Cascade appearance signatures of sterile neutrinos at 1–100 TeV

B. R. Smithers^(D),^{1,*} B. J. P. Jones,¹ C. A. Argüelles^(D),² J. M. Conrad,³ and A. Diaz³

¹Department of Physics, University of Texas at Arlington, Arlington, Texas 76019, USA

²Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

³Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA

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Neutrino telescopes provide strong sensitivity to sterile-neutrino oscillations through matter effects occurring in the few TeV energy range for eV²-scale neutrino mass-squared splittings. Prior searches have focused on ν_{μ} disappearance, which has a particularly strong sensitivity to the mixing angle θ_{24} via $\nu_{\mu} \rightarrow \nu_s$ transitions. Nowadays, the $\nu_{\mu} \rightarrow \nu_e$ and $\nu_{\mu} \rightarrow \nu_{\tau}$ appearance channels have been considered less promising at neutrino telescopes, due in part to the much smaller target volume for cascades relative to tracks. This work explores the detectability of these signatures at neutrino telescopes given present constraints on sterile-neutrino mixing, and as an example, forecasts the sensitivity of the IceCube Neutrino Observatory to the mixing angles θ_{14} , θ_{24} , and θ_{34} in the 3 + 1 sterile-neutrino model using the cascade channel with 10 yr of data. We find that ν_{τ} appearance signatures consistent with the existing IceCube ν_{μ} disappearance best-fit point are discoverable for values of θ_{34} consistent with world constraints, and that the sterile-neutrino parameters favored by the BEST and gallium anomalies are expected to be testable at the 95% confidence level.

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I. INTRODUCTION

The three-mass and three active-flavor neutrino paradigm has been well studied [1–6]. However, several anomalies persist at short baselines, including in $\nu_{\mu} \rightarrow \nu_{e}$ appearance in decay-in-flight [7] and decay-at-rest [8] beams and $\nu_{e} \rightarrow \nu_{e}$ disappearance at reactors [9,10] and with ⁷¹Ga electron capture sources [11,12]. These anomalies have been attributed to possible oscillations of unknown neutrinos with mass-squared differences in the range of $\Delta m^{2} \sim 0.1-10 \text{ eV}^{2}$ [13]. Such an additional neutrino flavor state must be nonweakly interacting, or "sterile," to be consistent with observed decay widths of the Z boson [5]; the simplest such model is known as the "3 + 1" light sterile-neutrino model in which a single sterile neutrino is added.

There have been interesting recent developments for the 3 + 1 model. The BEST experiment appears to validate the anomalous electron neutrino disappearance signature of the previous gallium anomalies with a new level of statistical significance and experimental precision [14].

^{*}Corresponding author. benjamin.smithers@mavs.uta.edu The Neutrino-4 experiment claims evidence of short-baseline oscillations in the $\bar{\nu}_e$ disappearance channel with $\Delta m^2 \sim 7.3 \text{ eV}^2$ at the 2.9 σ level. Meanwhile results from the MicroBooNE [15–17] experiment challenge the interpretation that the MiniBooNE low-energy excess [7] is due entirely to the electron neutrino by placing a constraint on the sterile-neutrino interpretation of the excess, though the impact of this observation on the 3 + 1 model is just beginning to be assessed [18,19]. Continued exploration of sterile-neutrino mixing in all channels and all energy ranges thus remains strongly motivated [20].

The addition of a fourth neutrino mass and flavor eigenstate expands the unitary mixing matrix to four dimensions. The four-neutrino oscillation model becomes an extension of the three-neutrino model with three additional mixing angles θ_{14} , θ_{24} , and θ_{34} , and two new *CP*-violating phases δ_{14} and δ_{24} . These three new mixing angles parametrize the amplitude of oscillations between the three active states and the one sterile state, and lead to additional short-baseline vacuumlike oscillations as well as novel effects in the presence of matter [21–25]. In this work we consider *CP*-violating models with all *CP*-violating phases set to zero.

Of particular interest to neutrino telescopes, matter effects can result in the near complete disappearance of TeV-scale muon antineutrinos passing through Earth's core for a sterile neutrino with eV-scale mass-squared differences [26–32]. This signature of matter-enhanced resonant disappearance has been targeted by the IceCube

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Neutrino Observatory [33,34], leading to one of the most sensitive ν_{μ} disappearance analyses to date. The result of the analysis was a closed 90% contour with a best-fit point at $\sin^2 2\theta_{24} \sim 0.1$ and $\Delta m_{41}^2 = 4.5 \text{ eV}^2$, under the conservative assumption (for the ν_{μ} disappearance channel) that $\theta_{34} = \theta_{14} = 0$. In addition to being a strong refutation, lower mass solutions consistent with the LSND [8] and MiniBooNE anomalies and constraints around 1 eV² [13,35–39], a possible interpretation of this result is as a statistically weak hint of a disappearance signature around $\Delta m_{41}^2 \sim 4.5 \text{ eV}^2$. Further exploration of this region of parameter space in other channels at neutrino telescopes is therefore strongly motivated.

