

Threshold Upsilon-meson photoproduction at the EIC and EicC

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High-accuracy Υ -meson photoproduction data from EIC and EicC experiments will allow the measurement of the near-threshold total cross section of the reaction $\gamma p \rightarrow \Upsilon p$, from which the absolute value of the Υp -scattering length, $|\alpha_{\Upsilon p}|$, can be extracted using a vector-meson dominance model. For this evaluation, we used Υ -meson photoproduction quasidata from the QCD approach (the production amplitude can be factorized in terms of gluonic generalized parton distributions and the quarkonium distribution amplitude). A comparative analysis of $|\alpha_{\Upsilon p}|$ with the recently determined scattering lengths for ωp , ϕp , and $J/\psi p$ using the A2, CLAS, and GlueX experimental data are performed. The role of the “young” vector-meson effect is evaluated.

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I. INTRODUCTION

In 1977, the observation of an enhancement at 9.5 GeV in the dimuon mass spectrum produced in 400 GeV proton-nucleus collisions at the Fermi Lab resulted in a new vector-meson (V) [1], then called $\Upsilon(1S)(9460)$.

Compared to other mesons, vector-mesons can be measured to very high precision. This stems from the fact that vector-mesons have the same quantum numbers as the photon $I^G(J^{PC}) = 0^-(1^{--})$.

The photoproduction of $J/\psi(1S)$ and $\Upsilon(1S)$ are among the key reactions that will be measured at the electron-ion colliders (EIC) hosted by the Brookhaven National Laboratory [2] and EicC at the High Intensity heavy-ion Accelerator Facility in China [3]. Charmonium and bottomonium are important not only for understanding the interaction mechanisms of the photoproduction of the heavy vector-mesons, but also for probing the gluonic properties of the nucleon. The large statistics of the exclusive $J/\psi(1S)$ and $\Upsilon(1S)$ production data at the hard scale are very helpful in probing the generalized parton distribution (GPD) of the gluon [4,5]. These measurements will advance our understanding of QCD which governs the properties of hadrons and the interactions involving hadrons.

Exclusive vector meson photoproduction can also shed light on the bound meson-nucleon system, since the generated charmonium and bottomonium interact with an intact nucleon. We point out that the bottomonium, $\Upsilon(1S)$, can be measured using real photons at EIC and EicC, where the quality of the expected data near-threshold will give access to a variety of interesting physics aspects, e.g., trace anomaly, pentaquarks, cusp effects, vector-meson–nucleon scattering length, and so on. The main object of this paper is to estimate the magnitude of the absolute value of the Υp scattering length, $|\alpha_{\Upsilon p}|$, using quasidata generated from the QCD model of Ref. [4], and compare it with the results for the other vector mesons. Our analysis is based also on the vector-meson dominance (VMD) model [6,7] relying on the transparent current-field identities of Kroll, Lee, and Zumino [8]. The VMD model can be used for a variety of qualitative estimates of observables in vector-meson photoproduction [9,10]—at least as the first step towards their more extended theoretical studies. The use of the VMD model in case of the J/ψ and Υ requires special attention due to the heavy mass of these vector-mesons. For the critical review of the VMD model, we refer to papers of Boreskov and Ioffe [11] and Kopeliovich *et al.* [12] and references therein. Recently, in Ref. [13], the VMD approach has been examined based on Dyson-Schwinger equations.

