


Probing μeV ALPs with future LHAASO observations of AGN γ -ray spectra

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 (Received 29 January 2021; revised 8 July 2021; accepted 9 September 2021; published 7 October 2021)

Axionlike particles (ALPs) are predicted in some well-motivated theories beyond the Standard Model. The TeV gamma-rays from active galactic nuclei (AGN) suffer attenuation by the pair production interactions with the cosmic background light (EBL/CMB) during its travel to the earth. The attenuation can be circumvented through photon-ALP conversions in the AGN and Galaxy magnetic-field, and a flux enhancement is expected to arise in the observed spectrum. In this work, we study the potential of the AGN gamma-ray spectrum for energy up to above 100 TeV to probe ALP-parameter space at around μeV , where the coupling $g_{a\gamma}$ is so far relatively weakly constrained. We find the nearby and bright sources, Mrk 501, IC 310 and M 87, are suitable for our objective. Assuming an intrinsic spectrum exponential cutoff energy, we extrapolate the observed spectra of these sources up to above 100 TeV by the models with/without ALPs. For $g_{a\gamma} \gtrsim 2 \times 10^{-11} \text{ GeV}^{-1}$ with $m_a \lesssim 0.5 \mu\text{eV}$, the flux at around 100 TeV predicted by the ALP model can be enhanced more than an order of magnitude than that from the standard absorption, and could be detected by LHAASO. Our result is subject to the uncertainty from the intrinsic cutoff energy and the AGN lobe (or plume) magnetic-field. For an optimistic estimation, the constraint can be improved to $g_{a\gamma} \gtrsim 2 \times 10^{-11} \text{ GeV}^{-1}$ with $m_a \lesssim 1 \mu\text{eV}$. This require further observations on these sources by the forthcoming CTA, LHAASO, SWGO and so on.

DOI: [10.1103/PhysRevD.104.083014](https://doi.org/10.1103/PhysRevD.104.083014)

I. INTRODUCTION

Several extensions of the Standard Model suggest the existence of very light pseudoscalar bosons called axionlike particles (ALPs) [1,2]. These spin-0 neutral particles are a sort of generalization of the axion, which was originally proposed to solve the strong CP problem naturally [3–5], and they are also a promising dark-matter candidate [6–9]. One of their characteristics is their coupling to photons by $g_{a\gamma} \mathbf{E} \cdot \mathbf{B} a$, with $g_{a\gamma}$ being the coupling strength, \mathbf{E} the electric field of the photons, \mathbf{B} an external magnetic field, and a the ALP field strength [10,11]. As a consequence, the phenomenon of photon-ALP mixing take place, and lead to photon-ALP oscillations (or conversions) [10–13]. To reach efficient conversions, they should take place above a critical energy given by [14–16]

$$E_{\text{crit}} \sim 38 \left(\frac{m_a}{10^{-6} \text{ eV}} \right)^2 \left(\frac{10^{-5} \text{ G}}{B} \right) \times \left(\frac{6.5 \times 10^{-11} \text{ GeV}^{-1}}{g_{a\gamma}} \right) \text{ TeV}, \quad (1)$$

where B is the homogeneous magnetic-field component transverse to the propagation direction. In contrast to axion,

ALP mass m_a is independent of $g_{a\gamma}$. Around the critical energy, oscillatory features that depend on the configuration of magnetic field are expected to occur [17].

Many laboratory experiments and astronomical observations are being carried out to search for ALPs via the effect mentioned above. The representative experiments are photon-regenerated experiments, such as “Light shining through a wall” experiments ALPS [18], solar ALPs experiments CAST [19] and dark-matter haloscopes ADMX [20].

Owing to the universal presence of magnetic fields along the line of sight to active galactic nuclei (AGN), photon-ALP oscillations can lead to distinctive signatures in AGN spectra [13–15,21,22]. Thus, ALP-photon coupling can be detected through the observations of AGN (see, e.g., Refs [15,23–26]).

On the one hand, it is possible to detect the ALP-induced observational effects on the γ -rays transparency of the Universe [15,21,23–25,27–31]. The very-high-energy (VHE, above 100 GeV) γ -rays from the extragalactic sources suffer attenuation by pair-production interactions with the background (extragalactic background light, EBL; or cosmic microwave background, CMB) photons during the propagation [32–36]. The attenuation increases with the distance to the source and the energy of the VHE photons [35]. If the photon-ALP conversions exist for a sufficiently large coupling, the emitted photons convert into ALPs and then

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these ALPs reconvert back into photons before arriving in the Earth, i.e., ALPs circumvent pair production. Thus, the opacity of the Universe for VHE gamma-rays is reduced and the observed flux is enhanced significantly (i.e., causing a hardening of the spectra above E_{crit} , see e.g., Refs. [15,16,25,27,29,37–40]). The range of the parameters where ALPs would increase the γ -ray transparency of the Universe (for 1.3 times the optical depth of Franceschini *et al.* EBL model [41]) is constrained from VHE γ -rays observations of blazar (AGN with jet closely aligned to the line of sight) [27]. Data from the Fermi-LAT observations of distant (redshift $z > 0.1$) blazar limit $g_{a\gamma} < 10^{-11} \text{ GeV}^{-1}$ for $m_a < 3 \text{ neV}$ assuming a value of the intergalactic magnetic field strength of 1 nG [31].

On the other hand, taking seriously the irregularities of AGN gamma-ray spectra produced by the oscillations in cluster magnetic-field at energies around E_{crit} , strong bounds on $g_{a\gamma}$ have been derived. In particular, for $0.4 \text{ neV} < m_a < 100 \text{ neV}$, the strongest bounds on $g_{a\gamma}$ are derived from the absence of irregularities in H.E.S.S. and Fermi-LAT observations as well as Fermi-LAT observations of AGN [42–45]. It is worth emphasizing that this method highly depend on the configuration of magnetic-fields adopted [46].

So far, the coupling $g_{a\gamma} < 6.6 \times 10^{-11} \text{ GeV}^{-1}$ for $0.2 \text{ } \mu\text{eV} \lesssim m_a \lesssim 2 \text{ } \mu\text{eV}$, containing viable ALP dark matter parameter space (i.e., $g_{a\gamma} \lesssim 2 \times 10^{-11} \text{ GeV}^{-1}$ for $m_a \sim \mu\text{eV}$) [47], almost have not been limited (see, e.g., Fig. 5 of Ref. [31]), although they are expected to be probed by future experiments (e.g., ALPS II [18], IAXO [48]) or radio-astronomical observations (e.g., Refs. [49–52]). According to Eq. (1), effective oscillations for ALPs at this parameter range take place when the energy of photons is larger than $\sim 38 \text{ TeV}$ for the common value of AGN magnetic-field $B \sim 10^{-5} \text{ G}$ [43,53]. If considering more complicated and larger jet magnetic-field (e.g., 10^{-4} G , in kpc-scale jet), the energy E_{crit} for these ALP parameters can be less than 1 TeV and the method of searching for the ALP-induced irregularities of blazar spectra may work [54]. Nevertheless, the method based on the observational effects on the γ -rays transparency should be ineffective to search for these ALPs (even though the photons with energy $E_{\text{crit}} \lesssim E \lesssim 38 \text{ TeV}$ can convert into ALPs in stronger jet magnetic-field), as the critical energy of reconversion from survival VHE photons to ALPs at Galaxy magnetic-field ($\sim 1 \text{ } \mu\text{G}$) is above 300 TeV. Therefore, photons with energy larger than 38 TeV are required to be detected if probing these ALPs through a reduced opacity for AGN γ -rays. However, the highest energy photons detected from extragalactic sources are only about 20 TeV so far [55,56].

Thanks to the upcoming Large High Altitude Air Shower Observatory (LHAASO [57]) with the ability to survey the TeV sky continuously, it is expected to reach sensitivities

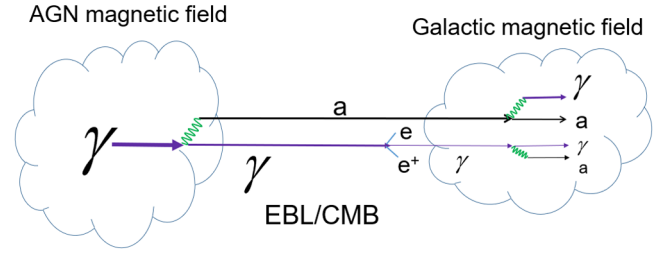


FIG. 1. Cartoon of the formalism adopted in this article inspired by Ref. [23], where the TeV photon (γ , purple line)/ALP (a , black line) beam propagates from the AGN γ -ray source to the Earth. The interaction $\gamma + \gamma_{\text{EBL/CMB}} \rightarrow e^\pm$ takes place during the photon propagation. The photon-ALP conversions (green line) take place in the lobe magnetic-field around the gamma-ray emission region and GMF respectively, leading to an improvement of photon survival probability. There are two $\gamma \rightarrow \gamma$ channels: $\gamma \rightarrow \gamma(e^\pm) \rightarrow \gamma$; $\gamma \rightarrow a \rightarrow \gamma$, and the latter is dominant in this situation.

above 30 TeV about 100 times higher than that of the current VHE instruments (e.g., H.E.S.S. [58], MAGIC [59], VERITAS [60]) [57]. Furthermore, the conversions in the intergalactic magnetic field (IGMF) can be neglected. With current upper limits on the IGMF strength of $\lesssim 10^{-9} \text{ G}$ and on $g_{a\gamma} < 6.6 \times 10^{-11} \text{ GeV}^{-1}$ [19,61], Eq. (1) gives that $E_{\text{crit}} \lesssim 100 \text{ TeV}$ only for $m_a \lesssim 16 \text{ neV}$. Obviously, the unprecedented sensitivities of LHAASO to detect TeV AGN provide a good chance to probe μeV ALPs with the observational effects on the γ -rays transparency.

In this paper, we assume ALPs converted from the gamma-rays photons in the AGN's magnetic field travel unhindered through extragalactic space, and then these ALPs partially back-convert into photons in galactic magnetic field (GMF), see Fig. 1. We investigate the LHAASO sensitivity to detect the ALP-induced flux enhancement at the highest energies by using the extrapolated observations of suitable AGNs for energy up to above 100 TeV, and estimate the corresponding ALP-parameter space.

The paper is structured as follows. In Sec. II we give the formula for evaluating the photon survival probability along the line of sight. The sample selection is described and the data analysis is introduced in Sec. III before presenting our results in Sec. IV. We discuss our model assumptions in Sec. V and conclude in Sec. VI.

II. PHOTON SURVIVAL PROBABILITY

During the propagation from γ -ray emission regions to the Earth, we assume the emitted photons mix with ALPs in the AGN B -field and in the GMF respectively, and undergo the pair production with EBL/CMB in extragalactic space, shown in Fig. 1. The photon survival probability $P_{\gamma \rightarrow \gamma}$ will be calculated under these effects.

A. Photon-ALP conversion

The probability of the conversion from an unpolarized photon to an ALP after passing through a homogeneous magnetic field \mathbf{B} over a distance of length r , is expressed as [26,37,62]

$$P_{\gamma \rightarrow a} = \frac{1}{2} \left[\frac{g_{a\gamma} B}{\Delta_{\text{osc}}(E)} \right]^2 \sin^2 \left[\frac{\Delta_{\text{osc}}(E) r}{2} \right] \quad (2)$$

with $\Delta_{\text{osc}}(E) = g_{a\gamma} B \sqrt{1 + \left(\frac{E_{\text{crit}}}{E} + \frac{E}{E_{\text{H}}} \right)^2}$, where E_{crit} is the critical energy defined in Eq. (1) and E_{H} is derived from the Cotton-Mouton (CM) effect accounting for the photon one-loop vacuum polarization given by [26]

$$E_{\text{H}} = 2.1 \times 10^5 \left(\frac{10^{-5} \text{ G}}{B} \right) \left(\frac{g_{a\gamma}}{10^{-11} \text{ GeV}^{-1}} \right) \text{ GeV}. \quad (3)$$

The factor “1/2” in Eq. (2) results from the average over the photon helicities [53].

