

**Erratum: Constraining black-hole binary spin precession  
and nutation with sequential prior conditioning  
[Phys. Rev. D 106, 024019 (2022)]**

Daria Gangardt<sup>1,\*</sup>, Davide Gerosa,<sup>2,3,1</sup> Michael Kesden,<sup>4</sup> Viola De Renzis,<sup>2,3</sup> and Nathan Steinle<sup>1</sup>

<sup>1</sup>*School of Physics and Astronomy & Institute for Gravitational Wave Astronomy,  
University of Birmingham, Birmingham, B15 2TT, United Kingdom*

<sup>2</sup>*Dipartimento di Fisica “G. Occhialini”, Università degli Studi di Milano-Bicocca,  
Piazza della Scienza 3, 20126 Milano, Italy*

<sup>3</sup>*INFN, Sezione di Milano-Bicocca, Piazza della Scienza 3, 20126 Milano, Italy*

<sup>4</sup>*Department of Physics, The University of Texas at Dallas, Richardson, Texas 75080, USA*

(Received 5 April 2023; published 2 May 2023)

DOI: 10.1103/PhysRevD.107.109901

In this paper on measuring binary black-hole spin precession from LIGO-Virgo data, the prior on the parameter  $\Delta\Phi$  was incorrectly sampled, leading to a change in the numerical results. The qualitative conclusions from the original article are not affected, but here, we revise Figs. 1–8 and Table I with the correct samples.

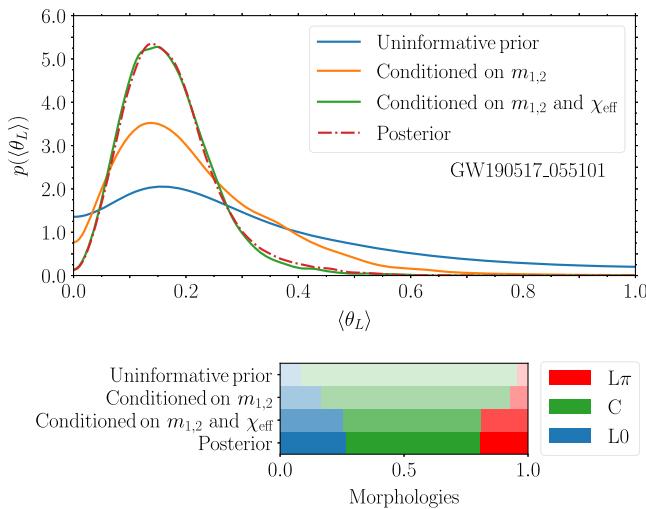


FIG. 1. Revised version of Fig. 1.

\*ddg672@star.sr.bham.ac.uk

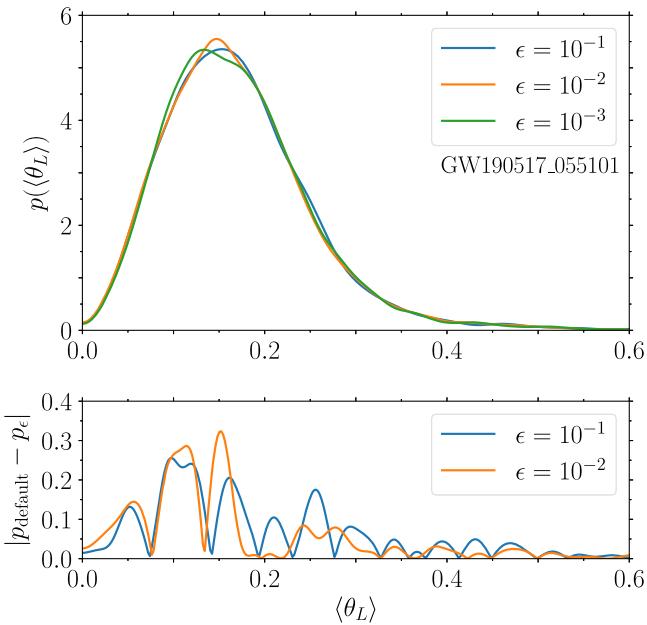


FIG. 2. Revised version of Fig. 2.

