

Search for the decay  $B_s^0 \rightarrow \eta\eta$ 

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We report results from a search for the decay  $B_s^0 \rightarrow \eta\eta$  using  $121.4 \text{ fb}^{-1}$  of data collected at the  $\Upsilon(5S)$  resonance with the Belle detector at the KEKB asymmetric-energy  $e^+e^-$  collider. We do not observe any signal and set an upper limit on the branching fraction of  $14.3 \times 10^{-5}$  at 90% confidence level. This result represents a significant improvement over the previous most stringent limit.

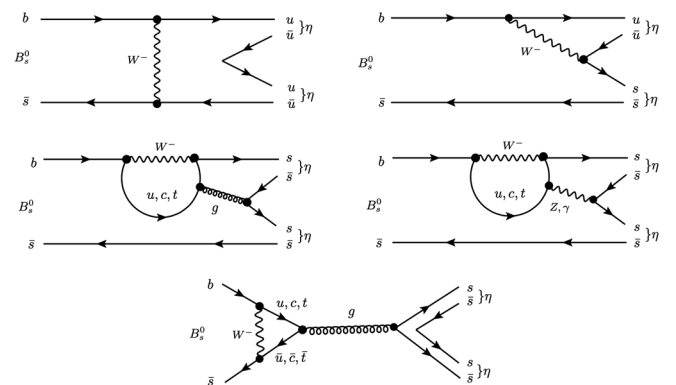
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Studies of two-body charmless  $B$  decays can shed light on the validity of the various theory approaches which are used to study them. The decay  $B_s^0 \rightarrow \eta\eta$  is a neutral charmless process that can occur through a variety of amplitudes such as the Cabibbo-suppressed  $b \rightarrow u$  transition or one loop diagrams with a quark and a virtual  $W^\pm$  boson, as shown in Fig. 1. Contributions can also come from electroweak ‘‘penguin’’ diagrams. Theoretically, the decay has been studied within the framework of soft-collinear effective theory [1], perturbative quantum chromodynamics (QCD) [2], and QCD factorization [3]. All these approaches predict a branching fraction ( $\mathcal{B}$ ) in the range of  $(7\text{--}16) \times 10^{-6}$ , albeit with large model uncertainties. Thus far, the only experimental result is an upper limit (UL) on  $\mathcal{B}$  at 90% confidence level (C.L.) of  $1.5 \times 10^{-3}$ , obtained by the L3 experiment [4]. This analysis constitutes the first attempt to search for this decay using  $e^+e^-$  collision data recorded by the Belle experiment.

The Belle detector [5,6] is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter composed of CsI(Tl) crystals (ECL). All these components are located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. The analysis is based on  $121.4 \text{ fb}^{-1}$  of data collected by Belle near the  $\Upsilon(5S)$  resonance, corresponding to  $(16.60 \pm 2.68) \times 10^6 B_s^0$  mesons produced.

The  $b\bar{b}$  production cross section at the  $\Upsilon(5S)$  center-of-mass energy is measured to be  $\sigma_{b\bar{b}}^{\Upsilon(5S)} = (0.340 \pm 0.016) \text{ nb}$  [7], while the fraction of  $B_s^{(*)}\bar{B}_s^{(*)}$  in  $b\bar{b}$  events is  $f_s = 0.201 \pm 0.031$  [8]. The  $B_s^{(*)}\bar{B}_s^{(*)}$  pairs include  $B_s^*\bar{B}_s^*$ ,  $B_s^*\bar{B}_s$ , and  $B_s\bar{B}_s$ , the fraction of the first two being  $f_{B_s^*\bar{B}_s^*} = (87.0 \pm 1.7)\%$  and  $f_{B_s^*\bar{B}_s} = (7.3 \pm 1.4)\%$ , respectively [7]. The  $B_s^*$  mesons decay to ground-state  $B_s^0$  mesons via the emission of a photon.

