Strengthening the bound on the mass of the lightest neutrino with terrestrial and cosmological experiments

Patrick Stöcker Φ ,^{1[,*](#page-0-0)} Csaba Balázs Φ ,² Sanjay Bloor Φ ,^{3,4} Torsten Bringmann Φ ,⁵ Tomás E. Gonzalo Φ ,² Will Handley Φ , 6,7,8 Selim Hotinli Φ ,⁴ Cullan Howlett Φ , 3,⁵ Felix Kahlhoefer, ¹ Janina J. Renk Φ , 3,4,9,[‡](#page-0-2) Pat Scott^o,^{3,[4,§](#page-0-3)} Aaron C. Vincent^o,^{10,11,12} and Martin White¹³

(The GAMBIT Cosmology Workgroup)

¹Institute for Theoretical Particle Physics and Cosmology (TTK), RWTH Aachen University, D-52056 Aachen, Germany
²Sekool of Physics and Astronomy Monsch University Mel School of Physics and Astronomy, Monash University, Melbourne, Victoria 3800, Australia
³School of Mathematics and Physics. The University of Queensland 3 School of Mathematics and Physics, The University of Queensland, St. Lucia, Brisbane, Queensland 4072, Australia ⁴Department of Physics, Imperial College London, Blackett Laboratory, Prince Consort Road, London SW7 2AZ, United Kingdom ⁵Department of Physics, University of Oslo, Box 1048, Blindern, N-0316 Oslo, Norway 6 Cavendish Laboratory, University of Cambridge, JJ Thomson Avenue, Cambridge CB3 0HE, United Kingdom ⁷ Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA, United Kingdom ⁸ Gonville & Caius College, Trinity Street, Cambridge CB2 1TA, United Kingdom 9 Oskar Klein Centre for Cosmoparticle Physics, AlbaNova University Centre, $SE-10691$ Stockholm, Sweden 10 Department of Physics, Engineering Physics and Astronomy, Queen's University, Kingston Ontario K7L 3N6, Canada
¹¹Arthur B. McDonald Canadian Astroparticle Physics Research Institute, Kingston Ontario K7L 3N6, Canada
¹²Perimeter Institute for Theoretical Physics, Waterloo Ontario N2L 2Y5, Canada
¹³ARC Centre for Dark Matter Particle Physics, Department of Physics, University of Adelaide,

Adelaide, South Australia 5005, Australia

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We determine the upper limit on the mass of the lightest neutrino from the most robust recent cosmological and terrestrial data. Marginalizing over possible effective relativistic degrees of freedom at early times (N_{eff}) and assuming normal mass ordering, the mass of the lightest neutrino is less than 0.037 eV at 95% confidence; with inverted ordering, the bound is 0.042 eV. These results improve upon the strength and robustness of other recent limits and constrain the mass of the lightest neutrino to be barely larger than the largest mass splitting. We show the impacts of realistic mass models and different sources of N_{eff} .

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I. INTRODUCTION

Neutrino masses are arguably the most concrete evidence to date of physics beyond the Standard Model (SM). Measurements of their flavor oscillations at reactor $[1-5]$ $[1-5]$, accelerator [6–[11\],](#page-7-1) solar [\[12](#page-7-2)–22], and atmospheric [\[23,24\]](#page-7-3) experiments show that at least two of the three SM neutrinos must be massive. While oscillation experiments probe mass-squared differences between eigenstates, the expansion history of the Universe, growth of cosmic structure, and the cosmic microwave background (CMB) are sensitive to absolute masses, which determine when a neutrino becomes nonrelativistic; for most cosmological applications, this is expressed in terms of the sum of masses $\sum m_{\nu}$. Robust and precise inference on the mass of the lightest state can therefore only be obtained by combining the latest results of all these probes self-consistently, including associated uncertainties from each, as well as

[^{*}](#page-0-4) stoecker@physik.rwth-aachen.de

[[†]](#page-0-5) c.howlett@uq.edu.au

[[‡]](#page-0-5) janina.renk@fysik.su.se

[[§]](#page-0-6) pat.scott@uq.edu.au

constraints on other relevant parameters from, e.g., big bang nucleosynthesis (BBN) and late-time cosmological observables [\[25](#page-7-4)–31].

