Absolute measurements of branching fractions of Cabibbo-suppressed hadronic $D^{0(+)}$ decays involving multiple pions

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By analyzing e^+e^- annihilation data with an integrated luminosity of 2.93 fb⁻¹ collected at the center-ofmass energy $\sqrt{s} = 3.773$ GeV with the BESIII detector, we present the first absolute measurements of the branching fractions of twenty Cabibbo-suppressed hadronic $D^{0(+)}$ decays involving multiple pions. The highest four branching fractions obtained are $\mathcal{B}(D^0 \to \pi^+\pi^-\pi^0) = (1.343 \pm 0.013_{\text{stat}} \pm 0.016_{\text{syst}})\%$, $\mathcal{B}(D^0 \to \pi^+\pi^-2\pi^0) = (1.002\pm0.019_{\text{stat}}\pm0.024_{\text{syst}})\%$, $\mathcal{B}(D^+ \to 2\pi^+\pi^-\pi^0) = (1.165\pm0.021_{\text{stat}}\pm0.021_{\text{syst}})\%$, and $\mathcal{B}(D^+ \to 2\pi^+\pi^-2\pi^0) = (1.074\pm0.040_{\text{stat}}\pm0.030_{\text{syst}})\%$. The *CP* asymmetries for the six decays with highest signal yields are also determined and found to be compatible with zero.

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I. INTRODUCTION

Investigations of hadronic $D^{0(+)}$ decays are of general importance for both charm and bottom physics. For example, Ref. [1] suggests that hadronic $D^{0(+)}$ decays involving three charged pions are crucial backgrounds for the tests of lepton flavor universality (LFU) in semileptonic *B* decays. However, many Cabibbo-suppressed hadronic $D^{0(+)}$ decays with three charged pions are unexplored mainly due to low detection efficiencies and high background contamination. Precision and comprehensive measurements of the absolute branching fractions (BFs) of these decays provide necessary inputs to unravel the hints of LFU violation observed in semileptonic *B* decays.

According to theoretical predictions, direct *CP* violation in charmed hadron decays is expected to be at the order of 10^{-3} for singly Cabibbo-suppressed processes, and much smaller for Cabibbo-favored and doubly Cabibbosuppressed processes [2–9]. The LHCb experiment reported the first observation of *CP* violation in $D^0 \rightarrow K^+K^-$ and $\pi^+\pi^-$ with an asymmetry difference of $\Delta A_{CP} = (1.54 \pm$ $0.29) \times 10^{-3}$ [10]. A similar magnitude of *CP* asymmetry is predicted in $D^0 \rightarrow K^+K^{*-}$ and $D^0 \rightarrow \rho^+\pi^-$ [8]. References [2,3] suggest that the *CP* asymmetries in $D \rightarrow \rho\pi$ decays are in the range of $(0.3 \sim 5) \times 10^{-4}$. Therefore, searching for *CP* violation in Cabibbo-suppressed $D^{0(+)}$ decays into three pions is an interesting pursuit. The Cabibbo-suppressed hadronic neutral *D* decays into $\pi^+\pi^-\pi^0$ and $\pi^+\pi^-\pi^0\pi^0$ also provide a promising way to extract the Cabibbo-Kobayashi-Maskawa angle γ in $B^+ \rightarrow D^{(*)0}K^{(*)+}$ [11]. More precise measurements of these BFs or improved knowledge of *CP*-even fractions can improve the measurement precision for the *CP* violation phase angle γ with these modes.

This paper reports the first absolute measurements of the BFs of the Cabibbo-suppressed hadronic decays $D^0 \rightarrow \pi^+\pi^-\pi^0$, $\pi^+\pi^-2\pi^0$, $\pi^+\pi^-2\eta$, $4\pi^0$, $3\pi^0\eta$, $2\pi^+2\pi^-\pi^0$, $2\pi^+2\pi^-\eta$, $\pi^+\pi^-3\pi^0$, $2\pi^+2\pi^-2\pi^0$, and $D^+ \rightarrow 2\pi^+\pi^-$, $\pi^+2\pi^0$, $2\pi^+\pi^-\pi^0$, $\pi^+3\pi^0$, $3\pi^+2\pi^-$, $2\pi^+\pi^-2\pi^0$, $2\pi^+\pi^-\pi^0\eta$, $\pi^+4\pi^0$, $\pi^+3\pi^0\eta$, $3\pi^+2\pi^-\pi^0$, $2\pi^+\pi^-3\pi^0$ based on 2.93 fb⁻¹ of e^+e^- annihilation data taken at the center-of-mass energy $\sqrt{s} = 3.773$ GeV with the BESIII detector [12]. Moreover, the *CP* asymmetries for the six decays with the highest yields are determined. To date, only the BFs of seven of these decay modes have been measured relative to reference modes and only the *CP* asymmetries in $D^0(\bar{D}^0) \rightarrow \pi^+\pi^-\pi^0$ and $D^{\pm} \rightarrow$ $\pi^+\pi^-\pi^{\pm}$ have been measured by various experiments [13]. Throughout this article, charge-conjugated processes are implied except when discussing *CP* asymmetries.

