Theory of Dirac dark matter: Higgs boson decays and EDMs

Pavel Fileviez Pérez¹,* and Alexis D. Plascencia²,†

¹Physics Department and Center for Education and Research in Cosmology and Astrophysics (CERCA), Case Western Reserve University, Cleveland, Ohio 44106, USA ²INFN, Laboratori Nazionali di Frascati, C.P. 13, 100044 Frascati, Italy

(Received 21 January 2022; accepted 2 May 2022; published 16 May 2022)

We discuss a simple theory predicting the existence of a Dirac dark matter candidate from gauge anomaly cancellation. In this theory, the spontaneous breaking of the local baryon number at the low scale can be understood. We show that the constraint from the dark matter relic abundance implies an upper bound on the theory of a few tens of TeV. We study the correlation between the dark matter constraints and the prediction for the electric dipole moment of the electron. We point out the implications for the diphoton decay width of the Standard Model Higgs boson. Furthermore, we study the decays of the new Higgs boson presented in the theory, and we show that the branching ratio into two photons can be large. We also discuss the correlation between the dark matter constraints and the properties of the new Higgs boson decays. This theory could be tested at current or future experiments by combining the results from dark matter, collider, and electric dipole moment experiments.

DOI: 10.1103/PhysRevD.105.095021

I. INTRODUCTION

The possible existence of dark matter (DM) in the Universe has motivated many studies in particle physics and cosmology in order to address this problem. Currently, there is a large number of experiments looking for dark matter signatures using different approaches. This experimental program could be successful; however, the nature of dark matter remains unknown. From a theoretical point of view, we should aim to understand theories that predict the existence of dark matter following some well-defined theoretical principles.

For many years the particle physics community supported the idea of having a cold dark matter candidate in the minimal supersymmetric Standard Model (MSSM); namely, the lightest neutralino. The MSSM could describe physics at the multi-TeV scale, but in order to have a dark matter candidate, we need to impose by hand the wellknown R-parity discrete symmetry, which could also be used to suppress dimension five contributions to the decay of the proton. Since this symmetry is imposed by hand, it cannot be said that the MSSM generically predicts a dark matter candidate. Unfortunately, we have a similar situation

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP³.

in other extensions of the Standard Model such as in theories with extra dimensions where the KK parity is also imposed to ensure the stability of the dark matter candidate.

Recently, we investigated simple theories [1,2] for physics beyond the Standard Model where the existence of dark matter is predicted from the cancellation of gauge anomalies. The main motivation to study these theories is the possibility to understand the spontaneous breaking of the baryon number in nature if this symmetry is a local gauge symmetry as the other gauge symmetries of the SM. The field content of these theories, determined by anomaly cancellation, is very simple and as an extra feature it predicts a cold dark matter candidate. In these theories, the stability of the dark matter candidate is a natural consequence of the spontaneous breaking of the local baryon number.

In this article we investigate the simple theory for Dirac dark matter proposed in Ref. [1]. This theory provides a theoretical framework to understand the spontaneous breaking of baryon number. In order to define an anomaly free theory the particle content is composed of six new fermionic representations, and the dark matter is the lightest new neutral fermionic field in the theory. For a detailed study of this theory, see the previous studies in Refs. [3–6]. We revisit the implications coming from the relic density and direct detection constraints, and find an upper bound on the theory around 30 TeV. Therefore, we can hope to test the theory at current or future experiments. We study the correlation between the dark matter constraints and the decays of the new Higgs boson present in the theory. We also show that the current bounds on the SM Higgs

pxf112@case.edu alexis.plascencia@lnf.infn.it

diphoton decay width provide a nontrivial bound on the particle spectrum.

Experimental searches for CP violation are some of the most sensitive to contributions from new physics. Namely, they are able to probe energy scales much higher than the electroweak scale whenever the CP-violating phase is large. Recently, the ACME collaboration has set a strong limit on the electron electric dipole moment (EDM) [7], $|d_e|/e \le 1.1 \times 10^{-29}$ cm, at the 90% confidence level and they expect to improve this measurement during stage III. For reviews on CP violation and EDMs we refer the reader to Refs. [8–11]. In this article, we study the implications of the electron EDM bound in this theory. Since there is a strong upper bound on the masses of all new fermions, the EDM bounds are very important. We also study the correlation between the dark matter constraints, Higgs bounds, and EDM experimental limits. For a study of EDMs in the context of local baryon number and Majorana dark matter see Ref. [12].

This article is organized as follows: In Sec. II we briefly review the theory of local baryon number predicting a Dirac dark matter candidate. In Sec. III we study the phenomenology of Dirac dark matter, focusing on the upper bound that comes from not overproducing the dark matter relic density and the perturbativity of the couplings. In Sec. IV we study how the new fermions modify the diphoton decay width of the SM Higgs boson. We also study the tree-level and loop-induced decays of the new baryonic Higgs boson. In Sec. V we present the study of *CP* violation and the implications for the EDM of the electron. Our main results are summarized in Sec. VI.

For completeness, we present different appendices with the details of the calculations performed in this work. Appendix A contains the complete Feynman rules of the theory, Appendix B has the diagonalization of the mass matrices, in Appendix C we present a discussion on the *CP*-violating phases, and in Appendix D we present the different contributions to the EDMs. In Appendix E we provide the full expressions for the tree-level and loop-induced decay widths of the baryonic Higgs boson and Appendix F has the loop functions involved in these decays and also in the Higgs diphoton decay.

II. SIMPLE THEORY FOR DIRAC DARK MATTER

The origin of baryon number violation in nature is unknown. The theory proposed in Ref. [1] provides a way to understand the spontaneous violation of baryon number in nature. This theory is based on the gauge symmetry

$$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)_B$$

where the extra Abelian symmetry, $U(1)_B$, corresponds to local baryon number. In order to study the spontaneous breaking of local baryon number we need to define an

TABLE I. Fermionic representations needed for gauge anomaly cancellation with $B_1 - B_2 = -3$ [1].

Fields	$SU(3)_C$	$SU(2)_L$	$U(1)_{\gamma}$	$U(1)_B$
$\Psi_L = \left(egin{array}{c} \Psi_L^0 \ \Psi_L^- \end{array} ight)$	1	2	$-\frac{1}{2}$	B_1
$\Psi_R = \left(egin{array}{c} \Psi_R^0 \ \Psi_R^- \end{array} ight)$	1	2	$-\frac{1}{2}$	B_2
η_R	1	1	-1	\boldsymbol{B}_1
η_L	1	1	-1	B_2
χ_R	1	1	0	B_1
χ_L	1	1	0	B_2

anomaly free theory. In Table I we list the extra fermionic content needed to cancel all the gauge anomalies. Notice that the extra fermions have baryon numbers B_1 or B_2 , but anomaly cancellation imposes the condition $B_1 - B_2 = -3$. The full Lagrangian of this theory can be written as

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{g_B}{3} (\bar{Q}_L \gamma^{\mu} Q_L + \bar{u}_R \gamma^{\mu} u_R + \bar{d}_R \gamma^{\mu} d_R) Z_{\mu}^B - \frac{1}{4} Z_{\mu\nu}^B Z^{B,\mu\nu} + \mathcal{L}_K^B + \mathcal{L}_Y^B - V(H, S_B),$$
 (2.1)

where \mathcal{L}_{SM} is the SM Lagrangian, Z_{μ}^{B} is the leptophobic gauge boson associated to U(1)_B and $Z_{\mu\nu}^{B} = \partial_{\mu}Z_{\nu}^{B} - \partial_{\nu}Z_{\mu}^{B}$. In the above equation $Q_{L} \sim (\mathbf{3},\mathbf{2},1/6,1/3), u_{R} \sim (\mathbf{3},\mathbf{1},2/3,1/3),$ and $d_{R} \sim (\mathbf{3},\mathbf{1},-1/3,1/3)$ are the multiplets for the Standard Model quarks. Here we are neglecting the kinetic mixing between the Abelian symmetries and assuming that $B_{1} \neq -B_{2}$ in order to avoid the case with Majorana dark matter that has been already studied in Ref. [13].

The new kinetic terms are given by

$$\mathcal{L}_{K}^{B} = i\bar{\Psi}_{L}\mathcal{D}\Psi_{L} + i\bar{\Psi}_{R}\mathcal{D}\Psi_{R} + i\bar{\eta}_{R}\mathcal{D}\eta_{R} + i\bar{\eta}_{L}\mathcal{D}\eta_{L} + i\bar{\chi}_{R}\mathcal{D}\chi_{R} + i\bar{\chi}_{L}\mathcal{D}\chi_{L} + (D_{\mu}S_{R})^{\dagger}(D^{\mu}S_{R}),$$
(2.2)

while the new Yukawa interactions can be written as

$$-\mathcal{L}_{Y}^{B} = y_{1}\bar{\Psi}_{L}H\eta_{R} + y_{2}\bar{\Psi}_{R}H\eta_{L} + y_{3}\bar{\Psi}_{L}\tilde{H}\chi_{R} + y_{4}\bar{\Psi}_{R}\tilde{H}\chi_{L} + y_{\Psi}\bar{\Psi}_{L}\Psi_{R}S_{B}^{*} + y_{\eta}\bar{\eta}_{R}\eta_{L}S_{B}^{*} + y_{\chi}\bar{\chi}_{R}\chi_{L}S_{B}^{*} + \text{H.c.},$$
(2.3)

where $H \sim (\mathbf{1}, \mathbf{2}, 1/2, 0)$ is the Standard Model Higgs boson, and $\tilde{H} = i\sigma_2 H^*$. The scalar $S_B \sim (\mathbf{1}, \mathbf{1}, 0, 3)$ is responsible for the spontaneous breaking of baryon number. We define the following mass parameters,

$$\mu_{\Psi} = \frac{y_{\Psi}}{\sqrt{2}} v_B, \qquad \mu_{\eta} = \frac{y_{\eta}}{\sqrt{2}} v_B, \qquad \mu_{\chi} = \frac{y_{\chi}}{\sqrt{2}} v_B, \qquad (2.4)$$

and in Appendix B we discuss the diagonalization of the mass matrices to obtain the physical states. These

interactions can generate large masses (above the electroweak scale) for the new fermions. This happens after S_B acquires a nonzero vacuum expectation value (VEV) and spontaneously breaks the $\mathrm{U}(1)_B$ symmetry. From Eq. (2.3) we see that S_B must carry the baryon number equal to 3. Therefore, local baryon number must be broken in three units and the theory predicts the proton to be stable. Since the proton is stable in this theory, it can describe physics at the low scale in agreement with experimental constraints.

