

# Full-shape cosmology analysis of the SDSS-III BOSS galaxy power spectrum using an emulator-based halo model: A 5% determination of $\sigma_8$

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We present the results obtained from the full-shape cosmology analysis of the redshift-space power spectra for four galaxy samples of the SDSS-III BOSS DR12 galaxy catalog over  $0.2 < z < 0.75$ . For the theoretical template, we use an emulator that was built from an ensemble set of  $N$ -body simulations, which enables fast and accurate computation of the redshift-space power spectrum of “halos.” Combining with the halo occupation distribution to model the galaxy-halo connection, we can compute the redshift-space power spectrum of BOSS-like galaxies in less than a CPU second, for an input model under flat  $\Lambda$ CDM cosmology. In our cosmology inference, we use the monopole, quadrupole, and hexadecapole moments of the redshift-space power spectrum and include seven nuisance parameters, with broad priors, to model uncertainties in the galaxy-halo connection for each galaxy sample, but do not use any information on the abundance of galaxies. We demonstrate a validation of our analysis pipeline using the mock catalogs of BOSS-like galaxies, generated using different recipes of the galaxy-halo connection and including the assembly bias effect. Assuming weak priors on cosmological parameters, except for the BBN prior on  $\Omega_b h^2$  and the CMB prior on  $n_s$ , we show that our model well reproduces the BOSS power spectra. Including the power-spectrum information up to  $k_{\max} = 0.25h \text{ Mpc}^{-1}$ , we find  $\Omega_m = 0.301^{+0.012}_{-0.011}$ ,  $H_0 = 68.2 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , and  $\sigma_8 = 0.786^{+0.036}_{-0.037}$  for the mode and 68% credible interval, after marginalization over galaxy-halo connection parameters. We find little improvement in the cosmological parameters beyond a maximum wavelength  $k_{\max} \simeq 0.2h \text{ Mpc}^{-1}$  due to the shot noise domination and marginalization of the galaxy-halo connection parameters. Our results are consistent with the Planck CMB results within  $1\sigma$  statistical uncertainties.

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## I. INTRODUCTION

The three-dimensional distribution of galaxies, measured from wide-area spectroscopic surveys of galaxies, is a powerful probe of cosmology—e.g., for constraining cosmological parameters such as parameters characterizing the nature of dark energy and for testing gravity theory on cosmological scales [1–7]. To attain the fundamental cosmology, there are various existing, ongoing, and planned galaxy redshift surveys: the SDSS-III Baryon Oscillation Spectroscopic Survey (BOSS [8]), the SDSS-IV extended Baryon Oscillation Spectroscopic Survey (eBOSS [9]), the Subaru Prime Focus Spectrograph (PFS [10]), the Dark

Energy Spectroscopic Instrument (DESI [11]), the ESA *Euclid* satellite mission [12], and the NASA Nancy Grace Roman Space Telescope [13].

The galaxy distribution observed by spectroscopic surveys is modulated by the Doppler effect due to the line-of-sight peculiar velocities of galaxies, and it exhibits characteristic anisotropies, called the redshift-space distortion (RSD) [14–16]. The RSD effect is useful to improve cosmological constraints by breaking degeneracies between the cosmological parameters and uncertainties in galaxy bias relative to the underlying matter distribution [17]. In addition, since the RSD effect is a gravitational effect, it can be used, if precisely measured, to probe the strength of the gravitational field in large-scale structure, which can in turn be used to test gravity theory on cosmological scales [18].

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In order to exploit the full information from galaxy redshift surveys, we need a sufficiently accurate theoretical template that enables a high-fidelity comparison with the measured clustering statistics of galaxies to obtain a robust estimation of cosmological parameters. The linear theory of cosmological fluctuations, which has been a remarkable success in CMB analyses, ceases to be accurate at  $k \gtrsim 0.1h \text{ Mpc}^{-1}$  due to nonlinear effects of structure formation [17]. The standard approach to tackling this difficulty has been analytic prescriptions based on the perturbation theory (PT) of large-scale structure [19,20]. This approach describes the distribution of galaxies in terms of a series expansion of both the matter density and velocity fields with a set of free coefficients/terms including bias parameters, under the single-stream approximation [21,22]. A further refined model consistently separating short-scale physics including the galaxy bias from large-scale dynamics of interest, the so-called effective field theory of large-scale structure (EFTofLSS), has also been developed [23]. These models have been applied to actual datasets to obtain cosmological constraints [5,24–29]. While these PT-based templates give useful predictions at linear and quasi-nonlinear scales up to  $k \sim 0.2h \text{ Mpc}^{-1}$ , an application of these models to even smaller scales is still disturbed by even higher-order contributions of both the density and velocity fields, as well as nonperturbative effects arising from the dynamics beyond shell crossing—i.e., the formation of galaxies (or dark matter halos) (e.g., Refs. [30–36]). Consequently, the cosmology analysis of the galaxy power spectrum has been typically limited to the wave number  $k \lesssim 0.15h\text{--}0.2h \text{ Mpc}^{-1}$ , depending on the redshift and the accuracy of the model required to meet the statistical precision of data [25,26,37]. In other words, the clustering information on the higher- $k$  scales does not seem practical for cosmology in this method, because the information is used to basically constrain higher-order bias parameters and other nuisance parameters that need to be introduced for the theoretical consistency of models.

As an alternative approach, in this paper we use a simulation-based theoretical template, the *emulator*, which enables fast and accurate computation of the redshift-space power spectrum of “halos” in the flat  $\Lambda$ CDM framework, developed in our previous paper [38]. Dark matter halos are locations where galaxies likely form. It is relatively straightforward to accurately simulate the formation and evolution processes of halos using  $N$ -body simulations and then have an accurate prediction of their clustering properties including the redshift-space power spectrum [20,39]. Kobayashi *et al.* [38] developed an emulator by training a feed-forward neural network with a dataset of the redshift-space power spectra of halos measured from halo catalogs in an ensemble set of  $N$ -body simulations for 80 models within the flat  $w$ CDM framework in the DARK QUEST campaign [40]. The emulator was validated using the test dataset consisting of 20 cosmological models that are not in

training, and it was shown that the power spectra are sufficiently accurate up to  $k = 0.6h \text{ Mpc}^{-1}$ . The emulator includes all the nonperturbative, nonlinear effects relevant to the formation and evolution of halos: nonlinear clustering, nonlinear RSD, nonlinear bias of halos, and the halo exclusion effect. By combining with a halo occupation distribution (HOD) model [41–46], the emulator enables us to compute the redshift-space power spectrum of galaxies in less than a CPU second on a typical recent laptop computer. Thus, the emulator allows for cosmological parameter inference of the galaxy power spectrum in a multidimensional parameter space. Such an emulator-based method is equivalent to estimating cosmological parameters from comparison of the observed power spectrum with mock spectra from simulated galaxy catalogs generated from costly high-resolution  $N$ -body simulations with varying cosmological models.

Hence, the purpose of this paper is to perform a cosmology analysis of the redshift-space galaxy power spectrum measured from the public BOSS DR12 large-scale structure catalog over  $0.2 < z < 0.75$  [47], using the aforementioned emulator. In doing this, we analyze the “full-shape” information in the monopole, quadrupole, and hexadecapole moments of the redshift-space power spectra, beyond the traditional approach to extract only geometrical information through the features of baryon acoustic oscillations (BAOs) and the anisotropy originating from RSD. We first show a series of validation checks of our method to ensure unbiased cosmological inference beyond the accuracy assessment of the emulator at the halo power-spectrum level already presented in our previous paper. We apply the full analysis pipeline to mock signals of the galaxy power spectrum measured from the galaxy mock catalogs, and then check whether our method can recover the cosmological parameters to within the statistical errors. For this validation, we use the mock catalogs generated using different recipes of galaxy-halo connection from our fiducial HOD model (also see Ref. [37] for similar analyses but with different observables) and also use mock catalogs including the assembly bias effect that is one of the most dangerous, physical systematic effects in the halo model approach. We then apply the analysis method to the BOSS galaxy power spectra under the flat  $\Lambda$ CDM cosmology. In doing this, we employ weak priors on the cosmological parameters, except for the BBN prior on  $\Omega_b h^2$  [48] and the CMB prior on  $n_s$  [49], employ very broad priors for the galaxy-halo connection parameters, and then estimate the cosmological parameters after marginalization over uncertainties in the nuisance parameters. We also compare our cosmological constraints with the recent PT-based results [29,50] and the Planck 2018 cosmological results [49].

The structure of this paper is as follows: In Sec. II, we will describe the power-spectrum data and covariance we use in this work. In Sec. III, we will describe details of the emulator-based halo model as the theoretical template and

then the parameters and priors used in the cosmology analysis. In Sec. IV, we show the main results of this paper: the cosmological parameters for the flat  $\Lambda$ CDM model. In Sec. V, we give discussion on possible residual systematic effects in the data and the theoretical template. Section VI is devoted to the conclusion.

## II. DATA

For the galaxy power-spectrum data and the covariance matrix, we use the updated measurement of the BOSS DR12 power spectrum recently provided in Ref. [51], which is publicly available from [https://fbeatler.github.io/hub/deconv\\_paper.html](https://fbeatler.github.io/hub/deconv_paper.html). We use four data chunks, named “NGC  $z_1$ ,” “SGC  $z_1$ ,” “NGC  $z_3$ ,” and “SGC  $z_3$ ,” which mean the measurements for different galaxy samples in two nonoverlapping redshift bins (“ $z_1$ ” and “ $z_3$ ”) for both the northern and southern Galactic caps (“NGC” and “SGC”). “ $z_1$ ” (“ $z_3$ ”), which we hereafter call “low- $z$ ” (“high- $z$ ”), corresponds to the range  $0.2 < z < 0.5$  ( $0.5 < z < 0.75$ ) with its effective redshift  $z_{\text{eff}} = 0.38$  (0.61). We compute the theoretical model of the power spectrum for each redshift bin at its effective redshift.

The estimator adopted in Ref. [51] gives the power-spectrum multipoles convolved with the survey window function, which can be expressed by a matrix-vector multiplication. Therefore, we construct a consistent model prediction of the window-convolved power spectrum as

$$\mathbf{P}^{\text{conv}} = \mathbf{WMP}^{\text{true,flat-sky}}, \quad (1)$$

where  $\mathbf{P}^{\text{conv}}$  is the vector of the convolved power-spectrum multipoles,  $\mathbf{P}^{\text{true,flat-sky}} = \{P_0, P_2, P_4\}$  is that of the true (unconvolved) power-spectrum multipoles computed in the global plane-parallel approximation, where the monopole, quadrupole, and hexadecapole moments are concatenated.  $\mathbf{M}$  is the matrix that induces the odd multipoles (dipole and octopole) arising from the wide-angle effect.  $\mathbf{W}$  is the matrix that consists of Fourier-space multipole moments of the survey window function (see Ref. [51] for details). Due to the correction for the wide-angle effect through the matrix  $\mathbf{M}$ , the dipole and octopole moments (the real parts, since they are purely imaginary) are induced by the leakage from the standard even multipole moments, but we do not use these odd multipoles in this work. We compute the power-spectrum monopole, quadrupole, and hexadecapole using the emulator-based theoretical model we describe in the next section and substitute them for  $\mathbf{P}^{\text{true,flat-sky}}$  in Eq. (1). The matrices  $\mathbf{W}$  and  $\mathbf{M}$  are also made publicly available on the same website.

In the measurement of the convolved power-spectrum multipoles, Ref. [51] assumes the flat-geometry  $\Lambda$ CDM model with  $\Omega_m = 0.31$ , which is the same as the model assumed in the original measurement of the BOSS DR12 public spectra for their cosmology analysis [26]. They measure the power spectrum in a cubic box by a fast Fourier transform

(FFT) with the side length  $L = 3500h^{-1}$  Mpc and Nyquist wave number  $k_{\text{Ny}} = 0.628h$  Mpc $^{-1}$ . Each Fourier mode is divided into wave number bins in the range  $k \in (0, 0.4)h$  Mpc $^{-1}$  with width  $\Delta k = 0.01h$  Mpc $^{-1}$ .

As for the power-spectrum covariance matrix, we use the matrix provided by Ref. [51], which was estimated from 2048 realizations of the MULTIDARK-PATCHY (hereafter PATCHY) mock catalogs [52,53]. These mock catalogs were generated using an approximate  $N$ -body solver which combines the Lagrangian perturbation theory, a small-scale halo collapse model, and a semianalytical galaxy biasing scheme, augmented by calibration to a reference large-volume  $N$ -body simulation sample selected from the BIGMULTIDARK simulations [54]. To correct the biased estimate of the inverse covariance, we multiply the so-called Hartlap factor [55] to the inverse of the estimated covariance:

$$f_{\text{Hartlap}} = \frac{N_r - n_{\text{bin}} - 2}{N_r - 1}, \quad (2)$$

where  $n_{\text{bin}}$  is the number of bins we use in the parameter inference. For instance, in the case where we use the monopole, quadrupole, and hexadecapole moments up to  $k_{\text{max}} = 0.25h$  Mpc $^{-1}$ , the number of bins is  $n_{\text{bin}} = 25 \times 3 = 75$  for each galaxy sample, yielding  $f_{\text{Hartlap}} = 0.9629$ .

## III. THEORETICAL MODEL AND PARAMETERS

### A. Theoretical model

To investigate the cosmological parameter constraint from the BOSS galaxy power spectrum, we use the theoretical template computed using the emulator for the redshift-space power spectrum of halos combined with the HOD model, developed in our previous work [38]. We below give a brief description of our theoretical template, and see Ref. [38] (and also Ref. [17]) for further details.