$P_{a \rightarrow \gamma}$ ($= 2P_{\gamma \rightarrow a}$) tends to be sizable and constant, when $E_{\text{crit}} < E < E_{\text{H}}$ and $1 \lesssim g_{a\gamma} B r / 2$. For the case of the Galaxy, the latter can be expressed as

$$1 \lesssim \left(\frac{r}{10 \text{ kpc}} \right) \left(\frac{B}{1.23 \mu\text{G}} \right) \left(\frac{g_{a\gamma}}{5 \times 10^{-11} \text{ GeV}^{-1}} \right). \quad (4)$$

Here, we refer to Ref [63] for the values corresponding to r and B .

B. Magnetic field assumption

The magnetic fields around the AGN gamma-ray source commonly include those in the jet, the radio lobes, and the host galaxy. The jet B is believed to decrease as the distance to the central engine along the jet axis [22,64,65]. At the VHE emission region, the typical value of B is in the interval of 0.1–5 G [22,64–68]. The actual field strength in the radio lobes might be of order 1 to a few tens of μG in large [69],

which depends strongly on the lobe size and power. The magnetic field in the host galactic is poorly known and its strength is approximately equal to μG with coherence lengths of the order of 0.1 to 0.2 kpc [22,48,70]. A part of VHE γ – ray AGNs are located in galaxy clusters [38], where the typical B value is 5 μG with coherence lengths of 10–100 kpc [43,48,70].

Our method takes advantage of the ALP-induced flux enhancement. It is more sensitive to the average size of magnetic fields than the complicated magnetic field configuration and detail with considerable uncertainty [22,27,43]. Furthermore, our study only give a estimation of LHAASO sensitivity to probe ALPs. Therefore, for simplicity, we assume the “source” magnetic-field is homogeneous. According to Eqs. (1) and (3), the optimal size of magnetic field to probe the μeV ALPs within the preponderant energy range of LHAASO ($E > 30 \text{ TeV}$) is $\sim 10 \mu\text{G}$. The magnetic-field at the VHE region is so high that the leading role played by the CM effect suppresses the photon-ALP conversion while the galaxy one is too weak, so the lobe B-field is expected to be responsible for the conversion site around the gamma-ray source. In this paper, the diffuse structures located at the terminal of the jet including plumes are collectively referred to as “lobes.” If the γ -ray source locates in the cluster and thus the lobe should be inside the cluster too, we only consider the cluster B-field in the lobe and the lobe B-field should be stronger than without cluster.

Due to the uncertainty of the lobe magnetic-field, we discuss the values of the B-field parameters including the strength B_s and region size r_s with two scenarios in our study. In the scenario of fiducial (slightly conservative) parameters, they are mainly inferred from observations for each source, see Sec. III and the fiducial parameters in Table I for details. In present, almost all of detected TeV AGN are Fanaroff-Riley I (FR I) radio galaxies and their aligned counterparts BL Lacs [71]. Due to the low luminosity for this type AGN and their lobe [72], the upper bound of B_s should be $\sim 10 \mu\text{G}$, and thus we take

TABLE I. Magnetic fields and the best-fitting intrinsic spectra for the sources in the fiducial and optimistic cases. The values of the B-field parameters including the size of the homogeneous B-field B_s and region scale r_s respond to the AGN lobe. α is the photon index of the chosen intrinsic spectrum determined by the best fit. The BPLC spectrum has two spectral indices. In the fiducial case, the values of B_s are mainly inferred from references and r_s is conservatively assumed to 10 kpc. The minimum cutoff energy E_c is determined by the best-fitting of ψ_0 (Eq. (7), without ALP) to the observed spectrum, where the goodness of fit is measured by the minimum chi-square on every degree of freedom ($\chi^2/\text{d.o.f.}$). In the optimistic scenario, the values of B_s are roughly equal to the upper limit of the FR I and BL Lacs lobe. While the value of r_s is motivated from the assumption that the TeV sources are acceleration sites of high energy cosmic rays up to 10^{19} eV at most [14,53], where B_s and r_s are satisfied the famous “Hillas condition.” We take the cutoff energy $E_c = 100 \text{ TeV}$ which is larger than the minimum one and the minimum $\chi^2/\text{d.o.f.}$ remains unchanged. See text for further details.

Source	Fiducial			Intrinsic spectrum		Optimistic			Intrinsic spectrum	
	B_s (μG)	r_s (kpc)	E_c (TeV)	α (model)	$\chi^2/\text{d.o.f.}$	B_s (μG)	r_s (kpc)	E_c (TeV)	α (model)	$\chi^2/\text{d.o.f.}$
M 87	5	10	90	2.1 (PLC)	1.2	10	10	100	2.1 (PLC)	1.2
IC 310	2	10	40	1.13,1.78 (BPLC)	0.18	10	10	100	1.18,1.74 (BPLC)	0.18
Mrk 501	2	10	70	1.83,2.54 (BPLC)	1.4	10	10	100	1.83,2.58 (BPLC)	1.4

$B_s = 10 \mu\text{G}$ as the optimistic B value of the lobe, see Table I. Besides, the AGN lobe is expected to be the candidate for ultrahigh-energy cosmic rays sources, where the cosmic rays can be accelerated up to $\geq 10^{19}$ eV and the ‘‘Hillas condition’’ is satisfied. Then the size of conversion region satisfies $r_s \geq 10$ kpc for $B_s = 10 \mu\text{G}$. Coincidentally, the condition (4) is also automatically satisfied for the value of g_{11} ($= g_{a\gamma} \times 10^{11}$ GeV) relevant to the present paper [14,53]. Therefore, in the optimistic scenario, we assume $r_s = 10$ kpc, where we take the lower limit of r_s given that the B value is significantly large (even if larger r_s were considered, the change on the conversion probability could be small due to the strong conversion conditions (3) and (4) have already been satisfied). Note that the optimistic values of B-field were also applied in Refs. [14,53] and suggested in Refs. [48] for the photon-ALP mixing in AGN jet or lobe.

For the Galactic magnetic field (GMF), an average value of $B_{\text{GMF}} = 1.23 \mu\text{G}$ with scale 10 kpc is assumed in our model [63].

According to Eq. (4), the minimum coupling g_{11} reaching the significant transformation is about 2.5 for the GMF. As the larger B_s , the minimum g_{11} corresponding to the conversion in the source can be low to 1. Analogously, the critical energy for the conversion in the GMF, ~ 300 TeV for $g_{11} \simeq 6.5$, $m_a \simeq 1 \mu\text{eV}$, is higher than that (the critical energy) for the source. However, the CM effect can suppress the source conversion above 210 TeV for $g_{11} = 1$ due to the larger B_s , as seen in Eq. (3), and it can be neglected in the case of GMF for the energy considered in this paper.

For more realistic models of jet magnetic-fields in connection with photon-ALP oscillations, the recent work in Ref. [54] has investigated the effects of more complicated jet magnetic field configurations on the irregularities of GeV-10 TeV spectrum. They find that this method can be used to search 1–1000 neV ALP with $g_{a\gamma} \gtrsim 5 \times 10^{-12}$ GeV $^{-1}$.

We neglect the photon-photon dispersion effect on the propagation of TeV gamma rays. First, the dispersion contributed by CMB is dominant in the energy range of 100 GeV to 1000 TeV, even though radiation in the Galaxy or the source regions can far exceed the CMB [73]. Therefore, we only consider the CMB dispersion. Second, the CMB dispersion term in mixing matrix is $\Delta_{\text{CMB}} \simeq 8 \times (\frac{E}{100 \text{ TeV}}) \text{ Mpc}^{-1}$, and the photon-ALP mixing term $\Delta_{a\gamma} \simeq 15 (\frac{g_{a\gamma}}{10^{-11} \text{ GeV}^{-1}}) (\frac{B}{10^{-6} \text{ G}}) \text{ Mpc}^{-1}$. When $\Delta_{\text{CMB}} > 2\Delta_{a\gamma}$, the dispersion effect is more important than the mixing, see, e.g., Supplementary Material of Ref. [30]. Thus, the dispersion effect usually plays an important role in weaker magnetic field, e.g., the IGMF [30,40]. But the photon-ALP mixing in IGMF is completely negligible in this work. For the Galaxy magnetic-field ($\sim 1 \mu\text{G}$) and the coupling ($\gtrsim 10^{-11}$ GeV $^{-1}$) relevant to the present paper, the dispersion effect is important only when $E \gtrsim 460$ TeV.

C. Photon survival probability

We employ the EBL model of Ref. [74] to account the VHE photon absorption onto the EBL. This recent EBL model has been tested repeatedly and is generally consistent with the VHE γ -ray observations (e.g., Ref. [75–82]). Furthermore, the infrared EBL intensity from this model is in the mid-level among several recent EBL models [41,83,84], which are more inconsistent but basically match the direct measurements at infrared band [85]. Hence, choosing this model to account the EBL optical depth is helpful to reduce EBL uncertainty. Above 140 TeV, the CMB optical depth of TeV photons becomes dominant as its intensity is much stronger than the EBL’s at the wavelength longer than 400 μm .

After obtaining the EBL/CMB spectrum, we can further estimate the optical depth $\tau_{\gamma\gamma}(E, z)$ for the photon with energy E from the source of redshift z [74,86]. Then, the photon survival probability on the whole path from the source to the earth can be derived

$$P_{\gamma \rightarrow \gamma} = P_{\gamma \rightarrow \gamma}^{\text{S}} \exp(-\tau_{\gamma\gamma}) P_{\gamma \rightarrow \gamma}^{\text{G}} + P_{\gamma \rightarrow a}^{\text{S}} P_{a \rightarrow \gamma}^{\text{G}}, \quad (5)$$

where $P_{\gamma \rightarrow a}^{\text{S}}$ and $P_{a \rightarrow \gamma}^{\text{S}}$ are the conversion probabilities from photons/ALPs to ALPs/photons in the source respectively. There is a relation $P_{\gamma \rightarrow \gamma}^{\text{S}} = 1 - P_{\gamma \rightarrow a}^{\text{S}}$; Similarly, the variables with a superscript ‘‘G’’ represent those for the GMF. The derivation of Eq. (5) can be illustrated vividly in Fig. 1: the first term corresponds to $\gamma \rightarrow \gamma(e^\pm) \rightarrow \gamma$ channel suffered from EBL/CMB absorption. the second is related to $\gamma \rightarrow a \rightarrow \gamma$ channel unaffected by the absorption.