In this work, we explore the potential of sterile-neutrino searches at gigaton-scale neutrino telescopes using matterenhanced ν_{τ} and ν_{e} appearance signatures that occur when either θ_{34} or θ_{14} are nonzero [40]. We will show that ν_{τ} appearance of considerable strength may accompany ν_{μ} disappearance within the IceCube allowed region for Δm_{41}^2 and θ_{24} , for values of θ_{34} that remain consistent with world datasets. We will also demonstrate that these signatures can be probed using IceCube's public data samples. Finally, we will also explore possible sensitivity to ν_{e} appearance at levels consistent with the gallium and BEST anomalies.

The IceCube Neutrino Observatory is described at length in Ref. [41]. Briefly, the detector is a cubic-kilometer Cherenkov neutrino observatory 1.5 km deep in the Antarctic ice [41]. There, 5160 photomultiplier tubes encased within glass pressure vessels, or "digital optical modules" (DOMs) [42] detect Cherenkov emission from charged particles traversing the ice. The DOMs are arranged vertically with a 17 m spacing into 79 strings, which themselves are aligned into a hexagonal lattice with a 125 m spacing. An additional, more densely instrumented subdetector called DeepCore exists toward the bottom center of the main detector [43]. The observatory has been running for over a decade and has accumulated large numbers of ν_u charged-current (CC) interactions which make depositions of light that make long signatures in the detector called tracks, and neutral current, electron neutrino, and tau neutrino events which deposit light in bloblike shapes called cascades. These event topologies are elaborated upon in Sec. II.

IceCube analyses targeting ν_{μ} disappearance are considered tracklike only, since the only available signature under the previous mixing assumptions $\theta_{14} = \theta_{34} = 0$ is $\nu_{\mu} \rightarrow \nu_s$ disappearance. In similar models with both non-zero θ_{24} and θ_{34} , however, resonant $\nu_{\mu} \rightarrow \nu_{\tau}$ oscillations lead to a strong appearance signature of ν_{τ} as shown in Fig. 1. While some of the ν_{τ} will produce τ^{\pm} that decay leptonically to produce additional tracks, dampening the ν_{μ} disappearance signature, most charged-current ν_{τ} and $\bar{\nu}_{\tau}$ interactions will produce localized energy deposits that will be reconstructed as single cascades at these energies [44]. As in the $\nu_{\mu} \rightarrow \nu_s$ channel, the most striking feature of the



FIG. 1. Transition probabilities $P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{\alpha})$ for $\bar{\nu}_{e}$ (top panel), $\bar{\nu}_{\mu}$ (middle panel), and $\bar{\nu}_{\tau}$ (bottom panel) for a sterile-neutrino flux with $\sin^{2}(2\theta_{24}) = 0.1$, $\sin^{2}(2\theta_{34}) = 0.2$, and $\Delta m_{41}^{2} = 4.5 \text{ eV}^{2}$. A dashed black line is used to denote the outer core-mantle boundary, and a solid black line denotes the inner-outer core boundary. These probabilities are shown as a function of the neutrino's energy (E_{ν}^{true}) and the cosine of the angle measured from an upward direction, toward the neutrino's origin.

signature is a resonant flavor oscillation for Earth-corecrossing antineutrinos at a specific energy, proportional to the sterile neutrino Δm_{41}^2 value. Since this matter effect occurs because of an interference between the vacuum oscillation phase and the matter-driven phase, the latter changing sign between neutrinos and antineutrinos, for small mixing angles the resonance is only present in antineutrinos, given a heavier sterile neutrino. The



FIG. 2. Appearance probabilities for $P(\nu_{\mu} \rightarrow \nu_{\tau})$ (top panel) and $P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{\tau})$ (bottom panel) for a sterile-neutrino flux with $\sin^2(2\theta_{24}) = 0.1$, $\sin^2(2\theta_{34}) = 0.19$, and $\Delta m_{41}^2 = 4.5 \text{ eV}^2$.

appearance probabilities for $\nu_{\mu} \rightarrow \nu_{\tau}$ and $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{\tau}$ are shown separately in Fig. 2.