As no probe has yet directly measured the mass of a single neutrino, the most convenient three-flavor parametrization is in terms of the mass m_{ν_0} of the lightest neutrino and two squared mass splittings, $\Delta m_{21}^2 \equiv m_2^2 - m_1^2$ and $\Delta m_{3l}^2 \equiv m_3^2 - m_l^2$. Here, 1, 2, and 3 label the mass eigenstates with the largest component of ν_e , ν_μ , and ν_τ , respectively. Two mass orderings are presently permitted by the data: the normal ($m_1 < m_2 \ll m_3$; NH) and inverted hierarchies ($m_3 \ll m_1 < m_2$; IH). Δm_{3l}^2 refers to the splitting between the lightest and heaviest states, i.e., $l = 1$ for the NH and $l = 2$ for the IH. In terms of the splitting parameters, the physical masses are

NH:
$$
(m_1^2, m_2^2, m_3^2) = m_{\nu_0}^2 + (0, \Delta m_{21}^2, \Delta m_{3l}^2),
$$

\nIH: $(m_3^2, m_1^2, m_2^2) = m_{\nu_0}^2 + (0, |\Delta m_{3l}^2| - \Delta m_{21}^2, |\Delta m_{3l}^2|).$

In this article, we make use of the new cosmology module CosmoBit [\[32\]](#page-7-5) within the beyond-the-SM global fitting package GAMBIT [\[33\]](#page-7-6) in order to perform the most precise and robust combination to date of cosmological and experimental constraints on the mass of the lightest neutrino. We include the most recent CMB likelihoods from Planck [\[34\],](#page-7-7) recent three-flavor neutrino global fit results from NuFit [\[35\],](#page-7-8) and correlated measurements of the baryon acoustic oscillation (BAO) scale by 6dF [\[36\]](#page-7-9), SDSS-MGS [\[37\]](#page-7-10), BOSS DR12 [\[38\],](#page-7-11) eBOSS DR14 [\[39](#page-7-12)–41], and DES [\[42\].](#page-7-13) We also compute and propagate the primordial helium abundance and number of effective relativistic degrees of freedom N_{eff} through all our calculations and likelihoods self-consistently and account for the uncertainty on the lifetime of the neutron. When computing bounds on neutrino masses, we illustrate the impact of different physical assumptions about N_{eff} and show the impact of the choice of neutrino mass model on the derived value of the Hubble parameter H_0 , of particular interest given the present tension between expansion measurements at early and late times [43–[45\].](#page-8-0)

II. METHODOLOGY

Our likelihoods are based on the latest and most con-straining data implemented in CosmoBit [\[32\]](#page-7-5), NeutrinoBit [\[46\]](#page-8-1), and PrecisionBit [\[47\]](#page-8-2).

(i) Neutrino oscillations: Two-dimensional NH and IH $\Delta \chi^2$ tables for Δm_{3l}^2 and Δm_{21}^2 from NuFit 4.1 [\[35\]](#page-7-8). These come from fits to the data from solar [Homestake chlorine [\[12\],](#page-7-2) Gallex/GNO [\[13\],](#page-7-14) SAGE [\[14\]](#page-7-15), SNO [\[15\]](#page-7-16), four phases of Super-Kamiokande [\[16](#page-7-17)–19], two phases of Borexino [20–[22\]\)](#page-7-18), atmospheric (IceCube/DeepCore [\[23\]](#page-7-3), Super-Kamiokande [\[24\]](#page-7-19)), reactor (KamLAND [\[1\],](#page-7-0) Double Chooz [\[4\],](#page-7-20) Daya Bay [\[2,3\]](#page-7-21), Reno [\[5\]](#page-7-22)), and accelerator experiments (MINOS [\[6,7\]](#page-7-1), T2K [\[8,9\],](#page-7-23) NOνA [\[10,11\]](#page-7-24)]. The other oscillation parameters (mixing angles θ_{ij} and CP phase δ_{CP}) have no bearing on neutrino mass studies and do not enter our analysis. Updates contained in NuFit 5.[0\[48\]](#page-8-3) released when this article was in the final stages of preparation include only small improvements to the likelihoods for Δm_{3l}^2 and Δm_{21}^2 , so they have minimal impact on the results we show here.

- (ii) BBN: Primordial abundances of ⁴He, $Y_p = 0.245 \pm 0.245$ 0.003 [\[49\]](#page-8-4) and deuterium, $D/H = (2.527 \pm 0.030) \times$ 10^{-5} [\[50\].](#page-8-5)
- (iii) CMB: Planck 2018 baseline likelihoods consisting of high- ℓ and low- ℓ temperature and polarization data, plus CMB lensing [\[34\].](#page-7-7)
- (iv) Supernovae type Ia (SN Ia): 1048 SN Ia included in the Pantheon compilation [\[51\]](#page-8-6).
- (v) BAO scale: Measurements of the transverse comoving distance D_M and the Hubble parameter $H(z)$ from the BOSS DR12 anisotropic consensus [\[38\]](#page-7-11), D_M from DES Y1 [\[42\]](#page-7-13), and the volume-averaged distance D_V from the combined 6dF and MGS galaxy surveys [\[36,37,52\]](#page-7-9) and the eBOSS DR14 luminous red galaxy (LRG) and quasi-stellar object (QSO) samples [\[39,40\]](#page-7-12). All measurements are relative to r_s , the radius of the sound horizon at the baryon-drag epoch.