The full scalar potential is given by

$$V = -\mu_H^2 H^{\dagger} H + \lambda_H (H^{\dagger} H)^2 - \mu_B^2 S_B^{\dagger} S_B + \lambda_B (S_B^{\dagger} S_B)^2 + \lambda_{HB} (H^{\dagger} H) (S_B^{\dagger} S_B).$$
 (2.5)

The Higgs fields can be written as

$$H = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v_0 + h_0 + iG_0) \end{pmatrix}$$
, and $S_B = \frac{1}{\sqrt{2}}(v_B + s_B + iG_B)$, (2.6)

with the physical Higgs bosons defined as follows:

$$h = h_0 \cos \theta_B - s_B \sin \theta_B,$$

$$h_B = s_B \cos \theta_B + h_0 \sin \theta_B,$$
(2.7)

where θ_B corresponds to the mixing angle that diagonalizes the mass matrix for the Higgs bosons, and it is given by

$$\tan 2\theta_B = \frac{v_0 v_B \lambda_{HB}}{v_R^2 \lambda_B - v_0^2 \lambda_H},\tag{2.8}$$

where v_0 and v_B correspond to the VEVs of H and S_B , respectively. It is important to mention that this simple theory predicts only few extra physical fields:

- (i) Two neutral Dirac fermions, χ_i^0 , with i = 1, 2.
- (ii) Two electrically charged fermions χ_i^{\pm} with j = 1, 2.
- (iii) A new Higgs boson, h_B , called baryonic Higgs boson.
- (iv) The spin one gauge boson, Z_B , associated to $U(1)_B$. After symmetry breaking there is an anomaly free global symmetry in the new sector:

$$\begin{split} \chi_L &\to e^{i\theta} \chi_L, & \chi_R \to e^{i\theta} \chi_R, & \Psi_L \to e^{i\theta} \Psi_L, \\ \Psi_R &\to e^{i\theta} \Psi_R, & \eta_L \to e^{i\theta} \eta_L, & \eta_R \to e^{i\theta} \eta_R, \end{split} \tag{2.9}$$

this is a remnant from the local baryon symmetry. Therefore, the lightest new field in this sector is stable. The stable field in this sector should be neutral to avoid issues with cosmology and then we have a candidate to describe the cold dark matter in the Universe. It is possible to consider two different scenarios for the lightest field: (i) χ_1^0 is Ψ -like, (ii) χ_1^0 is χ -like. The first scenario is ruled out by direct detection experiments because Ψ^0 is a SU(2)_L

doublet and the cross section is several orders of magnitude above the experimental limit [6]. We focus on the second scenario, which is consistent with all the experimental limits, as we will discuss below.

III. DIRAC DARK MATTER

This theory predicts generically a Dirac dark matter candidate that is χ -like. Here $\chi = \chi_L + \chi_R$ is the DM candidate and the relevant interactions are given by

$$\mathcal{L} \supset \frac{1}{3} g_B \bar{q} \gamma^\mu q Z_\mu^B - g_B \bar{\chi} \gamma^\mu (B_2 P_L + B_1 P_R) \chi Z_\mu^B$$
$$- M_\chi \bar{\chi} \chi + \frac{M_\chi \cos \theta_B}{v_B} \bar{\chi} \chi h_B - \frac{M_\chi \sin \theta_B}{v_B} \bar{\chi} \chi h, \qquad (3.1)$$

where $M_{\gamma} = y_{\gamma} v_B / \sqrt{2}$ and $P_{L(R)} = (1 \mp \gamma_5)/2$.

In order to study the relic density constraints we need to consider all possible annihilation channels:

$$\bar{\gamma}\gamma \rightarrow \bar{q}q, Z_RZ_R, hZ_R, h_RZ_R, hh, hh_R, h_Rh_R, WW, ZZ.$$

The constraints from DM direct detection are very important to understand the allowed parameter space in this theory. The elastic nucleon- χ cross section has two main contributions mediated by the Z_B gauge boson and the Higgs boson.

In Fig. 1 we present our results for the calculation of the dark matter relic density which has been computed numerically using MicrOMEGAs5.0.6 [14]. The solid blue line reproduces the measured value of $\Omega_{\rm DM} h^2 = 0.12$ [15] while the region shaded in blue overproduces the dark matter relic abundance. In the upper panel we fixed the gauge coupling to its largest value allowed by perturbativity $g_B = \sqrt{2\pi}/3$. The red line corresponds to the maximal value for the Yukawa coupling allowed by perturbativity: namely, $y_{\gamma} = 2\sqrt{2\pi}$. We find that the results for the relic density are almost independent of the scalar mixing angle; for the plots we set $\theta_B = 0$. The peak that can be observed in the plots corresponds to the resonance $M_{\chi} \simeq M_{Z_R}/2$ so that $\chi \bar{\chi} \to q \bar{q}$ is the dominant annihilation channel. The bump in the lower part of the plot also corresponds to a resonance $M_{\chi} \simeq M_{h_B}/2$. In the entire region above the TeV scale the dominant annihilation channel is $\chi \bar{\chi} \to Z_B h_B$ and this does not require being close to any resonance; therefore it is the generic DM annihilation channel.

In contrast to the case with Majorana dark matter studied in Ref. [13], in this scenario the direct detection cross section does not have velocity suppression, and hence, these bounds are much stronger. In Fig. 1 we show with a solid green line what is excluded by Xenon-1T [18] while the solid black line shows the projected sensitivity for Xenon-nT [19]. This is discussed in more detail in Ref. [6] where a study of the Dirac dark matter phenomenology was performed. As it was shown in that work, the experimental

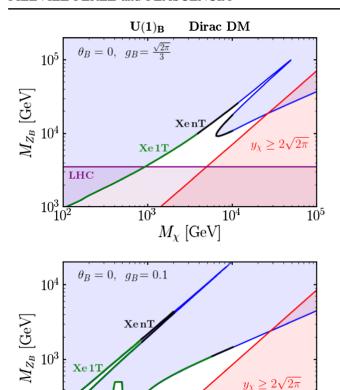


FIG. 1. Dark matter relic density in the M_{Z_B} vs M_χ plane. The solid blue line reproduces the measured value of $\Omega_{\rm DM}h^2=0.12$ [15] while the region shaded in light blue overproduces the DM relic density. The region shaded in purple is excluded by dijet resonance searches at the LHC [16,17]. The region shaded in red is excluded by the perturbativity of the Yukawa coupling y_χ . The solid green line is excluded by Xenon-1T [18] while the solid black line shows the projected sensitivity for Xenon-nT [19]. The upper panel corresponds to the maximal coupling $g_B = \sqrt{2\pi}/3$, while the lower panel is for $g_B = 0.1$. In both panels we fixed $M_{h_B} = 1$ TeV, $\theta_B = 0$ and the baryonic charge to $B_1 = -1/2$, which implies $B_2 = 5/2$.

 M_{χ} [GeV]

 10^{3}

 10^{4}

 10^{5}

bound from Xenon-1T rules out multi-TeV dark matter masses even in the case of zero mixing with the SM Higgs bosons. Furthermore, the projected sensitivity for Xenon-nT will be able to probe a large region in the parameter space.

The region shaded in purple in Fig. 1 shows the parameter space excluded by dijet resonance searches at the LHC [16,17]. In the lower panel of that figure we show the results for $g_B = 0.1$, in this scenario the gauge boson can evade the constraints from the dijet searches. However, the experimental constraint from direct detection requires $M_{\gamma} \gtrsim 850$ GeV if the dark matter density is saturated.

The upper panel in Fig. 1 also shows that there is an upper bound on the masses of the gauge boson and the dark

matter in order to not overclose the Universe. In summary, we obtain $M_{Z_B} \lesssim 100$ TeV and $M_\chi \lesssim 50$ TeV as upper bounds for the masses of the gauge boson and the dark matter, respectively. This bound is stronger than the one coming from the unitarity of the S matrix which is around 200 TeV [6]. Furthermore, ignoring the resonant region, which requires $M_\chi \approx M_{Z_B}/2$, the upper bounds become $M_{Z_B} \lesssim 19$ TeV and $M_\chi \lesssim 26$ TeV, which are more generic.

Furthermore, since all the new fermions acquire their mass from the U(1)_B breaking scale, there is a nondecoupling effect within the new sector, and the upper bound also applies to the charged fields that contribute to the EDMs. Namely, in the limit of small fermionic mixing we have that $M_{\chi_1^{\pm}} \simeq y_{\eta} v_B / \sqrt{2} = y_{\eta} M_{Z_B} / (3\sqrt{2}g_B)$ and $M_{\chi_2^{\pm}} \simeq y_{\Psi} v_B / \sqrt{2}$, and hence, setting the Yukawa couplings to their allowed values by perturbativity $y_{\Psi}, y_{\eta} \leq 2\sqrt{2\pi}$, we find that

$$M_{\chi^{\pm}_{+}} \lesssim 140 \text{ TeV } (30 \text{ TeV}),$$
 (3.2)

where the number in the parentheses is more generic since it does not require the theory to live in a resonance. This is a striking result that implies that we can hope to fully test this theory at current or future collider experiments.¹

IV. HIGGS BOSON DECAYS

In 2012 both the ATLAS and CMS announced the discovery of a scalar particle with properties similar to the SM Higgs boson with a mass of 125 GeV. The presence of new physics coupled to this particle motivates a detailed experimental study of its properties. The diphoton decay of the Higgs boson represents one of its cleanest signatures and its measurement is expected to be improved by the high luminosity run of the LHC. In this section, we study how the new charged fermions could modify this branching ratio. Furthermore, the theory also predicts a second Higgs boson that mixes with the SM Higgs boson, with mixing angle θ_B , and we study its decays channels in detail including the loop-induced decays with the anomaly canceling fermions running in the loop.