On the basis of recent threshold measurements of the photoproduction of three vector mesons off the proton by the A2 (MAMI), CLAS (JLab), and GlueX (JLab) Collaborations, one can determine vector-meson–proton scattering lengths (SLs) using the VMD model [14–16]. This results in

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$$|\alpha_{J/\psi p}| \ll |\alpha_{\phi p}| \ll |\alpha_{\omega p}|, \quad (1)$$

which indicates that the proton is more transparent for the ϕ -meson compared to the ω -meson, and at the same time it is much less transparent for the ϕ -meson than for the J/ψ -meson. Due to the small size of “young” vector mesons relative to those that have had time to fully form, scattering lengths determined phenomenologically in the near threshold photoproduction are smaller. Recall that when the photon produces a vector meson, V , it first creates a $q\bar{q}$ pair in point-like configuration. Near the threshold, this pair lacks sufficient time to form the complete wave function of the vector meson; that is, the proton interacts with the “young” (undressed) vector meson whose size is smaller than that of the “old” one participating in the elastic $Vp \rightarrow Vp$ scattering. Therefore, one observes stronger suppression for the vector-meson–proton interaction [17].

II. EXCLUSIVE VECTOR-MESON PHOTOPRODUCTION AT THE EIC

Exclusive vector-meson photoproduction is one of the key physics measurements for the EIC as discussed in the Yellow Report [2]. The proposed design for EIC is to collide electrons with energy of $E_e = 5\text{--}18$ GeV and protons with energy of $T_p = 41\text{--}275$ GeV. The proposed EIC detector has a number of specific features that will enable photoproduction measurements, and to ensure exclusivity. First, the energy of quasireal photons will be determined by tagger detectors in the so-called “far-backward” region, i.e., in the direction of the electron beam. Tagger detectors placed approximately 24 m and 37 m from the interaction point can cover a low- Q^2 acceptance better than 10^{-7} GeV²/c². Produced $\Upsilon(1S)$ mesons will be reconstructed from their leptonic decays, e.g., to an e^+e^- pair. The proposed EIC detector aims for momentum resolution sufficient to cleanly separate the Υ -states, a $\Delta p/p$ of better than 1% in the 4 GeV/c–10 GeV/c momentum range. Finally, exclusivity can be ensured by the detection of the final state proton, which, at threshold, will largely travel to the so-called “far-forward” region of the detector. The far-forward region, covering angles within approximately 13 mrad from the proton beam line, will be instrumented with a series of tracking detectors including Roman Pots, to track charged particles with slightly different magnetic rigidities than beam protons. Thus threshold Υ production will require the combination of the far-backward, far-forward and main EIC detectors in order to reconstruct the full event and ensure exclusivity.

III. SCATTERING LENGTH FOR UPSILON-PROTON

The total cross section of a binary reaction $ab \rightarrow cd$ with particle masses $m_a + M_b < m_c + M_d$ can be written as

TABLE I. Kinematical parameters for the vector-meson photoproduction off the proton at thresholds [18].

Vector-Meson	m_V (MeV)	$\sqrt{s_{\text{thr}}}$ (MeV)	E_{thr} (MeV)	k_{thr} (MeV/c)
$\omega(782)$	782.65	1720.9	1109.1	604.7
$\phi(1020)$	1019.461	1957.7	1573.3	754.0
$J/\psi(1S)$	3096.900	4035.2	8207.8	1908.5
$\Upsilon(1S)$	9460.30	10398.6	57152.9	5156.9

$$\sigma_t = \frac{q}{k} \cdot F(q, s), \quad (2)$$

where s is the square of the total center of mass energy, k is center of mass momentum of a (and b), and q is the center of mass momentum of c (and d). In photoproduction, i.e., when $m_a = 0$, $k = (s - M_b^2)/(2 \cdot \sqrt{s})$. Vector-meson kinematical parameters for the vector-meson photoproduction off the proton, i.e., $\gamma p \rightarrow Vp$, are given in Table I and Fig. 1, where m_V is the vector-meson mass, s_{thr} is the value of s at threshold, k_{thr} is the value of k at threshold, and E_{thr} is the photon energy at threshold in the frame where the proton is initially at rest.

The factor $F(q, s)$ in Eq. (2) is proportional to the square of the invariant amplitude and does not vanish at threshold, i.e., when $q \rightarrow 0$ and $k \rightarrow k_{\text{thr}}$, but instead approaches a constant value. Thus, near threshold, $\sigma_t \rightarrow 0$ and is at least proportional to q .