We employ the five-parameter HOD model in Ref. [45], which splits the galaxies into central and satellite galaxies. The mean halo occupation numbers of central and satellite galaxies within host halos with mass  $M$  are given as

$$\langle N_c \rangle(M) = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\log M - \log M_{\text{min}}}{\sigma_{\log M}} \right) \right] \quad (3)$$

and

$$\begin{aligned} \langle N_s \rangle(M) &= \langle N_c \rangle(M) \lambda_s(M) \\ &\equiv \langle N_c \rangle(M) \left( \frac{M - \kappa M_{\text{min}}}{M_1} \right)^{\alpha_{\text{sat}}}, \end{aligned} \quad (4)$$

respectively, where  $\text{erf}(x)$  is the error function, and the logarithms in Eq. (3) are base 10. Note that in our model,

we adopt  $M \equiv M_{200} = (4\pi/3)200\bar{\rho}_{m0}R_{200}^3$  as the halo mass definition, where  $\bar{\rho}_{m0}$  is the mean comoving mass density in the Universe and  $R_{200}$  is the spherical comoving radius within which the mean mass density is 200 times  $\bar{\rho}_{m0}$ . Here  $\{\log M_{\min}, \sigma_{\log M}^2, \log M_1, \alpha_{\text{sat}}, \kappa\}$  are model parameters. The probability distribution of galaxies given the mean number is assumed to be Bernoulli for centrals and Poisson for satellites, given that the halo of interest has a central halo. This HOD model is also used in the cosmology analysis of the galaxy-galaxy weak lensing and projected galaxy correlation function measured from the Hyper Suprime-Cam Year 1 catalog and the BOSS DR11 catalog [56].

Using the above HOD model, our full model of the redshift-space galaxy power spectrum is given by the sum of the one- and two-halo terms:

$$P_{\text{gg}}(\mathbf{k}) = P_{\text{gg}}^{\text{1h}}(\mathbf{k}) + P_{\text{gg}}^{\text{2h}}(\mathbf{k}), \quad (5)$$

where

$$P_{\text{gg}}^{\text{1h}}(\mathbf{k}) = \frac{1}{\bar{n}_{\text{g}}^2} \int dM \frac{dn}{dM}(M) \langle N_{\text{c}} \rangle(M) \times [2\lambda_{\text{s}}(M)\tilde{\mathcal{H}}(\mathbf{k}; M) + \lambda_{\text{s}}(M)^2\tilde{\mathcal{H}}(\mathbf{k}; M)^2], \quad (6)$$

and

$$P_{\text{gg}}^{\text{2h}}(\mathbf{k}) = \frac{1}{\bar{n}_{\text{g}}^2} \int dM_1 \frac{dn}{dM}(M_1) [\langle N_{\text{c}} \rangle(M_1) + \langle N_{\text{s}} \rangle(M_1)\tilde{\mathcal{H}}(\mathbf{k}; M_1)] \times \int dM_2 \frac{dn}{dM}(M_2) [\langle N_{\text{c}} \rangle(M_2) + \langle N_{\text{s}} \rangle(M_2)\tilde{\mathcal{H}}(\mathbf{k}; M_2)] \times P_{\text{hh}}(\mathbf{k}; M_1, M_2), \quad (7)$$

where  $P_{\text{hh}}(\mathbf{k}; M_1, M_2)$  is the redshift-space halo power spectrum, for which we use our emulator [38] that includes the RSD effects in both linear and nonlinear regimes for an input set of model parameters (cosmological parameters, redshift, and halo masses). These power spectra depend on the two-dimensional wave vector,  $\mathbf{k} = (k_{\parallel}, k_{\perp})$  or  $k(\mu, \sqrt{1-\mu^2})$ , due to the redshift-space distortion effect, where  $\mu$  is the cosine angle between the wave vector  $\mathbf{k}$  and the line-of-sight direction  $\hat{\mathbf{n}}$ . In the above formulas,  $dn/dM$  is the halo mass function and  $\bar{n}_{\text{g}}$  is the global mean number density of galaxies, defined as

$$\bar{n}_{\text{g}} = \int dM \frac{dn}{dM}(M) [\langle N_{\text{c}} \rangle(M) + \langle N_{\text{s}} \rangle(M)]. \quad (8)$$

For satellite galaxies, we model the intrahalo profile in redshift space as the multiplication of the Navarro-Frenk-White (NFW) profile [57] and the velocity distribution [17,58,59]:

$$\tilde{\mathcal{H}}(\mathbf{k}; M) = \tilde{u}_{\text{NFW}}(k; M)\tilde{\mathcal{F}}(k_{\parallel}; M), \quad (9)$$

where  $\tilde{u}_{\text{NFW}}(k; M)$  is the Fourier transform of the NFW density profile normalized by halo mass  $M$ . To specify the NFW profile, we assume the median concentration-mass relation  $c(M_{200})$  following the model in Refs. [60,61].  $\tilde{\mathcal{F}}(k_{\parallel}; M)$  is the Fourier transform of the Gaussian velocity distribution, whose velocity dispersion is given as

$$\mathcal{F}(\Delta r_{\parallel}; M) = \frac{1}{\sqrt{2\pi\sigma_{\text{v}}^2(M)}} \exp\left[-\frac{\Delta r_{\parallel}^2}{2\sigma_{\text{v}}^2(M)}\right]. \quad (10)$$

The velocity dispersion,  $\sigma_{\text{v}}^2(M)$ , is given by

$$\sigma_{\text{v}}^2(M) = \frac{1}{a^2 H^2} \frac{GM}{2aR_{200}(M)}, \quad (11)$$

where  $G$  is the gravitational constant,  $a$  is the scale factor,  $H$  is the Hubble parameter at scale factor  $a$ , and  $R_{200}(M)$  is the halo radius  $R_{200}$  for halos with mass  $M$ . The factor  $1/(aH)^2$  is to convert the velocity to the redshift-space displacement. The above velocity distribution models the ‘‘fingers of God’’ (FoG) effect due to virial motions of satellite galaxies in their host halos. In order to further include uncertainties in the FoG effect, we will introduce a nuisance parameter to model the uncertainty,  $\sigma_{\text{v}}(M) \rightarrow c_{\text{vel}}\sigma_{\text{v}}(M)$ , and treat  $c_{\text{vel}}$  as a model parameter in the cosmology analysis.

As described above, we use our emulator [38] to compute the redshift-space halo power spectrum  $P_{\text{hh}}(\mathbf{k}; M_1, M_2)$  in the two-halo term [Eq. (7)] for an input model in the flat  $\Lambda$ CDM cosmology. The emulator outputs  $P_{\text{hh}}(\mathbf{k}; M_1, M_2)$ , given as a function of the two-dimensional wave vector  $\mathbf{k}$ , rather than the multipole moments such as  $P_{\text{hh},\ell}(k; M_1, M_2)$ . This modeling allows us to straightforwardly include the Alcock-Paczyński effect (see the next subsection), even in the presence of the FoG effect. We also use the publicly available DARK EMULATOR (<https://dark-emulator.readthedocs.io/en/latest/>) [40] to compute the halo mass function, and the COLOSSUS code (<http://www.benediktmeier.com/code/colossus/>) [62] to compute the halo concentration-mass relation. In the theoretical model, the redshift-space halo power spectrum in the two-halo term,  $P_{\text{hh}}(\mathbf{k}; M_1, M_2)$ , carries cosmological information, and other functions, such as the HOD and the distribution of galaxies in their host halos, are all nuisance and are needed to account for uncertainties in the galaxy-halo connection.

## B. Alcock-Paczyński effect

Since we need to assume a reference cosmology ( $\Omega_{\text{m}} = 0.31$ ) in the measurement of the power spectrum, we incorporate the Alcock-Paczyński (AP) effect [63,64] into the theoretical model. Due to the difference between



the true and reference cosmologies, the Fourier-space wave numbers are transformed as

$$\begin{aligned} k_{\perp}^{\text{ref}} &= \alpha_{\perp} k_{\perp} \equiv \frac{D_A(z)}{D_A^{\text{ref}}(z)} k_{\perp}, \\ k_{\parallel}^{\text{ref}} &= \alpha_{\parallel} k_{\parallel} \equiv \frac{H^{\text{ref}}(z)}{H(z)} k_{\parallel}, \end{aligned} \quad (12)$$

where  $D_A(z)$  and  $H(z)$  are the angular diameter distance and Hubble parameter at the effective redshift  $z$ . Quantities with the superscript ‘‘ref’’ denote those for the reference cosmology. By this coordinate transformation, the power-spectrum multipole is transformed as

$$P_{\text{gg},\ell}^{\text{ref}}(k^{\text{ref}}) = \frac{2\ell + 1}{2\alpha_{\perp}^2 \alpha_{\parallel}} \int_{-1}^1 d\mu^{\text{ref}} P_{\text{gg}}(k, \mu) \mathcal{L}_{\ell}(\mu^{\text{ref}}), \quad (13)$$

where  $k$  and  $\mu$  in the argument of  $P_{\text{gg},\ell}^{\text{ref}}$  are given in terms of  $k^{\text{ref}}$  and  $\mu^{\text{ref}}$ ;  $k = k(k^{\text{ref}}, \mu^{\text{ref}})$  and  $\mu = \mu(\mu^{\text{ref}})$ , given as

$$k(k^{\text{ref}}, \mu^{\text{ref}}) = k^{\text{ref}} \frac{1}{\alpha_{\perp}} \left[ 1 + (\mu^{\text{ref}})^2 \left( \frac{\alpha_{\perp}^2}{\alpha_{\parallel}^2} - 1 \right) \right]^{1/2}, \quad (14)$$

$$\mu(\mu^{\text{ref}}) = \mu^{\text{ref}} \frac{\alpha_{\perp}}{\alpha_{\parallel}} \left[ 1 + (\mu^{\text{ref}})^2 \left( \frac{\alpha_{\perp}^2}{\alpha_{\parallel}^2} - 1 \right) \right]^{-1/2}. \quad (15)$$

Since the reference cosmology is generally different from the underlying true cosmology, the AP effect induces an additional anisotropy in the measured power spectrum. In other words, the measured anisotropy enables us to infer the true cosmology through the geometrical information.

### C. Model parameters and priors

In this subsection, we describe the model parameters that we infer, as well as their prior settings. The default setting is summarized in Table I.

#### 1. Cosmological parameters

Since we want to infer the cosmological parameters within the flat-geometry  $\Lambda$ CDM framework, we sample all of the five parameters:

$$\mathbf{p}_{\text{cosmo}} = \{\omega_b, \omega_c, \Omega_{\Lambda}, \ln(10^{10} A_s), n_s\}, \quad (16)$$

where  $\omega_b = \Omega_b h^2$  and  $\omega_c = \Omega_c h^2$  are the physical energy density parameters of baryon and cold dark matter,  $\Omega_{\Lambda}$  is the energy density parameter of the cosmological constant, and  $A_s$  and  $n_s$  are the amplitude (at the pivot scale  $k_{\text{pivot}} = 0.05 \text{ Mpc}^{-1}$ ) and the spectral tilt of the power spectrum of primordial curvature perturbations. For  $\omega_b$  and  $n_s$ , we impose priors that are inferred from other cosmological probes. More specifically, we adopt a Gaussian prior on  $\omega_b$  from the primordial deuterium and helium

TABLE I. Model parameters and priors used in our cosmology analysis in flat  $\Lambda$ CDM cosmology.  $\mathcal{N}(\mu, \sigma)$  denotes the Gaussian distribution with mean  $\mu$  and standard deviation  $\sigma$ .  $\mathcal{U}(a, b)$  denotes the uniform distribution between the minimum value  $a$  and the maximum value  $b$ . The Gaussian priors on  $\omega_b$  and  $n_s$  are based on the BBN and Planck CMB constraints, respectively (see text for details). The flat priors on other cosmological parameters are set to be within the parameter ranges on which the emulator is supported.

Parameter	Prior
<i>Cosmological parameters</i>	
$\omega_b$	$\mathcal{N}(0.02268, 0.00038)$
$\omega_c$	$\mathcal{U}(0.10782, 0.13178)$
$\Omega_{\Lambda}$	$\mathcal{U}(0.54752, 0.82128)$
$\ln(10^{10} A_s)$	$\mathcal{U}(2.4752, 3.7128)$
$n_s$	$\mathcal{N}(0.9649, 0.0042)$
<i>HOD parameters</i>	
$\log M_{\text{min}}$	$\mathcal{U}(12.0, 15.0)$
$\sigma_{\log M}^2$	$\mathcal{U}(0.0001, 2.0)$
$\log M_1$	$\mathcal{U}(12.0, 16.0)$
$\alpha_{\text{sat}}$	$\mathcal{U}(0.01, 5.0)$
$\kappa$	$\mathcal{U}(0.01, 5.0)$
<i>Other nuisance parameters</i>	
$c_{\text{vel}}$	$\mathcal{U}(0.01, 10.0)$
$P_{\text{shot}}$	$\mathcal{U}(-10^4, 10^4) h^{-3} \text{ Mpc}^3$
<i>Derived parameters</i>	
$\Omega_m$	...
$H_0$	...
$\sigma_8$	...

abundance data compared with the standard big bang nucleosynthesis (BBN) model [48,65,66]. On the other hand, we impose a Gaussian prior on  $n_s$  given in Table 1 of Ref. [49] for the Planck 2018 ‘‘TT, TE, EE + lowE + lensing’’ data. We treat  $\Omega_m (= 1 - \Omega_{\Lambda})$ , the total matter energy density,  $H_0 = 100h \text{ km s}^{-1} \text{ Mpc}^{-1}$ , the Hubble constant, and  $\sigma_8$ , the standard deviation of linear matter perturbations at  $z = 0$  averaged within a sphere with comoving radius  $8h^{-1} \text{ Mpc}$ , as the derived parameters. We fix the density parameter of neutrinos to  $\omega_{\nu} = 0.00064$ , corresponding to 0.06 eV for the total mass of the three mass eigenstates, which is used when computing the linear matter power spectrum used to set up the initial conditions of cosmological simulations that are used for the DARK EMULATOR development [40].

#### 2. Nuisance parameters

As we described in Sec. III A, we employ five parameters to specify the HOD model for each galaxy sample. In addition, we include two additional nuisance parameters:

- (1)  $c_{\text{vel}}$ : The multiplicative coefficient on the velocity dispersion of galaxies relative to the halo center.

It regulates the uncertainty on the strength of the FoG effect [see around Eq. (10)].

- (2)  $P_{\text{shot}}$ : The residual shot noise contribution apart from the simple Poisson shot noise. We add  $P_{\text{shot}}$  to the galaxy power spectrum  $P_{\text{gg}}(k, \mu)$ , and hence it is relevant only to the monopole moment.