A. SM Higgs boson diphoton decay

The presence of new physics coupled to the SM Higgs boson can modify some of its properties. In this theory, the new charged fermions introduced to cancel the gauge anomalies give new contributions to the Higgs boson decay into two photons. In Fig. 2 we present the Feynman diagrams that contribute to the $h \to \gamma \gamma$ decay. The signal strength for this channel normalized with respect to the SM prediction has been measured by the ATLAS collaboration

¹This upper bound is obtained from the largest value of g_B allowed by perturbativity. However, due to the positive β function for g_B , such a large value will quickly run into a Landau pole, and, hence, we expect the theory to live at a much lower scale.

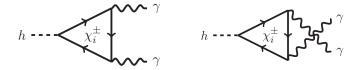


FIG. 2. Feynman diagrams for the contribution of the new fermions to the $h \rightarrow \gamma \gamma$ decay.

to be $\mu_{\gamma\gamma}=1.16\pm0.14$ [20], while the CMS collaboration reports $\mu_{\gamma\gamma}=1.12\pm0.09$ [21]. The high luminosity run at the LHC is expected to improve the measurement of this rate by a factor of 2 [22], and a possible deviation from the SM prediction could be observed.

There are different extensions of the SM that lead to a modification of the Higgs diphoton rate, for studies from an EFT perspective see, e.g., Refs. [23–27]. For phenomenological studies of models with new vectorlike fermions that have Yukawa interactions with the SM Higgs boson see, e.g., Refs. [28–31]. In this theory, the Higgs diphoton decay width is given by

$$\Gamma(h \to \gamma \gamma) = \frac{\alpha^2}{64\pi^3 M_h^5} \left| \sum_{i=1}^2 M_{\chi_i^{\pm}} \text{Re}[C_{hc}^{ii}] F_{\chi_i^{\pm}} + \frac{\cos \theta_B}{v_0} \left(\sum_{f^{+}} N_c^f Q_f^2 m_{f^{+}}^2 F_{f^{+}} - F_W \right) \right|^2 + \frac{\alpha^2}{64\pi^3 M_h} \left| \sum_{i=1}^2 M_{\chi_i^{\pm}} \text{Im}[C_{hc}^{ii}] G_{\chi_i^{\pm}} \right|^2, \tag{4.1}$$

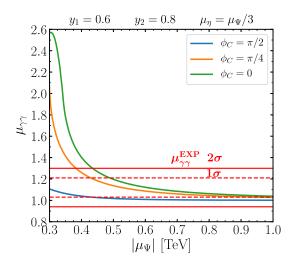
where the sum over f^+ is over the SM fermions, v_0 corresponds to the VEV of the SM Higgs boson and the loop functions are given in Appendix F. The CP-even part of the new Yukawa interactions (real part) interfere with the SM contribution, and, hence, the rate for $h \to \gamma \gamma$ can be

enhanced or suppressed depending on the sign of the new couplings [28]. The *CP*-odd part of the new interactions (imaginary part) does not interfere with the SM contribution and always enhances this rate; however, it only gives a small contribution. Consequently, this observable will give stronger constraints for small *CP*-violating phases and will be complementary to the bounds from EDMs.

As we discuss in Appendix C the theory contains two independent *CP*-violating phases: $\phi_C = \arg(y_\eta y_\Psi^* y_1 y_2^*)$ in the charged sector and $\phi_N = \arg(y_\chi y_\Psi^* y_3 y_4^*)$ in the neutral sector. In order to make predictions we need to fix some of the parameters, throughout this article we fix the Yukawa couplings y_i to different $\mathcal{O}(1)$ values in order to show different slices of the parameter space. We also require the charged fermion masses to satisfy the lower bound from LEP of 90 GeV [32].

In Fig. 3 we show our results for the Higgs diphoton signal strength $\mu_{\gamma\gamma} \equiv \sigma^{\rm prod} {\rm Br}(h \to \gamma\gamma)/(\sigma_{\rm SM}^{\rm prod} {\rm Br}(h \to \gamma\gamma)_{\rm SM})$ as a function of the mass parameter $|\mu_{\Psi}|$. The region within the solid (dashed) red lines shows the measurement by the CMS collaboration within 2σ (1σ). On the left panel we fix the parameters to $y_1=0.6,\ y_2=0.8,\ {\rm and}\ \mu_{\eta}=\mu_{\Psi}/3$. The green line corresponds to $\phi_C=0$ and using the 2σ range for $\mu_{\gamma\gamma}^{\rm EXP}$ we find that $|\mu_{\Psi}|<0.43$ TeV is excluded. The orange line corresponds to $\phi_C=\pi/4$ for which $|\mu_{\Psi}|<0.38$ TeV is excluded. Finally, the blue line is for $\phi_C=\pi/2$ for which we find that the measurement of $\mu_{\gamma\gamma}$ provides no constraint

On the right panel in Fig. 3 we fix $y_1 = 0.6$ and $y_2 = -0.8$ from which it is possible to obtain a destructive interference and lower the prediction for $\mu_{\gamma\gamma}$. The green line corresponds to $\phi_C = 0$ and using the 2σ range for $\mu_{\gamma\gamma}^{\rm EXP}$ we find that $|\mu_{\Psi}| < 0.74$ TeV is excluded. The orange line corresponds to $\phi_C = \pi/4$ for which $|\mu_{\Psi}| < 0.6$ TeV is



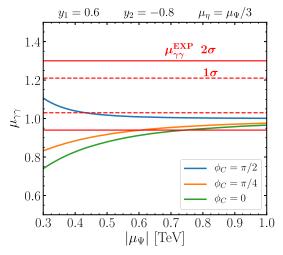


FIG. 3. Diphoton signal strength of the SM Higgs boson $\mu_{\gamma\gamma}$ as a function of the mass parameter $|\mu_{\Psi}|$ in units of TeV. The region within the solid (dashed) red lines shows the measurement by the CMS collaboration within 2σ (1σ) [21]. The green, orange, and blue solid lines correspond to different values for the *CP*-violating phase $\phi_C = 0$, $\phi_C = \pi/4$, and $\phi_C = \pi/2$, respectively.

excluded. Finally, the blue line is for $\phi_C = \pi/2$ for which we find again that the measurement of $\mu_{\gamma\gamma}$ provides no constraint.

We note that even though the addition of large Yukawa couplings with the Higgs boson could push the electroweak vacuum to the instability region at a high scale, this can be easily addressed by the positive contribution from the Higgs portal coupling λ_{HB} between the Higgs boson and the scalar responsible for the breaking of baryon number. Regarding the CP-violating phase in the neutral sector, ϕ_N , this parameter does not enter at one-loop in the calculation of $h \to \gamma \gamma$, and hence, it is not constrained by this observable.

The Yukawa couplings y_1 and y_2 will induce a mass splitting among the components of the $SU(2)_L$ doublet Ψ , and, hence, there will be a contribution to the electroweak precision observables S, T, and U. This was studied for a similar scenario in Ref. [33]. Nevertheless, there exists freedom in the couplings y_3 and y_4 that also contribute to the mass splitting and those bounds can be easily satisfied. Furthermore, if the dark matter relic density is saturated, the bound from direct detection requires the dark matter mass to be above 850 GeV, and hence, the new charged fermions will be above this value so the contribution to those parameters is further suppressed.

B. Baryonic Higgs boson decays

In this section, we study the phenomenology of the scalar responsible for the spontaneous breaking of $\mathrm{U}(1)_B$. As we have discussed in Sec. III the strong constraints from DM direct detection experiments require the new gauge boson and the dark matter to be above the TeV scale. Therefore, if the baryonic Higgs boson has a mass around the electroweak scale it will decay dominantly into SM gauge bosons. In this section we neglect the effect of CP violation.

From the Yukawa interactions in Eq. (2.3) it can be seen that the anomaly canceling fermions running in the loop will induce decays of h_B into SM gauge bosons including $\gamma\gamma$. We computed these decay widths with the help of Package-X [34] and present the full expressions in Appendix E. Of particular interest is the clean diphoton channel that, as we will show, can have a branching ratio much larger than the one for the SM Higgs boson.

In Fig. 4 we show our results for the branching ratio of h_B as a function of the scalar mixing angle θ_B . As we have discussed in Sec. III the most generic case is for $\chi\bar{\chi}\to Z_Bh_B$ to be the dominant DM annihilation channel. Consequently, we fix the parameters to be in this regime and reproduce the measured relic abundance of $\Omega_{\rm DM}h^2=0.12$. The experimental bound from Xenon-1T is shaded in red and constrains the mixing angle to be $\theta_B\lesssim 0.009$, while the projected sensitivity for Xenon-nT will be able to probe the Z_B mediated cross section and, hence, will be sensitive to a vanishing scalar mixing angle. For the whole range of mixing angles the branching ratio for the decay into a pair

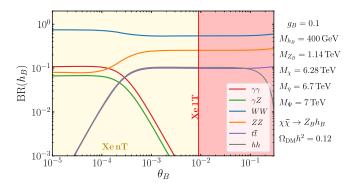


FIG. 4. Branching ratios of the baryonic Higgs boson h_B as a function of the scalar mixing angle θ_B . The relevant parameters have been fixed to reproduce the dark matter relic density $\Omega_{\rm DM}h^2=0.12$ as indicated in the plot, the dominant DM annihilation channel is $\chi\bar\chi\to Z_Bh_B$. The different colors correspond to different decay channels as shown in the plot. The area shaded in red is ruled out by Xenon-1T direct detection constraints, while in yellow we show the region that will be probed by Xenon-nT.

of Z bosons is large, and, hence, the decay channel $h_B \to ZZ \to 4\ell$ can be used to search for this new scalar. Moreover, for small values of the mixing angle $\theta_B \le 10^{-4}$ the branching ratio for the loop-induced decay $h_B \to \gamma\gamma$ can be as large as 10%. Finally, since we fix $M_{h_B} = 400$ GeV for large values of the mixing angle there is a large branching ratio into a top antitop quark pair.

