Remarks on bosonic super-WIMP search experiments

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Bosonic super-weakly interacting massive particles (WIMPs), including pseudoscalar and vector particles, are dark-matter candidates. To date, many underground experiments searches for super-WIMPs have been performed in the mass range of a few keV/c^2 to $1 \text{ MeV}/c^2$. All these searches utilize the absorption process of a super-WIMP by a target atom in the detector, which is similar to the photoelectric effect. We consider another process—namely, a Compton-like process. As an example, we compare the cross section of a germanium atom for the absorption process becomes dominant relative to that for the absorption process for mass above approximately 150 keV/c^2 for both pseudoscalar and vector super-WIMPs. In particular, the cross section for the Compton-like process for a vector super-WIMP becomes increasingly greater than that for the absorption process by 1 to 2 orders of magnitude in the 400 keV/c^2 to 1 MeV/c^2 mass range, respectively. By including the Compton-like process, which has not been used in any other super-WIMP search experiments, the experimental upper limits can be improved.

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I. INTRODUCTION

One of the most fundamental questions in physics is the nature of dark matter (DM). The existence of DM, which constitutes approximately 80% of the matter in the Universe [1], has been inferred from a wide range of astrophysical and cosmological systems based solely on gravitational effects [2,3]. Although the standard model (SM) of particle physics is extraordinarily successful, it cannot explain the nature of DM.

The freeze-out mechanism is a plausible method for the generation of the DM population in our Universe. It has been assumed that DM particles, commonly called weakly interacting massive particles (WIMPs), interacted with SM particles in thermal equilibrium at very high temperatures in the early Universe, and the DM particles that were out of equilibrium remained as the Universe expanded. The currently observed dark-matter relic abundance has been generated due to the weak mass scale O(100 GeV) of DM with weak interaction strength between the WIMPs and SM particles [4,5]. The DM produced by this mechanism is

*yjko@ibs.re.kr [†]Corresponding author. hyangkyu@korea.ac.kr commonly referred to as a WIMP. Extensive searches over the past 40 years for a WIMP with O(100 GeV) mass have not yielded any results. Hence, it is desirable to investigate various theoretical models of DM.

Based on the numerical simulation results for the smallscale structure formation of a WIMP based on gravitational interaction, the DM mass is considered to be greater than \sim 3 keV [6]. A mass on this scale implies weak interaction between the DM and SM particles. Several models have been proposed with DM mass scales ranging from keV to MeV for the so-called super-WIMP [7–12]. Fermionic super-WIMPs, sterile neutrinos, and gravitinos have been thoroughly studied and are extremely difficult to detect experimentally. On the other hand, bosonic super-WIMPs allow the decay of lighter SM particles [7], and such decays with superweak interactions can be strongly suppressed. Nonetheless, super-WIMPs can be absorbed or emitted by SM particles, which can be directly detected through terrestrial experiments. In particular, their absorption process in the target material deposits energy into the target atom, which corresponds to the rest mass of the super-WIMP.

The upper limits of the bosonic super-WIMP masses are about 300 keV/ c^2 and are estimated by comparing the gamma rays from the extragalactic halo with the expected photon flux due to the bosonic super-WIMP decays [13]. If the bosonic super-WIMPs do not constitute a significant fraction of the DM, this estimation does not give such a constraint for the upper limits of the masses. Furthermore, the masses in some extensions of the bosonic super-WIMP model can be sub-MeV/ c^2 [14] or larger than 1 MeV/ c^2

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[15]. If the masses of the bosonic super-WIMPs are larger than twice the electron mass, they can decay into an e^+e^- pair such that their lifetime could be too short to be the DM. It would be worthwhile to search for the bosonic super-WIMP mass in the range of $\mathcal{O}(\text{MeV}/c^2)$.

Experimental explorations for pseudoscalar (vector) super-WIMPs, known as axionlike-particles (dark photons), have been performed based on their absorption in detector material. The constraints for the coupling strength of super-WIMPs with electrons for the super-WIMP mass have been determined through underground experiments [16–26], which investigate the super-WIMP mass region from $\sim \text{keV}/c^2$ to 1 MeV/ c^2 . To detect super-WIMP events, all these studies utilize the absorption process of the super-WIMP by target atoms, which is similar to the photoelectric effect; the cross sections for this process are proportional to those of the photoelectric effect, where the photon energy is equal to the super-WIMP mass. When using the absorption process for super-WIMP detection, the upper limit becomes weak with the increase in the super-WIMP mass. For example, the cross section of Ge for the photoelectric effect decreases significantly from 4306 b/atom at 10 keV to 0.0086 b/atom at 1 MeV for the incoming photon energy.