To reconstruct  $B_s^0 \rightarrow \eta\eta$  candidates, we first reconstruct  $\eta$  candidates from either  $\eta \rightarrow \gamma\gamma$  ( $\eta_{\gamma\gamma}$ ) or  $\eta \rightarrow \pi^+\pi^-\pi^0$  ( $\eta_{3\pi}$ ) decays. To calculate the experimental acceptance and reconstruction efficiency, signal Monte Carlo (MC) events are generated for the  $B_s^0 \rightarrow \eta_{\gamma\gamma}\eta_{\gamma\gamma}$ ,  $B_s^0 \rightarrow \eta_{\gamma\gamma}\eta_{3\pi}$  and  $B_s^0 \rightarrow \eta_{3\pi}\eta_{3\pi}$  modes with the EvtGen [9] event generator. Backgrounds are due to the copious production of quark-antiquark ( $u, d, s, c$ ) pairs in  $e^+e^-$  annihilation; this is referred to as the continuum background. Additional background arises from  $B_s^{(*)}\bar{B}_s^{(*)}$  decays (referred to as  $bsbs$ ) and  $B^*\bar{B}^*$ ,  $B^*\bar{B}$ ,  $B\bar{B}$ ,  $B^*\bar{B}^*\pi$ ,  $B^*\bar{B}\pi$ ,  $B\bar{B}\pi$  and  $B\bar{B}\pi\pi$  decays (referred to as  $nonbsbs$ ) from  $B^0$  and  $B^\pm$  near  $\Upsilon(5S)$  resonance. Dedicated MC samples are generated to

FIG. 1. Feynman diagrams for  $B_s^0 \rightarrow \eta\eta$ .

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study these background processes. The detector response is simulated using GEANT3 [10], with beam-related backgrounds from data being embedded to produce a more realistic simulated event sample.

Photons are reconstructed by identifying energy deposits in the ECL that are not associated with any charged track. We require a minimum energy of 0.1 GeV. The timing characteristics of energy clusters used in photon reconstruction must be consistent with the beam collision time, which is determined at the trigger level for the candidate event. Daughter photons from  $\pi^0$  decays pose a significant background for  $\eta \rightarrow \gamma\gamma$  reconstruction. To suppress this background, we calculate a  $\pi^0$  likelihood for each pair of photons using the energies and polar angles of the photons as well as the diphoton invariant mass. This likelihood is optimized using the figure-of-merit,  $S/\sqrt{S+B}$  to increase the signal significance, where  $S$  and  $B$  represents the estimated number of signal and background events, respectively. The optimized value of the likelihood is 0.4, which is 90% efficient in selecting the signal and rejects 62% of backgrounds.

To reject merged  $\gamma$ 's and neutral hadrons, the ratio of the energy deposited in an innermost ( $3 \times 3$ ) array of crystals compared to that deposited in the ( $5 \times 5$ ) array centered around the most energetic crystal is required to be greater than 0.95. Selected photons are combined to form  $\eta_{\gamma\gamma}$  candidates, with the diphoton invariant mass required to be in the range (0.50–0.60) GeV/ $c^2$ . This range corresponds to  $\pm 3\sigma$  in resolution around the  $\eta$  mass. The candidate  $\pi^0$  is required to have a  $\gamma\gamma$  invariant mass between 0.117 GeV/ $c^2$  and 0.149 GeV/ $c^2$ , which corresponds to  $\pm 3\sigma$  in resolution around the nominal  $\pi^0$  mass. For the reconstruction of both  $\eta$  and  $\pi^0$  candidates, we perform mass-constrained fits to improve the momentum resolution.

Charged tracks must have an impact parameter with respect to the interaction point of less than 0.3 cm in the  $r$ - $\phi$  plane, and less than 3.0 cm along the  $e^+$  beam direction. The  $r$ - $\phi$  plane is perpendicular to the  $e^+$  beam direction, where,  $r$  represents the radius of the hit and  $\phi$  measures the azimuthal angle. The transverse momentum of the selected tracks is required to be greater than 0.1 GeV/ $c$ . Charged pions are identified using information obtained from the CDC, the TOF, and the ACC. This information is combined to form a likelihood ( $\mathcal{L}$ ) for hadron identification. We require that charged pions satisfy  $\mathcal{L}_K/(\mathcal{L}_K + \mathcal{L}_\pi) < 0.4$ , where  $\mathcal{L}_K(\mathcal{L}_\pi)$  denotes the likelihood for a track to be a kaon (pion). The efficiency of this requirement is approximately 92%, while the probability for a kaon to be misidentified as a pion is about 8%. Two oppositely charged pions are combined with a  $\pi^0$  candidate to reconstruct an  $\eta_{3\pi}$  candidate, with the resulting invariant mass required to lie in the range (0.527–0.568) GeV/ $c^2$ . This range corresponds to  $\pm 3\sigma$  in resolution around the  $\eta$  mass. For each such  $\eta$  candidate, a mass-constrained fit is performed and the  $\chi^2$  is required to be less than 20, to reject backgrounds from low energy photons.

