# Big bang nucleosynthesis and early dark energy in light of the EMPRESS  $Y_p$  results and the  $H_0$  tension

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Recent measurements of the primordial <sup>4</sup>He abundance  $Y_p$  from EMPRESS suggest a cosmological scenario with an effective number of neutrino species that deviates from the standard value and a nonzero lepton asymmetry. We argue that the standard cosmological model would be extended further if the Hubble tension were taken into account, in which the derived baryon density could be somewhat higher than the in the standard ΛCDM framework. We also discuss the issue by assuming early dark energy whose energy density can have a sizable fraction at the epoch of big bang nucleosynthesis. We show that the existence of early dark energy can reduce some of the tension implied by the EMPRESS  $Y_p$  results.

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#### I. INTRODUCTION

The concordance model of cosmology—the so-called ΛCDM model—has now been established and can successfully explain various cosmological observations almost consistently. However, in recent years several tensions in the framework of ΛCDM have come under debate, which may suggest a modification/extension of the concordance  $\Lambda$ CDM model. One of them is the Hubble tension (the  $H_0$ tension), i.e., the discrepancy in the values of the Hubble constant  $H_0$  measured directly in the local Universe and indirectly from sources such as the cosmic microwave background (CMB) in the framework of ΛCDM. More specifically, the Cepheid-calibrated supernova distance ladder measurements give  $H_0 = 73.04 \pm 1.04$  km/s/Mpc [\[1](#page-13-0)], while CMB data from Planck in combination with baryon acoustic oscillation (BAO) measurements infer  $H_0 =$  $67.66 \pm 0.42$  km/s/Mpc [\[2\]](#page-13-1), which are discrepant at the  $4.8\sigma$  level. Even without CMB data, the tension between direct and indirect measurements still persists [\[3](#page-13-2)–[5\]](#page-13-3) and indeed other direct and indirect measurements also show a similar tendency for each category (see, e.g., Refs. [\[6](#page-13-4),[7\]](#page-13-5) for a review), which has motivated many efforts to resolve the tension and pursue models beyond the standard ΛCDM (see, e.g., Refs. [\[6](#page-13-4),[8\]](#page-13-6) for a review).

Another issue has appeared recently from the measurement of the primordial <sup>4</sup>He abundance  $Y_p$  by the Extremely Metal-Poor Representatives Explored by the Subaru Survey (EMPRESS) experiment, which obtained  $Y_p =$  $0.2370^{+0.0033}_{-0.0034}$  [\[9\]](#page-13-7). This value is somewhat smaller than the previously obtained ones, such as  $Y_p = 0.2449 \pm 0.0040$  [[10](#page-13-8)],  $Y_p = 0.2436^{+0.0039}_{-0.0040}$  [\[11\]](#page-13-9), and  $Y_p = 0.2462 \pm 0.0022$  [[12](#page-13-10)]. Further confirmation of the value of  $Y_p$  measured by the

EMPRESS may be awaited in investigating its implications to cosmological parameters, once we take the EMPRESS value of  $Y_p$ , by combining the measurement of the deuterium abundance  $D_p$  from Ref. [[13](#page-13-11)],  $D_p = (2.527 \pm 0.030) \times 10^{-5}$ , one obtains constraints on the effective number of neutrino species  $N_{\text{eff}} = 2.37_{-0.24}^{+0.19}$  and the baryon-to-photon ratio  $\eta \times 10^{10} = 5.80^{+0.13}_{-0.16}$  [\[9](#page-13-7)] in the framework of the  $\Lambda$ CDM +  $N<sub>eff</sub>$  model. The value of  $N<sub>eff</sub>$  deviates from the standard one<sup>1</sup> and the baryon-to-photon ratio is slightly smaller than that obtained from Planck in the framework of the ΛCDM model. This may create another tension in the standard cosmological model, which is referred to as the "helium anomaly" in some literature.

Actually, when one introduces a nonzero chemical potential for the electron neutrino  $\mu_{\nu_e}$ , which is commonly characterized by the degeneracy parameter  $\xi_e = \mu_{\nu_e}/T$ , with T being the neutrino temperature, one obtains  $\xi_e =$  $0.05^{+0.03}_{-0.02}$  and  $N_{\text{eff}} = 3.11^{+0.34}_{-0.31}$  [\[9](#page-13-7)] with a Gaussian prior for the baryon-to-photon ratio  $\eta \times 10^{10} = 6.132 \pm 0.038$  motivated by the *Planck* result in the  $\Lambda$ CDM framework  $[2]$  $[2]$ .<sup>2</sup> This suggests a nonzero lepton asymmetry, and its implications have been discussed in Refs. [[21](#page-14-0)–[24](#page-14-1)]. Instead of invoking a nonzero lepton asymmetry, one can also envisage a model with modified gravity [\[25\]](#page-14-2) to resolve the helium anomaly. In any case, the EMPRESS result may indicate that we need a model beyond the standard paradigm and it would raise another tension in cosmology.

<sup>&</sup>lt;sup>1</sup>Although we use  $N_{\text{eff}} = 3.046$  [[14](#page-13-12)] as a reference value for the standard case, recent precise calculations gave  $N_{\text{eff}} =$ <sup>3</sup>.044–3.<sup>045</sup> [\[15](#page-13-13)–[19\]](#page-14-3). <sup>2</sup>

<sup>&</sup>lt;sup>2</sup>See Ref. [[20](#page-14-4)] for the implications of a nonzero lepton asymmetry and extra radiation for the  $H_0$  tension.

<span id="page-1-0"></span>TABLE I. Constraints on the baryon density  $\Omega_b h^2$  and its corresponding baryon-to-photon ratio  $\eta_{10}$  in models proposed to resolve the  $H_0$ tension. For the data set shown in the fifth column, (a)–(f) denotes: (a)  $Planck 2018 + BAO$ , (b)  $Planck 2018 + BAO +$ <br>Supernova  $(SN) + H_0$ , (c)  $Planck 2018 + BAO + SN + H_0 + RSD + DES$ , (d)  $Planck 2018 + BAO + SN + BBN + H_0$ ,  $Planck 2018 + BAO + SN + H<sub>0</sub> + RSD + DES,$ (e) Planck  $2018 + SN + H_0$ , and (f) Planck  $2018 + BAO + SN + DES + H_0$ . Here "Planck 2018" refers to Planck 2018 TT, TE, EE + lensing, and "H<sub>0</sub>" indicates that the analysis adopts the H<sub>0</sub> prior with the value motivated by a direct local measurement such as the one from distance ladder observations. For details of the analysis, see the references shown in the last column. We should note that most analyses quoted in the table include the  $H_0$  prior, and hence some caution should be taken when interpreting the value of  $H_0$  obtained in the analyses.

Model	$100\Omega_h h^2$	$\eta_{10}$	$H_0$	Data set	Ref.
$\Lambda$ CDM	$2.242 \pm 0.014$	$6.14 \pm 0.038$	$67.66 \pm 0.42$	(a)	$[2]$
Varying $m_e + \Omega_k$	$2.365_{-0.037}^{+0.033}$	$6.48^{+0.090}_{-0.101}$	$72.84_{-1.0}^{+1.0}$	(b)	$[33]$
Early dark energy $(\phi^4 + AdS)$	$2.346^{+0.017}_{-0.016}$	$6.42^{+0.047}_{-0.044}$	$72.64^{+0.57}_{-0.64}$	(b)	$[34]$
Early dark energy (axion type)	$2.285 \pm 0.021$	$6.26 \pm 0.057$	$70.75_{-1.09}^{+1.05}$	(c)	$[35]$
New early dark energy	$2.292^{+0.022}_{-0.024}$	$6.27^{+0.060}_{-0.066}$	$71.4^{+1.0}_{-1.0}$	(d)	$[36]$
Early modified gravity	$2.275 \pm 0.018$	$6.23 \pm 0.049$	$71.21 \pm 0.93$	(e)	$[37]$
Primordial magnetic field	$2.266 \pm 0.014$	$6.20 \pm 0.038$	$70.57 \pm 0.61$	(f)	[38]
Majoron	$2.267 \pm 0.017$	$6.21 \pm 0.047$	$70.18 \pm 0.61$	(a)	$[39]$

Actually, as we will argue in this paper, when the Hubble tension is taken into account the above EMPRESS result would imply a nonstandard scenario even more. In many attempts to explain the  $H_0$  tension, it can be resolved in such a way that the value of  $H_0$  derived indirectly from, e.g., CMB and BAO data increases and becomes similar to that from direct measurements. Indeed, the baryon density obtained in such model frameworks tends to be higher than the value in the ΛCDM case, which makes the abovementioned discrepancy more severe. We discuss this issue quantitatively by investigating the fit to the EMPRESS  $Y_p$ result in combination with deuterium abundance from recent observations compiled by the Particle Data Group [\[26\]](#page-14-5),  $D_p = (2.547 \pm 0.025) \times 10^{-5}$ ,<sup>3</sup> with the prior for the baryon density suggested by the  $H_0$  tension.