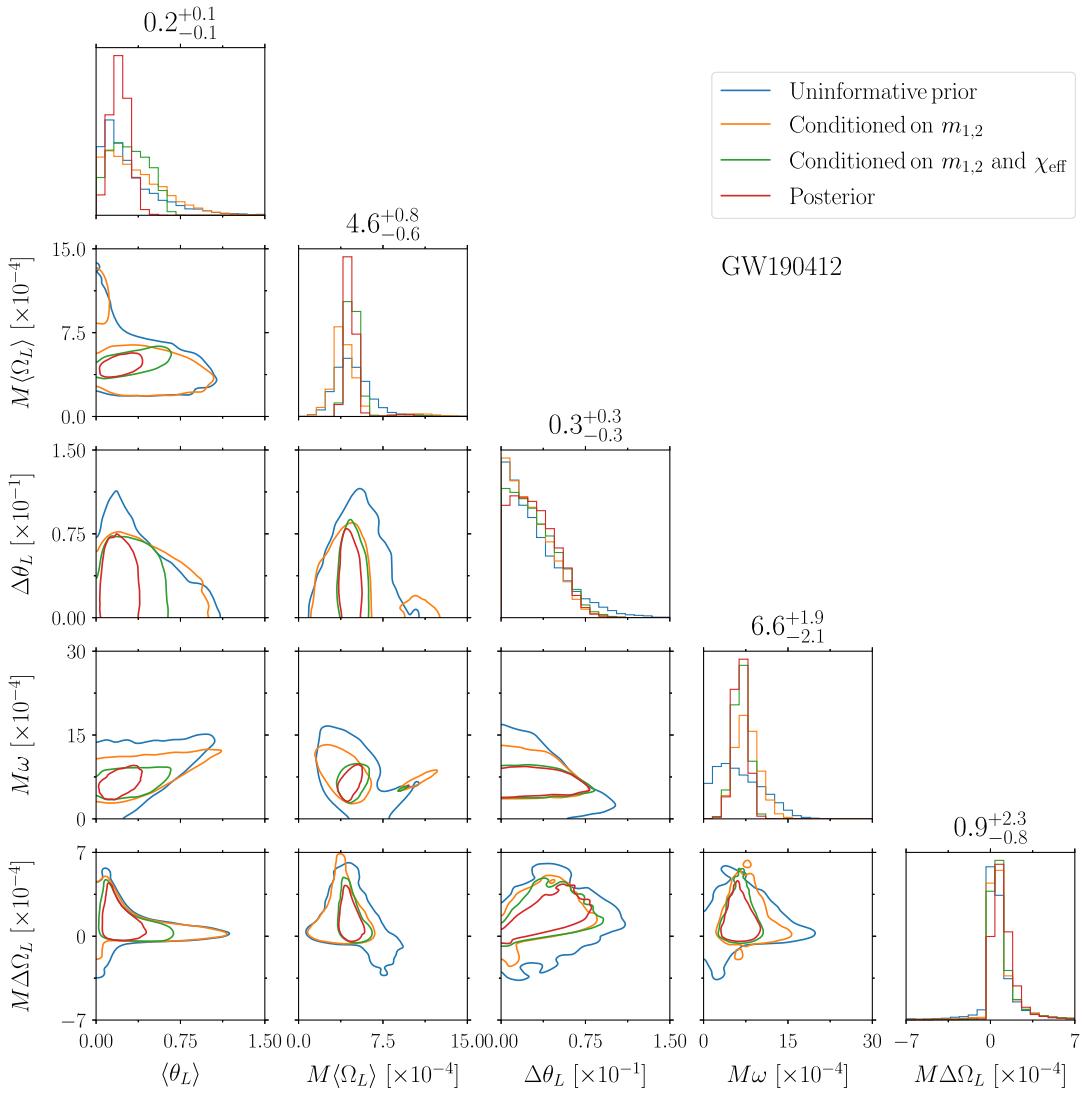


FIG. 3. Revised version of Fig. 3.