For zero θ_{24} very little signal is expected since the muon neutrinos, which dominate the flux at IceCube, cease to mix with the heavier mass state. As a consequence there will be a negligible ν_{τ} appearance, regardless of the value of θ_{34} . However, recent IceCube results favor a nonzero value for $\sin^2(2\theta_{24})$ of around 0.1, and assuming ν_{μ}/ν_4 mixing at this level, the observable ν_{τ} appearance will depend strongly on the value of θ_{34} . At the smallest values of θ_{34} ($\theta_{34} \lesssim 0.1$), $\nu_{\mu} \rightarrow \nu_{s}$ oscillations dominate over the $\nu_{\mu} \rightarrow \nu_{\tau}$ appearance from standard oscillations, and ν_{μ} disappearance is the only visible signature. For values of θ_{34} larger than this threshold, the $\nu_{\mu} \rightarrow \nu_{\tau}$ oscillations begin to dominate and ν_{τ} appearance manifests, leading to the appearance signature shown in Fig. 1 (bottom panel). Increasing Δm_{41}^2 has the effect of broadening the appearance signature until $\sim 10 \text{ eV}^2$, after which raising the mass-squared splitting has only a marginal effect. Increasing θ_{24} while reducing θ_{34} proportionately leaves the appearance signatures mostly unchanged while diminishing the disappearance amplitude.

In addition, the effects of nonzero mixing angle θ_{14} can also be considered, having the consequence of introducing similar appearance signatures into the ν_e appearance channel [45]. For practical purposes ν_e and ν_{τ} chargedcurrent events are indistinguishable at these energies in IceCube. Notably, neutrino telescopes are the only experiments in the world with substantial sensitivity to a sterile neutrino-induced ν_{τ} appearance, so such direct constraints on the θ_{34} parameter are specific to these programs. Constraints on θ_{14} , on the other hand, may directly relate to anomalies in $\nu_{\mu} \rightarrow \nu_{e}$ and ν_{e} disappearance. As we will show, constraining the ν_{e} appearance signature at IceCube under the nonzero presently favored value of θ_{24} from ν_{μ} disappearance have direct implications for the BEST anomaly and the associated reactor- $\bar{\nu}$ anomaly.

This rich phenomenology motivates multi-mixing-angle and multichannel searches to fully explore sterile-neutrino mixing around the matter resonance at neutrino telescopes. In this work, we explore this space of mixing parameters by using publicly available tools, effective areas, and Monte Carlo simulation to estimate IceCube's sensitivity to θ_{24} , θ_{34} , and Δm_{41}^2 through cascades.

II. NEUTRINO ENERGY DEPOSITION

Large-volume neutrino telescopes typically are sensitive in the TeV to PeV energies; here, deep-inelastic scattering (DIS) [46] and the recently observed [47] Glashowresonance [48] interactions dominate. The detected neutrino interaction events fall into two morphological categories: tracks and cascades.

CC ν_{μ} DIS events result in muons at energies where radiative processes dominate energy loss rates. As a result, energy losses are stochastically driven and the produced muons travel for kilometers. The results are threefold: muons are difficult to fully contain in neutrino telescopes, muon energies are poorly correlated with progenitor muonneutrino energies, and muons' long travel distance can allow for reconstructing their direction to within 1° [49]. These events are called *tracks* [50].

All neutral-current DIS events result in a hadronic shower spreading around the interaction point and a secondary neutrino invisibly carrying away a proportion of the parent neutrino's energy. These events are often contained with a spherical topology. ν_e -CC interactions develop similarly to neutral-current interactions, but repeated inverse Compton scattering of the produced electron initiates an electromagnetic shower superimposed over the hadronic shower. Thus, nearly all of the interacting neutrino's energy is observable as detectable light. These events are called *cascades*. Such events tend to be well contained, permitting an efficient energy reconstruction, although they suffer from poor angular reconstruction [50].

The evolution of a ν_{τ} -CC interaction is highly dependent on the energies involved. A tau is produced simultaneously with a hadronic cascade propagating around the interaction point, and then the tau decays. Due to their large mass, taus have a short lifetime and a decay length of ~50 m per PeV of tau energy [44]. From the tau branching ratios [6], 17.37% of the charged tau decays evolve as muon tracks, while the remainder of the decays evolve as electromagnetic or hadronic cascades. Only at neutrino energies above 60 TeV do ν_{τ} -CC interactions yield events with distinguishable primary and secondary cascades [44].