Figure 2 shows the change of $P_{\gamma \rightarrow \gamma}(E, z)$ with energy E for different z , where the ALP mass $m_a = 1 \mu\text{eV}$ and coupling $g_{11} = 3$. $P_2 = P_{\gamma \rightarrow \gamma}^{\text{S}} \exp(-\tau_{\gamma\gamma}(E, 0.01)) P_{\gamma \rightarrow \gamma}^{\text{G}}$ and $P_1 = P_{\gamma \rightarrow a}^{\text{S}} P_{a \rightarrow \gamma}^{\text{G}}$, i.e., the first and second term in Eq. (5). In the low energy region, the conversion is noneffective and $P_{\gamma \rightarrow \gamma}(E, z)$ is dominated by the absorption term $P_2 \sim \exp(-\tau_{\gamma\gamma})$. As the energy turns to the higher region, $\exp(-\tau_{\gamma\gamma}) \rightarrow 0$, while the channel $\gamma \rightarrow a \rightarrow \gamma$ is getting ‘‘wider’’, and hence $P_{\gamma \rightarrow \gamma} \simeq P_1$, which is independent of z . As a consequence, the curves of $P_{\gamma \rightarrow \gamma}(E, z)$ for different z at high energy region show v-shaped lines, and converge to P_1 . When $E > E_{\text{crit}}$, P_1 is getting closer and closer to its maximum, and when $E > E_{\text{H}} \approx 630$ TeV, the CM effect suppresses the source conversion. Thus the peak appears at the highest energy band. Note that since we do not concern the spectral irregularities, we take the average value for the square of the sine function in Eq. (2) when the phase is larger than 1 rad, e.g., according to Refs. [14,53,87], smearing out the rapid-oscillatory features of the probability function. The average value is approximatively taken 2/3 rather than 1/2 to match the saturation-conversion probability ($P_{\gamma \rightarrow a}$) of 1/3, which corresponds to a more realistic scenario the beam propagates through many

domains of randomly oriented magnetic fields with constant size B , for instance, in Refs. [28,87].

In the limit of saturated conversion $E_{\text{crit}} \ll E \ll E_{\text{H}}$ and $1 < g_{a\gamma}Br/2$, about

$$P_{\gamma \rightarrow a}^{\text{S}} P_{a \rightarrow \gamma}^{\text{G}} = \frac{1}{3} \times \frac{2}{3} \quad (6)$$

of the original photons survive through $\gamma \rightarrow a \rightarrow \gamma$ channel. Obviously, for the ALP-parameter value applied to Fig. 2, the condition of the saturated conversion does not match, for example $g_{a\gamma}B_{\text{GMF}}r_{\text{GMF}}/2 < 1$.

III. METHOD

A. Sample selection

In our method, the VHE γ -ray observations are utilized to model the intrinsic spectrum of the emitted source. So far about 75 VHE AGN have been detected by the VHE instruments [71]. In principle, most of these sources may be used to search for the ALP-induced flux boost since it is independent of the redshift above E_{crit} , as shown in Fig. 2. But we should acquire as many data below E_{crit} as possible, which are expected to be slightly affected by the ALPs, so that a more realistic spectrum at higher energy could be extrapolated by the observations together with the assumed model (see Eq. (7)). Hence, we preferentially consider the nearby sources whose $P_{\gamma \rightarrow \gamma}$ curve can show a ‘‘shallow valley’’ due to the relatively slight $\gamma\gamma$ -absorption (see Fig. 2).

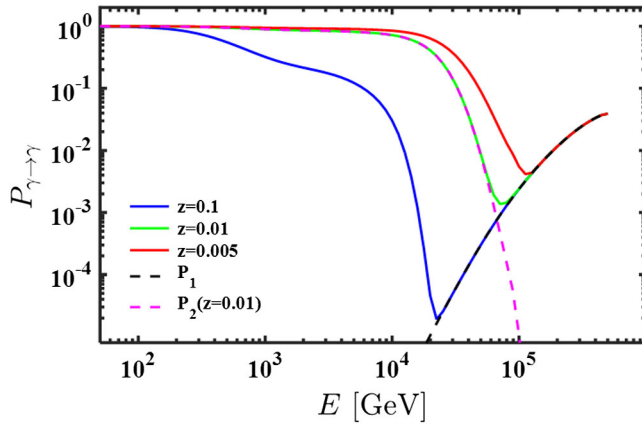


FIG. 2. The photon survival probability $P_{\gamma \rightarrow \gamma}(E, z)$ on the whole path from the γ -ray source to the earth for the optimistic B-field parameters, where the ALP mass $m_a = 1 \mu\text{eV}$ and coupling $g_{11} = 3$. The meaning of each colored curve is annotated in the diagram. $P_1 = P_{\gamma \rightarrow a}^{\text{S}} P_{a \rightarrow \gamma}^{\text{G}}$ and $P_2 = P_{\gamma \rightarrow \gamma}^{\text{S}} \exp(-\tau_{\gamma\gamma}(E, 0.01)) P_{\gamma \rightarrow \gamma}^{\text{G}}$, i.e., the second and first (redshift-independent) term in Eq. (5). They correspond to the channels of $\gamma \rightarrow a \rightarrow \gamma$ and $\gamma \rightarrow \gamma(e^\pm) \rightarrow \gamma$ shown in Fig. 1, respectively.

Based on the study of Franceschini *et al.* [88], the adjacent sources of M 87, IC 310 and Mkn 501 would likely be detected by LHAASO up to 75 TeV, 50 TeV, 25 TeV respectively, when taking into account the standard EBL-absorption. Thus, we predict that they could provide more detectable data below E_{crit} . In this paper, we will fit and extrapolate the spectral data of these sources to the highest VHE energies.

M 87(Gal Long: 283.74, Gal Lat: 74.49; $z = 0.004$)—a giant radio galaxy of FR I with kpc radio jet, located in the Virgo Cluster. It has been detected by almost all the Imaging Air Cherenkov telescopes (IACTs) [89]. Strong and rapid flux variability in gamma-ray band was shown, but no significant spectral changes with a typical photon index of 2.2 [89–91]. We adopt H.E.S.S. data taken during 21 h of effective observation, during the 2005 12. Feb.-15. May high state (see Fig. 3).

From the results of minimum-pressure analysis for the magnetic fields, which have combined the radio imaging of the large-scale radio structure of M 87 with the VLA at 90 cm, the B-fields at different sites of the lobe within a region about 40 kpc in size are greater than or equal to $6.9 \mu\text{G}$, see Table I in Ref. [92]. Hence, we conservatively assume a homogeneous B-field for the lobe with strength $5 \mu\text{G}$, as shown in Table I.

IC 310(Gal Long: 150.8, Gal Lat: -13.3; $z = 0.019$)—seems to be a transitional AGN between a low-luminosity HBL (high-frequency peaked BL Lac, namely blazar with weak optical emission lines [72]) and a radio galaxy [88], located on the outskirts of the Perseus galaxy cluster. An extraordinary TeV flare in 2012 Nov. 12-13 and then a low state during several of the following months was detected by MAGIC [93]. A high state also has been observed by the MAGIC telescopes between 2009 October and 2010 February. The photon spectral index at VHE band is 2 during an effective observation of 3.5 h in the (2009/2010) high state, and in this paper we adopt this high state observations together with the first three year (2008-2011) data taken with Fermi-LAT [94] (see Fig. 3).

This head-tail radio galaxy has a radio lobe with a length of about 350 kpc ($15'$) [95,96]. The equipartition values of the lobe magnetic-field derived by Ref. [95] (Table 2) decrease from $4.3 \mu\text{G}$ at a distance of 10 kpc to the core to $1.9 \mu\text{G}$ at 140 kpc. However, based on the observation at 610 MHz, Fig. 10 of Ref. [97] shows that the equipartition magnetic-field decrease from $3 \mu\text{G}$ at a distance of about 1 kpc to the head to $1.5 \mu\text{G}$ at 70 kpc. Besides, from an XMM-Newton observation of IC 310, Ref. [96] derived the lower limit of the magnetic field strength to be $B > 1 \mu\text{G}$. Accordingly, we assume the strength of the lobe B-field is $2 \mu\text{G}$, as shown in Table I.

Mrk 501(Gal Long: 60.3, Gal Lat: 38.86; $z = 0.034$)—the next-closest known HBL. It is known for showing the spectral variability at VHE band. During a long outburst observed with HEGRA in 1997, the source showed a very

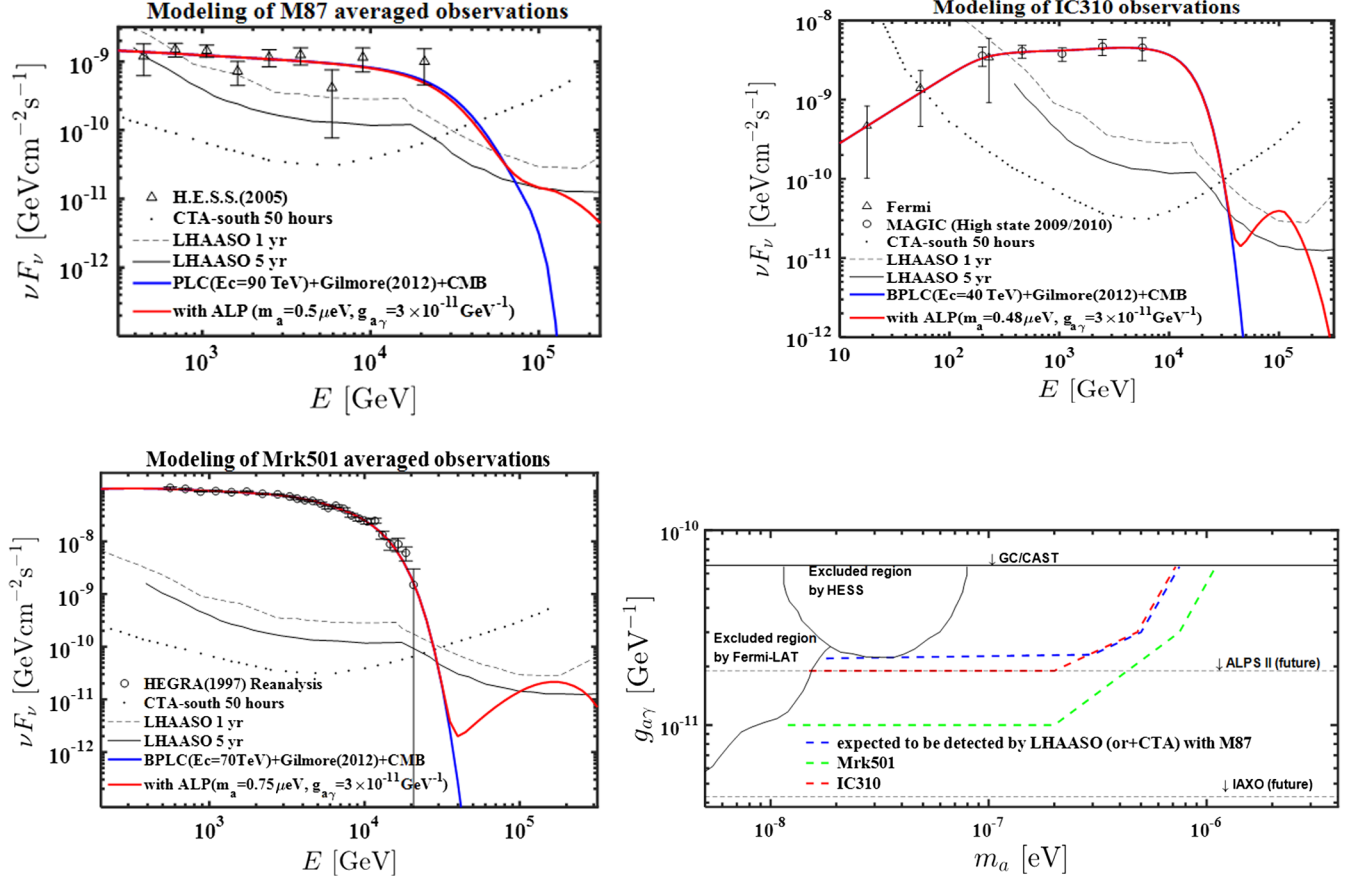


FIG. 3. The results for the fiducial parameters in Table I. Top panel and left of the bottom panels: fitting and extrapolating the observations of M 87, IC 310 and Mrk 501. The blue and red lines represents respectively the PLC or BPLC fit with the EBL (Gilmore)/CMB-absorption correction and that considering further the photon-ALP conversion and the CM effect. E_c is the minimum cut-off energy allowed by the best-fitting intrinsic spectrum. The meaning of other symbols are indicated in the legend. Right of the bottom panel: expected ALP limits, based on our model as well as the future LHAASO (or + CTA) observations of M 87 (blue dash line), Mrk 501 (green dash line) and IC 310 (red dash line). For comparison, limits (black line) and 5σ sensitivities of future experiments (black dashed line) are also shown.

hard intrinsic spectrum with no softening up to the highest-energy detected photons of 20 TeV [88,98]. We choose this spectrum that is detected during much of the 110 h observation time, spread over 6 months [98] (see Fig. 3). It is worth mentioning that, on the night of 2014 June 23-24, a flare comparable to the 1997 maximum was observed by HESS [56].