II. BESIII AND MONTE CARLO SIMULATION

The BESIII detector is a magnetic spectrometer [14] located at the Beijing Electron Positron Collider (BEPCII) [15]. The cylindrical core of the BESIII detector consists of a helium-based multilayer drift chamber, a plastic scintillator time-of-flight system (TOF), and a CsI (Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive-plate counter muon-identifier modules interleaved with steel. The acceptance of charged particles and photons is 93% over 4π solid angle. The charged-particle momentum resolution at 1 GeV/c is 0.5%, and the resolution of the specific ionization energy loss (dE/dx) is 6% for the electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the

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barrel (end cap) region. The time resolution of the TOF barrel part is 68 ps, while that of the end cap part is 110 ps.

Simulated samples produced with a GEANT4-based [16] Monte Carlo (MC) package including the geometric description of the BESIII detector and the detector response, are used to determine the detection efficiencies and to estimate backgrounds. The simulation of $e^+e^$ annihilations modeled with the generator KKMC [17] includes the beam-energy spread and initial-state radiation. The inclusive MC samples consist of the production of $D\bar{D}$ pairs with consideration of quantum coherence for all neutral D modes, the non- $D\bar{D}$ decays of the $\psi(3770)$, the initial-state radiation production of the J/ψ and $\psi(3686)$ states, and continuum processes. Known decay modes are modeled with EVTGEN [18] using the BFs taken from Ref. [13], and the remaining unknown decays of the charmonium states are modeled with LUNDCHARM [19,20]. Final-state radiation from charged final-state particles is incorporated using PHOTOS [21].

III. MEASUREMENT METHOD

At $\sqrt{s} = 3.773$ GeV, the $D^0\bar{D}^0$ or D^+D^- pairs are produced without accompanying hadron(s), thereby offering a clean environment to investigate hadronic D decays with the double-tag (DT) method [22]. The single-tag (ST) \bar{D} candidates are selected by reconstructing a \bar{D}^0 or D^- in the hadronic decay modes: $\bar{D}^0 \rightarrow K^+\pi^-$, $K^+\pi^-\pi^0$, and $K^+\pi^-\pi^-\pi^+$, and $D^- \rightarrow K^+\pi^-\pi^-$, $K^0_S\pi^-$, $K^+\pi^-\pi^-\pi^0$, $K^0_S\pi^-\pi^0$, $K^0_S\pi^+\pi^-\pi^-$, and $K^+K^-\pi^-$. Events in which a signal candidate is reconstructed in the presence of an ST \bar{D} meson are referred to as DT events. The BF of the signal decay is determined by [23]

$$\mathcal{B}_{\rm sig} = N_{\rm DT} / (N_{\rm ST}^{\rm tot} \cdot \epsilon_{\rm sig}), \tag{1}$$

where $N_{\text{ST}}^{\text{tot}} = \sum_{i} N_{\text{ST}}^{i}$ and N_{DT} are the total yields of the ST and DT candidates in data, respectively. The ST yield for the tag mode *i* is N_{ST}^{i} , and the efficiency ϵ_{sig} for detecting the signal *D* decay is averaged over the tag modes *i*.

IV. DATA ANALYSIS

The selection criteria of K^{\pm} , π^{\pm} , K_S^0 , π^0 , and η are the same as those used in the analyses presented in Refs. [23,24]. For $\bar{D}^0 \to K^+\pi^-$, the backgrounds from cosmic rays and Bhabha events are rejected by using the same requirements described in Ref. [25]. For $\bar{D}^0 \to K^+\pi^-\pi^-\pi^+$, the $\bar{D}^0 \to K_S^0K^{\pm}\pi^{\mp}$ decays are suppressed by requiring the invariant masses of all $\pi^+\pi^-$ pairs to be outside the mass window (0.483, 0.513) GeV/ c^2 .

Tagged \bar{D} mesons are identified using two variables: the energy difference $\Delta E_{\text{tag}} \equiv E_{\text{tag}} - E_{\text{b}}$ and the beam-constrained mass $M_{\text{BC}}^{\text{tag}} \equiv \sqrt{E_{\text{b}}^2 - |\vec{p}_{\text{tag}}|^2}$. Here, E_{b} is the beam energy, \vec{p}_{tag} and E_{tag} are the momentum and energy of \bar{D} in the rest

frame of e^+e^- system, respectively. The ΔE_{tag} of ST \overline{D} candidates must be in the range (-55, 40) MeV for the tag modes involving π^0 and (-25, 25) MeV for the other tag modes, due to differing resolutions. For each tag mode, if there are multiple candidates in an event, only the one yielding the least $|\Delta E_{\text{tag}}|$ is accepted.

