

Current bounds and future prospects of light neutralino dark matter in the NMSSM

Rahool Kumar Barman^{*}

*Indian Association for the cultivation of Science, Jadavpur, Kolkata 700032, India
and Centre for High Energy Physics, Indian Institute of Science, Bangalore 560012, India*

Genevieve Bélanger[†]

LAPTh, Université Savoie Mont Blanc, CNRS, B.P. 110, F-74941 Annecy Cedex, France

Biplob Bhattacharjee[‡] and Rohini Godbole[§]

Centre for High Energy Physics, Indian Institute of Science, Bangalore 560012, India

Dipan Sengupta^{||}

*Department of Physics and Astronomy, University of California, San Diego, 9500 Gilman Drive,
La Jolla, California 92037, USA*

Xerxes Tata[¶]

Department of Physics and Astronomy, University of Hawaii, Honolulu, Hawaii 96822, USA



(Received 22 July 2020; accepted 23 December 2020; published 26 January 2021)

Unlike its minimal counterpart, the next to minimal supersymmetric Standard Model (NMSSM) allows the possibility that the lightest neutralino could have a mass as small as ~ 1 GeV while still providing a significant component of relic dark matter (DM). Such a neutralino can provide an invisible decay mode to the Higgs as well. Further, the observed SM-like Higgs boson (H_{125}) could also have an invisible branching fraction as high as $\sim 19\%$. Led by these facts, we first delineate the region of parameter space of the NMSSM with a light neutralino ($M_{\tilde{\chi}_1^0} < 62.5$ GeV) that yields a thermal neutralino relic density smaller than the measured relic density of cold dark matter, and is also compatible with constraints from collider searches, searches for dark matter, and from flavor physics. We then examine the prospects for probing the NMSSM with a light neutralino via direct DM detection searches, via invisible Higgs boson width experiments at future e^+e^- colliders, via searches for a light singlet Higgs boson in $2b2\mu$, $2b2\tau$ and $2\mu2\tau$ channels and via pair production of winos or doublet Higgsinos at the high luminosity LHC and its proposed energy upgrade. For this last-mentioned electroweakino search, we perform a detailed analysis to map out the projected reach in the $3l + \cancel{E}_T$ channel, assuming that chargino decays to $W\tilde{\chi}_1^0$ and the neutralino(s) decay to Z or $H_{125} + \tilde{\chi}_1^0$. We find that the HL-LHC can discover SUSY in just part of the parameter space in each of these channels, which together can probe almost the entire parameter space. The HE-LHC probes essentially the entire region with Higgsinos (winos) lighter than 1 TeV (2 TeV) independently of how the neutralinos decay, and leads to significantly larger signal rates.

DOI: [10.1103/PhysRevD.103.015029](https://doi.org/10.1103/PhysRevD.103.015029)

I. INTRODUCTION

The LHC Run-II has ushered in a new era in terms of energy, luminosity and discovery potential. At the end of the Run-II with about 140 fb^{-1} of data collected at 13 TeV, the status of the Higgs as the last frontier to be conquered as concerns the Standard Model has been firmly established [1]. As yet, there is no unambiguous evidence for any physics beyond the Standard Model (BSM). In case of the primary candidate for BSM physics *viz.* TeV scale supersymmetry (SUSY), large swaths of parameter space have been ruled out. However the LHC 13 TeV still holds

^{*}rahoolbarman@iisc.ac.in

[†]belanger@lapth.cnrs.fr

[‡]biplob@iisc.ac.in

[§]rohini@iisc.ac.in

^{||}disengupta@physics.ucsd.edu

[¶]tata@phys.hawaii.edu

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP³.

promise of further exploring the BSM landscape including SUSY. In particular, the electroweak sector of SUSY is still largely unconstrained. A better coverage of this sector is expected with larger integrated luminosities, as production of electroweakinos not only suffers from weak production cross sections but limits from the current searches can also be evaded as an intricate combination of parameters can lead to compressed spectra, see for example [2–16]. Compressed Higgsinos are expected in models of natural SUSY [17,18]. Experiments at the LHC have also begun to probe such scenarios [19–21]. Moreover, the electroweak sector contains one of the most promising dark matter (DM) candidate, the lightest neutralino. It is imperative that we continue to probe the complementarity between LHC searches for SUSY and astrophysical observations as far as supersymmetric dark matter is concerned [22,23]. A study of complementarity between future direct detection experiments and future collider searches for the case of a light neutralino DM ($M_{\tilde{\chi}_1^0} \leq 62.5$ GeV), both thermal and nonthermal, in the MSSM framework was carried out in [24]. Results in [24] indicated that the MSSM parameter space with a light neutralino DM and with a correct or underabundant relic density could be entirely probed via the future dark matter experiments.

This then naturally motivates us to examine the extent to which the considerations of [24] would be altered in the simplest extension of the MSSM, the next-to-minimal supersymmetric Standard Model (NMSSM) [25,26]. As in [24] we focus on $M_{\tilde{\chi}_1^0} \leq 62.5$ GeV, that can potentially contribute to invisible decays of the Higgs boson discovered at CERN [27–30], hereafter referred to as H_{125} . In the MSSM with heavy sfermions, the current limit for light neutralinos after taking into account various cosmological, astrophysics and collider constraints lies around 30 GeV [24,31–37]. This arises mainly from a combination of the direct detection constraint which requires a weak coupling of the DM to the Higgs and of the relic density constraint which requires that the neutralino annihilates efficiently through a mediator that is nearly on-shell. Within the NMSSM, much lighter neutralinos, as light as 1 GeV, can satisfy all current constraints [38–45]. This is because additional scalars present in the NMSSM may provide an efficient annihilation mechanism for light neutralinos in the early universe [46–48]. Moreover, the singlet component of these new scalars entails that they can evade detection at the LHC even if their masses are below that of the standard model-like Higgs [49–56]. In this article, assuming a standard cosmological scenario, we perform a comprehensive exploration of the light neutralino as a thermal cold dark matter candidate in the NMSSM by imposing current low energy, collider and astrophysical constraints. These include flavor physics constraints, LEP bounds, recent results from LHC measurements of the Higgs sector including searches for light

Higgses [51,57–59] and measurements of the Higgs signal strengths, direct chargino/neutralino searches at the LHC [60–62] as well as limits from direct detection experiments in spin-independent neutralino-nucleon scattering (Xenon-1T [63]) and from indirect detection of DM in the photon channel (Fermi-LAT [64]). We concentrate on the electroweakino sector and assume that squarks and sleptons are heavy and do not play an important role in DM or collider observables. After having established the region in parameter space compatible with current experimental results, we assess the impact of future searches. We reemphasize that for the (thermally produced) neutralino LSP (lightest SUSY particle) to not produce too much dark matter in the early universe, we require a light spin-zero particle close to twice the LSP mass. Correspondingly, we choose parameter space points which also feature M_{A_1} and M_{H_1} below 122 GeV. We focus on three specific directions that we find more promising for discovery:

- (1) multiton direct detection experiments,
- (2) the measurement of the invisible decay width of the Higgs at the LHC or a future collider like FCC, CEPC and ILC,
- (3) direct searches for light Higgses and electroweakinos at the LHC and its future upgrades *viz* the proposed high luminosity LHC (HL-LHC: $\sqrt{s} = 14$ TeV, 3000 fb^{-1}) and the high energy LHC (HE-LHC: $\sqrt{s} = 27$ TeV, 15 ab^{-1}).

Specifically, we assess the reach of direct electroweakino searches in the WZ mediated and WH_{125} mediated $3l + \cancel{E}_T$ search channel, at HL-LHC as well as HE-LHC. The impact of the projected search limits from direct light Higgs searches in the $2b2\tau$, $2b2\mu$, $2\mu2\tau$ and 4μ channels at the future upgrades of LHC are also examined [65]. Finally we emphasize the complementarity of future measurements of an invisible branching ratio for the Higgs, searches for Higgs and electroweakino at colliders, and direct and indirect detection experiments for discovering or probing the light neutralino in the NMSSM.

The rest of the paper is organized as follows. In Sec. II, we present the NMSSM framework and discuss the parameter space of interest in Sec. III. The relevant constraints and their implications are described in Sec. IV. The characteristic features of the allowed parameter space region obtained after imposing the current constraints are discussed in Sec. V. In Sec. VI, we investigate the future reach of Xenon-nT (through spin-independent WIMP-nucleon interactions), the future prospects for ILC and CEPC (through Higgs invisible width measurements) and the scope of direct light Higgs searches at future runs of LHC, and study their implications on the allowed parameter space. In Sec. VII, we explore the reach via searches for direct production of electroweakinos in the $3l + \cancel{E}_T$ final state at the HL-LHC and the HE-LHC. We conclude in Sec. VIII.

II. THE NMSSM FRAMEWORK

The NMSSM Higgs sector consists of two doublet Higgs superfields, \hat{H}_u and \hat{H}_d , and a Higgs singlet superfield \hat{S} . The scale invariant NMSSM superpotential has the form [66]

$$W = W_{\text{MSSM}}(\mu = 0) + \lambda \hat{S} \hat{H}_u \cdot \hat{H}_d + \frac{\kappa}{3} \hat{S}^3 \quad (1)$$

where $W_{\text{MSSM}}(\mu = 0)$ refers to the MSSM superpotential without the μ -term, while λ and κ are dimensionless parameters, and $\hat{H}_u \cdot \hat{H}_d = \hat{H}_u^+ \hat{H}_d^- - \hat{H}_u^0 \hat{H}_d^0$. The soft SUSY breaking terms which contain the Higgs scalar fields are

$$-V_{\text{soft}} = m_{H_d}^2 H_d^\dagger H_d + m_{H_u}^2 H_u^\dagger H_u + m_S^2 S^\dagger S + \left\{ \lambda A_\lambda H_u \cdot H_d S + \frac{1}{3} \kappa A_\kappa S^3 + \text{H.c.} \right\} \quad (2)$$

where A_κ and A_λ are the trilinear soft-breaking parameters, while m_{H_d} , m_{H_u} and m_S are the soft breaking Higgs masses. An effective μ -term with $\mu = \lambda v_s$ is generated when S develops a vacuum expectation value. The F- and D-terms also contribute to the Higgs scalar potential, and are given by

$$V_F = |\lambda H_u \cdot H_d + \kappa S^2|^2 + \lambda^2 S^\dagger S (H_u^\dagger H_u + H_d^\dagger H_d) \quad (3)$$

$$V_D = \frac{g_1^2 + g_2^2}{8} (H_u^\dagger H_u - H_d^\dagger H_d)^2 + \frac{g_2^2}{2} |H_d^\dagger H_u|^2 \quad (4)$$

where, g_1 and g_2 are the $U(1)_Y$ and $SU(2)_L$ gauge couplings of the SM. Expanding the scalar potential, $V_{\text{soft}} + V_F + V_D$, around the real neutral vacuum expectation values (*vevs*), v_u , v_d and v_s of H_u , H_d and S , respectively, gives the physical Higgs states. Following the notation of [67],

$$H_u^0 = \frac{v_u + H_u^R + iH_u^I}{\sqrt{2}}, \quad H_d^0 = \frac{v_d + H_d^R + iH_d^I}{\sqrt{2}},$$

$$S = \frac{s + H^S + iA^S}{\sqrt{2}} \quad (5)$$

where, H_u^R , H_d^R , H^S , are the real components while H_u^I , H_d^I , A^S are the imaginary components. Three scalar neutral Higgs bosons are obtained from H_u^R , H_d^R and H^S , while a pseudo-scalar Higgs boson is obtained from the combination of H_u^I and H_d^I , and a second pseudoscalar Higgs is obtained from A^S . At tree-level, the symmetric squared mass matrix (M_s^2) of the neutral scalar Higgs bosons in the Higgs interaction basis $\{H^{\text{NSM}}, H^{\text{SM}}, H^S\}^1$ is given by [66–68]

$$\begin{pmatrix} (m_Z^2 - \frac{1}{2}\lambda^2)\sin 2\beta^2 + \frac{\mu}{\sin\beta\cos\beta}(A_\lambda + \frac{\kappa\mu}{\lambda}) & (\frac{1}{2}\lambda^2 v^2 - m_Z^2)\sin 2\beta \cos 2\beta & -\frac{1}{\sqrt{2}}\lambda v \cos 2\beta(\frac{2\kappa\mu}{\lambda} + A_\lambda) \\ (\frac{1}{2}\lambda^2 v^2 - m_Z^2)\sin 2\beta \cos 2\beta & m_Z^2 \cos 2\beta^2 + \frac{1}{2}\lambda^2 v^2 \sin 2\beta^2 & \sqrt{2}\lambda v \mu(1 - \frac{A_\lambda}{2\mu}\sin 2\beta - \frac{\kappa}{\lambda}\sin 2\beta) \\ -\frac{1}{\sqrt{2}}\lambda v \cos 2\beta(\frac{2\kappa\mu}{\lambda} + A_\lambda) & \sqrt{2}\lambda v \mu(1 - \frac{A_\lambda}{2\mu}\sin 2\beta - \frac{\kappa}{\lambda}\sin 2\beta) & \frac{1}{4}\lambda^2 v^2 \sin 2\beta(\frac{A_\lambda}{\mu}) + \frac{\kappa\mu}{\lambda}(A_\kappa + \frac{4\kappa\mu}{\lambda}) \end{pmatrix} \quad (6)$$

Here, β is defined as $\tan^{-1} \frac{v_u}{v_d}$, m_Z represents the Z boson mass and $v = \sqrt{v_u^2 + v_d^2}$. Defining

$$M_A^2 = \frac{\mu}{\sin\beta\cos\beta} \left(A_\lambda + \frac{\kappa\mu}{\lambda} \right), \quad (7)$$

the elements of the symmetric 2×2 pseudoscalar Higgs squared mass matrix (M_p^2) in the interaction basis $\{A^{\text{NSM}}, A^S\}^2$ can be written as follows [66–68]:

$$\begin{pmatrix} M_A^2 & -\frac{1}{\sqrt{2}}\lambda v \left(\frac{3\kappa\mu}{\lambda} - \frac{M_A^2}{2\mu} \sin 2\beta \right) \\ -\frac{1}{\sqrt{2}}\lambda v \left(\frac{3\kappa\mu}{\lambda} - \frac{M_A^2}{2\mu} \sin 2\beta \right) & \frac{1}{2}\lambda^2 v^2 \sin 2\beta \left(\frac{M_A^2}{4\mu^2} \sin 2\beta + \frac{3\kappa}{2\lambda} \right) - \frac{3\kappa A_\kappa \mu}{\lambda} \end{pmatrix}. \quad (8)$$

The Higgs mass eigenstates are defined in terms of the Higgs interaction basis

$$H_i = s_{i1} H^{\text{NSM}} + s_{i2} H^{\text{SM}} + s_{i3} H^S, \quad i = 1, 2, 3 \quad (9)$$

$$A_j = p_{j1} A^{\text{NSM}} + p_{j2} A^S, \quad j = 1, 2 \quad (10)$$

¹ H^{SM} refers to the eigenstate which has SM Higgs boson like couplings with the SM particles, H^{NSM} refers to the eigenstate which has couplings similar to the additional scalar Higgs boson in MSSM and H^S refers to the singletlike scalar eigenstate.

²Here, A^{NSM} refers to the pseudoscalar eigenstate with couplings similar to the MSSM pseudoscalar Higgs boson and A^S refers to the singletlike pseudoscalar eigenstate.

where, s_{ik} and p_{jk} are obtained by diagonalizing the corresponding mass squared matrices.