We employ a flat prior over the range  $[-10^4, 10^4] (h^{-1} \text{ Mpc})^3$  for the latter. The mean number density of galaxies for each sample is a factor of a few times  $10^{-4} (h^{-1} \text{ Mpc})^3$ , so the prior range is sufficiently wide. Thus, we have seven nuisance parameters on the galaxy-halo connection:

$$\mathbf{p}_{\text{galaxy}} = \{\log M_{\min}, \sigma_{\log M}^2, \log M_1, \alpha_{\text{sat}}, \kappa, c_{\text{vel}}, P_{\text{shot}}\}, \quad (17)$$

for each of the four galaxy samples. Hence, the total number of parameters is  $5 + 7 \times 4 = 33$  within the flat  $\Lambda$ CDM framework. As can be found from Table I, we employ a broad prior range for each of the galaxy-halo connection parameters. For example, the range of  $M_{\min}$ , which is one of the parameters that are sensitive to the linear bias of the galaxy sample, corresponds to halos that have  $b_1 \simeq [1.2, 10.2]$  at  $z = 0.5$  for the Planck cosmology. Thus, our approach can be considered conservative in parameter inference.

#### D. Parameter inference

We employ the Bayesian inference to derive the parameter posterior distribution:

$$p_{\text{post}}(\mathbf{p}|\mathcal{D}) \propto \mathcal{L}(\mathcal{D}|\mathbf{p})p_{\text{prior}}(\mathbf{p}), \quad (18)$$

where  $p_{\text{prior}}$  and  $p_{\text{post}}$  are the prior and posterior distributions of model parameters, and  $\mathcal{L}(\mathcal{D}|\mathbf{p})$  is the likelihood function of the observational data  $\mathcal{D}$  given parameters  $\mathbf{p}$ . Using the power-spectrum data vector and the covariance matrix, we compute the log-likelihood function:

$$\begin{aligned} \ln \mathcal{L}(\mathcal{D}|\mathbf{p}) = & -\frac{1}{2} \sum_{\text{samp}} \sum_{\ell, \ell'} \sum_{i, j}^{k_{\max}} [P_{\ell}^{\mathcal{D}}(k_i) - P_{\ell}(k_i; \mathbf{p})] \\ & \times \text{Cov}^{-1}[P_{\ell}(k_i), P_{\ell'}(k_j)] [P_{\ell'}^{\mathcal{D}}(k_j) - P_{\ell'}(k_j; \mathbf{p})], \end{aligned} \quad (19)$$

where we assume the Gaussian likelihood and omit the normalization factor.  $P_{\ell}^{\mathcal{D}}(k_i)$  denotes the data of the  $\ell$ th multipole moment of the power spectrum in the  $i$ th wave number bin,  $P_{\ell}(k_i; \mathbf{p})$  is its theoretical model prediction, and  $\mathbf{p}$  is the model parameters. We include the power-spectrum information over  $k_{\min} \leq k \leq k_{\max}$ , and we employ  $k_{\min} = 0.005h \text{ Mpc}^{-1}$  and  $k_{\max} = 0.25h \text{ Mpc}^{-1}$  as our fiducial choices, respectively. We will below give a validation of the choice of  $k_{\max} = 0.25h \text{ Mpc}^{-1}$  and discuss how different choices of  $k_{\min}$  or  $k_{\max}$  change the

cosmological results. The summation  $\sum_{\text{samp}}$  denotes the summation over galaxy samples when the power-spectrum information for different galaxy samples are combined.

For the parameter sampling, we employ the Markov-chain Monte Carlo (MCMC) sampling of the standard Metropolis algorithm [67], or the nested sampling algorithm MultiNest [68] implemented in the public Python package PyMultiNest [69]. In the MCMC sampling, we monitor the convergence for the cosmological parameters by using a method in Ref. [70], which is an improved variant of the Gelman-Rubin diagnostic [71,72]. More specifically, we apply the rank normalization [70] to the MCMC chains and measure the Gelman-Rubin statistic  $\hat{R}$  of the chains split in half (the so-called split- $\hat{R}$  [73]), after discarding 1000 points at the beginning of each chain as the burn-in phase. We run the MCMCs until the criteria  $\hat{R} < 1.05$  for the cosmological parameters are met. We use the GetDist [74] package to draw triangle plots of parameter posteriors.

We should note that, throughout this paper, we *do not* include the abundance of galaxies (the mean number density) or the BAO information after reconstruction (e.g., see Ref. [75] for such a study) in the data vector in the parameter inference.

## IV. RESULTS

We show the main results of our cosmology analysis in this section. Throughout this paper, we mainly focus on the constraints on three cosmological parameters,  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$ , which are well constrained by the redshift-space galaxy power spectrum, in a flat  $\Lambda$ CDM model.

### A. Validation tests

Before showing the main results, we first present validation tests of our emulator-based method. To test the validity and usefulness of the emulator-based method, we perform various cosmology challenges: we apply our cosmology analysis pipeline to simulated mock signals of the redshift-space galaxy power spectrum to address whether the pipeline can recover the underlying true cosmological parameters used in the simulations. Please see Ref. [37] for details of the procedures and aims. Y. K., who is one of the authors of this paper and led the actual cosmology inference analysis of the BOSS data, applied the pipeline to the mock signals for the BOSS-like galaxies used in Ref. [37]. The mock galaxy catalogs were generated using a different recipe for the galaxy-halo connection based on subhalos, so it is not entirely clear whether our HOD method can recover the underlying cosmological parameters. For instance, the spatial and velocity structures of satellite galaxies in host halos are generally different from those in our fiducial halo model. In this test, Y. K. was not informed of the cosmological parameters, and the validation test was done effectively in a blind manner.

He submitted the results to T.N., who is a coauthor of this paper and is the main organizer and the maintainer of the challenge program, and then the ground truth cosmological parameters were revealed with the mutual agreement not to update the analysis anymore. The submitted results are recorded and presented on the challenge webpage (<https://www2.yukawa.kyoto-u.ac.jp/takahiro.nishimichi/data/PTchallenge/>).

In Fig. 1, we show the results of our validation tests. The left panel shows the results using the simulated signals that are generated from the mock catalogs of the above cosmology challenges of Ref. [37]. To mimic the cosmology analysis of the BOSS power spectra, we use the mock catalogs at  $z = 0.38$  and  $0.61$  to simulate the redshift-space spectra for the four subsamples, the NGC/SGC in the low- $z$  and high- $z$  bins, and use the same covariance matrix as that used in the following cosmology analysis of BOSS spectra (see Sec. II). These mock catalogs are based on the realizations of  $N$ -body simulations for the total volume of  $566(h^{-1} \text{ Gpc})^3$  [37], which is about 100 times that of the BOSS DR12 galaxy sample. The large volume of the simulations allows us to sufficiently reduce the sample variance errors in the simulated power spectra. Therefore,

we can conduct a fairly stringent test of the systematic error due to an imperfect modeling of the power spectrum. The figure shows that our analysis method recovers the true cosmological parameters to within the statistical errors of the BOSS galaxy spectra. We also stress that our emulator-based method passes the validation test even if including the power-spectrum information up to  $k_{\text{max}} = 0.3h \text{ Mpc}^{-1}$ , where the perturbation theory breaks down. Here, the constraints on  $\Omega_m$  and  $H_0$  are mainly from the BAO features and partly from the power spectrum shape via the AP effect. On the other hand, the constraint on  $\sigma_8$  is from the power-spectrum amplitude, after the degeneracies with galaxy bias uncertainty (uncertainties in the galaxy-halo connection in our model) are lifted by measurements of the RSD effect, as we will discuss later (Sec. V F). However, including the information beyond  $k \simeq 0.2h \text{ Mpc}^{-1}$  gives little improvement in the cosmological parameters, due to the shot noise domination and the degeneracies with the galaxy-halo connection parameters. On the other hand, we find that the constraints on HOD parameters are improved by including the higher- $k$  information.

As another sanity check, we also perform the validation tests using the mock galaxy catalogs generated in

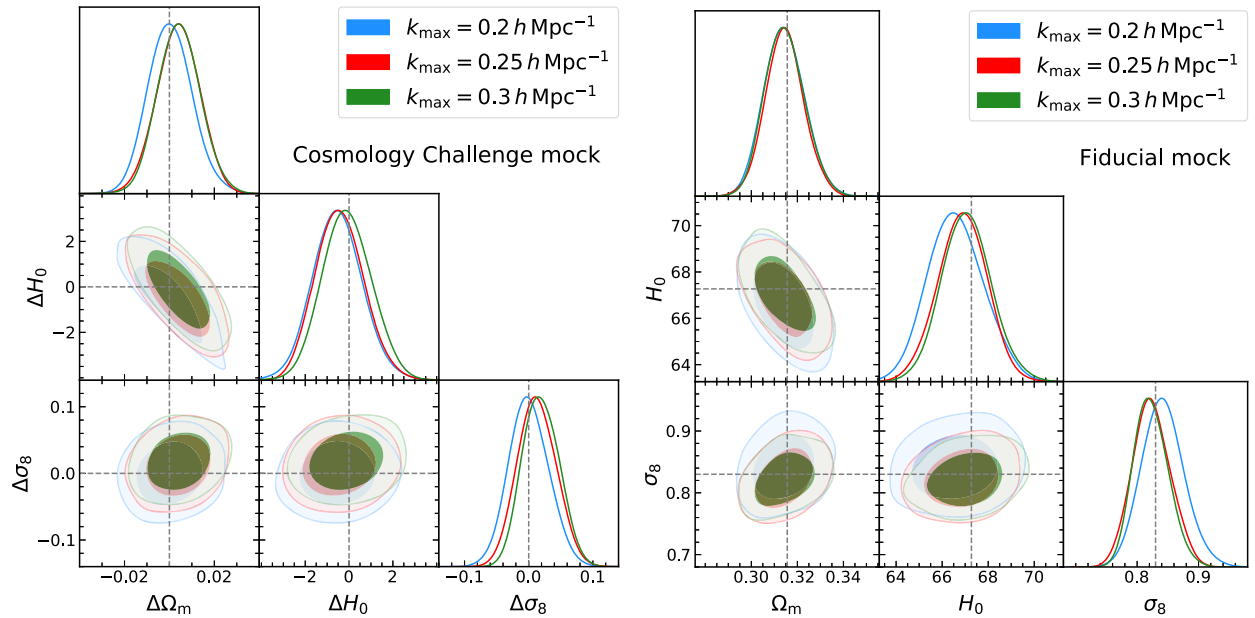


FIG. 1. Results of validation tests of our cosmology analysis pipeline: we apply the analysis pipeline to the mock signals for the four BOSS-like galaxy samples using the covariance matrix of the actual BOSS spectra. We include the monopole, quadrupole, and hexadecapole moments of the redshift-space power spectrum for each of the four galaxy samples over  $0.005h \text{ Mpc}^{-1} \leq k \leq k_{\text{max}}$ , and we show the results for  $k_{\text{max}} = 0.20h$ ,  $0.25h$ , or  $0.30h \text{ Mpc}^{-1}$ , respectively. The contours show the posterior distributions of  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$  including marginalization over uncertainties in other parameters including the galaxy-halo connection parameters. The left plot shows the results for the galaxy mocks that are generated using a different recipe of the galaxy-halo connection from our fiducial HOD model: the mock galaxy catalogs used in the cosmology challenges in Ref. [37] (see text for details). Since we would like to blind the true values of the cosmological parameters, we show the results in terms of the parameter difference such as  $\Delta\Omega_m = \Omega_m - \Omega_{m,\text{true}}$ . The right plot shows the results for the mock catalogs generated using the same form of HOD model as in our HOD model. The dashed lines in the right panel are the true values of the cosmological parameters used in the mock catalogs—i.e., those for the Planck cosmology.

Refs. [17,40]. They are based on the simulations for the Planck cosmology using the same HOD prescription as that in our analysis. Similarly to the above test, we use the outputs of  $N$ -body simulations at  $z = 0.251$  and  $0.617$ , adopt the same HOD model as that in Ref. [76] to populate galaxies into halos of each realization, and then simulate the mock galaxy spectra for the four galaxy samples. We use the simulations of total volume  $128(h^{-1} \text{ Gpc})^3$  to generate the simulated data vector (see Ref. [17] for details of the simulations) and perform the cosmology analysis using the same covariance matrix of the BOSS spectra. The right panel of Fig. 1 shows that our analysis method recovers the cosmological parameters to within the statistical errors for all the  $k_{\text{max}}$  values. One might notice a slight bias in each cosmological parameter, even if both the theoretical template and the mock catalogs employ the same form of HOD model. We ascribe the parameter shift to the projection effect of the full posterior distribution in a multidimensional parameter space (see Ref. [77] for a similar discussion). Here we note that some of the galaxy-halo connection parameters are not necessarily recovered by the analysis, as explicitly shown in Fig. 14 of Appendix A. The figure in the appendix also shows that including the power-spectrum information on the higher  $k_{\text{max}}$  gives smaller error bars for the galaxy-halo connection parameters, although the central values are biased for some of the galaxy-halo parameters. On the other hand, the credible intervals of the cosmological parameters are not much improved by including the information from  $k_{\text{max}} = 0.25h$  to  $0.30h \text{ Mpc}^{-1}$ , as can be found from Fig. 1. Hence, from these results, we conclude that our method can robustly recover the cosmological parameters to within the statistical errors of the BOSS power spectra, after marginalization over the galaxy-halo connection parameters. Here, we note that the cosmological information is extracted from the redshift-space power spectrum of halos predicted by the emulator in our method. In this paper, we employ  $k_{\text{max}} = 0.25h \text{ Mpc}^{-1}$  as our fiducial choice of the maximum wave number.

We will also later show the validation test of our analysis method using the mock catalogs including the assembly bias effect, which is one of the most dangerous physical systematic effects in the halo model approach.