In this paper, we consider a Compton-like process $a + e^- \rightarrow e^- + \gamma$ ($V + e^- \rightarrow e^- + \gamma$) for a pseudoscalar (vector) super-WIMP, where a and V represent a pseudoscalar and vector super-WIMP, respectively. In general, the cross section for the Compton process is greater than that for the photoelectric effect at photon energies above ~100 keV. By including the Compton-like process, we expect an improvement in the experimental sensitivity in the mass range of ~100 keV/ c^2 to a few MeV/ c^2 . The most recent search for super-WIMPs used Ge atoms as the target material in the GERDA experiment [20] for a super-WIMP mass range up to 1 MeV/ c^2 . We study the cross section for the absorption and Compton-like processes with a Ge target for a super-WIMP model in the 1 keV/ c^2 to 1 MeV/ c^2 mass range.

II. THE MODEL FOR SUPER-WIMP

In this section, we discuss the absorption process, which is similar to the photoelectric effect, and a Compton-like process for the interaction of a pseudoscalar super-WIMP and vector super-WIMP with an atom and electron, respectively. The Lagrangian for the interaction of pseudoscalar super-WIMP a with an electron [7] can be expressed as follows:

$$\mathcal{L} = 2 \frac{m_e}{f_a} a \bar{\psi} i \gamma_5 \psi, \qquad (1)$$

where f_a is the interaction strength, m_e is the electron mass, and ψ is the electron field. Therefore, this interaction Lagrangian gives the cross section for the absorption process $\sigma_{a,abs}$ [7] with an atom, which is the so-called axioelectric effect, in terms of the cross section for the photoelectric effect σ_{pe} , with the photon energy ω equivalent to the mass of the pseudoscalar super-WIMP (m_a):

$$\frac{\sigma_{a,abs}v}{\sigma_{\rm pe}(\omega=m_a)c} \approx \frac{3m_a^2}{4\pi\alpha f_a^2},\tag{2}$$

where v is the incoming velocity of the super-WIMP, c is the velocity of light, and α is the fine structure constant. Equation (2) can be rewritten by introducing dimensionless coupling $g_{aee} = 2m_e/f_a$ as follows:

$$\frac{\sigma_{a,abs}v}{\sigma_{\rm pe}(\omega=m_a)c} \approx g_{aee}^2 \frac{3m_a^2}{16\pi\alpha m_e^2}.$$
 (3)

For the interaction of vector super-WIMP V with an electron, the Lagrangian [7] is given by

$$\mathcal{L} = e\kappa V_{\mu} \bar{\psi} \gamma^{\mu} \psi, \qquad (4)$$

where V_{μ} is the field of the super-WIMP, *e* is the electron charge, and κ is the kinetic mixing parameter with the electromagnetic field. The absorption cross section of the vector super-WIMP ($\sigma_{V,abs}$) by an atom [7] is calculated as

$$\frac{\sigma_{V,abs}v}{\sigma_{\rm pe}(\omega=m_V)c} \approx \frac{\alpha'}{\alpha},\tag{5}$$

where m_V is the mass of the vector super-WIMP and α' is $\frac{(e\kappa)^2}{4\pi}$.

The Compton-like process where a pseudoscalar super-WIMP or vector super-WIMP interacts with an electron and produces a photon (γ) is as follows:

$$e + \phi \to e + \gamma,$$
 (6)

where ϕ can be either a pseudoscalar super-WIMP or vector super-WIMP. The cross section for the Comptonlike process of a pseudoscalar (vector) super-WIMP, $\sigma_{a,\text{cmp}}$ ($\sigma_{V,\text{cmp}}$) [27], can be determined as follows:

$$\sigma_{a,\text{cmp}} = g_{aee}^2 \frac{\alpha}{4m_e |\mathbf{k}|} \int_{-1}^{1} d\cos\theta_{\gamma} \frac{|\mathbf{q}|\mathcal{A}_P}{E_k + m_e - |\mathbf{k}|\cos\theta_{\gamma}}, \quad (7a)$$