In addition to the 3 CP -even neutral Higgs states, H_1, H_2, H_3 , one of which is identified with H_{125} (H_1 being the lightest and H_3 being the heaviest), and, 2 CP -odd neutral Higgs bosons, A_1, A_2 (A_1 being the lighter one), the NMSSM Higgs spectrum also contains two charged Higgs bosons. The tree-level mass of the charged Higgs bosons is given by

$$M_{H^\pm}^2 = M_A^2 + M_W^2 - \frac{1}{2}\lambda^2 v^2 \quad (11)$$

where, M_W represents the mass of W boson.

$$M_{\tilde{\chi}_i^0} = \begin{pmatrix} M_1 & 0 & -m_Z \sin \theta_W \cos \beta & m_Z \sin \theta_W \sin \beta & 0 \\ 0 & M_2 & m_Z \cos \theta_W \cos \beta & -m_Z \cos \theta_W \sin \beta & 0 \\ -m_Z \sin \theta_W \cos \beta & m_Z \cos \theta_W \cos \beta & 0 & -\mu & -\lambda v \sin \beta \\ m_Z \sin \theta_W \sin \beta & -m_Z \cos \theta_W \sin \beta & -\mu & 0 & -\lambda v \cos \beta \\ 0 & 0 & -\lambda v \sin \beta & -\lambda v \cos \beta & 2\kappa v_s \end{pmatrix} \quad (13)$$

where, M_1 is the bino mass parameter, M_2 is the wino mass parameter, m_Z is the mass of the Z boson and θ_W is the Weinberg angle.

The neutralino mass eigenstates are given by

$$\tilde{\chi}_i^0 = N_{i1}\tilde{B} + N_{i2}\tilde{W}^3 + N_{i3}\tilde{H}_d^0 + N_{i4}\tilde{H}_u^0 + N_{i5}\tilde{S} \quad (14)$$

where, the N_{ij} 's are obtained by diagonalizing the neutralino mass matrix in Eq. (13). It follows from Eq. (13) that the neutralino sector at tree level is governed by the following input parameters:

$$M_1, M_2, \mu, \tan \beta, \lambda, \kappa. \quad (15)$$

It must be noted that the phenomenology of the electroweakino and Higgs sectors is modified from that in the MSSM due to additional parameters $\lambda, \kappa, A_\lambda, A_\kappa$.

Standard big bang cosmology with thermally produced neutralinos with $M_{\tilde{\chi}_1^0} \lesssim 62.5$ GeV as the cold dark matter results in too large a density of cold dark matter, unless resonance enhancements of annihilation are operative in the early universe. The Z boson and the SM-like Higgs boson enables the LSP neutralino to generate a correct or underabundant relic density in the $M_{\tilde{\chi}_1^0} \sim M_Z/2$ and $M_{\tilde{\chi}_1^0} \sim M_{H_{125}}/2$ regions. At lower LSP masses ($\lesssim M_Z/2$), efficient annihilation can be achieved via exchange of a light scalar Higgs (H_1) or a pseudoscalar Higgs (A_1), with mass, $M_{A_1/H_1} \sim 2M_{\tilde{\chi}_1^0}$.

It can be observed from Eq. (6)–(11) that the tree-level Higgs sector of the NMSSM can be parametrized by 6 input parameters:

$$\lambda, \kappa, A_\lambda, A_\kappa, \tan \beta, \mu. \quad (12)$$

Compared with the MSSM, the electroweakino sector of the NMSSM is phenomenologically richer and contains 5 neutralinos and 2 charginos. The neutralino mass matrix, in the basis of $\{\tilde{B}, \tilde{W}_3, \tilde{H}_d^0, \tilde{H}_u^0, \tilde{S}\}$ (\tilde{B} : bino, \tilde{W}^3 : neutral wino, \tilde{H}_d^0 and \tilde{H}_u^0 : neutral Higgsinos, \tilde{S} : singlino) is given by (following the notation of [67])

III. SCANNING THE NMSSM PARAMETER SPACE

The first step of our analysis is to delineate the NMSSM parameter space region which is compatible with current constraints from collider and dark matter searches. A detailed discussion of constraints is found in Sec. IV. Note that a light $\tilde{\chi}_1^0$ is completely consistent with all the current data in the NMSSM unlike in the MSSM and we intend to focus on the case of a light neutralino LSP with mass $M_{\tilde{\chi}_1^0} < 62.5$ GeV. We find that there is a significant region with $M_{\tilde{\chi}_1^0} < 62.5$ GeV where the invisible decay of H_{125} into a $\tilde{\chi}_1^0$ pair is kinematically allowed. We zero in on this region and also explore prospects for invisible Higgs boson searches at future facilities.

The main focus of this study involves the exploration of the Higgs and electroweakino sectors of the NMSSM parameter space. The relevant input parameters which captures the physics of these two sectors are: $\lambda, \kappa, A_\lambda, A_\kappa, \tan \beta, \mu, M_1, M_2$ [from Eq. (12) and (15)], M_3 : the gluino mass parameter, A_t, A_b, A_τ : the stop, sbottom and stau trilinear coupling, and $M_{U_R^3}, M_{D_R^3}, M_{Q_L^3}$: the mass of the third generation squarks. The first and second generation squark masses, and the slepton masses are fixed at 3 TeV.

The scenario with $\lambda, \kappa \approx 0$ is referred to as the effective MSSM [25]. From Eq. (1), it becomes clear that the singlet superfield \hat{S} does not interact with the MSSM Higgs superfields, \hat{H}_u and \hat{H}_d , when $\lambda \rightarrow 0$. In the limit of effective MSSM, the singlet scalar, the singlet pseudoscalar and the singlinolike neutralino does not couple with the MSSM sector. Thus, it is not possible to distinguish

between the $\lambda, \kappa \rightarrow 0$ limit (with $\lambda\langle s \rangle$ fixed) of the NMSSM and the MSSM scenario. It is however possible for the singlinolike neutralino to be the LSP with mass $\sim 2\kappa\langle s \rangle$. In order to allow the interaction between the singlet sector and the MSSM sector, it is essential to have a nonzero λ . For the case of a singlinolike LSP and $\lambda \ll 1$, the MSSM-like NLSPs would undergo cascade decay into singlinolike LSP + SM particles with a long lifetime which could also lead to potential LLP (long-lived particles) signatures, the study of which is beyond the scope of this work. Therefore, in this article, we focus on the regions of parameter space where λ and κ are not ≈ 0 or $\ll 1$.

The `NMSSMTools-5.3.1` [46,69–73] package is used to generate the particle spectrum, and to compute the couplings and branching fraction of the Higgses and the branching ratios of the SUSY particles. The presence of a large number of input parameters makes it difficult to find parameter space points in the $M_{\tilde{\chi}_1^0} \lesssim 62.5$ GeV region and it becomes essential to choose an optimized scan range for the input parameters. Initially, a random scan of the parameter space is performed using the `NMSSMTools-5.3.1` package, for a wide range of input parameters. In the next step, the parameter space points, thus generated, are checked against the theoretical, collider and astrophysical constraints, implemented within `NMSSMTools-5.3.1`. Parameter space points are then chosen from the previous step to be used as seeds for the Markov Chain Monte Carlo (mcmc) scanning technique implemented in the `NMSSMTools-5.3.1` package. The parameter space points generated from the mcmc scan are distributed over the following range of input parameters:

$$\begin{aligned}
0.01 < \lambda < 0.7, \quad 10^{-5} < \kappa < 0.05, \quad 3 < \tan\beta < 40 \\
100 \text{ GeV} < \mu < 1 \text{ TeV}, \quad 1.5 \text{ TeV} < M_3 < 10 \text{ TeV} \\
2 \text{ TeV} < A_\lambda < 10.5 \text{ TeV}, \quad -150 \text{ GeV} < A_\kappa < 100 \text{ GeV} \\
M_1 = 2 \text{ TeV}, \quad 70 \text{ GeV} < M_2 < 2 \text{ TeV} \\
A_t = 2 \text{ TeV}, \quad A_{b,\tilde{\tau}} = 0, \quad M_{U_R^3}, \quad M_{D_R^3}, \\
M_{Q_L^3} = 2 \text{ TeV}, \quad M_{e_L^3}, \quad M_{e_R^3} = 3 \text{ TeV} \quad (16)
\end{aligned}$$

The collider and astrophysical observables that constrain the points generated from this scan are detailed in the next section.

IV. CONSTRAINTS

As we have just mentioned, our demand that the singlino is lighter than 62.5 GeV, along with the chosen range of input parameters, leads to H_1 and A_1 lighter than 125 GeV, so that H_2 then plays the role of the observed SM-like Higgs boson. The SM-like Higgs boson is required to lie within the mass range allowed by the measurements at the LHC and its couplings must be compatible with those measured at the LHC. The NMSSM parameter space

considered in our study is further constrained by the low-energy flavor physics limits, LEP limits, searches of directly produced light Higgs bosons and measurements of the Higgs boson signal strengths at the LHC, gluino searches, direct searches of electroweakinos in the $3l + \cancel{E}_T$ and the $l^+l^- + \cancel{E}_T$ final state as well as from direct and indirect DM searches. These constraints are discussed in more detail below.

- (i) Mass of SM-like Higgs boson: The combined measurement by the ATLAS and CMS collaborations has determined the Higgs boson mass to lie within 124.4–125.8 GeV (3σ) [1]. Adopting a conservative approach, we require H_2 (we will henceforth also refer to this as H_{125}) to be within the interval 122–128 GeV, to allow for theoretical uncertainties in the Higgs boson mass computation [74–76].
- (ii) Limits from LEP: Measurements at LEP have excluded a chargino with mass below $M_{\tilde{\chi}_1^\pm} \lesssim 103.5$ GeV [77]. This constraint, together with our choice $M_1 = 2$ TeV [see Eq. (16)] requires that the LSP below 62.5 GeV is dominantly singlino, with only small Higgsino, wino and bino admixture. We also impose the upper limit on the production cross section of $\tilde{\chi}_1^0\tilde{\chi}_2^0$ pair at 95% C.L. ($\sigma_{\tilde{\chi}_1^0\tilde{\chi}_2^0} \lesssim 0.1$ pb [77]) for $|M_{\tilde{\chi}_2^0} - M_{\tilde{\chi}_1^0}| > 5$ GeV as well as upper limits on $e^+e^- \rightarrow ZH_j$ and $e^+e^- \rightarrow A_iH_j$ processes in various final states. The `NMSSMTools-5.3.1` framework was used to implement these constraints.
- (iii) Upper bound on relic density: Results from the PLANCK Collaboration have put the DM relic density at $\Omega_{\text{DM}}^{\text{obs}} h^2 = 0.120 \pm 0.001$ [78], and assuming a 2σ window, the relic density can fall within an interval of 0.118–0.122. `micrOMEGAS` [79,80] is used to compute the relic density of the LSP neutralino in the standard cosmological scenario, and adopting a conservative approach, we only exclude over-abundant DM, that is we require $\Omega_{\text{DM}(\tilde{\chi}_1^0)}^{\text{obs}} h^2 \leq 0.122$. This constraint would not apply if DM production entails nonstandard cosmology [81–83]. In this work, the scenario of nonstandard cosmology has not been considered.
- (iv) Flavor physics constraints: Constraints from the measurement of flavor physics observables offer sensitive probes of new physics scenarios. We impose the flavor physics constraints through bounds on the branching fraction of the rare decay modes $B \rightarrow X_s\gamma$, $B_s \rightarrow \mu^+\mu^-$ and $B^+ \rightarrow \tau^+\nu_\tau$. Recent measurements obtain $\text{Br}(B \rightarrow X_s\gamma) = (3.32 \pm 0.16) \times 10^{-4}$ [84], $\text{Br}(B_s \rightarrow \mu^+\mu^-) = (3.0 \pm 0.6_{-0.2}^{+0.3}) \times 10^{-9}$ [85] and $\text{Br}(B^+ \rightarrow \tau^+\nu_\tau) = (1.06 \pm 0.19) \times 10^{-4}$ [84]. In the current study, we use `micrOMEGAS-5.0.6` [79,86,87] to compute these branching fractions and we allow 2σ experimental

uncertainty. Note that we do not use the `NMSSMTools-5.3.1` framework to implement the aforementioned B -physics constraints, rather, we impose the more recent bounds on the flavor physics observables discussed in this section. Additionally, the constraints on $\Upsilon(1s) \rightarrow H/A\gamma$, ΔM_s and ΔM_d are also imposed using the `NMSSMTools-5.3.1` package.

- (v) Higgs signal strength measurements: The signal strength constraints in the $b\bar{b}$, $\tau^+\tau^-$, ZZ , W^+W^- and $\gamma\gamma$ final states, derived from LHC Run-II data, are imposed using the `NMSSMTools-5.3.1` package.
- (vi) Invisible decay width of the Higgs boson: The CMS Collaboration has derived an upper limit on the total decay width of the observed 125 GeV Higgs boson, using the dataset collected at 5.1 fb^{-1} and 19.7 fb^{-1} , for $\sqrt{s} = 7 \text{ TeV}$ and $\sqrt{s} = 8 \text{ TeV}$, respectively. At 95% C.L., the upper limit stands at $\Gamma_{H_{125}} < 22 \text{ MeV}$ [88]. Correspondingly, in the current analysis, we require the total decay width of H_{125} to lie below 22 MeV.

The total invisible branching fraction of the SM like Higgs can also be probed by directly searching for the invisibly decaying Higgs boson through its production in association with a vector boson [89,90] and *jets* [91] or vector boson fusion [92]. We have imposed upper limits obtained from such studies. The ATLAS Collaboration has also used LHC Run-II data ($\mathcal{L} \sim 140 \text{ fb}^{-1}$) to probe the invisibly decaying Higgs, produced via VBF mode, and have set an upper limit of 13% [93]. We must note that Ref. [93] is a preprint and the published result from the ATLAS collaboration used LHC Run-I data, considered Higgs production via WH_{125} , ZH_{125} and VBF modes, and have set an upper limit of 25% [94]. Similar search by the CMS Collaboration, using the entire Run-I data and 35.9 fb^{-1} of the Run-II data, have derived an upper limit at 19% [95]. The prospects of probing the invisibly decaying Higgs boson at the future LHC has also been studied, see for example Refs. [65,96]. In the context of our analysis, the invisible decay modes of the SM-like Higgs (H_{125}) are: $H_{125} \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0$, $H_{125} \rightarrow H_1 H_1 \rightarrow 4\tilde{\chi}_1^0$ and $H_{125} \rightarrow A_1 A_1 \rightarrow 4\tilde{\chi}_1^0$. We impose an upper limit of 13% on the sum of these branching fractions. We note that the Higgs signal strength constraints also impose an indirect upper limit on the invisible branching fraction of the Higgs boson. The indirect limit can be comparable or, at times, even stronger than the direct upper limit, *viz* see Ref. [24]. In our case, we find the indirect upper limit to be nearly comparable with the latest direct upper limit from ATLAS [93] and our results do not change upon increasing the direct upper limit on the invisible branching fraction of the Higgs boson from 13% to the published limit of 19%.

- (vii) Gluino searches at the LHC: Searches by the ATLAS and CMS collaborations using the LHC Run-II data collected at $\sim 36 \text{ fb}^{-1}$ and $\sim 139 \text{ fb}^{-1}$ of integrated luminosity has excluded gluinos up to 2 TeV [97] and 2.2 TeV [98], respectively, at 95% C.L. for a binolike LSP with mass up to $\sim 600 \text{ GeV}$. Correspondingly, we impose a lower limit of 2.2 TeV on the gluino mass.
- (viii) Direct search of light Higgs bosons at the LHC: The ATLAS Collaboration has searched for a Higgs boson decaying into a pair of light spin-zero particles (A_1 or H_1), one of which further decay into $b\bar{b}$ and the other decays into a pair of muons [99]. This search probed the mass range of $20 \text{ GeV} < M_{H_{1, A_1}} < 60 \text{ GeV}$ using the LHC dataset collected at $\sqrt{s} = 13 \text{ TeV}$ corresponding to an integrated luminosity of 36.1 fb^{-1} and derived upper limits on the production cross section of the SM-like Higgs (H_{125}) normalized with its SM value ($\sigma_{H_{125}}/\sigma_{H_{SM}}$) times the branching fraction of $H_{125} \rightarrow A_1 A_1 \rightarrow 2b2\mu$. We have computed the value of $\sigma_{H_{125}}/\sigma_{H_{SM}} \times \text{Br}(H_{125} \rightarrow A_1 A_1 \rightarrow 2b2\mu)$ at $\sqrt{s} = 13 \text{ TeV}$ for each point in the parameter scape and exclude points which exceed the upper limit.