Candidate  $B_s^0 \rightarrow \eta\eta$  decays are formed by combining a pair of  $\eta$  mesons, and further selections are applied to their beam-energy constrained mass ( $M_{bc}$ ) and the energy difference ( $\Delta E$ ). These quantities are defined as

$$M_{bc} = \frac{\sqrt{(E_{\text{beam}})^2 - (\vec{p}_{\text{reco}})^2} c^2}{c^2} \quad (1)$$

$$\Delta E = E_{\text{reco}} - E_{\text{beam}}, \quad (2)$$

where  $E_{\text{beam}}$  is the beam energy, and  $\vec{p}_{\text{reco}}$  and  $E_{\text{reco}}$  are the momentum and energy, respectively, of the reconstructed  $B_s^0$  candidate. All quantities are calculated in the  $e^+e^-$  center-of-mass frame. Signal candidates are required to satisfy  $5.30 \text{ GeV}/c^2 < M_{bc} < 5.44 \text{ GeV}/c^2$  and  $-0.60 \text{ GeV} < \Delta E < 0.20 \text{ GeV}$ .

The dominant source of background is continuum events. As the outgoing light quarks carry significant momenta, these events tend to be jetlike and thus topologically different from more spherical  $B_s^{(*)}\bar{B}_s^{(*)}$  events, in which the  $B_s^0$  mesons have small momenta. To suppress this background, a neural network (NN) based on the NeuroBayes algorithm [11] is used. The inputs consist of sixteen event shape variables that include modified Fox-Wolfram moments [12], and the absolute value of the cosine of the angle between the thrust axis [13] of the  $B_s^0$  decay products and the rest of the event. The NN output,  $\mathcal{C}_{\text{NN}}$ , ranges from  $-1$  to  $+1$ , with a value near  $+1$  ( $-1$ ) being more likely due to a signal (background) event.

To reduce the continuum background,  $\mathcal{C}_{\text{NN}}$  is required to be greater than  $-0.6$ . This requirement suppresses the continuum background by a factor of 2.5, with a signal efficiency of about 95%. The contribution from other background processes such as  $bsbs$  and  $nonbsbs$  is estimated to be less than one event. The  $\mathcal{C}_{\text{NN}}$  value is transformed to a new variable,  $\mathcal{C}'_{\text{NN}}$ , to facilitate its modeling with a simple analytical function:

$$\mathcal{C}'_{\text{NN}} = \log\left(\frac{\mathcal{C}_{\text{NN}} - \mathcal{C}_{\text{NN}(\min)}}{\mathcal{C}_{\text{NN}(\max)} - \mathcal{C}_{\text{NN}}}\right), \quad (3)$$

where  $\mathcal{C}_{\text{NN}(\min)} = -0.6$  and  $\mathcal{C}_{\text{NN}(\max)}$  is the maximum value of  $\mathcal{C}_{\text{NN}}$  obtained from the NN distribution.

After applying all the selection criteria, about 6% of events in the  $\eta_{\gamma\gamma}\eta_{\gamma\gamma}$  decay mode are found to have more than one signal candidate, whereas for the  $\eta_{\gamma\gamma}\eta_{3\pi}$  and  $\eta_{3\pi}\eta_{3\pi}$  decay modes, about 16% and 28% of events, respectively, have more than one signal candidate. For events with multiple candidates, we select the candidate having the smallest value of the sum of  $\chi^2$  values from the two mass-constrained fits. The overall efficiency of the best candidate selection criteria obtained from a signal MC study is 94%. The fraction of misreconstructed signal events, referred to as self-cross-feed (SCF), is found from MC studies to be

TABLE I. PDFs used to model the  $M_{bc}$ ,  $\Delta E$ , and  $C'_{NN}$  distributions. The notations G, CB, CP, and A correspond to Gaussian, Crystal Ball [14], Chebyshev polynomial, and ARGUS functions [15], respectively.

Fit component	$M_{bc}$	$\Delta E$	$C'_{NN}$
Signal	CB	CB + G	G + G
SCF	CB	CB + CP	G + G
Continuum	A	CP	G

TABLE II. Summary of fit results. The quoted uncertainties are statistical only.