## B. Results: $\Lambda$ CDM cosmology

Figure 2 shows the main results of this paper, the cosmological parameters obtained from the actual BOSS power spectra. The figure shows the projected posterior distributions of  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$  for the flat  $\Lambda$ CDM model, after marginalizing over the other parameters such as the galaxy-halo connection parameters. These constraints include the BAO and full shape information of the redshift-space power spectrum for the four samples of the low- $z$ /high- $z$  NGC and SGC samples, up to  $k_{\text{max}} = 0.25h \text{ Mpc}^{-1}$ , where the nonlinear effects such as nonlinear bias, nonlinear

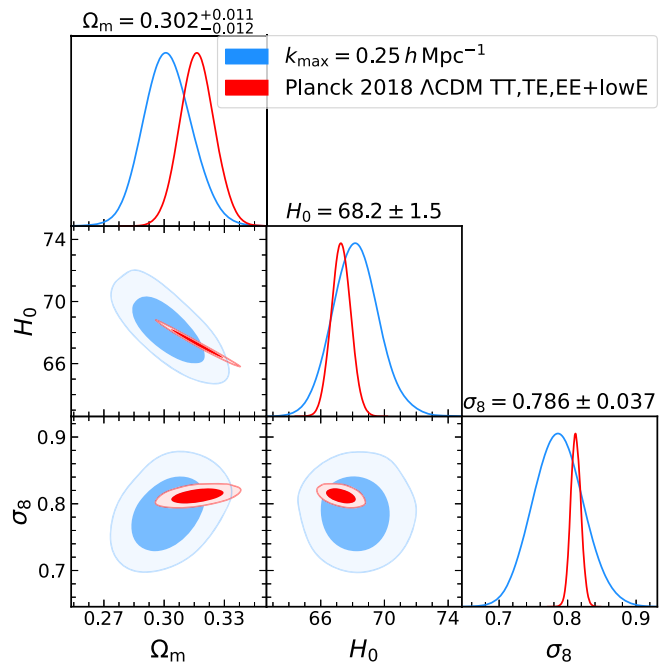


FIG. 2. The posterior distributions of  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$ , obtained from the cosmology inference including the full shapes of the monopole, quadrupole, and hexadecapole moments of the BOSS DR12 galaxy power spectra up to  $k_{\text{max}} = 0.25h \text{ Mpc}^{-1}$  for the flat  $\Lambda$ CDM model. For the theoretical templates, we use the emulator-based halo model, and the posteriors include marginalization over uncertainties in other cosmological parameters and the nuisance parameters including the galaxy-halo connection parameters. For comparison, the red contours show the results from the Planck 2018 “TT, TE, EE + lowE” analysis.

clustering, and nonlinear RSD are properly included. Our method achieves precise measurements of the cosmological parameters:

$$\begin{aligned} \Omega_m &= 0.301^{+0.012}_{-0.011}, \\ H_0 &= 68.2 \pm 1.4, \\ \sigma_8 &= 0.786^{+0.036}_{-0.037}, \end{aligned} \quad (20)$$

where we report the mode and the 68% credible interval of the marginalized posterior distribution for each parameter, respectively. Note that  $H_0$  is in units of  $\text{km s}^{-1} \text{ Mpc}^{-1}$ .

Our results can be compared with the Planck 2018 CMB constraints: we overplot the Planck 2018 cosmological constraints from the baseline likelihood of “TT, TE, EE + lowE”; the MCMC chains of the Planck 2018 cosmology analysis are downloaded from the Planck Legacy Archive (<http://pla.esac.esa.int/pla/#cosmology>), where the neutrino mass is fixed to  $0.06 \text{ eV}$ , as we did in our analysis. Our results are in good agreement with the Planck results for all three of the cosmological parameters. In Table II, we also show the parameter value at the *maximum a posteriori* (MAP), the median, and the mode



TABLE II. The results of the cosmological parameter inference of the BOSS power spectra for a  $\Lambda$ CDM model as in Fig. 2. Note that we include the BBN prior on  $\omega_b$  and the Planck CMB prior on the spectral tilt  $n_s$  (see Table I). For each parameter, we show the parameter value at the *maximum a posteriori* (MAP), the median, and the mode with a 68% credible interval (CI) for the 1D posterior distribution of each parameter. The parameters other than  $\ln(10^{10}A_s)$  are derived parameters (see Table I). For comparison with constraints from other experiments, we also show the constraints on  $S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$  and  $f(z)\sigma_8(z)$ , where  $f$  is the linear growth rate  $f \equiv d \ln D/d \ln a$ . For  $f\sigma_8$ , we show the results obtained from the cosmology analysis using the subsample of a low- $z$  NGC + SGC or high- $z$  NGC + SGC sample at the effective redshift  $z_{\text{eff}} = 0.38$  and  $0.61$ , respectively (see the right panel of Fig. 5). For comparison, we also show the 68% credible interval from the Planck 2018 “TT, TE, EE + lowE” analysis, taken from Table 2 of Ref. [49].

Parameter	MAP	Median	68% CI	Planck 68% CI
$\ln(10^{10}A_s)$	2.93	3.01	$3.01^{+0.089}_{-0.087}$	$3.045 \pm 0.016$
$\Omega_m$	0.300	0.302	$0.301^{+0.012}_{-0.011}$	$0.3166 \pm 0.0084$
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	68.3	68.2	$68.2^{+1.4}_{-1.4}$	$67.27 \pm 0.60$
$\sigma_8$	0.754	0.786	$0.786^{+0.036}_{-0.037}$	$0.8120 \pm 0.0073$
$S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$	0.754	0.787	$0.784^{+0.048}_{-0.042}$	$0.834 \pm 0.016$
$f\sigma_8(z_{\text{eff}} = 0.38)$	0.474	0.471	$0.467^{+0.035}_{-0.028}$	$0.4771 \pm 0.0066$
$f\sigma_8(z_{\text{eff}} = 0.61)$	0.434	0.434	$0.430^{+0.034}_{-0.026}$	$0.4696 \pm 0.0053$

with a 68% credible interval (CI) for the 1D posterior distribution of each parameter. For comparison with the weak lensing survey results (e.g., Refs. [56,81]), we also give the results for  $S_8$ , the parameter on which the weak lensing surveys can give most the stringent constraint. In addition, we show the results for  $f(z)\sigma_8(z)$ , which is the parameter often used to characterize the constraint mainly from the RSD measurement on linear scales. Note that, since we assume a flat  $\Lambda$ CDM cosmology, the linear growth rate  $f(z)$  is determined solely by  $\Omega_m$  through

$$f(z) = -\frac{3}{2}\Omega_m(z) + \left[ \int_0^1 \frac{dx}{\{\Omega_m(z)x^{-1} + (1 - \Omega_m(z))x^2\}^{\frac{3}{2}}} \right]^{-1}, \quad (21)$$

where  $\Omega_m(z) = \Omega_m(1+z)^3[H_0/H(z)]^2$  is the time-dependent matter density parameter. It is in contrast to traditional RSD analyses such as Ref. [26], where one performs *model-independent* linear growth measurements, marginalizing over possible nonlinear corrections and focusing only on the amplitude of the apparent anisotropies arising from the linear RSD effect. Therefore, as we have already quoted earlier in this subsection, we can determine fundamental cosmological parameters, breaking the degeneracy between  $\sigma_8$  and  $f$  under the assumed cosmological model. The table gives the constraints for  $f(z)\sigma_8(z)$  that are obtained from the MCMC analyses using either the low- $z$

TABLE III. Comparison of the parameter bounds from recent “full-shape” analyses of the BOSS DR12 power spectrum (68% CI). For the analysis of the EFTofLSS model, we quote the results using the window-convolved power spectrum (top row of Table IV of Ref. [50]). All the results shown here are obtained from exactly the same power-spectrum data provided by Ref. [51].

Parameter	This work	EFTofLSS	LPT
		model [50]	model [29]
$\Omega_m$	$0.301^{+0.012}_{-0.011}$	$0.312^{+0.011}_{-0.012}$	$0.305 \pm 0.01$
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	$68.2 \pm 1.4$	$68.5^{+1.1}_{-1.3}$	$68.5 \pm 1.1$
$\sigma_8$	$0.786^{+0.036}_{-0.037}$	$0.737^{+0.040}_{-0.044}$	$0.738 \pm 0.048$

NGC + SGC sample or the high- $z$  NGC + SGC sample at the effective redshifts  $z_{\text{eff}} = 0.38$  or  $0.61$ , respectively (see below). Our constraint is from the combined information of the BAO, the AP effect, the RSD effect, and the amplitude and shape information of the power spectrum under the flat  $\Lambda$ CDM framework.

Table III compares our result with those from the recent similar full-shape analyses of the power-spectrum multipoles using the PT-based theory models: the EFTofLSS model [50] and the model based on Lagrangian perturbation theory (LPT) [29]. These models use the same power-spectrum signals and window function of BOSS DR12 provided by Ref. [51]—i.e., the same dataset that we use.

It is interesting to note that our results are consistent with these two analyses to within the statistical errors, even though our halo-model-based method and the PT-based ones are constructed based on totally different frameworks. The size of the error bar in each parameter is comparable with those of the their results. This might be counter-intuitive, because one might think that our halo-model-based method is a more restrictive model than PT-based models and expect our method to give tighter constraints on the cosmological parameters. The lack of difference is probably due to the wide priors of the galaxy-halo connection parameters in our analysis, and we will later discuss possible room for improvement in the cosmological parameters within our method.

We also note other works [27,28,78–80] that recently performed the full-shape cosmology analysis of the BOSS power spectrum. However, these works used different dataset and/or analysis methods from those in this paper, so it is not easy to make an apple-to-apple comparison with our result. For completeness of our discussion, we stress that it is becoming possible to obtain a full-shape cosmology analysis and find cosmological constraints for a given cosmological framework, such as the flat  $\Lambda$ CDM model.

Figure 3 shows that our model at MAP well reproduces all the measured multipoles of redshift-space power spectra. The reduced chi-squared value at the MAP is  $\chi^2/d.o.f. \simeq 1.05$  for 267(= 300 – 33) degrees of freedom (the  $p$ -value  $p \simeq 0.28$ ), implying that the MAP model gives

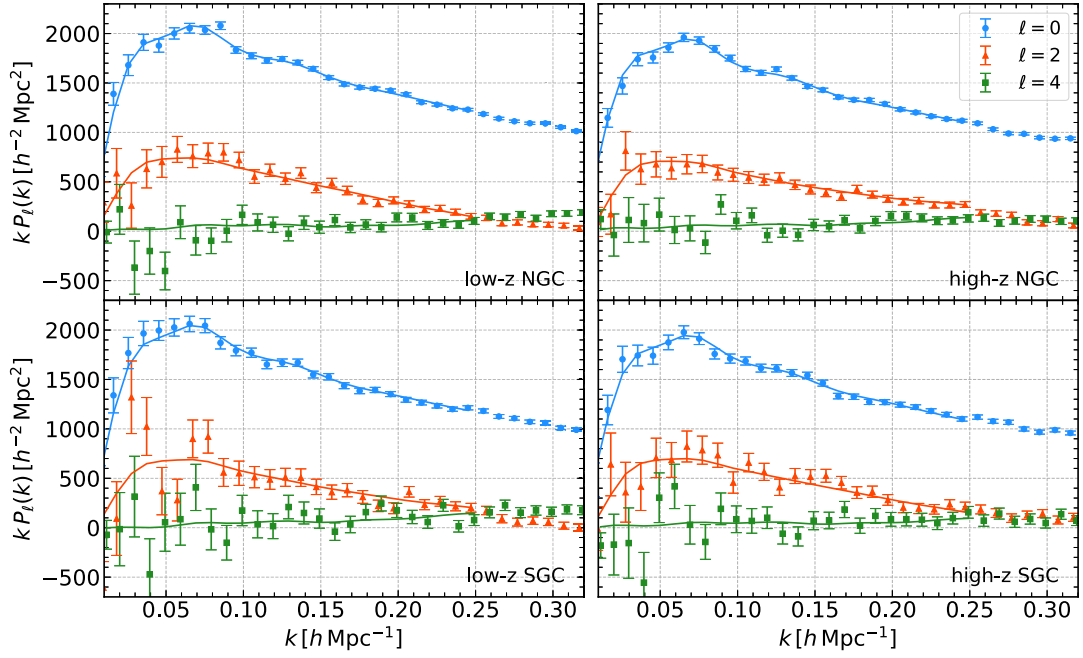


FIG. 3. The comparison of monopole (blue), quadrupole (red), and hexadecapole (green) moments between the data (symbols with error bars) and the model predictions (solid lines) at MAP of the MCMC chains in our cosmology analysis shown in Fig. 2. The error bars are computed from the diagonal elements of the covariance matrix, described in Sec. II.

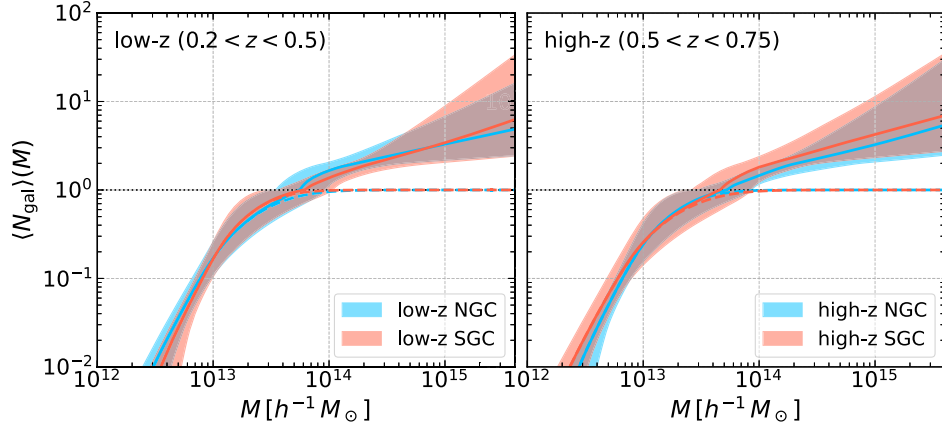


FIG. 4. The median and 68% percentile interval of the HOD functions for each of the BOSS galaxy samples (low-z/high-z NGC/SGC samples), obtained from the MCMC chains in Fig. 2. The solid and dashed lines are the medians of central + satellite and central-only HOD functions, respectively.

an acceptable fit to the data. Taking a closer look at the figure, our model has a slightly weaker BAO feature than data. This tendency reflects the fact that our power-spectrum emulator is based on the training data which have a larger  $k$ -bin width ( $\Delta k = 0.02 h \text{ Mpc}^{-1}$ ) than the data ( $\Delta k = 0.01 h \text{ Mpc}^{-1}$ ) to suppress the statistical scatters on the training data (also see Appendix A of Ref. [38]). Since the BAO feature leads to a tight constraint on  $\Omega_m$  through the AP effect, the sharpening of the BAO feature in the emulator could improve the cosmological constraints.