Moreover, we also argue that one can reduce the helium anomaly by extending the standard cosmological model with an extra component called early dark energy (EDE) [\[27\]](#page-14-6) which has been extensively discussed in the context of the  $H_0$  tension (for various works on EDE, see, e.g., Ref. [[6\]](#page-13-4)). Although the EDE model we consider in this paper has a different energy scale than the one introduced to resolve the  $H_0$  tension, the behavior is quite similar in the sense that the energy density of EDE gives a sizable contribution to the total one during the epoch of big bang nucleosynthesis (BBN). Indeed, as we discuss in this paper, we do not need to assume nonzero lepton asymmetry or a nonstandard value of  $N_{\text{eff}}$  by assuming the existence of EDE in some cases to relax the helium anomaly.

The structure of this paper is as follows. In the next section, we discuss the implications of the Hubble tension for BBN, particularly focusing on its consequences for the EMPRESS  $Y_p$  results through the value of the baryon density suggested by models that may resolve the  $H_0$ tension. Then, in Sec. [III](#page-4-0) we argue that, by introducing EDE whose energy fraction becomes relatively large during the BBN era, the anomaly implied by the EMPRESS results can be alleviated. In the final section, we conclude our paper.

## II. IMPLICATIONS OF THE HUBBLE TENSION FOR BBN

In this section, we discuss the implication of the  $H_0$ tension for BBN, especially focusing on the effects of the assumption of baryon density suggested by the tension on the parameter estimation in BBN. In Table [I](#page-1-0) we list the constraints on the baryon density  $\Omega_b h^2$  in the ΛCDM model and example models proposed to resolve the  $H_0$  tension. Most models in the list are taken from among those referred to as "successful" models as a possible solution to the  $H_0$ tension in Ref. [[8\]](#page-13-6) based on the criteria of the Gaussian tension, the difference of the maximum a posteriori and the Akaike information criterium (see Table 1 in Ref. [[8](#page-13-6)]). We take the constraints on  $\Omega_b h^2$  from the references cited in the last column of Table [I](#page-1-0). We should note that the data set used in the analysis for each model quoted in Table [I](#page-1-0) are different, and currently there is no consensus on which model is more plausible, and hence the values quoted in the table can be regarded as just a reference. Nevertheless, we can clearly see that, in models proposed as a solution to the  $H_0$  tension, the value of  $\Omega_b h^2$  tends to be higher than that in the ΛCDM model, which shows that the  $H_0$  tension affects another aspect of cosmology.4

 $3$ In Ref. [[9\]](#page-13-7), the deuterium abundance obtained in Ref. [\[13\]](#page-13-11) was adopted in the analysis, while we use the one given in Ref.  $[26]$  $[26]$  $[26]$  in our analysis. We note that the use of either value scarcely affects our argument.

<sup>&</sup>lt;sup>4</sup>Other implications of the  $H_0$  tension for other aspects of cosmology have been discussed, such as cosmological bounds on neutrino masses [\[28\]](#page-14-14) and the scale dependence of the primordial power spectrum [[29](#page-14-15)–[32](#page-14-16)].

<span id="page-2-1"></span>

FIG. 1. Parameter ranges within 1 $\sigma$  and 2 $\sigma$  errors for Y<sub>p</sub> [\[9](#page-13-7)] (light and dark dotted (blue) regions) and  $D_p$  [\[26\]](#page-14-5) (light and dark magenta regions for  $1\sigma$  and  $2\sigma$ ) in the  $\eta_{10}N_{\text{eff}}$  plane. Here the  $1\sigma$  and  $2\sigma$  errors include both observational and theoretical ones. We take the neutrino degeneracy parameter as  $\xi_e = 0$  (left), 0.05 (middle), and 0.08 (right).

Actually, this is somewhat expected given the correlation between  $\Omega_b h^2$  and  $H_0$  in the position and height of acoustic oscillations in the CMB angular power spectrum (see, e.g., Refs. [\[40,](#page-14-17)[41\]](#page-14-18)), although it becomes somewhat involved in models where the  $H_0$  tension can be solved. To resolve the tension, one needs to reduce the sound horizon at recombination,  $r_s$ , but also keep the CMB angular power spectra almost intact to obtain a good fit to CMB (and BAO) data. For example, in the time-varying electron mass model [\[33\]](#page-14-7), one can reduce  $r<sub>s</sub>$  by slightly raising the electron mass  $m_e$  at the recombination epoch; however, to keep a good fit to CMB data, the baryon density  $\Omega_b h^2$ should also be increased in accordance with the change of  $m_e$  as  $\delta m_e/m_e = \delta(\Omega_b h^2)/\Omega_b h^2$  (see Ref. [\[33\]](#page-14-7) for a detailed discussion). Also in the early dark energy model, in order to increase the value of  $H_0$ , one needs to shift  $\Omega_b h^2$  to a higher value to have the CMB angular power spectrum almost the same, which can be realized by keeping the acoustic scale and angular damping scale almost unchanged (for details, see, e.g., Ref. [[29](#page-14-15)]).

When one discusses BBN, the baryon density is usually quoted by the baryon-to-photon ratio  $\eta = n_b/n_\gamma$ , with  $n_b$ and  $n_{\gamma}$  being the number densities of baryons and photons, respectively. The conversion factor from the baryon density  $\Omega_b h^2$  to the baryon-to-photon ratio  $\eta_{10} = 10^{10} \eta$  is given by [[42](#page-14-19)] (see also, e.g., Refs. [\[43](#page-14-20)[,44\]](#page-14-21))

<span id="page-2-0"></span>
$$
\eta_{10} = \frac{273.279}{1 - 0.007125Y_p} \left(\frac{2.7255 \text{ K}}{T_{\gamma 0}}\right)^3 \Omega_b h^2, \quad (2.1)
$$

where  $T_{\gamma 0}$  is the present photon temperature. Precisely speaking, the conversion factor depends on the primordial helium abundance. Although we adopt the EMPRESS mean value of  $Y_p = 0.2379$  to obtain  $\eta_{10}$ , the dependence on  $Y_p$ is very weak and thus its uncertainty can be neglected compared to the error in  $\Omega_b h^2$  obtained from CMB data, and hence the actual value of  $Y_p$  in Eq. [\(2.1\)](#page-2-0) scarcely affects the following argument. We also list the value of  $\eta_{10}$  derived by using Eq. [\(2.1\)](#page-2-0) for each model in Table [I.](#page-1-0) As seen from the table, models proposed to resolve the  $H_0$  tension tend to suggest a higher value of  $\eta_{10}$  compared to that in  $\Lambda$ CDM. In some cases, the mean value of  $\eta_{10}$  can be as high as  $\eta_{10}$  ~ 6.48, although, in general, the error is also somewhat larger than that for the ΛCDM case.

Indeed, as already argued in Ref. [\[9\]](#page-13-7), the value of  $Y_p$ obtained by EMPRESS would imply a nonzero lepton asymmetry, which is characterized by a nonzero electron neutrino degeneracy parameter  $\xi_e$ , and the value of  $N_{\text{eff}}$  is somewhat larger than the standard one. This tendency becomes more prominent when the baryon density is high, which can be understood from Fig. [1](#page-2-1) where the  $1\sigma$  and  $2\sigma$ allowed regions from the measurements of  $Y_p$  [\[9](#page-13-7)] and  $D_p$  [[26](#page-14-5)] are shown in the  $\eta_{10}$ - $N_{\text{eff}}$  plane for several values of  $\xi_e$ . The errors include both observational and theoretical ones. [For the uncertainties from theoretical calculations, see the paragraph below Eq. [\(2.2\).](#page-2-2)] We use the public code PARTHENOPE [[42](#page-14-19),[45](#page-14-22),[46](#page-14-23)] to calculate the helium and deuterium abundances. As seen from the figure, as  $\xi_e$  takes more positive values,  $Y_p$  decreases [[47](#page-14-24)], which makes a higher  $\eta_{10}$  preferred from the combination of the EMPRESS  $Y_p$  results [[9](#page-13-7)] and  $D_p$  from Ref. [\[26\]](#page-14-5). This indicates that when a higher value of the baryon density is favored from CMB data, which can be taken into account in the analysis as a prior for  $\eta_{10}$  (as will be done in the following), a more (positively) nonzero value of  $\xi_e$  and a  $N_{\text{eff}}$  higher than the standard value are preferred.