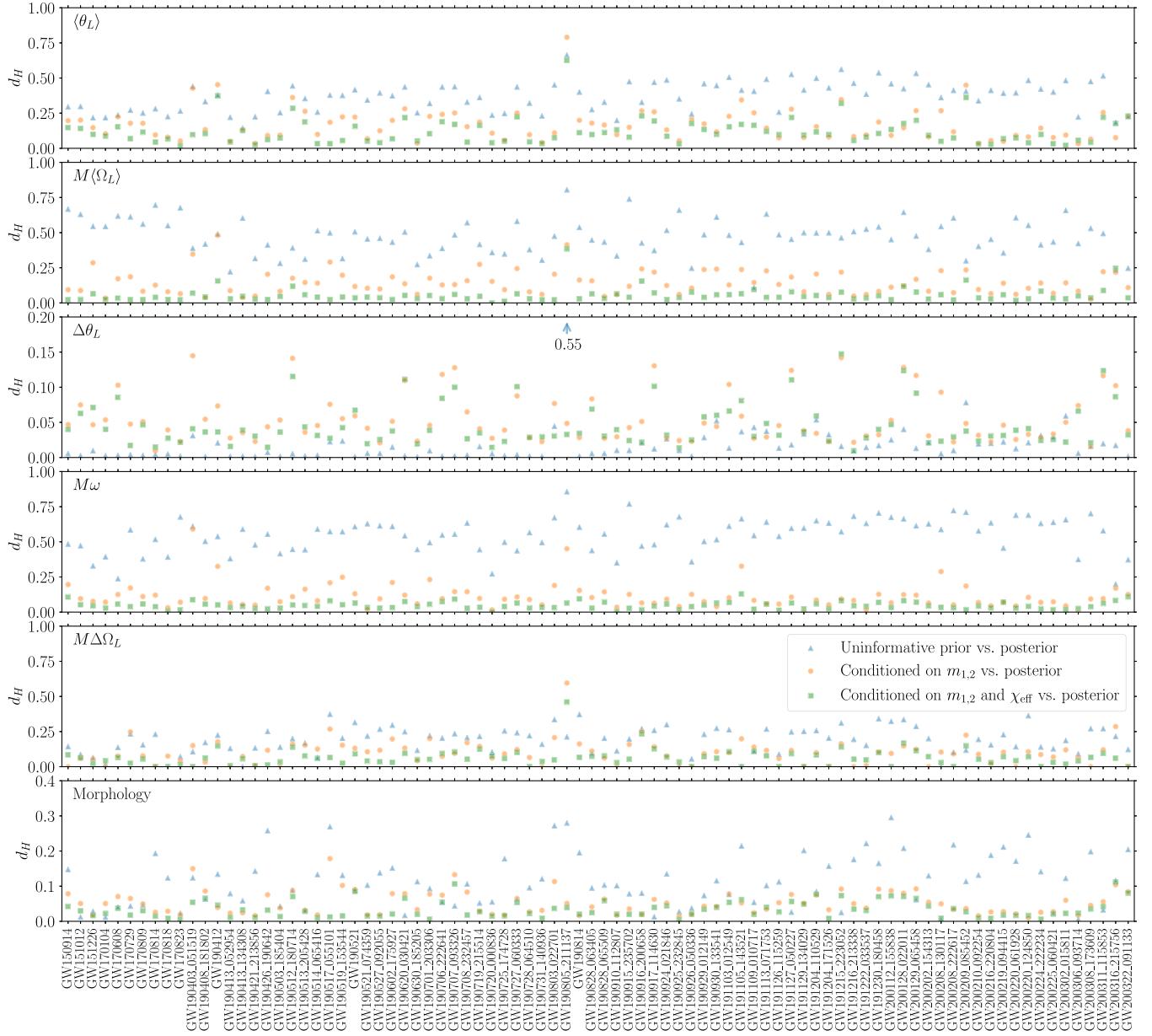


FIG. 4. Revised version of Fig. 4.