Decay mode	$\eta_{\gamma\gamma}\eta_{\gamma\gamma}$	$\eta_{\gamma\gamma}\eta_{3\pi}$	$\eta_{3\pi}\eta_{3\pi}$
Signal	$3.9 \pm 3.2$	$7.7 \pm 4.4$	$0.2 \pm 5.9$
Background	$882 \pm 30$	$797 \pm 28$	$1244 \pm 36$
Efficiency (%)	$9.68 \pm 0.09$	$9.48 \pm 0.09$	$8.14 \pm 0.08$
$\mathcal{B}$ ( $10^{-5}$ )	$1.84 \pm 1.38$	$6.54 \pm 3.27$	$1.65 \pm 9.90$
Total $\mathcal{B}$	$(10.03 \pm 10.52) \times 10^{-5}$		
$\mathcal{B}$ UL at 90% C.L.	$14.3 \times 10^{-5}$		

5.5%, 8.9%, and 12.9% for the  $\eta_{\gamma\gamma}\eta_{\gamma\gamma}$ ,  $\eta_{\gamma\gamma}\eta_{3\pi}$ , and  $\eta_{3\pi}\eta_{3\pi}$  decay modes, respectively.

We extract signal yields for the three decay modes by performing an unbinned maximum likelihood fit to the variables  $M_{bc}$ ,  $\Delta E$ , and  $C'_{NN}$ . We consider signal candidates originating only from  $B_s^* \bar{B}_s^*$  production. The likelihood function is defined as

$$\mathcal{L}_{\text{fit}} = e^{-\sum_j n_j} \prod_i \left( \sum_j n_j P_j(M_{bc}^i, \Delta E^i, C'_{NN}{}^i) \right), \quad (4)$$

where  $P_j(M_{bc}^i, \Delta E^i, C'_{NN}{}^i)$  is the probability density function (PDF) of the signal or background component (specified by index  $j$ ),  $n_j$  is the yield of this component, and  $N$  is the total number of events in the sample. The signal and background PDFs are determined from the respective MC samples, after applying all selection criteria. These PDFs used for modeling the signal, SCF, and continuum background are listed in Table I. Correlations among the fit variables are found to be negligible. Thus, the