Several distinct event samples have been developed to study these different types of events in IceCube. The highenergy starting event sample [51], for example, was developed to study both taus and high-energy neutrinos that are likely astrophysical in origin. There exist other event samples optimized for higher event rates at lower energies, such as the medium-energy starting events [52], and the 5-yr inelasticity sample [53]. There are also samples optimized for muon purity, such as the 8-yr atmospheric muon sample [34] and others optimized for accurate energy resolution such as the 6-yr cascade sample [54]. This work will consider the cascade event selection described in [55] and the track event selection previously used in IceCube sterile-neutrino searches [56].

III. NEUTRINO FLUXES

We calculate the expected event rates in IceCube exclusively using publicly available data on effective areas and publicly available Monte Carlo simulation samples. By studying the expected event rates in both track and cascade channels, we are able to estimate IceCube's sensitivities to sterile-neutrino parameters given the existing 10-yr dataset. At sensitive energies there are two relevant neutrino populations whose flux must be modeled: atmospheric and astrophysical neutrinos.

Predicting atmospheric neutrino event rates requires a progenitor cosmic-ray flux, simulation of the resulting air showers, propagation of the shower-born neutrinos through Earth, and convolution of these fluxes with effective areas for a given sample selection to yield a final predicted event rate. For this work, we use the MCEq cascade equation solver [57] with the three-population Hillas-Gaisser 2012 H3a cosmic-ray-flux model [58] and using the SYBILL 2.3c hadronic interaction model [59] to simulate air showers. The polygonato model for the cosmic-ray flux [60] and the QGSJET-II-04 model for hadronic interactions [61] were also found to produce similar results for this analysis.

These fluxes are then propagated through Earth using the Simple Quantum Integro-Differential Solver for neutrino oscillations (nuSQuIDS) [62–64]. We have configured nuSQuIDS to propagate the fluxes according to a spherically symmetric preliminary reference Earth model [65] where it accounts for both coherent and noncoherent interactions relevant at these energies [48,66] as well as tau-neutrino regeneration [67]. For this work, we use the cross sections calculated in Ref. [68]. We fix the three-neutrino oscillation parameters to their global best-fit values [69].

Astrophysical neutrino event rates are calculated similarly, although the neutrino flux prior to propagation through Earth instead is expected to follow a power-law spectrum as a function of neutrino energy E_{ν} ,

$$\Phi_{\text{astr},\alpha}(E_{\nu}) = r_{\alpha} \Phi_0 \left(\frac{E_{\nu}}{E_0}\right)^{-\gamma},\tag{1}$$

normalized at $E_0 = 100 \text{ TeV}$ and with $\Phi_0 = 2.85 \times 10^{-18} \text{ [GeV} \cdot \text{cm}^2 \cdot \text{sr} \cdot \text{s}]^{-1}$, a spectral index of $\gamma = 2.39$ [34], and a flavor ratio r_{α} for $\alpha \in (e, \mu, \tau)$. The flux is assumed isotropic and to have a $\nu:\bar{\nu}$ ratio of 1:1. Astrophysical neutrinos are assumed to be created with regard to the pion decay–induced flavor ratio of 1:2:0 [70,71]; these are then propagated through vacuum over large energy-baseline ratios, recovering the expected $\frac{1}{3}:\frac{1}{3}:\frac{1}{3}$ flavor ratio at Earth for the three-neutrino model [72]. The same is done for sterile-neutrino hypotheses to predict expected four-flavor flavor ratios [73].

A. Cascade rates

Total cascade event rates in IceCube are calculated binwise, linearly in $\log(E^{\text{true}})$ and $\cos \theta_z^{\text{true}}$, by integrating over a product of flux and effective area A_{eff} in each bin (i,j), summing for each neutrino species (α), and multiplying by lifetime τ . This is shown below in Eq. (2):

$$N_{i,j}^{\text{evt}} = 2\pi\tau \sum_{\alpha} \int_{E_i}^{E_{i+1}} dE_{\nu}^{\text{true}} \int_{\cos\theta_j}^{\cos\theta_{j+1}} d(\cos\theta_z^{\text{true}}) \\ \times \Phi_{\alpha}(E_{\nu}^{\text{true}}, \cos\theta_z) A_{\text{eff},\alpha}(E_{\nu}^{\text{true}}, \cos\theta_z^{\text{true}}).$$
(2)