The CMS collaboration has also searched for the exotic decay of a Higgs boson into two pseudoscalar Higgses in the $2b2\tau$ final state [51] and $2\mu2\tau$ final state [52]. From the $\sqrt{s} = 13 \text{ TeV}$ dataset collected with $\mathcal{L} \sim 36 \text{ fb}^{-1}$, upper limits were derived on $\sigma_{H_{125}}/\sigma_{H_{SM}} \times \text{BR}(H_{125} \rightarrow A_1 A_1 \rightarrow b\bar{b}\tau^+\tau^-)$ and $\sigma_{H_{125}}/\sigma_{H_{SM}} \times \text{BR}(H_{125} \rightarrow A_1 A_1 \rightarrow \mu^+\mu^-\tau^+\tau^-)$ over the mass range of $15 \text{ GeV} < M_{A_1} < 60 \text{ GeV}$. We have excluded points which exceed these upper limits as well.

- (ix) Direct electroweakino searches at the LHC: Numerous searches have been performed by both ATLAS and CMS, to probe the neutralinos and charginos, and limits have been derived on the mass of electroweakinos within simplified model scenarios [100]. The most stringent limits are offered by the search channel $pp \rightarrow (\tilde{\chi}_i^0 \rightarrow Z/H_{125}\tilde{\chi}_1^0)(\tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0)$ resulting in a $3l + \cancel{E}_T$ final state. A recent study by CMS which looked into the $3l + \cancel{E}_T$ final state, originating from the cascade decay of directly produced mass degenerate winolike $\tilde{\chi}_2^0\tilde{\chi}_1^\pm$ pair ($\tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0, \tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0$), has excluded winolike $\tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ up to $\sim 600 \text{ GeV}$ for $M_{\tilde{\chi}_1^0} \lesssim 60 \text{ GeV}$ (Fig. 7 in [62]). It must be noted that this search assumes a 100% branching ratio for $\text{Br}(\tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0)$ and $\text{Br}(\tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0)$. In regards to the parameter space considered in this study, $\tilde{\chi}_2^0$ has additional decay modes namely $\tilde{\chi}_2^0 \rightarrow H_1\tilde{\chi}_1^0$, $\tilde{\chi}_2^0 \rightarrow A_1\tilde{\chi}_1^0$ and $\tilde{\chi}_2^0 \rightarrow H_2\tilde{\chi}_1^0$, and, therefore, the assumption of $\text{Br}(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z) \sim 100\%$ does not always hold true. As a result,

the wino exclusion limit derived in [62] cannot be directly applied to the parameter space of interest. The limits derived in [62] have been translated to the case of Higgsino-like NLSP's ($M_2 > \mu$) in [44], where the direct production of mass-degenerate Higgsino-like $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ and $\tilde{\chi}_3^0 \tilde{\chi}_1^\pm$, is considered. This translation procedure enables recasting of the electroweakino search limits derived within a simplified model framework to any generic parameter space point. This translation scheme is implemented in the `NMSSMTools-5.3.1` package, and has been used to evaluate the impact of direct electroweakino search limits in the $3l + \cancel{E}_T$ final state, performed using LHC $\sqrt{s} = 13$ TeV dataset collected at $\sim 36 \text{ fb}^{-1}$ [62], on the parameter space under study.

The ATLAS Collaboration has also probed the electroweakino sector via direct chargino pair-production in the WW -mediated opposite-sign dilepton $+ \cancel{E}_T$ final state within a simplified model framework with winolike $\tilde{\chi}_1^\pm$ [101]. This search was performed using the LHC Run-II data collected with $\mathcal{L} \sim 139 \text{ fb}^{-1}$. The limits obtained from this search exclude a winolike chargino up to $M_{\tilde{\chi}_1^\pm} \sim 400$ GeV for a binolike $\tilde{\chi}_1^0$ with mass up to $M_{\tilde{\chi}_1^0} \sim 90$ GeV assuming 100% branching ratio in the $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$ channel. This condition holds true for the parameter space considered in this study since the only possible two body decay mode for $\tilde{\chi}_1^\pm$ is into a $W^\pm \tilde{\chi}_1^0$ pair. Therefore these search limits can directly be translated in the current analysis by excluding dominantly winolike charginos (wino-content in $\tilde{\chi}_1^\pm \gtrsim 90\%$) with mass $M_{\tilde{\chi}_1^\pm} \lesssim 400$ GeV.

- (x) Direct detection constraints: The spin-independent (SI) and spin-dependent (SD) DM-nucleon scattering cross sections form the basis of DM direct detection experiments. We impose the latest upper limits on spin-independent WIMP-nucleon cross section (σ_{SI} ; Xenon-1T [63]), the spin-dependent WIMP-neutron cross section ($\sigma_{\text{SD-neutron}}$; Xenon-1T [102]), and the spin-dependent WIMP-proton cross section ($\sigma_{\text{SD-proton}}$; PICO-60 [103]) derived at 90% C.L.. Among the points allowed by the latest upper limits on σ_{SI} , a small fraction ($\lesssim 4\%$) of points are excluded by the current upper limits on $\sigma_{\text{SD-proton}}$ and $\sigma_{\text{SD-neutron}}$. These points which are exclusively excluded by the current upper limits on the spin-dependent WIMP-neutron/proton cross sections feature a large $\lambda (\gtrsim 0.1)$ and a relatively large Higgsino component is $\tilde{\chi}_1^0$.

We illustrate in Fig. 1 the impact of current constraints in the M_2 - μ plane. The grey points are excluded by either the LEP limits, LHC signal strength constraints, B physics constraints or direct light Higgs searches and sparticle searches at the LHC. In particular, the points generated in the large M_2 region are excluded by constraints on the Higgs

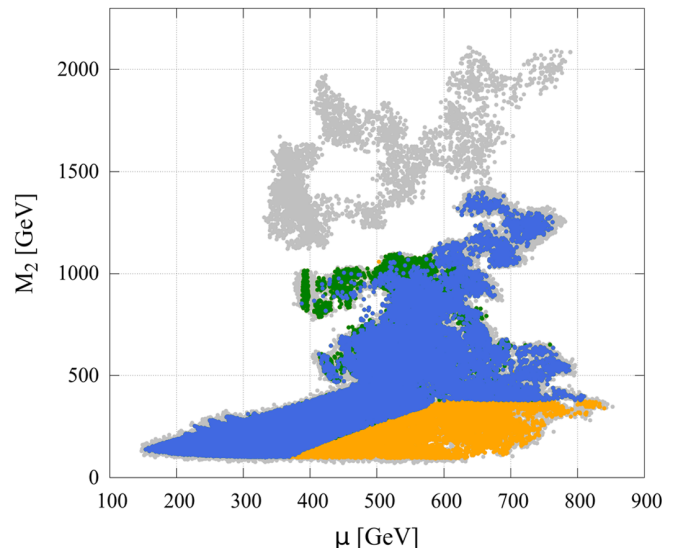


FIG. 1. Parameter space points are shown in the μ - M_2 plane. The grey colored points are excluded by the LEP limits, LHC signal strength constraints, B physics constraints, direct light Higgs searches at the LHC and sparticle searches at the LHC. The green colored points are excluded by the latest limits on σ_{SI} ([63]), $\sigma_{\text{SD-neutron}}$ ([102]) and $\sigma_{\text{SD-proton}}$ ([103]) at 90% C.L. while the orange colored points are excluded by the current 95% C.L. limits from direct electroweakino searches in $3l + \cancel{E}_T$ and $2l + \cancel{E}_T$ channels. The blue colored points represent the currently allowed parameter space.

sector including the requirement of having a Higgs around 125 GeV as well as the constraints on the Higgs signal strengths and from the LEP searches for light Higgses. Indeed in this region, the one-loop corrections to the Higgs masses from charginos can be large [66], thus impacting both the mass spectrum of the scalars and their singlet/doublet content. Note also that the Higgs sector depends strongly on the third generation squark sector, hence the impact of the Higgs constraints could be relaxed in a more general framework where parameters of the squark sector are allowed to vary, and not kept fixed as we have in Eq. (16). We also indicate those points (green) that are excluded by the latest upper limits from the direct detection experiments and those (orange) that are excluded by the current direct electroweakino searches limits discussed in Sec. IV. The blue colored points represent the set of currently allowed parameter space points with light neutralinos that we will use to study the impact of current indirect detection constraints and the reach of future experiments.

- (xi) Indirect detection constraints: The indirect detection of DM aims at identifying the visible signatures originating from interactions between the dark matter already present in the universe. The FERMI-LAT Collaboration has derived constraints on the

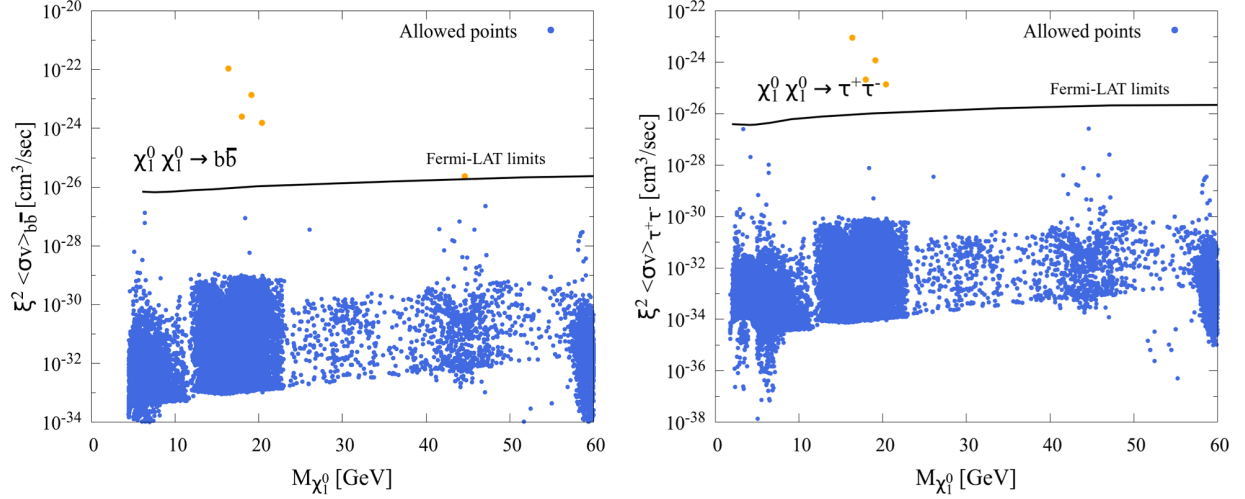


FIG. 2. The ξ^2 scaled thermally averaged DM annihilation cross section times velocity ($\langle \sigma v \rangle$) in the $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow b\bar{b}$ (left) and $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow \tau^+ \tau^-$ (right) channels has been shown in the y-axis against $M_{\tilde{\chi}_1^0}$ in the x-axis. The parameter space points shown here are allowed by all the current constraints discussed till now in the present section. The black dashed line represents the 95% C.L. upper limits on the $\langle \sigma v \rangle$ from search for excess γ -ray emission in dwarf galaxies by the FERMI-LAT Collaboration [64]. The orange colored points are excluded by the current indirect limits, while the blue colored points are still allowed.

thermally averaged DM annihilation cross section times the relative velocity between the DM candidates ($\langle \sigma v \rangle$) in $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow b\bar{b}, \tau^+ \tau^-$ channels [64]. In the current study, we use micrOMEGAs-5.0.6 to compute $\langle \sigma v \rangle$. Recall that the annihilation rate scales as the square of the local dark matter density. Assuming thermal DM, this then is scaled by a factor $\xi = \Omega_{\tilde{\chi}_1^0}^{\text{thermal}}/0.12$. This then means that the detection rate will scale by ξ^2 . After this scaling, we find that only a few points are constrained by current FERMI-LAT limits, see Fig. 2. Moreover values of $\xi^2 \langle \sigma v \rangle$ can lie several orders of magnitude below current upper limits as well as below the typical value expected, 3×10^{-26} cm³/sec, even for points with ξ close to unity.

The very small values of $\xi^2 \langle \sigma v \rangle$ that we found in our scenarios can be explained as follows. As already noted, the relic density constraint requires that DM annihilation be enhanced by s -channel exchange of a boson (Z or scalar/pseudoscalar) near a resonance. For low dark matter masses below ~ 10 GeV where one may also have to worry about CMB constraints (from DM annihilation injecting electromagnetic energy during the era of matter-radiation decoupling), the enhancement is due to *very narrow* A_1/H_1 resonances which have very small couplings and tiny values of $\Gamma/M_{A_1/H_1}$, $\sim 10^{-9}$ – 10^{-7} , resulting in a very strong velocity dependence of the annihilation cross section. Typically the thermal energy of the DM in the early universe will allow for the required enhancement of the cross section while for the lower DM galactic

velocities, there is no such enhancement. For the same reason, CMB constraints which involve even smaller velocities, will also not apply [104], even though the thermal relic density may be close to its observed value. The only exception is when the DM mass is very near $M_{A_1/H_1}/2$ or even slightly above, then the full resonant enhancement can occur at small velocities $v \sim 10^{-3}c$ while for the higher velocities in the early universe $v \sim 0.3c$ only the tail of the resonance will contribute. The fact that DM annihilation cross section in the galaxy can be enhanced as compared with the one in the early universe—the so-called Breit-Wigner enhancement—was discussed in [40,105]. It requires a very narrow resonance, as is the case here for the light scalar/pseudoscalar here, as well as a fine-tuned mass difference $M_{\tilde{\chi}_1^0} - M_{A_1/H_1}/2$. In our scan we find a few points which feature such a large cross section and are thus excluded by FermiLAT. Following the same line of argument, we also expect only a few fine-tuned points to be subject to CMB constraints.

The parameter space points from Fig. 2 which are allowed by all constraints discussed above will be referred to as the allowed parameter space points in the remainder of this paper.

V. THE THERMAL NEUTRALINO

Having discussed the relevant experimental constraints, we will move on to discuss the characteristic features of the NMSSM parameter space under study. At this point, we reiterate that we remain confined to the region where the

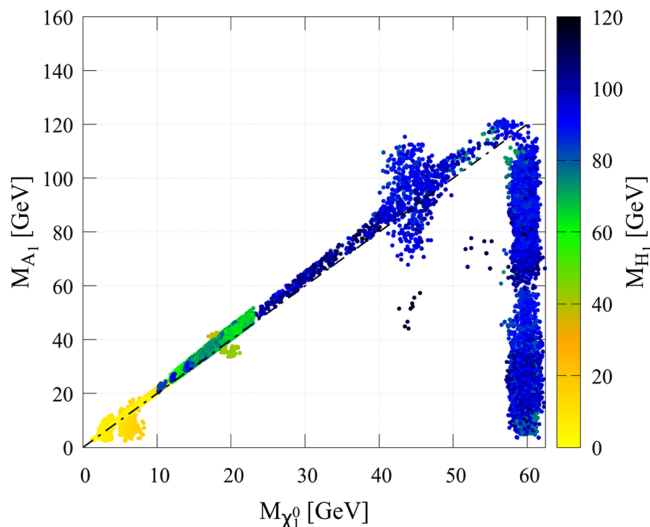


FIG. 3. Correlation between the mass of the LSP neutralino ($M_{\tilde{\chi}_1^0}$) and the mass of the light pseudoscalar Higgs (M_{A_1}) in the $M_{\tilde{\chi}_1^0}$ and M_{A_1} plane. The mass of lightest scalar Higgs (M_{H_1}) is represented along the color axis. The black dashed line corresponds to $M_{A_1} = 2M_{\tilde{\chi}_1^0}$. The parameter space points shown here are allowed by all the constraints listed in Sec. IV.

decay of SM-like Higgs boson into a pair of LSP neutralinos is kinematically feasible, and, correspondingly, we impose an upper bound on the mass of $\tilde{\chi}_1^0$, $M_{\tilde{\chi}_1^0} \leq 62.5$ GeV. In addition, the parameter space is also subjected to the collider and astrophysical constraints discussed in Sec. IV.