To discuss the implication of a high value of  $\eta_{10}$ suggested by the  $H_0$  tension in a more quantitative manner, we investigate a constraint in the  $N_{\text{eff}}-\xi_e$  plane from the helium abundance  $Y_p$  of EMPRESS [\[9](#page-13-7)] and deuterium  $D_p$  [\[26\]](#page-14-5) with the prior for the baryon-to-photon ratio  $\eta_{10}$ . To obtain the constraint, we calculate  $\chi^2$  as

<span id="page-2-2"></span>
$$
\chi^{2} = \frac{(Y_{p}^{\text{obs}} - Y_{p}^{\text{th}})^{2}}{\sigma_{Y_{p},\text{obs}}^{2} + \sigma_{Y_{p},\text{sys}}^{2}} + \frac{(D_{p}^{\text{obs}} - D_{p}^{\text{th}})^{2}}{\sigma_{D_{p},\text{obs}}^{2} + \sigma_{D_{p},\text{sys}}^{2}} + \frac{(\eta_{10}^{\text{ref}} - \eta_{10})^{2}}{\sigma_{\eta_{10}}^{2}}.
$$
\n(2.2)

In our analysis, we adopt  $Y_p^{\text{obs}} = 0.2379$ ,  $\sigma_{Y_p, \text{obs}} = 0.00335$ for the helium abundance, which is obtained by EMPRESS [\[9\]](#page-13-7). For the deuterium abundance, we use the weighted mean of 11 recent measurements of  $D_p$  compiled by the Particle Data Group [[26](#page-14-5)]:  $D_p^{obs} = 2.547 \times 10^{-5}$  $\sigma_{D_p,obs} = 0.025 \times 10^{-5}$ . We also include the errors in the theoretical calculation for helium as  $\sigma_{Y_p,sys}^2 = (0.0003)^2 +$  $(0.00012)^2$ , where the first and second errors come from the uncertainties on the nuclear rate and neutron decay rate with  $\tau_n = 879.4 \pm 0.6$  sec [[48](#page-14-25)], respectively [[46](#page-14-23)]. For deuterium, we adopt  $\sigma_{D_p,sys}^2 = (0.06 \times 10^{-5})^2$  which comes from nuclear rate uncertainties [[46](#page-14-23)].  $Y_p^{\text{th}}$  and  $D_p^{\text{th}}$  are theoretically predicted values for given model parameters, such as  $\eta_{10}$ ,  $N_{\text{eff}}$ , and  $\xi_e$ . How the abundances  $Y_p^{\text{th}}$  and  $D_p^{\text{th}}$ depend on  $\eta_{10}$ ,  $N_{\text{eff}}$ , and  $\xi_e$  can be read off from some fitting formulas given in, e.g., Ref. [\[49\]](#page-14-26). When we vary the baryon density  $\eta_{10}$  in the analysis, we add the third term to determine the value of  $\chi^2$ .

For the baryon density, we consider three priors motivated by the constraints from CMB analysis in the standard  $\Lambda$ CDM model and models proposed to solve the  $H_0$ tension. We take the following reference values for  $\eta_{10}^{\text{ref}}$ and  $\sigma_{\eta_{10}}$ :

$$
\eta_{10}^{\text{ref},1} = 6.14, \qquad \sigma_{\eta_{10},1} = 0.038, \tag{2.3}
$$

$$
\eta_{10}^{\text{ref},2} = 6.40, \qquad \sigma_{\eta_{10},2} = 0.060, \tag{2.4}
$$

$$
\eta_{10}^{\text{ref},3} = 6.25, \qquad \sigma_{\eta_{10},3} = 0.060. \tag{2.5}
$$

For the reference value 1 (denoted as "ref,1"), which is motivated by the analysis in the standard ΛCDM

framework, we take  $\eta_{10}^{\text{ref},1}$  and  $\sigma_{\eta_{10},1}$  to be the same as in the ΛCDM model in Table [I](#page-1-0).

For the reference values 2 and 3, we take the values motivated from the analysis which can resolve the  $H_0$ tension. As seen from Table [I,](#page-1-0) the mean value of  $\eta_{10}$  varies from model to model; however, one can see the tendency that a higher  $\eta_{10}$  is preferred when a model allows a higher value of  $H_0$ . In order for the value of  $H_0$  from indirect measurements such as the CMB to be consistent with that obtained from direct measurements, it should be high enough to be close to  $H_0 = 73.04 \pm 1.04 \text{ km/s/Mpc}$  $H_0 = 73.04 \pm 1.04 \text{ km/s/Mpc}$  $H_0 = 73.04 \pm 1.04 \text{ km/s/Mpc}$  [1]. Among the values for  $H_0$  listed in Table [I](#page-1-0), the ones in varying  $m_e$  +  $\Omega_k$  and early dark energy (EDE:  $\phi^4$  + AdS) models are close to it, in which the mean values of the baryon density are  $\eta_{10} = 6.48$  and 6.42, respectively. Furthermore, new dark energy models and early modified gravity can also give a relatively high value of  $H_0$ , although its values are not as high as the ones in the models above (varying  $m_e + \Omega_k$  and EDE  $\phi^4$  + AdS). In those models, the mean baryon densities are  $\eta_{10} = 6.27$  and 6.23 and are somewhat larger than the one in ΛCDM. Motivated by these observations, we consider two reference values of  $\eta_{10} = 6.40$  and 6.25 ("ref, 2" and "ref, 3," respectively). The uncertainty of  $\eta_{10}$  in models to resolve the  $H_0$  tension is somewhat larger than that in the  $\Lambda$ CDM case. Therefore, we take  $\sigma_{\eta_{10},2} = \sigma_{\eta_{10},3} = 0.060$  for reference values 2 and 3, which corresponds to the average value for the uncertainty of  $\eta_{10}$  listed in Table [I](#page-1-0) excluding ΛCDM (rounded up to the second decimal place).

In Fig. [2,](#page-3-0) we show the  $1\sigma$  and  $2\sigma$  allowed regions in the  $N_{\text{eff}}$ -ξ<sub>e</sub> plane obtained by evaluating  $\chi^2$  given in Eq. [\(2.2\)](#page-2-2). From the figure, one can see that when a higher value of  $\eta_{10}$ is assumed for the prior, a more positively nonzero lepton asymmetry (nonzero degeneracy parameter for the electron

<span id="page-3-0"></span>

FIG. 2. 1 $\sigma$  and  $2\sigma$  allowed regions in the N<sub>eff-</sub> $\xi_e$  plane from measurements of Y<sub>p</sub> and D<sub>p</sub> with an  $\eta_{10}$  prior. For the  $\eta_{10}$  prior, we take  $\eta_{10} = \eta_{10}^{\text{ref},1} \pm \sigma_{\eta_{10},1} = 6.14 \pm 0.038$  (black dotted and solid lines for  $1\sigma$  and  $2\sigma$  in both panels) obtained from CMB + BAO data [\[2](#page-13-1)] in the ΛCDM framework and  $\eta_{10} = \eta_{10}^{\text{ref},2} \pm \sigma_{\eta_{10},2} = 6.4 \pm 0.060$  (light and dark shaded (magenta) regions for  $1\sigma$  and  $2\sigma$  in the right panel) and  $\eta_{10} = \eta_{10}^{\text{ref},3} \pm \sigma_{\eta_{10},3} = 6.25 \pm 0.060$  (light and dark shaded (blue) regions for  $1\sigma$  and  $2\sigma$  in the left panel), which are suggested by the  $H_0$  tension.

neutrino  $\xi_e$ ) and larger value of  $N_{\text{eff}}$  are preferred, which indicates that, in light of the  $H_0$  tension, the EMPRESS result for  $Y_p$  gives more significant effects on  $N_{\text{eff}}$  and the lepton asymmetry. (When a previous measurement of  $Y_p$ , such as from Refs. [\[10](#page-13-8)–[12](#page-13-10)], is adopted, the allowed ranges for  $N_{\text{eff}}$  and  $\xi_e$  are closer to the standard ones compared to the case using the EMPRESS  $Y_p$ .)

In this section, we discussed the implications of a high baryon density, which may be suggested by the  $H_0$  tension, for the EMPRESS  $Y_p$  results in the framework where a nonzero lepton asymmetry characterized by  $\xi_e$  and a nonstandard value of  $N_{\text{eff}}$  are allowed. Then, we showed that a positively large nonzero  $\xi_e$  and a larger  $N_{\text{eff}}$  than in the standard case are preferred. However, we can also consider another framework to discuss the implications of the EMPRESS  $Y_p$  results in light of the  $H_0$  tension. As such an example, we will consider early dark energy model in the next section.