The effective areas used are publicly available and are determined from the gradient boosted decision tree method event selection developed and available in Ref. [55]. The expected binwise event counts N^{mn} at reconstructed energy $(E_{\nu}^{\text{reco}})_m$ and zenith $(\cos \theta_z^{\text{reco}})_n$ follow from smearing from these expected true values by a bin-to-bin reconstruction probability P_{mn}^{ij} ,

$$N_{mn}^{\text{reco}} = N_{ii}^{\text{true}} P_{ijmn},\tag{3}$$

calculated according to published reconstruction resolutions [50,74]. Angular error in reconstruction is nominalized with a Kent distribution [75] over azimuths to extract the zenith error. The width of the Kent distribution, θ_z^{err} , is energy dependent according to the 50% angular error presented in Ref. [74], so we solve for the parameter (κ) using

$$-\int_{1}^{\cos\theta_{z}^{\text{err}}(E_{\nu}^{\text{true}})}\frac{\kappa}{2\sinh\kappa}e^{\kappa\cos\theta}d\cos\theta = 0.50 \qquad (4)$$

at each analysis bin.

The expected number of events for 10 yr of lifetime is shown at the bottom of Fig. 3, and one-dimensional histograms of the number of events are shown in Fig. 4.



FIG. 3. Expected number of through-going tracks (top panel) and cascades (bottom panel) for 10 yr of lifetime using the Hillas Gaisser H3a cosmic-ray-flux model, the SYBILL 2.3c interaction model, and the event selection described in Ref. [55].

B. Track rates

In order to calculate the expected track event rate in IceCube, we use a Monte Carlo set published as part of a previous 1-yr search for sterile neutrinos [56]. We use the same energy and cosine-zenith binning used in Sec. III A, and similarly scale the data to 10 yr of lifetime. The expected number of tracks for 10 yr of lifetime is shown in Fig. 3 (top panel).

IV. SYSTEMATIC UNCERTAINTIES

A detailed treatment of IceCube's sources of systematic uncertainties would be prohibitively complex and would require proprietary IceCube tools, so a truly rigorous sensitivity calculation for each channel can only be provided by the IceCube Collaboration. Nevertheless, to estimate the expected impact of such effects we use publicly available data from Ref. [34] to apply a simplified treatment of the expected scale of systematic uncertainties. Dominant sources of systematic uncertainty are expected to derive from the shape and normalization of the atmospheric and astrophysical neutrino fluxes and the properties of the



FIG. 4. Expected number of cascades for 10 yr of lifetime using the Hillas Gaisser H3a cosmic-ray-flux model, the SYBILL 2.3c interaction model, and the event selection described in Ref. [55] for a three-neutrino model (salmon) and a 3 + 1 sterile neutrino model (black line) with $\sin^2(2\theta_{24}) = 0.1$, $\sin^2(2\theta_{34}) = 0.2$, and $\Delta m_{41}^2 = 4.5 \text{ eV}^2$. The number of events is summed over zenith angles (top panel) and energy (bottom panel) bins. Note that the oscillation signature is a correlated function of both variables, so it appears very indistinctly in these projections.

South Pole ice as in Ref. [34]. Other sources of uncertainty, such as the efficiencies of IceCube's DOMs, neutrino, and antineutrino interaction cross sections, were not used in this preliminary analysis since they are subleading effects.

Absorption and scattering of light in the ice are treated using the effective gradient approach developed in Ref. [76] and used by Ref. [33]. Uncertainties in the depth dependence of the absorption and scattering of South Pole ice leads to uncertainties in energy reconstruction, and therefore an uncertainty in the energy spectrum of expected event rates.

The 1σ deviations to the cosmic-ray flux are considered as in Ref. [34]. These deviations calculate the expected 1σ shifts in the expected atmospheric neutrino rates. Similarly, we perturb the slope of the astrophysical neutrino flux to determine variances in expected astrophysical neutrino rates. Per-bin uncertainties are then summed in quadrature to calculate a net systematic uncertainty.



FIG. 5. 2 d.o.f., 90% C.L. sensitivity to $|U_{24}|^2$ and Δm_{41}^2 with $\theta_{34} = 0.0$. These results closely reproduce those of Ref. [34].

Overall normalization of fluxes is treated as a nuisance parameter and allowed to float freely, such that we are studying energy and zenith shape and flavor ratio effects only, and not the absolute neutrino rate. We fit to the normalization before calculating the log-likelihood at each physics point. As will be described below, this simplified prescription has been tested by regenerating IceCube's sensitivity to θ_{24} via ν_{μ} disappearance, and a similar median sensitivity to the published IceCube analysis is obtained (shown in Fig. 5). Although both imperfect and incomplete, we believe that this prescription captures the majority of the important effects of the relevant systematic uncertainties for present purposes.

