Precise measurement of the f_s/f_d ratio of fragmentation fractions and of B_s^0 decay branching fractions

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The ratio of the B_s^0 and B^0 fragmentation fractions, f_s/f_d, in proton-proton collisions at the LHC, is obtained as a function of B-meson transverse momentum and collision center-of-mass energy from the combined analysis of different B-decay channels measured by the LHCb experiment. The results are described by a linear function of the meson transverse momentum or with a function inspired by Tsallis statistics. Precise measurements of the branching fractions of the $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^- \pi^+$ decays are performed, reducing their uncertainty by about a factor of 2 with respect to previous world averages. Numerous B_s^0 decay branching fractions, measured at the LHCb experiment, are also updated using the new values of f_s/f_d and branching fractions of normalization channels. These results reduce a major source of systematic uncertainty in several searches for new physics performed through measurements of B_s^0 branching fractions.

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I. INTRODUCTION

Measurements of branching fractions of B_s^0 meson decays are sensitive tools to test the Standard Model (SM) of particle physics. They often require knowledge of the B_s^0 production rate. To avoid uncertainties related to the b-hadron production cross section and integrated luminosity, and to partly cancel those related to detection efficiencies, at hadron colliders the B_s^0 branching fractions are often measured relative to other B-meson decay channels. In the absence of any precisely known B_s^0 branching fraction, most measurements are normalized to B^+ or B^0 meson decays, and thus require the ratio of their fragmentation fractions as input. The fragmentation fractions, denoted as f_u, f_d, f_s, and f_{baryon}, are the probabilities for a b quark to hadronize into a B^+, B^0, B_s^0 meson or a b baryon.[1] These fractions include contributions from intermediate states decaying to the aforementioned hadrons via the strong or electromagnetic interaction.

The b-hadron fragmentation fractions in proton-proton (pp) collisions at the Large Hadron Collider (LHC) energies are in general different from those measured at e^+e^- colliders [1–4] or in $p\bar{p}$ collisions at the Tevatron [5], with which they were previously averaged [6,7]. The ratios of fragmentation fractions are found to depend on kinematics, in particular on the b-hadron transverse momentum with respect to the beam direction (p_{T}); the dependence on the b-hadron pseudorapidity (η) has also been studied, but not found to be significant [5,8,9]. The ratio of fragmentation fractions f_s/f_u has also been shown to depend on the pp collision center-of-mass energy $\sqrt{s}$ [10]. In the following, $f_u = f_d$ is assumed to hold due to isospin symmetry.

The $B_s^0 \to J/\psi\phi$ decay is among the most studied of the B_s^0-meson decays, owing to its relative abundance and high reconstruction efficiency. As such, this decay is used as the normalization channel for several other B_s^0 decays [11–15]. Despite this, the precision on its branching fraction is still limited; the most precise measurement was performed by the LHCb experiment with pp collision data collected at $\sqrt{s} = 7$ TeV, corresponding to an integrated luminosity of 1 fb^{-1}. This measurement yields $\mathcal{B}(B_s^0 \to J/\psi\phi) = (1.050 \pm 0.013 \pm 0.064 \pm 0.082) \times 10^{-3}$ [16], where the first uncertainty is statistical, the second systematic, including the external branching fraction measurement of $B^+ \to J/\psi K^+$ decays, and the third is due to the measurement of f_s/f_d [8]. Other measurements were performed by the Belle [17] and CDF [18] Collaborations.

The $B_s^0 \to D_s^- \pi^+$ decay is another important B_s^0 meson decay mode, which is used as the normalization channel for several hadronic B_s^0 decays with a single charm meson in the final state; its branching fraction can be used to test for the presence of physics beyond the SM in tree-level hadronic B decays [19]. However, the current

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[1]The inclusion of the charge-conjugate modes is implied throughout this paper.

TABLE I. Five sets of measurements by the LHCb experiment combined in this paper and their sensitivity to fragmentation fractions and branching fractions.

Final state	$\sqrt{s}$, TeV	Relative or absolute	Sensitivity	References
$B \to \bar{D}X\mu^+\nu_\mu$	7	Absolute	f_s/f_d	[8]
$B \to \bar{D}X\mu^+\nu_\mu$	13	Absolute	f_s/f_d	[23]
$B_s^0 \to D_s^-\pi^+$, $B^0 \to D^-K^+$	7	Absolute	f_s/f_d	[9]
$B_s^0 \to D_s^-\pi^+$, $B^0 \to D^-\pi^+$	7	Relative	f_s/f_d	[9]
$B_s^0 \to D_s^-\pi^+$, $B^0 \to D^-\pi^+$	7,8,13	Absolute	f_s/f_d, $\mathcal{B}(B_s^0 \to D_s^-\pi^+)$	[24]
$B_s^0 \to J/\psi\phi$, $B^+ \to J/\psi K^+$	7,8,13	Relative	f_s/f_d, $\mathcal{B}(B_s^0 \to J/\psi\phi)$	[10]

precision on its branching fraction is also limited; the current best measurement by the LHCb experiment was performed using pp collision data collected at $\sqrt{s} = 7$ TeV, corresponding to 0.37 fb^{-1} of integrated luminosity. This measurement yields $\mathcal{B}(B_s^0 \to D_s^-\pi^+) = (2.95 \pm 0.05 \pm 0.17^{+0.18}_{-0.22}) \times 10^{-3}$ [20], where the first uncertainty is statistical, the second systematic, including the external branching fraction measurement of $B^0 \to D^-\pi^+$ decays, and the third due to the measurement of f_s/f_d taken from Ref. [8]. Other measurements were performed by the Belle [21] and CDF [22] collaborations.

The knowledge of B_s^0 branching fractions is thus often limited by the precision of the fragmentation fraction ratios. This paper presents a simultaneous determination of the fragmentation fractions and B_s^0 branching fractions with different decay modes. A combined analysis of LHCb measurements sensitive to f_s/f_d is performed in order to determine a precise value of this ratio as a function of $\sqrt{s}$ and p_T as well as the $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^-\pi^+$ branching fractions. This analysis employs previous LHCb measurements performed with ratios of semileptonic decays $B \to \bar{D}X\mu^+\nu_\mu$ at $\sqrt{s} = 7$ [8] and 13 TeV [23], where X denotes possible additional particles, hadronic $B \to Dh$ decays, where $h = \pi, K$, at $\sqrt{s} = 7$, 8, and 13 TeV [9,24], and $B \to J/\psi h'$ decays, where $h' = K, \phi$, at $\sqrt{s} = 7$, 8, and 13 TeV [10]. Measurements at 7 and 8 TeV were performed with data taken in 2010, 2011, and 2012, during Run 1 of the LHC; measurements at 13 TeV were performed with data taken in 2015 and 2016, during Run 2 of the LHC. Combinations of the Run 1 measurements were performed in Refs. [9,25] and are superseded by this paper.

This paper is organized as follows: In Sec. II, the LHCb detector and the measurements used in this analysis are presented, along with their sensitivities to the fragmentation fractions and branching fractions. The combined fit to the data is introduced in Sec. III. The results of the fit for the differential and integrated fragmentation fractions and for the $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^-\pi^+$ branching fractions are presented in Sec. IV. In Sec. V, these results are used to update about 60 different B_s^0 branching fractions measured so far by the LHCb experiment. In Sec. VI, the data are also described by a function inspired by the Tsallis statistics. Finally, conclusions are drawn in Sec. VII.

II. MEASUREMENTS

The LHCb detector [26,27] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. Simulation is used to model the effects of the detector acceptance and the imposed selection requirements. In the simulation, pp collisions are generated using PYTHIA [28] with a specific LHCb configuration [29]. Decays of unstable particles are described by EvtGen [30], in which final-state radiation is generated using PHOTOS [31]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [32] as described in Ref. [33].

The five sets of measurements by the LHCb experiment [8–10,23,24] that are combined in this paper rely on three different final states, referred to as semileptonic, hadronic, and charmonium final states. They are used to determine the ratio of efficiency-corrected yields n_corr of $B_s^0 \to Y$ decays relative to B^+ or $B^0 \to Z$ decays, which is sensitive to the ratio of branching fractions $\mathcal{B}$ multiplied by $f_s/f_{d(u)}$,

$$\frac{n_\mathrm{corr}(B_s^0 \to Y)}{n_\mathrm{corr}(B^{0(+)} \to Z)} = \frac{\mathcal{B}(B_s^0 \to Y)}{\mathcal{B}(B^{0(+)} \to Z)} \frac{f_s}{f_{d(u)}}, \qquad (1)$$

where $\mathcal{B}$ is the exclusive branching fraction for the hadronic and charmonium measurements and the inclusive one for the semileptonic measurement. The five sets of measurements and their sensitivity to fragmentation fractions and branching fractions are summarized in Table I.

The various measurements have different ranges in pseudorapidity and transverse momentum of the B meson. The semileptonic and hadronic measurements are performed for $\eta \in [2, 5]$, while the charmonium measurement extends this range to $\eta \in [2, 6.4]$. As no pseudorapidity dependence is seen in the measurements under consideration, the fiducial region in which the combined analysis is considered valid includes the latter range. The combined analysis is performed as a function of p_T in the widest of the individual ranges, $p_\mathrm{T} \in [0.5, 40]$ GeV$/c$, which is used in the charmonium measurement; it is maintained as the fiducial region. The semileptonic measurement is performed for $p_\mathrm{T} \in [4, 25]$ GeV$/c$ and the hadronic measurement for $p_\mathrm{T} \in [1.5, 40]$ GeV$/c$.