Figure 4 shows the mean HOD functions obtained from the MCMC chains. It can be found that the galaxy population inferred from the BOSS DR12 galaxy power spectra is almost confined to halos with masses  $M \gtrsim 10^{12} h^{-1} M_{\odot}$ . This figure also shows that there is no remarkable difference in the HOD among the four galaxy samples. Our results are qualitatively consistent with the HODs estimated in the previous works [82–84]. We again stress that the HOD constraints are obtained from the fitting of the emulator-based halo model to the redshift-space

power spectrum, without employing any strong priors on the HOD parameters or using the abundance information (the mean number density of galaxies). Hence, the posterior distributions of HOD are purely from the redshift-space clustering information, while the previous works take into account different clustering information such as the galaxy-galaxy weak lensing and/or the projected correlation function (see, e.g., Ref. [56] for such a study).

## V. DISCUSSION

In this section, we discuss the robustness of our cosmology results: we study how different analysis methods and datasets change the inferred cosmological parameters.

### A. Variations in the cosmological parameters for different galaxy subsamples

In Fig. 5, we study how the cosmological parameters are changed when using different subsets of the data vector: the left panel shows the results for four individual galaxy samples, and the right panel shows the combined results for each of the two redshift bins, where the two galactic hemispheres, NGC and SGC, are combined. Shifts in each parameter display a similar trend to those shown in Fig. 2 of Ref. [27], even though we use a totally different theoretical template—i.e., the halo-model-based method, compared to the EFTofLSS in their paper. Hence, we think that the parameter shifts are likely due to the sample variances in each subsample. For completeness of our discussion, in Appendix B we show the 2D posterior distributions for the

full parameters for each of the four individual galaxy samples (see Fig. 15). The low- $z$  SGC sample displays a sizable difference in some parameters compared to the other samples, but the difference is still within the statistical errors. Hence, we cannot give any definite conclusion as to whether that sample has a potential observational systematics compared to the others. For completeness, we also show the cosmological constraints obtained from the four individual subsamples in Table IV.

### B. The impact of hexadecapole moments

Figure 6 shows that the inclusion of the hexadecapole moment of the redshift-space power spectrum yields only a subtle improvement in the cosmological parameters, because the hexadecapole moments have lower signal-to-noise ratios than the monopole and quadrupole moments, as shown in Fig. 3. However, we note that the hexadecapole indeed improves some of the HOD parameters, which is consistent with the finding in Ref. [85].

### C. The cosmological information in different ranges of $k$

One advantage of our approach—e.g., compared to a PT-based method such as the EFTofLSS—is that ours enables us to compare the model predictions with the measurements up to higher  $k_{\max}$ . As described in our previous paper [38], our emulator is designed to give an accurate prediction of the redshift-space power spectrum up to  $k = 0.6h \text{ Mpc}^{-1}$ . However, the power-spectrum

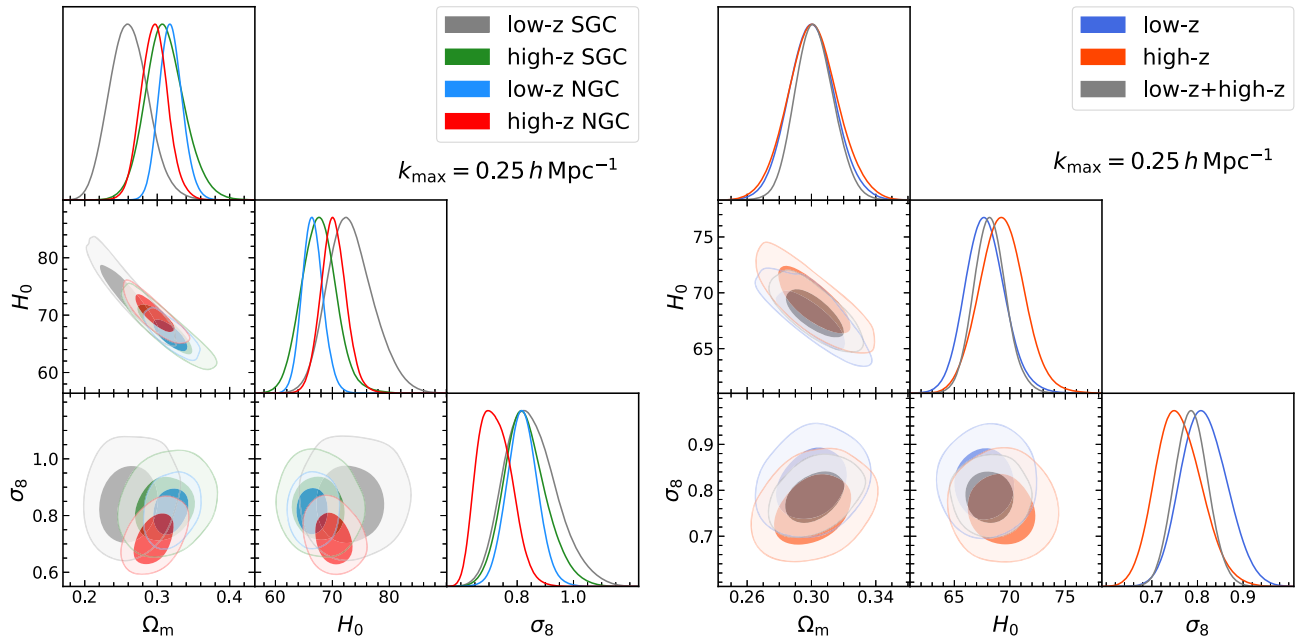


FIG. 5. The posterior distributions for cosmological parameters, obtained from the different galaxy subsamples. The left panel shows the results for four individual galaxy samples: low- $z$  NGC, low- $z$  SGC, high- $z$  NGC, and high- $z$  SGC. The right panel shows the results for each of the low- $z$  or high- $z$  NGC + SGC samples. In the right panel, we overplot the gray contours to show the distribution for the full sample for comparison, which is the same as the blue contours in Fig. 2.

TABLE IV. Similar to Table II, but this table shows the results obtained from the cosmology analysis using each of the four galaxy samples.

Parameter	low- $z$ NGC			low- $z$ SGC		
	MAP	Median	68% CI	MAP	Median	68% CI
$\ln(10^{10}A_s)$	3.05	3.10	$3.12^{+0.11}_{-0.14}$	3.17	3.14	$3.14^{+0.20}_{-0.21}$
$\Omega_m$	0.311	0.318	$0.317^{+0.016}_{-0.015}$	0.261	0.261	$0.259^{+0.028}_{-0.025}$
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	66.1	66.5	$66.4^{+1.8}_{-1.7}$	71.1	73.0	$72.4^{+4.2}_{-3.6}$
$\sigma_8$	0.782	0.817	$0.816^{+0.055}_{-0.051}$	0.811	0.842	$0.826^{+0.102}_{-0.077}$
$S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$	0.796	0.841	$0.840^{+0.063}_{-0.061}$	0.756	0.783	$0.763^{+0.106}_{-0.084}$
$f\sigma_8(z_{\text{eff}} = 0.38)$	0.457	0.481	$0.481^{+0.034}_{-0.033}$	0.451	0.467	$0.455^{+0.061}_{-0.045}$
Parameter	high- $z$ NGC			high- $z$ SGC		
	MAP	Median	68% CI	MAP	Median	68% CI
$\ln(10^{10}A_s)$	2.65	2.76	$2.78^{+0.127}_{-0.193}$	3.02	3.11	$3.10^{+0.18}_{-0.17}$
$\Omega_m$	0.298	0.296	$0.297^{+0.017}_{-0.020}$	0.305	0.310	$0.307^{+0.028}_{-0.024}$
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	70.3	70.1	$70.1^{+2.2}_{-2.1}$	67.6	67.6	$67.7^{+2.8}_{-3.1}$
$\sigma_8$	0.685	0.717	$0.697^{+0.074}_{-0.044}$	0.783	0.824	$0.814^{+0.079}_{-0.066}$
$S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$	0.683	0.711	$0.692^{+0.084}_{-0.056}$	0.789	0.838	$0.824^{+0.096}_{-0.079}$
$f\sigma_8(z_{\text{eff}} = 0.61)$	0.393	0.410	$0.399^{+0.043}_{-0.027}$	0.450	0.475	$0.470^{+0.047}_{-0.040}$

measurements at  $k \gtrsim 0.2h$  Mpc $^{-1}$  are in the shot-noise-dominated regime, and therefore it is not clear whether the cosmological parameters are improved even if we include the data points at higher wave numbers. In Fig. 7, we study how the cosmological parameters are changed for different choices of  $k_{\text{max}}$ ; we consider  $k_{\text{max}} = 0.2h$ ,  $0.25h$ , and  $0.3h$  Mpc $^{-1}$ . The figure shows that the size of the credible intervals is not largely changed for the different  $k_{\text{max}}$  values, confirming the shot-noise domination in the power-spectrum measurements at  $k \gtrsim 0.2h$  Mpc $^{-1}$ . We confirm that the statistical errors of the galaxy-halo connection parameters such as the residual shot noise and the HOD parameters are indeed improved by including the information on the higher  $k$ . A closer look reveals that the results for  $k_{\text{max}} = 0.2h$  and  $0.25h$  Mpc $^{-1}$  are consistent with each other. However, the result for  $k_{\text{max}} = 0.3h$  Mpc $^{-1}$  shows a sizable shift in  $\sigma_8$ . For the validation tests using the *noiseless* mock signals in Fig. 1, we did not find this level of shift in the cosmological parameters.

As a further test of this shift, we use 50 realizations of *noisy* signals that are generated by adding random noise realizations drawn from the BOSS covariance matrix to the noiseless mock signals (the mock signals in the right panel of Fig. 1). Then we apply the same cosmology analysis pipeline to each of the mock signals to estimate the cosmological parameters. Figure 8 shows the distributions of shifts in the cosmological parameters at  $k_{\text{max}} = 0.25$  or  $0.30h$  Mpc $^{-1}$  with respect to those at  $k_{\text{max}} = 0.20h$  Mpc $^{-1}$ , for the low- $z$  and high- $z$  NGC samples which give the dominant contributions to the cosmological constraints of our full analysis. The figure shows that there is a

reasonable chance to have the parameter shifts for  $k_{\text{max}} = 0.25h$  Mpc $^{-1}$  seen from the actual BOSS data. However, the shifts in some parameters for  $k_{\text{max}} =$

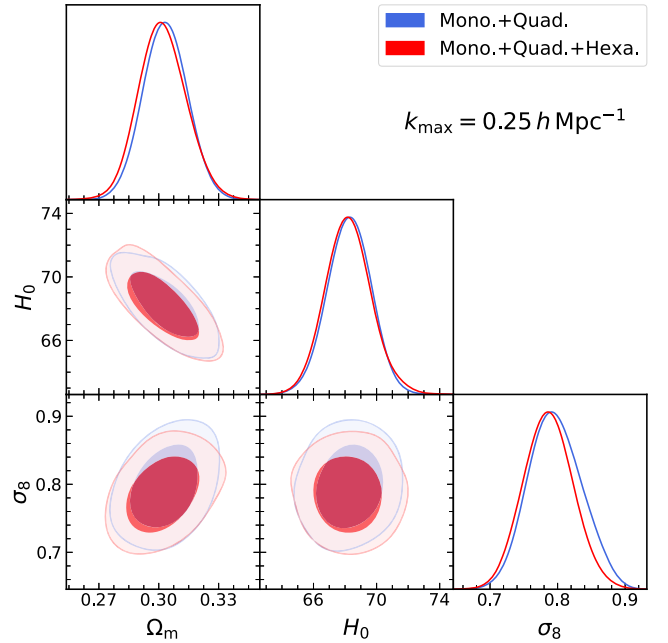


FIG. 6. The posterior distributions of cosmological parameters in our fiducial cosmology analysis for the full galaxy sample, obtained both with and without including the hexadecapole moments of the redshift-space power spectrum in the parameter inference. The red contours are the same as those in Fig. 2.



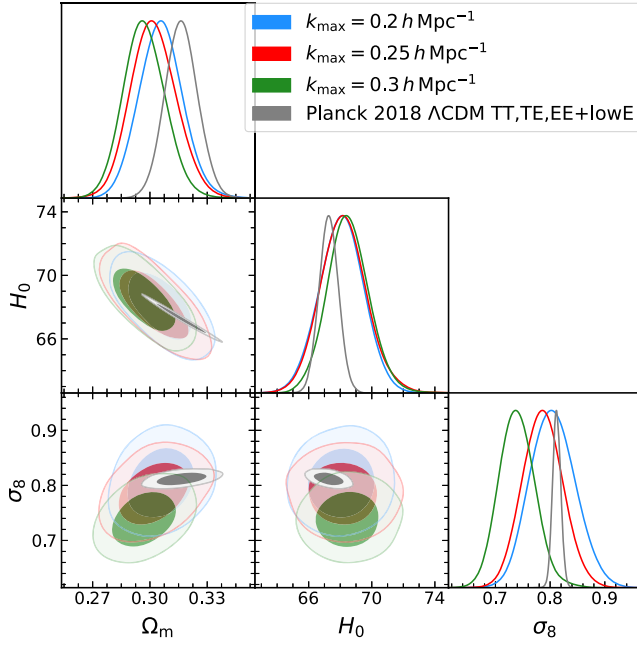


FIG. 7. Comparison of the posterior distributions obtained when including the redshift-space power-spectrum information up to a different  $k_{\max}$  in the analysis. We show the cases of  $k_{\max} = 0.2$  (blue),  $0.25$  (red), and  $0.3$  (green)  $h \text{ Mpc}^{-1}$ , and also show the results of the Planck 2018  $\Lambda\text{CDM}$  “TT, TE, EE + lowE” (gray). The cases of  $k_{\max} = 0.25h \text{ Mpc}^{-1}$  and the Planck results are identical to those in Fig. 2.

$0.3h \text{ Mpc}^{-1}$  are at the tail of the distribution of the mock results, indicating a possible hint in the systematic effects at  $k \gtrsim 0.25h \text{ Mpc}^{-1}$ —e.g., a limitation of the halo model approach at such high- $k$  scales or a residual systematic error in the power-spectrum data. Hence, our fiducial choice of  $k_{\max} = 0.25h \text{ Mpc}^{-1}$  seems reasonable against possible systematic effects.