Traditionally, the σ_t behavior of a near-threshold binary inelastic reaction is described as a series of odd powers in q (see, for instance, Ref. [14]). In the energy range under study, we use

$$\sigma_t(q) = b_1 \cdot q + b_3 \cdot q^3 + b_5 \cdot q^5, \quad (3)$$

which assumes contributions from only the lowest S -, P -, and D -waves. Very close to threshold, the higher-order terms can be neglected and the linear term is determined by the S -wave only with a total spin of 1/2 and/or 3/2.

For the evaluation of the absolute value of the vector-meson–proton SL, we apply the commonly used and effective VMD approach (Fig. 2), which links the near-threshold cross sections of the vector-meson photoproduction, $\gamma p \rightarrow Vp$, and the elastic scattering, $Vp \rightarrow Vp$, processes via [10]

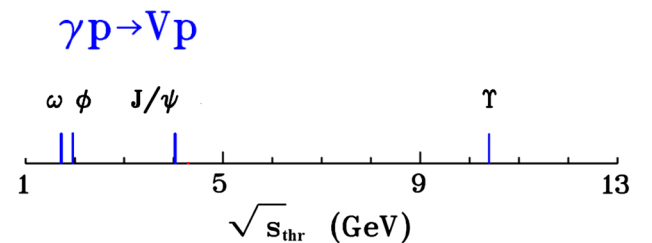


FIG. 1. Thresholds of meson photoproduction off the proton. Blue vertical lines are for vector-mesons including charmonium and b -quarkonium.

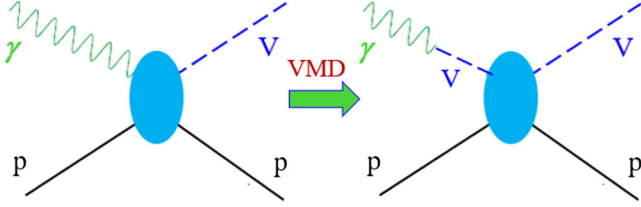


FIG. 2. Schematic diagrams of vector-meson photoproduction (left) and the VMD model (right) in the energy region at threshold experiments.

$$\begin{aligned}
 \left. \frac{d\sigma^{\gamma p \rightarrow V p}}{d\Omega} \right|_{\text{thr}} &= \frac{q}{k} \cdot \frac{1}{64\pi} \cdot |T^{\gamma p \rightarrow V p}|^2 \\
 &= \frac{q}{k} \cdot \frac{\pi\alpha}{g_V^2} \cdot \left. \frac{d\sigma^{V p \rightarrow V p}}{d\Omega} \right|_{q \rightarrow 0} \\
 &= \frac{q}{k} \cdot \frac{\pi\alpha}{g_V^2} \cdot |\alpha_{V p}|^2,
 \end{aligned} \quad (4)$$

where $T^{\gamma p \rightarrow V p}$ is the invariant amplitude of the vector-meson photoproduction, α is the fine-structure constant, and g_V is the VMD coupling constant, related to the vector-meson electromagnetic (EM) decay width $\Gamma_{V \rightarrow e^+ e^-}$

$$g_V^2 = \frac{\pi \cdot \alpha^2 \cdot m_V}{3 \cdot \Gamma(V \rightarrow e^+ e^-)}, \quad (5)$$

where m_V is the vector-meson mass.

Combining Eq. (3) (which is also valid for ω - ϕ -, and J/ψ -photoproduction [14–16]) and Eq. (4) with Eq. (5), one can express the absolute value of the SL as a product of the pure EM, VMD-motivated kinematic factor

$$B_V^2 = \frac{\alpha \cdot m_V \cdot k}{12\pi \cdot \Gamma(V \rightarrow e^+ e^-)}, \quad (6)$$

and the factor

$$h_{V p} = \sqrt{b_1} \quad (7)$$

that is determined by an interplay of strong (hadronic) and EM dynamics as

$$|\alpha_{V p}| = B_V \cdot h_{V p}. \quad (8)$$

Numerical values of both g_V and B_V are given in Table II. Let us note that these EM quantities B_V for each vector-meson are close to each other except for Υ .