To extract the yields of ST \overline{D} candidates for individual tag modes, binned maximum-likelihood fits are performed to the corresponding M_{BC}^{tag} distributions of the accepted ST candidates following Ref. [24]. The \overline{D} signal is modeled by an MC-simulated shape convolved with a double-Gaussian function describing the resolution difference between the data and MC simulation. The combinatorial background shape is described by an ARGUS function [26]. The total yields of the ST \overline{D}^0 and D^- candidates in data are (232.8 ± $0.2_{stat}) \times 10^4$ and (155.8 ± $0.2_{stat}) \times 10^4$, respectively.

The signal *D* decays are selected from the remaining tracks and showers recoiling against the tagged \overline{D} candidates. To reject the main backgrounds from Cabibbo-suppressed decays containing K_S^0 , the $\pi^+\pi^-$ and $\pi^0\pi^0$ combinations are required to not fall in the mass windows (0.468, 0.528) and (0.428, 0.548) GeV/ c^2 , respectively. These mass windows correspond to at least 4σ of resolution.

Signal *D* mesons are identified using the energy difference ΔE_{sig} and the beam-constrained mass M_{BC}^{sig} , calculated similarly to the ST side. For each signal mode, if there are multiple candidates in an event, only the one with the minimum $|\Delta E_{sig}|$ is chosen. Signal decays are required to satisfy the ΔE_{sig} requirements shown in Table I.

For each signal decay mode, the signal yield $(N_{\rm DT})$ is obtained from a two-dimensional (2D) unbinned maximumlikelihood fit [27] to the $M_{\rm BC}^{\rm tag}$ versus $M_{\rm BC}^{\rm sig}$ distribution of the accepted DT candidates. Figure 1 shows the $M_{\rm BC}^{\rm tag}$ versus $M_{\rm BC}^{\rm sig}$ distribution of the accepted DT candidates in data. The signal events concentrate around $M_{\rm BC}^{\rm tag} = M_{\rm BC}^{\rm sig} = M_D$, where M_D is the averaged mass of D [13]. The events with correctly reconstructed D (\bar{D}) and incorrectly reconstructed \bar{D} (D), referred to as BKGI, spread along the lines around $M_{\rm BC}^{\rm sig} =$ M_D ($M_{\rm BC}^{\rm tag} = M_D$). Events smeared along the diagonal (BKGII) are mainly from the $e^+e^- \rightarrow q\bar{q}$ processes. Events with uncorrelated and incorrectly reconstructed Dand \bar{D} (BKGIII) disperse across the whole allowed kinematic region.

In the fit, the probability density functions (PDFs) for signal, BKGI, BKGII, and BKGIII contributions are constructed as a(x, y), $b_x(x) \cdot c_y(y; M_{BC}^{end}, \xi_y) + b_y(y) \cdot c_x(x; M_{BC}^{end}, \xi_x)$, $c_z(z; \sqrt{2}M_{BC}^{end}, \xi_z) \cdot g(k; 0, \sigma_k)$, and $c_x(x; M_{BC}^{end}, \xi_x) \cdot c_y(y; M_{BC}^{end}, \xi_y)$, respectively. Here, $x = M_{BC}^{sig}$, $y = M_{BC}^{sig}$, $z = (x + y)/\sqrt{2}$, and $k = (x - y)/\sqrt{2}$. The PDFs of signal, a(x, y), $b_x(x)$, and $b_y(y)$, are described by the MC-simulated shapes smeared with individual

TABLE I. Requirements of ΔE_{sig} , DT yields in data (N_{DT}), detection efficiencies (ϵ_{sig} , including the BFs of η , and π^0 as well as correction factors described later), and the obtained BFs (\mathcal{B}_{sig}). The first nine modes are D^0 decays and the others are D^+ decays. For \mathcal{B}_{sig} , numbers in the first and second parentheses are the last two digits of the statistical and systematic uncertainties, respectively. For N_{DT} , uncertainties are statistical only.