In the MSSM parameter space considered in our previous work [24], it was observed that the imposition of the relic density constraint resulted in a lower bound ($M_{\tilde{\chi}_1^0} \gtrsim 34$ GeV) on the mass of the LSP neutralino. The lower bound on $M_{\tilde{\chi}_1^0}$ was implied by the presence of only the Z boson and the Higgs boson as mediators for efficient $\tilde{\chi}_1^0\tilde{\chi}_1^0$ annihilation. Correspondingly, the MSSM parameter space points were confined to the Z funnel ($\sim M_Z/2$) and Higgs-funnel ($M_{H_{125}}/2$) regions only. The NMSSM framework, on the other hand, features additional light Higgses (H_1 and A_1) with mass below M_Z , which can potentially mediate the annihilation of lighter LSP neutralinos with mass below the Z funnel region. Correspondingly, we obtain allowed parameter space points with $M_{\tilde{\chi}_1^0}$ as low as ~ 1 GeV, which are consistent with the upper bound on relic abundance.

In order to emphasize upon the mass correlations between the LSP neutralino and light Higgs boson states, we plot the allowed parameter space points from Fig. 2 in the $M_{\tilde{\chi}_1^0}$ - M_{A_1} plane shown in Fig. 3. The color palette in Fig. 3 represents the mass of lightest scalar Higgs boson, M_{H_1} . It is evident from Fig. 3 that the allowed points below the Z funnel region are mostly populated along the line $M_{A_1} \sim 2M_{\tilde{\chi}_1^0}$, those that lie below this line actually satisfy

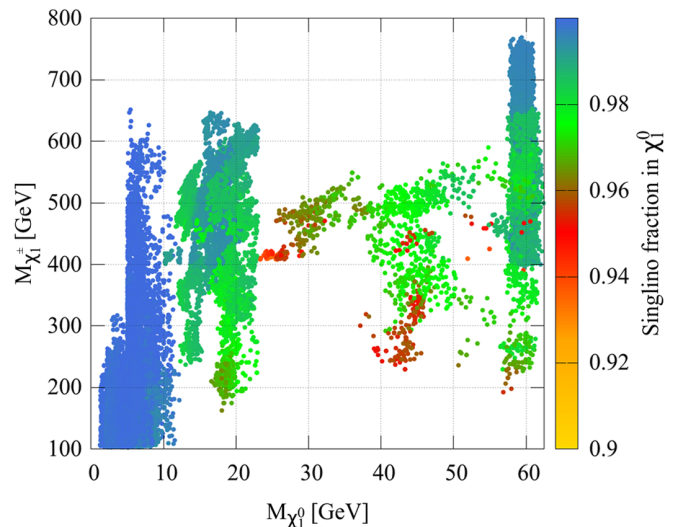


FIG. 4. The allowed parameter space points are shown in the $M_{\tilde{\chi}_1^0}$ - $M_{\tilde{\chi}_1^\pm}$ plane. The color palette represents the fraction of singlino content in the LSP $\tilde{\chi}_1^0$.

the condition $M_{H_1} \sim 2M_{\tilde{\chi}_1^0}$. Accord with the relic density constraint is then attained by efficient annihilation via the A_1/H_1 resonance. We also exhibit the currently allowed parameter space points in the $M_{\tilde{\chi}_1^0}$ - $M_{\tilde{\chi}_1^\pm}$ plane in Fig. 4. The color palette in Fig. 4 corresponds to the singlino content of the LSP.

The LEP limit on the chargino mass ($M_{\tilde{\chi}_1^\pm} > 103.5$ GeV) implies a lower limit on the doublet Higgsino and wino mass parameters and restricts them to values roughly above ~ 100 GeV. Since our region of interest concerns $M_{\tilde{\chi}_1^0} \leq M_{H_{SM}}/2$, the $\tilde{\chi}_1^0$ has to be either binolike or singlinolike. However, a bino or singlino dominated $\tilde{\chi}_1^0$ can only satisfy the relic density upper bound if it undergoes co-annihilation or pair annihilates via a resonance at roughly twice its mass. Within the NMSSM parameter space considered in the present analysis, co-annihilation is not feasible since there is a large mass splitting between the LSP and all other sparticles. Thus $\tilde{\chi}_1^0\tilde{\chi}_1^0$ annihilation through an intermediate resonance remains the only feasible option with either a light scalar and pseudoscalar Higgs states at mass $\sim 2M_{\tilde{\chi}_1^0}$. In the present analysis, M_1 has been fixed at ~ 2 TeV. Therefore, the possibility of obtaining a bino-dominated $\tilde{\chi}_1^0$ is eliminated. Moreover, a bino-dominated $\tilde{\chi}_1^0$ requires a nonzero doublet Higgsino admixture in order to couple with a Higgs state and since the chargino mass limits constrains the amount of Higgsino fraction in $\tilde{\chi}_1^0$, the relic density limit disfavors a binolike LSP neutralino below the Z funnel region.³ The singlinolike neutralino, on the other

³The possibility of Z funnel annihilation of a binolike LSP also occurs in the MSSM and has been examined in detail in Ref. [24]. Since our goal was to study new possibilities in the MSSM, we have taken the bino to be very heavy in our study.

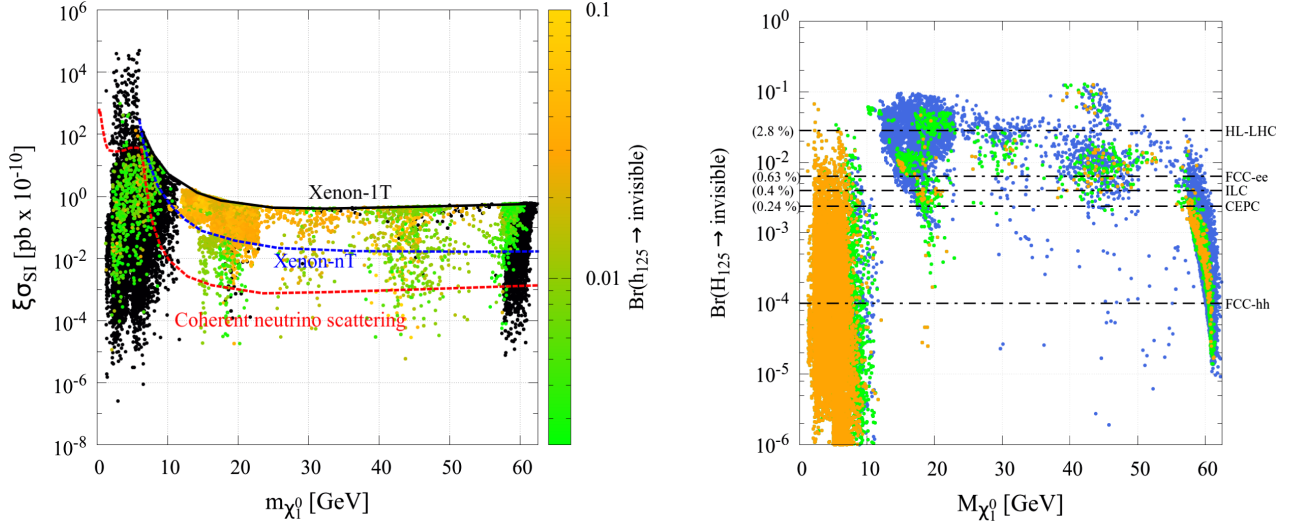


FIG. 5. Left: the currently allowed parameter space points from Fig. 2 are shown in the $\xi\sigma_{\text{SI}}-M_{\tilde{\chi}_1^0}$ plane. The color palette represents the value of $\text{Br}(H_{125} \rightarrow \text{invisible})$ computed by summing over all invisible decay modes of H_{125} . The black colored points have $\text{Br}(H_{125} \rightarrow \text{invisible}) \leq 0.24\%$, and therefore, are outside the projected reach of Higgs invisible width measurement capability of CEPC. The solid black, dashed blue and red dashed lines represent the current upper limits on σ_{SI} from Xenon-1T, the projected upper limits on σ_{SI} from Xenon-nT and the coherent neutrino scattering floor, respectively. Right: allowed parameter space points are shown in the $\text{Br}(H_{125} \rightarrow \text{invisible}) - M_{\tilde{\chi}_1^0}$ plane. The black dashed lines represent the projected capability of measuring the Higgs invisible branching fraction at (from top to bottom): HL-LHC [108], FCC-ee [109], ILC [110], CEPC [107] and FCC-hh [111]. The orange colored points fall below the coherent neutrino scattering floor, while the green colored points are outside Xenon-nT's projected reach and above the coherent neutrino scattering floor. The blue colored points are within the projected reach of Xenon-nT.

hand, can couple with either a singlet scalar or pseudoscalar Higgs with the coupling being proportional to κN_{15}^2 . Therefore the only possibility to obtain a LSP neutralino below $\lesssim 34$ GeV that satisfies the relic density constraint, is to have a singlinolike $\tilde{\chi}_1^0$ and at least one singlet Higgs states at roughly twice its mass.

A study of the composition of light pseudoscalar and scalar Higgses within the allowed parameter space points show that A_1 and H_1 are dominantly singlet in nature,⁴ with singlet fraction $\gtrsim 90\%$. Similarly, in accordance with the previous discussion, the LSP neutralinos are also found to be dominantly singlino in nature, as illustrated in Fig. 4.

VI. PROSPECTS AT FUTURE EXPERIMENTS

This section is subdivided into two parts. In the first part, we study the projected reach of Xenon-nT (via bounds on $\sigma_{\text{SD-neutron}}$), PICO-250 (via bounds on $\sigma_{\text{SD-proton}}$) and at the FCC, ILC and CEPC (through the measurement of the invisible width of H_{125}). The second part investigates the scope of direct light Higgs boson searches in the $2b2\mu$, $2b2\tau$ and $2\mu2\tau$ channels at the future upgrades of LHC. This is, of course, in addition to continuing searches for signals from direct production of superpartners at the LHC, some of which are discussed in Sec. VII.

⁴Similar features have also been reported in a recent work (see Ref. [53]).

A. Reach of Xenon-nT, FCC-hh and the future electron-positron colliders

The projected reach of Xenon-nT [106] in probing SI WIMP-nucleon cross sections extends upto a factor of ~ 50 beyond the current limits from Xenon-1T in the DM mass range of ~ 15 GeV to 62.5 GeV. Correspondingly, a considerable region of the currently allowed parameter space is expected to lie within the future reach of Xenon-nT. We show the projected reach of Xenon-nT (represented as blue dashed line) in the $\xi\sigma_{\text{SI}}-M_{\tilde{\chi}_1^0}$ plane in Fig. 5 (left). The points shown in Fig. 5 (left) correspond to the currently allowed parameter space points. A significant fraction of those points fall within the projected reach of Xenon-nT while another large fraction remains out of reach. Moreover, an important fraction of these points, especially at low masses, lie below the coherent neutrino scattering floor and thus will remain out of reach of even larger detectors. In the same figure, the black points represent those parameter space points for which the invisible branching fraction of the SM-like Higgs boson, $\text{Br}(H_{125} \rightarrow \text{invisible}) < 0.24\%$, and thereby, are outside the projected reach of even the CEPC invisible Higgs boson branching fraction measurements [107]. The color palette represents the value of $\text{Br}(H_{125} \rightarrow \text{invisible})$ for those allowed parameter space points which have $\text{Br}(H_{125} \rightarrow \text{invisible}) > 0.24\%$ and hence fall within the CEPC's projected capability of Higgs invisible branching fraction measurements. The invisible branching fraction has been

computed by adding the contributions from the following decay modes:

- (i) $H_{125} \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0$
- (ii) $H_{125} \rightarrow A_1 A_1 \rightarrow 4\tilde{\chi}_1^0$
- (iii) $H_{125} \rightarrow H_1 H_1 \rightarrow 4\tilde{\chi}_1^0$
- (iv) $H_{125} \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0 \rightarrow (\tilde{\chi}_2^0 \rightarrow H_1 \tilde{\chi}_1^0) \tilde{\chi}_1^0 \rightarrow (H_1 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0) \times 2\tilde{\chi}_1^0 \rightarrow 4\tilde{\chi}_1^0$
- (v) $H_{125} \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0 \rightarrow (\tilde{\chi}_2^0 \rightarrow A_1 \tilde{\chi}_1^0) \tilde{\chi}_1^0 \rightarrow (A_1 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0) \times 2\tilde{\chi}_1^0 \rightarrow 4\tilde{\chi}_1^0$

An important observation to be made from Fig. 5 is that CEPC will be able to probe a small fraction of parameter space points in the $M_{\tilde{\chi}_1^0} \lesssim 10$ GeV region which may be forever outside the reach of DM detectors unless directional detection technologies become available.

The complementarity between direct detection experiments and Higgs boson invisible width measurements at the future electron-positron colliders is further explored in Fig. 5 (right), where the allowed parameter space points are displayed in the $\text{Br}(H_{125} \rightarrow \text{invisible})$ - $M_{\tilde{\chi}_1^0}$ plane together with the future reach of HL-LHC ($\gtrsim 2.8\%$) [108], FCC-ee ($\gtrsim 0.63\%$) [109], ILC ($\gtrsim 0.4\%$) [110], CEPC ($\gtrsim 0.24\%$) [107] and FCC-hh ($\gtrsim 0.01\%$) [111]. The color code illustrates whether points are within (blue) or outside (orange and green) the projected reach of Xenon-nT (via σ_{SI} measurements). The orange colored points also lie below the coherent neutrino scattering floor. It can be observed from Fig. 5 that a majority of the points in the $M_{\tilde{\chi}_1^0} \gtrsim 10$ GeV region would be accessible via invisible Higgs boson branching fraction measurements at future e^+e^- colliders, except when the invisible decay of H_{125} is kinematically suppressed.

In the NMSSM, the spin-independent $\tilde{\chi}_1^0$ -nucleon interaction is mainly mediated through the CP -even Higgs bosons and the squarks. Since we have set the squark mass to a large value ($M_{U_R^3}, M_{D_R^3}, M_{Q_L^3} = 2$ TeV), the main contribution to σ_{SI} comes from the t -channel exchange of H_1 and H_{125} between the $\tilde{\chi}_1^0$ and the light flavored quarks. The respective amplitudes from the exchange of H_1 and H_{125} can also undergo destructive interference for some specific choice of input parameters with substantial fine-tuning [112–116]. Such scenarios, also referred to as blind spots, can escape the current constraints on σ_{SI} and also be compatible with the relic density limits. In NMSSM with singlinolike $\tilde{\chi}_1^0$ LSP, these blind spots can arise when $M_{\tilde{\chi}_1^0}/(\mu \sin \beta) \sim 1$ [117]. In this work, although we do not probe the blind spot scenarios exclusively, however, we do obtain parameter points with small σ_{SI} values (which fall below the projected reach of Xenon-nT), many among which even fall below the neutrino scattering floor [orange colored points in Fig. 5 (right)]. We obtain such points over the entire range of $M_{\tilde{\chi}_1^0} \lesssim M_{H_{125}}/2$ region as illustrated in Fig. 5. Spin-dependent measurements at the future experiments can be potential probes for these points in the $M_{\tilde{\chi}_1^0} \gtrsim 15$ GeV region.