There are no precise observations for the lobe of the BL Lac Mrk 501. But BL Lacs are the aligned counterparts of FR I radio galaxies in the famous unified schemes for radio-loud AGN [72]. Hence, we assume that the lobe B-field for this source is the same as IC 310, which is classified into a transitional population between BL Lac objects and FR I radio galaxies [94]. Furthermore, there is observational evidence that Mrk 501 is also a member of a small cluster [99,100]. This source is believed to be located in galaxy clusters by Ref. [38] in the study of the photon-ALP mixing. Hence, it seems reasonable to assume $B_s = 2 \mu\text{G}$.

For simply, we conservatively assume the region sizes of the lobe B-field for the three sources $r_s = 10$ kpc in our fiducial scenario, as shown in Table I.

Finally, we model the Galaxy B-field with a homogeneous and isotropic field, however the realistic magnetic field in the Milky Way depends on the source position in the sky and thus the back-conversion probability $P_{a\gamma}^G$ for an ALP at the edge of the Galaxy to convert into a photon at Earth also depends on the source position [38]. Therefore we should ensure our sample at least are not in the position with relatively weak conversion. With the help of Fig. 2 in Refs. [38], which gives an illustrative sky map of the line-of-sight dependent probability for the common Jansson and Farrar magnetic field model [43,101], we find the three sources under consideration are just located in regions where the back-conversion probabilities are in the moderate intensity range. Also NGC 1275 (NGC 1275 and IC 310 are both in the Perseus galaxy cluster) [43] and Mrk 501

[27,38,40] have been studied to research ALPs involving photon-ALP conversion in the Galaxy B-field.

B. Theoretical and intrinsic spectra

We model VHE gamma-ray spectra with

$$\psi_0 = e^{-\tau_{\gamma\gamma}} \phi \quad \text{or} \quad \psi_1 = P_{\gamma \rightarrow \gamma} \phi, \quad (7)$$

where $P_{\gamma \rightarrow \gamma}$ and $\tau_{\gamma\gamma}$ are defined in Eq. (5). ϕ represents the intrinsic spectrum assumed for the sources. The model with ALP has two additional free parameters, $g_{a\gamma}$ and m_a , relative to the traditional model.

ϕ is assumed as one of the three common models [76]: power-law with exponential cut-off (PLC), log-parabola with exponential cut-off (LPC) and broken power-law with exponential cut-off (BPLC). The PLC spectrum is described by three parameters: $\phi_{\text{PLC}} = \phi_0 (E/E_0)^{-\alpha} \exp(-E/E_c)$, where E_c is the cutoff energy, α is the photon spectral index constrained by the particle acceleration theory as $\alpha \geq 1.5$, ϕ_0 is the flux normalization, and E_0 is the fixed reference energy. While the LPC spectrum has additional curvature parameter $t > 0$: $\phi_{\text{LPC}} = \phi_0 (E/E_0)^{-s-t \log(E/E_0)} \exp(-E/E_c)$ and also $\langle s + t \log(E/E_0) \rangle \geq 1.5$. The BPLC spectrum $\phi_{\text{BPLC}} = \phi_0 (E/E_0)^{-\alpha_1} [1 + (\frac{E}{E_0})^g]^{\frac{\alpha_1 - \alpha_2}{g}} \exp(-E/E_c)$ has 5 parameters.

Since the EBL absorption-corrected spectrum of Mrk 501 and even the other two observed ones in our samples are hard with no sign of convergence, the observations together with the chosen intrinsic spectrum only can give a relatively weak constraint on E_c and in principle give the minimum E_c above which the goodness of best-fit (parametrized by the minimum $\chi^2/\text{d.o.f.}$) remains unchanged. Here, we take the minimum E_c as the fiducial value, see Sec. IV and Table I. The highest energy of the detected photons in our samples is $\lesssim 20$ TeV, therefore the minimum E_c determined by the observations should above 20 TeV. If the parent particles responsible for the VHE emission are electrons, the cutoff can be derived from the Klein-Nishina suppression, energy loss of the electrons and pair attenuation in the VHE emission region (see, e.g., [102–107]), and the cutoff is more likely to be less than 100 TeV. Hence, we uniformly take $E_c = 100$ TeV as the optimistical one for our samples [88], even though E_c could be higher if the VHE γ -ray emission is of a hadronic origin [57,108].

C. Fitting and extrapolating the observations

To simulate the observations at the highest energies, we first fit the three observed spectra with ψ_0 and extrapolate it to hundreds of TeV energies, respectively. Meanwhile, the form (PLC, LPC or BPLC) of intrinsic spectrum ϕ to be chosen for each source is determined in terms of its minimum chi-square value per degree of freedom ($\chi^2/\text{d.o.f.}$), and we find the minimum E_c above which the goodness of fit of ψ_0 with the best chosen ϕ remains

unchanged. Then, we use ψ_1 containing the determined ϕ and $P_{\gamma \rightarrow \gamma}$ to fit and extrapolate the observations of each source, under the given fiducial B_s , r_s , $g_{a\gamma}$ and m_a .

We repeat the process above with the optimistic parameters in Table I for the optimistic case. In this process, we take $E_c = 100$ TeV for the chosen intrinsic spectrum ϕ above, but other parameters of ϕ such as the spectral index can change when fitting.

We assume if the ALP-induced flux enhancement $\frac{\psi_1}{\psi_0}$ is more than one order of magnitude and the predicted spectra ψ_1 is over the equipment sensitivity, then the given ALP could be constrained. As the continuity and (approximative) monotonicity of $P_{\gamma \rightarrow \gamma}$, we only need to test the ALP parameters with small $g_{a\gamma}$ and that with large m_a to obtain the constrained region.

IV. RESULTS

Crucial parameters for the best-fitting intrinsic spectra and the goodness of fit $\chi^2/\text{d.o.f.}$ are listed in Table I. Fig. 3, Fig. 7 in the Appendix and Fig. 4 report the predicted sensitivity limits for future LHAASO/CTA observations of the three most promising nearby AGNs. Fig. 3 together with Fig. 7 correspond to the fiducial parameters in Table I and Fig. 4 the optimistic ones. The blue line in Fig. 3 and Fig. 7 represents the standard absorption fit including an extrapolation above 100 TeV. The results corresponding to the minimum allowable coupling $g_{a\gamma}$ for different mass m_a are shown by the red line. The 50-h 5σ sensitivity limits for CTA, 5-year and 1-year 5σ limits for LHAASO are shown with the black dotted line, the black dashed line and the black solid line, respectively. Combined observations from the instruments will reach sensitivities of a few times $10^{-11} \text{ GeV cm}^{-1} \text{ s}^{-1}$.

M 87. The best-fitting intrinsic spectrum for the VHE observations is PLC with goodness of fit $\chi^2/\text{d.o.f.} = 1.2$.

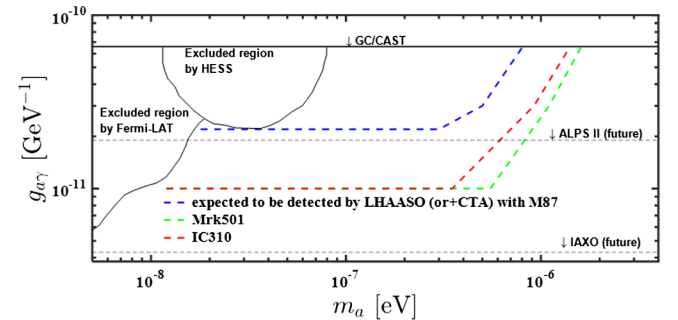


FIG. 4. The expected ALP limits on our model as well as the future LHAASO (or + CTA) observations on the three sources for the optimistic parameters in Table I. For these limited parameters, the ALP-induced flux enhancement is more than an order of magnitude. The limit from Mrk 501 and M 87 are predicted with 5-years sensitivity of LHAASO and IC 310 with one year. The meanings of various symbols in the diagram are the same as Fig. 3.

and the minimum cutoff energy is $E_c = 90$ TeV, see Fig. 3 and Fig. 7. The predicted spectra extrapolated by the best-fitting model (ψ_0 and ψ_1) are above the 5-year sensitivity of LHAASO up to 70 TeV (this will allow measurements of the M 87 spectrum up to about 70 TeV), which is beneficial to constrain the intrinsic spectrum. Above 100 TeV, the photon-ALP conversion gradually become important so that the photons survive mainly through $\gamma \rightarrow a \rightarrow \gamma$ channel. Consequently, the flux enhancement is more than an order of magnitude and the flux is over the LHAASO sensitivity around 100 TeV for three given ALP-parameter values. The line of ψ_1 take a very shallow “valley” or descending shape, as the low redshift of M 87 lead to a smooth transition of survival probability $P_{\gamma \rightarrow \gamma} \approx P_1$ to $P_{\gamma \rightarrow \gamma} \approx P_2$. At the highest energy band, the intrinsic-spectrum cutoff makes the curve go down.

IC 310. The spectrum shows an obvious break at 200 GeV and a BPLC model can fit the spectrum very well with goodness of fit $\chi^2/\text{d.o.f.} = 0.18$, see Fig. 3 and Fig. 7. The minimum cutoff energy is constrained to $E_c = 40$ TeV. The predicted spectra extrapolated by the best-fitting model (ψ_0 and ψ_1) are above the sensitivity of LHAASO up to about 30 TeV, which theoretically will allow measurements of the IC 310 spectrum up to 30 TeV. Above ~ 50 TeV, the photon-ALP conversion gradually become important, so that the flux enhancement is over an order of magnitude and is above the one-year LHAASO sensitivity around about 100 TeV. But the intrinsic-spectrum cutoff or it together with the CM effect makes the curve turn down at the highest energy band.

Mrk 501. The spectrum after EBL-absorption correction obviously takes the shape of a broken power-law [88], so the best-fitting intrinsic spectrum is BLPC with goodness of fit $\chi^2/\text{d.o.f.} = 1.4$, see Fig. 3 and Fig. 7. The minimum cutoff energy is $E_c = 70$ TeV. The predicted observed spectrum without ALP is over the five-years sensitivity of LHAASO up to about 30 TeV, which theoretically will give a relatively weak constraint on the intrinsic spectrum up to above 100 TeV. The very prominent enhanced flux at around 100 TeV is over the LHAASO sensitivity.