We carefully consider correlations between overlapping samples in the BAO scale measurements. The 6dF+MGS result can be considered independent of the others, as these samples do not overlap in redshift with the others. Similarly, we treat the DES results as independent of all others, as less than 10% of the DES footprint overlaps with BOSS DR12 or eBOSS DR14. The DES sample also consists of very different targets to BOSS and eBOSS and uses a different methodology (photometric rather than spectroscopic redshifts). However, the BOSS DR12 and eBOSS results are correlated: The eBOSS LRG sample actually contains some of the same galaxies as BOSS DR12, while the eBOSS QSO sample overlaps substantially with the LRGs both on the sky and in redshift. Overall, there are nonzero correlations that should be accounted for between the measurements $(D_M/r_s)^{\text{BOSS}}$, $(Hr_s)^{\text{BOSS}}$, $(D_V/r_s)^{\text{eBOSS,LRG}}$, and $(D_V/r_s)^{\text{eBOSS,QSO}}$.

To do this in a way that accounts for variation with cosmological parameters, we implement a novel method to compute the cross-correlation coefficients using Fisher matrices, following BAO forecasting techniques [\[53,54\]](#page-8-7). We sum the Fisher information that each sample contributes to the four overlapping measurements listed above, accounting for redshift and sky overlap. Inverting the full Fisher matrix then gives the correlation coefficients. We do this separately for every combination of cosmological parameters in the fit, using the number density of objects, matter power spectrum, and growth rate of structure to model the BOSS/eBOSS galaxy power spectra and their

covariance matrices as a function of the redshift. We split the models into smooth and oscillatory components to obtain the derivatives of the BAO feature in the power spectrum with respect to the distance measurements, and fix the galaxy bias and nonlinear damping of the power spectra to their best-fit values as reported in the original works. The Fisher matrix calculation then uses these all as inputs, integrating over angles and scales in the clustering measurements consistent with the range used in the original measurements.

We find a value for the cross-correlation between BOSS DR12 and the eBOSS LRGs comparable to the one reported in Ref. [\[40\]](#page-7-25). The benefits of our technique are that it includes information from all scales included in the measurement and does so self-consistently for each combination of cosmological parameters. More details on the calculation and the computed correlation coefficients can be found in the Appendix [A.](#page-5-0)

We compute the BAO scale and SN Ia likelihoods via an interface to MontePYTHON 3.3.0 [\[55,56\];](#page-8-8) our novel BAO scale correlation treatment will appear in a future release. For computing observable predictions, we use routines in CosmoBit and associated interfaces to AlterBBN 2.2 ([\[57,58\]](#page-8-9); for BBN yields) and CLASS 2.9.3 ([\[59\]](#page-8-10); for solving the background cosmology and Boltzmann equations).

We perform separate fits of the NH and IH, varying m_{ν_0} , Δm_{21}^2 , and Δm_{3l}^2 , the six free parameters of the standard Lambda cold dark matter cosmology ((Λ)CDM; see [\[32\]](#page-7-5) for detailed definitions), and $\Delta N_{\text{eff}} \equiv N_{\text{eff}} - N_{\text{SM}}$ with $N_{SM} = 3.045$ [\[60](#page-8-11)–62] (Table [I](#page-2-0)). For our main analysis,

TABLE I. Parameters and ranges varied in the main analysis of this article. All parameters are sampled with linear priors. For the nuisance parameters associated with the Planck likelihood, we adopt the same prior ranges as done for the Planck baseline analysis [\[34\]](#page-7-7) and apply the recommended Gaussian priors as additional likelihood contributions.

Sector	Parameter	Range
ν masses		$[0, 1.1]$ eV
(NH) (IH)	Δm_2^2 Δm_{31}^2 Δm_{3I}^2	$[6, 9] \times 10^{-5}$ eV ² $[2.2, 2.8] \times 10^{-3}$ eV ² $[-2.8, -2.2] \times 10^{-3}$ eV ²
ACDM	H_0 $\Omega_{\rm b}h^2$ $\Omega_{\rm cdm}h^2$ $\tau_{\rm reionization}$ $\ln{(10^{10}A_s)}$ $n_{\rm s}$	[50, 80] $\rm km\,s^{-1}\,Mpc^{-1}$ [0.020, 0.024] [0.10, 0.15] [0.004, 0.20] [2.5, 3.5] [0.90, 1.10]
N_{eff}	r_{ν}	[0.75, 1.15]
Nuisance	SN Ia abs. magnitude M Neutron lifetime τ_n <i>Planck</i> likelihood	$[-20, -18]$ [876, 883] s 21 parameters varied

we conservatively adopt a linear prior on m_{ν_0} between 0 and 1.1 eV. In Appendix [B](#page-6-0), we show how the limit on m_{ν_0} strengthens if we change to a logarithmic prior above $m_{\nu_0} = 0.0003$ eV. We adopt linear priors on the ΛCDM parameters, as these are sufficiently well constrained by data that their priors are inconsequential.