The projected reach of PICO-250 [118] and Xenon-nT [119] in probing SD WIMP-proton and WIMP-neutron cross sections extend up to a factor of ~ 75 and ~ 7 , respectively, beyond the current limits from PICO-60 [103] and Xenon-1T [102] in the DM mass range of ~ 15 GeV to 62.5 GeV. We illustrate the future reach of PICO-250 and Xenon-nT in probing the currently allowed parameter space points in the $\xi\sigma_{\text{SD-proton}}-M_{\tilde{\chi}_1^0}$

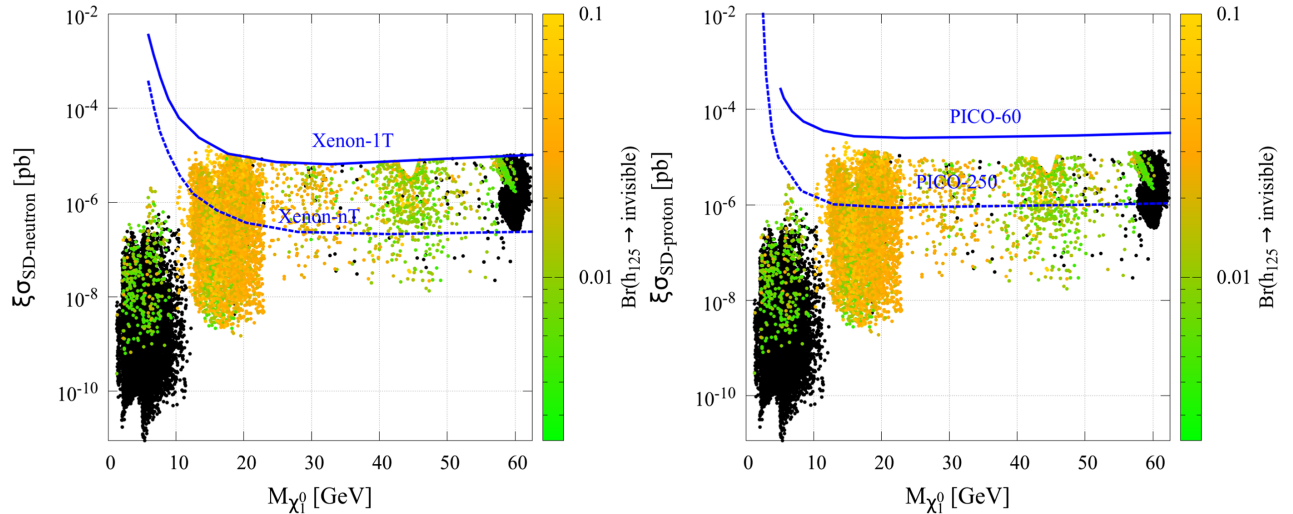


FIG. 6. Left: the currently allowed parameter space points are shown in the $\xi\sigma_{\text{SD-neutron}}-M_{\tilde{\chi}_1^0}$ plane. The solid blue and dashed blue lines represent the current upper limits on $\sigma_{\text{SD-neutron}}$ from Xenon-1T [102] and the projected upper limits on $\sigma_{\text{SD-proton}}$ from Xenon-nT [119], respectively. Right: allowed parameter space points are shown in the $\xi\sigma_{\text{SD-neutron}}-M_{\tilde{\chi}_1^0}$ plane. The solid blue and dashed blue lines represent the current upper limits on $\sigma_{\text{SD-proton}}$ from PICO-60 [103] and the projected upper limits on $\sigma_{\text{SD-proton}}$ from PICO-250 [118], respectively. The color code is similar to that followed in Fig. 5 (left).

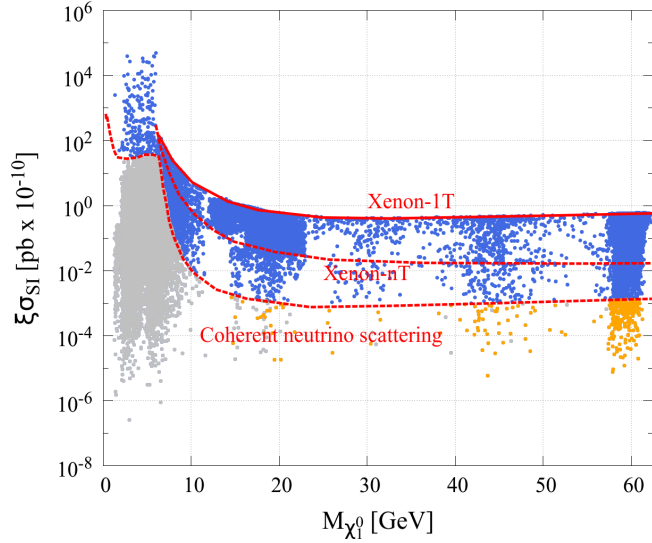


FIG. 7. The currently allowed parameter space points are shown in the $\xi\sigma_{\text{SI}}-M_{\tilde{\chi}_1^0}$ plane. The blue points fall above the coherent neutrino scattering floor while the grey and orange points fall below. The orange points also fall within the projected reach of Xenon-nT (via $\sigma_{\text{SD-neutron}}$ measurements) or PICO-250 (via $\sigma_{\text{SD-neutron}}$ measurements).

and $\xi\sigma_{\text{SD-neutron}}-M_{\tilde{\chi}_1^0}$ plane in Fig. 6 (left) and (right), respectively. Here as well, a significant region of currently allowed parameter space points fall within the projected reach of Xenon-nT as well as PICO-250 while another considerable fraction remains out of reach. In Fig. 7 we again illustrate the currently allowed parameter space points in the $\xi\sigma_{\text{SI}}-M_{\tilde{\chi}_1^0}$ plane. The grey and orange points fall below the coherent neutrino scattering floor [they correspond to the orange colored points in Fig. 5 (right)] and will remain outside the projected coverage of any future σ_{SI} measurement experiment. The orange points, however, fall within the projected reach of Xenon-nT [119] and PICO-250 [118] via $\sigma_{\text{SD-neutron}}$ and $\sigma_{\text{SD-proton}}$ measurements, respectively. Thus, it can be observed from Fig. 7 that spin-dependent measurements can provide coverage of parameter space points which lie even below the coherent neutrino scattering floor in the $M_{\tilde{\chi}_1^0} \gtrsim 15$ GeV region.

B. Direct searches for the light Higgs bosons at LHC luminosity and energy upgrades

The projected sensitivity of HL-LHC and HE-LHC in probing light A_1 via direct searches in the $H_{125} \rightarrow A_1 A_1 / H_1 H_1 \rightarrow 2b2\mu$ channel has been discussed in [65], where the corresponding 95% C.L. projection contours on $\sigma_{H_{125}}/\sigma_{H_{\text{SM}}} \times \text{Br}(H_{125} \rightarrow A_1 A_1 / H_1 H_1 \rightarrow 2b2\mu)$ have also been derived, however, under the assumption that $\sigma_{H_{125}}/\sigma_{H_{\text{SM}}} = 1$. We have translated these projection limits on to the currently allowed NMSSM parameter space of our

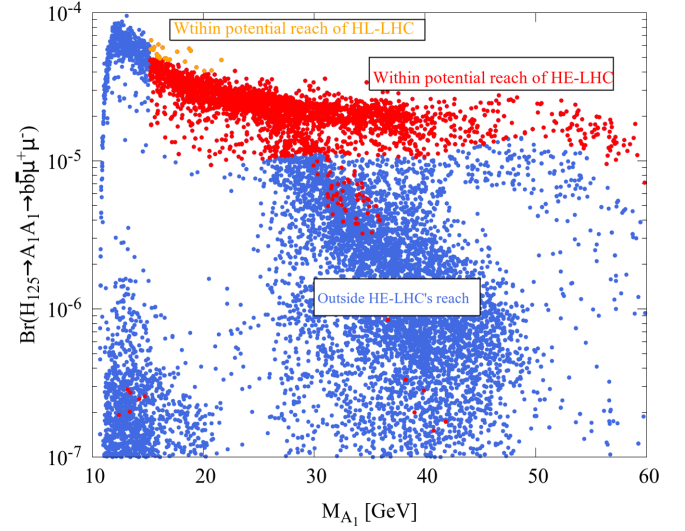


FIG. 8. The allowed parameter space points (allowed by all constraints listed in Sec. IV) are shown in the $\text{Br}(H_{125} \rightarrow A_1 A_1 \rightarrow 2b2\mu)-M_{A_1}$ plane. The orange and red colored points fall within the potential reach of direct light Higgs searches in the $H_{125} \rightarrow A_1 A_1 / H_1 H_1 \rightarrow 2b2\mu$ channel, at HL-LHC and HE-LHC [65], respectively. The blue colored points fall outside the projected reach of light Higgs searches in $2b2\mu$ channel at HE-LHC.

interest and the projected reach has been shown in Fig. 8, where, the horizontal and vertical axes represent M_{A_1} and $\text{Br}(H_{125} \rightarrow A_1 A_1 \rightarrow 2b2\mu)$, respectively. The orange colored points in Fig. 8 are within the projected reach of HL-LHC at 95% C.L. while the red colored points fall within the projected reach of HE-LHC at 95% C.L. The blue colored parameter space points would be undetectable at HE-LHC via direct light Higgs searches in the $2b2\mu$ final state. These projections show that the discovery potential of light Higgs bosons produced via direct decays of H_{125} is not very strong. Indeed no points are observable with 5σ sensitivity. We note though that we have made no attempt to optimize the analysis (which was based on an ATLAS analysis for $\sim 36 \text{ fb}^{-1}$) for either the increased luminosity or increased energy of the HE-LHC. Our conclusion should be viewed with caution.

Projected limits from direct light Higgs searches in the $2b2\mu$ channel, at the HL-LHC and the HE-LHC, has the potential to probe the $M_{A_1/H_1} \gtrsim 15$ GeV region (as shown in Fig. 8), however, it could be observed that a major region of the currently allowed parameter space lies outside its reach. It is to be noted that, along with light scalars and pseudoscalars, the particle spectrum of the parameter space under study also features light electro-weakinos. Therefore, the question that arises next is, whether it would be possible to probe the parameter space through direct electroweakino searches at the future colliders. The next section intends to provide a conservative answer to this question.

VII. FUTURE REACH OF DIRECT ELECTROWEAKINO SEARCHES AT HL- AND HE-LHC

The ATLAS Collaboration has made MSSM projections for the wino reach of the HL-LHC via trilepton searches $pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm$, assuming that $\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 + (W^\pm \rightarrow l^\pm \nu)$ ($l = e, \mu, \tau$ and $\nu = \nu_e, \nu_\mu, \nu_\tau$) and $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + (Z \rightarrow l^+ l^-)$ or $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + (H_{125} \rightarrow WW^* \rightarrow l^+ l^- + \nu\nu, H_{125} \rightarrow \tau^+ \tau^-)$ ⁵ [120,121]. Hereafter, we will refer to these as the WZ - and WH_{125} -mediated channels, respectively. In Sec. VII A, we perform our own analysis of the wino reach in the WZ -mediated channel, and compare our results with those in [121]. Our purpose in doing so is to assess how our “theorist’s computation” does, *vis a vis* the ATLAS analysis. We then project the reach for *doublet Higgsino production* via the WZ - as well as the WH_{125} -channels, assuming that these Higgsinos directly decay to a lighter LSP.⁶ This is, of course, not possible in the MSSM with our assumption of a heavy bino. We perform this analysis as a prelude to our goal of mapping out how well experiments at the HL-LHC will be able to probe the NMSSM parameter space with a light LSP even though this analysis covers a much larger range of masses for the LSP. In Sec. VII B, we translate the discovery projections (and exclusion reach) derived in Sec. VII A to the currently allowed NMSSM parameter space of interest. In Sec. VII C, we perform another collider study to obtain the discovery reach (and exclusion regions) of Higgsinos at the HE-LHC. These are then translated in Sec. VII D to the corresponding reach in the parameter space of the NMSSM.

A simplified model with degenerate Higgsino-like $\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm$, and binolike $\tilde{\chi}_1^0$ is considered while evaluating the HL-LHC and HE-LHC projections. Within the simplified framework, the relevant branching fractions: $\text{Br}(\tilde{\chi}_3^0/\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z)$ or $\text{Br}(\tilde{\chi}_3^0/\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 H_{125})$, and, $\text{Br}(\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 W^\pm)$, are assumed to be 100%. Note that in the NMSSM, this assumption remains valid for the lighter chargino but not for the heavier chargino or for neutralinos. Indeed the $\tilde{\chi}_2^0, \tilde{\chi}_3^0$ and $\tilde{\chi}_4^0$ are an admixture of the winos and Higgsinos while the LSP is a singlino resulting in variedly different values of the relevant branching fractions. Moreover, additional decay channels into light Higgses are possible. In order to translate the projected discovery/exclusion regions on to the NMSSM parameter space, we first map out the efficiency grid for the corresponding search strategy in the doublet-Higgsino LSP mass plane. Since this grid is determined largely by the kinematics, the details of the composition of the parent Higgsinos or the daughter

LSP are completely irrelevant: the efficiency grid is determined by the kinematics and the branching fractions of the parent Higgsinos to decay to the LSP and the associated boson (W, Z or H_{125}).

A. Direct electroweakino searches at HL-LHC

As stated previously, the aim of the present subsection is twofold: to derive the projected discovery reach and exclusion range for direct Higgsino searches ($pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm + \tilde{\chi}_3^0 \tilde{\chi}_1^\pm$) in the WZ mediated and WH_{125} mediated $3l + \cancel{E}_T$ final state at the HL-LHC, and, map out the efficiency grid for the WZ and WH_{125} -mediated channels that we will use to delineate the region of NMSSM parameter space that can be probed at the luminosity and energy upgrades of the LHC.

1. WZ -mediated $3l + \cancel{E}_T$ channel at HL-LHC

We begin by considering the trilepton signal produced via $pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm + \tilde{\chi}_3^0 \tilde{\chi}_1^\pm \rightarrow (\tilde{\chi}_3^0/\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z)(\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0)$. We assume that the W and Z bosons are close to their mass shell and focus on the trilepton $+\cancel{E}_T$ final state from their leptonic decays to electrons, muons and taus. We use PYTHIA-6 [122,123] to simulate the signal events for different values of $M_{\tilde{\chi}_1^0}$ and $M_{\tilde{\chi}_2^0 \tilde{\chi}_3^0 \tilde{\chi}_1^\pm}$ ($M_{\tilde{\chi}_1^0}$ is varied from 0–800 GeV with a step size of 30 GeV while $M_{\tilde{\chi}_2^0} (= M_{\tilde{\chi}_3^0} = M_{\tilde{\chi}_1^\pm})$ is varied from 100 GeV to 1300 GeV with a step size of 30 GeV, with an additional condition: $M_{\tilde{\chi}_2^0 \tilde{\chi}_3^0} - M_{\tilde{\chi}_1^0} > M_Z$, in order to ensure on-shell production of W and Z bosons.). The direct Higgsino production cross section ($\sigma_{pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm + \tilde{\chi}_3^0 \tilde{\chi}_1^\pm}$) has been computed at next to leading order (NLO) using Prospino [124–126], while the branching fraction of $\tilde{\chi}_2^0/\tilde{\chi}_3^0 \rightarrow Z\tilde{\chi}_1^0$ and $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$ has been considered to be 100%.

A signal event is required to have three isolated leptons ($l = e, \mu$) in the final state. The lepton isolation criteria requires the ratio: $p_T^{\text{charged}}/p_T^l$ to be ≤ 0.15 (for both electrons and muons), where, p_T^{charged} is the scalar sum of transverse momentum (p_T) of all charged particles with $p_T \geq 1.0$ GeV within a cone of radius $\Delta R = 0.3$ around the lepton momentum direction while p_T^l represents the transverse momentum of the lepton. Here, ΔR is defined as $\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$ with $\Delta\eta$ and $\Delta\phi$ representing the difference in pseudorapidity and azimuthal angle, respectively, between the charged particle and the lepton under consideration. Candidate leptons are required to have $p_T > 20$ GeV and must lie within a pseudorapidity range of $|\eta| < 2.5$. Two of the three final state leptons are required to form a same flavor opposite sign (SFOS) lepton pair with invariant mass (M_{ll}^{SFOS}) in the range $M_Z \pm 10$ GeV, where M_Z is the mass of the Z boson. In the presence of more than one pair of SFOS leptons with invariant mass in the above range, the SFOS pair which minimizes the transverse mass of the non-SFOS lepton and \cancel{E}_T is chosen to have its origin

⁵Here both taus decay leptonically.

⁶For direct Higgsino searches via the WH_{125} -mediated trilepton channel, we closely follow the analysis strategy of [120]. It may be possible to further optimize the analysis for the higher luminosity, and also the higher energy that may be available in the future.