Decay	$\Delta E_{\rm sig}~({\rm MeV})$	N _{DT}	$\epsilon_{ m sig}~(\%)$	$\mathcal{B}_{sig}~(\times 10^{-4})$
$\pi^+\pi^-\pi^0$	(-62, 36)	12792.6(120.1)	40.91	134.3(13)(16)
$\pi^+\pi^-2\pi^0$	(-75, 37)	3801.3(70.6)	16.29	100.2(19)(24)
$\pi^+\pi^-2\eta$	(-37, 29)	42.5(6.7)	2.14	8.5(13)(04)
$4\pi^0$	(-105, 41)	96.0(11.5)	5.41	7.6(09)(07)
$3\pi^0\eta$	(-82, 40)	155.3(14.7)	2.83	23.6(22)(17)
$2\pi^+ 2\pi^- \pi^0$	(-52, 33)	942.4(40.0)	11.70	34.6(15)(15)
$2\pi^+2\pi^-\eta$	(-36, 28)	48.5(7.8)	3.46	6.0(10)(06)
$\pi^{+}\pi^{-}3\pi^{0}$	(-76, 39)	182.7(20.9)	5.13	15.3(17)(13)
$2\pi^+ 2\pi^- 2\pi^0$	(-64, 36)	350.0(22.9)	3.15	47.7(31)(21)
$2\pi^+\pi^-$	(-30, 28)	2579.0(57.6)	50.63	32.7(07)(05)
$\pi^+ 2\pi^0$	(-96, 44)	1963.9(51.6)	27.33	46.1(12)(09)
$2\pi^+\pi^-\pi^0$	(-59, 35)	4614.4(83.1)	25.42	116.5(21)(21)
$\pi^+ 3 \pi^0$	(-86, 39)	573.7(30.2)	8.83	41.7(22)(13)
$3\pi^{+}2\pi^{-}$	(-37, 33)	462.1(28.7)	16.26	18.2(11)(10)
$2\pi^{+}\pi^{-}2\pi^{0}$	(-74, 39)	1207.1(45.4)	7.21	107.4(40)(30)
$2\pi^+\pi^-\pi^0\eta$	(-51, 33)	191.4(15.9)	3.17	38.8(32)(12)
$\pi^+ 4 \pi^0$	(-90, 41)	56.7(10.4)	1.87	19.5(36)(23)
$\pi^+ 3 \pi^0 \eta$	(-66, 37)	79.7(10.9)	1.77	28.9(40)(22)
$3\pi^+2\pi^-\pi^0$	(-49, 34)	182.8(17.3)	5.02	23.4(22)(15)
$2\pi^+\pi^-3\pi^0$	(-66, 37)	185.9(17.0)	3.49	34.2(31)(16)



FIG. 1. The $M_{\rm BC}^{\rm tag}$ versus $M_{\rm BC}^{\rm sig}$ distribution of the accepted DT candidates of $D^0 \rightarrow \pi^+ \pi^- \pi^0$ in data. Here, the ISR denotes initial state radiation, which spreads along the diagonal direction and extends to the higher $M_{\rm BC}$ side. The $D_{\rm right}^{\rm sig}$ and $D_{\rm right}^{\rm tag}$ denote the signal spreading around $M_{\rm BC}^{\rm sig} = M_D$ and $M_{\rm BC}^{\rm tag} = M_D$.

Gaussian resolution function with parameters derived from the corresponding one-dimensional $M_{\rm BC}$ fits, to consider resolution difference between data and MC simulation. The $c_f(f; M_{BC}^{end}, \xi_f)$ is an ARGUS function [26] (f denotes x, y, or z), where the end point $M_{\rm BC}^{\rm end} = 1.8865 \, {\rm GeV}/c^2$ is fixed in the fit. The Gaussian function $g(k; 0, \sigma_k)$ has a mean of zero and a standard deviation parametrized by $\sigma_k = \sigma_0$. $(\sqrt{2}M_{\rm BC}^{\rm end}-z)^p$, where σ_0 and p are fit parameters. In addition, the yields and shapes of the peaking background (PBKG) components, which are mainly from D decays into the same final state as a signal mode but involve $K_S^0 \rightarrow \pi^+ \pi^$ or $\pi^0 \pi^0$ and $K^- \rightarrow \pi^- \pi^0$ decay, are fixed based on MC simulations and the known BFs of various PBKG components [13,28]. Relative to the corresponding signal yields, the PBKG components are 9.5%, 18.2%, and 36.2% for $D^+ \to \pi^+ 4 \pi^0$, $D^0 \to 2 \pi^+ 2 \pi^- \pi^0$, and $D^0 \to \pi^+ \pi^- 3 \pi^0$, respectively, and range from 0.1% to 6.3% for the other signal decays.

The M_{BC}^{tag} and M_{BC}^{sig} projections of the 2D fits of the DT candidates reconstructed from data are shown in Fig. 2 and the fitted DT yields are summarized in Table I.

