIDER ANALYSIS

In broad terms, the phenomenology of this model depends on three parameters, namely, $m_{H^{\pm\pm}}$, v_t , and $\Delta m = m_{H^{\pm\pm}} - m_{H^\pm}$; see Refs. [16,20,44] for detailed discussions. As mentioned earlier, the present work concerns the unconstrained parameters space characterized by $\Delta m \sim \mathcal{O}(10)$ GeV and $v_t \lesssim \mathcal{O}(10^{-4})$, where $H^{\pm\pm}$ and H^\pm exclusively decay into off-shell W^\pm bosons and H^0/A^0 , with the latter further decaying into $\nu\nu$.³ Therefore, the resulting final state is populated with soft leptons and jets and low p_T^{miss} . A pair of same-sign leptons constitute the final state signature of the search presented in this work; see Fig. 2.

In the following, we briefly outline the relevant SM background processes, the selection of various physics objects, and event selection and then perform a multivariate analysis to distinguish the signal from background.

A. SM backgrounds

The final state with a pair of same-sign leptons is beset with fewer SM background contributions compared to other final states with leptons and jets. However, for the present analysis, we consider numerous SM processes such as diboson, triboson, and tetraboson processes, Higgsstrahlung processes, single and multitop productions in association with or without gauge bosons, and Drell-Yan processes. All these processes are generated using MadGraph5_aMC_v2.7.3 [90,91] at the LO precision in perturbative QCD, with the *MLM merging* scheme to consolidate additional partons using PYTHIA 8.2 [95], and then naively scaled by appropriate NLO (or higher, whichever is available in the literature) K factors [91,96–110].

The relevant backgrounds can be broadly divided into three categories.

- (i) *Prompt background.*—Particles originating from (very close vicinity of) the primary interaction point constitute this background, with the dominant contributions coming from the diboson and top-pair production processes.

³The analysis presented in this work is largely insensitive to the value of v_t as long as $v_t \lesssim \mathcal{O}(10^{-4})$; thus, we do not commit to a fixed value for v_t .

- (ii) *Nonprompt and fake background.*—Processes where a jet is misidentified as a lepton or additional leptons originate from initial and final state radiation (ISR and FSR, respectively) photon conversions and in-flight heavy-flavor decays constitute this background. Though the lepton isolation requirements (mentioned in Sec. III B) significantly subdue this contribution, a considerable fraction passes the object selection. Estimating this contribution requires a data-driven approach, the so-called *fake factor* method, which is beyond the scope of this work. We adopt a conservative approach, assuming a p_T -dependent probability of 0.1%–0.3% for a jet to be misidentified as a lepton [111].
- (iii) *Electron charge misidentification.*—Bremsstrahlung interaction of the electrons with the inner detector material triggering trident events and sniff tracks could lead to charge misidentification. Therefore, a small fraction of prompt background events with a pair of opposite-sign leptons (mainly from Drell-Yan and top-pair production processes) can lead to same-sign leptons in the final states. To account for this effect, all prompt electrons are naively corrected with a p_T - and η -dependent charge misidentification probability: $P(p_T, \eta) = \sigma(p_T) \times f(\eta)$, where $\sigma(p_T)$ and $f(\eta)$ ranges from 0.02 to 0.1 and 0.03 to 1, respectively [112].

B. Object selection

We pass the MadGraph5_aMC_v2.7.3 generated parton-level events into PYTHIA 8.2 [95] to simulate subsequent decays for the unstable particles, ISR and FSR, showering, fragmentation and hadronization and then into DELPHES 3.4.2 with the default CMS card [113] for simulating detector effects as well as reconstructing various physics objects, viz. photons, electrons, muons, and jets.