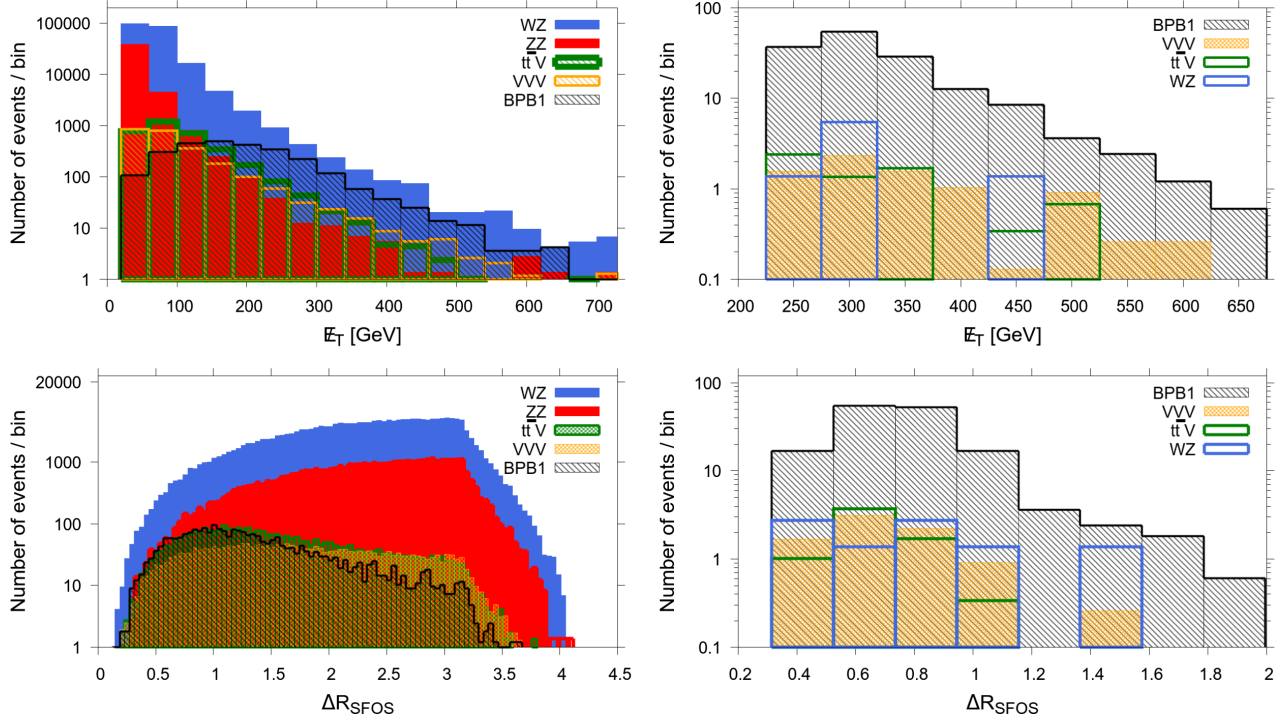


FIG. 9. The event distribution of \cancel{E}_T (top) and ΔR_{SFOS} (bottom) at the HL-LHC, for the signal benchmark point (BPB1: $M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm} = 310$ GeV, $M_{\tilde{\chi}_1^0} = 0$ GeV) and the relevant backgrounds are shown. The signal events have been illustrated in black color while on- and off-shell WZ , VVV , $t\bar{t}V$ and ZZ backgrounds have been shown in blue, orange, green and red colors, respectively. The left (right) panel shows the event distribution before (after) the application of SRB1 cuts.

in the decay of the Z boson, with the non-SFOS lepton coming from the decay of the W boson.

Standard model backgrounds to the WZ -mediated $3l + \cancel{E}_T$ final state mainly come from: on-shell and off-shell WZ , $t\bar{t}V$ ($V = W^\pm, Z$), triple vector boson (VVV) production and ZZ processes. The $t\bar{t}V$ and the ZZ samples have been produced by decaying $V (= W^\pm, Z)$ and the Z bosons, respectively, via leptonic decay modes. In the remaining sections of this work, the $t\bar{t}V$ and the ZZ backgrounds have always been generated in a similar way with the V and the Z bosons, respectively, decaying leptonically. The leading order (LO) MADGRAPH5_aMC@NLO cross section values for $t\bar{t}V$ and the ZZ process considered in this work accounts for the aforementioned decay channels. Events containing a b -tagged jet with $p_T > 30$ GeV and $|\eta| < 2.5$ are also rejected in order to suppress the $t\bar{t}V$ background.⁷ These background events have been generated using the MADGRAPH5_aMC@NLO [123,128] framework and for both, the signal as well as the background, detector effects are simulated using DELPHES-3.4.2 [129].

A cut based analysis is performed by considering 8 signal regions with different set of cuts on the following kinematic variables: $p_T^{l_1, l_2, l_3}$ (transverse momenta of the

three final state leptons with l_1 being the leading p_T lepton and l_3 being the lepton with the smallest p_T), \cancel{E}_T (missing transverse energy), M_T^W (transverse mass of the non-SFOS lepton (l_W) and \cancel{E}_T system), M_{CT}^W (contransverse mass [130] of the $l_W - \cancel{E}_T$ system), $\Delta\phi_{l_W \cancel{E}_T}$ (difference between azimuthal angles of l_W and \cancel{E}_T), $\Delta\phi_{\text{SFOS} - \cancel{E}_T}$ (difference between the azimuthal angles of the SFOS pair of leptons and \cancel{E}_T) and ΔR_{SFOS} ($\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$, where $\Delta\eta$ and $\Delta\phi$ are the differences in pseudorapidity and azimuthal angle, respectively, of the two leptons which constitute the SFOS pair). The 8 signal regions: SRA1, SRB1, SRC1, SRD1, SRE1, SRF1, SRG1 and SRH1, have been chosen by optimizing the signal significance for the following benchmark signal events [$M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm}, M_{\tilde{\chi}_1^0}$] (in GeV): BPA1 [130, 0], BPB1 [310, 0], BPC1 [310, 210], BPD1 [610, 0], BPE1 [610, 300], BPF1 [610, 510], BPG1 [1000, 0], BPH1 [1000, 420], respectively. Here, we have chosen benchmark points with small, intermediate and large mass difference between the NLSP and the LSP, for several choices of the NLSP mass.

As an illustration, in Fig. 9, we show the kinematic distribution of \cancel{E}_T and ΔR_{SFOS} for the signal benchmark point BPB1 (shown in black color) and the relevant backgrounds: on-shell and off-shell WZ (blue color), VVV (orange color), $t\bar{t}V$ (green color) and ZZ (red color), at the HL-LHC. The distributions shown in the left panel of

⁷A flat b -tagging efficiency of 70% has been used. The $c \rightarrow b$ and $u, d, s \rightarrow b$ mistag rates have been fixed at 30% and 1%, respectively [127].

TABLE I. List of selection cuts corresponding to the signal regions for WZ mediated $3l + \cancel{E}_T$ final state. The signal regions have been optimized to yield maximum signal significance for the signal samples corresponding to the respective benchmark points.

	Benchmark points							
	BPA1	BPB1	BPC1	BPD1	BPE1	BPF1	BPG1	BPH1
$M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm}$ [GeV]	130	310	310	610	610	610	1000	1000
$M_{\tilde{\chi}_1^0}$ [GeV]	30	0	210	0	300	510	0	420
Kinematic variables	Signal regions							
	SRA1	SRB1	SRC1	SRD1	SRE1	SRF1	SRG1	SRH1
$\Delta\Phi_{lW\cancel{E}_T}$	≤ 0.2	...	≤ 1.5
$\Delta\Phi_{\text{SFOS}-\cancel{E}_T}$...	$[2.7:\pi]$	$[1.8:\pi]$	$[1.5:\pi]$	$[1.8:\pi]$...	$[1.6:\pi]$	$[1.5:\pi]$
ΔR_{SFOS}	$[1.4:3.8]$	$[0.3:2.1]$...	$[0.1:1.3]$	$[0.1:1.3]$	$[1.6:4.0]$	$[0.1:1.0]$	$[0.1:1.3]$
\cancel{E}_T [GeV]	$[50:290]$	≥ 220	$[100:380]$	≥ 200	≥ 250	...	≥ 200	≥ 200
M_T^{lw} [GeV]	...	≥ 100	$[100:225]$	≥ 300	≥ 150	$[150:350]$	≥ 150	≥ 200
M_{CT}^{lw} [GeV]	...	≥ 100	...	≥ 100	≥ 150	$[100:400]$	≥ 200	≥ 200
p_T^1 [GeV]	$[50:150]$	≥ 120	$[60:110]$	≥ 150	≥ 150	$[60:150]$	≥ 210	≥ 200
p_T^2 [GeV]	$[50:110]$	≥ 60	≥ 30	≥ 100	≥ 100	$[50:80]$	≥ 150	≥ 100
p_T^3 [GeV]	≥ 30	≥ 30	≥ 30	≥ 50	≥ 50	$[30:60]$	≥ 50	≥ 50

Fig. 9 have been obtained by imposing the following conditions on the generated event samples: presence of only three isolated leptons in the final state, presence of at least one SFOS pair with invariant mass in the range of $M_Z \pm 10$ GeV, and b jet veto. The \cancel{E}_T distribution of BPB1 peaks roughly at 150 GeV while the \cancel{E}_T distribution for the WZ , VVV , $t\bar{t}V$ and ZZ backgrounds peaks roughly below $\lesssim 50$ GeV. Due to the large mass gap between $\tilde{\chi}_3^0/\tilde{\chi}_2^0$ and $\tilde{\chi}_1^0$ in BPB1, the Z boson produced from the cascade decay of $\tilde{\chi}_3^0/\tilde{\chi}_2^0$ carries a relatively larger boost causing the ΔR_{SFOS} distribution of BPB1 to peak at smaller values. The SFOS lepton pairs for the background events are however, produced with relatively larger angular separation. The same is reflected in the ΔR_{SFOS} distribution of BPB1 and the background events shown in the lower left panel of Fig. 9.

We optimize the signal significance of the 8 benchmark points by applying various combination of selection cuts. The signal significance is computed as:

$$S_\sigma = \frac{S}{\sqrt{B + (\text{sys_un} * B)^2}} \quad (17)$$

where, S and B represents the signal and background yields, respectively, while sys_un corresponds to the systematic uncertainty taken to be 5%. The selection cuts corresponding to the 8 signal regions, obtained from the cut-based analysis, have been listed in Table I. The figures on the right panel of Fig. 9 have been obtained on further imposing the selection cuts labeled SRB1.

The efficiency grids for SRB1, SRC1, SRE1 and SRG1 are illustrated in the four panels of Fig. 10 where the

efficiency values are shown as a color palette in the $M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane. The efficiency (Eff.) of a signal region for a particular signal point is computed by taking the ratio of the number of signal events which pass through the signal region selection cuts to the total number of generated signal events. We note that SRB1, SRD1 and SRG1 cuts were particularly optimized to maximize the signal significance of signal processes with larger mass difference between the directly produced doublet Higgsinos and the LSP (BPB1, BPD1 and BPG1, respectively), while SRA1, SRC1 and SRF1 were optimized to maximize the signal significance of such signal events where the mass difference between the directly produced Higgsinos and the LSP was just above the Z mass threshold (BPA1, BPC1 and BPF1, respectively). On the other hand, SRE1 and SRH1 were optimized for signal process with intermediate mass difference between the NLSP Higgsinos and the LSP (BPE1 and BPH1, respectively).

The signal yield is computed as $S = \sigma_{\tilde{\chi}_2^0, \tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^\pm} + \sigma_{\tilde{\chi}_3^0, \tilde{\chi}_1^\pm} \times \text{Br}(\tilde{\chi}_2^0, \tilde{\chi}_3^0 \rightarrow Z\tilde{\chi}_1^0) \times \text{Br}(\tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0) \times \text{Br}(Z \rightarrow l'l') \times \text{Br}(W \rightarrow l'\nu) \times \text{Eff.} \times \mathcal{L}$, where \mathcal{L} corresponds to the integrated luminosity (3000 fb^{-1} for HL-LHC) and $l' = e, \mu, \tau$. The values of $\text{Br}(\tilde{\chi}_2^0, \tilde{\chi}_3^0 \rightarrow Z\tilde{\chi}_1^0)$ and $\text{Br}(\tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0)$ are assumed to be 100%, while SM values for $\text{Br}(Z \rightarrow l'l')$ and $\text{Br}(W \rightarrow l'\nu)$ are considered. Similarly, in the calculation of background yields, the leading order (LO) cross section computed by MADGRAPH5_aMC@NLO are considered. The background yields for WZ , $t\bar{t}V$, VVV and ZZ processes, corresponding to the 8 different signal regions, are listed in Table II. The leading order cross section labeled WZ refers to the tree-level cross section for $l\nu ll$ production from MADGRAPH5_aMC@NLO with generator-level

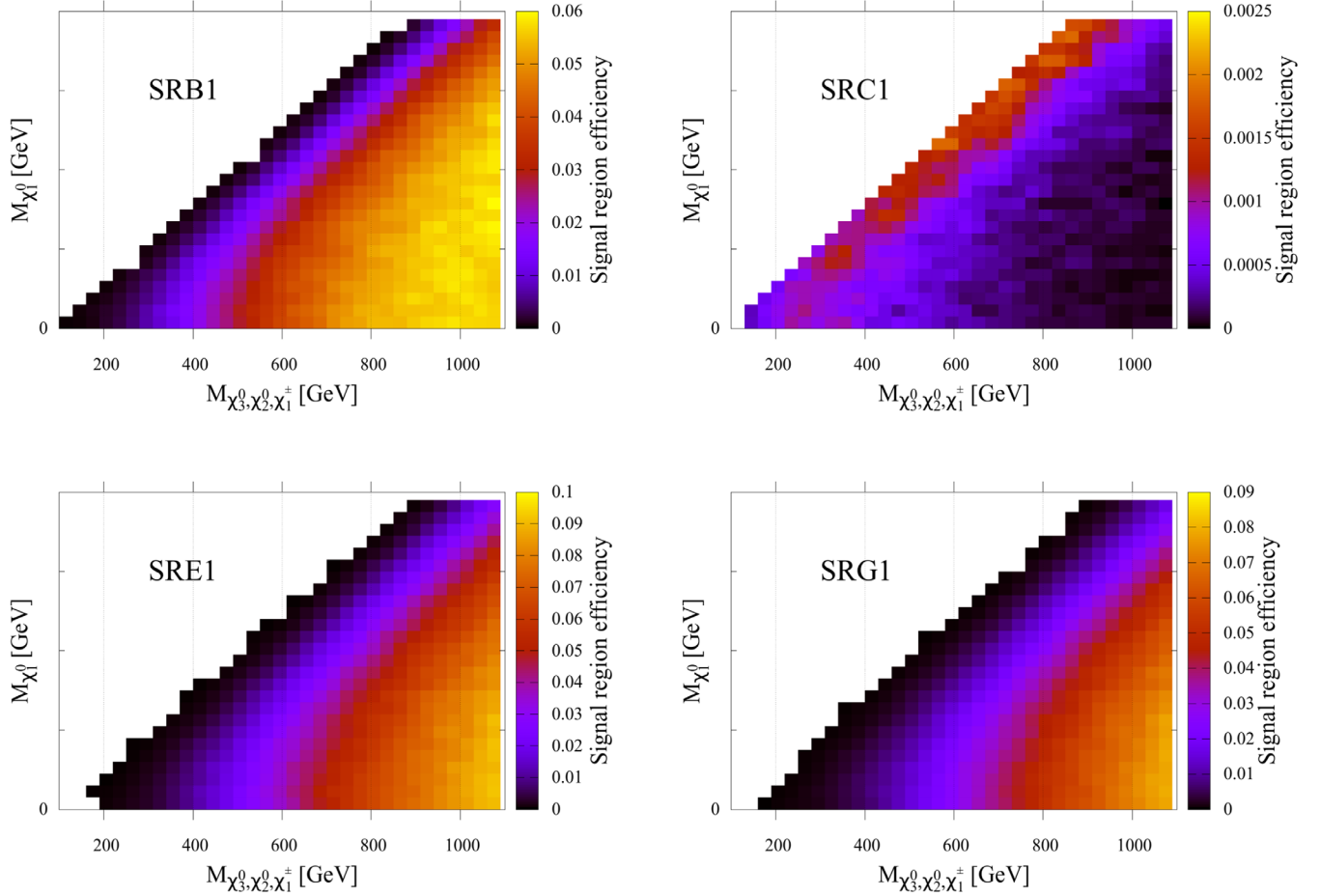


FIG. 10. Efficiency map for the WZ -mediated $3l + \cancel{E}_T$ signal from Higgsino pair production at the HL-LHC with the SRB1 cuts (top left), SRC1 cuts (top right), SRE1 cuts (bottom left) and SRG1 cuts (bottom right) in the $M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane. Note that the z-axis scale for SRC1 is different from the other three frames.

cuts $p_T > 5$ GeV and $|\eta| < 3.5$ on the leptons. These include contributions from *off-shell* W , Z and γ amplitudes.⁸ The off-shell W contributions are crucial for obtaining a reliable estimate of the background remaining after a hard cut on the transverse mass M_T^{lw} , which is very efficient in reducing the background where the W boson is close to its mass shell.