Figure 3 shows the fit of the QCD model of Ref. [4] to the GlueX J/ψ photoproduction data [19] and the prediction of this model for the Υ photoproduction total cross section. Our phenomenological fit of the GlueX data using Eq. (3) is shown, as well. This is a rather general model assuming factorization in terms of gluonic generalized parton distributions and quarkonium wave function on

TABLE II. Vector-meson EM properties. The decay $\Gamma(V \rightarrow e^+ e^-)$ from PDG2020 [18] (second column), g_V was calculated using Eq. (5) (third column) and B_V using Eq. (6) (fourth column).

Vector-Meson	$\Gamma(V \rightarrow e^+ e^-)$ (keV)	g_V	B_V (MeV ^{1/2})
$\omega(782)$	0.60 ± 0.02	8.53 ± 0.14	390.49 ± 6.35
$\phi(1020)$	1.27 ± 0.04	6.69 ± 0.10	342.50 ± 5.27
$J/\psi(1S)$	5.53 ± 0.10	5.59 ± 0.05	454.92 ± 4.06
$\Upsilon(1S)$	1.340 ± 0.018	19.85 ± 1.21	2654.96 ± 162.15

one side and hard quark-gluon interaction on the other side. This work extends the validity of the factorization, as studied previously in Ref. [5] for high energies, down to the threshold region in leading order and in the case of a heavy quark mass.

We have generated quasidata (Fig. 4) for the Υ cross sections from this model [4] and fit it with Eq. (3) in order to extrapolate the data to the threshold. The exact q_{\min} attainable in an ep collider experiment will depend heavily on the exact placement of the low- Q^2 tagging detectors. For the purposes of this paper, we assume that the detector will have comparable coverage to the EIC Yellow Report detector [2], where the backward calorimeter coverage down to a pseudorapidity of -4 would allow q_{\min} for Υ photoproduction to be as low as ≈ 500 MeV/c. Further optimization of the low- Q^2 taggers may allow an even smaller q_{\min} to be achieved. Gryniuk *et al.* assumed a total integrated luminosity of 100 fb^{-1} for the Υ photoproduction at EIC, which corresponds to

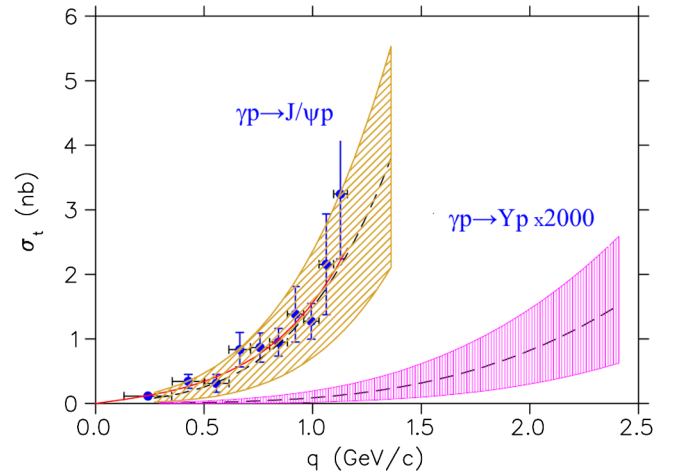


FIG. 3. The total $\gamma p \rightarrow J/\psi p$ and $\gamma p \rightarrow \Upsilon p$ cross sections σ_t . GlueX threshold J/ψ photoproduction data [19] shown by blue filled circles and the best-fit results are from Ref. [16] and shown by red solid curve. Theoretical fit of the GlueX data from Ref. [4] is shown by yellow shaded band at 95% C.L. Theoretical predictions for Υ photoproduction [4] are shown by magenta shaded band.