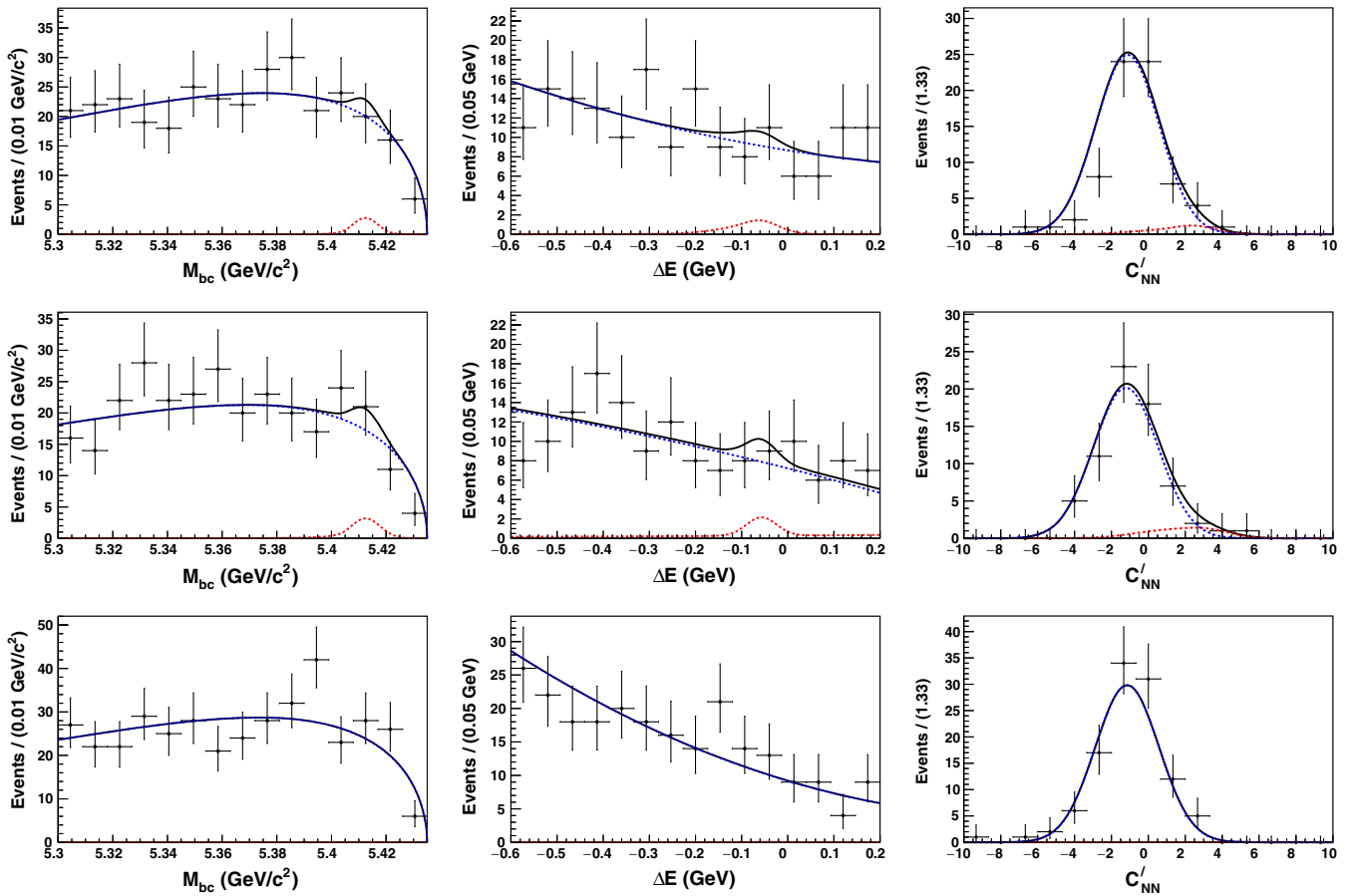


FIG. 2. Fit results for the  $B_s^0 \rightarrow \eta_{\gamma\gamma}\eta_{\gamma\gamma}$  (top),  $B_s^0 \rightarrow \eta_{\gamma\gamma}\eta_{3\pi}$  (middle) and  $B_s^0 \rightarrow \eta_{3\pi}\eta_{3\pi}$  (bottom) modes. The projections are shown for events inside a signal region in  $M_{bc}$ ,  $\Delta E$  and  $C'_{NN}$ , except for the variable plotted. The signal region is defined as  $5.39 < M_{bc} < 5.43$   $\text{GeV}/c^2$ ,  $-0.27 < \Delta E < 0.12$   $\text{GeV}$ , and  $C'_{NN} > 2.91$ . Points with the error bars show the data, solid black curves show the total fit function, and dotted red (dashed blue) curves show the signal (background) contribution.

three-dimensional PDF  $P_j$  is expressed as the product of three one-dimensional PDFs,

$$P_j \equiv P_j(M_{bc})P_j(\Delta E)P_j(C'_{NN}). \quad (5)$$

The signal PDF parameters and the endpoint of the ARGUS function for the background  $M_{bc}$  distribution are fixed to values obtained from an MC study, while all the other background PDF parameters are floated. The signal and background yields are floated in the fit, while the fraction of SCF events is fixed. The mean and standard deviation of the signal PDFs are corrected for small data-MC differences. These corrections are obtained by comparing the shapes of data and MC distributions for a control sample of  $B^0 \rightarrow \eta\eta$  decays, which have the same final-state particles.

From fitting the data, we obtain  $3.9 \pm 3.2$ ,  $7.7 \pm 4.4$ , and  $0.2 \pm 5.9$  signal events for  $\eta_{\gamma\gamma}\eta_{\gamma\gamma}$ ,  $\eta_{\gamma\gamma}\eta_{3\pi}$ , and  $\eta_{3\pi}\eta_{3\pi}$  decay modes, respectively. The common branching fraction by taking into account the signal yields of each decay mode (with index  $k$ ) is expressed as,

$$\mathcal{B}(B_s^0 \rightarrow \eta\eta) = \sum_{k=1}^3 \frac{N_k^{\text{sig}}}{N_{B_s\bar{B}_s} \times \epsilon_k^{\text{rec}} \times \prod \mathcal{B}_{\eta k}} \quad (6)$$

where  $N_{B_s\bar{B}_s}$  is the number of  $B_s\bar{B}_s$  pairs;  $\epsilon_k^{\text{rec}}$  and  $N_k^{\text{sig}}$  is the signal selection efficiency obtained from MC simulation and number of signal events, respectively, for each of the decay modes; and  $\prod \mathcal{B}_{\eta k}$  is the product of the two  $\eta$ -decay branching fractions corresponding to each of the decay modes [8]. The fit results are summarized in Table II, and their projections in the signal regions are shown in Fig. 2.