We assume that N_{eff} has the same value during BBN and recombination, varying ΔN_{eff} by scanning linearly over the effective neutrino temperature ratio $r_{\nu,eff} \equiv T_{\nu}/T_{\nu,SM} =$ $(\Delta N_{\text{eff}}/N_{\text{SM}} + 1)^{\frac{1}{4}}$. This approach enables us to explore the full range of the number of effective relativistic degrees of freedom in the early Universe, corresponding to both positive and negative values of ΔN_{eff} . We later explore the impact of restricting our analysis to $\Delta N_{\text{eff}} \geq 0$, in which case, ΔN_{eff} can be interpreted as the contribution of additional ultrarelativistic (radiation) species and to the pure SM case ($\Delta N_{\text{eff}} = 0$).

Finally, we vary a total of 23 nuisance parameters representing uncertainties in the SN Ia absolute magnitude, the Planck analysis, and the neutron lifetime. These nuisance parameters are constrained, respectively, with the MontePYTHON likelihood for the magnitude of Pantheon supernovae, a likelihood implementation of the Planck nuisance priors [\[34\],](#page-7-7) and the combination of all "bottle" measurements of the lifetime of the neutron $\tau_{n,\text{bottle}} = 879.4 \pm 0.6 \text{ s}$ [\[63\]](#page-8-12). We employ the nested sampler PolyChord 1.17.1 [\[64\]](#page-8-13) in fast-slow mode via ScannerBit [\[65\]](#page-8-14) in order to oversample Planck and SN Ia nuisances. Our fits use 500 live points, 5000 initial samples from the prior, a stopping tolerance of 0.01, $n_{\text{repeats}} = 2n_{\text{slow}} = 22$, a 1:3 fast-slow timing split (leading to approximately 340 likelihood evaluations with different nuisance parameters per combination of the remaining parameters), and default values for all other settings.

III. RESULTS

Assuming Λ CDM cosmology plus a free N_{eff} and normal mass ordering, we find a global 95% confidence upper bound on the lightest neutrino mass of m_{ν_0} < 0.037 eV; for inverted ordering, this increases slightly to m_{ν_0} < 0.042 eV. In terms of the sum of neutrino masses, this corresponds to $0.058 < \sum m_{\nu}/eV < 0.139$ (NH) and $0.098 < \sum m_{\nu}/eV < 0.174$ (IH).

The lower-left triangle of Fig. [1](#page-3-0) compares the one- and two-dimensional marginalized posterior distributions for the normal and inverted hierarchies. Here we show both the lightest neutrino mass and the sum of neutrino masses, as well as their correlations with N_{eff} and H_0 . We also show the result for the canonical scenario considered in most previous analyses, such as those by both Planck [\[28\]](#page-7-26) and eBOSS [\[66\],](#page-8-15) where a single parameter specifies a common degenerate mass for all three neutrinos. In all cases, the maximum posterior probability density is achieved for a massless lightest neutrino, reflecting the fact that there

FIG. 1. 1D and joint 2D posteriors (bottom left) and profile likelihoods (upper right) on the lightest neutrino mass, the sum of neutrino masses, the number of effective neutrino species at the time of CMB formation, and the Hubble parameter, based on the most robust and complete combination to date of CMB, BAO scale, SN Ia, BBN, and neutrino oscillation data. Posteriors are shown for normal and inverted neutrino hierarchies and are compared with the often-seen (but unphysical) scenario of three degenerate-mass neutrinos. Profile likelihoods are for the normal hierarchy only and assume the best-fit values from the corresponding posterior scan for the 21 *Planck* nuisance parameters. Shading indicates 68% and 95% credible/confidence regions.

remains no positive cosmological hint for neutrino mass to date. The degenerate-mass assumption would lead one to erroneously infer that $\sum m_{\nu}/eV < 0.115$ at 95% confidence. This result is plainly biased toward lower values due to the fact that the majority of the probability distribution lies within the unphysical region excluded by neutrino oscillation experiments. Using a physically realistic mass model shifts the 95% interval for H_0 from 67.7 ± 1.7 km s⁻¹ Mpc⁻¹ to 67.5 ± 1.8 km s⁻¹ Mpc⁻¹ (NH) or 67.4 ± 1.7 km s⁻¹ Mpc⁻¹ (IH), and the 95% interval for N_{eff} from 3.04 ± 0.24 to 3.06 ± 0.24 (NH) or 3.08 ± 0.24 (IH).