We estimate the ALP parameter space that will be possible probed by the future LHAASO (or + CTA) observations in the last picture of Fig. 3 for the fiducial scenario, where other limits and sensitivity projections are also given for comparing. For M 87, LHAASO would be able to explore g_{11} down to about 2.3 for $m_a < 0.3 \mu\text{eV}$. For IC 310 and Mrk 501, a lower value of $g_{11} \simeq 1.9$ for $m_a < 0.2 \mu\text{eV}$ and $g_{11} \simeq 1$ for $m_a < 0.2 \mu\text{eV}$ would be explored respectively, some of which is invoked to explain the cold dark matter [43]. The results corresponding to Mrk 501 give the strongest exploitable bound on the coupling for $m_a \lesssim 0.5 \mu\text{eV}$: $g_{11} \simeq 2$. In the case of M 87, a relatively weak bound is given, as its observed flux is lower and its lower redshift leads to that higher energy is required to achieve the same enhancement.

For the optimistic scenario in Table I, the ALP parameter space that will be possible probed is shown as Fig. 4. No surprise, it predicts stronger restrictions than the fiducial scenario. For M 87, the ALP parameters expected to be probed are almost unchanged compared to the fiducial scenario, though the source B-field increases by a factor 2 and the cutoff energy increase to 100 TeV from 90 TeV. In the case of IC 310, the limited parameter space significantly expands to $g_{11} \gtrsim 2$ for $m_a \lesssim 0.35 \mu\text{eV}$, benefiting from the increase of cutoff energy from 40 TeV to 100 TeV and increases of the source B-field by a factor 5. Though the parameter region from Mrk 501 becomes wider owing to the increase of cutoff energy from 70 TeV to 100 TeV and increases (same as IC 310), it is only slightly larger than that from IC 310. Therefore, the result seems to more sensitive to the cutoff energy than the source B-field.

V. DISCUSSION

In this section, we will discuss our model assumptions about the source B-field, the cutoff energy of the intrinsic spectrum and the results from IC 310.

As one of the effective conversion conditions requires the photon energy to satisfy $E_{\text{crit}} < E < E_{\text{H}}$ and depends on the B – field, particularly the highest energy conversions in the source B – field is prone to be suppressed by the CM effect. Therefore, the uncertainty of B_s can translate into an uncertainty of the photon survival probability and our result. Fig. 5 shows how B_s affects $P_{\gamma \rightarrow \gamma}$ for a fixed redshift $z = 0.005$ and ALP parameters $m_a = 1 \mu\text{eV}$, $g_{11} = 3$. For B_s in the range from $5 \mu\text{G}$ to $20 \mu\text{G}$ (even if $B_s \gtrsim 20 \mu\text{G}$ were too high and unrealistic for FR I lobe), the photon survival probabilities are close around 200 TeV. When $B_s = 2 \mu\text{G}$, the critical energy of photon-ALP conversion is higher, and thus the ALP-induced enhancement occurs at higher energy. The CM effect almost completely suppresses the photon-ALP conversion for $B_s = 50 \mu\text{G}$.

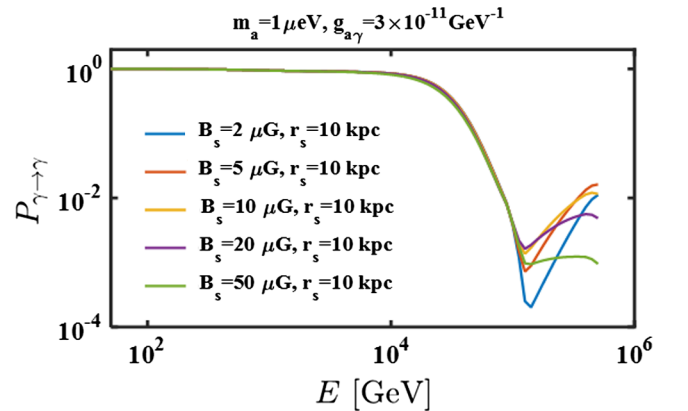


FIG. 5. The photon survival probabilities $P_{\gamma \rightarrow \gamma}$ for different values of the source field magnetic B_s . The redshift $z = 0.005$ and field-magnetic region $r_s = 10$ kpc. For B_s in the range from $5 \mu\text{G}$ to $20 \mu\text{G}$ (even if $B_s \gtrsim 20 \mu\text{G}$ were too high and unrealistic for FR I lobe), the photon survival probabilities are close around 200 TeV. When $B_s = 2 \mu\text{G}$, the critical energy of photon-ALP conversion is higher, and thus the ALP-induced enhancement occurs at higher energy. The CM effect almost completely suppresses the photon-ALP conversion for $B_s = 50 \mu\text{G}$.

TABLE II. The lobe magnetic fields and intrinsic spectra with a certain cutoff energy $E_c = 20$ TeV for every source. The values of the B-field parameters are fiducial as in Table I, while we take smaller cutoff energy $E_c = 20$ TeV even though it is disfavor by the current limited observations, i.e., the minimum $\chi^2/\text{d.o.f.}$ of the ψ_0 (without ALP) fitting for each spectrum is significantly larger.

Source	$B_s(\mu\text{G})$	$r_s(\text{kpc})$	$E_c(\text{TeV})$	$\alpha(\text{model})$	$\chi^2/\text{d.o.f.}$
M 87	5	10	20	2.1 (PLC)	1.4
IC 310	2	10	20	1.18,1.74 (BPLC)	0.23
Mrk 501	2	10	20	1.83,2.28 (BPLC)	1.6

the photon survival probabilities are close at around 200 TeV. It means that provided B_s is between $5 \mu\text{G}$ and $20 \mu\text{G}$ the ALP-induced flux enhancement could be achieved and comparable as done with $B_s = 10 \mu\text{G}$ above. When $B_s = 2 \mu\text{G}$, the critical energy of photon-ALP conversion is close to 100 TeV, and thus the ALP-induced enhancement occurs at higher energy. At the highest energy, $P_{\gamma \rightarrow \gamma}$ for $B_s = 2 \mu\text{G}$ can rise to that resulted from $B_s = 10 \mu\text{G}$. When the mass m_a is larger or the coupling $g_{a\gamma}$ is smaller and thus the critical energy is higher, $P_{\gamma \rightarrow \gamma}$ with $B_s = 10 \mu\text{G}$ can be about a factor five larger than $P_{\gamma \rightarrow \gamma}$ with $B_s = 2 \mu\text{G}$, as shown in Fig. 5.

But the intrinsic spectral exponential cutoff can lead to an exponential reduction of the source photons and thus indirectly reduce the photon-survival possibility with the same way. It means that our results are more sensitive to the uncertainty from the cutoff energy than the source B-field.

Our results are sensitive to the cutoff energy E_c , as the predicted photons around 100 TeV are mainly from the conversion channel $\gamma \rightarrow a \rightarrow \gamma$. In the fiducial scenario, the minimum cutoff energy is constrained by a

limited amount of observations and the assumed intrinsic spectrum. The cutoff energy might still be more lower if it were obtained by fitting more comprehensive observations, especially those at higher energy. We therefore investigate the limit, where we assume the cutoff energy E_c is equal to the highest photon energy of 20 TeV in our sample. Crucial parameters for the best-fitting intrinsic spectra and the goodness of fit $\chi^2/\text{d.o.f.}$ are listed in Table II. The goodness of fit ($\chi^2/\text{d.o.f.}$) in this case is noticeably worse compared to the fiducial case. The B-field parameters are the same as the fiducial ones. We find the limited ALP-parameter region drastically reduces to $g_{11} \gtrsim 2$ with $m_a \lesssim 0.3 \mu\text{eV}$ and M 87 can not give any constraint due to the weak detectable ALP-induced enhancement, see Fig. 6.

We discuss the possible of $E_c = 100$ TeV assumed in the optimistic case in two ways below.

First, the optical depths due to internal pair-creation at such high energy can lead to an intrinsic spectral cutoff. In simple one-zone SSC scenarios, if requiring the optical depth τ less than 1, then the jet Doppler factor must satisfy (e.g., Refs. [107,109])

$$\delta \gtrsim 8.6(1+z)^{\frac{1}{3}} \left(\frac{E}{100 \text{ TeV}} \frac{F_0}{10^{-11} \text{ erg cm}^{-2} \text{ s}^{-1}} \frac{1 \text{ day}}{t_{\text{var}}} \right)^{\frac{1}{6}}, \quad (8)$$

where F_0 is the observed monochromatic flux energy density as measured at the observed photon energy ϵ_0 , t_{var} is an observed minimum (typical) variability time scale, and $\epsilon_0 \simeq 0.5 \left(\frac{100 \text{ TeV}}{E} \right) \left(\frac{\delta}{10} \right)^2 \text{ eV}$. Usually, the flux F_0 increases slowly with the photon energy ϵ_0 and thus with δ up to the synchrotron peak, see e.g., Refs. [107]. Hence, we fix F_0 at near-infrared energy $\epsilon_0 \simeq 1 \text{ eV}$ ($2.4 \times 10^{14} \text{ Hz}$) for $E = 100 \text{ TeV}$ and $\delta \simeq 14$. For Mrk

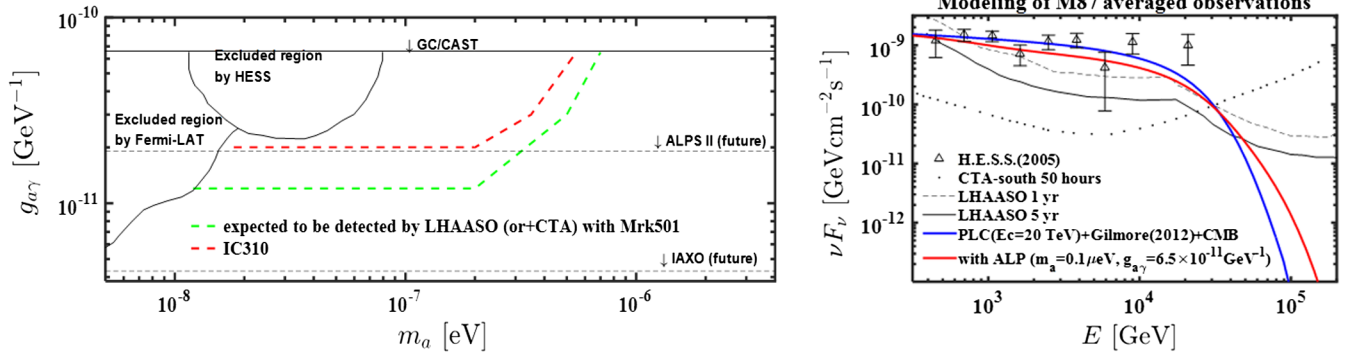


FIG. 6. The results for the parameters in Table II, where the cutoff energy $E_c = 20$ TeV for each spectrum. Right: expected ALP limits, based on our model as well as the future LHAASO (or + CTA) observations of IC 310 (red dash line) and Mrk 501 (green dash line). The limit from Mrk 501 is predicted with 5-years sensitivity of LHAASO and IC 310 with one year. For these limited parameters, the ALP-induced flux enhancement is more than an order of magnitude. Left: fitting and extrapolating the observations of M 87. The detectable ALP-induced flux enhancement $\frac{\psi_1}{\psi_0}$ for unconstrained ALP parameters is less than 10 for M 87, so we consider that this spectrum and our model can not give the limit on ALP. The meanings of various symbols in the diagram are the same as Fig. 3.