The semileptonic measurements [8,23] use inclusive $B \to \bar{D}X\mu^+\nu_\mu$ decays, having reconstructed a ground-state charm meson and a muon. The decay width of $b \to u$ decays is expected to be approximately 1% [7] of the total semileptonic width and almost equal for B_s^0, B^0, and B^+ mesons and is thus ignored. The modes studied are $B_s^0 \to D_s^- X\mu^+\nu_\mu$, $B_s^0 \to \bar{D}\,\bar{K}\,X\mu^+\nu_\mu$ for the B_s^0 meson, and $B^{+,0} \to \bar{D}^0 X\mu^+\nu_\mu$ and $B^{+,0} \to D^- X\mu^+\nu_\mu$ for the B^+ and B^0 mesons, the contributions of which are not separated. As the $B_s^0 \to D^-\bar{K}^0 X\mu^+\nu_\mu$ final state cannot be reconstructed with high efficiency at the LHCb experiment, its contribution is inferred from the $B_s^0 \to \bar{D}^0 K^- X\mu^+\nu_\mu$ rate and the known decay modes of excited D_s^+ mesons to $D\,K$ and $D^*\,K$ final states. The charm mesons are reconstructed using the decays $D_s^- \to K^-K^+\pi^-$, $D^- \to K^+\pi^-\pi^-$, and $\bar{D}^0 \to K^+\pi^-$. The inclusive semileptonic decay widths for B_s^0, B^0, and B^+ mesons are almost equal, apart from an SU(3) breaking correction factor of $1-\xi_s = 1.010 \pm 0.005$ [34], and are normalized to the corresponding total widths through the ratio of B_s^0 over B^+ and B^0 lifetimes, denoted as $\tau_{B_s^0}$, τ_{B^+}, and τ_{B^0}. Accordingly, $f_s/(f_u+f_d)$ is determined as

$$\frac{f_s}{f_u+f_d} = \frac{n_{\rm corr}(B_s^0 \to D_s^- X\mu^+\nu_\mu) + n_{\rm corr}(B_s^0 \to \bar{D}\,\bar{K}\,X\mu^+\nu_\mu)}{n_{\rm corr}(B^{+,0} \to \bar{D}^0 X\mu^+\nu_\mu) + n_{\rm corr}(B^{+,0} \to D^- X\mu^+\nu_\mu)} \frac{\tau_{B^+}+\tau_{B^0}}{2\tau_{B_s^0}}(1-\xi_s) - \varepsilon_{\rm ratio}\frac{\mathcal{B}(B^{+,0} \to D_s^-\bar{K}X\mu^+\nu_\mu)}{\mathcal{B}_{\rm SL}}, \quad (2)$$

where the efficiency-corrected yields $n_{\rm corr}$ incorporate the relevant charm-meson branching fractions. The second term is small and is included to subtract the components from $B^{+,0} \to D_s^-\bar{K}X\mu^+\nu_\mu$ decays which are reconstructed in the $B_s^0 \to D_s^- X\mu^+\nu_\mu$ sample, and contains $\varepsilon_{\rm ratio}$, which is the ratio of efficiencies of reconstructing $B_s^0 \to D_s^- X\mu^+\nu_\mu$ and $B^{+,0} \to D_s^-\bar{K}X\mu^+\nu_\mu$ through reconstruction of the $D_s^-\mu^+$ pair, and $\mathcal{B}_{\rm SL}$, which is the semileptonic branching fraction of B_s^0 mesons [23]. The efficiency-corrected yields have been corrected for cross feeds; e.g., those in the denominator have had cross feed contributions, from $B_s^0, \Lambda_b^0 \to \bar{D}X\mu^+\nu_\mu$ decays, subtracted. The Run 1 measurement determines the integrated[2] value of $f_s/(f_u+f_d)$ at $\sqrt{s} = 7$ TeV using a data sample corresponding to an integrated luminosity of 3 pb^{-1} [8]. The Run 2 measurement determines the value of $f_s/(f_u+f_d)$ in intervals of B meson $p_{\rm T}$ at $\sqrt{s} = 13$ TeV using data corresponding to an integrated luminosity of 1.7 fb^{-1} [23].

The hadronic measurements [9,24] make use of $B^0 \to D^-\pi^+$, $B^0 \to D^-K^+$, and $B_s^0 \to D_s^-\pi^+$ decays, using the same decay modes for the charm mesons as for the semileptonic analysis ($D_s^- \to K^-K^+\pi^-$ and $D^- \to K^+\pi^-\pi^-$). As the ratio of branching fractions of the $B_s^0 \to D_s^-\pi^+$ decay relative to $B^0 \to D^-h^+$ decays is predicted [35,36], f_s/f_d can be determined according to

$$\frac{f_s}{f_d} = \Phi_{{\rm PS},D^-K^+}\left|\frac{V_{us}}{V_{ud}}\right|^2\left(\frac{f_K}{f_\pi}\right)^2\frac{\tau_{B^0}}{\tau_{B_s^0}}\frac{1}{\mathcal{N}_a\mathcal{N}_F} \times \frac{\mathcal{B}(D^- \to K^+\pi^-\pi^-)}{\mathcal{B}(D_s^- \to K^-K^+\pi^-)}\frac{n_{\rm corr}(B_s^0 \to D_s^-\pi^+)}{n_{\rm corr}(B^0 \to D^-K^+)}, \quad (3a)$$

$$\frac{f_s}{f_d} = \Phi_{{\rm PS},D^-\pi^+}\frac{\tau_{B^0}}{\tau_{B_s^0}}\frac{1}{\mathcal{N}_a\mathcal{N}_F\mathcal{N}_E}\frac{\mathcal{B}(D^- \to K^+\pi^-\pi^-)}{\mathcal{B}(D_s^- \to K^-K^+\pi^-)} \times \frac{n_{\rm corr}(B_s^0 \to D_s^-\pi^+)}{n_{\rm corr}(B^0 \to D^-\pi^+)}, \quad (3b)$$

where $\Phi_{\rm PS}$ is a phase-space factor, V_{us} and V_{ud} are the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements, and f_K and f_π are the kaon and pion decay constants, which have permille uncertainties [7]. The remaining factors describe corrections to this ratio from nonfactorizable effects $\mathcal{N}_a$, the form factors $\mathcal{N}_F$, and exchange diagram contributions to the $B^0 \to D^-\pi^+$ decay $\mathcal{N}_E$. The hadronic Run 1 measurement in Ref. [9] uses a data sample corresponding to an integrated luminosity of 1 fb^{-1} at $\sqrt{s} = 7$ TeV and determines both ratios in Eqs. (3a) and (3b). The integrated value of f_s/f_d is determined using Eq. (3a); the $p_{\rm T}$ dependence of f_s/f_d is determined in intervals of $p_{\rm T}$ using Eq. (3b). These results are included in a single dataset by scaling the $p_{\rm T}$ -dependent measurement with the $D^-\,\pi^+$ final state to the integrated value of f_s/f_d measured with the $D^-\,K^+$ final state. The hadronic ratio measurement in Ref. [24] uses data samples corresponding to integrated luminosities of 1, 2, and 2 fb^{-1} at $\sqrt{s} = 7$, 8, and 13 TeV, respectively, to determine the ratio with $D^-\,\pi^+$ final state in Eq. (3b), which is sensitive to the integrated value for f_s/f_d at each collision energy.

The charmonium measurement determines the $p_{\rm T}$ dependence of f_s/f_u at $\sqrt{s} = 7$, 8, and 13 TeV using data samples corresponding to integrated luminosities of 1, 2, and 1.4 fb^{-1}, respectively [10]. It uses the decay modes $B_s^0 \to J/\psi\phi$ and $B^+ \to J/\psi K^+$, where the ϕ meson decays to K^+K^- and leads to

$$\frac{f_s}{f_u} = \frac{n_{\rm corr}(B_s^0 \to J/\psi\phi)}{n_{\rm corr}(B^+ \to J/\psi K^+)}\frac{\mathcal{B}(B^+ \to J/\psi K^+)}{\mathcal{B}(B_s^0 \to J/\psi\phi)\mathcal{B}(\phi \to K^+K^-)} = \frac{\mathcal{R}}{\mathcal{F}_R}, \quad (4)$$

[2]Throughout this text, integrated f_s/f_d or $f_s/(f_u+f_d)$ refer to measurements integrated over B-meson kinematics.

TABLE II. External inputs used in the hadronic and semileptonic analyses updated with respect to previous publications. The value of $\mathcal{N}_E$ is updated using Ref. [7]. The values of CKM matrix elements ratio $|V_{us}|/|V_{ud}|$ and of the meson decay constants' ratio f_K/f_π are the same as in Ref. [9].

Input	Value	References
$\mathcal{B}(\bar{D}^0 \to K^+\pi^-)$	$(3.999 \pm 0.045)\%$	[6]
$\mathcal{B}(D^- \to K^+\pi^-\pi^-)$	$(9.38 \pm 0.16)\%$	[7]
$\mathcal{B}(D_s^- \to K^-K^+\pi^-)$	$(5.47 \pm 0.10)\%$	[6,39]
$\tau_{B_s^0}/\tau_{B^0}$	1.006 ± 0.004	[6]
$(\tau_{B^+} + \tau_{B^0})/2\tau_{B_s^0}$	1.032 ± 0.005	[6]
$(1-\xi_s)$	1.010 ± 0.005	[34]
$\mathcal{N}_a$	1.000 ± 0.020	[36]
$\mathcal{N}_F$	1.000 ± 0.042	[19,40]
$\mathcal{N}_E$	0.966 ± 0.062	[7,36]
$\lvert V_{us}\rvert f_K/\lvert V_{ud}\rvert f_\pi$	0.2767	[9]

where $\mathcal{R}$ is the ratio of efficiency-corrected yields and $\mathcal{F}_R$ denotes the ratio of branching fractions. As no prediction is available for the ratio $\mathcal{F}_R$, this is included as a free parameter in the fit and is an additional result from this analysis.[3] The ratio $\mathcal{F}_R$ is therefore constrained in this measurement by the overall scale of f_s/f_d through the information provided by the analysis of the other final states; however, the large yield of this decay mode is very powerful for studying the $\sqrt{s}$ and p_{T} dependence of the fragmentation fraction ratio. The measurement in Ref. [16] includes a full amplitude analysis of the $B_s^0 \to J/\psi K^+K^-$ decay in order to separate the components in the K^+K^- spectrum. The largest resonant contributions are from the $f_0(980)$, the ϕ, and the $f'(1525)$ mesons. In the mass region close to the ϕ resonance, in addition to the $f_0(980)$ meson, there is also a nonresonant S-wave component. The total S-wave fraction is in general not negligible [16] and varies as a function of the K^+K^- invariant mass. When considering a small window around the ϕ resonance mass, the S-wave contribution is significantly reduced. The $B_s^0 \to J/\psi\phi$ measurement from Ref. [10] required a tight mass window of ± 10 MeV around the ϕ mass; therefore, the contribution of the S-wave component is suppressed to $(1.0 \pm 0.2)\%$. This contribution is subtracted from the final value of the branching fraction reported in this paper.