The jet constituents are clustered using the anti- k_T algorithm [114] with a jet radius $R = 0.4$ as implemented in FastJet 3.3.2 [115]. While the jets are required to be within the pseudorapidity range $|\eta| < 2.4$ and have a transverse momentum $p_T > 20$ GeV, the leptons (electrons and muons) are required to have $|\eta| < 2.5$ and $p_T > 10$ GeV. Furthermore, to ensure that the leptons are isolated, we demand the scalar sum of the p_T 's of all other objects lying within a cone of radius 0.3 (0.4) around an electron (a muon) to be smaller than 10% (15%) of its p_T . Finally, p_T^{miss} is estimated from the momentum imbalance in the transverse direction associated to all reconstructed objects (including photons) in an event.

C. Event selection

The present analysis requires events with a pair of same-sign isolated leptons. For such events, we apply the following preselection requirements.

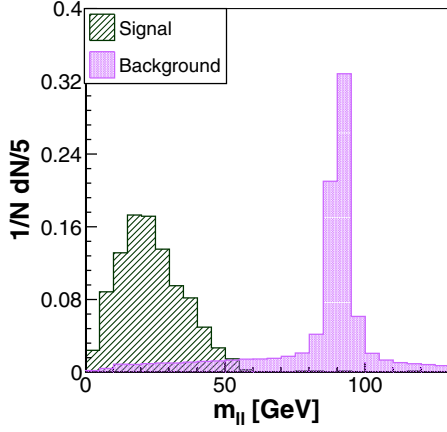


FIG. 3. Normalized distributions of $m_{\ell\ell}$ for the signal (BP1) and background events after the $p_T(\ell_{1,2}) > 15$ GeV selection.

- (i) We reject events with $m_{\ell\ell} \in [3, 3.2]$ GeV to lessen the contribution from J/ψ resonance. No veto is applied around other resonances like Υ or Ψ , as these contributions are rather subdominant.
- (ii) We require $m_{\ell\ell} > 1$ GeV and the angular separation between the leptons $\Delta R_{\ell\ell} > 0.05$ to suppress the nearly collinear lepton pairs resulting from ISR and FSR photon conversions or spurious pairs of tracks with shared hits from muon bremsstrahlung interactions.
- (iii) Leptons are required to be separated from the reconstructed jets by $\Delta R_{\ell,j} > 0.4$. This, along with the lepton isolation requirements, suppresses non-prompt leptons from in-flight heavy-flavor decays.
- (iv) Both the leptons are required to have $p_T > 15$ GeV. Though this is at par with the dilepton triggers used in 2015 in the run 2 LHC [116], a little higher p_T thresholds have been used [117,118] in the later years. A trigger with higher p_T thresholds would reduce the signal acceptance. Therefore, to retain the signal rate, a “combined” trigger with $p_T(\ell_{1,2}) > 15$ GeV and the dilepton invariant mass $m_{\ell\ell} < 60$ GeV can be used.

Shown in Fig. 3 are the normalized distributions of $m_{\ell\ell}$ for the signal and background events after the $p_T(\ell_{1,2}) > 15$ GeV selection. The signal events are shown for a benchmark defined by

$$\text{BP1} : m_{H^{\pm\pm}} = 200 \text{ GeV}, \quad \Delta m = 30 \text{ GeV}.$$

For the signal, it falls rapidly with an end point near 60 GeV as occasioned by the compressed mass spectrum considered in BP1. On the contrary, the background boasts a peak at the Z -boson mass with the lion’s share of the contributions accruing from $Z \rightarrow e^-e^+$ due to electron charge misidentification. Not only does the selection $m_{\ell\ell} < 60$ GeV help with the trigger, but it also vanquishes the oversized background contribution.

TABLE I. Summary of optimized BDT hyperparameters.