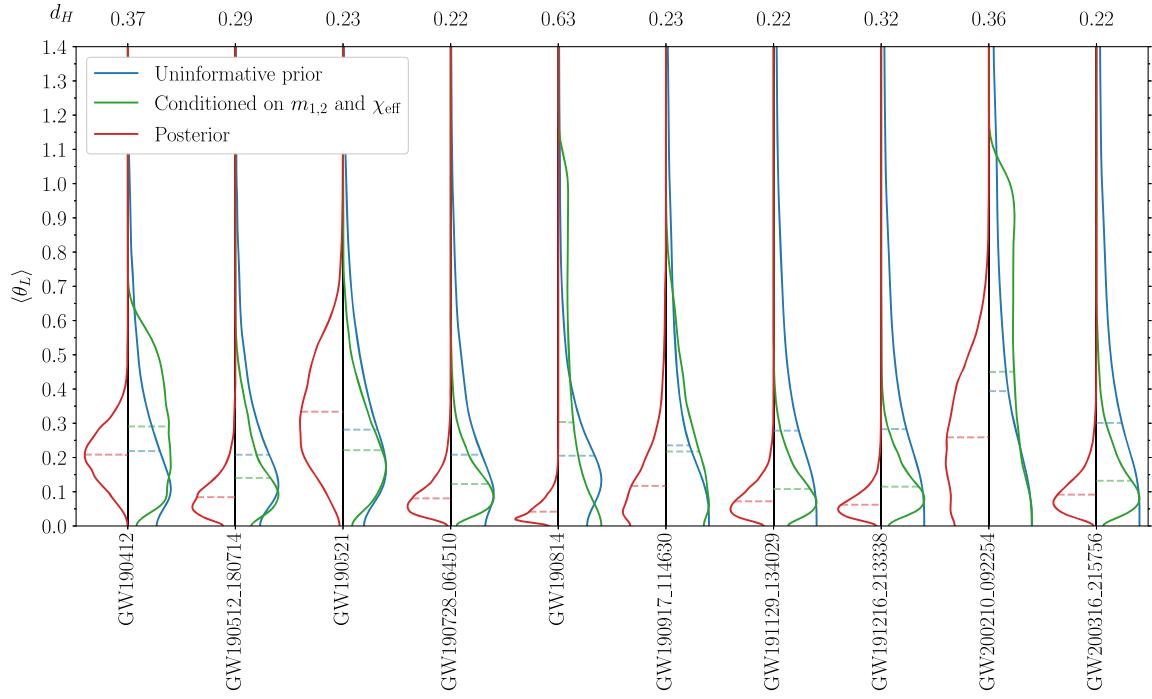


FIG. 5. Revised version of Fig. 5. Note that the gravitational wave event GW190917\_114630 now replaces event GW190630\_185205 from the original figure.