To determine f_s/f_d, the semileptonic and hadronic measurements rely on external inputs from theory and experiment: most prominently, the D^-, $\bar{D}^0$, and D_s^- meson branching fractions to the considered decay modes, the B^+, B^0, and B_s^0 meson lifetimes, and the theory predictions for the $\mathcal{N}_a$, $\mathcal{N}_F$, and $\mathcal{N}_E$ parameters. In this combined analysis, all of the external inputs have been updated to their currently best known values, as shown in Table II. For $\mathcal{B}(D_s^- \to K^-K^+\pi^-)$, a recent result from BESIII [39] is included and the weighted average of all current measurements is taken. For $\mathcal{N}_E$, the prediction from Ref. [36] is used, which is based on the ratio of branching fractions of the decays $B^0 \to D^{*-}K^+$ and $B^0 \to D^{*-}\pi^+$ and is updated using their current world averages [7]. The measurements and their uncertainties are thus rescaled to take into account the updated external inputs. The variation of the B-meson lifetimes could affect the estimates of the efficiencies used to determine f_s/f_d; it has been checked that this effect is negligible compared to the systematic uncertainties associated with each measurement.

[3]In a measurement by the ATLAS Collaboration [37] the ratio $\mathcal{R}$ was converted to a value for f_s/f_d using a prediction for the ratio of the $B_s^0 \to J/\psi\phi$ and $B^0 \to J/\psi K^{*0}$ branching fractions [38]. In this paper, results from Ref. [38] are not used because of disputed theoretical uncertainties arising from the assumption of factorization.

III. COMBINED FIT

The fit to the data is performed as a minimization of the χ^2 function

$$\chi^2 = (f(x|\theta) - y)V^{-1}(f(x|\theta) - y)^T + \sum_i \left(\frac{\theta_i - \hat{\theta}_i}{\sigma_{\theta_i}}\right)^2, \qquad (5)$$

where f is the function describing f_s/f_d in the data, with $x = p_{\mathrm{T}}$ or η, and y is the vector containing the central values of the measured observables sensitive to f_s/f_d, and V is their covariance matrix. The set of parameters to be determined θ includes a subset of parameters that are constrained to external measurements $\hat{\theta}_i$ with their uncertainties σ_{θ_i}. While the first term in Eq. (5) is due to the experimental data compared with the function to be fitted, the second is due to external constraints on some of the parameters. These constraints are of two kinds: external constraints on theoretical input parameters and overall scaling parameters to take into account scale-related systematic uncertainties for some of the analyses. These uncertainties are not included in the data points, to avoid the bias described in Ref. [41], due to the failure of the intrinsic assumptions of the χ^2 method and are thus taken into account as suggested in Ref. [42].

The scale factors related to the theoretical inputs, owing to their larger uncertainties, are found to have fitted values that differ from the input ones by up to 1 standard deviation. For this reason, these are kept indicated explicitly as ratios of the fitted value to the input value in the presentation of results. They are indicated by $r_{AF} = (\mathcal{N}_a\mathcal{N}_F)^{\mathrm{fitted}}/(\mathcal{N}_a\mathcal{N}_F)^{\mathrm{input}}$ for those common to the hadronic measurements and as $r_E = \mathcal{N}_E^{\mathrm{fitted}}/\mathcal{N}_E^{\mathrm{input}}$ for the exchange-diagram inputs.

TABLE III. Observables and related parameters of the default fit. See text for a detailed explanation.

Observable	Parameters	Fit mode
f_s/f_d	$a(7)$, $a(8)$, $a(13)$ TeV	Free
	$b(7)$, $b(8)$, $b(13)$ TeV	Free
$\mathcal{B}(B_s^0 \to D_s^- \pi^+)$	r_{AF}	Gaussian constrained
	r_E	Gaussian constrained
$\mathcal{B}(B_s^0 \to J/\psi\phi)$	$\mathcal{F}_R$	Free
	S_1	Gaussian constrained
	S_2, S_3, S_4	Gaussian constrained

The uncertainties from inputs common to the semileptonic and hadronic measurements, including the B-meson lifetimes and D-meson branching fractions, are 100% correlated among the hadronic measurements and 68% correlated with the semileptonic measurement, based on the relative rates of the $B_s^0 \to D_s^- X\mu^+\nu_\mu$ and $B_s^0 \to \bar{D}\,\bar{K}\,X\mu^+\nu_\mu$ decays and of the $B^{+,0} \to \bar{D}^0 X\mu^+\nu_\mu$ and $B^{+,0} \to D^- X\mu^+\nu_\mu$ decays.

The fit model as a function of p_T assumes the common functional form

$$\frac{f_s}{f_d}(p_\mathrm{T}, \sqrt{s}) = a + b \cdot p_\mathrm{T}. \tag{6}$$

The dependence on collision energy is expressed by letting intercept a and slope b parameters have different values at different $\sqrt{s}$. Fits with different functional forms have been performed and the data can also be described with exponential, Gaussian, or power-law functions, with similar fit quality. Attempts to describe the data with other functional forms suggested in Ref. [43] resulted in significantly worse fit quality. No attempt was made to describe the data with more parameters, with the exception of the physics-motivated fit with the Tsallis-statistics-inspired function, described at the end of the paper.

The parameters of the default fit are summarized in Table III together with the observables to which they are sensitive. In addition to the a and b parameters of Eq. (6), the only free parameter is $\mathcal{F}_R$, the ratio of $B_s^0 \to J/\psi\phi$ and $B^+ \to J/\psi K^+$ branching fractions. The other parameters are all Gaussian constrained to unity with the relevant uncertainty. They include r_{AF}, r_E as defined above, S_1, the parameter propagating the correlated systematic uncertainty of semileptonic and hadronic measurements due to external parameters, and S_2, S_3, and S_4, the parameters propagating experimental systematic uncertainties on the input measurements.

IV. RESULTS

Results of the default fit are presented in the following described separately for the differential f_s/f_d results (Sec. IV A), for the $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^- \pi^+$ branching fractions (Sec. IV B), and for the integrated f_s/f_d (Sec. IV C). Values and uncertainties of the parameters and their correlations are reported in the Supplemental Material [44].

A. Determination of f_s/f_d

The data as a function of p_T together with the result of the fit are shown in Fig. 1. The obtained functions at the three different energies are

$$f_s/f_d(p_\mathrm{T}, 7\ \mathrm{TeV}) = (0.244 \pm 0.008) + ((-10.3 \pm 2.7) \times 10^{-4}) \cdot p_\mathrm{T},$$
$$f_s/f_d(p_\mathrm{T}, 8\ \mathrm{TeV}) = (0.240 \pm 0.008) + ((-3.4 \pm 2.3) \times 10^{-4}) \cdot p_\mathrm{T},$$
$$f_s/f_d(p_\mathrm{T}, 13\ \mathrm{TeV}) = (0.263 \pm 0.008) + ((-17.6 \pm 2.1) \times 10^{-4}) \cdot p_\mathrm{T},$$

where the p_T is in units of GeV$/c$ and the slope parameters are expressed in $(\mathrm{GeV}/c)^{-1}$. The resulting χ^2 is 133, for a number of effective degrees of freedom of 74. The statistical robustness of the procedure has been verified using ensembles of pseudoexperiments. They demonstrate that the procedure obtains the correct coverage and minimal bias for the parameters of interest. In the most extreme case, the bias corresponds to about 10% of the uncertainties on the parameters related to the overall scale. This is considered negligible and not corrected for. The p-value of the fit to data, calculated from the distribution of pseudoexperiment χ^2 values, is 1.4×10^{-4}. When artificially increasing the data uncertainties such that the χ^2 corresponds to a p-value of 0.5, following similar procedures to those in Ref. [7], the central values and uncertainties obtained in this paper are unchanged, with the exception of uncertainties on the slopes versus p_T, which would increase by approximately a relative 25% but not affect the integrated measurement of f_s/f_d. More data will be needed to resolve the exact p_T dependence of f_s/f_d.

Requiring identical intercepts and slopes at the three energies results in significantly worse fit quality, with a difference in χ^2 of 115 for two fewer parameters. An F-test [45] is performed to verify the significance of the dependence of the intercept on the energy; the difference in χ^2 corresponds to an F-test statistic of 13.2 and to a significance of 5.9 standard deviations (σ). Similarly, but less significantly, requiring only the slope parameters to be common among the energies increases the χ^2 by 22 for two fewer parameters, corresponding to an F-test significance of 2.7σ.