BDT hyperparameter	Optimized choice
NTrees	500
MinNodeSize	5%
MaxDepth	5
BoostType	AdaBoost
AdaBoostBeta	0.1
UseBaggedBoost	True
BaggedSampleFraction	0.5
SeparationType	GiniIndex
nCuts	20

D. Multivariate analysis

We now perform a multivariate analysis with the boosted decision tree (BDT) classifier implemented in the TMVA 4.3 toolkit [119] integrated into ROOT 6.24 [120] to distinguish the signals from backgrounds. For training and testing the classifier, 10^6 signal events for each $m_{H^{\pm\pm}}$ within the [150,400] GeV range in steps of 50 GeV and at least of worth 3000 fb^{-1} luminosity of background events are fed. Of these, 50% are picked randomly for training, and the rest are used for testing. The classifier is trained with the *adaptive boost* algorithm with a learning rate of 0.1, 500 decision trees with 5% minimum node size, and a depth of five layers per tree into a forest, and the *Gini index* is used for node splitting. The relevant BDT hyperparameters are summarized in Table I.

We use the following kinematic variables as input features to the BDT classifier⁴:

$$p_T(\ell_{1,2}), \quad p_T^{\text{miss}}, \quad m_{\ell\ell}, \quad \Delta R_{\ell\ell},$$

$$\frac{p_T(\ell\ell)}{L_T} \quad \text{and} \quad \Delta\phi(\ell\ell, p_T^{\text{miss}}),$$

where $p_T(\ell\ell)$ is the dilepton system’s p_T and L_T is the scalar sum of all jets and leptons’ p_T . Normalized distributions for some of these features are shown in Fig. 4; the rest are not shown for brevity. These features constitute a minimal set with a good separation power between the signal and background, which is usually measured in terms of the method-unspecific separation and method-specific ranking. For a given feature x , the former is defined as

$$\langle S^2 \rangle = \frac{1}{2} \int \frac{[\hat{x}_S(x) - \hat{x}_B(x)]^2}{\hat{x}_S(x) + \hat{x}_B(x)} dx,$$

where $\hat{x}_S(x)$ and $\hat{x}_B(x)$ are the probability density functions of x for the signal and background, respectively. The method-specific ranking demonstrates the relative

⁴Just like $\Delta R_{\ell\ell}$, the azimuthal separation between the leptons $\Delta\phi_{\ell\ell}$ can be used as an input feature. However, these two variables are highly correlated; thus, we drop the latter.

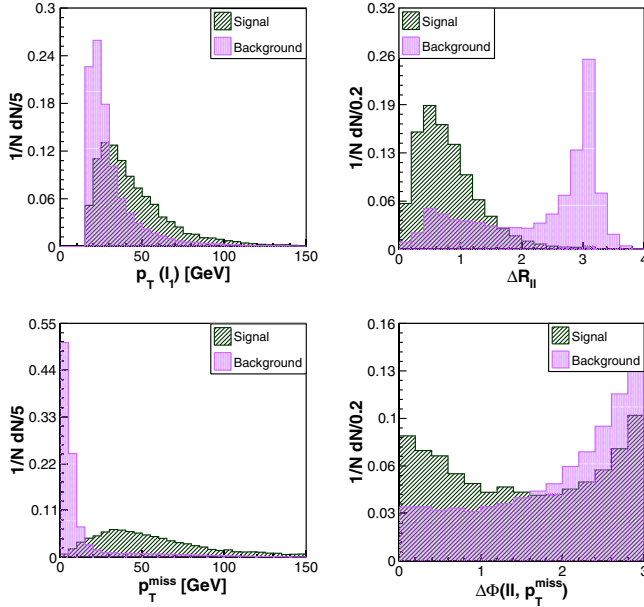


FIG. 4. Normalized distributions for some of the input features. The signal distributions are for BP1.

importance of the input features in separating the signal from background. Both these measures are shown in Table II. As it turns out, $\Delta R_{\ell\ell}$ is the best separating variable, while $p_T(\ell_{1,2})$ are the ones with least separating power. Shown in Fig. 5 is the Pearson linear correlation matrix, with the coefficients defined as

$$\rho(x, y) = \frac{\langle xy \rangle - \langle x \rangle \langle y \rangle}{\sigma_x \sigma_y},$$

where $\langle x \rangle$ and σ_x , respectively, are the expectation value and standard deviation of x . These input features are not highly correlated and, thus, constitute a minimal set. Lastly, the classifier is checked for overtraining by performing the Kolmogorov-Smirnov test which compares the BDT response curves for the training and testing subsamples. The response curves shown in Fig. 6 exhibit no considerable overtraining.