For comparison, in the upper-right triangle of Fig. [1](#page-3-0), we also show prior-independent profile likelihoods for the NH obtained from the differential evolution sampler DIVER [\[65\]](#page-8-14) with a population of $10⁴$, a convergence threshold of 10[−]⁴, and the Planck nuisance parameters fixed to their best-fit values from the NH PolyChord fit (as DIVER has no fast-slow feature). The results match the posteriors reasonably closely, but give slightly stronger implied constraints at 95% confidence: $m_{\nu_0} < 0.033$ eV and

FIG. 2. Comparison of posterior probabilities for the mass of the lightest neutrino under three different assumptions: $\Delta N_{\text{eff}} = 0$, $\Delta N_{\text{eff}} \geq 0$ corresponding to dark radiation, or ΔN_{eff} free to take on positive or negative values, corresponding to a modified effective neutrino temperature.

 $0.058 < \sum m_{\nu}/eV < 0.127$.¹ These findings confirm the robustness of our main (Bayesian) results. We have also calculated Bayesian evidences and find that the IH is disfavored relative to the NH with Bayes factors between $\log B = 5.6$ and $\log B = 7.0$ (depending on the treatment of N_{eff}), a result driven mostly by the neutrino oscillation likelihoods [\[67\]](#page-8-16).

In Fig. [2,](#page-3-1) we examine the impacts of different physical sources of N_{eff} : (a) changes in the neutrino temperature, where ΔN_{eff} is allowed to be positive or negative, as in our benchmark analyses, (b) dark radiation, where $\Delta N_{\text{eff}} \geq 0$, and (c) the pure SM case, where $\Delta N_{\text{eff}} = 0$. The resulting posteriors only change very slightly, corresponding to shifts of the order of 0.002–0.003 eV in the 95% limit on m_{ν_0} . Our final results can therefore be considered rather robust to assumptions about ΔN_{eff} . Figure [2](#page-3-1) suggests that at the 68% confidence level, allowing positive ΔN_{eff} may weaken the limits slightly compared to $\Delta N_{\text{eff}} = 0$, with the effect offset to some extent by also allowing $\Delta N_{\text{eff}} < 0$. Any such effect is however small enough that it is difficult to distinguish from sampling noise. Notably, bounds on m_{ν_0} and $\sum m_{\nu}$ can be weakened substantially in cosmologies featuring both dark radiation and a modified neutrino temperature [\[32\],](#page-7-5) neutrino self-interactions, or exotic dark energy, even to the level where a direct measurement of the neutrino mass may be within reach of the KATRIN experiment [\[68\]](#page-8-17).

¹The slightly higher profile likelihood than posterior for much of the allowed range of $\sum m_{\nu}$ should be understood in the context of frequentist confidence levels deriving from isolikelihood contours, rather than integrated posterior probabilities as in the case of Bayesian credible regions.

IV. DISCUSSION

Our analysis provides a more precise and robust limit on the sum of neutrino masses than either those of Planck [\[28\]](#page-7-26) or eBOSS [\[66\]](#page-8-15), mainly due to our use of physical neutrino mass models rather than the assumption of degenerate masses. Comparing results for the unphysical degeneratemass model however provides an indication of the constraining power of the cosmological data used in each case. Our limit $(\sum m_{\nu}/eV < 0.115)$ is very close to the most similar combination in Ref. [\[28\]](#page-7-26) $(\sum m_{\nu}/eV < 0.12)$, Planck TT, TE, $EE + lowE + lensing + BAO$, with varying N_{eff}), indicating that within $\Lambda \text{CDM} + N_{\text{eff}}$ the eBOSS DR14 and DES BAO and Pantheon SN Ia measurements only add limited additional information.

The most similar eBOSS limit ($\sum m_{\nu}/eV < 0.099$) is stronger. Reference [\[66\]](#page-8-15) includes slightly more up-to-date eBOSS BAO scale measurements compared to our analysis, but the improved sensitivity is mainly driven by their inclusion of redshift-space distortions (RSDs). We do not include RSD measurements, as to date they have been based on templates for the matter power spectrum that assume a particular neutrino mass, and the fits then neglect the scale dependence in the growth rate of structure. As such, we believe they cannot robustly be used to constrain neutrino masses. Reference [\[66\]](#page-8-15) also includes new (DR16) Ly α constraints on the BAO scale. We checked that including DR14 Ly α measurements has no impact on our limit. Given this result, the fact that the redshifts probed by $Ly\alpha$ data are intermediate between those of the CMB and other BAO measurements, that $Ly\alpha$ BAO are slightly discrepant with other BAO, and that the $Ly\alpha$ BAO results require more precise control over observational and astrophysical systematics than galaxy BAO [\[41\]](#page-7-27), we argue that excluding the DR14 Ly α result gives a more robust limit on neutrino masses at no decrease in the statistical constraining power.