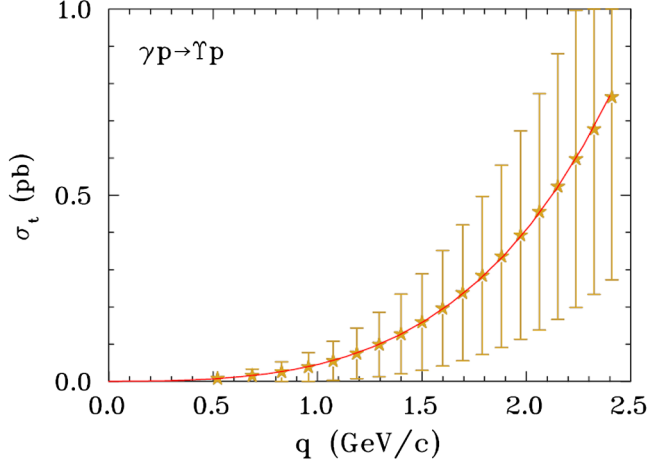


FIG. 4. The total $\gamma p \rightarrow \Upsilon p$ cross sections σ_t . Quasidata from Ref. [4] ($q_{\min} = 521$ MeV/c) shown by yellow filled stars. The phenomenological best fit for a quasi cross section [4] is shown by red solid curve. The uncertainties for quasidata were taken from Ref. [4].

116 days of the beam with the 10^{34} cm $^{-2}$ s $^{-1}$, for Monte Carlo calculations [20]. As Guo *et al.* [4] pointed out, the large mass of the Υ -meson implies that the calculations in the heavy meson limit works better for the Υ photoproduction, as there are fewer theoretical uncertainties from higher-order corrections. We account here for the theoretical accuracy and do not include the statistical/experimental errors. The expected luminosity of 10^{34} cm $^{-2}$ s $^{-1}$ will be able to provide smaller statistical uncertainty than the theoretical one. However, as the parameters of the EIC detector have not been defined yet, this estimate will depend on the actual detector acceptance and run time. Figure 5 illustrates the dramatic differences in the hadronic factors $h_{Vp} = \sqrt{b_1}$ (see Table III), as the slopes [b_1 from Eq. (3)] of the total cross sections at threshold as a function of q vary significantly from ω to J/ψ and now to Υ .

Therefore, such a big difference in SLs of the vector-meson–proton systems is determined mainly by the hadronic factor h_{Vp} , and reflects a strong weakening of the interaction in the $b\bar{b} - p$ and $c\bar{c} - p$ systems compared to that of the light $\bar{q}q - p$ ($q = u, d$) configurations. The interaction in the $\bar{s}s - p$ has an intermediate strength that is manifested in an intermediate value of the ϕp SL.

The corresponding results for the scattering lengths are shown in Fig. 6 as a function of the inverse vector-meson mass. Starting from the ϕ meson and for higher masses, the scattering lengths are significantly smaller than the typical hadron size of 1 fm, indicating increasing transparency of the proton for these mesons. Moreover, our analysis shows almost linear (in exponential scale) increase $|\alpha_{Vp}| \propto \exp(1/m_V)$ with increasing $1/m_V$. Actually, $p \rightarrow V$ coupling is proportional to the strong coupling α_s and the separation of the corresponding