TABLE II. Method-unspecific separation and method-specific ranking of the input features.

Feature	Method-unspecific separation	Method-specific ranking
p_T^{miss}	0.5945	0.214
$\Delta R_{\ell\ell}$	0.4777	0.3015
$\frac{p_T(\ell\ell)}{L_T}$	0.4586	0.2086
$m_{\ell\ell}$	0.368	0.08534
$p_T(\ell_1)$	0.1481	0.04751
$p_T(\ell_2)$	0.08474	0.05806
$\Delta\phi(\ell\ell, p_T^{\text{miss}})$	0.03997	0.08499

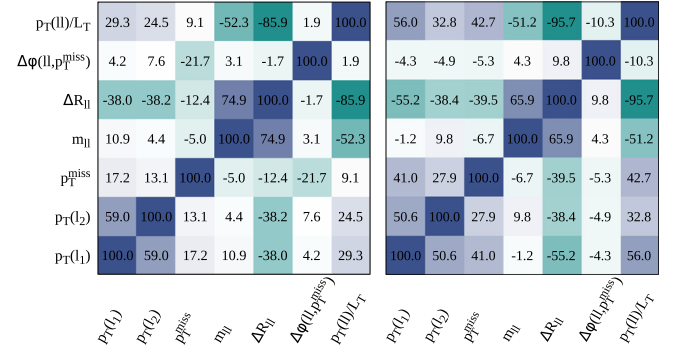


FIG. 5. Correlations in percent among the input features for the signal (left) and background (right).

For brevity, the receiver-operator-characteristic curve quantifying the BDT performance is not shown. Instead, we show the variation of the discovery significance (estimated using the formula given in Sec. III E) as a function of the BDT response for $m_{H^{\pm\pm}} = 200, 300,$ and 400 GeV with $\Delta m = 30$ GeV in Fig. 7. As apparent from this, the discovery significance reaches its maximum for the BDT response of 0.4, albeit irrespective of $m_{H^{\pm\pm}}$, demonstrating the robustness of the BDT classifier's training. Therefore, to maximize the sensitivity of the search, we require

$$\text{BDTresponse} > 0.4.$$

Table III shows the remaining background and signal (for $m_{H^{\pm\pm}} = 200, 300,$ and 400 GeV with $\Delta m = 30$ GeV) cross sections after the above selection.

E. Discovery and exclusion projection

Finally, we estimate the discovery and exclusion projection for different $m_{H^{\pm\pm}}$. The median expected discovery and exclusion significances are estimated as [121–123]

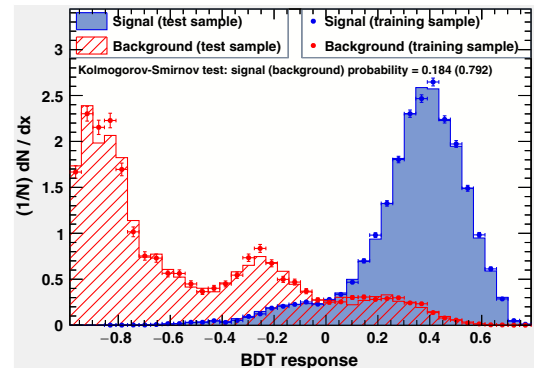


FIG. 6. BDT response curves for the training and testing subsamples.