In Appendix C, we also study possible effects of the fiber collision and the minimum wave number  $k_{\min}$  on the cosmological results. Here,  $k_{\min}$  is the minimum wave number, in that we include the power-spectrum information over  $k_{\min} \leq k \leq k_{\max}$  in the cosmology analysis. A brief summary is that these effects do not appear to cause any major systematic effect in our cosmological results.

#### D. A further test of emulation accuracy

Now, we turn to discussion on a possible uncertainty in the model predictions. As discussed in Refs. [38,40], our emulator for the redshift-space halo power spectrum is calibrated using a dataset of  $N$ -body simulations for the 101 flat  $w\text{CDM}$  models, where we use 15 realizations for the fiducial Planck cosmology and one realization for each of 100 models (more exactly, among these we use the data for 80 models as training data). Here, the 100 models are sampled using the optimal maximum-distance sliced Latin hypercube design in the six-dimensional parameter space

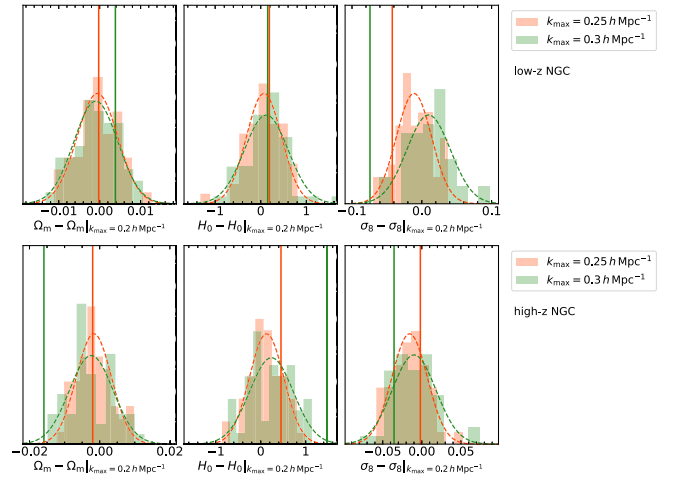


FIG. 8. The distribution of scatters in each cosmological parameter, obtained from the cosmology analysis of noisy mock power spectra for the low- $z$  and high- $z$  NGC samples, using different  $k_{\max}$  cuts; the  $x$  axis shows a shift in the mode value in the 1D posterior of each parameter at  $k_{\max} = 0.25h$  or  $0.3h \text{ Mpc}^{-1}$ , compared to that at  $k_{\max} = 0.2h \text{ Mpc}^{-1}$ . We use 50 realizations of the noisy mock spectra, and the histogram in each panel displays the distribution of parameter shifts. The vertical red and green lines denote the shift found from the cosmology analyses of the real BOSS data, shown in Fig. 7. The dashed curves denote the Gaussian distributions specified by the mean and variance of the parameter shifts among the 50 realizations.

of  $w\text{CDM}$  cosmology (see Ref. [40] for details). One might think that our emulator has a better accuracy around the Planck cosmology, which is different from the MAP model or the model preferred by our cosmology analysis of the BOSS power spectra. To test this possible uncertainty, we run a new set of  $N$ -body simulations for a model at the MAP cosmology in Table II: the model with  $\Omega_m = 0.300$ ,  $H_0 = 68.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $\sigma_8 = 0.754$ , and other cosmological parameters is set to use the values at MAP. More exactly, we run each  $N$ -body simulation with a box side length of  $2.5h^{-1} \text{ Gpc}$  and  $3000^3$  particles, and use five realizations. The total volume is about  $78(h^{-1} \text{ Gpc})^3$ , much larger than the BOSS volume [ $\sim 5.7(h^{-1} \text{ Gpc})^3$ ], so we can sufficiently reduce the sample variance effect in the simulated power spectra. Then we populate galaxies into halos using the same recipe of the galaxy-halo connection used in the Cosmology Challenge paper [37], which is different from our fiducial HOD method. Using the same covariance matrix as we used in the actual cosmology analysis of BOSS data, we perform the same cosmology analysis on the simulated power spectra. This is very similar to the validation test of our method using the simulated power spectrum used in the Cosmology Challenge [37], but this new test gives a validation of our method at the MAP model. Also note that the new set of  $N$ -body simulations employs the fixed neutrino mass of  $0.06 \text{ eV}$  as in the simulations used for the emulator

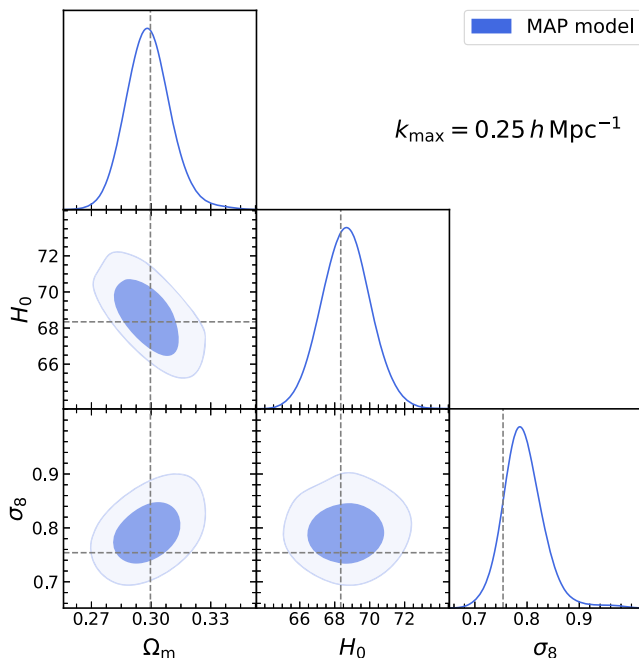


FIG. 9. The posterior distributions of the cosmological parameters using the mock catalogs that are generated from the  $N$ -body simulations for a cosmological model at MAP in Table II (see text for details). The horizontal and vertical dashed lines show the input parameter values—i.e., the cosmology at MAP. This is a similar test to Fig. 1, and the mock catalogs are generated using the same recipe of galaxy-halo connection as that in the left panel of Fig. 1.

development, while the simulations in the Cosmology Challenges assume zero neutrino mass. Hence, this test also gives a confirmation on the subtle effect of the nonzero neutrino mass, which mainly affects the transfer function of matter density fluctuations. Figure 9 shows that our method recovers each cosmological parameter accurately.

### E. Assembly bias

Another concern of the halo model approach is the impact of the “assembly bias” effect; although the simple halo model assumes that the clustering amplitudes of halos (and galaxies) are determined by halo masses, they might depend on a secondary parameter, depending on the assembly history of halos/galaxies [86,87]. Even in the presence of the assembly bias, the redshift-space distortion effect due to the peculiar velocities is unlikely to be affected by the assembly bias, because the peculiar velocities arise directly from the gravitational field [17]. To test a possible effect of the assembly bias on cosmology analysis, we use the mock catalogs of galaxies including the assembly bias effect in Ref. [17], where galaxies are populated preferentially into halos that have lower concentrations as a proxy of the assembly history (see Ref. [17] for details). The mock catalogs including the assembly bias effect are generated from the same  $N$ -body simulations as

those used in the right panel of Fig. 1; therefore, the total volume is about  $128(h^{-1} \text{ Gpc})^3$ . The mock galaxies have about 30% higher amplitudes in the real-space correlation function at large scales, compared to those of the mock galaxies without the assembly bias effect, which otherwise have the same HOD (see Fig. 12). We generate the mock signals for each of the BOSS-like galaxy samples, and we apply the same pipeline of cosmology analysis to the mock signals. Note that the assembly bias has not been detected with high significance from the BOSS galaxies (e.g., Ref. [88]).

Figure 10 shows the cosmological parameters obtained from the mock catalogs including the assembly bias effect. It can be found that the assembly bias does not cause a significant bias in the inferred cosmological parameters,  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$ . This is consistent with the Fisher forecast in the previous work [17], confirming that the BAO and RSD information are not affected by the assembly bias effect, even after marginalization over the galaxy-halo connection parameters. In other words, the cosmology analysis using the redshift-space power spectrum does not rely on the halo mass estimate. This result is contrasted with that in Ref. [76]: they found that the assembly bias causes a significant bias in the cosmological parameters, especially  $\sigma_8$  and  $\Omega_m$ , if a hypothetical joint-probe

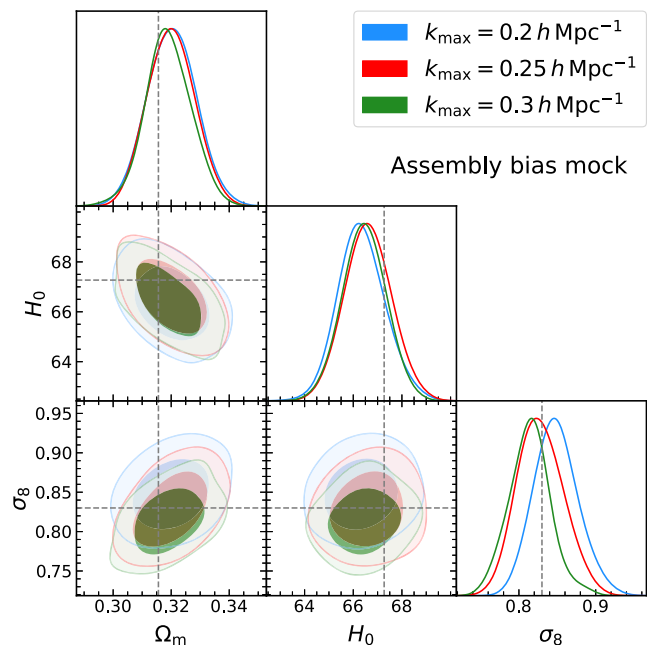


FIG. 10. The posterior distributions of  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$ , obtained when we apply our analysis pipeline to the mock power-spectrum signals that are generated from the mock galaxy catalogs including the assembly bias effect (see text for details). The horizontal and vertical dashed lines show the input parameter values. The mock galaxy catalogs have the same HOD shape as that of the mock catalogs in the right panel of Fig. 1, but they were generated by populating mock galaxies preferentially into halos that have lower concentrations, in each halo mass bin.

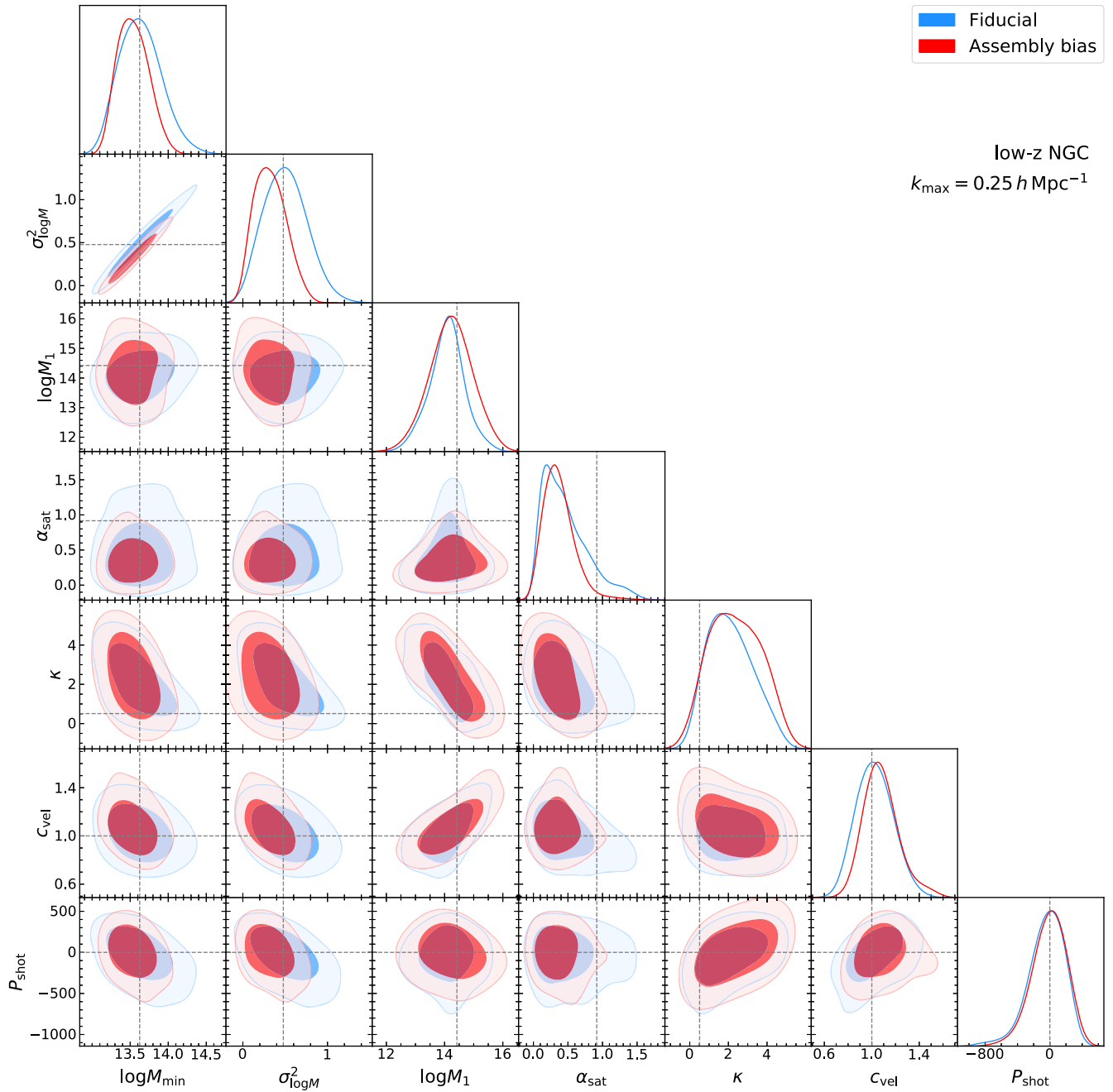


FIG. 11. The red contours show the posterior distributions of the galaxy-halo connection parameters for the low- $z$  NGC sample, obtained for the same analysis using the assembly bias mock catalog as in Fig. 10. For comparison, the blue contours show the posterior distributions obtained from the fiducial mock catalog, which are from the same analysis in the right panel of Fig. 1. The two mock catalogs are constructed using the same galaxy-halo connection model, and the horizontal and vertical dashed lines show the input parameter values.