501, $F_0 \approx 5 \times 10^{-11} \text{ erg cm}^{-2} \text{ s}^{-1}$ [110] and $t_{\text{var}} \approx 1$ day [55], so we derive $\delta \gtrsim 11.1$ with $E = 100$ TeV and Eq. (8); Similarly, for M 87, $F_0 \approx 3 \times 10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}$ (derived from almost all of the infrared luminosity $L_{\text{IR}} \approx 10^{41} \text{ erg s}^{-1}$ of M 87 observed in 2000 [111]), $t_{\text{var}} \approx 2$ days [91], $\delta \gtrsim 6.3$, and for IC 310, $F_0 \approx 1 \times 10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}$ (inferred from the SSC model that is fitted the multi-frequency observations [93]), $t_{\text{var}} \approx 0.55$ day [94], $\delta \gtrsim 6.6$. These derived values of Doppler factor are not in tension with the typical values, especially for Mrk

501 [107]. Note that even if $\tau > 1$, the VHE flux would not reduce exponentially by $\exp(-\tau)$, but only by a factor of τ (i.e., lead to a spectral break), owing to those photons produced in the last transparent layer are still able to escape unabsorbed [112,113]. If the intrinsic absorption is outside the VHE region along line of sight, the cutoff is exponential, but it is complicated to estimate it and may be less important [94].

Second, even though the spectrum is dominated by emission of leptonic origin (with evidence that most of

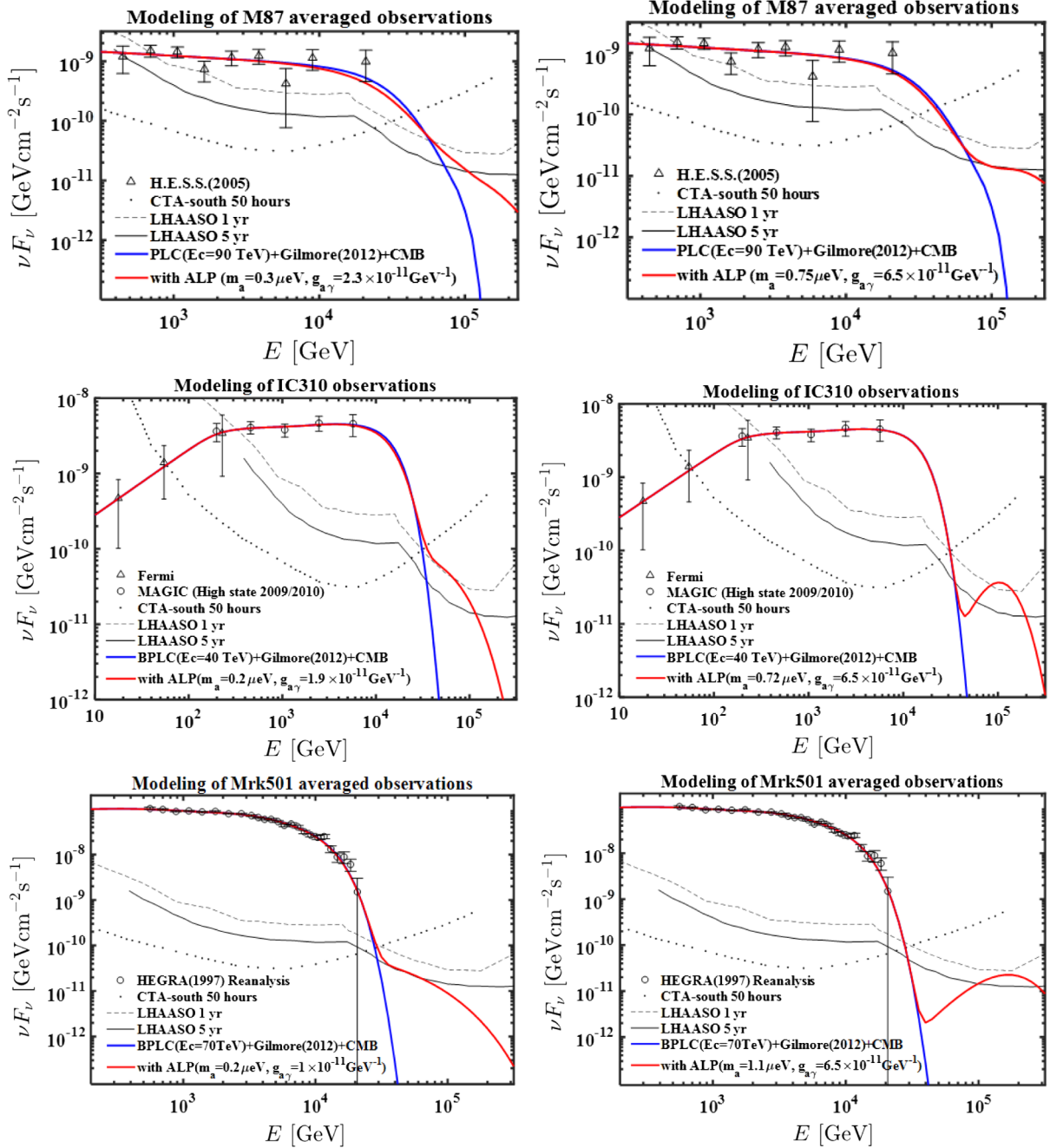


FIG. 7. The results for the fiducial parameters in Table I. The meanings of various symbols in the diagram are the same as the top panel and left of the bottom panels of Fig. 3.

the rapid variable emission has a leptonic origin), the emitted spectrum with cutoff above 100 TeV at VHE region is still possible. The recent observation from the Crab Nebula with energy beyond 100 TeV show no exponential cutoff below 100 TeV, which is usually interpreted in the framework of leptonic models [114,115]. As powerful cosmic particle accelerators [116], that may happen on some extreme TeV AGNs, too. Furthermore, AGNs are excellent candidates as ultrahigh-energy cosmic rays sources [117], and the hadronic cosmic rays are capable of producing spectrum without sharp cutoff below 100 TeV if the VHE emission is dominated by hadronic origin [118].

To determine the magnitude of E_c without ambiguity, we need to further research on the intrinsic physics (including parent particle species and its spectral energy distribution, the radiation mechanism, and pair attenuation in the emission region) of the γ -ray sources, as well as the forthcoming observations above tens of TeV by CTA, LHAASO, SWGO and so on.

The VHE emission from IC 310 only have been detected two times by MAGIC so far [93], which are relatively sparse compared to the two other sources. Therefore, we are more strict with IC 310 and simulate its observations at high state between 2009 October and 2010 February with 1 yr sensitivities of LHAASO. If such high state would occur more than three times during the whole performance period of LHAASO, our expected constraint on ALPs is possible.

VI. CONCLUSION

In this article, we have discussed the potential of the gamma-ray spectrum of AGN for energy up to above 100 TeV to probe ALP parameter space at around μeV , where the coupling $g_{a\gamma}$ is so far relatively weak constraint.

In case of conventional physics, most of the photons above tens of TeV emitted from distant (distance > 10 Mpc) AGN would be absorbed by the EBL/CMB during its travel to the earth (see Fig. 1 and 2). But more such photons, no matter how far away, could survive, if we assume that the photon-ALP conversions ($\gamma \rightarrow a \rightarrow \gamma$) take place separately in the homogeneous lobe (or plume) and Galaxy magnetic-field. Consequently, a very significant ALP-induced flux enhancement, shaped as a peak, is expected to arise in the observed spectrum above tens of

TeV (see Fig. 2). This provides the upcoming LHAASO a good chance to detect the enhancement as its unprecedented sensitivity above 30 TeV.

In order to acquire as many observations at tens of TeV as possible and thus reduce the uncertainty from the intrinsic spectrum, the nearby and bright sources, such as Mrk 501, IC 310 and M 87, are recommended to constrain the ALPs around μeV . Assuming an intrinsic spectrum with exponential cutoff, we have extrapolated the observed spectra of our sample up to above 100 TeV by the models with/without ALPs. For $g_{a\gamma} \gtrsim 2 \times 10^{-11} \text{ GeV}^{-1}$ with $m_a \lesssim 0.5 \mu\text{eV}$, the flux at around 100 TeV predicted by the ALP model can be more than an order of magnitude larger than that from the standard absorption, and the enhanced flux could be detected by LHAASO (see Fig. 3 and 7).

Our result is subject to the uncertainty from the extrapolation of intrinsic spectrum above tens of TeV and the source magnetic-field (see Fig. 4 and 6). For an optimistic estimation, the constraint can be improved to $g_{a\gamma} \gtrsim 2 \times 10^{-11} \text{ GeV}^{-1}$ with $m_a \lesssim 1 \mu\text{eV}$ (see Fig. 4). This will require further research on these sources (Mrk 501, IC 310, and M 87) based on the forthcoming observations by CTA, LHAASO, SWGO and so on.

ACKNOWLEDGMENTS

We would like to thank Weipeng Lin, P.H.T. Tam, Chengfeng Cai, Zhao-Huan Yu, Seishi Enomoto, Yi-Lei Tang, and Yu-Pan Zeng for useful discussions and comments. This work is supported by the National Natural Science Foundation of China (NSFC) under Grant No. 11875327, the Fundamental Research Funds for the Central Universities, China, and the Sun Yat-Sen University Science Foundation.

APPENDIX: FITTING RESULTS FOR THE OTHER DIFFERENT ALP PARAMETERS

As a supplement of Fig. 3, we show in Fig. 7 the fitting results for another different bounded ALP parameters, where the observations of M 87, IC 310 and Mrk 501 are fitted and extrapolated for the case of the fiducial parameters in Table I. The meanings of various symbols in the diagram are the same as Fig. 3.

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- [1] P. Svrcek and E. Witten, Axions in string theory, *J. High Energy Phys.* **06** (2006) 051.
 [2] J. Jaeckel and A. Ringwald, The low-energy frontier of particle physics, *Annu. Rev. Nucl. Part. Sci.* **60**, 405 (2010).

- [3] R. D. Peccei and H. R. Quinn, *CP* Conservation in the Presence of Pseudoparticles, *Phys. Rev. Lett.* **38**, 1440 (1977).
 [4] S. Weinberg, A New Light Boson?, *Phys. Rev. Lett.* **40**, 223 (1978).