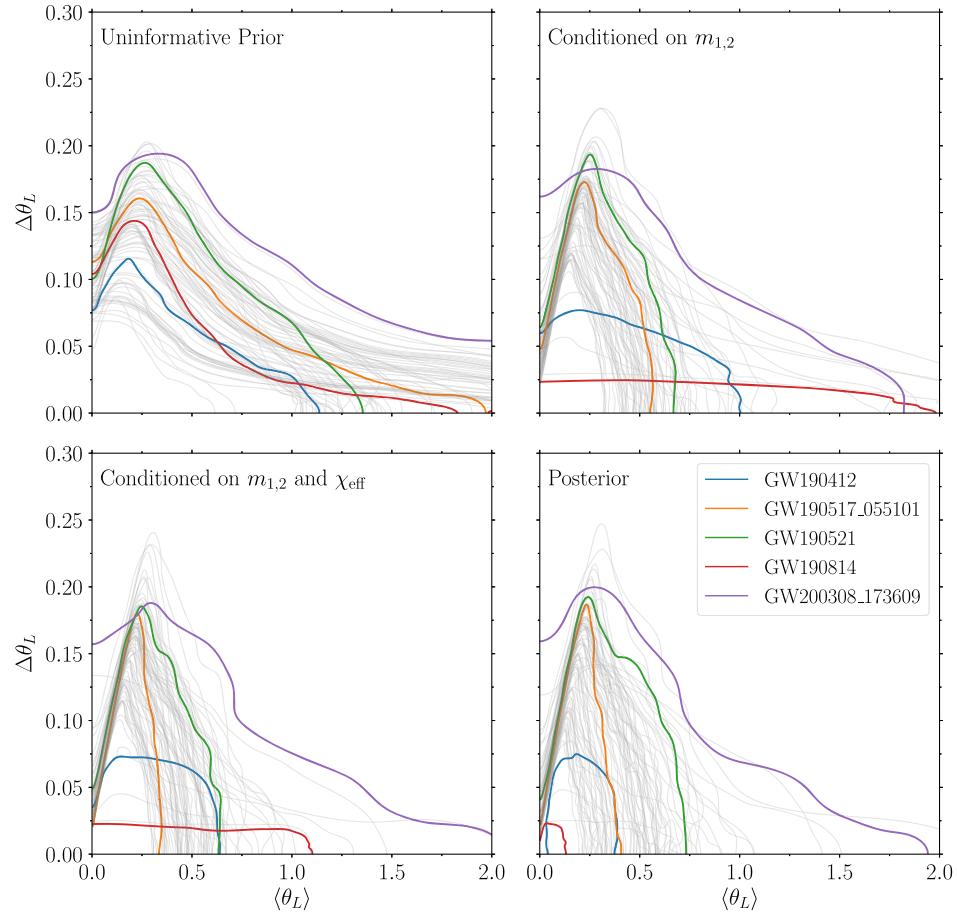


FIG. 6. Revised version of Fig. 6.



FIG. 7. Revised version of Fig. 7.

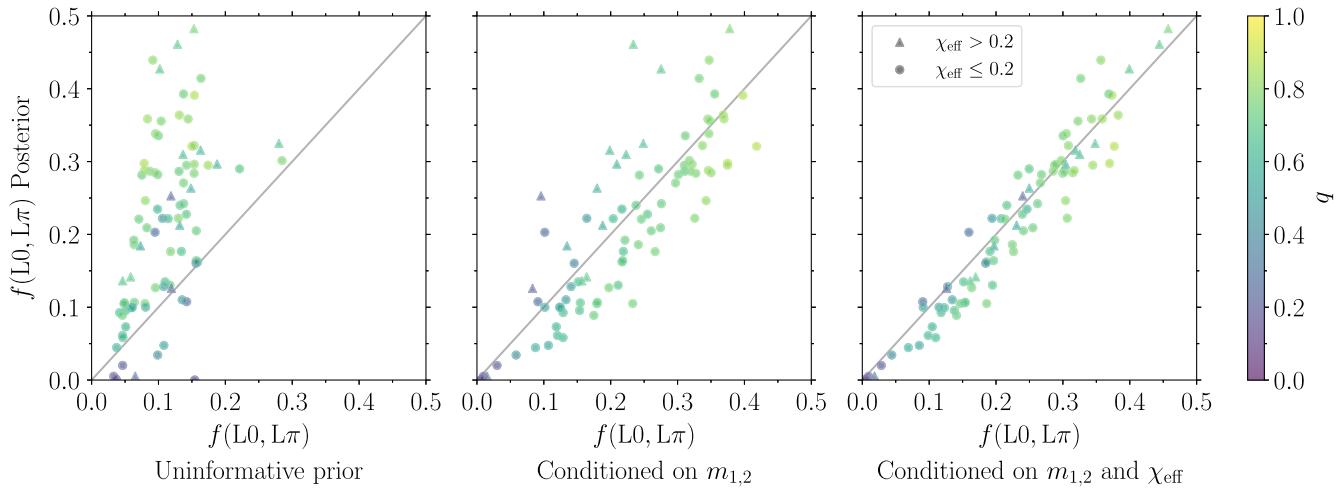


FIG. 8. Revised version of Fig. 8.

TABLE I. Revised version of Table I.