In Fig. 5 we present our results for a scenario in which the dominant contribution to the relic density comes from the annihilation channel $\chi \bar{\chi} \to q \bar{q}$, which needs to be very close to the resonance $M_{\chi} \approx M_{Z_B}/2$ to reproduce the measured value of the relic abundance. In this scenario there is no constraint from Xenon-1T; nonetheless, the projected sensitivity for Xenon-nT will be able to put the

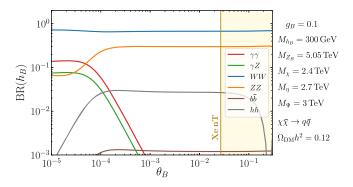


FIG. 5. Branching ratios of the baryonic Higgs boson h_B as a function of the scalar mixing angle θ_B . The relevant parameters have been fixed to reproduce the dark matter relic density $\Omega_{\rm DM}h^2=0.12$ as indicated in the plot, the dominant DM annihilation channel is $\chi\bar{\chi}\to q\bar{q}$. The different colors correspond to different decay channels as shown in the plot. The area shaded in yellow shows the projected sensitivity for Xenon-nT.

constrain of $\theta_B \lesssim 0.027$ on the mixing angle. As can be seen, the dominant decays are $h_B \to W^+W^-$ and $h_B \to ZZ$. Furthermore, for very small values of the mixing angle $\theta_B \leq 10^{-4}$ then the branching ratio $h_B \to \gamma\gamma$ can be as large as 13%.

There are two main channels for the production of h_R at the LHC. On the one hand we have the associated production $pp \to Z_B^* \to Z_B h_B$, which was studied recently in Ref. [35]. Even if the constraints from DM direct detection require that the mass of the Z_B has to be above the TeV, the production cross section for $M_{h_{\rm B}}=400~{\rm GeV}$ and $M_{Z_R} = 1.1 \text{ TeV}$ corresponds to $\sigma(pp \to Z_B h_B) \approx$ 10^{-2} fb for a center-of-mass energy of 14 TeV, and hence, $\mathcal{O}(10)$ events can be generated in the high luminosity run at the LHC. On the other hand, there is production via gluon fusion which is suppressed by the mixing angle $\sin^2 \theta_B$; however, the branching ratio for $h_B \rightarrow \gamma \gamma$ can be 10^2 times larger than the one for the SM Higgs boson. Consequently, for h_B with a mass of 400 GeV and $\theta_B \approx 10^{-2}$ there will be $\mathcal{O}(1)$ events generated in the high luminosity run at the LHC.

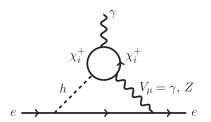
V. CP VIOLATION AND EDMs

This theory predicts new fermions needed for anomaly cancellation and their interactions can provide new sources of CP violation. In this section we study the new sources of CP violation and calculate the predictions for the electric dipole moment of the electron. These also induce an electric dipole moment for the neutron; however, the experimental bound is much weaker than the one for the electron. In general, all the Yukawa couplings in Eq. (2.3) can be complex, and as we discuss in Appendix C this leads to two independent CP-violating phases: $\phi_C = \arg(y_n y_{\Psi}^* y_1 y_2^*)$ in the charged sector and $\phi_N = \arg(y_y y_{\Psi}^* y_3 y_4^*)$ in the neutral sector. These *CP*violating phases contribute to the electric dipole moments of SM fermions via two-loop Barr-Zee diagrams shown in Fig. 6. The contributions with $h\gamma$, hZ, and hZ_B in the loop depend only on ϕ_C ; while both CP-violating phases contribute in the case with W^-W^+ in the loop. In Appendix D we provide the expressions for the different contributions to the EDM.

In Fig. 7 we present our results for the electron EDM as a function of the mass parameter μ_{Ψ} . The different contributions are shown by dashed lines of different colors. The largest contribution comes from the γh diagram, but the WW contribution can be of similar order and even larger in some regions of the parameter space. The Zh is small due to the cancellation in the overall term $(T_3^e/2 - s_W^2Q_e)$, as has been noted previously in the literature for other scenarios [36]. In the left panel we fix $\phi_C = \pi/2$ and $\phi_N = 0$ and the relevant Yukawa interactions to $|y_2| = 2|y_1| = 0.2$; the region excluded by the ACME collaboration, $|d_e|/e \le$ 1.1×10^{-29} cm [7], corresponds to the region shaded in gray and for this scenario we obtain the exclusion of $|\mu_{\Psi}| \lesssim 2.7$ TeV. The gray dashed line corresponds to the projected sensitivity for ACME III of $|d_e|/e \le 3 \times$ 10^{-31} cm [37] and for this scenario it will reach $|\mu_{\Psi}| \lesssim$ 21 TeV. The region shaded in green is excluded due to overproducing the dark matter relic abundance $\Omega_{\rm DM} h^2 > 0.12.$

In the right panel of Fig. 7 we set $\phi_C = 0$ and $\phi_N = \pi/2$, which implies that the dominant contribution is from WW in the loop and that is why we can see that the dashed and the solid line overlap. The relevant Yukawa couplings are fixed to $|y_4| = 2|y_2| = 0.2$; for this scenario we obtain the exclusion of $|\mu_\Psi| \lesssim 0.9$ TeV while ACME III will be able to reach $|\mu_\Psi| \lesssim 7$ TeV. In both panels we fix $\mu_\eta = \mu_\Psi/3$ and we find that the results are almost independent of μ_χ since the χ fermion is a SM singlet and only gives a small contribution through fermionic mixing. We note that in the limit in which either one of the relevant couplings $y_i \to 0$ then the EDM will also vanish.

These results are relevant for the baryogenesis scenarios proposed in Refs. [38,39] where it was argued that EDMs only appear at four loops. We demonstrated that the effects from the anomaly canceling charged fermions cannot be neglected and that EDMs already appear at two-loops. Nonetheless, our conclusions hold for the minimal scenario and could change in a nonminimal scenario with more scalars charged under $U(1)_B$ that acquire a nonzero VEV. As an alternative solution to the baryon asymmetry of the Universe, Ref. [40] recently studied the implementation of high-scale leptogenesis in theories with local lepton and baryon number. As a side note, we comment on the EDM of the muon which even though it receives and enhancement



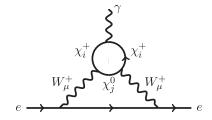


FIG. 6. Feynman graphs for the Barr-Zee contribution to the electric dipole moment of the electron. V_{μ} can either be the photon or the Z boson. Here χ_i^+ and χ_j^0 correspond to the anomaly canceling fermions.

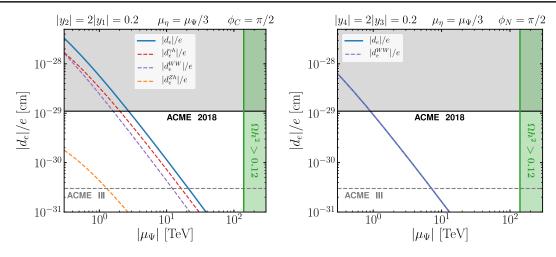


FIG. 7. Left panel: the solid blue line shows the electron EDM as a function of the mass parameter μ_{Ψ} . The dashed red, purple, and orange lines show the different contributions d_e^{rh} , d_e^{WW} , and d_e^{Zh} , respectively. The region shaded in gray corresponds to the experimental bound from the ACME Collaboration [7] and the gray dashed line gives the projected sensitivity for ACME III [37]. The region shaded in green is excluded due to overproducing the dark matter relic abundance $\Omega_{\rm DM}h^2 > 0.12$. The CP-violating phases are set to $\phi_C = \pi/2$ and $\phi_N = 0$ and the other parameters have been fixed as shown in the title of the plot. Right panel: same as left panel but with the CP-violating phases set to $\phi_C = 0$ and $\phi_N = \pi/2$.

of (m_{μ}/m_e) compared to the electron, the experimental sensitivity is much weaker than in the case of the electron. The current bound from Brookhaven Muon (g-2) experiment is $|d_{\mu}| < 1.5 \times 10^{-19} \ e \ cm$ [41], which lies more than six orders of magnitude below our predictions.

In Fig. 8 we present our results for the parameter space allowed by the ACME bound and the measurement of $\mu_{\gamma\gamma}$. The region excluded by the measurement of the Higgs diphoton channel is shown in red. The gray dashed line is the bound from DM direct detection that requires $M_{\gamma} \gtrsim 850 \text{ GeV}$; nevertheless, this bound applies when the relic density is saturated. The region excluded by ACME is shown in orange. In the case that $\phi_C = \pi/2$ then this bound already excludes $|\mu_{\Psi}| \lesssim 16$ TeV. This bound also has consequences for the low-mass regime. Assuming these values for the Yukawas, i.e., $|y_1| = 0.6$, $|y_2| = 0.8$, and a maximal *CP*-violating phase, then we can find an indirect bound on the symmetry breaking scale by requiring perturbativity of y_{Ψ} and y_n ; namely, the bound translates into $M_{Z_B}/g_B \gtrsim 13.5$ TeV, so for example for a light boson of $M_{Z_R} = 1$ GeV the coupling needs to be $g_B \lesssim 10^{-4}$. The blue dashed line corresponds to the projected sensitivity for ACME III and shows that for a maximal CP violation it is expected to reach $|\mu_{\Psi}| \lesssim$ 115 TeV. The region shaded in green overproduces the dark matter relic density. Consequently, the allowed parameter space is constrained from above and below.