The systematic uncertainties associated with the analysis are listed in Table III. To investigate possible fit bias, we

TABLE III. Summary of systematic uncertainties. The uncertainties listed in the lower section of the table are external to the analysis.

Source	Value (%)
Fit bias	$\pm 6.0$
PDF modeling	8.0
$\eta \rightarrow \gamma\gamma$ selection efficiency	3.0
$\pi^0 \rightarrow \gamma\gamma$ selection efficiency	3.0
Pion identification efficiency	3.2
Tracking efficiency	2.1
$C'_{NN}$ requirement	10.6
Calibration factors	3.1
MC statistics	1.8
$L_{\text{int}}$	1.3
$\sigma_{b\bar{b}}^{\Upsilon(5S)}$	4.7
$\mathcal{B}(\eta \rightarrow \gamma\gamma)$	0.5
$\mathcal{B}(\eta \rightarrow \pi^+\pi^-\pi^0)$	1.2
$f_s$	15.4
Total	22.8

perform an ensemble test in which signal MC events are generated using EVTGEN and subsequently passed through a detector simulation based on GEANT3. The background events are generated from the corresponding PDFs used for fitting. For different numbers of input signal events, we generate and fit ensembles of 3000 experiments each. From the pull distributions obtained from these ensemble tests, we observe an average fit bias of 6%, which we include as a source of systematic uncertainty.

The uncertainty due to PDF modeling is estimated from the variation in the signal yield while varying each fixed parameter by  $\pm 1\sigma$ . The uncertainty in the selection efficiency of the  $\eta \rightarrow \gamma\gamma$  or  $\pi^0 \rightarrow \gamma\gamma$  decay is 3.0%, determined from a comparison of the data and signal MC selection efficiency ratios for large samples of  $\eta \rightarrow \pi^+\pi^-\pi^0$  and  $\eta \rightarrow 3\pi^0$  decays [16]. The systematic uncertainties due to the charged pion identification and tracking efficiency are 3.2% and 2.1% respectively, measured using control samples of  $D^{*+} \rightarrow D^0\pi^+$ ,  $D^0 \rightarrow K^-\pi^+$ , and  $D^{*+} \rightarrow D^0\pi^+$ ,  $D^0 \rightarrow K_S^0\pi^+\pi^-$ ,  $K_S \rightarrow \pi^+\pi^-$  decays. The systematic uncertainty due to the  $C'_{NN}$  requirement is estimated by comparing the efficiencies in data and MC simulations of a large  $B^0 \rightarrow \eta\eta$  control sample. As mentioned above, the shapes of the signal PDFs are calibrated using the  $B^0 \rightarrow \eta\eta$  control sample. The  $M_{bc}$  mean is found to be consistent within the statistical uncertainty, while the  $\Delta E$  mean is shifted by 3 MeV. The systematic uncertainty associated with the small difference in  $C'_{NN}$  mean and width as well as  $M_{bc}$  and  $\Delta E$  width values are evaluated by varying these parameters by  $\pm 3\sigma$ , and is measured to be 3.1%. The uncertainty in the signal reconstruction efficiency due to MC statistics is 1.8%. We also assign a systematic uncertainty of 4.7% due to the uncertainty in the production cross-section of  $b\bar{b}$  events at  $\Upsilon(5S)$  resonance. Systematic uncertainties of 0.5% and 1.2% are assigned due to the branching fractions of  $\eta \rightarrow \gamma\gamma$  and  $\eta \rightarrow \pi^+\pi^-\pi^0$  [8]. Lastly, the uncertainty due to the fraction,  $f_s$  is 15.4% [8].

Using the signal yields obtained from the fits of the three decay modes, the combined branching fraction for  $\mathcal{B}(B_s^0 \rightarrow \eta\eta)$  and  $f_s \times \mathcal{B}(B_s^0 \rightarrow \eta\eta)$  is calculated to be  $(10.0 \pm 10.5 \pm 2.3) \times 10^{-5}$  and  $(2.0 \pm 2.1 \pm 0.3) \times 10^{-5}$ , respectively. The first uncertainty is statistical and the second is systematic. As we do not observe any significant signal yield, we use a Bayesian approach to set an upper limit(UL) on the branching fraction by integrating the combined likelihood function from 0 to 90% of the total area under

TABLE IV. Summary of results on branching fractions and UL for  $\mathcal{B}(B_s^0 \rightarrow \eta\eta)$  and  $f_s \times \mathcal{B}(B_s^0 \rightarrow \eta\eta)$ .