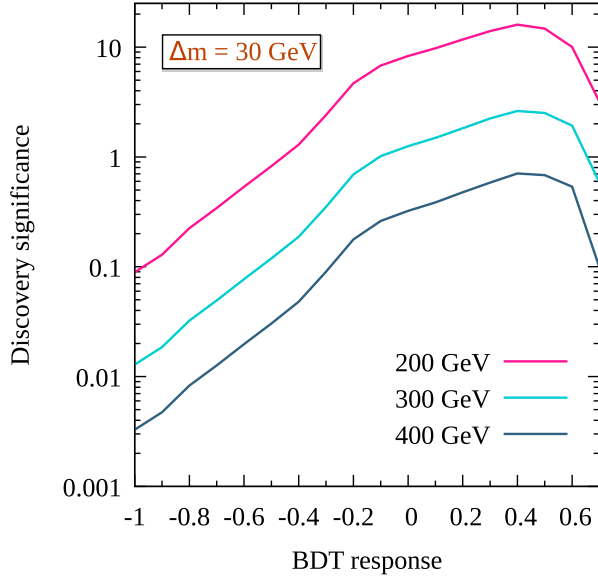


FIG. 7. Discovery significance as a function of the BDT response for $m_{H^{\pm\pm}} = 200, 300,$ and 400 GeV with $\Delta m = 30$ GeV.

$$Z_{\text{dis}} = \left[2 \left((s+b) \ln \left[\frac{(s+b)(b+\delta_b^2)}{b^2 + (s+b)\delta_b^2} \right] - \frac{b^2}{\delta_b^2} \ln \left[1 + \frac{\delta_b^2 s}{b(b+\delta_b^2)} \right] \right) \right]^{1/2},$$

$$Z_{\text{exc}} = \left[2 \left\{ s - b \ln \left(\frac{b+s+x}{2b} \right) - \frac{b^2}{\delta_b^2} \ln \left(\frac{b-s+x}{2b} \right) \right\} - (b+s-x)(1+b/\delta_b^2) \right]^{1/2},$$

where $x = \sqrt{(s+b)^2 - 4sb\delta_b^2/(b+\delta_b^2)}$, s and b are the numbers of signal and background events, respectively, and δ_b is the background uncertainty. Without going into the intricacy of estimating the latter, we assume it to be 20%,

TABLE III. Background and signal cross sections (fb) after the selection: BDT response > 0.4 .

Event sample	Cross section (fb)
γ^*/Z^*	2.6344
$W^\pm Z$	1.4435
$W^\pm W^\pm V$ ($V = W, Z$)	0.7913
$i\bar{i}V$	0.7313
$i\bar{i}$	0.5535
Others	1.0618
Total background	7.2158
Signal: $(m_{H^{\pm\pm}}, \Delta m) = (200, 30)$ GeV	4.6235
Signal: $(m_{H^{\pm\pm}}, \Delta m) = (300, 30)$ GeV	0.6906
Signal: $(m_{H^{\pm\pm}}, \Delta m) = (400, 30)$ GeV	0.1841

albeit conservatively. In Fig. 8, we show the required luminosities (in fb^{-1}) needed to achieve 95% confidence limits (C.L.) (1.645σ) exclusion and 5σ discovery as a function of $m_{H^{\pm\pm}}$ for $\Delta m = 20, 30,$ and 40 GeV. For high $m_{H^{\pm\pm}}$, the signal cross section falls quickly and, thus, the sensitivity.

We find that, for $\Delta m = 30$ GeV, this model could be probed up to $m_{H^{\pm\pm}} = 260(330)$ GeV with 5σ discovery (95% C.L. exclusion) significance with the already collected run 2 LHC data ($\sim 139 \text{ fb}^{-1}$), whereas, for the high-luminosity LHC (HL-LHC) with 3000 fb^{-1} data, this limit extends to $360(420)$ GeV. For a smaller or larger Δm