## <span id="page-4-0"></span>III. BIG BANG NUCLEOSYNTHESIS WITH EARLY DARK ENERGY

In this section we discuss the impact of EDE, which has been intensively studied in the context of the  $H_0$  tension, on BBN in light of the EMPRESS result for  $Y_p$ . First we present the EDE model considered in this paper, and then we investigate constraints on  $\eta_{10}$ ,  $N_{\text{eff}}$ , and  $\xi_e$  from the EMPRESS  $Y_p$  in combination with the measurement of  $D_p$ for the case when EDE exists.

### A. Early dark energy

EDE models have been extensively investigated in the context of the  $H_0$  tension, whose typical realization is given by a scalar field  $\phi$  with a potential, for example, such as  $V(\phi) = V_0[1 - \cos(\phi/f)]^{\alpha}$  [[50](#page-14-27)], with  $V_0$  representing the energy scale, f being a parameter in the model, and  $\alpha$ controlling the scaling of its energy density after  $\phi$  starts to oscillate. A general behavior of the energy density of EDE,  $\rho_{\rm EDE}$ , is that when  $\phi$  slowly rolls on the potential at early times,  $\rho_{\rm EDE}$  is almost constant and acts like a cosmological constant, and then when the effective mass of  $\phi$  becomes the same as the Hubble rate it starts to oscillate around the minimum of its potential. Around the minimum, the potential can be approximated as  $V \propto \phi^{2\alpha}$  and hence its energy density scales as  $\rho_{EDE} \propto a^{-4}$  for  $\alpha = 2$ ,  $\rho_{EDE} \propto a^{-9/2}$ for  $\alpha = 3$ , and so on. If EDE starts to oscillate around the epoch of recombination and has some energy fraction at the beginning of its oscillation, EDE affects the evolution of perturbations around recombination, and then soon becomes irrelevant to the evolution of the Universe since  $\rho_{\rm EDE}$  dilutes away faster than matter, which is a scenario considered in the context of the  $H_0$  tension. However, here we discuss a case where EDE can have a sizable energy density fraction at some time during BBN.

In the following, we consider two types of EDE. The first one is essentially the same as that adopted to resolve the  $H_0$ tension [[27](#page-14-6)], in which an EDE component behaves like a cosmological constant at early times, and then its energy density quickly dilutes away at some epoch during BBN. As mentioned above, the energy scale of EDE considered here is different from that motivated by the  $H_0$  tension; such an EDE can be realized by assuming appropriate model parameters even for the same potential as that adopted to resolve the  $H_0$  tension. One could also think of a scenario where two (or more) EDEs are embedded in one framework such as chain dark energy model [\[51](#page-14-28)] in which the Universe experiences multiple first-order phase transitions and some of them act as EDE at the BBN and recombination epochs. Another example of such models is cascading dark energy [\[52\]](#page-14-29) where multiple scalar fields can act as dark energy during different eras, which can also accommodate a scenario where EDEs affect the epochs of recombination and BBN such that they relax both the  $H_0$ tension and the helium anomaly.

Here we just assume an EDE which can have a sizable energy fraction during the BBN epoch, and then its energy density dilutes quickly, and we describe the evolution of its energy density by adopting the following phenomenological model for simplicity and generality such that the description can capture the essential behavior of the model. We model the evolution of the energy density of the first type of EDE, which we refer to as "EDE1" in the following, as

$$
\rho_{\rm EDE1} = \begin{cases} \rho_0 & (T \ge T_t), \\ \rho_0 (\frac{T}{T_t})^n & (T < T_t), \end{cases} \tag{3.1}
$$

where T is the cosmic temperature and  $T<sub>t</sub>$  is the transition temperature at which the energy density changes its behavior.  $n$  is a parameter that describes the scaling of the energy density. Since the Universe is radiationdominated during BBN, the temperature essentially scales as  $T \propto 1+z \propto 1/a$ .  $\rho_0$  is assumed to be constant, and hence it represents the vacuum energy before EDE starts to dilute away. We have modified the PARTHENOPE code [\[42](#page-14-19)[,45,](#page-14-22)[46](#page-14-23)] to include the EDE. In the calculation, we actually use the energy fraction of EDE at the time of transition, denoted as  $f_{\text{EDE}}$ , to control the transition time instead of directly using  $T_t$ , which is defined by

$$
f_{\rm EDE} \equiv \frac{\rho_{\rm EDE}(T_t)}{\rho_{\rm tot}(T_t)} = \frac{\rho_{\rm EDE}(T_t)}{\rho_{\rm EDE}(T_t) + \rho_{rB}(T_t)},\qquad(3.2)
$$

where  $\rho_{\text{tot}}$  is the total energy density including the EDE component and  $\rho_{rB}(T)$  is the sum of energy densities of photons, neutrinos, electrons, and baryons. In our calculation, we properly take account of the time variation of  $\rho_{rB}$  and set  $T_t$  for a given  $f_{\text{EDE}}$ . One can approximately evaluate  $T_t$  for a given  $f_{\text{EDE}}$  as  $T_t \sim 1 \text{ MeV}((\rho_0/1 \text{ MeV}^4)(1 - f_{\text{EDE}}))^{1/4}$ .

<span id="page-5-0"></span>

FIG. 3. Contours of  $D_p$  (left),  $Y_p$  (middle), and  $T_t$  [MeV] (right) in the  $f_{\text{EDE}}-p_0$  plane for EDE1 with  $n = 4$ . 1 $\sigma$  allowed ranges for  $Y_p$ and  $D_p$ , in which both observational and theoretical uncertainties are included, are lightly shaded (magenta). The value of  $\rho_0$  is shown in units of MeV<sup>4</sup>. In this figure, we take  $\eta_{10} = 6.14$ ,  $N_{\text{eff}} = 2.3$ , and  $\xi_e = 0$ .

Since  $\rho_{rB}$  monotonically decreases, but  $\rho_{EDE}$  is constant when  $T > T_t$ , the impact of EDE is the largest at around  $T = T_t$ .

The second type of EDE we consider is one that behaves as a negative cosmological constant until some time during BBN and it quickly settles down to the observed cosmological constant today. Although EDE with a negative energy density may be considered to be somewhat contrived or exotic, a negative cosmological constant has been investigated in the context of the  $H_0$  tension [[34](#page-14-8)[,53,](#page-14-30)[54\]](#page-15-0) and the tension in BAO observations at  $z \approx 2.4$  between the ones observed from Lyman- $\alpha$  forest observations and the predicted values in the  $\Lambda$ CDM model<sup>3</sup> [\[59,](#page-15-1)[60](#page-15-2)]. Furthermore, some theoretical frameworks motivate a negative dark energy such as bimetric gravity [[61](#page-15-3)–[63](#page-15-4)], graduated dark energy [[64](#page-15-5)–[66\]](#page-15-6), ever-present  $\Lambda$  [\[67,](#page-15-7)[68\]](#page-15-8), and so on. In particular, in the ever-present  $\Lambda$  model, the energy fraction of negative dark energy can give a sizable contribution to the total one at some time due to its stochastic nature [[67](#page-15-7),[68](#page-15-8)]. Although one could predict the evolution of such dark energy for a given model, here we assume that the EDE energy density changes from a negative constant to almost zero (actually, to a very small value which can explain the present-day dark energy) at some time during BBN. Since a tiny cosmological constant should be negligible compared to other energy components during the BBN epoch, to study the effect of this second type of EDE, which we refer to as "EDE2" in the following, we model the energy density of EDE2 simply as

$$
\rho_{\rm EDE2} = \begin{cases}\n-\rho_0 & (T \ge T_t), \\
0 & (T < T_t),\n\end{cases} \tag{3.3}
$$

where  $\rho_0$  is a constant, whose value represents the energy density of EDE2 at early times. As in the case of EDE1, instead of using  $T<sub>t</sub>$  we in practice use the energy density fraction of EDE,  $f_{\text{EDE}}$ , to specify the time when the transition from  $\rho_{\text{EDE},2} = -\rho_0$  to  $\rho_{\text{EDE},2} = 0$  occurs in our analysis. Since this kind of EDE can reduce the expansion rate of the Universe at some certain period during BBN, the study of this type of EDE also gives a general insight into models where the expansion rate diminishes at some particular epoch during BBN.

By assuming the two types of EDE described above, we discuss the impact of EDE on the abundance of light elements and its implications for the helium anomaly. In particular, we investigate constraints on the parameters such as  $\eta_{10}$ ,  $N_{\text{eff}}$ , and  $\xi_e$  in the presence of EDE to discuss its impact on BBN, which will be presented in the next section.