Many of the input measurements also provide results as a function of pseudorapidity, none of them reporting any dependence on η. A combined fit as a function of η is also performed here. No dependence on pseudorapidity is found and the f_s/f_d value is found to be in agreement with the

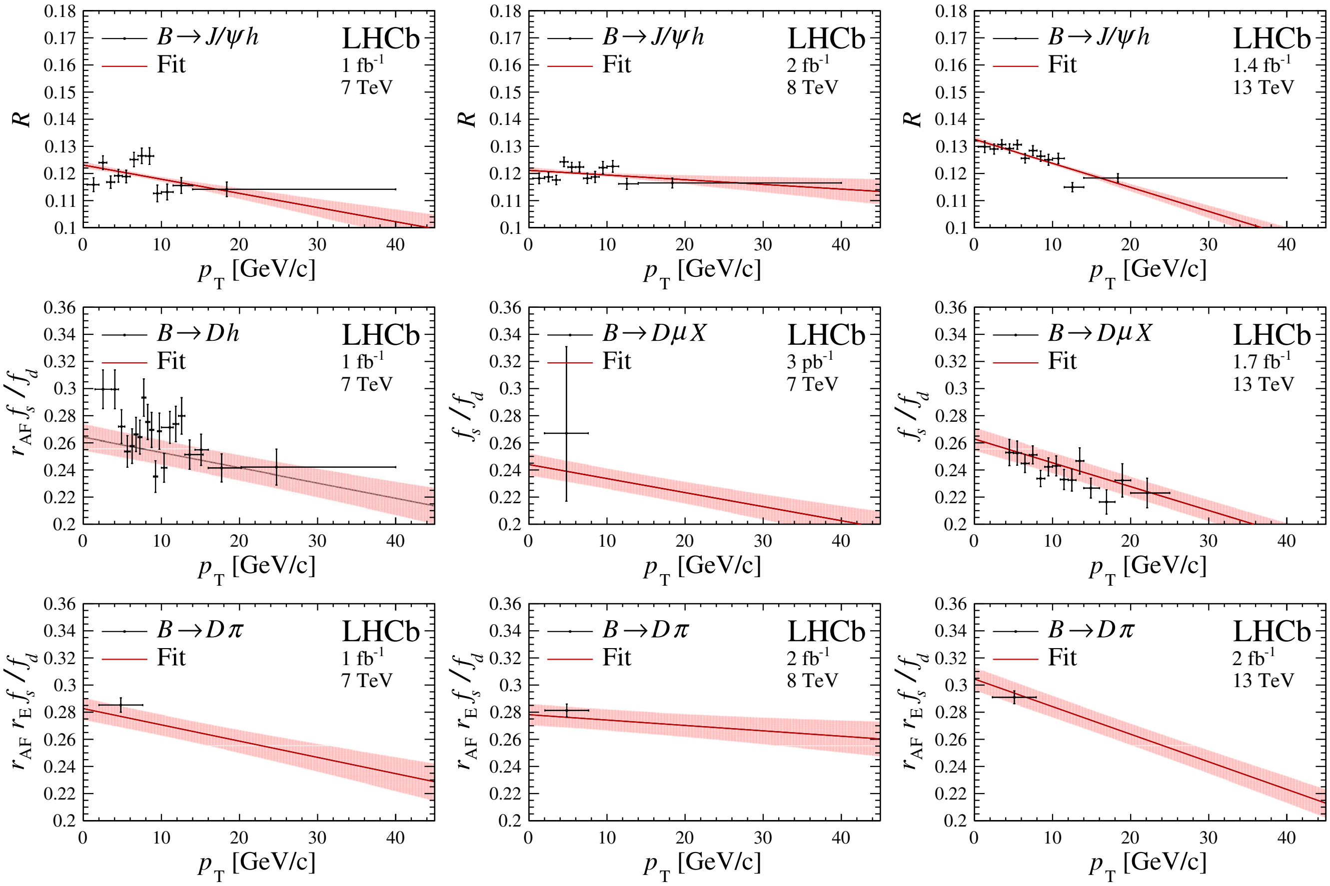

FIG. 1. Measurements of f_s/f_d sensitive observables as a function of the B-meson transverse momentum p_{T} overlaid with the fit function. The scaling factors r_{AF} and r_E are defined in the text; the variable $\mathcal{R}$ is defined in Eq. (4). The vertical axes are zero suppressed. The uncertainties on the data points are fully independent of each other; overall uncertainties for measurements in multiple p_{T} intervals are propagated via scaling parameters, as described in the text. The band associated with the fit function shows the uncertainty on the postfit function for each sample.

one obtained through the fit as a function of transverse momentum.

B. $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^- \pi^+$ branching fractions

An additional output from the fit is $\mathcal{F}_R$, the ratio of the relative $B_s^0 \to J/\psi\phi$ (with $\phi \to K^+K^-$) to $B^+ \to J/\psi K^+$ branching fractions, as in Eq. (4). The measurement of the $B_s^0 \to J/\psi\phi$ branching fraction reported here is time integrated and as such should be compared with theoretical predictions that include a correction for the finite $B_s^0 - \bar{B}_s^0$ width difference [46]. In addition, the total efficiency varies for different effective lifetimes; therefore, branching fraction measurements should be reported for a given effective lifetime value [47]. In this paper the results are obtained assuming the $B_s^0 \to J/\psi\phi$ parameters measured in Ref. [48], which reports the time-dependent analysis of this decay and the combination with previous LHCb measurements. The parameters used in this analysis correspond to a $B_s^0 \to J/\psi\phi$ effective lifetime of $\tau_{\mathrm{eff}} = 1.487$ ps, which is different by 2.4% from that used in the simulation for the efficiency in Ref [10]. The $\mathcal{R}$ measurements are corrected to take this into account. A scaling for different effective lifetimes is reported in Fig. 2 and should be used as multiplicative

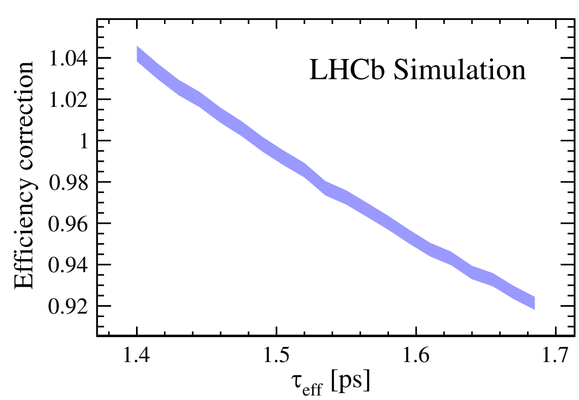

FIG. 2. Efficiency correction versus effective lifetime hypothesis for the $B_s^0 \to J/\psi\phi$ branching fraction. The band shows the uncertainty on the correction due to the simulated sample size for a given effective lifetime.

correction to recompute the $B_s^0 \to J/\psi\phi$ branching fraction under different hypotheses.

The fit value for the $\mathcal{F}_R$ parameter is 0.505 ± 0.016. The uncertainty is reduced to 0.012 when fixing external parameters, the remaining portion is dominated by the experimental systematic uncertainties on the input measurements. The $\mathcal{F}_R$ result can be converted to the $B_s^0 \to J/\psi\phi$ branching fraction including the $\phi \to K^+K^-$ decay branching fraction, by multiplying with the $B^+ \to J/\psi K^+$ branching fraction. The relative production fraction of B^+ and B^0 mesons at B factories [49], 1.027 ± 0.037, is used to correct the input measurements [7] and the $B^+ \to J/\psi K^+$ branching fraction is found to be $(1.003 \pm 0.035) \times 10^{-3}$, resulting in

$$\mathcal{B}(B_s^0 \to J/\psi\phi, \phi \to K^+K^-) = (5.01 \pm 0.16 \pm 0.17) \times 10^{-4},$$

where the first uncertainty includes statistical and systematic uncertainties on the yield ratio as well as the uncertainties on external parameters, and the second arises from the external measurement of $\mathcal{B}(B^+ \to J/\psi K^+)$. This result is corrected for the presence of the S-wave component and for the effective lifetime, as mentioned earlier. Taking into account the $\phi \to K^+K^-$ branching fraction, $(49.2 \pm 0.5)\%$ [7], the $B_s^0 \to J/\psi\phi$ branching fraction is

$$\mathcal{B}(B_s^0 \to J/\psi\phi) = (1.018 \pm 0.032 \pm 0.037) \times 10^{-3},$$

where again the first uncertainty includes statistical and systematic uncertainties on the yield ratios as well as the uncertainties on external parameters, and the second is from external inputs. This result is compatible with and significantly more precise than the Particle Data Group (PDG) world average of $(1.08 \pm 0.08) \times 10^{-3}$ [7]. It should be noted that the PDG average includes a measurement by the LHCb experiment at 7 TeV that is at least partially correlated with the 7 TeV data sample used in the $\mathcal{R}$ measurement included in this paper. The measurement is consistent with the individual measurements by the Belle Collaboration, $(1.25 \pm 0.07 \pm 0.23) \times 10^{-3}$ [17], and the CDF Collaboration, $(1.5 \pm 0.5 \pm 0.1) \times 10^{-3}$ [18], although these have larger uncertainties.

The ratio of the branching fractions of $B_s^0 \to D_s^-\pi^+$ and $B^0 \to D^-\pi^+$ decays is expressed in terms of the theory parameters in Eq. (3a). However, the theory constraints can be removed and the fit can be repeated to estimate this quantity from data. The normalization of the f_s/f_d function is correspondingly shifted by a relative 2.5%, which is within the final uncertainties. The other parameters are found to be in good agreement. The uncertainties on all parameters do not change significantly with respect to the default fit. The output of this fit is then converted to a measurement of the above-mentioned ratio of branching fractions. The result is

$$\frac{\mathcal{B}(B_s^0 \to D_s^-\pi^+)}{\mathcal{B}(B^0 \to D^-\pi^+)} = 1.18 \pm 0.04,$$

where the correlation of the D -meson branching fractions is considered when calculating this uncertainty. The uncertainty is reduced to 0.033 when fixing external parameters; the remaining portion is dominated by the experimental systematic uncertainties on the input measurements. This result can be compared with the ratio measured by the LHCb Collaboration using only 2011 data [20], which yields $\mathcal{B}(B_s^0 \to D_s^-\pi^+)/\mathcal{B}(B^0 \to D^-\pi^+) = 1.10 \pm 0.018 \pm 0.033^{+0.07}_{-0.08}$, where the uncertainties are statistical, systematic, and due to f_s/f_d, and with the current ratio of PDG averages of 1.19 ± 0.19 [7]. This result is in excellent agreement with both and significantly more precise. The relative production fraction of B^+ and B^0 mesons at the B factories [49], 1.027 ± 0.037, is used to correct the input measurements for the $B^0 \to D^-\pi^+$ branching fraction [7]; it is found to be $(2.72 \pm 0.14) \times 10^{-3}$. Using this value, the branching fraction of $B_s^0 \to D_s^-\pi^+$ decays is measured to be

$$\mathcal{B}(B_s^0 \to D_s^-\pi^+) = (3.20 \pm 0.10 \pm 0.16) \times 10^{-3},$$

where the first uncertainty is due to the total experimental uncertainties on the yield ratios and the uncertainties from external parameters and the second is due to the $B^0 \to D^-\pi^+$ branching fraction. This result is in agreement with and significantly more precise than the previous LHCb measurement [20], $\mathcal{B}(B_s^0 \to D_s^-\pi^+) = (2.95 \pm 0.05 \pm 0.17^{+0.18}_{-0.22}) \times 10^{-3}$, where the uncertainties are again statistical, systematic, and due to f_s/f_d, and the PDG average, $(3.00 \pm 0.23) \times 10^{-3}$, which is dominated by the latter.