As we have already mentioned, the ATLAS collaboration has also derived the projected exclusion and discovery contours at 95% C.L. from direct wino searches in the WZ mediated $3l + \cancel{E}_T$ searches at the HL-LHC (see Fig. 9 from [121]). In order to check the consistency of our analysis setup, we rederive the projection contours for direct wino searches in the WZ mediated $3l + \cancel{E}_T$ final state at the HL-LHC by using the signal regions: SRA1—SRH1, which were obtained through optimization of the signal significances for BPA1-BPH1, respectively. The corresponding projection contours derived by using our analysis setup are

⁸In the remainder of this article, WZ background will refer to $l\nu ll$ production process with the aforesaid generator level cuts and will include contribution from off-shell W , Z and γ amplitudes.

illustrated in Fig. 11, in the $M_{\tilde{\chi}_2^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ mass plane. The projection contours in Fig. 11 display a potential to discover (exclude) a winolike $\tilde{\chi}_1^\pm, \tilde{\chi}_2^0$ up to a mass of $\sim 960(1150)$ GeV for a massless LSP. This is comparable to the corresponding projections of ATLAS which are respectively $\sim 950(1110)$ GeV. Our discovery (exclusion) projections degrade by less than $\sim 50(100)$ GeV for LSP masses up to 400 (600) GeV. Next, we move on to derive the projected reach of direct doublet Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final state at the HL-LHC.

The projected exclusion and discovery contours from direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final state at HL-LHC are illustrated in Fig. 12 with the same color code as Fig. 11. While deriving the HL-LHC projections, we compute the value of signal significance at a grid point for all 8 signal regions and the maximum among them is ascribed to S_σ . We conclude that HL-LHC will be capable of discovering (excluding) pure doublet Higgsinos up to 820 (1000) GeV for a massless binolike $\tilde{\chi}_1^0$ through direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final state.

TABLE II. The background yields for $\sqrt{s} = 14$ TeV LHC corresponding to 3 ab^{-1} of integrated luminosity, for the 8 different signal regions considered for the cut-based analysis, are tabulated. The leading order (LO) cross sections generated by MADGRAPH5_AMC@NLO are also shown. The $t\bar{t}V$ background has been generated with V decaying leptonically while the generic sample of triple vector boson production has been used in the analysis.

Background process	LO cross section	Background yield (14 TeV, 3 ab^{-1})							
		SRA1	SRB1	SRC1	SRD1	SRE1	SRF1	SRG1	SRH1
WZ	686 fb	407	9.60	12.3	5.49	4.12	9.60	5.49	6.86
$t\bar{t}V$ ($V = W, Z$) ($W \rightarrow l\nu, Z \rightarrow ll$)	343 fb	18.2	6.86	5.48	3.09	3.43	0.69	3.43	2.34
VVV ($V = W, Z$)	261 fb	13.6	8.22	2.22	2.48	3.00	1.57	2.48	2.22
ZZ (leptonic)	926 fb	62.5	0.0	1.4	0.0	0.0	1.4	0.0	0.0
Total Background		502	24.7	21.4	11.0	10.5	13.2	11.4	11.5

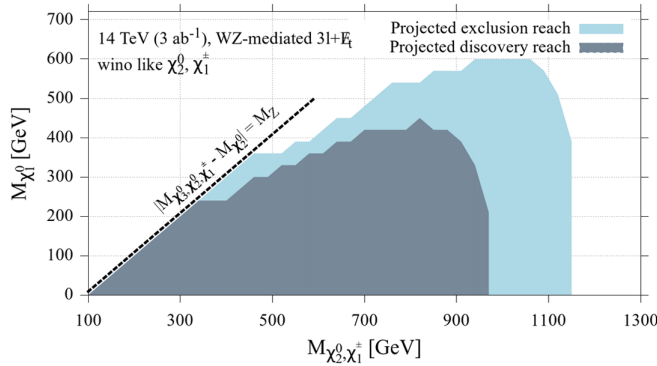


FIG. 11. The projected exclusion ($> 2\sigma$, light blue) and discovery ($> 5\sigma$, grey) contours in the $M_{\tilde{\chi}_2^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane, derived from direct wino searches ($pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm$) in the WZ mediated $3l + \cancel{E}_T$ search channel, in the context of future HL-LHC. The projection contours shown here are comparable with the future projections from ATLAS [121].

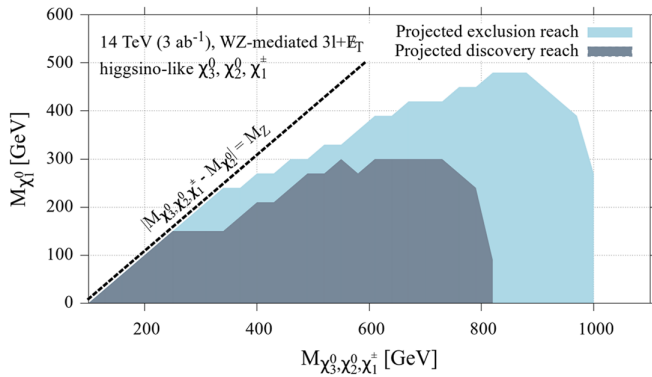


FIG. 12. The projected exclusion ($> 2\sigma$, light blue color) and discovery ($> 5\sigma$, grey color) contours in the $M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane, derived from direct Higgsino searches ($pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm + \tilde{\chi}_3^0 \tilde{\chi}_1^\pm$) in the WZ mediated $3l + \cancel{E}_T$ search channel, in the context of future HL-LHC.

2. WH_{125} -mediated $3l + \cancel{E}_T$ at HL-LHC

The two important decay modes of H_{125} which contribute to the $3l + \cancel{E}_T$ final state produced from WH_{125} mediated processes are: $H_{125} \rightarrow WW^* \rightarrow l'\nu l'\nu$ and $H_{125} \rightarrow \tau^+ \tau^-$. Contributions from both have been considered in the present analysis. The signal decay chain proceeds as $pp \rightarrow \tilde{\chi}_2^0 / \tilde{\chi}_3^0 + \tilde{\chi}_1^\pm \rightarrow (\tilde{\chi}_2^0, \tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 H_{125}) \times (\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 (W \rightarrow l'\nu))$. The signal samples have been generated for different values of $M_{\tilde{\chi}_1^0}$ (varied from 0–800 GeV, with a step size of 30 GeV) and $M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm}$ (varied from 100 GeV to 1300 GeV with a step size of 30 GeV), with the condition, $M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0} - M_{\tilde{\chi}_1^0} > 125$ GeV, in order to ensure on-shell production of the H_{125} . Here, $\text{Br}(\tilde{\chi}_2^0, \tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 + H_{125})$ and $\text{Br}(\tilde{\chi}_1^\pm \rightarrow W^\pm + \tilde{\chi}_1^0)$ are assumed to be 100%, while the SM values of $\text{Br}(H_{125} \rightarrow WW^*)$ and $\text{Br}(W \rightarrow l'\nu)$ have been used. The important sources of background are: on-shell and off-shell WZ and WH_{125} , VVV ($V = W, Z$), $t\bar{t}V$ and ZZ.

An event is required to have exactly three isolated leptons ($l = e, \mu$) with $p_T > 10$ GeV and must lie within a pseudorapidity range of $|\eta| < 2.47$ (for electrons) and $|\eta| < 2.4$ (for muons). The lepton isolation criteria requires the ratio $p_T^{\text{charged}} / p_T^l$ to be ≤ 0.15 for both, e and μ , with p_T^{charged} being the sum of transverse momenta of all charged particles with $p_T > 1$ GeV within a cone of radius $\Delta R = 0.3$.⁹ Events containing a SFOS pair of leptons with invariant mass in the range $M_Z \pm 12$ GeV are rejected in order to suppress the on-shell WZ background. Events containing a b tagged jet with $p_T > 20$ GeV and $|\eta| < 2.5$ are also rejected in order to suppress the $t\bar{t}V$ background. We choose four optimized signal regions: SRA2, SRB2, SRC2 and SRD2, with different set of cuts on \cancel{E}_T , $M_T^{l_1, l_2, l_3}$

⁹Here, we have followed the lepton isolation criteria considered in [120].

TABLE III. List of selection cuts corresponding to the signal regions for WH_{125} -mediated $3l + \cancel{E}_T$ final state. The choice of signal regions is motivated by a similar analysis in [120].

Kinematic variables	Signal regions			
	SRA2	SRB2	SRC2	SRD2
$M_{\text{OS,min}}^{\text{inv}}$ [GeV]			<75	
\cancel{E}_T [GeV]			>100	
M_T^1 [GeV]	≥ 200	≥ 200	≥ 300	≥ 400
M_T^2 [GeV]	≥ 100	≥ 150	≥ 200	≥ 150
M_T^3 [GeV]	≥ 100	≥ 100	≥ 150	≥ 100

and $M_{\text{OS,min}}^{\text{inv}}$. Here, M_T^i ($i = 1, 2, 3$) corresponds to the transverse mass of the i^{th} lepton and \cancel{E}_T system, while $M_{\text{OS,min}}^{\text{inv}}$ is the invariant mass of the opposite sign (OS) lepton pair with minimum ΔR separation. The choice of signal regions is motivated by a similar analysis in [120] which probes the future prospect of direct wino searches at the HL-LHC. The list of selection cuts for the four optimized signal regions have been listed in Table III.

The background yields corresponding to the four signal regions are shown in Table IV along with the LO MADGRAPH5_aMC@NLO cross section values. The background estimates for WZ , WH_{125} , $t\bar{t}V$, VVV and ZZ have been obtained by passing the simulated background samples through the signal region cuts. The tree-level cross section for WH_{125} has been computed using MADGRAPH5_aMC@NLO with generator level cuts: $p_T > 5$ GeV and $|\eta| < 3.5$ on the leptons and includes contribution from off-shell W amplitudes.¹⁰ In order to correctly estimate the background yield, it is essential to consider the contribution from off-shell W due to the hard cuts on M_T^i ($i = 1, 2, 3$). The two final states of H_{125} from the WH_{125} background process which dominantly contributes to the $3l + \cancel{E}_T$ signal are $H_{125} \rightarrow WW^* \rightarrow l'\nu_{l'}l\nu_{l'}$ and $H_{125} \rightarrow \tau^+\tau^-$. We generate these two final states separately.

We should mention that the ATLAS study [120] reports a substantial background from inclusive $t\bar{t}$ production tripling (doubling) the background in the signal region SRA2 (SRB2) but with not very significant contributions in the SRC2 and SRD2 signal regions. We anticipate that $t\bar{t}W$, $W \rightarrow l\nu$ and both tops decaying leptonically is the dominant physics source of *isolated* tripletons from $t\bar{t}$ production. The tripleton topology can also result if a lepton from the semileptonic decay of one of the bottom quarks is accidentally isolated, or if one of jets is misidentified as an lepton. Evaluation of these detector-dependent backgrounds is beyond the scope of our study, but we mention it for completeness. We have been unable

¹⁰Henceforth, the WH_{125} background process will refer to the off-shell and on-shell WH_{125} production process generated with the aforesaid generator level cuts.

TABLE IV. The background yields for $\sqrt{s} = 14$ TeV LHC corresponding to 3 ab^{-1} of integrated luminosity, for the 4 different signal regions considered for the cut-based analysis, are tabulated. The leading order (LO) cross sections generated by MADGRAPH5_aMC@NLO are also shown. The $t\bar{t}V$ background has been generated by decaying V through leptonic decay modes while the VVV sample is allowed to decay through all possible decay modes.

Background process	Cross section [LO]	Background yield (14 TeV, 3 ab^{-1})			
		SRA2	SRB2	SRC2	SRD2
WZ	686 fb	130	97.4	57.6	34.3
$t\bar{t}V$ ($V = W, Z$) ($W \rightarrow l\nu, Z \rightarrow ll$)	343 fb	12.3	4.73	1.64	0.82
VVV ($V = W, Z$)	261 fb	7.7	3.00	1.43	0.52
ZZ (leptonic)	834 fb	6.95	6.95	2.78	2.78
WH_{125} ($H_{125} \rightarrow \tau^+\tau^-$)	14.2 fb	0.11	0.11	10^{-2}	0.0
WH_{125} $H_{125} \rightarrow (W \rightarrow l\nu)$ $\times (W^* \rightarrow l\nu)$	0.14 fb	10^{-2}	10^{-2}	10^{-3}	10^{-3}
Total background		157	112	63.5	38.4

to ascertain the origin of the large background reported in Ref. [120] and do not include it in the rest of our analysis (except where we mention it in our discussion of Fig. 14 below). The efficiency maps of SRA2, SRB2, SRC2 and SRD2 for the $W(H_{125} \rightarrow WW^* \rightarrow l'\nu_{l'}l\nu_{l'})$ mediated $3l + \cancel{E}_T$ final state are shown in Fig. 13.

The projected exclusion contour for direct Higgsino searches in the $3l + \cancel{E}_T$ final state is illustrated in light blue color in Fig. 14. The contribution from $W(H_{125} \rightarrow WW^* \rightarrow l\nu_{l'})$ mediated and $W(H_{125} \rightarrow \tau^+\tau^-)$ mediated $3l + \cancel{E}_T$ signal processes have been added together in order to compute the signal yield. The signal significance for all four signal regions is computed, and the maximum among them is considered in the derivation of the projection contours shown in Fig. 14. Furthermore, we do not consider any systematic uncertainty in the current analysis since we do not perform the signal-background optimization of our own and use the signal region cuts from [120]. Our results indicate that the searches in the WH_{125} mediated $3l + \cancel{E}_T$ final state has the potential to discover (exclude) Higgsinos up to 400(590) GeV for a massless $\tilde{\chi}_1^0$. We mentioned previously that the signal regions SRA2, SRB2, SRC2 and SRD2 were motivated from Ref. [120] which probes the future reach of direct wino searches at the HL-LHC. We remark that if we include the $t\bar{t}$ background yields corresponding to the afore-mentioned signal regions from Ref. [120] (this double counts the $t\bar{t}W$ background), the projected discovery (exclusion) reach shown by the solid