The limits that we present here on the mass of the lightest neutrino are almost 60% stronger than those derived from a combined fit to both mass hierarchies in a recent similar analysis (m_{ν_0} < 0.086 eV [\[29\]](#page-7-28)), and 14% stronger than those appearing in a similar contemporaneous analysis [\[67\]](#page-8-16). At the limiting value of m_{ν_0} , this brings the absolute scale of neutrino masses down to a level comparable to the larger of the two mass splittings $(m_3 - m_1 = 0.025 \text{ eV} \text{ in}$ the NH, $m_2 - m_3 = 0.023$ eV in the IH). We use the same BBN and SN Ia data as Ref. [\[29\]](#page-7-28) but improved neutrino and CMB data: results from NuFit 4.1 rather than 2.1 for neutrino experiments (leading to roughly 20% stronger bounds), and a CMB likelihood based on 2018 rather than 2015 Planck data (leading to roughly 30% stronger bounds). Compared to [\[67\],](#page-8-16) we add BBN constraints, DES, and eBOSS BAO scale data and marginalize over N_{eff} . We also propagate the primordial helium abundance fully and incorporate the uncertainty on the lifetime of the neutron (see also discussion in Ref. [\[32\]\)](#page-7-5). From galaxy surveys, we and Ref. [\[67\]](#page-8-16) rely exclusively on scale measurements, as a correct statistical combination of scale data can provide a strong limit on neutrino masses that is also very robust. Reference [\[29\]](#page-7-28) instead used an angular clustering reanalysis of the BOSS DR12 data. Their approach used the full shape of the clustering more self-consistently than template-based RSD measurements but still required several uncertainties such as the galaxy bias, redshift error dispersions, and spectroscopic redshift errors to be modeled, and data cuts to be made, adding 28 more nuisance parameters. In principle, nonlinear scales should provide the most constraining power on neutrino mass parameters but difficulty in the modeling limits the accessibility of this information [\[69\]](#page-8-18). With current analysis techniques, BAO scale measurements still add more constraining power for neutrino masses than data encoding the full shape of the galaxy power spectrum—although this is not expected to remain true for much longer [\[30\]](#page-7-29).

V. SUMMARY

We have presented a comprehensive combined analysis of recent neutrino oscillation, CMB, SN Ia, BBN, and BAO scale data deriving the most accurate and precise limits to date on the mass of the lightest neutrino and the sum of neutrino masses. Assuming normal mass ordering and standard cosmology plus $\Delta N_{\text{eff}} \neq 0$, we have found m_{ν_0} < 0.037 eV and $0.058 < \sum m_{\nu}/eV < 0.139$. With inverted ordering, $m_{\nu_0} < 0.042$ eV and $0.098 < \sum m_{\nu}/eV < 0.174$. These results should serve as a benchmark in the coming years, as neutrino cosmology continues its inexorable progress toward a measurement of the absolute neutrino mass scale.

All input files and parameter samples produced for this article can be found on Zenodo [\[70\].](#page-8-19)

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APPENDIX A: DETAILS OF BAO SCALE CORRELATION COEFFICIENTS

Here we provide more detail on our novel method to account for the correlations between overlapping BAO experiments in a cosmology-dependent way. We acknowledge that the use of cosmology-dependent Gaussian covariance matrices can lead to an overestimation of the Fisher information [\[74\];](#page-8-23) however, in our method we are only computing the cross-correlation coefficients, which are then scaled by the original measurement errors. We do not modify these original errors and so are not underestimating the uncertainty. More so, we argue that including cosmology dependence in the correlation coefficients is the correct thing to do, as the overlap between BAO measurements is mainly related to the (effective) cosmological volume shared by the experiments, which is clearly a function of the cosmological model.