This result shows a complementarity between the electron EDM and the Higgs diphoton decay. The region with vanishing CP violation can be probed by measuring a deviation in the Higgs diphoton decay. For the parameters shown in Fig. 8 the current measurement of $\mu_{\gamma\gamma}$ within 2σ

excludes $|\mu_{\Psi}| \lesssim 0.37$ TeV. We also find that the projected sensitivity of ACME III will probe a *CP*-violating phase as small as $\phi_C \approx 10^{-4}$ for charged fermions below the TeV scale.

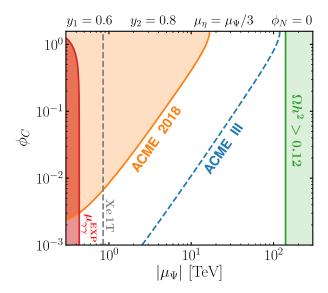


FIG. 8. Allowed parameter space in the ϕ_C vs $|\mu_\Psi|$ plane. The region shaded in orange corresponds to the experimental bound from the ACME collaboration [7] and the blue dashed line gives the projected sensitivity for ACME III [37]. The region shaded in red is excluded by the measurement of the Higgs diphoton signal strength $\mu_{\gamma\gamma}$ at the LHC. The gray dashed line gives the bound from DM direct detection, which applies when the dark matter relic density is saturated. The region shaded in green is excluded since it overproduces the dark matter relic abundance $\Omega_{\rm DM}h^2>0.12$. We set $\phi_N=0$ and the other parameters have been fixed as shown in the title of the plot.

VI. SUMMARY

We studied a simple theory based on local baryon number $\mathrm{U}(1)_B$ that predicts a dark matter candidate from the cancellation of gauge anomalies. We found that the constraint on the DM relic density gives an upper bound on the full theory. This gauge theory contains new sources of CP violation and can give a large electric dipole moment for the electron. Also, since the new charged fermions cannot be decoupled from the baryonic Higgs boson; the theory predicts a large branching ratio for the latter into SM gauge bosons.

Generically, dark matter is predicted to be a Dirac fermion. We studied the dark matter phenomenology and found that the currents bounds from direct detection already require the dark matter mass to be above the TeV scale. We showed that not overproducing the relic density sets a generic upper bound on the masses of the gauge boson and the dark matter, $M_{Z_B} \lesssim 19$ TeV and $M_\chi \lesssim 26$ TeV, respectively. Moreover, since all the new fermions acquire their masses from the new symmetry breaking scale this implies an upper bound on the charged fermions responsible for the EDMs; namely, $M_{\chi^\pm} \lesssim 30$ TeV.

We calculated the contribution from the new fermions running in the loop for the decay of the SM Higgs boson into two photons and found the constraint on the parameter space from the current measurement of the Higgs signal strength $\mu_{\gamma\gamma}$ at the LHC. We also studied the decays for the new Higgs boson in the theory responsible for the spontaneous breaking of the U(1)_B. We found that the loop-induced decay $h_B \rightarrow \gamma\gamma$ can have a large branching ratio

around 10% and that the process $pp \to Z_B^* \to Z_B h_B$ could be observed in the high luminosity run at the LHC.

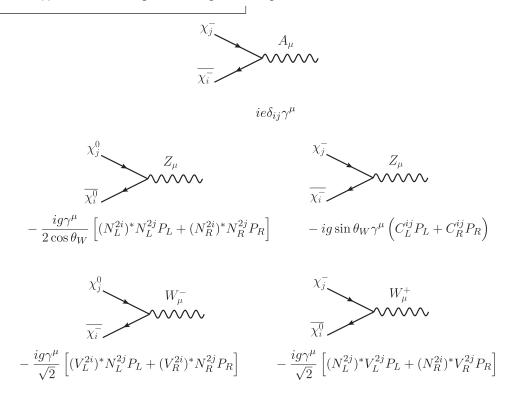
Furthermore, we showed that the theory contains two new CP-violating phases that cannot be removed by field rotations. We computed the Barr-Zee contributions to the EDM of the electron and found that the current bound by ACME already excludes $\mu_{\Psi} \lesssim 16 \text{ TeV}$ for maximal *CP* violation. Furthermore, the projected sensitivity for ACME III will be able to probe a large region in the parameter space of the theory; namely, for maximal CP violation it could reach $\mu_{\Psi} \lesssim 115$ TeV. Consequently, the theory is being constrained from above by the measured dark matter relic abundance and from below by the lack of experimental evidence for an electron EDM. Finally, we demonstrated there is a complementarity between measurements of the Higgs diphoton decay and the electron EDM. Namely, the bound from the Higgs diphoton decay is the dominant constraint for small CP-violating phases. This theory could be tested at current or future experiments by combining the results from dark matter, collider, and EDM experiments.

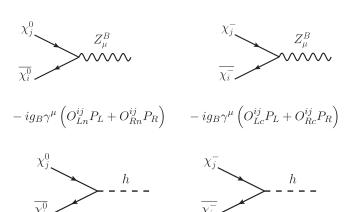
ACKNOWLEDGMENTS

A. D. P. is supported in part by the INFN "Iniziativa Specifica" Theoretical Astroparticle Physics (TAsP-LNF).

APPENDIX A: FEYNMAN RULES

In this appendix we list all the Feynman rules for the new particles:





$$\begin{array}{cccc}
\chi_{j}^{0} & & \chi_{j}^{-} & \\
& & \chi_{i}^{0} & & \\
& & & \chi_{i}^{-} & & \\
-i \left[C_{Bn}^{ij} P_{L} + (C_{Bn}^{ij})^{*} P_{R} \right] & & -i \left[C_{Bc}^{ij} P_{L} + (C_{Bc}^{ij})^{*} P_{R} \right]
\end{array}$$

 $-i\left[C_{hc}^{ij}P_L+(C_{hc}^{ij})^*P_R\right]$

where

 $-i\left[C_{hn}^{ij}P_L+(C_{hn}^{ij})^*P_R\right]$

$$C_L^{ij} = \tan \theta_W (V_L^{1i})^* V_L^{1j} - \frac{1}{\tan 2\theta_W} (V_L^{2i})^* V_L^{2j}, \qquad (A1)$$

$$C_R^{ij} = \tan \theta_W (V_R^{1i})^* V_R^{1j} - \frac{1}{\tan 2\theta_W} (V_R^{2i})^* V_R^{2j}, \qquad (A2)$$

$$\begin{split} C_{hn}^{ij} &= \frac{1}{\sqrt{2}} \cos \theta_B [y_3^* (N_R^{1i})^* N_L^{2j} + y_4 (N_R^{2i})^* N_L^{1j}] \\ &- \frac{1}{\sqrt{2}} \sin \theta_B [y_\Psi^* (N_R^{2i})^* N_L^{2j} + y_\chi (N_R^{1i})^* N_L^{1j}], \end{split} \tag{A3}$$

$$C_{hc}^{ij} = \frac{1}{\sqrt{2}} \cos \theta_B [y_1^* (V_R^{1i})^* V_L^{2j} + y_2 (V_R^{2i})^* V_L^{1j}]$$

$$-\frac{1}{\sqrt{2}} \sin \theta_B [y_\Psi^* (V_R^{2i})^* V_L^{2j} + y_\eta (V_R^{1i})^* V_L^{1j}], \quad (A4)$$

$$\begin{split} C_{Bn}^{ij} &= \frac{1}{\sqrt{2}} \sin \theta_B [y_3^* (N_R^{1i})^* N_L^{2j} + y_4 (N_R^{2i})^* N_L^{1j}] \\ &+ \frac{1}{\sqrt{2}} \cos \theta_B [y_\Psi^* (N_R^{2i})^* N_L^{2j} + y_\chi (N_R^{1i})^* N_L^{1j}], \end{split} \tag{A5}$$

$$C_{Bc}^{ij} = \frac{1}{\sqrt{2}} \sin \theta_B [y_1^* (V_R^{1i})^* V_L^{2j} + y_2 (V_R^{2i})^* V_L^{1j}]$$

$$+ \frac{1}{\sqrt{2}} \cos \theta_B [y_{\Psi}^* (V_R^{2i})^* V_L^{2j} + y_{\eta} (V_R^{1i})^* V_L^{1j}], \qquad (A6)$$

$$O_{L_n}^{ij} = B_2(N_L^{1i})^* N_L^{1j} + B_1(N_L^{2i})^* N_L^{2j},$$
 (A7)

$$O_{Rn}^{ij} = B_1(N_R^{1i})^* N_R^{1j} + B_2(N_R^{2i})^* N_R^{2j},$$
 (A8)

$$O_{Lc}^{ij} = B_2(V_L^{1i})^* V_L^{1j} + B_1(V_L^{2i})^* V_L^{2j},$$
 (A9)

$$O_{Rc}^{ij} = B_1(V_R^{1i})^* V_R^{1j} + B_2(V_R^{2i})^* V_R^{2j},$$
 (A10)

where the matrices N_L , N_R , V_L , and V_R are the ones that diagonalize the mass matrices as we discuss in Appendix B.

APPENDIX B: MASS MATRICES

The anomaly canceling fermions consist of two Dirac neutral fermions and two charged fermions. In this appendix we go through the diagonalization to the physical states.