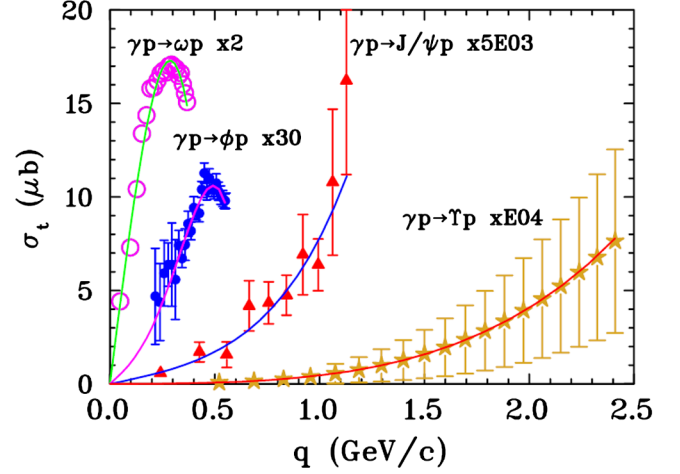


FIG. 5. The total $\gamma p \rightarrow Vp$ cross section σ_t derived from the A2 (magenta open circles) [14], CLAS (blue filled circles) [15], and GlueX (red filled triangles) [16], data, and EIC/EicC (yellow filled stars) quasidata is shown as a function of the center of mass momentum q of the final-state particles. The vertical (horizontal) error bars represent the total uncertainties of the data summing statistical and systematic uncertainties in quadrature (energy binning). Solid curves are the fit of the data with Eq. (3).

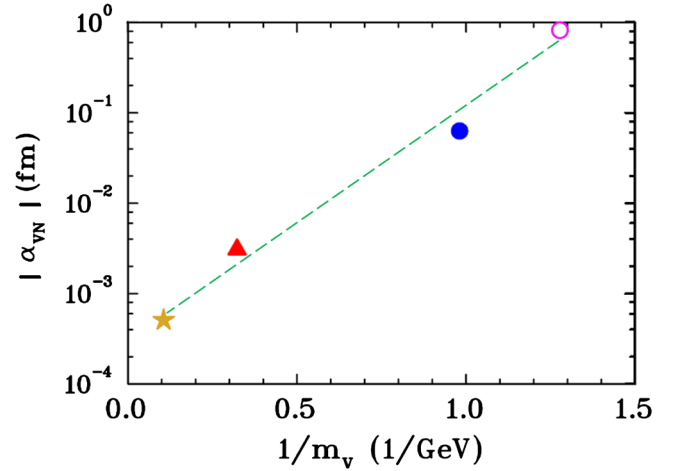


FIG. 6. Comparison of the $|\alpha_{Vp}|$ SLs estimated from vector-meson photoproduction at threshold vs the inverse mass of the vector mesons. The magenta open circle shows the analysis of the A2 ω -meson data [14], the blue-filled circle shows the analysis of the CLAS ϕ -meson data [15], the red-filled triangle shows the analysis of the GlueX J/ψ -meson data [16], and the yellow-filled star shows the analysis of the EIC and EicC Υ -meson quasidata [4]. The green dashed line is hypothetical.

quarks. This separation (in zero approximation) is proportional to $1/m_V$, which may explain the above relation.

IV. DISCUSSIONS AND OUTLOOK

In summary, one can extend the relationship (1) including the result for Υ (Table III)

TABLE III. The second column showed the minimal momentum q_{\min} for vector-mesons in photoproduction experiments and the source of data. The linear term (third column) of the best fit of the total cross section data using Eq. (3). The errors represent the total uncertainties (summing statistical and systematic uncertainties in quadrature). The fourth column showed vector-meson-proton SLs.