$$\sigma_{V,\rm cmp} = \kappa^2 \frac{\pi \alpha^2}{3m_e |\mathbf{k}|} \int_{-1}^{1} d\cos\theta_{\gamma} \frac{|\mathbf{q}|\mathcal{A}_V}{E_k + m_e - |\mathbf{k}|\cos\theta_{\gamma}}, \quad (7b)$$

where **k** is the momentum of the incoming super-WIMP, **q** is the momentum of the outgoing photon, θ_{γ} is the angle between the photon and super-WIMP, and \mathcal{A}_P and \mathcal{A}_V are the matrix elements of the Compton-like process for the pseudoscalar super-WIMP and vector super-WIMP [27],



FIG. 1. Cross sections (unit, b/atom) for the absorption and Compton-like processes, and the total cross section, including both processes, for the pseudoscalar (left panel) and vector (right panel) super-WIMPs as a function of the mass. We used the dimensionless coupling constant $g_{aee} = 1$ (kinetic mixing parameter $\kappa = 1$) for a pseudoscalar (vector) super-WIMP.

respectively. Here, $|\mathbf{q}|$ for the Compton-like process in Eqs. (7a) and (7b) is given by

$$|\mathbf{q}| = \frac{m_{\phi}^2 + 2E_k m_e}{2(m_e + E_k - |\mathbf{k}| \cos \theta_{\gamma})},\tag{8}$$

where m_{ϕ} is the mass of the super-WIMP and E_k is the energy of the super-WIMP, which can be considered the mass of the super-WIMP.

III. CROSS-SECTION ESTIMATIONS FOR THE ABSORPTION AND COMPTON-LIKE PROCESSES

In this section, we discuss the cross section of the Ge atom for the absorption and Compton-like processes. For estimating the cross section for the absorption process, we used Eq. (3) for a pseudoscalar super-WIMP and Eq. (5) for a vector super-WIMP. For such an estimation, the cross sections for the photoelectric effect (σ_{pe}) of the Ge atoms were used in the XCOM: Photons Cross Sections Database [28].

For an atom, the cross sections of the Compton-like process for a pseudoscalar and vector super-WIMP are given by

$$\sigma_{a,\rm cmp}^Z = N_e \sigma_{a,\rm cmp},\tag{9a}$$

$$\sigma_{V,\rm cmp}^Z = N_e \sigma_{V,\rm cmp},\tag{9b}$$

where $\sigma_{a,\text{cmp}}^Z(\sigma_{V,\text{cmp}}^Z)$ is the cross section for the Comptonlike process for a pseudoscalar (vector super-WIMP) for an atom and N_e is the number of electrons (atomic number) in the atom. $\sigma_{a,\text{cmp}}$ and $\sigma_{V,\text{cmp}}$ can be calculated numerically using Eqs. (7a) and (7b), respectively. We set $N_e = 32$ as the atomic number of the Ge atom. The total cross section (σ_{atom}) for a super-WIMP interacting with an atom, including both the absorption and Compton-like processes, can be expressed as

$$\sigma_{\text{atom}} = \sigma_{a(V),abs} + \sigma_{a(V),\text{cmp}}^Z.$$
 (10)

To compare the cross sections for the absorption and Compton-like processes for the interaction of a pseudoscalar (vector) super-WIMP with a Ge atom, we applied the dimensionless coupling constant $g_{aee} = 1$ (kinetic mixing parameter $\kappa = 1$). The results for each process and the total cross section for the pseudoscalar and vector super-WIMP are shown in Fig. 1. As previously mentioned, the cross section for the Compton-like process is greater than that of the absorption process in the mass range above approximately 500 keV/ c^2 (100 keV/ c^2) for a pseudoscalar (vector) super-WIMP. In particular, the cross section for the Compton-like process for a vector super-WIMP continues to increase from 1 to 2 orders of magnitude in the 400 keV/ c^2 to 1 MeV/ c^2 mass range, respectively.