We begin by expressing the joint covariance matrix of BAO measurements from the overlapping BOSS DR12 and eBOSS results C in terms of the inverse of the Fisher matrix F,

$$
\mathbf{F}^{-1} = \mathbf{C} = \mathbf{E} \begin{pmatrix} 1 & \rho_{D_M/r_s, Hr_s}^{\text{BOSS}} & c_0 & 0 \\ \rho_{D_M/r_s, Hr_s}^{\text{BOSS}} & 1 & c_1 & 0 \\ c_0 & c_1 & 1 & c_2 \\ 0 & 0 & c_2 & 1 \end{pmatrix} \mathbf{E}.
$$
 (A1)

Here, c_0 is the correlation coefficient between measurements $(D_M/r_s)^{\text{BOSS}}$ and $(D_V/r_s)^{\text{eBOSS,LRG}}$, c_1 is the correlation between $(Hr_s)^{\text{BOSS}}$ and $(D_V/r_s)^{\text{eBOSS, LRG}}$ and c_2 is the correlation between $(D_V/r_s)^{6}$ BOSS,LRG and $(D_V/r_s)^{\text{eBOSS,QSO}}$. The cross-correlation $\rho_{D_M/r_s, Hr_s}^{BOSS}$ between the BOSS DR12 measurements of D_M/r_s and Hr_s is provided as part of the BOSS DR12 results in MontePYTHON and is not replaced in this analysis or made dependent upon cosmological parameters. The matrix $\mathbf{E} = \text{diag}(\sigma_{D_M/r_s}^{\text{BOSS}}, \sigma_{Hr_s}^{\text{BOSS}}, \sigma_{D_V/r_s}^{\text{eBOSS, QSO}} , \sigma_{D_V/r_s}^{\text{eBOSS, QSO}})$ contains the experimental uncertainties from the BAO measurements, which are also included in MontePYTHON. Hence, the only unknowns are c_i , which we calculate for each set of cosmological parameters by inverting the full Fisher matrix. In practice, we compute the Fisher matrix for the BAO scale parameters

$$
\alpha = \frac{D_V r_s^{\text{fid}}}{D_V^{\text{fid}} r_s}, \quad \alpha_\perp = \frac{D_M r_s^{\text{fid}}}{D_M^{\text{fid}} r_s}, \quad \alpha_{||} = \frac{H^{\text{fid}} r_s^{\text{fid}}}{H r_s}, \quad \text{(A2)}
$$

where "fid" corresponds to the fiducial cosmology used to make the original clustering measurements. It is trivial to convert the correlation coefficients to those for the distance scales that we actually fit in MontePYTHON.

We do this based on [\[75\],](#page-8-24) writing the Fisher matrix elements for each parameter of interest as a sum over the information from the different redshift bins and overlapping/nonoverlapping sky areas for each survey. For example, consider the redshift range $0.60 < z < 0.75$. For each redshift bin in this range, we have information contributing to three parameters: $\alpha_{\perp}^{\rm BOSS}$, $\alpha_{\parallel}^{\rm BOSS}$, and $\alpha^{\rm eBOSS, LRG}$. We first compute the 2 × 2 Fisher "submatrix" for $\alpha_{\perp}^{\text{BOSS}}$, $\alpha_{\parallel}^{\text{BOSS}}$ from the nonoverlapping sky area $\Omega^{BOSS} - \Omega^{eBOSS,LRG}$ and add this to the full matrix, then add on the 3×3 Fisher submatrix for all three parameters from the sky area $Ω$ ^{eBOSS,LRG}.

The Fisher matrix element for parameters λ_i and λ_j measured from survey A within a redshift bin is [\[76\]](#page-8-25)

$$
F_{ij}^A = \int_0^{k_{\text{max}}} k^2 dk \int_0^1 d\mu \frac{\partial P_g^A(k,\mu)}{\partial \lambda_i} C_{P_g^A}^{-1}(k,\mu) \frac{\partial P_g^A(k,\mu)}{\partial \lambda_j},
$$
\n(A3)

where we fix $k_{\text{max}} = 0.3h \,\text{Mpc}^{-1}$. $C_{P_g^A}(k,\mu)$ is the covariance matrix of the galaxy power spectrum $P_g^A(k,\mu)$,

$$
C_{P_g^A}(k,\mu) = \frac{4\pi^2}{V^A} \left[P_g^A(k,\mu) + \frac{V^A}{N^A} \right]^2, \tag{A4}
$$

where N^A is the number of galaxies in the redshift bin, and V^A is the cosmological volume contained within the redshift bin and sky area Ω^A . The first term in the covariance matrix models cosmic variance; the second is shot noise from the finite number of galaxies. We model the galaxy power spectrum as a function of the matter power spectrum $P_m(k)$ and potentially scale-dependent growth rate of structure $f(k)$, splitting it into two components using the smoothed matter power spectrum $P_{sm}(k)$,

$$
P_g^A(k,\mu) = (b^A + f(k)\mu^2)^2 P_{sm}(k)
$$

$$
\times \left[1 + \left(\frac{P_m(k)}{P_{sm}(k)} - 1\right) e^{-\frac{1}{2}k^2[\mu^2 \Sigma_{nl,||}^A + (1-\mu^2)\Sigma_{nl,\perp}^A]}\right].
$$
 (A5)

Here b^A represents the linear galaxy bias for the survey, and $\Sigma_{nl,||}^A$ and $\Sigma_{nl,\perp}^A$ account for nonlinear damping of the BAO feature. The values for these are fixed to the best-fit values from the BOSS and eBOSS analyses. We compute $P_{sm}(k)$ using the method of Ref. [\[77\]](#page-8-26).