- [5] F. Wiczek, Problem of Strong P and T Invariance in the Presence of Instantons, *Phys. Rev. Lett.* **40**, 279 (1978).
- [6] J. Preskill, M. B. Wise, and F. Wilczek, Cosmology of the invisible axion, *Phys. Lett.* **120B**, 127 (1983).
- [7] L. F. Abbott and P. Sikivie, A cosmological bound on the invisible axion, *Phys. Lett.* **120B**, 133 (1983).
- [8] M. Dine and W. Fischler, The not so harmless axion, *Phys. Lett.* **120B**, 137 (1983).
- [9] J. E. Marsh, Axiverse extended: Vacuum destabilization, early dark energy, and cosmological collapse, *Phys. Rev. D* **83**, 123526 (2011).
- [10] G. Raffelt and L. Stodolsky, Mixing of the photon with low-mass particles, *Phys. Rev. D* **37**, 1237 (1988).
- [11] P. Sikivie, Experimental Tests of the “Invisible” Axion, *Phys. Rev. Lett.* **51**, 1415 (1983).
- [12] K. A. Hochmuth and G. Sigl, Effects of axion-photon mixing on gamma-ray spectra from magnetized astrophysical sources, *Phys. Rev. D* **76**, 123011 (2007).
- [13] A. de Angelis, O. Mansutti, and M. Roncadelli, Axion-like particles, cosmic magnetic fields and gamma-ray astrophysics, *Phys. Lett. B* **659**, 847 (2008).
- [14] D. Hooper and P. D. Serpico, Detecting Axionlike Particles with Gamma Ray Telescopes, *Phys. Rev. Lett.* **99**, 231102 (2007).
- [15] A. De Angelis, M. Roncadelli, and O. Mansutti, Evidence for a new light spin-zero boson from cosmological gamma-ray propagation?, *Phys. Rev. D* **76**, 121301(R) (2007).
- [16] A. Mirizzi, D. Montanino, and J. Cosmol, Stochastic conversions of TeV photons into axion-like particles in extragalactic magnetic fields, *J. Cosmol. Astropart. Phys.* **12** (2009) 004.
- [17] D. Wouters and P. Brun, Irregularity in gamma ray source spectra as a signature of axionlike particles, *Phys. Rev. D* **86**, 043005 (2012).
- [18] R. Bahre *et al.* (ALPS Collaboration), Any light particle search II-Technical Design Report, *J. Instrum.* **8**, T09001 (2013).
- [19] S. Aune *et al.* (CAST Collaboration), CAST Search for sub-eV Mass Solar Axions with ^3He Buffer Gas, *Phys. Rev. Lett.* **107**, 261302 (2011).
- [20] L. D. Duffy, P. Sikivie, D. B. Tanner, S. J. Asztalos, C. Hagmann, D. Kinion, L. J. Rosenberg, K. van Bibber, D. B. Yu, and R. F. Bradley (ADMX Collaboration), High resolution search for dark-matter axions, *Phys. Rev. D* **74**, 012006 (2006).
- [21] M. Simet, D. Hooper, and P. D. Serpico, Milky Way as a kiloparsec-scale axionscope, *Phys. Rev. D* **77**, 063001 (2008).
- [22] M. Meyer, D. Montanino, and J. Conrad, On detecting oscillations of gamma rays into axion-like particles in turbulent and coherent magnetic fields, *J. Cosmol. Astropart. Phys.* **09** (2014) 003.
- [23] M. A. Sanchez-Conde, D. Paneque, E. Bloom, F. Prada, and A. Dominguez, Hints of the existence of Axion-Like-Particles from the gamma-ray spectra of cosmological sources, *Phys. Rev. D* **79**, 123511 (2009).
- [24] A. De Angelis, G. Galanti, and M. Roncadelli, Relevance of axionlike particles for very-high-energy astrophysics, *Phys. Rev. D* **84**, 105030 (2011).
- [25] A. Dominguez, M. A. Sanchez-Conde, and F. Prada, Axion-like particle imprint in cosmological very-high-energy sources, *J. Cosmol. Astropart. Phys.* **11** (2011) 020.
- [26] F. Tavecchio, M. Roncadelli, G. Galanti, and G. Bonnoli, Evidence for an axion-like particle from PKS 1222+216?, *Phys. Rev. D* **86**, 085036(E) (2012).
- [27] M. Meyer, D. Horns, and M. Raue, First lower limits on the photon-axion-like particle coupling from very high energy gamma-ray observations, *Phys. Rev. D* **87**, 035027 (2013).
- [28] M. Meyer and J. Conrad, Sensitivity of the Cherenkov Telescope Array to the detection of axion-like particles at high gamma-ray opacities, *J. Cosmol. Astropart. Phys.* **12** (2014) 016.
- [29] S. Troitsky, Towards discrimination between galactic and intergalactic axion-photon mixing, *Phys. Rev. D* **93**, 045014 (2016).
- [30] D. Montanino, F. Vazza, A. Mirizzi, and M. Viel, Enhancing the Spectral Hardening of Cosmic TeV Photons by Mixing with Axionlike Particles in the Magnetized Cosmic Web, *Phys. Rev. Lett.* **119**, 101101 (2017).
- [31] R. Buehler, G. Gallardo, G. Maier, A. Dominguez, M. Lopez, and M. Meyer, Search for the imprint of axion-like particles in the highest-energy photons of hard γ -ray blazars, *J. Cosmol. Astropart. Phys.* **09** (2020) 027.
- [32] A. I. Nikishov, Pair production by a constant external field, *J. Exp. Theor. Phys.* **393**, 14 (1962), http://83.149.229.155/cgi-bin/dn/e_030_04_0660.pdf.
- [33] M. G. Hauser and E. Dwek, The cosmic infrared background: Measurements and implications, *Annu. Rev. Astron. Astrophys.* **39**, 249 (2001).
- [34] F. Aharonian *et al.* (H.E.S.S. Collaboration), A low level of extragalactic background light as revealed by γ -rays from blazars, *Nature (London)* **440**, 1018 (2006).
- [35] E. Dwek and A. Kusenko, The extragalactic background light and the gamma-ray opacity of the universe, *Astropart. Phys.* **43**, 112 (2013).
- [36] L. Costamante, Gamma-rays from blazars and the extragalactic background light, *Int. J. Mod. Phys. D* **22**, 1330025 (2013).
- [37] A. De. Angelis, G. Galanti, and M. Roncadelli, Relevance of axion-like particles for very-high-energy astrophysics, *Phys. Rev. D* **87**, 109903(E) (2013).
- [38] D. Horns, L. Maccione, M. Meyer, A. Mirizzi, D. Montanino, and M. Roncadelli, Hardening of TeV gamma spectrum of active galactic nuclei in galaxy clusters by conversions of photons into axionlike particles, *Phys. Rev. D* **86**, 075024 (2012).
- [39] G. Galanti and M. Roncadelli, Behavior of axionlike particles in smoothed out domainlike magnetic fields, *Phys. Rev. D* **98**, 043018 (2018).
- [40] G. Galanti, F. Tavecchio, M. Roncadelli, and C. Evoli, Blazar VHE spectral alterations induced by photon-ALP oscillations, *Mon. Not. R. Astron. Soc.* **487**, 123 (2019).
- [41] A. Franceschini, G. Rodighiero, and M. Vaccari, Extragalactic optical-infrared background radiation, its time evolution and the cosmic photon-photon opacity, *Astron. Astrophys.* **487**, 837 (2008).
- [42] A. Abramowski, F. Acero, F. Aharonian, F. A. Benkhali, A. G. Akhperjanian, E. Anguner *et al.*, Constraints on axionlike particles with H.E.S.S. from the irregularity of

- the PKS 2155-304 energy spectrum, *Phys. Rev. D* **88**, 102003 (2013).
- [43] M. Ajello, A. Albert, B. Anderson, L. Baldini, G. Barbiellini, D. Bastieri *et al.*, Search for Spectral Irregularities due to Photon-Axionlike-Particle Oscillations with the Fermi Large Area Telescope, *Phys. Rev. Lett.* **116**, 161101 (2016).
- [44] C. Zhang, Y. F. Liang, S. Li, N.-H. Liao, L. Feng, Q. Yuan, Y.-Z. Fan, and Z.-Z. Ren, New bounds on axionlike particles from the Fermi Large Area Telescope observation of PKS 2155-304, *Phys. Rev. D* **97**, 063009 (2018).
- [45] H. J. Li, J. G. Guo, X. J. Bi, S. J. Lin, and P. F. Yin, Limits on axion-like particles from Mrk 421 with 4.5-years period observations by ARGO-YBJ and Fermi-LAT, *Phys. Rev. D* **103**, 083003 (2021).
- [46] M. Libanov and S. Troitsky, On the impact of magnetic-field models in galaxy clusters on constraints on axion-like particles from the lack of irregularities in high-energy spectra of astrophysical sources, *Phys. Lett. B* **802**, 135252 (2020).
- [47] P. Arias, D. Cadamuro, M. Goodsell, J. Jaeckel, J. Redondo, and A. Ringwald, WISPy cold dark matter, *J. Cosmol. Astropart. Phys.* **06** (2012) 013.
- [48] E. Armengaud *et al.* (IAXO Collaboration), Physics potential of the International Axion Observatory (IAXO), *J. Cosmol. Astropart. Phys.* **06** (2019) 047.
- [49] G. Sigl, Astrophysical haloscopes, *Phys. Rev. D* **96**, 103014 (2017).
- [50] T. D. P. Edwards, M. Chianese, B. J. Kavanagh, S. M. Nissanke, and C. Weniger, Unique Multimessenger Signal of QCD Axion Dark Matter, *Phys. Rev. Lett.* **124**, 161101 (2020).
- [51] A. Caputo, C. PenaGaray, and S. J. Witte, Detecting the stimulated decay of axions at radio frequencies. Looking for axion dark matter in dwarf spheroidal galaxies, *Phys. Rev. D* **98**, 083024 (2018).
- [52] O. Ghosh, J. Salvado, and J. Miralda-Escude, Axion gegenschein: Probing back-scattering of astrophysical radio sources induced by dark matter, [arXiv:2008.02729](https://arxiv.org/abs/2008.02729).
- [53] K. Kohri and H. Kodama, Axion-like particles and recent observations of the cosmic infrared background radiation, *Phys. Rev. D* **96**, 051701(R) (2017).
- [54] J. Davies, M. Meyer, and G. Cotter, Relevance of jet magnetic field structure for blazar axionlike particle searches, *Phys. Rev. D* **103**, 023008 (2021).
- [55] F. Aharonian (HEGRA Collaboration), The time averaged TeV energy spectrum of mkn 501 of the extraordinary 1997 outburst as measured with the stereoscopic Cherenkov telescope system of hegra, *Astron. Astrophys.* **349**, 11 (1999), <http://adsabs.harvard.edu/pdf/1999A%26A...349..11A>.
- [56] H. Abdalla *et al.* (H.E.S.S. Collaboration), The 2014 TeV γ -ray flare of Mrk 501 Seen with H.E.S.S.: Temporal and spectral constraints on lorentz invariance violation, *Astrophys. J.* **870**, 93 (2019).
- [57] X. Bai *et al.* (LHAASO Collaboration), The large high altitude air shower observatory (LHAASO) science white paper, [arXiv:1905.02773](https://arxiv.org/abs/1905.02773).
- [58] F. Aharonian *et al.* (HESS Collaboration), Observations of the Crab Nebula with H.E.S.S., *Astron. Astrophys.* **899**, 457 (2006), <https://www.aanda.org/articles/aa/abs/2006/39/aa5351-06/aa5351-06.html>.
- [59] J. Aleksic *et al.* (MAGIC Collaboration), Performance of the MAGIC stereo system obtained with Crab Nebula data, *Astropart. Phys.* **35**, 435 (2012).
- [60] J. Holder, V. A. Acciari, E. Aliu, T. Arlen, M. Beilicke *et al.*, Status of the VERITAS observatory, *AIP Conf. Proc.* **657**, 1085 (2009).
- [61] M. S. Pshirkov, P. G. Tinyakov, and F. R. Urban, New Limits on Extragalactic Magnetic Fields from Rotation Measures, *Phys. Rev. Lett.* **116**, 191302 (2016).
- [62] E. Masaki, A. Aoki, and Jiro Soda, Photon-axion conversion, magnetic field configuration, and polarization of photons, *Phys. Rev. D* **96**, 043519 (2017).
- [63] J. L. Han, Observing interstellar and intergalactic magnetic fields, *Annu. Rev. Astron. Astrophys.* **55**, 111 (2017).
- [64] F. Tavecchio, M. Roncadelli, and G. Galanti, Photons to axion-like particles conversion in active galactic nuclei, *Phys. Lett. B* **744**, 375 (2015).
- [65] Y. G. Zheng, C. Y. Yang, L. Zhang, and J. C. Wang, Discerning the gamma-ray-emitting region in the flat spectrum radio quasars, *Astrophys. J. Suppl. Ser.* **228**, 1 (2017).
- [66] S. J. Kang, L. Chen, and Q. W. Wu, Constraints on the minimum electron Lorentz factor and matter content of jets for a sample of bright Fermi blazars, *Astrophys. J. Suppl. Ser.* **215**, 5 (2014).
- [67] R. Xue, D. Luo, Z. R. Wang, Z. H. Xie, T. F. Yi, D. R. Xiong, Y. B. Xu, W. G. Liu, and X. L. Yu, Curvature of the spectral energy distribution, the inverse Compton component and the jet in Fermi 2LAC blazars, *Mon. Not. R. Astron. Soc.* **463**, 3038 (2016).
- [68] S. P. O. Sullivan and D. C. Gabuzda, Magnetic field strength and spectral distribution of six parsec-scale active galactic nuclei jets, *Mon. Not. R. Astron. Soc.* **400**, 26 (2009).
- [69] R. E. Pudritz, M. J. Hardcastle, and D. C. Gabuzda, Magnetic fields in astrophysical jets: From launch to termination, *Space Sci. Rev.* **169**, 27 (2012).
- [70] L. M. Widrow, Origin of galactic and extragalactic magnetic fields, *Rev. Mod. Phys.* **74**, 775 (2002).
- [71] see <http://tevcat.uchicago.edu/>.
- [72] C. M. Urry and P. Padovani, Unified schemes for radio-loud active galactic nuclei, *Publ. Astron. Soc. Jpn.* **107**, 803 (1995).
- [73] A. Dobrynina, A. Kartavtsev, and G. Raffelt, Photon-photon dispersion of TeV gamma rays and its role for photon-ALP conversion, *Phys. Rev. D* **91**, 083003 (2015).
- [74] R. C. Gilmore, R. S. Somerville, J. R. Primack, and A. Domínguez, Semi-analytic modelling of the extragalactic background light and consequences for extragalactic gamma-ray spectra, *Mon. Not. R. Astron. Soc.* **422**, 3189 (2012).
- [75] M. Ackermann *et al.* (Fermi-LAT Collaboration), The imprint of the extragalactic background light in the gamma-ray spectra of blazars, *Science* **338**, 1190 (2012).
- [76] A. Abramowski *et al.* (H.E.S.S. Collaboration), Measurement of the extragalactic background light imprint on the