### B. Impact of EDE on BBN

Here we discuss how the existence of EDE affects constraints on  $\eta_{10}$ ,  $N_{\text{eff}}$ , and  $\xi_e$  from the abundances of helium and deuterium, especially in light of the result from EMPRESS on  $Y_p$  and the  $H_0$  tension.

First we show contours of  $D_p$ ,  $Y_p$ , and  $T_t$  in the  $f_{\text{EDE}}-\rho_0$ plane for EDE1 with  $n = 4$  $n = 4$ , 5 and 6 in Figs. [3,](#page-5-0) 4, and [5](#page-6-1), respectively, where the other parameters are taken as  $\eta_{10} = 6.14$ ,  $N_{\text{eff}} = 2.3$ , and  $\xi_e = 0$ . The reason why we take  $N_{\text{eff}} = 2.3$ , which is smaller than the standard value, is that when  $N_{\text{eff}} = 3.046$  and  $\xi_e = 0$  are assumed, the value of  $Y_p$  is always larger than the  $1\sigma$  upper limit obtained by EMPRESS in the ranges of  $f_{\text{EDE}}$  and  $\rho_0$  shown in the figure, but by lowering the value of  $N_{\text{eff}}$ ,  $Y_p$  gets smaller so that the  $1\sigma$  allowed range for  $Y_p$  becomes visible. Indeed, this value of  $N_{\text{eff}}$  is almost the same as the mean value for the standard case with  $\xi_e = 0$  obtained in Ref. [\[9\]](#page-13-7). As seen from the figures, the dependences of  $Y_p$  on  $f_{EDE}$  and  $\rho_0$  are almost the same for  $n = 4, 5$ , and 6; on the other hand, the contours for  $D_p$  behave differently for  $n = 4, 5,$  and 6, especially in the large- $\rho_0$  region. However, when one combines the data from  $Y_p$  and  $D_p$ , the allowed region becomes almost independent of  $n$  as shown in Fig. [7](#page-7-0). Actually, the contours for  $T_t$  are the same for  $n = 4, 5$ ,

<sup>&</sup>lt;sup>5</sup>Although the tension has been suggested as  $\sim$ 2 $\sigma$ -2.5 $\sigma$  [\[55](#page-15-9)–[57\]](#page-15-10), it was reduced to  $1.5\sigma$  in a recent measurement [\[58](#page-15-11)].

<span id="page-6-0"></span>

FIG. 4. The same as Fig. [3](#page-5-0) except that  $n = 5$  is assumed in this figure.

<span id="page-6-1"></span>

FIG. 5. The same as Fig. [3](#page-5-0) except that  $n = 6$  is assumed in this figure.

<span id="page-6-2"></span>

FIG. 6. The same as Fig. [3](#page-5-0) except that  $\eta_{10} = 5.80$  and  $n = 6$  are assumed in this figure.

and 6 since  $T<sub>t</sub>$  is the temperature when the energy density of EDE1 changes its behavior, which is irrelevant to the scaling of  $\rho_{\text{EDE1}}$  below  $T = T_t$ .

In Fig. [6,](#page-6-2) the case with  $n = 6$  for  $\eta_{10} = 5.80$ ,  $N_{\text{eff}} = 2.3$ , and  $\xi_e = 0$  is shown, which can be compared with Fig. [5](#page-6-1) where  $\eta_{10} = 6.14$  is assumed with other parameters to be the same as those in Fig. [5](#page-6-1). Since  $\eta_{10} = 5.80$  corresponds to the mean value for the standard case with  $\xi_e = 0$  [[9](#page-13-7)], regions with a smaller  $f_{\text{EDE}}$  are more widely allowed. By comparing Figs. [5](#page-6-1) and [6,](#page-6-2) one can see that when  $\eta_{10}$  is large, the existence of EDE helps to improve the fit to  $Y_p$  and  $D_p$ .

When one assumes  $n > 6$ , the energy density of EDE dilutes faster than that for the cases presented here; however, we can expect that the allowed range from the combination of the data on  $Y_p$  and  $D_p$  will be almost unchanged as the cases for  $n = 4, 5$ , and 6 give the same results. On the other hand, in the case of  $n < 4$ , the energy density of EDE decreases slower than radiation and eventually dominates the Universe. Such an energy component would affect CMB anisotropies, which can easily exclude the model, and hence we do not consider such a case.

Since the existence of EDE affects the abundance of light elements through the change of the expansion rate of the Universe, in which the freeze-out time of nuclear reactions gets modified, the abundances of helium and deuterium

<span id="page-7-0"></span>

FIG. 7. 1 $\sigma$  and  $2\sigma$  allowed regions in the  $\eta_{10}$ -N<sub>eff</sub> plane from measurements of Y<sub>p</sub> and D<sub>p</sub> for EDE1 with  $n = 4$  (left), 5 (middle), and 6 (right). We take  $\rho_0 = 10^{-6}$  MeV<sup>4</sup> and  $f_{\rm EDE} = 0.09$  (light and dark dotted (magenta) for 1 $\sigma$  and 2 $\sigma$  regions) and 0.50 (dark and light striped (orange) for  $1\sigma$  and  $2\sigma$  regions) in all panels. For reference, we also show the constraint for the case without EDE with black dotted (1 $\sigma$ ) and solid (2 $\sigma$ ) lines. In this figure, we assume no lepton asymmetry (i.e.,  $\xi_e = 0$ ).

change depending on  $f_{\text{EDE}}$  and  $\rho_0$ . As  $f_{\text{EDE}}$  or  $\rho_0$  increases (i.e., the effects of EDE become larger), the expansion rate gets bigger, particularly around  $T = T_t$ , which makes the neutron freeze-out occur earlier and hence the value of  $Y_p$ increases. The same tendency also holds true for deuterium, which can be seen from the left panel of the figure. It should also be noticed that, in the bottom half region of the middle panel,  $Y_p$  scarcely changes even when  $f_{\text{EDE}}$  is increased. Indeed, this region corresponds to the one where the transition temperature is lower than 0.07 MeV, as seen from the right panel of the figure. Around this temperature, the helium abundance almost freezes out, below which the value of  $Y_p$  would not be affected even if the expansion rate is changed, i.e., the amount of EDE is irrelevant below  $T<sub>t</sub>$  ∼ 0.07 MeV. This is the reason why  $Y<sub>p</sub>$  almost stays constant regardless of the change of  $f_{\text{EDE}}$ . Compared to  $Y_p$ , since the deuterium abundance evolves gradually and does not reach a constant value until late times,  $D_p$  decreases continuously against the changes of  $f_{\text{EDE}}$  and  $\rho_0$  although the response becomes insensitive in the bottom region, as in the case of  $Y_p$ .

As mentioned above, the cases of  $n = 4, 5$ , and 6 show almost the same tendency for  $Y_p$ ; however, some differences appear for  $D_p$  in the region above  $\rho_0 \gtrsim \mathcal{O}(10^{-6})$  MeV<sup>4</sup>. Since the scaling of the energy density of EDE1 in the  $n = 4$ case is the same as that of radiation, it mimics the effects of  $N_{\text{eff}}$  below  $T = T_i$ ; on the other hand, when  $n = 6$ ,  $\rho_{\text{EDE}}$ quickly dilutes away and EDE scarcely affect the expansion rate any more. Therefore, the difference between the cases with  $n = 4$  and 6 only appears when EDE1 makes a contribution sufficient enough to affect the Hubble expansion rate even for  $T < T_t$ . (The case of  $n = 5$  shows a behavior that is somewhat in between those of  $n = 4$  and  $n = 6$ .) However, the allowed overlapping regions between  $Y_p$  and  $D_p$  are almost the same for the  $n = 4, 5$ , and 6 cases, and the final constraint is also virtually the same. To show this explicitly, we depict constraints from  $Y_p$  and  $D_p$  in the  $\eta_{10}$ -N<sub>eff</sub> plane for the cases of  $n = 4, 5$ , and 6 in Fig. [7.](#page-7-0) In the figure, no lepton asymmetry is assumed (i.e.,  $\xi_e = 0$ ). We fix the value of  $\rho_0$  as  $\rho_0 = 10^{-6}$  MeV<sup>4</sup>, whose value gives a good fit to the data, as shown in Fig. [9](#page-8-0). Furthermore, we take two values for  $f_{\text{EDE}}$  as  $f_{\text{EDE}}$  = 0.09 and 0.5 to show how the constraint depends on  $f_{\rm EDE}$ . As seen from the figure, regardless of the choice of the EDE parameters such as  $\rho_0$  and  $f_{\text{EDE}}$ , the constraints are virtually unchanged even if we assume a different value for *n* when both  $Y_p$  and  $D_p$  are taken into account. Therefore, we only consider the case of  $n = 6$  for EDE1 in the rest of this paper. We should also mention that since the energy density of EDE1 with  $n = 6$  dilutes faster than radiation and becomes negligible just below  $T = T<sub>t</sub>$ , and hence it does not affect the later evolution of the Universe, such an EDE would affect the evolution of the Universe only during the BBN epoch.