The split into smooth and nonsmooth components of the matter power spectrum ensures that we are only including information from the BAO scale and not the broadband shape of the power spectrum or redshift-space

FIG. 3. 1D and joint 2D posteriors for the correlation coefficients c_0 $[(D_M/r_s)^{BOSS}$ and $(D_V/r_s)^{eBOSS,LRG}$, c_1 $[(Hr_s)^{BOSS}]$ and $(D_V/r_s)^{\text{eBOSS,LRG}}$], and c_2 $[(D_V/r_s)^{\text{eBOSS,LRG}}]$ and $(D_V/r_s)^{\text{eBOSS, QSO}}$]. Also shown are the variations of the correlation coefficients with neutrino mass parameters N_{eff} and the Hubble parameter H_0 .

distortions. As such, the derivatives with respect to $\lambda_{i,j}$ in Eq. [\(A3\)](#page-5-1) are computed only on the $P_m(k)/P_{sm}(k)$ component of $P_g^A(k,\mu)$. We do this by finite differencing $P_m(k')/P_{sm}(k')$ evaluated at $k'=k/\alpha$ or

$$
k' = \frac{k}{\alpha_{\perp}} \left[1 + \mu^2 \left(\frac{\alpha_{\perp}^2}{\alpha_{\parallel}^2} - 1 \right) \right]^{1/2} . \tag{A6}
$$

Overall, the calculation of the Fisher matrix for a particular redshift bin and survey matches that commonly used in the literature [\[53,54\]](#page-8-7), and our model power spectrum is representative of how BAO constraints are actually extracted from the data [\[38,39\].](#page-7-11)

In Fig. [3](#page-6-1), we show the distribution of the correlation coefficients in our BAO scale joint likelihood from our main NH fit. The variation of the correlation coefficients with cosmological parameters is small but perceptible, with c_1 and c_2 both increasing along with H_0 and N_{eff} , and c_0 decreasing with larger H_0 and N_{eff} . The trends are weaker but in the opposite direction for the neutrino mass parameters. In general c_1 and c_2 are strongly correlated with each other and anticorrelated with c_0 . Our method can be easily extended to include other datasets, and we expect larger variation in the values of the coefficients for models including nonzero curvature or non-cosmological-constant models of dark energy.

APPENDIX B: IMPACTS OF PRIORS ON THE MASS OF THE LIGHTEST NEUTRINO

In the main body of this article, we presented only results based on a linear prior for the lightest neutrino mass m_{ν_0} . This is a conservative choice, as it is an essentially uninformative prior (but see Ref. [\[78\]](#page-8-27) for an objective Bayesian construction of the most uninformative prior for

FIG. 4. 1D and joint 2D posteriors on the neutrino mass and relevant cosmological parameters, assuming normal ordering. Here we reproduce the results from Fig. [1](#page-3-0) based on a linear prior for the mass of the lightest neutrino and compare them to the results when employing a hybrid prior, linear below $m_{\nu_0} = 0.0003$ eV and logarithmic above.

this problem). Although more informative, a logarithmic prior is arguably more physically justified: Given that we have no information suggesting any preferred scale for m_{ν_0} (or, in fact, any preference for $m_{\nu_0} > 0$ at all), one might argue that any scale for the mass is as likely as another. In Fig. [4](#page-6-2) we compare our result for the NH with the result if we instead adopt a logarithmic prior for m_{ν_0} above 0.0003 eV (and retain the linear prior below this value, enforcing continuity of the prior across the transition).

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Masses below 0.0003 eV are indistinguishable from the massless case in the outputs of CLASS, so there is little point in oversampling this region. As can be seen from Fig. [4](#page-6-2), this hybrid linear-logarithmic prior indeed results in a much stronger preference for very small neutrino masses, giving $m_{\nu_0} < 0.020$ eV and $0.058 < \sum m_{\nu}/eV < 0.100$ at 95% confidence. The effect is similar in the IH, producing m_{ν_0} < 0.024 eV and 0.098 < $\sum m_{\nu}/eV$ < 0.136 at 95% confidence.

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