To determine the signal efficiencies (ϵ_{sig}), the three-body decays are simulated with a modified data-driven generator BODY3 [18], which was developed to simulate different intermediate states in data for a given three-body final state. The Dalitz plot from data, corrected for backgrounds and efficiencies, is taken as input for the BODY3 generator. The efficiencies across phase space are obtained with MC samples generated according to a phase space distribution. Each of the four-body and five-body decays is simulated with a mixed signal MC sample. These decays generated with phase space models including contributions from η, ω , $\eta', \rho(770), a_0(980), a_1(1260), b_1(1235), and \phi$ intermediate states are mixed with fractions obtained by examining the corresponding invariant mass spectra. The data distributions for momenta and $\cos\theta$ (where θ is the polar angle of particle in the e^+e^- rest frame) of the daughter particles, and the invariant masses of each of the two-body and multibody particle combinations agree with the MC simulations. As an example, Fig. 3 shows the comparisons for the $D^0 \rightarrow \pi^+ \pi^- \pi^0$ candidates. Some comparisons of the other decay modes can be found in the Supplemental Material [29]. The imperfect data-MC consistencies in the $\pi\pi$ mass spectra will be considered as sources of systematic uncertainties related to the MC generator and K_s^0 rejection in the next section.

The results for $N_{\rm DT}$, $\epsilon_{\rm sig}$, and the extracted BFs are summarized in Table I. For each signal decay, the minimum statistical significance is 6.8 standard deviations for the $D^+ \rightarrow \pi^+ 4\pi^0$ mode. The signal efficiencies have been corrected by the data-MC differences in the selection efficiencies of π^{\pm} tracking, particle identification (PID) procedures and the reconstruction of π^0 or η .



FIG. 2. Projections of M_{BC}^{tag} (left) and M_{BC}^{sig} (right) of the 2D fits to the DT candidate events. Points with error bars are data and blue solid curves are the fit results. Black dotted, cyan blue solid, blue dotted, red dotted, and pink long-dashed correspond to the fitted signal, fixed peaking background, BKGI, BKGII, and BKGIII components, respectively.



FIG. 3. Comparisons of the distributions of invariant masses of two-body particle combinations, momenta and $\cos\theta$ of daughter particles for the $D^0 \rightarrow \pi^+\pi^-\pi^0$ candidates between data (points with error bars) and the BODY3 signal MC events (black solid line histograms) plus the MC-simulated backgrounds from the inclusive MC sample (yellow filled histograms).

V. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties relative to the obtained BFs are discussed below. In the BF determinations using Eq. (1), all uncertainties from selecting the ST \overline{D} candidates are canceled in the ratio. Systematic uncertainties in the total yields of ST \overline{D} mesons related to the $M_{\rm BC}^{\rm tag}$ fits to the ST \overline{D} candidates were previously estimated to be 0.5% for both neutral and charged \overline{D} [30–32].

The tracking and PID efficiencies of π^{\pm} are investigated using other DT $D\bar{D}$ hadronic events. The differences of efficiencies between data and MC simulation are weighted by the corresponding π^{\pm} momentum spectra of signal MC events. The systematic uncertainties due to tracking and PID efficiencies are assigned to be (0.2–0.4)% per π^{\pm} , based on the residual statistical uncertainties of the measured data-MC differences.

The π^0 reconstruction efficiency, which includes the effects of the photon selection, the π^0 mass window and the kinematic fit on $\pi^0 \rightarrow \gamma\gamma$, is studied with the DT $D\bar{D}$ hadronic decay samples of $D^0 \rightarrow K^-\pi^+$, $K^-\pi^+\pi^+\pi^-$ versus $\bar{D}^0 \rightarrow K^+\pi^-\pi^0$, $K_S^0\pi^0$ following Refs. [30,31]. After correcting our signal efficiencies by the momentum weighted data-MC differences, the residual uncertainties are assigned as the systematic uncertainties, which are (0.4-0.9)% per π^0 for various signal decays. Because of limited η statistics, the systematic uncertainty for η reconstruction is assigned by referring to that of π^0 .

The systematic uncertainty in the 2D fit to the $M_{\rm BC}^{\rm tag}$ versus $M_{\rm BC}^{\rm sig}$ distribution is examined by varying the smeared Gaussian function $(\pm 1\sigma)$, the end point of the ARGUS function $(\pm 0.2 \text{ MeV}/c^2)$, and the fixed PBKG yields $(\pm 1\sigma)$ of the quoted BF). Adding the changes from these three sources in quadrature yields the corresponding systematic uncertainties.