- spectra of the brightest blazars observed with H.E.S.S., *Astron. Astrophys.* **550**, A4 (2013).
- [77] A. U. Abeysekara *et al.* (VERITAS Collaboration), Gamma-rays from the quasar PKS 1441 + 25: Story of an escape, *Astrophys. J.* **815**, L22 (2015).
- [78] J. Biteau and D. A. Williams, The extragalactic background light, the Hubble constant, and anomalies: Conclusions from 20 years of TeV gamma-ray observations, *Astrophys. J.* **812**, 60 (2015).
- [79] M. L. Ahnen *et al.* (MAGIC Collaboration), MAGIC observations of the February 2014 flare of 1ES 1011 + 496 and ensuing constraint of the EBL density, *Astron. Astrophys.* **590**, A24 (2016).
- [80] T. Armstrong, A. M. Brown, and P. M. Chadwick, Fermi-LAT high z AGN and the extragalactic background light, *Mon. Not. R. Astron. Soc.* **470**, 4089 (2017).
- [81] Q. Yuan, H. L. Huang, X. J. Bi, and H. H. Zhang, Measuring the extragalactic background light from very high energy gamma-ray observations of blazars, [arXiv:1212.5866](https://arxiv.org/abs/1212.5866).
- [82] G. B. Long, W. P. Lin, P. H. T. Tam, and W. S. Zhu, Testing the CIBER cosmic infrared background measurements and axionlike particles with observations of TeV blazars, *Phys. Rev. D* **101**, 063004 (2020).
- [83] A. Dominguez, J. R. Primack, D. J. Rosario *et al.*, Extragalactic background light inferred from AEGIS galaxy-SED-type fractions, *Mon. Not. R. Astron. Soc.* **410**, 2556 (2011).
- [84] J. D. Finke, S. Razzaque, and C. D. Dermer, Modeling the extragalactic background light from stars and dust, *Astrophys. J.* **712**, 238 (2010).
- [85] H. Abdalla *et al.* (H.E.S.S. Collaboration), Measurement of the EBL spectral energy distribution using the VHE γ -ray spectra of H.E.S.S. blazars, *Astron. Astrophys.* **606**, A59 (2017).
- [86] Y. Gong and A. Cooray, The extragalactic background light from the measurements of the attenuation of high-energy gamma-ray spectrum, *Astrophys. J. Lett.* **772**, L12 (2013).
- [87] A. Mirizzi, G. G. Raffelt, and P. D. Serpico, Signatures of axion-like particles in the spectra of TeV gamma-ray sources, *Phys. Rev. D* **76**, 023001 (2007).
- [88] A. Franceschini, L. Foffano, E. Prandini, and F. Tavecchio, Very high-energy constraints on the infrared extragalactic background light, *Astron. Astrophys.* **629**, A2 (2019).
- [89] V. A. Acciari *et al.* (MAGIC Collaboration), Monitoring of the radio galaxy M 87 during a low-emission state from 2012 to 2015 with MAGIC, *Mon. Not. R. Astron. Soc.* **492**, 5354 (2020).
- [90] E. Aliu *et al.* (VERITAS Collaboration), VERITAS observations of day-scale flaring of M 87 in 2010 April, *Astrophys. J.* **746**, 141 (2012).
- [91] F. Aharonian (H. E. S. S. Collaboration), Fast variability of TeV γ -rays from the radio galaxy M87, *Science* **314**, 1424 (2006).
- [92] F. N. Owen, J. A. Eilek, and N. E. Kassim, M87 at 90 centimeters: A different picture, *Astrophys. J.* **543**, 611 (2000).
- [93] M. L. Ahnen *et al.*, First multi-wavelength campaign on the gamma-ray-loud active galaxy IC 310, *Astron. Astrophys.* **603**, A25 (2017).
- [94] J. Aleksic *et al.* (MAGIC Collaboration), Rapid and multiband variability of the TeV bright active nucleus of the galaxy IC 310, *Astron. Astrophys.* **563**, A91 (2014).
- [95] L. Feretti, G. Giovannini, U. Klein, K.-H. Mack, L. G. Sijbring, and G. Zech, Electron ageing and polarization in tailed radio galaxies, *Astron. Astrophys.* **331**, 475 (1998), <http://adsabs.harvard.edu/pdf/1998A%26A...331..475F>.
- [96] K. Sato, T. Furusho, N. Y. Yamasaki, M. Ishida, K. Matsushita, and T. Ohashi, Xmm-newton observation of ic 310 in the outer region of the perseus cluster of galaxies, *Publ. Astron. Soc. Jpn.* **57**, 743 (2005).
- [97] B. Sebastian, D. V. Lal, and A. P. Rao, Giant metrewave radio telescope observations of head-tail radio galaxies, *Astron. J.* **154**, 169 (2017).
- [98] F. Aharonian (HEGRA Collaboration), Reanalysis of the high energy cutoff of the 1997 mkn 501 TeV energy spectrum, *Astron. Astrophys.* **366**, 62 (2001).
- [99] J. T. Stocke, J. M. Shull, S. Penton, M. Donahue, and C. Carilli, The local Ly (α) forest: Association of clouds with superclusters and voids, *Astrophys. J.* **451**, 24 (1995).
- [100] K. Nilsson, T. Pursimo, L. O. Takalo, A. Sillanpaa, H. Pietila, and J. Heidt, Two-dimensional photometric decomposition of the TeV BL lacertae objects markarian 421, markarian 501, and 1ES 2344+514, *Publ. Astron. Soc. Jpn.* **111**, 1223 (1999).
- [101] R. Jansson and G. R. Farrar, A new model of the galactic magnetic field, *Astrophys. J.* **757**, 14 (2012).
- [102] E. Lefa, S. R. Kelner, and F. A. Aharonian, On the spectral shape of radiation due to inverse Compton scattering close to the maximum cut-off, *Astrophys. J.* **753**, 176 (2012).
- [103] L. Stawarz and V. Petrosian, On the momentum diffusion of radiating ultrarelativistic electrons in a turbulent magnetic field, *Astrophys. J.* **681**, 1725 (2008).
- [104] T. R. Lewis, P. A. Becker, and J. D. Finke, Electron acceleration in blazars: Application to the 3C 279 flare on 2013 December 20, *Astrophys. J.* **884**, 116 (2019).
- [105] D. C. Warren, C. A. A. Beauchemin, M. V. Barkov, and S. Nagataki, The maximum energy of shock-accelerated electrons in a microturbulent magnetic field, *Astrophys. J.* **906**, 33 (2021).
- [106] M. Lemoine and M. A. Malkov, Powerlaw spectra from stochastic acceleration, *Mon. Not. R. Astron. Soc.* **499**, 4972 (2020).
- [107] Fermi-LAT, MAGIC, and VERITAS Collaborations, Insights into the high-energy gamma-ray emission of Markarian 501 from extensive multifrequency observations in the Fermi era, *Astrophys. J.* **727**, 129 (2011).
- [108] R. Xue, R. Y. Liu, M. Petropoulou, F. Oikonomou, Z. R. Wang, K. Wang, and X. Y. Wang, Powerlaw spectra from stochastic acceleration, *Astrophys. J.* **886**, 23 (2019).
- [109] L. Dondi and G. Ghisellini, Gamma-ray-loud blazars and beaming, *Mon. Not. R. Astron. Soc.* **273**, 583 (1995).
- [110] D. Petry, M. Bottcher, and V. Connaughton, Multiwavelength observations of Markarian 501 during the 1997 high state, *Astrophys. J.* **536**, 742 (2000).

- [111] D. Whysong and R. Antonucci, Thermal emission as a test for hidden nuclei in nearby radio galaxies, *Astrophys. J.* **602**, 116 (2004).
- [112] A. Neronov and F. A. Aharonian, Production of TeV gamma-radiation in the vicinity of the supermassive black hole in the giant radiogalaxy M87, *Astrophys. J.* **671**, 85 (2007).
- [113] F. M. Rieger and F. A. Aharonian, Variable VHE gamma-ray emission from non-blazar AGNs, *Astron. Astrophys.* **479**, L5 (2008).
- [114] M. Amenomori *et al.* (Tibet AS γ Collaboration), First Detection of Photons with Energy Beyond 100 TeV from an Astrophysical Source, *Phys. Rev. Lett.* **123**, 051101 (2019).
- [115] A. U. Abeysekara *et al.* (HAWC Collaboration), Measurement of the crab nebula spectrum past 100 TeV with HAWC, *Astrophys. J.* **881**, 134 (2019).
- [116] K. Kotera and A. V. Olinto, The astrophysics of ultrahigh-energy cosmic rays, *Annu. Rev. Astron. Astrophys.* **49**, 119 (2011).
- [117] R. Mbarek and D. Caprioli, Bottom-up acceleration of ultra-high-energy cosmic rays in the jets of active galactic nuclei, *Astrophys. J.* **886**, 8 (2019).
- [118] B. S. Acharya *et al.* (CTA Collaboration), Science with the Cherenkov Telescope Array, [arXiv:1709.07997](https://arxiv.org/abs/1709.07997).