C. Integrated f_s/f_d results

Reference p_T spectra, needed to calculate the integrated f_s/f_d ratios, are obtained by generating B_s^0 and B^0 mesons in the fiducial acceptance, without any simulation of the detector. The average p_T for these spectra are very similar for B_s^0 and B^0 mesons; they are 4.80, 4.85, and 5.10 GeV/c for the $\sqrt{s} = 7$, 8, and 13 TeV generated samples, respectively, with a standard deviation of about 2.8 GeV/c at all energies. The following integrated f_s/f_d values for $p_\mathrm{T} \in [0.5, 40]$ GeV/c and $\eta \in [2, 6.4]$ are measured

$$f_s/f_d(7\ \mathrm{TeV}) = 0.2390 \pm 0.0076,$$
$$f_s/f_d(8\ \mathrm{TeV}) = 0.2385 \pm 0.0075,$$
$$f_s/f_d(13\ \mathrm{TeV}) = 0.2539 \pm 0.0079,$$

which are shown in Fig. 3. Ratios of the integrated values at different energies have also been calculated, incorporating correlations between the uncertainties, yielding

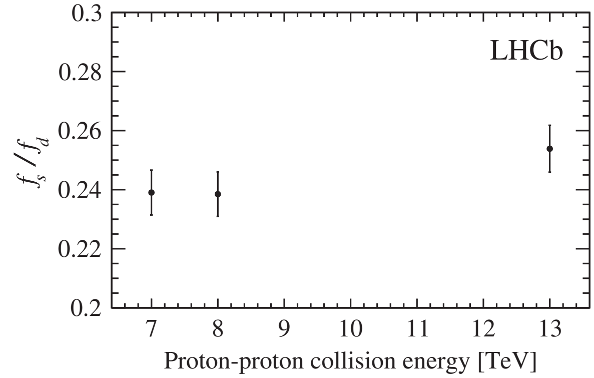

FIG. 3. Fragmentation fraction ratio f_s/f_d as a function of proton-proton center-of-mass energy.

$$\frac{f_s/f_d(13\ \text{TeV})}{f_s/f_d(7\ \text{TeV})} = 1.064 \pm 0.008,$$
$$\frac{f_s/f_d(13\ \text{TeV})}{f_s/f_d(8\ \text{TeV})} = 1.065 \pm 0.007,$$
$$\frac{f_s/f_d(8\ \text{TeV})}{f_s/f_d(7\ \text{TeV})} = 0.998 \pm 0.008,$$

which can be used to correctly normalize future analyses using data at different energies. These values are calculated assuming an equal average p_T of 5 GeV$/c$ for the different energies, however, it has been verified that varying this assumption does not modify the results significantly. In addition, the ratio of the Run 2 (13 TeV) over Run 1 (7 and 8 TeV) measurements has been computed, weighting the Run 1 values by their integrated luminosity (1 and 2 fb^{-1}, respectively), resulting in

$$\frac{f_s/f_d(\text{Run}\,2)}{f_s/f_d(\text{Run}\,1)} = 1.064 \pm 0.007.$$

TABLE IV. The branching fractions of B^0 and B^+ normalization channel decays used to update previous measurements of B_s^0 branching fractions, as reported in Ref. [7] for all but the $B^0 \to J/\psi K^{*0}$ branching fraction, which is taken from the amplitude analysis in Ref [50], and corrected for the relative production fraction of B^+ and B^0 mesons at B factories [49].

Decay mode	Branching fraction
$B^0 \to J/\psi K^{*0}$	$(1.21 \pm 0.08) \times 10^{-3}$
$B^0 \to J/\psi \rho^0$	$(2.58 \pm 0.18) \times 10^{-5}$
$B^0 \to J/\psi K^0_\mathrm{S}$	$(4.40 \pm 0.17) \times 10^{-3}$
$B^0 \to J/\psi K^0_\mathrm{S}\pi^+\pi^-$	$(2.18 \pm 0.19) \times 10^{-3}$
$B^0 \to \psi(2S) K^{*0}$	$(5.98 \pm 0.42) \times 10^{-4}$
$B^0 \to \psi(2S) K^+\pi^-$	$(5.88 \pm 0.42) \times 10^{-4}$
$B^0 \to K^+\pi^-$	$(1.98 \pm 0.07) \times 10^{-5}$
$B^0 \to K^0_\mathrm{S}\pi^+\pi^-$	$(2.51 \pm 0.11) \times 10^{-5}$
$B^0 \to K^{*+}\pi^-$	$(7.60 \pm 0.43) \times 10^{-6}$
$B^0 \to p\bar{p}K^+\pi^-$	$(6.30 \pm 0.50) \times 10^{-6}$
$B^0 \to p\bar{\Lambda}\pi^-$	$(3.18 \pm 0.30) \times 10^{-6}$
$B^0 \to K^{*0}\gamma$	$(4.13 \pm 0.26) \times 10^{-5}$
$B^0 \to \phi K^0_\mathrm{S}$	$(3.70 \pm 0.36) \times 10^{-6}$
$B^0 \to \phi K^{*0}$	$(1.01 \pm 0.05) \times 10^{-5}$
$B^0 \to D^-\mu^+\nu_\mu$	$(2.31 \pm 0.10)\%$
$B^0 \to D^{*-}\mu^+\nu_\mu$	$(5.05 \pm 0.14)\%$
$B^0 \to D^{*\pm}D^\mp$	$(6.2 \pm 0.6) \times 10^{-4}$
$B^0 \to D^+D^-$	$(2.14 \pm 0.19) \times 10^{-4}$
$B^0 \to D^-D_s^+$	$(7.3 \pm 0.8) \times 10^{-3}$
$B^+ \to \bar{D}^0 D_s^+$	$(9.0 \pm 0.9) \times 10^{-3}$
$B^0 \to \bar{D}^0\pi^+\pi^-$	$(8.8 \pm 0.5) \times 10^{-4}$
$B^0 \to \bar{D}^0\rho$	$(3.21 \pm 0.21) \times 10^{-4}$
$B^0 \to \bar{D}^0 K^0_\mathrm{S}$	$(5.3 \pm 0.7) \times 10^{-5}$
$B^0 \to \bar{D}^0 K^+K^-$	$(6.1 \pm 0.6) \times 10^{-5}$

V. UPDATED BRANCHING FRACTIONS MEASUREMENTS

Using the results for the integrated f_s/f_d, $\mathcal{B}(B_s^0 \to J/\psi\phi)$ and $\mathcal{B}(B_s^0 \to D_s^-\pi^+)$, previous LHCb measurements of B_s^0 branching fractions are updated by scaling these with either f_s/f_d and a B^0 or B^+ branching fraction, or with the associated normalization B_s^0 branching fraction. The B^0 and B^+ normalization branching fractions are updated using the current PDG world averages [7], corrected for the relative production fraction of B^+ and B^0 mesons at the B factories [49]. The sole exception is $\mathcal{B}(B^0 \to J/\psi K^{*0})$, for which the branching fraction is taken from the result of the only amplitude analysis, as performed by the Belle experiment [50]. The B^0 and B^+ normalization branching fractions are presented in Table IV. For LHCb measurements using both Run 1 and Run 2 data, an average f_s/f_d is estimated using the relative expected yields at the different energies, with the uncertainties from f_s/f_d and normalization mode branching fractions recomputed accordingly. Updating these inputs significantly reduces the systematic uncertainty from f_s/f_d on all previous B_s^0 branching fraction measurements, such that the updated results supersede those from the cited publications. The only exception is the branching fraction of $B_s^0 \to \mu^+\mu^-$ decays, for which the LHCb result updated here has less precision than the LHC-wide average determined recently [51], and which will be superseded only by future updates of this measurement with the full Run 2 data sample. The updated branching fractions are grouped according to decay type: rare B_s^0 decays are updated in Table V, B_s^0 decays with charmonium in Table VI, charmless B_s^0 decays in Table VII, and B_s^0 decays with charm mesons in Table VIII. As the estimated value of f_s/f_d for the Run 1 data samples decreased, in general the values of the branching fractions increase with

TABLE V. Updated branching fractions of rare B_s^0 decays. The uncertainties are statistical, systematic, due to f_s/f_d, and due to the normalization branching fraction. The $B_s^0 \to \phi\mu^+\mu^-$ branching fractions in different q^2 intervals, where q^2 is defined as dimuon invariant mass squared in GeV/c^2, are normalized with respect to $B_s^0 \to J/\psi\phi$. Results with the ⋆ symbol have had their normalization branching fraction updated as well.