(i) Neutral states:

The mass matrix for the neutral states in the basis $\chi_L^0 = (\chi_L^0 \Psi_L^0)$ and $\chi_R^0 = (\chi_R^0 \Psi_R^0)$ is given by

$$-\mathcal{L} \supset \left(\overline{\chi_R^0} \quad \overline{\Psi_R^0}\right) \mathcal{M}_0 \begin{pmatrix} \chi_L^0 \\ \Psi_I^0 \end{pmatrix} + \text{H.c.}, \quad (B1)$$

where

$$\mathcal{M}_0 = \frac{1}{\sqrt{2}} \begin{pmatrix} y_{\chi} v_B & y_3^* v_0 \\ y_4 v_0 & y_{\Psi}^* v_B \end{pmatrix},$$
 (B2)

where v_0 and v_B correspond to the VEVs of the SM Higgs bosons and the baryonic Higgs bosons, respectively. To obtain the physical fields χ_i^0 the mass matrix needs to be diagonalized. The relation between the fields in the Lagrangian and the physical fields is given by the N_L and N_R mixing matrices

$$\begin{pmatrix} \chi_L^0 \\ \Psi_L^0 \end{pmatrix} = N_L \begin{pmatrix} \chi_{1L}^0 \\ \chi_{2L}^0 \end{pmatrix}, \qquad \begin{pmatrix} \chi_R^0 \\ \Psi_R^0 \end{pmatrix} = N_R \begin{pmatrix} \chi_{1R}^0 \\ \chi_{2R}^0 \end{pmatrix}.$$
(B3)

The unitary matrices N_L and N_R diagonalize the mass matrix as follows

$$N_R^{\dagger} \mathcal{M}_0 N_L = \mathcal{M}_0^{\text{diag}},$$
 (B4)

and the following relations can be used to find N_L and N_R

$$|\mathcal{M}_0^{\text{diag}}|^2 = N_L^{\dagger} \mathcal{M}_0^{\dagger} \mathcal{M}_0 N_L = N_R^{\dagger} \mathcal{M}_0 \mathcal{M}_0^{\dagger} N_R, \quad (B5)$$

and the two mass eigenvalues correspond to

$$\begin{split} M_{\chi_i^0}^2 &= \frac{1}{2} \left[|\mu_\chi|^2 + |\mu_\Psi|^2 + |y_3|^2 \frac{v_0^2}{2} + |y_4|^2 \frac{v_0^2}{2} \right. \\ &+ \sqrt{ \left(|\mu_\chi|^2 + |\mu_\Psi|^2 + |y_3|^2 \frac{v_0^2}{2} + |y_4|^2 \frac{v_0^2}{2} \right)^2 - 4|\mu_\chi|^2 |\mu_\Psi|^2 - |y_3|^2 |y_4|^2 v_0^4 + 4v_0^2 \text{Re}[\mu_\chi \mu_\Psi^* y_3 y_4^*] } \right], \end{split}$$

where v_0 corresponds to the SM Higgs VEV and we have used $\mu_{\gamma} = y_{\gamma} v_B / \sqrt{2}$ and $\mu_{\Psi} = y_{\Psi} v_B / \sqrt{2}$.

(ii) Charged states:

The mass matrix for the new charged fermions in the basis $\chi_L^- = (\eta_L^- \Psi_L^-)$ and $\chi_R^- = (\eta_R^- \Psi_R^-)$ is given by

$$-\mathcal{L} \supset \left(\overline{\eta_{R}^{-}} \quad \overline{\Psi_{R}^{-}}\right) \mathcal{M}_{C} \begin{pmatrix} \eta_{L}^{-} \\ \Psi_{L}^{-} \end{pmatrix} + \text{H.c.}, \quad (B6)$$

where

$$\mathcal{M}_C = \frac{1}{\sqrt{2}} \begin{pmatrix} y_{\eta} v_B & y_1^* v_0 \\ y_2 v_0 & y_{\Psi}^* v_B \end{pmatrix}.$$
 (B7)

To obtain the physical fields χ_i^{\pm} the mass matrix needs to be diagonalized. The relation between the fields in the Lagrangian and the physical fields is given by the V_L and V_R mixing matrices

$$\begin{pmatrix} \eta_L^- \\ \Psi_L^- \end{pmatrix} = V_L \begin{pmatrix} \chi_{1L}^- \\ \chi_{2L}^- \end{pmatrix}, \qquad \begin{pmatrix} \eta_R^- \\ \Psi_R^- \end{pmatrix} = V_R \begin{pmatrix} \chi_{1R}^- \\ \chi_{2R}^- \end{pmatrix}.$$
(B8)

The unitary matrices V_L and V_R diagonalize the mass matrix as follows

$$V_R^{\dagger} \mathcal{M}_C V_L = \mathcal{M}_C^{\text{diag}},$$
 (B9)

and the following relations can be used to find ${\cal V}_L$ and ${\cal V}_R$

$$|\mathcal{M}_{C}^{\text{diag}}|^{2} = V_{L}^{\dagger} \mathcal{M}_{C}^{\dagger} \mathcal{M}_{C} V_{L} = V_{R}^{\dagger} \mathcal{M}_{C} \mathcal{M}_{C}^{\dagger} V_{R}, \quad (\text{B10})$$

and the two mass eigenvalues correspond to

$$\begin{split} M_{\chi_i^{\pm}}^2 &= \frac{1}{2} \left[|\mu_{\eta}|^2 + |\mu_{\Psi}|^2 + |y_1|^2 \frac{v_0^2}{2} + |y_2|^2 \frac{v_0^2}{2} \right. \\ & \pm \sqrt{ \left(|\mu_{\chi}|^2 + |\mu_{\Psi}|^2 + |y_1|^2 \frac{v_0^2}{2} + |y_2|^2 \frac{v_0^2}{2} \right)^2 - 4|\mu_{\eta}|^2 |\mu_{\Psi}|^2 - |y_1|^2 |y_2|^2 v_0^4 + 4v_0^2 \mathrm{Re}[\mu_{\eta} \mu_{\Psi}^* y_1 y_2^*] } \right], \end{split}$$

where we have used $\mu_{\eta} = y_{\eta} v_B / \sqrt{2}$ and $\mu_{\Psi} = y_{\Psi} v_B / \sqrt{2}$.

APPENDIX C: CP VIOLATION

The mass matrix for the charged fermions in Eq. (B7) can be written in general as

$$\mathcal{M}_{C} = \begin{pmatrix} \frac{|y_{\eta}|v_{B}}{\sqrt{2}} e^{i\delta_{\eta}} & \frac{|y_{1}|v_{0}}{\sqrt{2}} e^{-i\delta_{1}} \\ \frac{|y_{2}|v_{0}}{\sqrt{2}} e^{i\delta_{2}} & \frac{|y_{\psi}|v_{B}}{\sqrt{2}} e^{-i\delta_{\Psi}} \end{pmatrix}, \tag{C1}$$

which can be rotated into

$$\mathcal{M}_C' = \begin{pmatrix} \frac{|y_\eta| v_B}{\sqrt{2}} & \frac{|y_1| v_0}{\sqrt{2}} \\ \frac{|y_2| v_0}{\sqrt{2}} & \frac{|y_\psi| v_B}{\sqrt{2}} e^{i\phi_C} \end{pmatrix}, \tag{C2}$$

where

$$\phi_C = \delta_{\eta} - \delta_{\Psi} + \delta_1 - \delta_2 = \arg(y_{\eta} y_{\Psi}^* y_1 y_2^*), \quad (C3)$$

and the result of the EDMs are proportional to this CP-violating phase. A similar rotation can be performed to isolate ϕ_C to any matrix entry and this phase cannot be removed by phase rotations. Applying a similar procedure to the mass matrix for the neutral states, given in Eq. (B2), we conclude that there is another CP-violating phase in the neutral sector given by

$$\phi_N = \delta_{\gamma} - \delta_{\Psi} + \delta_3 - \delta_4 = \arg(y_{\gamma} y_{\Psi}^* y_3 y_4^*).$$
 (C4)

APPENDIX D: CONTRIBUTIONS TO THE EDMs

For the two-loop calculation of the diagram in Fig. 6 we follow the approach presented in Ref. [42]. The different contributions to the EDM of a SM fermion f are given by

$$d_f^{\gamma h} = \frac{\alpha^2 \cos \theta_B Q_f}{4\pi^2 s_W} \frac{m_f}{m_h^2 m_W} \sum_{i=1}^2 M_{\chi_i^\pm} \text{Im}[C_h^{ii}] I_{\gamma h}^i(M_{\chi_i^\pm}), \quad (D1)$$

$$d_f^{hZ} = \frac{e\alpha\cos\theta_B}{32\pi^2c_W s_W^2} \left(\frac{1}{2}T_3^f - s_W^2Q_f\right) \frac{m_f}{m_h^2 m_W} \sum_{i,j=1}^2 I_{hZ}^{ij}(M_{\chi_i^\pm}, M_{\chi_j^\pm}), \tag{D2}$$

$$\begin{split} d_f^{WW} &= \frac{T_3^f \alpha^2 e}{8\pi^2 s_W^4} \sum_{i,j=1}^2 \text{Im}[(V_L^{2i})^* N_L^{2j} V_R^{2i} (N_R^{2j})^*] \\ &\times \frac{m_f M_{\chi_i^\pm} M_{\chi_j^0}}{m_W^4} I_{WW}^{ij} (M_{\chi_i^\pm}, M_{\chi_j^0}), \end{split} \tag{D3}$$

$$d_f^{hZ_B} = \frac{g_B \alpha \cos \theta_B}{96\pi^2 s_W} \frac{m_f}{m_h^2 m_W} \sum_{i,j=1}^2 I_{hZ_B}^{ij}(M_{\chi_i^{\pm}}, M_{\chi_j^{\pm}}), \quad (D4)$$

where $M_{\chi_i^\pm}$ corresponds to the physical masses of the anomaly canceling fermions and the loop integrals I(m) are given by