V. PREDICTED SENSITIVITIES

A binned-likelihood approach is used in calculating the log-likelihood for the expected numbers of events for each set of physical parameters. The test statistic at each point in parameter space is calculated according to

$$TS = -2\Delta LLH = -2(\ln L - \ln L_{\max})$$
(5)

after removing the overall normalization effect by fitting the no-sterile-neutrino flux to the parameter point of interest and adjusting the hypothesis normalization accordingly. We have performed likelihood based analyses in three samples: tracks only, cascades only, and tracks and cascades combined.

A. Tracks-only sensitivity to ν_{μ} disappearance

We first perform likelihood analysis for IceCube's track sample: calculating the sensitivity to θ_{24} and Δm_{41}^2 , using the procedure described in Sec. III to predict the expected number of tracks in only 8 yr of lifetime. These results are shown in Fig. 5, which accurately reproduce the sensitivities presented in Ref. [56]. We have chosen this point of





FIG. 6. Ratio of expected tracks (top panel) and cascades (bottom panel) for a sterile-neutrino model with $\sin^2(2\theta_{24}) = 0.1$, $\sin^2(2\theta_{34}) = 0.2$, and $\Delta m_{41}^2 = 4.5 \text{ eV}^2$ and the standard three-neutrino model. Fluxes are calculated using the Hillas-Gaisser H3a cosmic-ray-flux model and the SYBILL 2.3c interaction model. A broad disappearance is expected in upgoing tracks coincident with an appearance of upgoing cascades.

comparison rather than the more recent results of Ref. [33] as the updated event selection there improves efficiencies at low energy, while the data release required to make these studies is only available at present for the earlier, 1-yr analysis. Approximate agreement of the median sensitivity, well within the bounds of expected fluctuations, validates our simplified analysis methodology as capturing the essential elements needed for a robust sensitivity estimate. For completeness we also present an 8-yr projection.

B. Cascades-only sensitivity to ν_{τ} appearance

Signatures of ν_{τ} appearance require nonzero values for all of Δm_{41}^2 , θ_{24} , and θ_{34} . An example of a point with a nontrivial appearance signature that is consistent with existing experimental limits is shown in Fig. 6. This signature in reconstructed space is calculated by fixing θ_{24} and Δm_{41}^2 at their best-fit points from IceCube's ν_{μ}



FIG. 7. 2 d.o.f., 90% C.L. sensitivity to the θ_{24} and θ_{34} neutrino mixing parameters from this work with $\Delta m_{41}^2 = 1 \text{ eV}^2$ for this work, IceCube's DeepCore [77], and Super-Kamiokande [79]. The sensitivity through cascades is shown in the solid contour, and the joint track-cascade contour is dashed.

disappearance searches, and fixing $\sin^2(2\theta_{34}) = 0.2$, comfortably consistent with current bounds, which are around $\sin^2(2\theta_{34}) \leq 0.6$ [77,78].

Since all three of the above parameters must be nonzero to observe ν_{τ} appearance, sensitivities should be expressed in three-dimensional spaces (or four dimensional, if θ_{14} is also included). However, to facilitate presentation of results on 2D plots in this work we have primarily opted to present two-dimensional sensitivities under specific and experimentally motivated assumptions on the third parameter.

Using the methods described in Sec. III, we calculate expected cascade rates in IceCube at combinations of θ_{24} , θ_{34} , and Δm_{41}^2 . The effects of θ_{14} are marginal unless large mixing angles are reached, and so for this part of the analysis it was kept to zero. The matter effects on these oscillations are similarly only marginally affected by the CP-violating phases [34], and so they are fixed to zero. The results of the sensitivity scan over cascade events only are shown as the solid line of Fig. 7, with sensitivities from other experiments overlaid, at the conventional benchmark point of $\Delta m_{41}^2 = 1 \text{ eV}^2$; sensitivities at other values of Δm_{41}^2 are shown as the solid lines of Fig. 8. We see that with cascades alone we expect a sensitivity competitive with other leading sensitivities from Super-Kamiokande [79] and IceCube's DeepCore [77]. Sensitivities are the most competitive for points in phase space where both θ_{24} and θ_{34} are large; here, the transition probability $P(\nu_{\mu} \rightarrow \nu_{\tau})$ is maximized.