Event	Probability	$\langle \theta_L \rangle [\times 10^{-1}]$	$M\langle \Omega_L \rangle [\times 10^{-4}]$	$\Delta\theta_L [\times 10^{-1}]$	$M\omega [\times 10^{-4}]$	$M\Delta\Omega_L [\times 10^{-4}]$	L0/C/Lπ
GW150914	Uninformative Prior	$1.8^{+5.7}_{-1.4}$	$13.8^{+20.4}_{-10.1}$	$2.7^{+6.7}_{-2.5}$	$0.8^{+4.4}_{-0.7}$	$6.7^{+125.8}_{-69.0}$	0.1/0.85/0.05
	Conditioned on $m_{1,2}$	$1.6^{+2.0}_{-1.2}$	$17.9^{+3.9}_{-4.0}$	$2.4^{+7.8}_{-2.3}$	$0.4^{+0.4}_{-0.2}$	$0.3^{+51.1}_{-43.5}$	0.29/0.58/0.13
	Conditioned on $m_{1,2}$ and $\chi_{\text{eff}}$	$1.5^{+1.9}_{-1.2}$	$17.8^{+3.5}_{-3.4}$	$2.3^{+7.9}_{-2.2}$	$0.4^{+0.3}_{-0.3}$	$0.5^{+51.0}_{-39.7}$	0.28/0.62/0.1
	Posterior	$1.1^{+1.8}_{-0.9}$	$17.7^{+3.4}_{-3.2}$	$2.0^{+7.3}_{-1.9}$	$0.3^{+0.4}_{-0.2}$	$0.6^{+54.8}_{-47.1}$	0.24/0.68/0.08
GW151012	Uninformative Prior	$1.8^{+5.8}_{-1.4}$	$14.0^{+20.4}_{-10.2}$	$2.7^{+6.9}_{-2.5}$	$0.8^{+4.4}_{-0.7}$	$6.8^{+118.5}_{-65.5}$	0.11/0.84/0.05
	Conditioned on $m_{1,2}$	$1.5^{+2.5}_{-1.1}$	$6.7^{+2.8}_{-1.9}$	$2.9^{+7.0}_{-2.7}$	$0.2^{+0.6}_{-0.1}$	$1.9^{+43.0}_{-33.1}$	0.15/0.78/0.07
	Conditioned on $m_{1,2}$ and $\chi_{\text{eff}}$	$1.4^{+2.2}_{-1.1}$	$6.8^{+3.1}_{-1.7}$	$2.7^{+7.3}_{-2.5}$	$0.2^{+0.6}_{-0.1}$	$1.5^{+46.9}_{-36.9}$	0.14/0.8/0.05
	Posterior	$1.0^{+1.8}_{-0.8}$	$6.8^{+3.2}_{-1.7}$	$2.3^{+6.4}_{-2.1}$	$0.2^{+0.5}_{-0.1}$	$1.5^{+53.0}_{-44.2}$	0.12/0.84/0.04
GW151226	Uninformative Prior	$1.2^{+4.0}_{-0.9}$	$2.7^{+2.2}_{-1.3}$	$2.0^{+4.8}_{-1.9}$	$0.2^{+0.7}_{-0.2}$	$1.6^{+22.2}_{-14.2}$	0.07/0.89/0.04
	Conditioned on $m_{1,2}$	$1.2^{+2.2}_{-0.9}$	$2.1^{+1.0}_{-0.5}$	$2.6^{+5.8}_{-2.4}$	$0.1^{+0.2}_{-0.1}$	$1.0^{+15.8}_{-12.6}$	0.11/0.85/0.04
	Conditioned on $m_{1,2}$ and $\chi_{\text{eff}}$	$1.2^{+1.8}_{-0.8}$	$2.2^{+0.9}_{-0.3}$	$2.8^{+6.2}_{-2.6}$	$0.1^{+0.1}_{-0.1}$	$0.8^{+15.9}_{-13.0}$	0.11/0.85/0.04