cosmology analysis using the galaxy-galaxy weak lensing and the projected correlation function is applied to the mock signals including the assembly bias effect. In such a method, the galaxy-galaxy weak lensing plays an important role to constrain the average mass of host halos, which in turn helps determine the galaxy bias uncertainties to obtain the clustering amplitude of matter at large scales. However, the assembly bias disturbs the scaling relation of the large-scale bias amplitude with halo mass, and in turn leads to

biases in the inferred cosmological parameters. On the other hand, our method using the redshift-space power spectrum does not rely on the halo mass estimate. As can be found from Fig. 11, some of the galaxy-halo connection parameters are changed between the results for the fiducial and assembly bias mocks, suggesting that the assembly bias effect is absorbed by changes in the galaxy-halo connection parameters in our method. For example, Fig. 11 shows that the model which has a slightly smaller

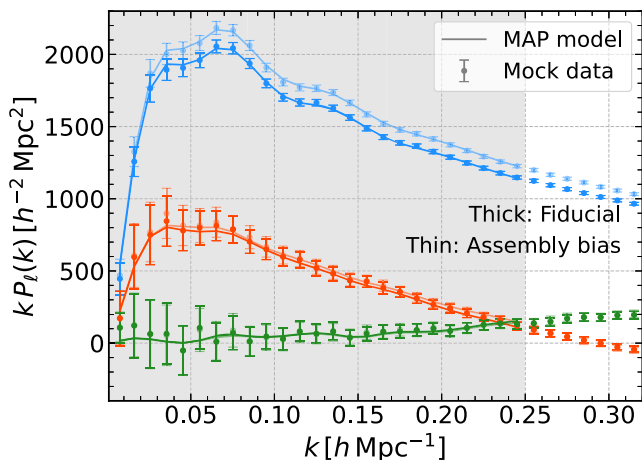


FIG. 12. Comparison of the multipole moments between the measurements from the mock catalog and the model predictions at MAP that are from the same analysis in Fig. 11. The gray shaded region is the  $k$  range on which we use the data in the analysis—i.e.,  $k_{\max} = 0.25 h \text{ Mpc}^{-1}$ .

$\sigma_{\log M}$  than the input value is favored for the assembly bias mock, which leads to a larger bias amplitude on large scales, as explicitly shown in Fig. 12. The figure clearly shows that the model well reproduces the mock measurements, especially the assembly bias effect that can be seen from a higher amplitude of the monopole moment (also see Fig. 16 in Ref. [17] for similar discussion). Hence, we conclude that our cosmological results for the BOSS galaxies are unlikely to be affected by the assembly bias, although the impact of more general assembly bias effects on cosmology inference with the redshift-space power spectrum needs to be studied further—e.g., using the results in cosmological hydrodynamical simulations (e.g., Ref. [89]).

### F. Impact of uncertainty in the galaxy-halo connection

Finally, we comment on the impact of the galaxy-halo connection parameters on the cosmological parameters. We have so far employed broad priors of these nuisance parameters. Other observables, such as galaxy-galaxy weak lensing [84,90], can be used to infer the HOD parameters. Throughout this paper, we have employed a fairly broad prior range for each of the seven halo connection parameters. In this subsection, we study how the cosmological parameter estimation can be improved if we have some knowledge on the HOD parameters.

As a working example, in Fig. 13 we show the posterior distributions of the cosmological parameters obtained from the BOSS data by fixing the galaxy-halo connection parameters to their values at MAP in our fiducial analysis (the results for Fig. 2). Therefore, this can be regarded as the best-case scenario where the galaxy-halo connection of the galaxy sample is perfectly known. The figure shows that the cosmological parameters are significantly

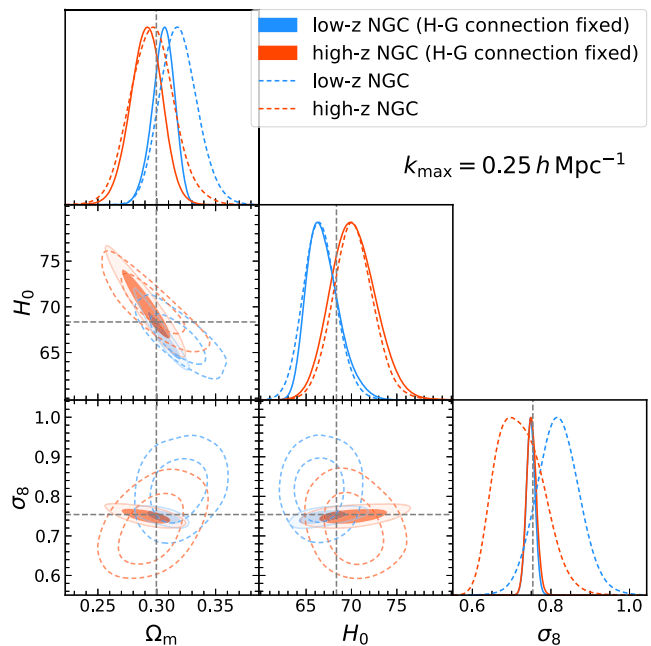


FIG. 13. The posterior distributions of the cosmological parameters, obtained from the cosmology analysis of the real BOSS data for either the low- $z$  or high- $z$  NGC sample, when fixing the seven galaxy-halo connection parameters to their values at MAP in Fig. 15. The dashed-line contours and 1D posterior distribution are the same as in Fig. 15.

improved. It is interesting to observe that the level of improvement of the parameter constraint varies with the parameters. We can see that  $\Omega_m$  and  $H_0$ , which are mostly determined by the geometrical information through the BAO feature and also partly from the spectral shape information, are not significantly improved as compared to  $\sigma_8$ , which is an amplitude-related parameter. This is telling, that the overall amplitude of the cosmological fluctuations is the hardest to interpret from observations due to the strong degeneracy with the galaxy bias uncertainty or the uncertainty in the galaxy-halo connection.

## VI. CONCLUSION

In this paper, we used an *emulator* of halo clustering statistics to estimate the cosmological parameters from the full-shape analysis of the redshift-space power spectra measured from the BOSS DR12 galaxy catalog over  $0.2 < z < 0.75$ . Combining with the HOD model, the emulator allows us to compute the redshift-space power spectra of galaxies for a given cosmological model within the flat  $\Lambda$ CDM cosmology in less than a CPU second. It enables the parameter inference of the BOSS spectra in a multidimensional parameter space (33 parameters in this study). We showed that the emulator model well reproduces the monopole, quadrupole, and hexadecapole moments of the redshift-space power spectra simultaneously for all four of the galaxy subsamples. Our method yields



stringent constraints on the cosmological parameters  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$ , even after marginalization over uncertainties in the nuisance parameters including the galaxy-halo connection parameters: more precisely,  $\Omega_m = 0.301^{+0.012}_{-0.011}$ ,  $H_0 = 68.2 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , and  $\sigma_8 = 0.786^{+0.036}_{-0.037}$ , for the mode and the 68% credible interval of the 1D posterior distribution (Fig. 2 and Table II). The cosmological parameters we obtained are consistent with those from the independent studies for the same BOSS spectra using PT-based models as the theoretical template [29,50], even though the theoretical templates are totally different. This shows the robustness of the redshift-space power-spectrum method for estimating the cosmological parameters: the BAO, AP effects, and RSD information can be robustly extracted as long as the uncertainties in the nonlinear effects and galaxy properties are marginalized over. The statistical precision for each of the main parameters  $\Omega_m$ ,  $H_0$ , and  $\sigma_8$  is also comparable with that from the PT-based methods. One might think that the halo model could allow us to use the redshift-space power spectra down to a larger  $k$  and therefore lead to a more stringent constraint on the parameters, compared to the PT-based methods that treat all the galaxy bias parameters as nuisance parameters. However, this is not the case. We think there are a few reasons for this result. First, we employed quite broad priors for each of the HOD parameters and did not include any information on the abundance of galaxies. Hence, our analysis might be considered a conservative approach. Second, the power-spectrum information at  $k \gtrsim 0.2h \text{ Mpc}^{-1}$  is in the shot-noise-dominated regime, and the cosmological parameters are not improved even if including the power-spectrum information on  $k \gtrsim 0.2h \text{ Mpc}^{-1}$  (Fig. 7). Our results are also in good agreement with the Planck 2018 results [49] for  $\Omega_m$  and  $H_0$ , but they indicate a slight tension for  $\sigma_8$  similar to those reported by the weak lensing analyses [81,91,92].

There is a promising route to improving our cosmological constraints. It is a joint-probes cosmology: although we use the redshift-space power spectrum as the data vector in this paper, there is another observable available in the BOSS footprint. The promising one is the galaxy-galaxy weak lensing, which can be obtained by cross-correlating the positions of BOSS galaxies with shapes of background galaxies, where the background galaxies can be taken from an imaging survey overlapping with some portion of the BOSS footprint. For this, the Subaru HSC and some parts of the DES and KiDS surveys have an overlapping region with the BOSS footprints, and the galaxy-galaxy weak lensing can be measured from the joint analysis of BOSS and these imaging surveys. Since the galaxy-galaxy weak lensing can measure the average mass distribution around the BOSS galaxies, it helps observationally disentangle the galaxy bias uncertainty or yields stringent constraints on the HOD parameters in the halo model picture. In fact, Ref. [56]

combines the galaxy-galaxy weak lensing, measured from the HSC data of a small area coverage of 140 square degrees, with the *projected* correlation function of BOSS galaxies in the cosmology analysis and then obtained at the accuracy of  $\sigma(S_8) \simeq 0.05$ , compared to our constraint of  $\sigma(S_8) \sim 0.04$ , although  $S_8$  is not a parameter to which the redshift-space power spectrum is the most sensitive. The galaxy-galaxy weak lensing arises mainly from Fourier modes in the two-dimensional space perpendicular to the line-of-sight direction, and it was shown that it carries almost independent information from the redshift-space power spectrum that arises from Fourier modes in the three-dimensional space [93]. Hence, combining the redshift-space power spectrum with the galaxy-galaxy weak lensing helps disentangle the degeneracy between the galaxy bias uncertainty (the galaxy-halo connection) and the cosmological parameters, leading to an improved estimation of the cosmological parameters (see Fig. 13 for a possible improvement in the best-case scenario). To do this, our emulator-based method easily enables us to jointly combine the two observables in the same halo model framework for parameter inference. This is definitely an interesting direction, and will be our future work.

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*Note added.*—Recently, Ref. [29] performed a full-shape cosmology analysis of the BOSS power spectrum using the EFTofLSS method. The authors, Stephen Chen and Martin White, kindly informed us of the updated measurements of the BOSS power spectrum done in Ref. [51]. We would like to thank them for useful discussion.

### APPENDIX A: POSTERIOR DISTRIBUTIONS OF THE GALAXY-HALO CONNECTION PARAMETERS IN THE VALIDATION TEST

Figure 14 shows the posterior distributions of the galaxy-halo connection parameters, obtained from the cosmology analysis of the mock data vector that is generated from the mock catalogs of BOSS-like galaxies. The mock galaxy

catalog is the same as that used in the right panel of Fig. 1. The figure shows that some of the galaxy-halo connection parameters are not necessarily well recovered, although the cosmological parameters are fairly well recovered, as shown in Fig. 1. The size of the posterior contours for the galaxy-halo connection parameters indeed shrinks with the inclusion of the power-spectrum information on the higher  $k$ .

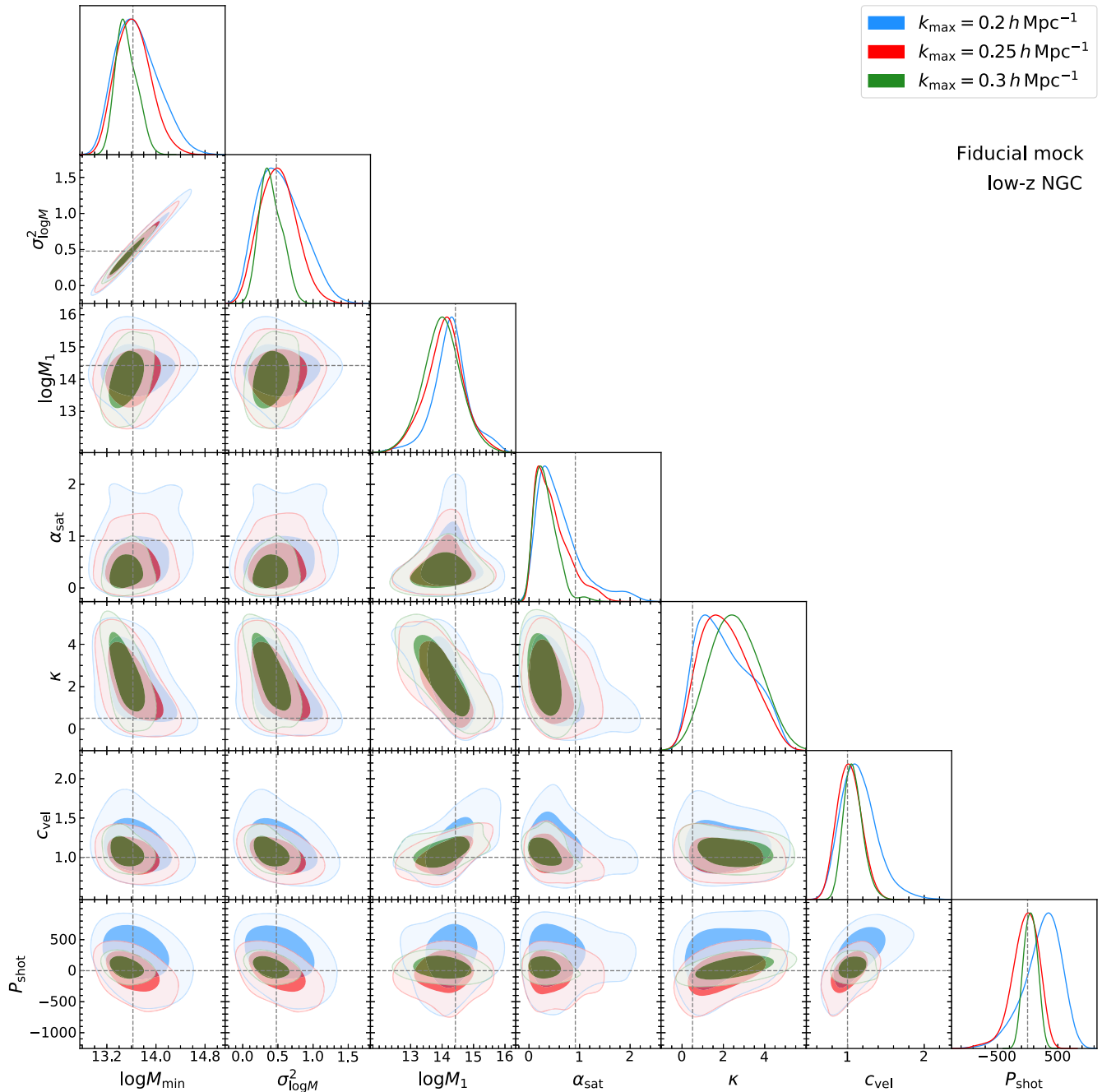


FIG. 14. The posterior distributions of the galaxy-halo connection parameters, for the low- $z$  NGC sample as an example, obtained from the combined analysis using the mock catalogs that are generated using the same HOD model as in our theoretical template (the right panel of Fig. 1). The dashed lines in each plot denote the input value of each parameter that is used when generating the mock galaxy catalogs.