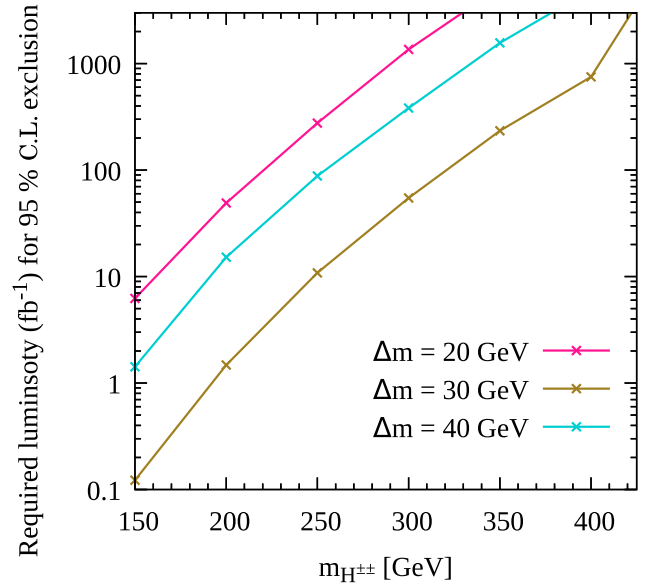
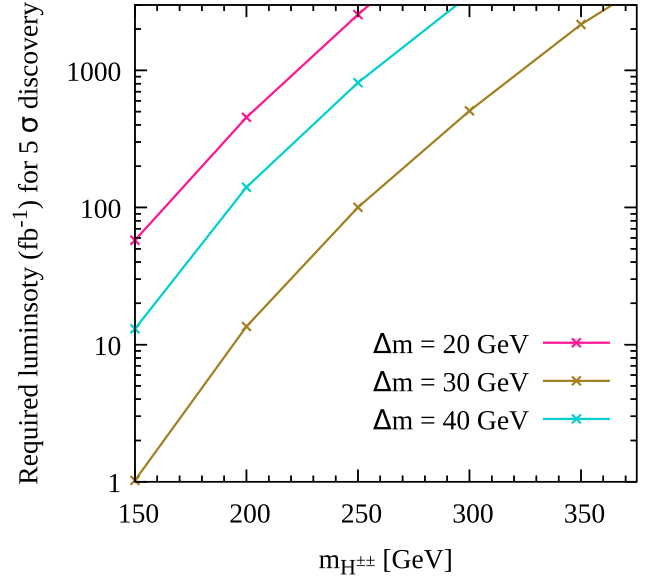


FIG. 8. Required luminosity (fb^{-1}) for 5σ discovery and 95% C.L. exclusion as a function of $m_{H^{\pm\pm}}$ for $\Delta m = 20, 30,$ and 40 GeV.

(say, 20 or 40 GeV), the discovery and exclusion reaches are lower compared to those for $\Delta m = 30$ GeV. Understandably, the BDT classifier, being trained with signals with $\Delta m = 30$ GeV, is not maximally sensitive to other Δm . In addition, for smaller Δm , a significantly large fraction of the leptons emanating from the off-shell W bosons fail to pass the dilepton trigger requirements in Sec. III C, and, thus, the sensitivity is lower.

IV. SUMMARY

Nonobservations of any significant excess over the SM expectation in all the experimental searches looking for doubly charged Higgses thus far have led to stringent limits on them. While interpreted in the context of the type-II seesaw model, the tripletlike Higgses are already excluded up to a few hundred GeV masses for a vast region of the model parameter space [44]. In this work, we peruse a scenario, akin to compressed mass spectra in supersymmetry, which these experimental searches are not sensitive

to and, consequently, is largely unconstrained. We perform a multivariate analysis to distinguish signals with a pair of same-sign leptons with low invariant mass from the SM processes, including those concerning fake leptons and electron charge misidentification, and find that a significant part of the hitherto unconstrained parameter space could be probed with the already collected run 2 LHC and future HL-LHC data.

In closing, we mention that the search strategy presented here is also applicable to other scalar extensions of the SM with compressed mass spectra where the lightest scalar state decays invisibly.

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