Decay mode	Updated branching fraction	Previous result		
$B_s^0 \to \phi\gamma$	$(3.75 \pm 0.18 \pm 0.12 \pm 0.12 \pm 0.24) \times 10^{-5}$	$(3.52 \pm 0.17 \pm 0.11 \pm 0.29 \pm 0.12) \times 10^{-5}$	[55]	⋆
$B_s^0 \to \mu^+\mu^-$	$(3.26 \pm 0.65^{+0.22}_{-0.11} \pm 0.10) \times 10^{-9}$	$(3.0 \pm 0.6^{+0.2}_{-0.1} \pm 0.2) \times 10^{-9}$	[56]	
$B_s^0 \to \bar{K}^{*0}\mu^+\mu^-$	$(3.09 \pm 1.07 \pm 0.21 \pm 0.10 \pm 0.22) \times 10^{-8}$	$(2.9 \pm 1.0 \pm 0.2 \pm 0.2 \pm 0.2) \times 10^{-8}$	[57]	
$B_s^0 \to \pi^+\pi^-\mu^+\mu^-$	$(8.66 \pm 1.50 \pm 0.47 \pm 0.28 \pm 0.60) \times 10^{-8}$	$(8.6 \pm 1.5 \pm 0.5 \pm 0.5 \pm 0.7) \times 10^{-8}$	[58]	⋆
$B_s^0 \to \phi\mu^+\mu^-$	$(7.54^{+0.43}_{-0.41} \pm 0.30 \pm 0.36) \times 10^{-7}$	$(7.97^{+0.45}_{-0.43} \pm 0.32 \pm 0.60) \times 10^{-7}$	[14]	⋆
$q^2 \in [1.0, 6.0]$	$(2.44^{+0.31}_{-0.30} \pm 0.07 \pm 0.12) \times 10^{-8}$	$(2.58^{+0.33}_{-0.31} \pm 0.08 \pm 0.19) \times 10^{-8}$	[14]	⋆
$q^2 \in [15.0, 19.0]$	$(3.82^{+0.38}_{-0.36} \pm 0.12 \pm 0.18) \times 10^{-8}$	$(4.04^{+0.39}_{-0.38} \pm 0.13 \pm 0.30) \times 10^{-8}$	[14]	⋆
$q^2 \in [0.1, 2.0]$	$(5.54^{+0.69}_{-0.65} \pm 0.13 \pm 0.27) \times 10^{-8}$	$(5.85^{+0.73}_{-0.69} \pm 0.14 \pm 0.44) \times 10^{-8}$	[14]	⋆
$q^2 \in [2.0, 5.0]$	$(2.42^{+0.40}_{-0.38} \pm 0.06 \pm 0.12) \times 10^{-8}$	$(2.56^{+0.42}_{-0.39} \pm 0.06 \pm 0.19) \times 10^{-8}$	[14]	⋆
$q^2 \in [5.0, 8.0]$	$(3.03^{+0.42}_{-0.40} \pm 0.07 \pm 0.15) \times 10^{-8}$	$(3.21^{+0.44}_{-0.42} \pm 0.08 \pm 0.24) \times 10^{-8}$	[14]	⋆
$q^2 \in [11.0, 12.5]$	$(4.45^{+0.65}_{-0.62} \pm 0.14 \pm 0.21) \times 10^{-8}$	$(4.71^{+0.69}_{-0.65} \pm 0.15 \pm 0.36) \times 10^{-8}$	[14]	⋆
$q^2 \in [15.0, 17.0]$	$(4.28^{+0.54}_{-0.51} \pm 0.11 \pm 0.21) \times 10^{-8}$	$(4.52^{+0.57}_{-0.54} \pm 0.12 \pm 0.34) \times 10^{-8}$	[14]	⋆
$q^2 \in [17.0, 19.0]$	$(3.75^{+0.54}_{-0.51} \pm 0.13 \pm 0.18) \times 10^{-8}$	$(3.96^{+0.57}_{-0.54} \pm 0.14 \pm 0.30) \times 10^{-8}$	[14]	⋆

respect to their published values; the branching fractions normalized to $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^-\pi^+$ instead decrease with respect to their published values.

The recent measurement of $|V_{cb}|$ with $B_s^0 \to D_s^{(*)-}\mu^+\nu_\mu$ decays using Run 1 data [52] also relies on an estimate of f_s/f_d and is independent of the uncertainty on the product $\mathcal{B}(D_s^- \to K^-K^+\pi^-) \times \tau_{B_s^0}$. For this estimate, the correlation of f_s/f_d with $\mathcal{B}(D_s^- \to K^-K^+\pi^-)$ from the semileptonic measurement is used. The resulting estimates for $|V_{cb}|$ are $|V_{cb}|_{\mathrm{CLN}} = (40.8 \pm 0.6 \pm 0.9 \pm 1.1) \times 10^{-3}$,

TABLE VI. Updated branching fractions of B_s^0 decays with charmonia in the final state. The uncertainties are statistical, systematic, due to f_s/f_d, and due to the normalization branching fraction. The second, third, and fourth set of branching fractions are normalized to $B_s^0 \to J/\psi\phi$, $B_s^0 \to J/\psi\eta^{(\prime)}$, $B_s^0 \to J/\psi\pi^+\pi^-$, respectively, and their third uncertainty covers the full normalization uncertainty. Results with the ⋆ symbol have had their normalization branching fraction updated as well.

Decay mode	Updated branching fraction	Previous result		
$B_s^0 \to J/\psi K_S^0$	$(2.06 \pm 0.08 \pm 0.06 \pm 0.07 \pm 0.08) \times 10^{-5}$	$(1.93 \pm 0.08 \pm 0.05 \pm 0.11 \pm 0.07) \times 10^{-5}$	[59]	
$B_s^0 \to J/\psi K_S^0 K^\pm\pi^\mp$	$(5.01 \pm 0.35 \pm 0.33 \pm 0.16 \pm 0.44) \times 10^{-4}$	$(4.6 \pm 0.3 \pm 0.3 \pm 0.3 \pm 0.4) \times 10^{-4}$	[60]	⋆
$B_s^0 \to \psi(2S)\bar{K}^{*0}$	$(3.62 \pm 0.37 \pm 0.26 \pm 0.12 \pm 0.25) \times 10^{-5}$	$(3.35 \pm 0.34 \pm 0.24 \pm 0.19 \pm 0.22) \times 10^{-5}$	[61]	
$B_s^0 \to \psi(2S)K^+\pi^-$	$(3.43 \pm 0.23 \pm 0.14 \pm 0.11 \pm 0.24) \times 10^{-5}$	$(3.12 \pm 0.21 \pm 0.13 \pm 0.18 \pm 0.22) \times 10^{-5}$	[61]	
$B_s^0 \to J/\psi\eta$	$(4.04 \pm 0.35^{+0.32}_{-0.43} \pm 0.13 \pm 0.28) \times 10^{-4}$	$(3.79 \pm 0.31^{+0.20}_{-0.41} \pm 0.28 \pm 0.56) \times 10^{-4}$	[62]	⋆
$B_s^0 \to J/\psi\eta'$	$(3.67 \pm 0.32^{+0.14}_{-0.38} \pm 0.12 \pm 0.25) \times 10^{-4}$	$(3.42 \pm 0.30^{+0.14}_{-0.35} \pm 0.26 \pm 0.51) \times 10^{-4}$	[62]	⋆
$B_s^0 \to \psi(2S)\phi$	$(4.98 \pm 0.26 \pm 0.24 \pm 0.24) \times 10^{-4}$	$(5.33 \pm 0.28 \pm 0.26^{+1.37}_{-1.12}) \times 10^{-4}$	[12]	⋆
$B_s^0 \to \chi_{c1}\phi$	$(1.92 \pm 0.18 \pm 0.14 \pm 0.09) \times 10^{-5}$	$(1.98 \pm 0.19 \pm 0.15 \pm 0.20) \times 10^{-5}$	[63]	⋆
$B_s^0 \to J/\psi\pi^+\pi^-$	$(2.01 \pm 0.05 \pm 0.05 \pm 0.10) \times 10^{-4}$	$(2.16 \pm 0.05 \pm 0.06^{+0.51}_{-0.42}) \times 10^{-4}$	[11]	⋆
$B_s^0 \to J/\psi\phi\phi$	$(1.17 \pm 0.12^{+0.05}_{-0.09} \pm 0.06) \times 10^{-5}$	$(1.19 \pm 0.12^{+0.05}_{-0.09} \pm 0.10) \times 10^{-5}$	[15]	⋆
$B_s^0 \to J/\psi\bar{K}^{*0}$	$(4.12 \pm 0.19 \pm 0.13 \pm 0.20) \times 10^{-5}$	$(4.20 \pm 0.20 \pm 0.13 \pm 0.36) \times 10^{-5}$	[64]	⋆
$B_s^0 \to J/\psi p\bar{p}$	$(3.54 \pm 0.19 \pm 0.24 \pm 0.16) \times 10^{-6}$	$(3.58 \pm 0.19 \pm 0.24 \pm 0.30) \times 10^{-6}$	[65]	⋆
$B^0 \to J/\psi p\bar{p}$	$(3.94 \pm 0.35 \pm 0.26 \pm 0.13) \times 10^{-7}$	$(4.51 \pm 0.40 \pm 0.30 \pm 0.32) \times 10^{-7}$	[65]	⋆
$B_s^0 \to \psi(2S)\eta$	$(3.35 \pm 0.57 \pm 0.48 \pm 0.50) \times 10^{-4}$	$(3.15 \pm 0.53 \pm 0.45^{+0.61}_{-0.67}) \times 10^{-4}$	[66]	⋆
$B_s^0 \to \psi(2S)\eta'$	$(1.42 \pm 0.33 \pm 0.06 \pm 0.20) \times 10^{-4}$	$(1.32 \pm 0.31 \pm 0.05^{+0.26}_{-0.28}) \times 10^{-4}$	[67]	⋆
$B_s^0 \to J/\psi\pi^+\pi^-\pi^+\pi^-$	$(7.49 \pm 0.30 \pm 0.44 \pm 0.42) \times 10^{-5}$	$(7.62 \pm 0.36 \pm 0.64 \pm 0.42) \times 10^{-5}$	[68]	⋆
$B_s^0 \to \psi(2S)\pi^+\pi^-$	$(6.87 \pm 0.81 \pm 0.65 \pm 0.39) \times 10^{-5}$	$(7.3 \pm 0.9 \pm 0.6^{+1.9}_{-1.6}) \times 10^{-5}$	[66]	⋆

TABLE VII. Updated branching fractions of B_s^0 decays with a charmless final state. The uncertainties are statistical, systematic, due to f_s/f_d, and due to the normalization branching fraction. The last two branching fractions are normalized with respect to $B_s^0 \to \phi\phi$, and their third uncertainty covers the full normalization uncertainty. Results with the ⋆ symbol have had their normalization branching fraction updated as well.