$$I_{\gamma h}^{i}(M_{\chi_{i}^{\pm}}) = \int_{0}^{1} \frac{dx}{x} j\left(0, \frac{M_{\chi_{i}^{\pm}}^{2}}{m_{h}^{2}} \frac{1}{x(1-x)}\right),$$

$$\begin{split} I_{hZ}^{ij}(M_{\chi_{i}^{\pm}},M_{\chi_{j}^{\pm}}) &= \int_{0}^{1} dx \frac{1}{x(1-x)} j \bigg(\frac{m_{Z}^{2}}{m_{h}^{2}}, \frac{\Delta_{ij}(x)}{m_{h}^{2}} \bigg) \\ & \times \text{Re} \big[(ig_{S}^{ji}(g_{A}^{ij})^{*} - g_{P}^{ji}(g_{V}^{ij})^{*}) M_{\chi_{i}^{\pm}} x(1-x) \\ & - (ig_{S}^{ji}(g_{A}^{ij})^{*} + g_{P}^{ji}(g_{V}^{ij})^{*}) M_{\chi_{j}^{\pm}} (1-x)^{2} \big], \\ I_{WW}^{ij}(M_{\chi_{i}^{\pm}},M_{\chi_{j}^{0}}) &= \int_{0}^{1} \frac{dx}{1-x} j \bigg(0, \frac{xr_{\chi_{i}^{\pm}} + (1-x)r_{\chi_{j}^{0}}}{x(1-x)} \bigg), \\ I_{hZ_{B}}^{ij}(M_{\chi_{i}^{\pm}},M_{\chi_{j}^{\pm}}) &= \int_{0}^{1} dx \frac{1}{x(1-x)} j \bigg(\frac{M_{Z_{B}}^{2}}{m_{h}^{2}}, \frac{\Delta_{ij}(x)}{m_{h}^{2}} \bigg) \\ & \times \text{Re} \big[(ig_{S}^{ji}(\kappa_{A}^{ij})^{*} - g_{P}^{ji}(\kappa_{V}^{ij})^{*}) M_{\chi_{i}^{\pm}} x(1-x) \\ & - (ig_{S}^{ji}(\kappa_{A}^{ij})^{*} + g_{P}^{ji}(\kappa_{V}^{ij})^{*}) M_{\chi_{i}^{\pm}} (1-x)^{2} \big], \end{split}$$

with the parameters

$$g_S^{ij} = -\text{Re}[C_h^{ij}], \qquad g_P^{ij} = \text{Im}[C_h^{ij}],$$
 (D5)

$$g_V^{ij} = -\frac{g\sin\theta_W}{2}(C_L^{ij} + C_R^{ij}), \qquad g_A^{ij} = \frac{g\sin\theta_W}{2}(C_L^{ij} - C_R^{ij}),$$
 (D6)

$$\kappa_V^{ij} = -\frac{g_B}{2}(O_L^{ij} + O_R^{ij}), \qquad \kappa_A^{ij} = -\frac{g_B}{2}(O_R^{ij} - O_L^{ij}), \quad (D7)$$

where the matrices C_h , C_L , C_R , O_L , and O_R are given in Appendix A. θ_W corresponds to the Weinberg angle and the functions in the integrands correspond to

$$j(y,z) = \frac{1}{y-z} \left(\frac{y \log y}{y-1} - \frac{z \log z}{z-1} \right),$$
 (D8)

$$\Delta_{ij}(x) = \frac{xM_{\chi_i^{\pm}}^2 + (1-x)M_{\chi_j^{\pm}}^2}{x(1-x)},$$
 (D9)

$$r_{\chi_i} = \left(\frac{M_{\chi_i}}{m_W}\right)^2. \tag{D10}$$

APPENDIX E: BARYONIC HIGGS BOSON

In this appendix, we present the expressions for the decays of the baryonic Higgs boson including the loop-induced channels and the full analytic expressions. To compute the loop functions we make use of the Package-X [34] *Mathematica* package. In the Feynman diagrams below, we use an orange dot for vertices that can only occur by the mixing of the baryonic Higgs boson with the SM Higgs boson.

(i)
$$h_B \rightarrow \gamma \gamma$$
:

• $h_B \rightarrow \gamma \gamma$:

$$h_{B} \cdots \bigcap_{\gamma}^{\gamma} = h_{B} \cdots \bigcap_{F^{+}}^{\gamma} + h_{B} \cdots \bigcap_{\gamma}^{\gamma} + h_{B} \cdots \bigcap_{W^{-}}^{\gamma} + h_{B} \cdots \bigcap_{W$$

(ii) $h_B \rightarrow Z\gamma$:

• $h_B \to Z\gamma$:

$$\Gamma(h_B \to Z\gamma) = \frac{\alpha^2}{8\pi^3} \frac{M_{h_B}^2 - M_Z^2}{M_{h_B}^3} \left| \frac{\sin \theta_B}{v_0 \, s2\theta_W} \left(\sum_u m_u^2 \left(1 - \frac{8}{3} \sin^2 \theta_W \right) A_u + \sum_d \frac{m_d^2}{2} \left(1 - \frac{4}{3} \sin^2 \theta_W \right) A_d \right. \\ \left. + \sum_d \frac{m_e^2}{2} \left(1 - 4 \sin^2 \theta_W \right) A_e - \frac{\cos^2 \theta_W}{2} A_W \right) + \frac{3 \, g_B \cos \theta_B}{M_{Z_P}} \left(t \theta_W M_{\eta^+}^2 A_{\eta^+} + \frac{M_{\Psi^+}^2}{t2\theta_W} A_{\Psi^+} \right) \right|^2.$$

(iii) $h_B \rightarrow WW$:

• $h_B \to WW$:

$$h_{B} \cdots \bigvee_{W^{+}}^{W^{-}} = h_{B} \cdots \bigvee_{F^{0}}^{W^{-}} \bigvee_{W^{+}}^{W^{-}} + h_{B} \cdots \bigvee_{W^{+}}^{W^{-}} \bigvee_{W^{+}}^{W^{-}} + h_{B} \cdots \bigvee_{W^{+}}^{W^{-}} \bigvee_{W^{+}}^{W^{-}} + h_{B} \cdots \bigvee_{W^{+}}^{W^{-}} \bigvee_{W^{+}}^{W^{+}} \bigvee_{W^{+}}^{W^{+}$$

(iv)
$$h_B \rightarrow ZZ$$
:

• $h_B \rightarrow ZZ$:

$$\Gamma(h_B \to ZZ) = \frac{\sqrt{M_{h_B}^2 - 4M_Z^2}}{128\pi M_{h_B}^2 M_Z^4} \left(\cos^2\theta_B \frac{9g_B^2}{M_{Z_B}^2} \left| \sum_F g_{ZF}^2 B_F[Z] \right|^2 + 2(M_{h_B}^2 - 2M_Z^2) \times \right]$$

$$\text{Re} \left\{ \cos\theta_B \frac{3g_B}{M_{Z_B}} \sum_F g_{ZF}^2 B_F[Z] \left(\cos\theta_B \frac{3g_B}{M_{Z_B}} \sum_F g_{ZF}^2 C_F^*[Z] + 2\frac{\sin\theta_B}{v_0} M_Z^2 \right) \right\}$$

$$+ \left| \cos\theta_B \frac{3g_B}{M_{Z_B}} \sum_F g_{ZF}^2 C_F[Z] + 2\frac{\sin\theta_B}{v_0} M_Z^2 \right|^2 (M_{h_B}^4 - 4M_{h_B}^2 M_Z^2 + 12M_Z^4) \right\}.$$

In all these formulas, F_i and f_i correspond to the anomaly canceling and the SM fermions, respectively. The couplings between the gauge bosons and the new anomaly canceling fermions are given by (see Feynman rules in Appendix A),

$$g_{Z\Psi^0} = rac{e}{\sin 2 heta_W}, \qquad g_{Z\Psi^+} = -rac{e}{\tan 2 heta_W},
onumber \ g_{Z\eta^+} = e \, an \, heta_W.$$

APPENDIX F: LOOP FUNCTIONS

In this appendix we present the loop functions for the decay $h \to \gamma \gamma$ given in Eq. (4.1) and the decays of h_B given in Appendix E. We calculated these functions with the Package-X [34] *Mathematica* package. We write explicitly the loop functions as a function of the fermion mass M_f or gauge boson mass M_V running inside the loop and the Passarino-Veltman functions defined in Package-X:

(i) Loop functions entering in the h_B and h decays to two massless gauge fields:

$$\begin{split} F_f &= 4M_h^2 + (4M_f^2 - M_h^2) \log^2 \left[1 - \frac{M_h^2}{2M_f^2} \left(1 - \sqrt{1 - \frac{4M_f^2}{M_h^2}} \right) \right], \\ F_W &= M_h^4 + 6M_h^2 M_W^2 - 3(M_h^2 - 2M_W^2) M_W^2 \log^2 \left[1 - \frac{M_h^2}{2M_W^2} \left(1 - \sqrt{1 - \frac{4M_W^2}{M_h^2}} \right) \right], \\ G_{\chi_i^\pm} &= \log^2 \left[1 - \frac{M_h^2}{2M_{\chi_i^\pm}^2} \left(1 - \sqrt{1 - \frac{4M_\chi^2}{M_h^2}} \right) \right]. \end{split}$$

(ii) Loop functions entering in the h_B decay to a massive and a massless gauge fields:

$$\begin{split} A_f &= (4m_f^2 - M_{h_B}^2 + M_V^2)C_0[0, M_{h_B}^2, M_V^2; m_f] + 2\bigg(\frac{M_V^2(\Lambda[M_{h_B}^2] - \Lambda[M_V^2])}{M_{h_B}^2 - M_V^2} + 1\bigg), \\ A_W &= 2M_W^2C_0[0, M_{h_B}^2, M_V^2; M_W]((M_{h_B}^2 - 2M_W^2)(\tan^2\theta_W - 5) - 2M_V^2(\tan^2\theta_W - 3)) \\ &+ \bigg(\frac{M_V^2}{M_{h_B}^2 - M_V^2}(\Lambda[M_{h_B}^2] - \Lambda[M_V^2]) + 1\bigg)(M_{h_B}^2(1 - \tan^2\theta_W) + 2M_W^2(5 - \tan^2\theta_W)). \end{split}$$