Next, in Fig. [8](#page-8-1) we show contours of  $Y_p$  and  $D_p$  for the case of EDE2 in the  $f_{\text{EDE}}$ - $\rho_0$  plane. Here we take  $\eta_{10} =$ 6.14 and  $\xi_e = 0$  as in Figs. [3](#page-5-0)–5, but we take  $N_{\text{eff}} = 3.046$ for this case. Since EDE2 gives a negative contribution to the total energy density of the Universe, which slows down the Hubble expansion rate, the responses of  $Y_p$ and  $D_p$  to the changes of  $f_{\text{EDE}}$  and  $\rho_0$  show an opposite tendency to those in the case of EDE1, i.e., as  $f_{\text{EDE}}$  and/or  $\rho_0$ increase, the values of  $Y_p$  and  $D_p$  decrease. However, as in the EDE1 case, the value of  $Y_p$  is almost unchanged near the bottom right region of the middle panel where the transition temperature is  $T<sub>t</sub> \lesssim 0.07$  MeV. As mentioned above, the helium abundance is almost fixed at this temperature, and hence the change of the expansion rate does not affect the final value of  $Y_p$  when  $T_t < 0.07$  MeV, which is the reason why  $Y_p$  stays almost the same as  $f_{\text{EDE}}$  increases.

Now we are going to discuss the effects of EDE in combination with  $N_{\text{eff}}$ . We show the allowed ranges from the  $Y_p$  and  $D_p$  measurements separately in the  $f_{\text{EDE}}-N_{\text{eff}}$ plane in Figs. [9](#page-8-0) and [10](#page-9-0) for the cases of EDE1 and EDE2, respectively. The  $1\sigma$  and  $2\sigma$  regions, in which both observational and theoretical uncertainties are included, are depicted. In the figures, we fix the baryon density to  $\eta_{10}^{\text{ref},1}$ ,  $\eta_{10}^{\text{ref},2}$ , and  $\eta_{10}^{\text{ref},3}$  as shown in the plots, and take

<span id="page-8-1"></span>

FIG. 8. Contours of  $D_p$  (left),  $Y_p$  (middle), and  $T_t$  [MeV] (right) in the  $f_{\text{EDE}}-\rho_0$  plane for EDE2. The 1 $\sigma$  allowed region for  $Y_p$  and  $D_p$  is shown with light shade (magenta). The value of  $\rho_0$  is shown in units of MeV<sup>4</sup>. In this figure, we take  $\eta_{10} = 6.14$ ,  $N_{\text{eff}} = 3.046$ , and  $\xi_e = 0$ .

<span id="page-8-0"></span>

FIG. 9. 1 $\sigma$  and  $2\sigma$  allowed ranges from observations of  $Y_p$  [\[9\]](#page-13-7) (light and dark dotted (blue)) and  $D_p$  [\[26\]](#page-14-5) (light and dark shaded (magenta)) in the  $f_{\text{EDE}}-N_{\text{eff}}$  plane for EDE1 with  $n = 6$ . The priors for  $\eta_{10}$  assumed in the analysis are  $\eta_{10} = \eta_{10}^{\text{ref},1}$  (top),  $\eta_{10}^{\text{ref},2}$  (middle), and  $\eta_{10}^{\text{ref},3}$  (bottom), as shown in the figure. The value of  $\rho_0$  is fixed and is also shown in the figure. In all panels, the electron neutrino degeneracy parameter is fixed as  $\xi_e = 0$ .

several values for  $\rho_0$  which are also indicated in the figure. In all cases, we take the electron neutrino degeneracy parameter as  $\xi_e = 0$ . From the figure, one can notice that when there is no EDE (i.e., when  $f_{\text{EDE}} \rightarrow 0$ , there is almost no overlapping region between the allowed ones from the  $Y_p$  and  $D_p$  measurements in all cases for both EDE1 and EDE2. This is because, as seen from Fig. [1,](#page-2-1) the allowed regions from  $Y_p$  and  $D_p$  overlap at  $\eta_{10} \sim 5.8$  in the  $\eta_{10} N_{\text{eff}}$  plane when  $\xi_e = 0$ , but here we fix  $\eta_{10}$  to  $\eta_{10}^{\text{ref},1}$ ,  $\eta_{10}^{\text{ref},2}$ , and  $\eta_{10}^{\text{ref},3}$ , which are larger than  $\eta_{10}$  ~ 5.8. However, as  $f_{\text{EDE}}$  increases, the overlapping region between the ones allowed by  $Y_p$  and  $D_p$  measurements appears, which indicates that EDE can improve the fit.

<span id="page-9-0"></span>

FIG. 10. The same as Fig. [9](#page-8-0) except that EDE2 is assumed in this figure.

For the case of EDE1 with the value of  $\rho_0$  shown in the figure, the transition temperature  $T<sub>t</sub>$  is smaller than 0.07 MeV in most of the range of  $f_{\rm EDE}$ , and hence the value of  $Y_p$  scarcely changes even when  $f_{\text{EDE}}$  is increased, as explained above. It should also be noticed that  $N_{\text{eff}}$  has to be smaller than the standard value ( $N_{\text{eff}} = 3.046$ ) when  $\xi_e = 0$  to satisfy the EMPRESS Y<sub>p</sub> value, as seen in the left panel of Fig. [1.](#page-2-1) Therefore, the allowed region from the  $Y_p$ measurement occupies somewhere below  $N_{\text{eff}} = 3.046$ almost along the horizontal direction to the axis of  $f_{EDE}$ . Contrary to the behavior of  $Y_p$ , the deuterium abundance  $D_p$  gets smaller as  $f_{\text{EDE}}$  increases, and hence the overlapping region appears at some value of  $f_{\text{EDE}}$ , which means that we do not need to assume lepton asymmetry (however, we need a nonstandard value of  $N_{\text{eff}}$ ) when the EDE exists. This holds true for all cases of  $\eta_{10}^{\text{ref},1}, \eta_{10}^{\text{ref},2}$ , and  $\eta_{10}^{\text{ref},3}$ , although a large fraction of EDE is required when the baryon density is larger (i.e., in the cases of  $\eta_{10}^{\text{ref},2}$  and  $\eta_{10}^{\text{ref},3}$ ), which can be noticed by comparing the top and other two lower panels in Fig. [9.](#page-8-0) When  $\rho_0$  is taken to be small, there is (almost) no overlapping region due to the small contribution from EDE, particularly for the priors of  $\eta_{10}^{\text{ref},2}$  and  $\eta_{10}^{\text{ref},3}$ .

In the case of EDE2 shown in Fig. [10](#page-9-0), the responses of  $D_p$  and  $Y_p$  against the increase of  $f_{\text{EDE}}$  are opposite to those for EDE1, which were already presented in Fig. [8](#page-8-1).

However, as in the EDE1 case shown in Fig. [9,](#page-8-0) the overlapping region between the allowed ones from the  $Y_p$  and  $D_p$  measurements appears as  $f_{\text{EDE}}$  increases. It should be noticed that the value of  $N_{\text{eff}}$  in the overlapping region lies around the standard value for the case of the prior of  $\eta_{10} = \eta_{10}^{\text{ref},1}$ . This means that the existence of EDE2 can help to fit the EMPRESS  $Y_p$  result [\[9\]](#page-13-7) in combination with the compiled data of  $D_p$  [[48](#page-14-25)] without assuming the deviation of  $N<sub>eff</sub>$  from the standard value and with no lepton asymmetry. On the other hand, when a higher baryon density prior such as  $\eta_{10} = \eta_{10}^{\text{ref},2}$  and  $\eta_{10}^{\text{ref},3}$  is adopted, having an overlapping region becomes a bit difficult, which can be observed from the lower two panels in Fig. [10.](#page-9-0) Even when such a region exists, the value of  $N_{\text{eff}}$  is somewhat higher than the standard value. However, we again remark that no lepton asymmetry is assumed in all cases shown in Fig. [10](#page-9-0). Thus the EMPRESS  $Y_p$  result can be well fitted by assuming the existence of EDE without lepton asymmetry although some nonstandard value for  $N<sub>eff</sub>$  could be required, particularly when the baryon density is high.