IV. CONCLUSIONS

In this paper, we examined the absorption and Comptonlike processes for the interaction of a super-WIMP with an atom. As an example, we compared the cross sections of both processes for a Ge atom. The obtained results demonstrated that the Compton-like process had a greater cross section than the absorption process for masses above approximately 150 keV/ c^2 for both pseudoscalar and vector super-WIMPs. The cross section for the Compton-like process for a pseudoscalar super-WIMP is increased to 1 order of magnitude at 1 MeV/ c^2 of mass. However, the cross section for the Compton-like process for a vector super-WIMP becomes increasingly greater than that for the absorption process by 1 to 2 orders of magnitude in the 400 keV/ c^2 to 1 MeV/ c^2 YOUNG JU KO and HYANGKYU PARK

mass range, respectively. By including the Compton-like process, which has not been used in any other super-WIMP search experiments, the experimental upper limits can be improved.

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- [1] P. A. R. Ade *et al.* (Planck Collaboration), Astron. Astrophys. **594**, A23 (2016).
- [2] L. Bergstrom, Ann. Phys. (Berlin) 524, 479 (2012).
- [3] J. L. Feng, Annu. Rev. Astron. Astrophys. 48, 495 (2010).
- [4] B. W. Lee and S. Weinberg, Phys. Rev. Lett. 39, 165 (1977).
- [5] M. I. Vysotsky, A. D. Dolgov, and Y. B. Zeldovich, JETP Lett. 26, 188 (1977), http://jetpletters.ru/ps/1375/article_ 20858.shtml.
- [6] K. Marković and M. Viel, Pub. Astron. Soc. Aust. 31, e006 (2014).
- [7] M. Pospelov, A. Ritz, and M. B. Voloshin, Phys. Rev. D 78, 115012 (2008).
- [8] M. Pospelov, A. Ritz, and M. B. Voloshin, Phys. Lett. B 662, 53 (2008).
- [9] S. Dodelson and L. M. Widrow, Phys. Rev. Lett. 72, 17 (1994).
- [10] A. D. Dolgov and S. H. Hansen, Astropart. Phys. 16, 339 (2002).
- [11] J. R. Ellis, D. V. Nanopoulos, and S. Sarkar, Nucl. Phys. B259, 175 (1985).
- [12] J. L. Feng, A. Rajaraman, and F. Takayama, Phys. Rev. D 68, 063504 (2003).
- [13] P. Arias, D. Cadamuro, M. Goodsell, J. Jaeckel, J. Redondo, and A. Ringwald, J. Cosmol. Astropart. Phys. 06 (2012) 013.
- [14] A. Aboubrahim, W. Z. Feng, P. Nath, and Z. Y. Wang, J. High Energy Phys. 06 (2021) 086.

[15] K. Kaneta, H. S. Lee, and S. Yun, Phys. Rev. D 95, 115032 (2017).

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- [16] K. Abe *et al.* (XMASS Collaboration), Phys. Lett. B 787, 153 (2018).
- [17] C. Fu *et al.* (PandaX Collaboration), Phys. Rev. Lett. **119**, 181806 (2017).
- [18] D. S. Akerib *et al.* (LUX Collaboration), Phys. Rev. Lett. 118, 261301 (2017).
- [19] E. Aprile *et al.* (XENON100 Collaboration), Phys. Rev. D 96, 122002 (2017).
- [20] M. Agostini *et al.* (GERDA Collaboration), Phys. Rev. Lett. 125, 011801 (2020).
- [21] T. Aralis *et al.* (SuperCDMS Collaboration), Phys. Rev. D 101, 052008 (2020); 103, 039901(E) (2021).
- [22] E. Armengaud *et al.* (EDELWEISS Collaboration), Phys. Rev. D 98, 082004 (2018).
- [23] S. K. Liu *et al.* (CDEX Collaboration), Phys. Rev. D 95, 052006 (2017).
- [24] N. Abgrall *et al.* (Majorana Collaboration), Phys. Rev. Lett. 118, 161801 (2017).
- [25] G. Angloher *et al.* (CRESST Collaboration), Eur. Phys. J. C 77, 299 (2017).
- [26] P. Adhikari *et al.* (COSINE-100 Collaboration), Astropart. Phys. **114**, 101 (2020).
- [27] Y. S. Liu and G. A. Miller, Phys. Rev. D 96, 016004 (2017).
- [28] Database website, http://physics.nist.gov/PhysRefData/ Xcom/html/xcom1.html.