The systematic uncertainty due to the ΔE_{sig} requirement ranges from (0.1–1.3)% depending on the signal mode. They are evaluated from the efficiency differences obtained with and without smearing the ΔE_{sig} distributions for signal MC events with parameters derived from $D^0 \rightarrow \pi^+ \pi^- \pi^0$, $D^0 \rightarrow \pi^+ \pi^- 2\pi^0$, $D^+ \rightarrow \pi^+ 2\pi^0$, and $D^+ \rightarrow 2\pi^+ \pi^- \pi^0$ to get the data-MC differences.

The systematic uncertainty due to the BODY3 generator is considered by varying the number of bins by $\pm 20\%$ and the systematic uncertainty in the mixed MC model is assigned by varying the fractions of various components by $\pm 1\sigma$ of the quoted BF, when available. Unmeasured components are varied by $\pm 25\%$, beyond which comparisons with observed mass spectra are unsatisfactory. The largest change of the signal efficiencies, (0.2-5.7)% for various signal modes, are assigned as the corresponding systematic uncertainties.

The systematic uncertainties due to the mass window applied to reject K_S^0 events are cross-checked by examining the changes of the BFs by varying the corresponding boundaries of the window by $\pm 5 \text{ MeV}/c^2$, which is about $\pm 1\sigma$ of the fitted resolution. If the difference of the BF is greater than the statistical uncertainty on the difference (taking the correlated samples into account), it is assigned as the corresponding systematic uncertainty. Otherwise, it is neglected.

The measurements of the BFs of the neutral *D* decays are affected by the quantum correlation (QC) effect [33]. To take this effect into account, the *CP*-even fractions in various decays are needed. The $D^0 \rightarrow 4\pi^0$ and $D^0 \rightarrow 3\pi^0\eta$ final states are both *CP*-even eigenstates. For $D^0 \rightarrow \pi^+\pi^-\pi^0$, its *CP*-even fraction has been determined to be 0.973 ± 0.017 [34]. For $D^0 \rightarrow \pi^+\pi^-2\pi^0$, $D^0 \rightarrow 2\pi^+2\pi^-\pi^0$, $D^0 \rightarrow \pi^+\pi^-3\pi^0$, and $D^0 \rightarrow 2\pi^+2\pi^-2\pi^0$, the *CP*-even fractions are estimated by the *CP*-even tag $D^0 \rightarrow K^+K^-$ and the *CP*-odd tag $D^0 \rightarrow K_s^0\pi^0$.

The obtained ST yields of the *CP*-even tag of $\overline{D}^0 \rightarrow K^+K^-$ and the *CP*-odd tag of $\overline{D}^0 \rightarrow K^0_S \pi^0$ are $S^-_{\text{measured}} = 57779 \pm 287$ and $S^+_{\text{measured}} = 70512 \pm 311$, respectively, which are derived from the fits to individual $M^{\text{tag}}_{\text{BC}}$ distributions of the accepted ST candidates. The DT yields tagged by $CP\pm$ tags from the 2D fits to the $M^{\text{tag}}_{\text{BC}}$ versus $M^{\text{sig}}_{\text{BC}}$ distributions of the accepted DT candidates, and the QC factors obtained with the same method as described in

TABLE II. The DT yields tagged by $CP \mp \text{tags} (M_{\text{measured}}^{\pm})$, the CP+ fractions (f_{CP+}) , and the QC factors (f_{QC}) . The f_{CP+} for $D^0 \rightarrow \pi^+\pi^-\pi^0$ is quoted from Ref. [34]; the f_{CP+} values for $D^0 \rightarrow \pi^+\pi^-2\pi^0$, $D^0 \rightarrow 2\pi^+2\pi^-\pi^0$, $D^0 \rightarrow \pi^+\pi^-3\pi^0$, and $D^0 \rightarrow 2\pi^+2\pi^-2\pi^0$ are determined in this work; and the f_{CP+} values for $D^0 \rightarrow 4\pi^0$ and $D^0 \rightarrow 3\pi^0\eta$ are taken to be 1 based on theoretical expectations. The uncertainties are statistical only.

Decay	$M^{-}_{\rm measured}$	$M^+_{ m measured}$	f_{CP+}	f _{QC} (%)
$D^0 o \pi^+ \pi^- \pi^0$			0.973 ± 0.017 [34]	93.5 ± 0.5
$D^0 ightarrow \pi^+ \pi^- 2 \pi^0$	65.7 ± 11.1	169.8 ± 13.9	0.682 ± 0.077	97.4 ± 0.7
$D^0 \rightarrow 4\pi^0$			1	93.1 ± 0.5
$D^0 \rightarrow 3\pi^0 \eta$			1	93.1 ± 0.5
$D^0 \rightarrow 2\pi^+ 2\pi^- \pi^0$	37.8 ± 8.3	35.5 ± 6.6	0.438 ± 0.104	100.9 ± 0.9
$D^0 \rightarrow \pi^+ \pi^- 3 \pi^0$	$5.2^{+3.5}_{-2.8}$	$6.8^{+3.4}_{-2.7}$	$0.520^{+0.338}_{-0.269}$	$99.7^{+3.0}_{-2.4}$
$D^0 \rightarrow 2\pi^+ 2\pi^- 2\pi^0$	$3.5^{+2.8}_{-2.1}$	15.9 ± 3.7	$0.790^{+0.269}_{-0.255}$	95.9 ^{+2.2} -2.1