**APPENDIX B: POSTERIOR DISTRIBUTIONS IN FULL PARAMETER SPACE**

For comprehensiveness of our discussion, in Fig. 15 we show the posterior distributions in each 2D subspace of the full parameters for the  $\Lambda$ CDM model for each galaxy sample, based on our baseline analysis setup (Table I).

**APPENDIX C: TESTS OF THE FIBER COLLISION EFFECT AND THE MINIMUM WAVE NUMBER  $k_{\min}$**

Next, we investigate the impact of the fiber collision on the cosmological parameter inference from the redshift-space galaxy power spectrum. The fiber collision, which

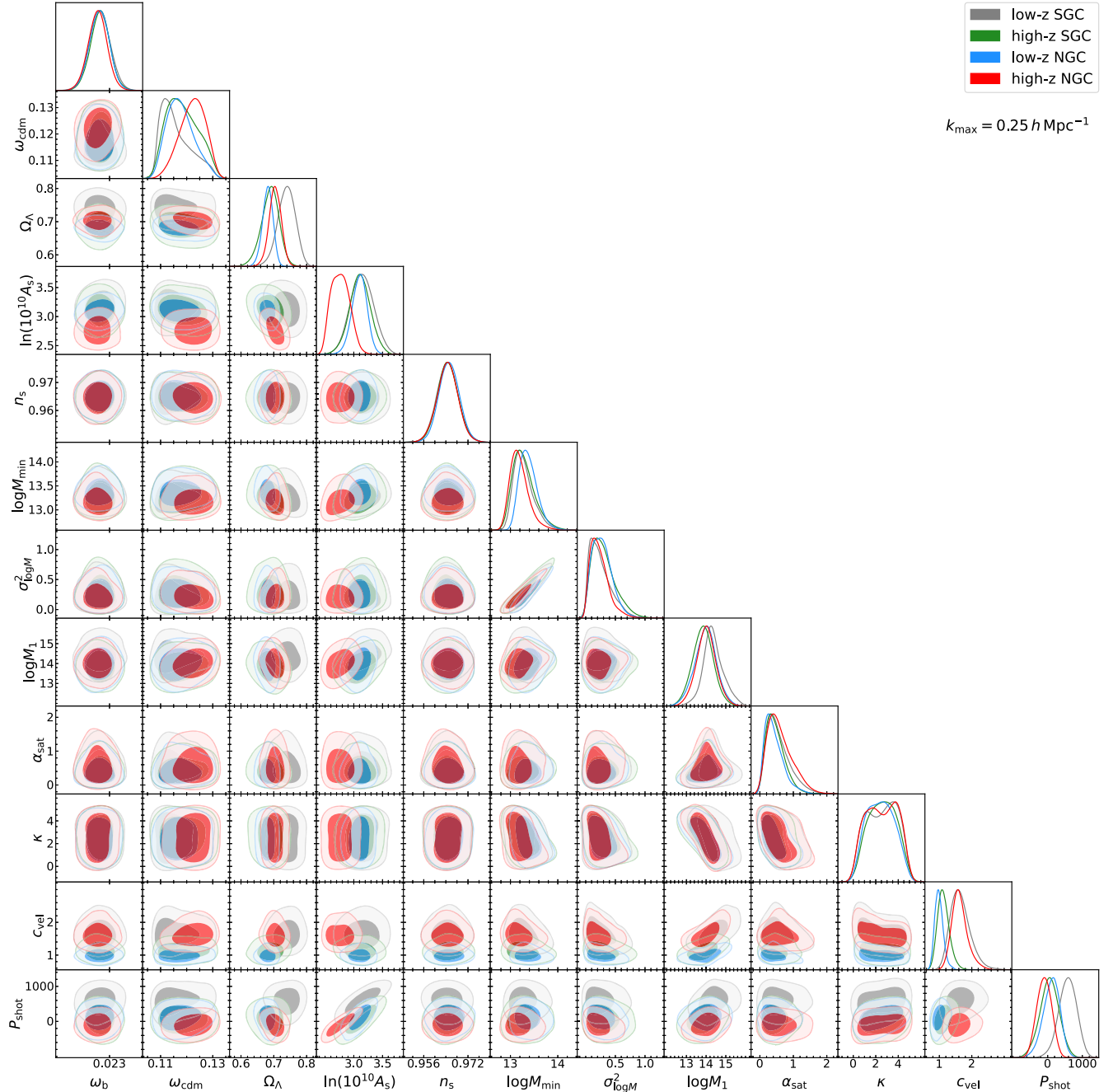


FIG. 15. The posterior distributions in each 2D subspace of the full parameters for each of the four galaxy samples, for the cosmology analysis in Fig. 2: the low- $z$  NGC, low- $z$  SGC, high- $z$  NGC, and high- $z$  SGC samples, respectively. The posterior distributions are from the joint parameter inference of these parameters (33 parameters in total, as given in Table I): five cosmological parameters (while we impose tight Gaussian priors to  $\omega_b$  and  $n_s$ ), and each sample is characterized by seven nuisance parameters (five HOD parameters, the virial velocity parameter, and the residual shot noise parameter).

occurs due to the inability of the two adjacent optical fibers to be closer than some finite separation angle, is a potential systematic effect on the cosmological parameter inference. The likelihood of the fiber collision depends on the number density of target galaxies on the celestial sphere, and it leads to an anisotropic effect in the measured power spectrum. Reference [94] shows that the correction to the fiber collision effect on the galaxy power spectrum depends on the true power spectrum itself, and it suggests the way for the correction. In this work, instead of implementing the correction in the model prediction, we examine the extent to which the fiber collisions affect the cosmology inference.

Figure 16 shows a comparison of the parameter inference between the cases with and without the fiber collisions. To investigate the influence of the fiber collisions on the cosmological parameter inference, we use the PATCHY mocks which have the fiber collision weights. The fiber collision weights in the PATCHY mocks are assigned following Ref. [53], which reflects the nearest neighbor (NN) method. In this figure, we see that there are only marginal differences in the parameter posteriors between the case with the fiber collisions corrected by the NN

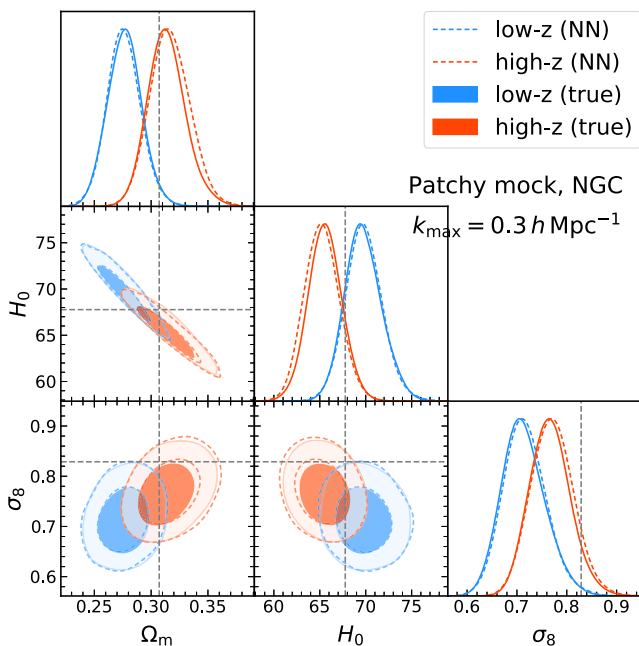


FIG. 16. The comparison of the cosmological parameter inferences between the PATCHY mock power spectra with and without the fiber collisions. We show the cases of the low- $z$  (blue) and high- $z$  (red) NGCs and  $k_{\max} = 0.3h \text{ Mpc}^{-1}$ . The empty dashed-line contours are the results for the PATCHY mocks where we include the fiber collision weights. The filled solid-line contours are those for the same mocks where we assume all of the fiber collision weights are unity—i.e., no fiber collisions. The gray horizontal and vertical dashed lines indicate the input cosmological parameter values used in the simulations from which the PATCHY mocks are created.

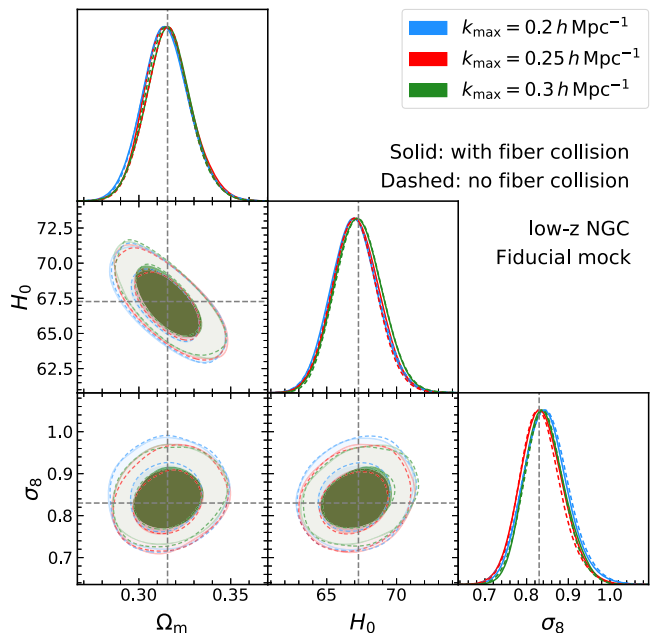


FIG. 17. The comparison of the cosmological parameter inferences between the fiducial mock power spectrum with and without the fiber collision effect. For mock signals with the fiber collisions, we add the fiber collision effect estimated by Ref. [94] (see their Fig. 3) to the power-spectrum monopole and quadrupole of the fiducial mock signals.

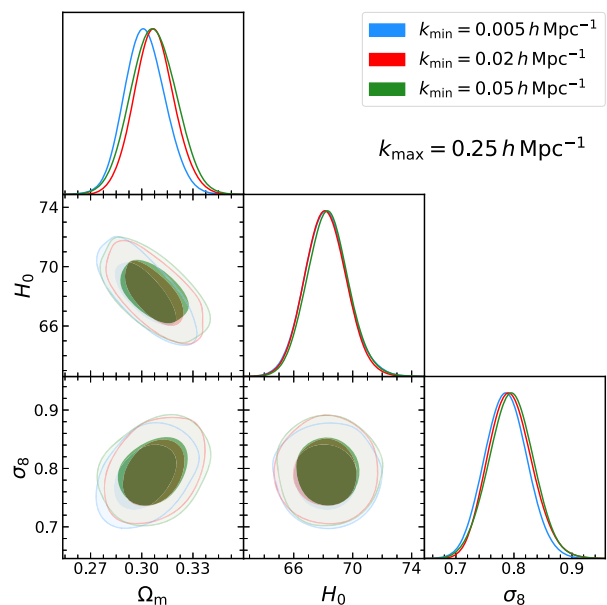


FIG. 18. The dependence of the cosmological parameter constraints on the minimum wave number  $k_{\min}$  used in the analysis. We test the cases of  $k_{\min} = 0.005h$  (our fiducial setting, blue),  $0.02h$  (red), and  $0.05h \text{ Mpc}^{-1}$  (green), while fixing  $k_{\max} = 0.25h \text{ Mpc}^{-1}$ .



weights (empty, dashed line contours) and that of the true power spectrum with no fiber collisions (filled, solid line contours), for both the low- $z$  and high- $z$  NGCs, up to  $k_{\max} = 0.3h \text{ Mpc}^{-1}$ .

Figure 17 shows another test based on mock power spectra. We quote the shifts of the power spectrum due to the fiber collisions [95] in the NSERIES mocks shown in the left panel of Fig. 3 of Ref. [94], and add them to our fiducial mock signals after spline interpolation to reduce the noise contributions. This mock fiber collision effect causes almost no change to the posterior distribution of the cosmological parameters, even in the case of  $k_{\max} = 0.3h \text{ Mpc}^{-1}$ . From these studies, we conclude that

the fiber collision effect has no significant impact on the cosmology analysis. Therefore, we conclude that the systematic shift in the  $\sigma_8$  posterior in our real data analysis when we increase  $k_{\max}$  (shown in Fig. 7) is not due to the fiber collisions.

We mention the influence of the minimum wave number  $k_{\min}$  of the power-spectrum signals we use in the cosmological inference. Figure 18 shows the parameter inference results for different values of  $k_{\min} = 0.005h$ ,  $0.02h$ , and  $0.05h \text{ Mpc}^{-1}$ , while we keep  $k_{\max} = 0.25h \text{ Mpc}^{-1}$ . Here,  $k_{\min} = 0.005h \text{ Mpc}^{-1}$  is our default choice throughout this paper. It shows that the choice of  $k_{\min}$  has no significant effect on the cosmological parameter inference.

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