(iii) Loop functions entering in the h_B decay to a two equal massive gauge bosons:

$$\begin{split} B_F[V] &= \frac{1}{16\pi^2} \frac{4M_F^2}{M_{h_B}^2 - 4M_V^2} \\ &\quad \times \left[(M_{h_B}^2 - 2M_V^2) (M_{h_B}^4 - 4M_F^2 (M_{h_B}^2 - 4M_V^2) - 6M_{h_B}^2 M_V^2 - 4M_V^4) C_0[M_{h_B}^2, M_V^2, M_V^2; M_F] \right. \\ &\quad \left. + 4M_V^2 (M_{h_B}^2 + 2M_V^2) (\Lambda[M_V^2] - \Lambda[M_{h_B}^2]) - 2(M_{h_B}^4 - 6M_{h_B}^2 M_V^2 + 8M_V^4) \right], \\ C_F[V] &= \frac{1}{16\pi^2} \frac{4M_F^2}{M_{h_B}^2 - 4M_V^2} \left[2(M_{h_B}^2 + 2M_V^2 (\Lambda[M_{h_B}^2] - \Lambda[M_V^2]) - 4M_V^2) \right. \\ &\quad \left. - (M_{h_B}^4 - 6M_{h_B}^2 M_V^2 - 4M_F^2 (M_{h_B}^2 - 4M_V^2) + 4M_V^4) C_0[M_{h_B}^2, M_V^2, M_V^2; M_F] \right]. \end{split}$$

- [1] M. Duerr, P. Fileviez Perez, and M. B. Wise, Gauge Theory for Baryon and Lepton Numbers with Leptoquarks, Phys. Rev. Lett. **110**, 231801 (2013).
- [2] P. Fileviez Perez, S. Ohmer, and H. H. Patel, Minimal theory for lepto-baryons, Phys. Lett. B 735, 283 (2014).
- [3] M. Duerr and P. Fileviez Perez, Baryonic dark matter, Phys. Lett. B **732**, 101 (2014).
- [4] M. Duerr and P. Fileviez Perez, Theory for baryon number and dark matter at the LHC, Phys. Rev. D 91, 095001 (2015).
- [5] P. Fileviez Perez, New paradigm for baryon and lepton number violation, Phys. Rep. **597**, 1 (2015).
- [6] P. Fileviez Perez, E. Golias, R.-H. Li, and C. Murgui, Leptophobic dark matter and the baryon number violation scale, Phys. Rev. D 99, 035009 (2019).
- [7] V. Andreev *et al.* (ACME Collaboration), Improved limit on the electric dipole moment of the electron, Nature (London) **562**, 355 (2018).
- [8] W. Bernreuther and M. Suzuki, The electric dipole moment of the electron, Rev. Mod. Phys. **63**, 313 (1991).
- [9] M. Pospelov and A. Ritz, Electric dipole moments as probes of new physics, Ann. Phys. (Amsterdam) **318**, 119 (2005).
- [10] T. Fukuyama, Searching for new physics beyond the Standard Model in electric dipole moment, Int. J. Mod. Phys. A 27, 1230015 (2012).
- [11] T. Chupp, P. Fierlinger, M. Ramsey-Musolf, and J. Singh, Electric dipole moments of atoms, molecules, nuclei, and particles, Rev. Mod. Phys. **91**, 015001 (2019).
- [12] P. Fileviez Perez and A. D. Plascencia, Electric dipole moments, new forces and dark matter, J. High Energy Phys. 03 (2021) 185.
- [13] P. Fileviez Perez, E. Golias, R.-H. Li, C. Murgui, and A. D. Plascencia, Anomaly-free dark matter models, Phys. Rev. D **100**, 015017 (2019).
- [14] G. Bélanger, F. Boudjema, A. Goudelis, A. Pukhov, and B. Zaldivar, micrOMEGAs5.0: Freeze-in, Comput. Phys. Commun. **231**, 173 (2018).
- [15] N. Aghanim *et al.* (Planck Collaboration), Planck 2018 results. VI. Cosmological parameters, Astron. Astrophys. 641, A6 (2020).

- [16] M. Aaboud *et al.* (ATLAS Collaboration), Search for new phenomena in dijet events using 37 fb⁻¹ of pp collision data collected at $\sqrt{s} = 13$ TeV with the ATLAS detector, Phys. Rev. D **96**, 052004 (2017).
- [17] A. M. Sirunyan *et al.* (CMS Collaboration), Search for narrow and broad dijet resonances in proton-proton collisions at $\sqrt{s} = 13$ TeV and constraints on dark matter mediators and other new particles, J. High Energy Phys. 08 (2018) 130.
- [18] E. Aprile *et al.* (XENON Collaboration), Dark Matter Search Results from a One Ton-Year Exposure of XEN-ON1T, Phys. Rev. Lett. **121**, 111302 (2018).
- [19] E. Aprile *et al.* (XENON Collaboration), Physics reach of the XENON1T dark matter experiment, J. Cosmol. Astropart. Phys. 04 (2016) 027.
- [20] M. Aaboud *et al.* (ATLAS Collaboration), Measurements of Higgs boson properties in the diphoton decay channel with 36 fb⁻¹ of pp collision data at \sqrt{s} = 13 TeV with the ATLAS detector, Phys. Rev. D **98**, 052005 (2018).
- [21] A. M. Sirunyan *et al.* (CMS Collaboration), Measurements of Higgs boson production cross sections and couplings in the diphoton decay channel at $\sqrt{s} = 13$ TeV, J. High Energy Phys. 07 (2021) 027.
- [22] CMS collaboration, Projected performance of an upgraded CMS detector at the LHC and HL-LHC: Contribution to the snowmass process, in *Proceedings of the Community* Summer Study 2013: Snowmass on the Mississippi, arXiv:1307.7135.
- [23] D. McKeen, M. Pospelov, and A. Ritz, Modified Higgs branching ratios versus *CP* and lepton flavor violation, Phys. Rev. D 86, 113004 (2012).
- [24] A. Y. Korchin and V. A. Kovalchuk, Polarization effects in the Higgs boson decay to γZ and test of *CP* and *CPT* symmetries, Phys. Rev. D **88**, 036009 (2013).
- [25] A. Alloul, B. Fuks, and V. Sanz, Phenomenology of the Higgs effective Lagrangian via FEYNRULES, J. High Energy Phys. 04 (2014) 110.

- [26] Y. Chen, R. Harnik, and R. Vega-Morales, Probing the Higgs Couplings to Photons in $h \to 4\ell$ at the LHC, Phys. Rev. Lett. **113**, 191801 (2014).
- [27] G. Aad *et al.* (ATLAS Collaboration), Constraints on non-Standard Model Higgs boson interactions in an effective Lagrangian using differential cross sections measured in the $H \rightarrow \gamma \gamma$ decay channel at $\sqrt{s} = 8$ TeV with the ATLAS detector, Phys. Lett. B **753**, 69 (2016).
- [28] M. B. Voloshin, CP violation in Higgs diphoton decay in models with vectorlike heavy fermions, Phys. Rev. D 86, 093016 (2012).
- [29] W. Altmannshofer, M. Bauer, and M. Carena, Exotic leptons: Higgs, flavor and collider phenomenology, J. High Energy Phys. 01 (2014) 060.
- [30] W. Chao and M. J. Ramsey-Musolf, Electroweak baryogenesis, electric dipole moments, and Higgs diphoton decays, J. High Energy Phys. 10 (2014) 180.
- [31] N. Bizot and M. Frigerio, Fermionic extensions of the Standard Model in light of the Higgs couplings, J. High Energy Phys. 01 (2016) 036.
- [32] D. Egana-Ugrinovic, M. Low, and J. T. Ruderman, Charged fermions below 100 GeV, J. High Energy Phys. 05 (2018) 012.
- [33] P. Fileviez Perez and M. B. Wise, Breaking local baryon and lepton number at the TeV scale, J. High Energy Phys. 08 (2011) 068.

- [34] H. H. Patel, Package-X: A Mathematica package for the analytic calculation of one-loop integrals, Comput. Phys. Commun. 197, 276 (2015).
- [35] P. Fileviez Perez, C. Murgui, and A. D. Plascencia, Baryonic Higgs and dark matter, J. High Energy Phys. 02 (2021) 163.
- [36] N. Arkani-Hamed, S. Dimopoulos, G. F. Giudice, and A. Romanino, Aspects of split supersymmetry, Nucl. Phys. B709, 3 (2005).
- [37] J. Doyle, Search for the electric dipole moment of the electron with thorium monoxide—The acme experiment, http://online.kitp.ucsb.edu/online/nuclear_c16/doyle/ (2016).
- [38] M. Carena, M. Quirós, and Y. Zhang, Electroweak Baryogenesis from Dark-Sector *CP* Violation, Phys. Rev. Lett. 122, 201802 (2019).
- [39] M. Carena, M. Quirós, and Y. Zhang, Dark CP violation and gauged lepton or baryon number for electroweak baryogenesis, Phys. Rev. D 101, 055014 (2020).
- [40] P. F. Perez, C. Murgui, and A. D. Plascencia, Baryogenesis via leptogenesis: Spontaneous B and L violation, Phys. Rev. D 104, 055007 (2021).
- [41] G. W. Bennett *et al.* (Muon (g-2) Collaboration), An improved limit on the muon electric dipole moment, Phys. Rev. D **80**, 052008 (2009).
- [42] Y. Nakai and M. Reece, Electric dipole moments in natural supersymmetry, J. High Energy Phys. 08 (2017) 031.