					D^0	\rightarrow				$D^+ \rightarrow$
Source	$\pi^+\pi^-\pi^0$	$\pi^+\pi^-2\pi^0$	$\pi^{+}\pi^{-}2$	$2\eta = 4\pi^0$	$3\pi^0\eta$	$2\pi^+ 2\pi^- \pi^0$	$2\pi^+2\pi^-\eta$	$\pi^+\pi^-3\pi^0$	$2\pi^+ 2\pi^- 2\pi$	0 $2\pi^{+}\pi^{-}$
$\overline{N_{\mathrm{tag}}}$	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
π^{\pm} tracking	0.4	0.4	0.7			0.8	1.0	0.4	0.8	0.6
π^{\pm} PID	0.4	0.4	0.4			0.8	0.8	0.4	0.8	0.6
π^0/η reconstruction	0.4	1.3	1.6	2.3	2.5	0.6	0.7	1.9	1.3	
2D fit	0.3	0.6	4.4	3.4	4.7	1.7	4.0	3.5	2.3	0.3
$\Delta E^{ m sig}$ cut	0.1	0.1	1.3	0.1	0.1	0.2	0.8	0.1	0.1	0.3
MC generator	0.6	1.5	0.2	3.4	2.8	1.1	1.5	5.3	1.4	0.8
K_S^0 rejection	0.1	0.4		7.4	3.5	3.2	8.1	4.7	1.6	0.5
Strong phase	0.5	0.7		0.5	0.5	0.9		3.0	2.2	
MC statistics	0.2	0.4	0.5	0.8	0.7	0.5	0.6	0.8	1.0	0.2
Daughter \mathcal{B}	0.03	0.07	1.02	0.14	0.52	0.03	0.51	0.10	0.07	
Total	1.2	2.4	5.1	9.2	7.0	4.2	9.4	8.7	4.3	1.4
	$D^+ ightarrow$									
Source	$\pi^+ 2\pi^0$	$2\pi^+\pi^-\pi^0$	$\pi^+ 3\pi^0$	$3\pi^{+}2\pi^{-}$	$2\pi^{+}\pi^{-}2\pi^{-}$	$2\pi^+\pi^-\pi^0$	$\eta \pi^+ 4\pi^0$	$\pi^+ 3 \pi^0 \eta$	$3\pi^+ 2\pi^- \pi^0$	$2\pi^+\pi^-3\pi^0$
N_{tag}	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
π^{\pm} tracking	0.2	0.6	0.2	1.1	0.6	0.8	0.2	0.2	1.2	0.6
π^{\pm} PID	0.2	0.6	0.2	1.0	0.6	0.6	0.2	0.2	1.0	0.6
π^0/η reconstruction	1.0	0.6	1.8		1.4	1.4	2.7	3.4	0.8	2.5
2D fit	0.3	0.6	1.7	2.1	1.8	2.3	3.1	3.4	2.8	2.7
$\Delta E^{ m sig}$ cut	0.1	0.1	0.1	0.2	0.1	0.5	0.1	0.1	0.4	0.1
MC generator	1.5	0.8	1.5	3.0	0.7	0.3	4.2	5.7	0.5	1.7
K_S^0 rejection		0.8	1.1	3.4	0.8		10.2		5.6	2.2

. . .

0.6

0.07

2.8

. . .

0.6

0.51

3.1

. . .

1.3

0.14

11.9

TABLE III. Systematic uncertainties (%) in the measurements of the BFs for various decay modes.

Ref. [35] and the necessary parameters quoted from Refs. [36–38] are summarized in Table II. After correcting the signal efficiencies by the individual factors, the residual uncertainties are assigned as systematic uncertainties.

. . .

0.3

0.03

1.8

0.3

0.07

1.9

. . .

0.6

3.2

0.10

. . .

0.4

. . .

5.3

Strong phase

MC statistics

Daughter \mathcal{B}

Total

The uncertainties of MC statistics for various signal decays, (0.2-1.3)%, are considered as a systematic uncertainty. The uncertainties of the daughter BFs of $\eta \rightarrow \gamma\gamma$ and $\pi^0 \rightarrow \gamma\gamma$ are 0.51% and 0.03%, respectively [13].