Meanwhile, in regions where $|U_{\tau4}|^2$ is small, ν_{μ} disappearance is most significant in a signal similar to those in Refs. [33,34], but as ν_{μ} cascades. A small increase to $|U_{\tau4}|^2$ can then lead to competing ν_{τ} appearance and ν_{μ} disappearance, and so for small values of Δm_{41}^2 , this leads to a reduction of sensitivity. Since ν_{μ} events overwhelmingly



FIG. 8. Cross sections of the 3 d.o.f., 90% C.L. sensivitivy surface to θ_{24} , θ_{34} , and Δm_{41}^2 . The sensitivity through cascades is shown in the solid contour, and the joint track-cascade contour is dashed.

lead to cascades while ν_{τ} often cause tracks, at higher $|U_{\mu4}|^2$ the ν_{τ} appearance begins to dominate and sensitivity improves. Finally, since a tau appearance follows a $\nu_{\mu} \rightarrow \nu_s \rightarrow \nu_{\tau}$ appearance channel, a nonzero $|U_{\mu4}|^2$ is needed to for any sensitivity; this causes a lower bound on the $|U_{\mu4}|^2$ sensitivity.

C. Joint sensitivity for ν_{μ} disappearance and ν_{τ} appearance

By performing a joint sensitivity using both cascadelike and tracklike events, we are able to significantly improve the sensitivity, by exploring a flavor ratio rather than a pure shape effect. Tracklike events will provide a method to fit to the overall flux normalization and further constrain sensitivities. Specifically, the process described in Sec. V B is performed for track events, and the fit event-number normalization is then used in calculating the log-likelihood in the cascade channel. The combined likelihood for both is then used in determining sensitivity contours. These results are shown in Fig. 7. A significant sensitivity enhancement relative to either tracks or cascades alone is obtained.

In addition to calculating sensitivity, we examine the results that may be expected in the presence of a sterile neutrino with nonzero θ_{24} and θ_{34} . In Fig. 9 we show the result obtained by injecting a signal with $\sin^2(2\theta_{24}) = 0.1$, $\sin^2(2\theta_{34}) = 0.2$, and $\Delta m_{41}^2 = 4.64 \text{ eV}^2$ and fitting over values of the mixing parameters; this mass-squared splitting was chosen out of computational convenience as it lines up with a point at which fluxes were calculated. We include four slices through the space in Δm_{41}^2 at several benchmark points, and provide contours at 90% C.L. calculated using χ^2 assuming that the test statistic, TS, satisfies Wilk's theorem and is distributed with a χ^2 distribution with thresholds consistent with 3 degrees of



FIG. 9. 3 d.o.f., 90% C.L. sensitivity to the $|U_{\mu4}|^2$ and $|U_{\tau4}|^2$ Pontecorvo-Maki-Nakagawa-Sakata matrix elements, at various values of Δm_{41}^2 , for this work using a joint track-cascade likelihood assuming a sterile neutrino with $\sin^2(2\theta_{24}) = 0.1$, $\sin^2(2\theta_{34}) = 0.2$, and $\Delta m_{41}^2 = 4.64 \text{ eV}^2$.

freedom. A signature of this form which is consistent with present constraints would be potentially discoverable in a joint track and cascade analysis at IceCube.

D. Joint sensitivity for ν_{μ} and disappearance generic cascade appearance

Cascade appearance may be introduced not only from ν_{τ} appearance, but also from ν_{e} appearance. A nonzero value for θ_{14} is motivated in particular by recent results from the BEST experiment, which motivates us to consider whether IceCube fitting both cascade and track channels has sensitivity to values of θ_{14} consistent with such a ν_{e} disappearance effect. IceCube can of course not rule out the BEST anomaly alone, since a scenario with $\theta_{24} = 0$ will generate no substantial appearance signatures in IceCube for any value of θ_{14} . But in principle it may be able confirm the BEST anomaly, given sizable enough values for both θ_{24} and θ_{14} . In such a model with nonzero θ_{14} , θ_{24} , and θ_{34} , resonant oscillations lead to appearances in both the ν_{τ} and ν_{e} channels shown in Fig. 10, wherein the BEST best-fit values were used for θ_{14} and Δm_{41}^2 .

To assess sensitivity to this effect in IceCube, scans over θ_{14} and θ_{34} were performed at multiple values of Δm_{41}^2 and θ_{24} . In Fig. 11 we show IceCube's sensitivity to a 3 + 1 sterile-neutrino model with $\theta_{14} = 0.0$. These contours represent the median expected 90% confidence level that could be drawn if no sterile neutrino were present, given assumptions on the nonplotted parameters shown in the caption. The two choices of assumptions made on the nonfitted parameters correspond to $\theta_{24} =$ 0.1609 (the ν_{μ} disappearance best-fit point from Ref. [33]) or $\theta_{24} = 0.3826$ (a value within the 90% results contour of Ref. [33]), and $\Delta m_{41}^2 = 1 \text{ eV}^2$ (a standard benchmark point in the field), $\Delta m_{41}^2 = 3.3 \text{ eV}^2$ (the BEST best-fit