Quantity	Value
$\mathcal{B}(B_s^0 \rightarrow \eta\eta)$	$(10.0 \pm 10.5 \pm 2.3) \times 10^{-5}$ $< 14.3 \times 10^{-5}$ @ 90% C.L.
$f_s \times \mathcal{B}(B_s^0 \rightarrow \eta\eta)$	$(2.0 \pm 2.1 \pm 0.3) \times 10^{-5}$ $< 2.9 \times 10^{-5}$ @ 90% C.L.

the curve for  $\mathcal{B} \geq 0$ . The results from the three  $B_s^0 \rightarrow \eta\eta$  decay modes are combined by adding the three individual log likelihoods as a function of branching fraction. Systematic uncertainties are included by convolving the combined likelihood curve with a Gaussian function of width equal to the total systematic uncertainty mentioned in Table III. We obtain a 90% C.L. UL of  $14.3 \times 10^{-5}$  on the branching fraction. In addition, the 90% C.L. UL on the product  $f_s \times \mathcal{B}(B_s^0 \rightarrow \eta\eta)$  is estimated to be less than  $2.9 \times 10^{-5}$ . The total fractional systematic uncertainty associated with  $\mathcal{B}(B_s^0 \rightarrow \eta\eta)$  and  $f_s \times \mathcal{B}(B_s^0 \rightarrow \eta\eta)$  is 22.8% and 16.8%, respectively. These results are summarized in Table IV.

In summary, we have searched for the decay  $B_s^0 \rightarrow \eta\eta$  using the complete  $\Upsilon(5S)$  dataset from the Belle experiment. We do not observe any statistically significant signal for the decay and set a 90% confidence level upper limit of  $14.3 \times 10^{-5}$  on its branching fraction. This is an improvement by about an order of magnitude over the previous limit [4].

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- [1] A. R. Williamson and J. Zupan, *Phys. Rev. D* **74**, 014003 (2006); **74**, 039901(E) (2006).
- [2] A. Ali, G. Kramer, Y. Li, C.-D. Lü, Y.-L. Shen, W. Wang, and Y.-M. Wang, *Phys. Rev. D* **76**, 074018 (2007).
- [3] M. Beneke and M. Neubert, *Nucl. Phys.* **B675**, 333 (2003).
- [4] M. Acciarri *et al.* (L3 Collaboration), *Phys. Lett. B* **363**, 127 (1995).
- [5] A. Abashian *et al.* (Belle Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **479**, 117 (2002).
- [6] J. Brodzicka *et al.* (Belle Collaboration), *Prog. Theor. Exp. Phys.* **2012**, 4D001 (2012).
- [7] S. Esen *et al.* (Belle Collaboration), *Phys. Rev. D* **87**, 031101(R) (2013).
- [8] P. A. Zyla *et al.* (Particle Data Group), *Prog. Theor. Exp. Phys.* **2020**, 083C01 (2020).
- [9] D. J. Lange, *Nucl. Instrum. Methods Phys. Res., Sect. A* **462**, 152 (2001).
- [10] R. Brun *et al.*, GEANT3.21. Report No. CERN DD/EE/84-1, 1984.
- [11] M. Feindt and U. Kerzel, *Nucl. Instrum. Methods Phys. Res., Sect. A* **559**, 190 (2006).
- [12] G. C. Fox and S. Wolfram, *Phys. Rev. Lett.* **41**, 1581 (1978); S. H. Lee *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **91**, 261801 (2003).
- [13] A. J. Bevan, B. Golob, T. Mannel, S. Prell, and B. D. Yabsley, *Eur. Phys. J. C* **74**, 3026 (2014).
- [14] T. Skwarnicki, Ph.D. thesis, Institute for Nuclear Physics, Krakow, DESY Internal Report, No. DESY F31-86-02, 1986.
- [15] H. Albrecht *et al.* (ARGUS Collaboration), *Phys. Lett. B* **241**, 278 (1990).
- [16] M. C. Chang *et al.* (Belle Collaboration), *Phys. Rev. D* **85**, 091102(R) (2012).