Decay mode	Updated branching fraction	Previous result		
$B_s^0 \to \pi^+\pi^-$	$(7.60 \pm 0.58 \pm 0.69 \pm 0.25 \pm 0.25) \times 10^{-7}$	$(6.91 \pm 0.54 \pm 0.63 \pm 0.40 \pm 0.19) \times 10^{-7}$	[69]	
$B_s^0 \to K^-\pi^+$	$(6.15 \pm 0.49 \pm 0.49 \pm 0.20 \pm 0.20) \times 10^{-6}$	$(5.4 \pm 0.4 \pm 0.4 \pm 0.4 \pm 0.2) \times 10^{-6}$	[70]	⋆
$B_s^0 \to K^+K^-$	$(2.63 \pm 0.08 \pm 0.16 \pm 0.09 \pm 0.09) \times 10^{-5}$	$(2.30 \pm 0.07 \pm 0.14 \pm 0.17 \pm 0.07) \times 10^{-5}$	[70]	⋆
$B_s^0 \to K_S^0K_S^0$	$(8.28 \pm 1.60 \pm 0.90 \pm 0.26 \pm 0.81) \times 10^{-6}$	$(8.3 \pm 1.6 \pm 0.9 \pm 0.3 \pm 0.8) \times 10^{-6}$	[71]	
$B_s^0 \to K_S^0\pi^+\pi^-$	$(5.21 \pm 0.74 \pm 0.85 \pm 0.17 \pm 0.23) \times 10^{-6}$	$(4.7 \pm 0.7 \pm 0.8 \pm 0.3 \pm 0.2) \times 10^{-6}$	[72]	
$B_s^0 \to K_S^0K^\pm\pi^\mp$	$(4.64 \pm 0.19 \pm 0.30 \pm 0.15 \pm 0.21) \times 10^{-5}$	$(4.22 \pm 0.18 \pm 0.28 \pm 0.25 \pm 0.17) \times 10^{-5}$	[72]	
$B_s^0 \to K^{*0}\bar{K}^{*0}$	$(2.70 \pm 0.44 \pm 0.43 \pm 0.09 \pm 0.19) \times 10^{-5}$	$(2.81 \pm 0.46 \pm 0.43 \pm 0.34 \pm 0.13) \times 10^{-5}$	[73]	⋆
$B_s^0 \to K^{*\pm}K^\mp$	$(1.23 \pm 0.18 \pm 0.13 \pm 0.04 \pm 0.07) \times 10^{-5}$	$(1.27 \pm 0.19 \pm 0.13 \pm 0.07 \pm 0.10) \times 10^{-5}$	[74]	
$B_s^0 \to K^{*-}\pi^+$	$(3.21 \pm 1.07 \pm 0.41 \pm 0.10 \pm 0.18) \times 10^{-6}$	$(3.3 \pm 1.1 \pm 0.4 \pm 0.2 \pm 0.3) \times 10^{-6}$	[74]	
$B_s^0 \to p\bar{p}K^\pm\pi^\mp$	$(1.41 \pm 0.23 \pm 0.12 \pm 0.05 \pm 0.11) \times 10^{-6}$	$(1.30 \pm 0.21 \pm 0.11 \pm 0.09 \pm 0.08) \times 10^{-6}$	[75]	
$B_s^0 \to \overset{(-)}{p}\,\overset{(-)}{\Lambda}K^\mp$	$(6.01 \pm 0.66 \pm 0.62 \pm 0.20 \pm 0.57) \times 10^{-6}$	$(5.46 \pm 0.61 \pm 0.57 \pm 0.32 \pm 0.50) \times 10^{-6}$	[76]	
$B_s^0 \to \phi\bar{K}^{*0}$	$(1.27 \pm 0.28 \pm 0.16 \pm 0.04 \pm 0.07) \times 10^{-6}$	$(1.10 \pm 0.24 \pm 0.13 \pm 0.08 \pm 0.06) \times 10^{-6}$	[77]	⋆
$B_s^0 \to \phi\phi$	$(2.02 \pm 0.05 \pm 0.08 \pm 0.07 \pm 0.11) \times 10^{-5}$	$(1.84 \pm 0.05 \pm 0.07 \pm 0.11 \pm 0.12) \times 10^{-5}$	[78]	
$B_s^0 \to \phi\pi^+\pi^-$	$(3.82 \pm 0.25 \pm 0.19 \pm 0.30) \times 10^{-6}$	$(3.48 \pm 0.23 \pm 0.17 \pm 0.35) \times 10^{-6}$	[79]	⋆
$B_s^0 \to \phi\phi\phi$	$(2.36 \pm 0.61 \pm 0.30 \pm 0.19) \times 10^{-6}$	$(2.15 \pm 0.54 \pm 0.28 \pm 0.21) \times 10^{-6}$	[80]	⋆

TABLE VIII. Updated branching fractions of B_s^0 decays to open-charm final states. The uncertainties are statistical, systematic, due to f_s/f_d, and due to the normalization branching fraction. The $B_s^0 \to D_s^\mp K^\pm$, $B_s^0 \to D_s^-\pi^+\pi^-\pi^+$, and $B_s^0 \to D_s^-K^+\pi^-\pi^+, B_s^0 \to D_{s1}(2536)^-\pi^+$ branching fractions are normalized with respect to $B_s^0 \to D_s^-\pi^+$ and $B_s^0 \to D_s^-\pi^+\pi^-\pi^+$, respectively, and their third uncertainty covers the full normalization uncertainty. Results with the ⋆ symbol have had their normalization branching fraction updated as well.

Decay mode	Updated branching fraction	Previous result		
$B_s^0 \to D_s^{*-}\mu^+\nu_\mu$	$(5.19 \pm 0.24 \pm 0.47 \pm 0.13 \pm 0.14) \times 10^{-2}$	$(5.38 \pm 0.25 \pm 0.48 \pm 0.20 \pm 0.15) \times 10^{-2}$	[52]	
$B_s^0 \to D_s^-\mu^+\nu_\mu$	$(2.40 \pm 0.12 \pm 0.15 \pm 0.06 \pm 0.10) \times 10^{-2}$	$(2.49 \pm 0.12 \pm 0.16 \pm 0.09 \pm 0.11) \times 10^{-2}$	[52]	
$B_s^0 \to D^+D_s^-$	$(3.01 \pm 0.32 \pm 0.10 \pm 0.08 \pm 0.34) \times 10^{-4}$	$(2.7 \pm 0.3 \pm 0.1 \pm 0.2 \pm 0.3) \times 10^{-4}$	[81]	
$B_s^0 \to D^+D^-$	$(2.47 \pm 0.46 \pm 0.23 \pm 0.08 \pm 0.22) \times 10^{-4}$	$(2.2 \pm 0.4 \pm 0.1 \pm 0.1 \pm 0.3) \times 10^{-4}$	[82]	
$B_s^0 \to D^0\bar{D}^0$	$(1.83 \pm 0.29 \pm 0.29 \pm 0.05 \pm 0.18) \times 10^{-4}$	$(1.9 \pm 0.3 \pm 0.2 \pm 0.2 \pm 0.3) \times 10^{-4}$	[82]	
$B_s^0 \to D_s^+D_s^-$	$(4.38 \pm 0.23 \pm 0.31 \pm 0.11 \pm 0.49) \times 10^{-3}$	$(4.0 \pm 0.2 \pm 0.2 \pm 0.2 \pm 0.4) \times 10^{-3}$	[82]	
$B_s^0 \to D^{*\pm}D^{*\mp}$	$(8.38 \pm 1.02 \pm 0.12 \pm 0.26 \pm 0.81) \times 10^{-5}$	$(8.41 \pm 1.02 \pm 0.12 \pm 0.39 \pm 0.79) \times 10^{-5}$	[83]	
$B_s^0 \to D_s^{+(*)}D_s^{-(*)}$	$(3.36 \pm 0.11 \pm 0.14 \pm 0.09 \pm 0.38) \times 10^{-2}$	$(3.05 \pm 0.10 \pm 0.13 \pm 0.14 \pm 0.34) \times 10^{-2}$	[84]	
$B_s^0 \to D_s^{*\pm}D_s^\mp$	$(1.49 \pm 0.06 \pm 0.07 \pm 0.04 \pm 0.17) \times 10^{-2}$	$(1.35 \pm 0.06 \pm 0.06 \pm 0.06 \pm 0.15) \times 10^{-2}$	[84]	
$B_s^0 \to D_s^{*+}D_s^{*-}$	$(1.39 \pm 0.09 \pm 0.10 \pm 0.04 \pm 0.16) \times 10^{-2}$	$(1.27 \pm 0.08 \pm 0.09 \pm 0.06 \pm 0.14) \times 10^{-2}$	[84]	
$B_s^0 \to \bar{D}^0K_S^0$	$(4.69 \pm 0.51 \pm 0.28 \pm 0.15 \pm 0.64) \times 10^{-4}$	$(4.3 \pm 0.5 \pm 0.3 \pm 0.3 \pm 0.6) \times 10^{-4}$	[85]	
$B_s^0 \to \bar{D}^{*0}K_S^0$	$(3.05 \pm 1.13 \pm 0.40 \pm 0.10 \pm 0.41) \times 10^{-4}$	$(2.8 \pm 1.0 \pm 0.3 \pm 0.2 \pm 0.4) \times 10^{-4}$	[85]	
$B_s^0 \to \bar{D}^0\bar{K}^{*0}$	$(5.31 \pm 1.22 \pm 0.54 \pm 0.17 \pm 0.35) \times 10^{-4}$	$(4.72 \pm 1.07 \pm 0.48 \pm 0.37 \pm 0.74) \times 10^{-4}$	[86]	⋆
$B_s^0 \to \bar{D}^0K^-\pi^+$	$(1.11 \pm 0.05 \pm 0.07 \pm 0.04 \pm 0.06) \times 10^{-3}$	$(1.00 \pm 0.04 \pm 0.06 \pm 0.08 \pm 0.10) \times 10^{-3}$	[87]	⋆
$B_s^0 \to \bar{D}^0\phi$	$(3.25 \pm 0.38 \pm 0.19 \pm 0.11 \pm 0.18) \times 10^{-5}$	$(3.0 \pm 0.3 \pm 0.2 \pm 0.2 \pm 0.2) \times 10^{-5}$	[88]	⋆
$B_s^0 \to \bar{D}^{*0}\phi$	$(4.01 \pm 0.48 \pm 0.27 \pm 0.13 \pm 0.23) \times 10^{-5}$	$(3.7 \pm 0.5 \pm 0.2 \pm 0.2 \pm 0.2) \times 10^{-5}$	[88]	⋆
$B_s^0 \to \bar{D}^0K^+K^-$	$(6.13 \pm 0.59 \pm 0.28 \pm 0.20 \pm 0.56) \times 10^{-5}$	$(5.7 \pm 0.5 \pm 0.2 \pm 0.3 \pm 0.5) \times 10^{-5}$	[89]	⋆
$B_s^0 \to D_s^\mp K^\pm$	$(2.41 \pm 0.05 \pm 0.06 \pm 0.14) \times 10^{-4}$	$(2.29 \pm 0.05 \pm 0.06 \pm 0.17) \times 10^{-4}$	[90]	⋆
$B_s^0 \to D_s^-\pi^+\pi^-\pi^+$	$(6.43 \pm 1.18 \pm 0.64 \pm 0.38) \times 10^{-3}$	$(6.01 \pm 1.11 \pm 0.60 \pm 0.48) \times 10^{-3}$	[91]	⋆
$B_s^0 \to D_s^-K^+\pi^-\pi^+$	$(3.34 \pm 0.32 \pm 0.19 \pm 0.73) \times 10^{-4}$	$(3.13 \pm 0.30 \pm 0.18 \pm 0.76) \times 10^{-4}$	[92]	⋆
$B_s^0 \to D_{s1}(2536)^-\pi^+$	$(2.57 \pm 0.64 \pm 0.26 \pm 0.56) \times 10^{-5}$	$(2.41 \pm 0.60 \pm 0.24 \pm 0.58) \times 10^{-5}$	[92]	⋆