FIG. 10. Transition probabilities $P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{\alpha})$ for $\bar{\nu}_{e}$ (top panel), $\bar{\nu}_{\mu}$ (middle panel), and $\bar{\nu}_{\tau}$ (bottom panel) for a sterile-neutrino flux with $\sin^{2}(2\theta_{14}) = 0.43$, $\sin^{2}(2\theta_{24}) = 0.1$, $\sin^{2}(2\theta_{34}) = 0.01$, and $\Delta m_{41}^{2} = 3.3 \text{ eV}^{2}$. A dashed black line is used to denote the outer core-mantle boundary.

point), and $\Delta m_{41}^2 = 4.64 \text{ eV}^2$ (close to the IceCube ν_{μ} disappearance best-fit point at 4.5 eV²). It is observed that IceCube has significant sensitivity in this high-dimensional parameter space for many values of the mixing parameters consistent with the present BEST and IceCube results, assuming a nonzero value of θ_{24} consistent with IceCube's existing preferred regions from ν_{μ} disappearance measurements.

A more intuitive picture of IceCube's capability to confirm the BEST anomaly as being sterile neutrino related, given values of other mixing parameters consistent with



FIG. 11. 2 d.o.f., 90% C.L. sensitivity contours for $\sin^2 \theta_{14}$ and $\sin^2 \theta_{34}$, using a joint track-cascade likelihood, for a 3 + 1 sterile-neutrino model with various values of Δm_{41}^2 and θ_{24} , and $\theta_{14} = 0.0$.



FIG. 12. Test statistics values for various different injected 3 + 1 sterile-neutrino models, using a joint track-cascade likelihood, compared to a three-neutrino hypothesis. The red line represents a 4 d.o.f. 95% C.L. sensitivity threshold; the shaded region represents the 95% confidence level bounds from the BEST best fit.

IceCube and world data, is shown in Fig. 12. Here, likelihoods are calculated according to injected sterileneutrino parameters and assuming a three-neutrino model; the resulting test statistics are shown. For all considered combinations, IceCube is seen to be capable of discriminating a BEST-like sterile-neutrino flux from a threeneutrino model at the 95% confidence level. Thus, IceCube appears to have the capability to confirm the best anomaly at least 95% confidence, given suitable values of the other mixing parameters, within existing constraints and uncertainties.

VI. CONCLUSIONS

We have considered IceCube's sensitivity to sterile neutrinos through the cascade appearance channel. Both ν_{τ} and ν_{e} appearance signatures are in principle observable by IceCube for θ_{14} and θ_{34} values within existing constraints, θ_{24} around IceCube's present preferred values from ν_{μ} disappearance, and many possible values Δm_{41}^2 .

We have found that IceCube's sensitivity in the joint $U_{\tau 4}$, $U_{\mu 4}$ space that has been explored by previous analyses at Super-Kamiokande and IceCube will be enhanced significantly at the benchmark point of $\Delta m^2 =$ 1 eV² by a joint fit to both track and cascade samples. Strong sensitivity is also obtained for other mass points, under the standard mixing assumption of $\theta_{14} = 0$. Cascade signatures that may accompany tentative but weak hints of ν_{μ} disappearance for $\Delta m_{41}^2 \sim 4.5$ eV² and $\sin^2(\theta_{24}) \sim 0.1$ are discoverable at IceCube with values θ_{34} that remain consistent with world data, strongly motivating investigation of ν_{τ} appearance via cascades in parallel with the established IceCube searches for ν_{μ} disappearance using tracks.

We have also explored the effect of introducing nontrivial ν_e appearance, consistent with the BEST and gallium anomalies, via nonzero θ_{14} . IceCube cannot rule out the BEST or gallium preferred regions in θ_{14} alone, since sensitivity of IceCube to this parameter requires nonzero θ_{24} . For modest values of θ_{24} at either the IceCube best-fit point in ν_{μ} disappearance or at a point near the 90% C.L. upper limit in this channel, however, values of θ_{14} and Δm_{41}^2 around the best-fit point can be probed at a better than 90% confidence level.

We conclude that our joint analysis of track and cascade topologies at IceCube can contribute to the ongoing worldwide project of understanding short-base-line anomalies in both ν_e appearance and disappearance channels. The IceCube dataset, probing both ν_{μ} disappearance and ν_e and ν_{τ} appearance near the matter resonance for core crossing neutrinos, provides unique and powerful insights into possible mixing of heavier neutrino mass states with the ν_{τ} flavor, as well as offering sensitivity to ν_e appearance in experimentally relevant parts of parameter space associated with the BEST and gallium anomalies.

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