To see what values are preferred for the EDE parameters from observations of  $Y_p$  and  $D_p$ , we show the  $1\sigma$  and  $2\sigma$ allowed regions in the  $f_{\text{EDE}}-\rho_0$  plane for the EDE1 and EDE2 cases in Figs. [11](#page-10-0) and [12,](#page-10-1) respectively. In these figures, we take  $\xi_e = 0$  and assume the prior for the baryon

<span id="page-10-0"></span>

FIG. 11. 1 $\sigma$  and  $2\sigma$  allowed regions (light and dark shade (magenta), respectively) in the  $\rho_0$ - $f_{\rm EDE}$  plane from measurements of  $Y_p$  and  $D_p$  for EDE1 with  $n = 6$  in the cases of  $\eta_{10} = \eta_{10}^{\text{ref},1}$  (left) and  $\eta_{10}^{\text{ref},2}$  (right). Here we vary  $N_{\text{eff}}$  and marginalize it. No lepton asymmetry is assumed (i.e.,  $\xi_e = 0$ ).

<span id="page-10-1"></span>

FIG. 12. The same as Fig. [11](#page-10-0) but for the case of EDE2.

density as  $\eta_{10}^{\text{ref},1}$  (left panel) and  $\eta_{10}^{\text{ref},2}$  (right panel). When we adopt the prior of  $\eta_{10}^{\text{ref},3}$ , we can easily expect that its behavior would be somewhat in between those for  $\eta_{10}^{\text{ref,1}}$ and  $\eta_{10}^{\text{ref},2}$ , and hence we do not show such a case here. To obtain the constraints, we vary  $N_{\text{eff}}$  and marginalize it by choosing the value of  $N_{\text{eff}}$  that minimizes the value of  $\chi^2$ for a given set of  $(f_{\text{EDE}}, \rho_0)$ . As seen from the figures, a nonzero value of  $f_{\text{EDE}}$  is preferred, which means that the existence of EDE can help to improve the fit. However, for the case of EDE1, although  $\xi_e = 0$  can be allowed with the existence of EDE, the value of  $N_{\text{eff}}$  preferred around the  $1\sigma$  allowed region in the  $f_{\text{EDE}}-\rho_0$  plane is  $2 \lesssim N_{\rm eff} \lesssim 2.5$  for the priors of both  $\eta_{10}^{\rm ref,1}$  and  $\eta_{10}^{\rm ref,2}$ . On the other hand, for the EDE2 case with the prior of  $\eta_{10}^{\text{ref,1}}$ , the standard value of  $N_{\text{eff}} \sim 3$  is preferred around the  $1\sigma$ allowed region, which indicates that the standard scenario with  $N_{\text{eff}} = 3.046$  and  $\xi_e = 0$  can be well allowed with the existence of EDE2. When the prior of  $\eta_{10}^{\text{ref},2}$  is adopted for EDE2, a large value for  $f_{\text{EDE}}$  is preferred, but with an  $N_{\text{eff}}$  larger than the standard case as  $N_{\text{eff}} \sim 4$ . Even though a nonstandard value for  $N_{\text{eff}}$  may still be needed in some cases (but with  $\xi_e = 0$ ), Figs. [11](#page-10-0) and [12](#page-10-1) show that EDE can help to improve the fit to EMPRESS  $Y_p$  in combination with  $D_n$ .

Next we show constraints from  $Y_p$  and  $D_p$  in the  $\eta_{10}$ -N<sub>eff</sub> plane in the presence of EDE with  $f_{\rm EDE}$  and  $\rho_0$  being fixed to some values in Fig. [13](#page-11-0). The EDE1 and EDE2 cases are, respectively, depicted in left and right panels with  $\xi_e = 0$ fixed. For the EDE1 case, we take  $f_{\text{EDE}} = 0.09$  (magenta) and 0.5 (orange) with  $\rho_0 = 10^{-6}$  MeV<sup>4</sup>, where light and dark regions, respectively, correspond to the  $1\sigma$  and  $2\sigma$ allowed regions. For the EDE2 case,  $f_{EDE} = 0.23$  (magenta) and 0.44 (orange) are assumed with  $\rho_0 = 10^{-2}$  MeV<sup>4</sup>. We fix the EDE parameters  $f_{\text{EDE}}$  and  $\rho_0$  to show how EDE can improve the fit to  $Y_p$  and  $D_p$ . For example, in the EDE1 case, when we take  $\rho_0 = 10^{-6}$  MeV<sup>4</sup>, the existence of EDE can improve the fit depending on the value of  $f_{\text{EDE}}$ . As seen

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FIG. 13. 1 $\sigma$  and  $2\sigma$  allowed regions in the  $\eta_{10}$ -N<sub>eff</sub> plane from measurements of  $Y_p$  and  $D_p$  for the cases of EDE1 (left) and EDE2 (right). In the left panel, we take  $\rho_0 = 10^{-6}$  MeV<sup>4</sup> with  $f_{\rm EDE} = 0.09$  (light and dark dotted (magenta) for  $1\sigma$  and  $2\sigma$  regions) and 0.50 (dark and light striped (orange) for 1 $\sigma$  and 2 $\sigma$  regions). In the right panel, we take  $\rho_0 = 10^{-2}$  MeV<sup>4</sup> with  $f_{\rm EDE} = 0.23$  (light and dark dotted (magenta) for  $1\sigma$  and  $2\sigma$  regions) and 0.44 (dark and light striped (orange) for  $1\sigma$  and  $2\sigma$  regions). For reference, we also show the constraint for the case without EDE with black dotted  $(1\sigma)$  and solid  $(2\sigma)$  lines. In both panels, we assume no lepton asymmetry (i.e.,  $\xi_e = 0$ ).

in the left panel of Fig. [11](#page-10-0), although  $f_{\text{EDE}} = 0.09$  corresponds to the parameter near the boundary of the  $1\sigma$  allowed region,  $f_{\text{EDE}} = 0.5$  can give a good fit such that the model is well allowed within  $1\sigma$ . By comparing these cases, one can see how the EDE parameters affect the constraints in the  $\eta_{10}$ -N<sub>eff</sub> plane. The choice for the EDE2 case is made in the same spirit.

In the EDE1 case, the deuterium abundance is more affected than  $Y_p$ , and hence the effect of  $f_{EDE}$  degenerates with that of the baryon density since  $D_p$  is sensitive to the change of  $\eta_{10}$ . Therefore, as  $f_{\text{EDE}}$  increases, the allowed region shifts almost horizontally to the right. As discussed in the previous section, when the baryon density is suggested to take a larger value,  $N_{\text{eff}}$  needs to be larger than the standard case and  $\xi_e$  should be (positively) nonzero when no EDE is assumed (see Fig. [1\)](#page-2-1). However, when EDE is present, as the fraction of EDE increases, the allowed region is shifted to a higher value of  $\eta_{10}$ , although  $N_{\text{eff}}$ needs to be smaller than the standard value of  $N_{\text{eff}} = 3.046$ . Even if the  $H_0$  tension really demands that we need a high value for  $\eta_{10}$ , the EDE1 model can reduce the discrepancy of the baryon density between the EMPRESS  $Y_p$  result and CMB data with a low value for  $N_{\text{eff}}$ .

In the case of EDE2, the value of  $Y_p$  is decreased by taking a larger value for  $f_{\text{EDE}}$ , which can cancel the increase of  $Y_p$  resulting from a larger value for  $N_{\text{eff}}$ . Therefore, by appropriately choosing the values of  $f_{\text{EDE}}$ and  $\rho_0$ , the EDE model can well fit the EMPRESS  $Y_p$  [\[9\]](#page-13-7) and  $D_p$  result from Ref. [\[26\]](#page-14-5) simultaneously with the standard value of  $N_{\text{eff}}$  and without assuming lepton asymmetry when the baryon density is  $\eta_{10} \sim 6.14$ , which was obtained from the Planck data in the framework of ΛCDM. However, when a higher baryon density is suggested from CMB data, which could be motivated in light of the  $H_0$  tension, one needs a larger value for  $N_{\text{eff}}$ than the standard one. When  $\eta_{10} \sim 6.4$ , the EDE2 model with  $f_{\text{EDE}} = 0.44$  and  $\rho_0 = 8 \times 10^{-2}$  MeV<sup>4</sup> can be well fitted to the data, but with  $N_{\text{eff}} = 4.0$ . In any case, the existence of EDE can help to improve the fit to the EMPRESS  $Y_p$  result without resorting to lepton asymmetry even if a higher baryon density is suggested.