Adding all individual effects for each signal decay quadratically yields the total systematic uncertainties to be (1.2–11.9)% depending on the signal mode. Table III summarizes the systematic uncertainties for various sources.

VI. ASYMMETRIES OF CHARGE-SEPARATED BFS

For the six decay modes with the highest yields, the BFs of D and \overline{D} decays, \mathcal{B}_{sig}^+ and $\mathcal{B}_{\overline{sig}}^-$, are measured separately. Their asymmetry is determined by $\mathcal{A}_{CP}^{sig} = \frac{\mathcal{B}_{sig}^+ - \mathcal{B}_{\overline{sig}}^-}{\mathcal{B}_{sig}^+ + \mathcal{B}_{\overline{sig}}^-}$. The obtained BFs and asymmetries are summarized in Table IV. We find no statistically significant *CP* violation. Several systematic

uncertainties cancel in the asymmetry: the tracking and PID efficiencies of $\pi^+\pi^-$ pairs, the π^0 and η reconstruction, the daughter BFs, the K_S^0 rejection windows, the MC modeling, and the strong phase of D^0 decays. The other systematic uncertainties, e.g., the tracking and PID efficiencies of bachelor π^{\pm} for D^{\pm} decays, are estimated separately as above.

. . .

0.8

7.5

0.52

. . .

0.8

0.03

6.6

. . .

0.9

0.10

4.8

TABLE IV. Charge-separated BFs (\mathcal{B}_{sig}^+ and $\mathcal{B}_{\overline{sig}}^-$), and their asymmetries (\mathcal{A}_{CP}^{sig}). The first and second uncertainties are statistical and systematic, respectively, for \mathcal{A}_{CP}^{sig} ; while uncertainties for \mathcal{B}_{sig}^+ and $\mathcal{B}_{\overline{sig}}^-$ are only statistical.

Decay	$\mathcal{B}^+_{\mathrm{sig}}(imes 10^{-4})$	$\mathcal{B}_{\overline{sig}}^{-}(\times 10^{-4})$	$\mathcal{A}_{CP}^{\mathrm{sig}}$ (%)
$\pi^+\pi^-\pi^0$	134.8 ± 1.8	133.3 ± 1.8	$+0.6 \pm 0.9 \pm 0.4$
$\pi^+\pi^-2\pi^0$	97.6 ± 2.6	102.7 ± 2.7	$-2.5\pm1.9\pm0.7$
$2\pi^+\pi^-$	33.1 ± 1.0	32.3 ± 1.0	$+1.2 \pm 2.2 \pm 0.6$
$\pi^+ 2\pi^0$	48.3 ± 1.8	43.2 ± 1.7	$+5.6 \pm 2.7 \pm 0.5$
$2\pi^+\pi^-\pi^0$	116.7 ± 3.0	116.0 ± 3.0	$+0.3 \pm 1.8 \pm 0.8$
$2\pi^{+}\pi^{-}2\pi^{0}$	102.7 ± 5.6	111.6 ± 5.8	$-4.2 \pm 3.8 \pm 1.3$

VII. SUMMARY

To summarize, by analyzing 2.93 fb⁻¹ of e^+e^- annihilation data recorded at $\sqrt{s} = 3.773$ GeV with the BESIII detector, we present the first absolute measurements of the BFs of twenty Cabibbo-suppressed hadronic $D^{0(+)}$ decays involving multiple pions. For $D^0 \to \pi^+ \pi^- \pi^0$, $\pi^+ \pi^- 2\pi^0$, $2\pi^+2\pi^-\pi^0$, and $D^+ \to 2\pi^+\pi^-$, $\pi^+2\pi^0$, $2\pi^+\pi^-\pi^0$, $3\pi^+2\pi^-$, the BF precisions are improved by factors of 1.2-2.9 compared to the world average values based on relative measurements. For the other 13 decay modes, the BFs are measured for the first time. The reported BFs offer important input for reliable estimations of potential background sources in the precision measurements of B and Ddecays, especially to properly evaluate the tensions found in the LFU tests with semileptonic B decays. Amplitude analyses of these multibody decays with larger data samples available in the near future [39,40] will open an opportunity to precisely extract more quasi-two-body hadronic $D^{0(+)}$ decay rates, e.g., $D^+ \rightarrow \rho^+ \pi^0$. Detailed knowledge of these hadronic $D^{0(+)}$ decays is essential to deeply explore quark U-spin and SU(3)-flavor symmetry breaking effects and thereby improve the predictions of CP violation in the charm sector [2,41,42]. Additionally, the asymmetries of the charge-conjugated BFs of the six $D^{0(+)}$ decays with highest signal yields are determined. No statistically significant CP violation is observed.

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