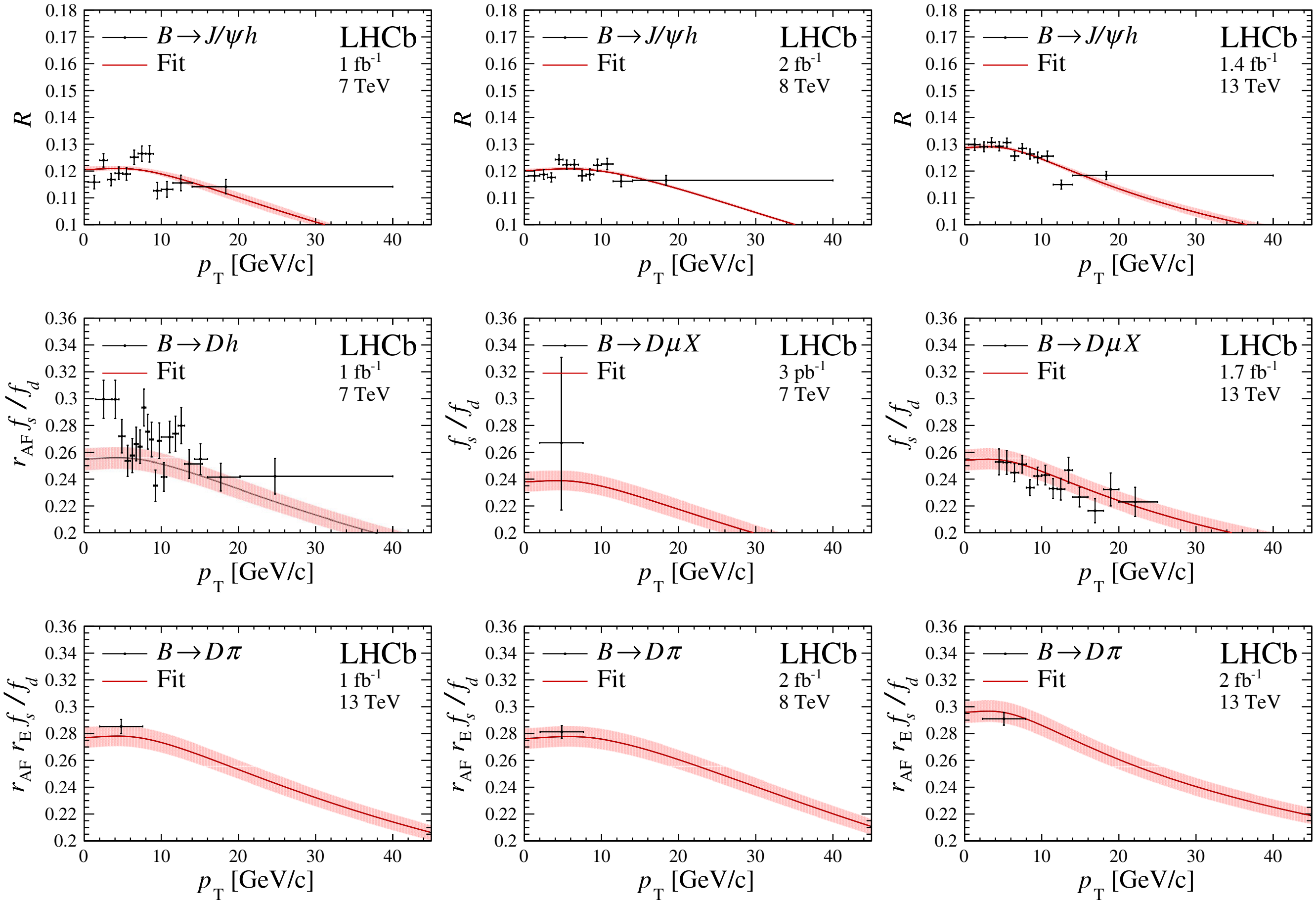

FIG. 4. Measurements of f_s/f_d sensitive observables as a function of the B-meson transverse momentum p_{T} overlaid with the fit function. A Tsallis-statistics-inspired function is used in this plot as described in the text. The scaling factors r_{AF} and r_E are defined in the text; the variable $\mathcal{R}$ is defined in Eq. (4). The vertical axes are zero suppressed. The uncertainties on the data points are fully independent of each other; overall uncertainties for measurements in multiple p_{T} intervals are propagated through scaling parameters, as described in the text. The band associated with the fit function shows the uncertainty on the postfit function for each sample.

$|V_{cb}|_{\mathrm{BGL}} = (41.7 \pm 0.8 \pm 0.9 \pm 1.1) \times 10^{-3}$, where CLN [53] and BGL [54] stand for two hadronic form-factor parametrizations. Both results are consistent with the current world average (see for example Ref. [7]).

VI. FIT TO f_s/f_d WITH A TSALLIS FUNCTION

The p_{T} distribution of produced mesons is often described through a function inspired by the Tsallis statistics [93,94]. Examples of this use can be found in Refs. [95–99]. In particular, factoring out the pseudorapidity-dependent part, this function is often written as

$$\frac{dN}{dp_{\mathrm{T}}} = C\frac{(n-1)(n-2)}{nT(nT+Mc^2(n-2))} \times p_{\mathrm{T}}\left[1+\frac{\sqrt{M^2c^4+p_T^2c^2}-Mc^2}{nT}\right]^{-n}, \tag{7}$$

where M is the mass of the meson, n and T are parameters linked to the Tsallis statistics, and C is a normalization constant. An attempt has been made to describe the data with a ratio of two such Tsallis functions. Reasonable agreement, albeit with large fit instabilities due to parametrization ambiguities, is obtained when considering the same value for the T parameter for the B_s^0 and B^0 mesons, and with the n differing by a factor of 0.9 between B_s^0 and B^0 mesons. The results of this fit tantalizingly reproduce the stabilization, or even decrease, of the f_s/f_d seen in the data at low p_{T} values and are reported in Fig. 4. The branching fractions obtained with this parametrization are in agreement with the default fit, but have larger uncertainties due to the fit instability.

VII. CONCLUSION

In conclusion, this paper presents a precise measurement of the ratio of B_s^0 and B^0 fragmentation fractions f_s/f_d as a function of pp center-of-mass energy $\sqrt{s}$ and B-meson p_{T}, from the combined analysis of LHCb measurements, significantly reducing the uncertainty with respect to the individual measurements. A significant dependence of f_s/f_d on $\sqrt{s}$ and p_{T}, described by linear functions, is observed. The integrated f_s/f_d values at the three energies, in the fiducial region of the measurements, are

$$f_s/f_d(7\ \text{TeV}) = 0.2390 \pm 0.0076,$$
$$f_s/f_d(8\ \text{TeV}) = 0.2385 \pm 0.0075,$$
$$f_s/f_d(13\ \text{TeV}) = 0.2539 \pm 0.0079,$$

and the ratio of the 13 to 8 TeV results is

$$\frac{f_s/f_d(13\ \text{TeV})}{f_s/f_d(8\ \text{TeV})} = 1.065 \pm 0.007.$$

Precise measurements of the $B_s^0 \to J/\psi\phi$ and $B_s^0 \to D_s^-\pi^+$ branching fractions,

$$\mathcal{B}(B_s^0 \to J/\psi\phi) = (1.018 \pm 0.032 \pm 0.037) \times 10^{-3},$$
$$\mathcal{B}(B_s^0 \to D_s^-\pi^+) = (3.20 \pm 0.10 \pm 0.16) \times 10^{-3},$$

are also obtained, halving their uncertainties with respect to previous world averages. Finally, previous LHCb measurements of B_s^0 branching fractions are updated, strongly reducing their normalization-related uncertainties and better constraining possible contributions from physics beyond the SM.

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