Finally, we discuss constraints in the  $N_{\text{eff}}-\xi_e$  plane. The  $1\sigma$  and  $2\sigma$  allowed regions are shown for the cases of EDE1 and EDE2 in Figs. [14](#page-12-0) and [15,](#page-12-1) respectively. In each figure, two priors for  $\eta_{10}$ , i.e.,  $\eta_{10} = \eta_{10}^{\text{ref},1} \pm \sigma_{\eta_{10},1}$  and  $\eta_{10}^{\text{ref},2} \pm \sigma_{\eta_{10},2}$ , are adopted, which are, respectively, shown in left and right panels in the figures. In these figures, we fix the EDE parameters  $f_{\text{EDE}}$  and  $\rho_0$  to some specific values, whose actual values are chosen in the same spirit as the one for Fig. [13](#page-11-0), which has already been mentioned above. For reference, we also show the constraints for the case without EDE.

In the case of EDE1 shown in Fig. [14,](#page-12-0) we take  $f_{\text{EDE}} =$ 0.09 (magenta) and 0.44 (orange) with  $\rho_0 = 10^{-6}$  MeV<sup>4</sup>, where light and dark regions correspond to the  $1\sigma$  and  $2\sigma$ allowed regions, respectively. Since a larger  $f_{\text{EDE}}$  gives larger  $Y_p$  and  $D_p$ , the decreases of  $N_{\text{eff}}$  and  $\xi_e$  are canceled by a large value of  $f_{\text{EDE}}$  and hence the allowed region shifts to the one with smaller  $N_{\text{eff}}$  and smaller  $\xi_e$  by increasing  $f_{\text{EDE}}$ . Although the standard point with  $N_{\text{eff}} = 3.046$  and  $\xi_e = 0$  is a bit away from the  $2\sigma$  bound for the priors of both  $\eta_{10}^{\text{ref,1}}$  and  $\eta_{10}^{\text{ref,2}}$ , either  $N_{\text{eff}} = 3.046$  or  $\xi_e = 0$  can be realized by appropriately choosing the values of  $f_{\text{EDE}}$  and  $\rho_0$  in the EDE1 case. Notice that this holds true even if the prior of a large baryon density  $\eta_{10}^{\text{ref},2}$  is adopted where a

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FIG. 14.  $1\sigma$  and  $2\sigma$  allowed regions in the  $N_{\text{eff}}$ - $\xi_e$  plane for the case with EDE1, adopting the priors of  $\eta_{10} = \eta_{10}^{\text{ref},1} \pm \sigma_{\eta_{10},1}$  (left) and  $\eta_{10} = \eta_{10}^{\text{ref},2} \pm \sigma_{\eta_{10},2}$  (right). We take  $f_{\text{EDE}} = 0.09$  (light and dark dotted (magenta) for  $1\sigma$  and  $2\sigma$  regions) and 0.44 (dark and light striped (orange) for  $1\sigma$  and  $2\sigma$  regions) with  $\rho_0 = 10^{-6}$  MeV<sup>4</sup>. For reference, we also show the constraint for the case without EDE with black dotted  $(1\sigma)$  and solid  $(2\sigma)$  lines.

<span id="page-12-1"></span>

FIG. 15. 1 $\sigma$  and 2 $\sigma$  allowed regions in the  $N_{\text{eff}}$ - $\xi_e$  plane for the case with the EDE2, adopting the priors of  $\eta_{10} = \eta_{10}^{\text{ref,1}} \pm \sigma_{\eta_{10},1}$  (left) and  $\eta_{10} = \eta_{10}^{\text{ref},2} \pm \sigma_{\eta_{10},2}$  (right). In the left panel, we take  $f_{\text{EDE}} = 0.17$  (light and dark dotted (magenta) for  $1\sigma$  and  $2\sigma$  regions) and 0.44 (dark and light striped (orange) for  $1\sigma$  and  $2\sigma$  regions). In the right panel, we take  $f_{\text{EDE}} = 0.41$  (light and dark dotted (magenta) for  $1\sigma$ and  $2\sigma$  regions) and 0.47 (dark and light striped (orange) for  $1\sigma$  and  $2\sigma$  regions). In both panels,  $\rho_0$  is assumed as  $\rho_0 = 10^{-1}$  MeV<sup>4</sup>. For reference, we also show the constraint for the case without EDE with black dotted  $(1\sigma)$  and solid  $(2\sigma)$  lines.

greater deviation from the standard values for both  $N_{\text{eff}}$  and  $\xi_e$  is required to fit the EMPRESS  $Y_p$  result without EDE.

In the case of EDE2, depicted in Fig. [15](#page-12-1), we assume  $f_{\rm EDE} = 0.17$  (magenta) and 0.44 (orange) in the left panel. In the right panel,  $f_{\rm EDE} = 0.41$  (magenta) and 0.47 (orange) are assumed. In both panels, we take  $\rho_0 = 10^{-1}$  MeV<sup>4</sup>. As can be noticed from the figure, by changing the values of  $f_{\text{EDE}}$  and  $\rho_0$ , the allowed region in the  $N_{\text{eff}}-\xi_e$  plane moves almost vertically downwards. One can see that, when the baryon density is  $\eta_{10} \sim 6.14$ , the standard value of  $N_{\text{eff}}$  with no lepton asymmetry can be well fitted to the EMPRESS  $Y_p$  result in the presence of EDE with appropriately chosen  $f_{\text{EDE}}$  and  $\rho_0$ . On the other hand, when a high baryon density prior of  $\eta_{10}^{\text{ref},2}$  is adopted, the EMPRESS result demands a value of  $N_{\text{eff}}$  higher than the standard one, even assuming the presence of EDE. However, it should be emphasized that both a high value of  $N_{\text{eff}}$  and a positively nonzero  $\xi_e$  are required to fit the EMPRESS  $Y_p$  result when EDE is absent, which can be seen from the right panel of Fig. [2](#page-3-0); on the other hand, once we assume EDE, one can fit the EMPRESS  $Y_p$  without any lepton asymmetry, which indicates that EDE can mitigate the helium anomaly caused by the EMPRESS  $Y_p$  results.

#### IV. CONCLUSION AND DISCUSSION

In this paper, we first investigated the impact of the  $H_0$ tension, in which a higher value for the baryon density than that in the ΛCDM framework could be preferred,

on BBN in light of recent  $Y_p$  measurement by EMPRESS. As already pointed out [[9\]](#page-13-7), the EMPRESS  $Y_p$  result would infer a value of  $N_{\text{eff}}$  higher than the standard case and a positively nonzero value of  $\xi_e$ . However, given that models proposed to resolve the  $H_0$  tension tend to prefer a higher baryon density than that in the ΛCDM model adopted in Ref. [[9\]](#page-13-7), the deviation from the standard assumption ( $N_{\text{eff}} = 3.046$  and  $\xi_e = 0$ ) would be more significant. As shown in Figs. [1](#page-2-1) and [2,](#page-3-0) when a large  $\eta_{10}$  is assumed, which is suggested by the  $H_0$  tension,  $N_{\text{eff}}$  needs to be much larger than the standard value of  $N_{\text{eff}} = 3.046$  and  $\xi_e$  should take a large positively nonzero value to explain the EMPRESS  $Y_p$  value in combination with the  $D_p$  measurement of Ref. [\[26\]](#page-14-5). Therefore, the  $H_0$  tension could also affect BBN, which shows that the tension would have a further impact on other aspects of cosmology.

We also studied the effects of early dark energy, which has been extensively investigated in the context of the  $H_0$ tension, on the abundances of helium and deuterium. As mentioned above, the EMPRESS  $Y_p$  results suggest that nonstandard values of  $N_{\text{eff}}$  and a nonzero  $\xi_e$  are necessary to have a good fit to  $Y_p$  and  $D_p$  data simultaneously; however, by assuming the existence of early dark energy which takes a sizable fraction in the total energy density during BBN, the values of  $N_{\text{eff}}$  and  $\xi_e$  can still take the standard values, depending on the EDE model and parameters. Even if a larger value of  $\eta_{10}$  is assumed, which could be demanded by models resolving the  $H_0$ tension, the existence of early dark energy can still reduce the tension such that  $N_{\text{eff}}$  and  $\xi_e$  can take values close to the standard ones. Therefore, early dark energy can improve the fit even in the case of a large baryon density in light of the EMPRESS  $Y_p$  results.

The recent EMPRESS results may suggest physics beyond the standard cosmological model. By taking account of the  $H_0$  tension, which is one of the most significant tensions in cosmology today, more modification and extension to the standard model would be required. Our study may indicate that the tensions in cosmology should be simultaneously investigated in order to pursue a new cosmological model, from which one can gain profound insight into not only the evolution of the Universe, but also the fundamental law of physics.

#### ACKNOWLEDGMENTS

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