Vector-Meson	q_{\min} (MeV/c)	b_1 ($\mu\text{b}/\text{MeV}/c$)	$ \alpha_{Vp} $ (fm)
$\omega(782)$	49 [14]	$(0.44 \pm 0.01) \times 10^{-1}$ [14]	0.82 ± 0.03 [14]
$\phi(1020)$	216 [21]	$(0.34 \pm 0.12) \times 10^{-3}$ [15]	0.063 ± 0.010 [15]
$J/\psi(1S)$	230 [19]	$(0.46 \pm 0.16) \times 10^{-6}$ [16]	$(3.08 \pm 0.55) \times 10^{-3}$ [16]
$\Upsilon(1S)$	521 [4]	$(0.37 \pm 0.04) \times 10^{-9}$	$(0.51 \pm 0.03) \times 10^{-3}$

$$|\alpha_{\Upsilon p}| \ll |\alpha_{J/\psi p}| \ll |\alpha_{\phi p}| \ll |\alpha_{\omega p}|. \quad (9)$$

The values of $|\alpha_{Vp}|$ for the heavy vector-mesons, as determined in the recent papers [14–16] using the VMD model, are smaller than most of the theoretical predictions; see references in Refs. [14–16]. As for the Υ case, we are not aware of any theoretical predictions for the Υp scattering length except, related to that, a nonrelativistic potential result for the radius of the bottomonium which is $r_{\Upsilon} = (0.14 \pm 0.0014)$ fm [22]. The same approach gives a radius of the charmonium of $r_{J/\psi} = (0.25 \pm 0.0025)$ fm. Gryniuk *et al.* reported recently $|\alpha_{\Upsilon p}| = (0.066 \pm 0.001)$ fm and $|\alpha_{\Upsilon p}| = (0.016 \pm 0.001)$ fm [20] for two different subtraction constants. The latter results are based on the dispersive relations, taking some assumptions from their J/ψ photoproduction model [23], and extrapolating the high-energy measurements at $W \approx 100$ GeV down to the threshold.

The smallness of the scattering lengths, as extracted with the help of the VMD model, can be related to the “young age” of the vector mesons participating in the interaction with the proton as introduced by Feinberg [17]. For more quantitative estimate of the theoretical uncertainty related to the VMD model, we refer to the paper by Boreskov and Ioffe [11]. They evaluated the cross section of J/ψ photoproduction in a peripheral model (a mechanism for the photoproduction of J/ψ off nucleon with an imaginary amplitude that arises as the shadow of the amplitudes for the photoproduction of charmed particles) by Ref. [11] and found a strong energy dependence because the nondiagonal process $\gamma p \rightarrow J/\psi p$ must have larger transfer momenta versus the elastic scattering $J/\psi p \rightarrow J/\psi p$. This result is in a violation of VMD by a factor of five or so. In the case of the Υ meson, we expect the disagreement to be even worse. Boreskov *et al.* showed that a fluctuation of a photon into open charm particles is preferable than into charmonium [24]. Later on, it was shown by Kopeliovich *et al.* that the open-charm cross section is larger than the

charmonium one by a factor of ten or more [25,26]. In addition, in Eq. (4), we did not include a factor introduced in the VMD model in Ref. [27], which takes into account the difference between polarization degrees of freedom in the $\gamma p \rightarrow J/\psi p$ and $pJ/\psi \rightarrow pJ/\psi$ reactions. Such a factor that equals $2/3$ at threshold for the S -wave has not been used in the previous analysis of the scattering lengths; we consider it as a systematic uncertainty related to the VMD model [16].

In the recent work of Ref. [13] the effect of the VMD assumption was studied in the formalism of the Dyson-Schwinger equations which one can consider as an alternative interpretation of the “young age” effect in another (more formal) language. Their result shows much dramatic effect, up to a factor of 50 overestimation of the cross sections when using VMD for the two heaviest vector mesons. Nevertheless, this translates into a factor of seven for the scattering lengths and the overall dependence in Fig. 6 remains similar.

Present and future experiments JLab, EIC, and EicC that are aimed to measure charmonium and bottomonium production on the proton and nuclei will allow further studies of $J/\psi N$ and ΥN interactions and will allow access to a variety of other interesting physics aspects that are present in the near-threshold region. Further studies on both nucleons and nuclei in heavy vector-meson photo and electroproduction will significantly extend our knowledge of the gluonic structure of the nuclear matter.

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