	Posterior	$1.1^{+1.4}_{-0.7}$	$2.2^{+0.8}_{-0.2}$	$2.6^{+5.2}_{-2.4}$	$0.1^{+0.1}_{-0.1}$	$1.0^{+13.5}_{-10.9}$	0.1/0.87/0.04
GW170104	Uninformative Prior	$1.8^{+5.8}_{-1.4}$	$13.9^{+19.9}_{-10.1}$	$2.7^{+6.8}_{-2.5}$	$0.8^{+4.5}_{-0.7}$	$6.6^{+122.1}_{-66.9}$	0.11/0.84/0.05
	Conditioned on $m_{1,2}$	$1.7^{+2.4}_{-1.3}$	$12.2^{+4.9}_{-3.8}$	$3.5^{+7.8}_{-3.3}$	$0.5^{+0.6}_{-0.3}$	$3.7^{+79.2}_{-65.6}$	0.15/0.78/0.07
	Conditioned on $m_{1,2}$ and $\chi_{\text{eff}}$	$1.6^{+2.5}_{-1.2}$	$12.1^{+5.3}_{-3.8}$	$3.2^{+7.9}_{-3.0}$	$0.5^{+0.6}_{-0.3}$	$3.5^{+78.2}_{-66.1}$	0.14/0.81/0.05
	Posterior	$1.4^{+2.1}_{-1.0}$	$12.1^{+5.1}_{-3.9}$	$3.0^{+7.1}_{-2.8}$	$0.5^{+0.5}_{-0.4}$	$3.9^{+81.0}_{-68.1}$	0.12/0.84/0.04
GW170608	Uninformative Prior	$1.0^{+3.4}_{-0.8}$	$1.3^{+1.0}_{-0.6}$	$1.7^{+4.2}_{-1.6}$	$0.1^{+0.3}_{-0.1}$	$0.8^{+10.3}_{-6.5}$	0.07/0.9/0.03
	Conditioned on $m_{1,2}$	$1.1^{+1.6}_{-0.8}$	$1.8^{+0.6}_{-0.4}$	$2.4^{+5.8}_{-2.2}$	$0.1^{+0.1}_{-0.1}$	$0.4^{+10.9}_{-8.7}$	0.14/0.8/0.06
	Conditioned on $m_{1,2}$ and $\chi_{\text{eff}}$	$1.0^{+1.6}_{-0.8}$	$1.8^{+0.6}_{-0.3}$	$2.1^{+6.1}_{-2.0}$	$0.0^{+0.2}_{-0.0}$	$0.3^{+11.3}_{-9.4}$	0.12/0.84/0.04
	Posterior	$0.8^{+1.1}_{-0.6}$	$1.8^{+0.6}_{-0.3}$	$1.8^{+4.9}_{-1.7}$	$0.0^{+0.2}_{-0.0}$	$0.3^{+12.4}_{-10.0}$	0.1/0.87/0.03
GW170729	Uninformative Prior	$2.6^{+5.6}_{-2.0}$	$86.4^{+234.7}_{-71.5}$	$3.7^{+10.0}_{-3.5}$	$5.0^{+11.6}_{-4.4}$	$17.8^{+565.1}_{-403.0}$	0.2/0.72/0.08
	Conditioned on $m_{1,2}$	$2.2^{+3.6}_{-1.7}$	$42.4^{+22.5}_{-18.5}$	$4.0^{+9.3}_{-3.8}$	$2.0^{+2.4}_{-1.3}$	$12.9^{+268.5}_{-219.3}$	0.17/0.75/0.08
	Conditioned on $m_{1,2}$ and $\chi_{\text{eff}}$	$1.9^{+2.3}_{-1.3}$	$49.5^{+22.3}_{-21.2}$	$4.7^{+10.1}_{-4.4}$	$1.8^{+1.5}_{-1.0}$	$-0.0^{+343.2}_{-303.6}$	0.22/0.65/0.13
	Posterior	$1.7^{+2.1}_{-1.1}$	$50.3^{+21.1}_{-22.0}$	$4.5^{+9.8}_{-4.2}$	$1.8^{+1.4}_{-1.1}$	$-0.9^{+366.4}_{-340.1}$	0.21/0.68/0.12

(Table continued)

