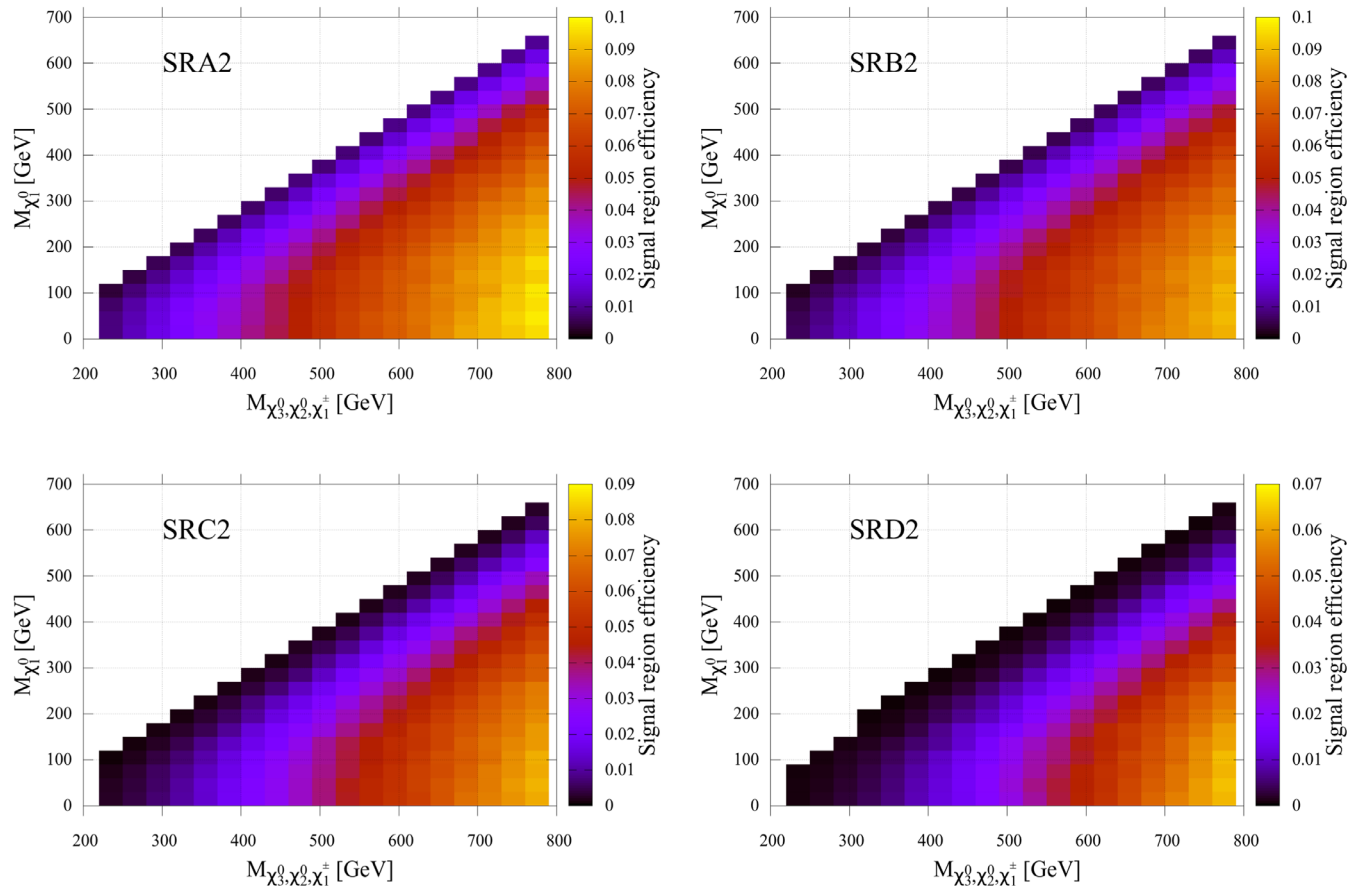


FIG. 13. Efficiency map of SRA2 (top left), SRB2 (top right), SRC2 (bottom left) and SRD2 (bottom right) signal regions, from searches in the $W(H_{125} \rightarrow WW^* \rightarrow l'\nu l'\nu)$ mediated $3l + \cancel{E}_T$ final state.

orange (blue-dashed) line for direct Higgsino searches via the WH_{125} mediated trilepton channel is altered to 375 (600) GeV. Note that the final projections are not very sensitive to our treatment of the top background.

The goal of the next section (Sec. VII B) is to translate the projected exclusion and discovery projections for HL-LHC derived from direct Higgsino searches in the WZ mediated and WH_{125} mediated $3l + \cancel{E}_T$ final state

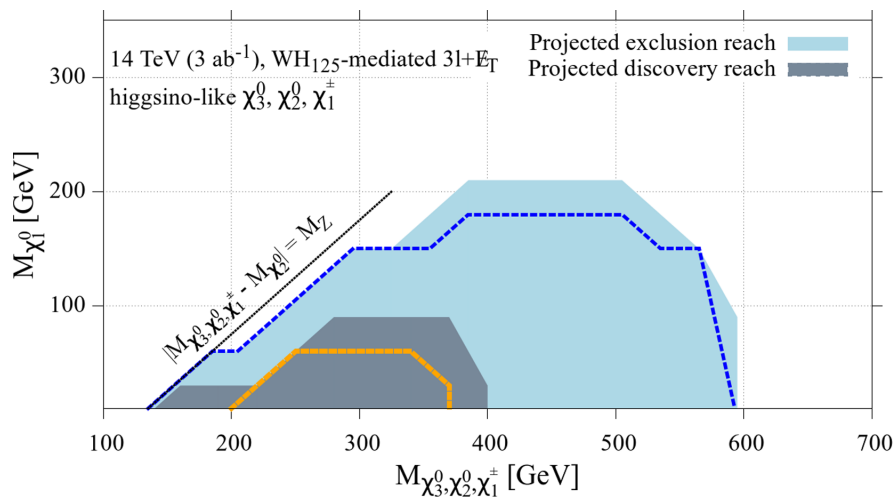


FIG. 14. The projected exclusion (2σ , blue color) contour and discovery (5σ , grey color) in the $M_{\chi_3^0, \chi_2^0, \chi_1^\pm} - M_{\chi_1^0}$ plane, derived from direct search of mass degenerate Higgsinos ($pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm + \tilde{\chi}_3^0 \tilde{\chi}_1^\pm$) in the WH_{125} mediated $3l + \cancel{E}_T$ search channel at the HL-LHC. The blue dashed and orange dashed lines illustrate the 2σ and 5σ exclusion regions upon including the ATLAS $\tilde{t}\tilde{t}$ background mentioned in the text.

(derived in Sec. VII A) on to the parameter space under study.

B. Impact of projected electroweakino search limits from HL-LHC

Because we have set the bino mass parameter to be 2 TeV, $\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$ as well as $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^\pm$ are either doublet Higgsino-like, winolike or a wino-Higgsino admixture. In the present scenario, the direct chargino-neutralino pair production modes which could potentially lead to WZ or WH_{125} mediated $3l + \cancel{E}_T$ final state are: $\tilde{\chi}_2^0\tilde{\chi}_1^\pm, \tilde{\chi}_3^0\tilde{\chi}_2^\pm, \tilde{\chi}_4^0\tilde{\chi}_1^\pm, \tilde{\chi}_3^0\tilde{\chi}_1^\pm, \tilde{\chi}_3^0\tilde{\chi}_2^\pm, \tilde{\chi}_4^0\tilde{\chi}_1^\pm$ and $\tilde{\chi}_4^0\tilde{\chi}_2^\pm$. The direct production cross section for each of these chargino-neutralino pairs is computed by scaling the pure Higgsino production cross section (computed at NLO using *Prospino*) with the respective reduced squared $W\tilde{\chi}_i^0\tilde{\chi}_j^\pm$ couplings. The reduced squared couplings have the following form:

$$C_{W\tilde{\chi}_i^0\tilde{\chi}_j^\pm}^2 = \{(N_{i3}V_{j2} - N_{i2}V_{j1}\sqrt{2})^2 + (N_{i4}U_{j2} + N_{i2}U_{j1}\sqrt{2})^2\} \quad (18)$$

where V, U are the chargino mixing matrices. V_{j1}/U_{j1} and V_{j2}/U_{j2} represents the wino and Higgsino component, respectively, in the j th chargino. N_{i2} represents the wino admixture while $N_{i3/i4}$ corresponds to the Higgsino admixture in the i th neutralino. In the case of direct production of a $\tilde{\chi}_i^0\tilde{\chi}_j^\pm$ pair where $\tilde{\chi}_i^0$ and the two chiral components of $\tilde{\chi}_j^\pm$ have dominant wino composition, $N_{i3}^2 + N_{i4}^2, V_{j2}^2$ and U_{j2}^2 will be $\ll 1$, while N_{i2}^2, V_{j1}^2 and U_{j1}^2 will be ~ 1 . Similarly, in the case of direct production of Higgsino-like chargino-neutralino pair, $N_{i3}^2 + N_{i4}^2, V_{j2}^2$ and U_{j2}^2 will be ~ 1 , while the other three components will be negligible. From Eq. (18), it can also be observed that the direct wino production cross section is roughly twice the direct Higgsino production cross section at the LO. However, the arguments of the simplified scenario will not hold for our allowed parameter space points since the neutralinos and charginos are an admixture of both winos and Higgsinos. Thereby, all terms in Eq. (18) could be non-negligible (depending upon the electroweakino mixing structure) and contribute toward the computation of the scaled production cross section. The production cross sections obtained are multiplied by the relevant branching fractions needed to obtain the $3l + \cancel{E}_T$ final state. The next step involves the computation of signal yield for all the optimized signal regions. For the WZ mediated $3l + \cancel{E}_T$ final state we compute the signal yields for all 8 signal regions, SRA1, SRB1, SRC1, SRD1, SRE1, SRF1, SRG1 and SRH1 prescribed in Sec. VII A 1 while for the WH_{125} mediated search we use the four regions SRA2, SRB2, SRC2 and SRD2. The only ingredient left in the computation of the signal yield is the efficiency of the particular signal region, where efficiency is defined as the ratio of the

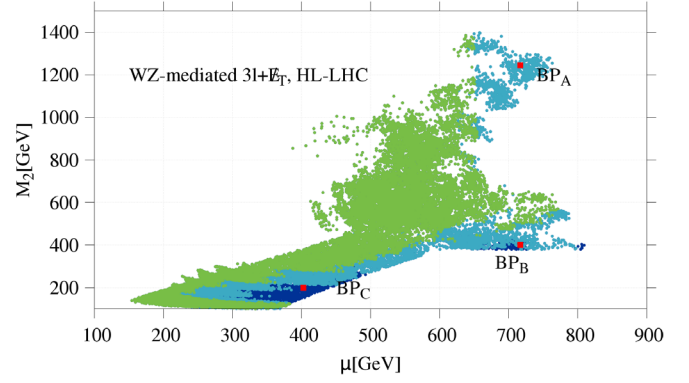


FIG. 15. The currently allowed parameter space points are shown in the μ - M_2 plane. The pale blue colored (green colored) points fall within the projected exclusion reach (discovery reach) of direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ channel at the HL-LHC. The dark blue colored points fall outside HL-LHC's projected reach. The representative benchmark points: BP_A ($\mu \sim 717$ GeV, $M_2 \sim 1244$ GeV), BP_B ($\mu \sim 717$ GeV, $M_2 \sim 400$ GeV) and BP_C ($\mu \sim 403$ GeV, $M_2 \sim 200$ GeV), are also shown in this figure.

number of events which are allowed by the selection cuts of a particular signal region to the total number of generated events. The efficiency is a function of the masses of $\tilde{\chi}_4^0/\tilde{\chi}_3^0/\tilde{\chi}_2^0/\tilde{\chi}_1^\pm/\tilde{\chi}_1^0$ and $\tilde{\chi}_1^\pm$, and, is extracted from the signal region efficiency maps, some of which are shown in Fig. 10 (for WZ mediated $3l + \cancel{E}_T$ searches) and Fig. 13 (for WH_{125} mediated $3l + \cancel{E}_T$ searches). The signal significance is then computed using Eq. (17) by adopting the signal region that yields the highest value of S_σ . Parameter space points which generate a signal significance >2 (>5) are considered to be within the projected exclusion (discovery) reach of HL-LHC.

The points shown in Fig. 15 correspond to the allowed parameter space points obtained after imposing all constraints specified in Sec. IV, see also Fig. 1. The parameter space points which fall within (outside) the projected exclusion reach of direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final state at HL-LHC are shown in pale blue (dark blue) color in Fig. 15, while the green colored points fall within the projected discovery reach.

Whether or not the signal is observable is the result of an intricate interplay between the production cross sections, determined by the doublet Higgsino and wino masses, and the signal efficiencies shown in Fig. 10. In the green region with $\mu \sim M_2 \sim 500$ GeV, the efficiencies in Fig. 10 are relatively large (the red/orange region) for small values of $M_{\tilde{\chi}_1^0}$, and doublet Higgsinos and gauginos are both in the kinematically accessible range, contributing to the WZ mediated tripleton signal. For larger values of μ and M_2 , though the efficiency increases, the production cross section becomes smaller and the signal is kinematically suppressed. For smaller values of M_2 and μ , though the production cross section remains large, the efficiency

TABLE V. The masses, wino and Higgsino fractions of neutralinos and charginos, neutralino-chargino production cross sections, branching ratios for neutralinos and signal significance for BP_A . The input parameters of BP_A are tabulated in Appendix. The HE-LHC projections and their translation on to the allowed parameter space has been studied in Sec. VII C.

BP_A	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$	$\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^\pm$
Mass [GeV]	58.3	723	732	1300	723	1300
Wino %	10^{-4}	0.01	10^{-4}	0.99	0.01	0.99
Higgsino %	10^{-4}	0.98	0.99	0.01	0.99	0.01
Singlino fraction in $\tilde{\chi}_1^0$: 0.99				$M_{H_1} = 83.7$ GeV, $M_{A_1} = 34.5$ GeV		
Cross-section (fb)	$\tilde{\chi}_2^0\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^0\tilde{\chi}_2^\pm$	$\tilde{\chi}_3^0\tilde{\chi}_1^\pm$	$\tilde{\chi}_3^0\tilde{\chi}_2^\pm$	$\tilde{\chi}_4^0\tilde{\chi}_1^\pm$	$\tilde{\chi}_4^0\tilde{\chi}_2^\pm$
$\sqrt{s} = 14$ TeV	2.4	5×10^{-3}	2.3	4×10^{-3}	5×10^{-3}	0.3
$\sqrt{s} = 27$ TeV	11.8	0.03	11.1	0.03	0.03	3.7
Branching ratio	$\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.50), $\tilde{\chi}_1^0 H_{125}$ (0.43), $\tilde{\chi}_1^0 H_1$ (0.07) $\tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.49), $\tilde{\chi}_1^0 H_{125}$ (0.44), $\tilde{\chi}_1^0 H_1$ (0.06) $\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_2^0 H_{125}$ (0.22), $\tilde{\chi}_2^0 Z$ (0.01), $\tilde{\chi}_1^\pm W^\mp$ (0.51), $\tilde{\chi}_3^0 Z$ (0.24)					
Significance at HL-LHC: WZ mediated $3l + \cancel{E}_T$: 3.8, WH_{125} mediated $3l + \cancel{E}_T$: 0.4						
Significance at HE-LHC: WZ mediated $3l + \cancel{E}_T$: 14, WH_{125} mediated $3l + \cancel{E}_T$: 6.6						

TABLE VI. The masses, wino and Higgsino fractions of neutralinos and charginos, neutralino-chargino production cross sections, branching ratios for neutralinos and signal significance for BP_B . The input parameters of BP_B are tabulated in Appendix.

	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$	$\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^\pm$
Mass [GeV]	60.4	421	734	742	421	741
Wino %	10^{-5}	0.96	2×10^{-3}	0.04	0.94	0.06
Higgsino %	10^{-4}	0.04	0.99	0.96	0.06	0.94
Singlino fraction in $\tilde{\chi}_1^0$: 0.99				$M_{H_1} = 97.2$ GeV, $M_{A_1} = 99$ GeV		
Cross-section (fb)	$\tilde{\chi}_2^0\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^0\tilde{\chi}_2^\pm$	$\tilde{\chi}_3^0\tilde{\chi}_1^\pm$	$\tilde{\chi}_3^0\tilde{\chi}_2^\pm$	$\tilde{\chi}_4^0\tilde{\chi}_1^\pm$	$\tilde{\chi}_4^0\tilde{\chi}_2^\pm$
$\sqrt{s} = 14$ TeV	104	0.27	0.28	2.1	0.25	2.3
$\sqrt{s} = 27$ TeV	363	1.1	1.1	10.2	1.0	11.2
Branching ratio	$\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.04), $\tilde{\chi}_1^0 H_{125}$ (0.82), $\tilde{\chi}_1^0 H_1$ (0.14) $\tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.13), $\tilde{\chi}_1^0 H_{125}$ (0.10), $\tilde{\chi}_1^0 H_1$ (0.01), $\tilde{\chi}_1^\pm W^\mp$ (0.51), $\tilde{\chi}_2^0 Z$ (0.23), $\tilde{\chi}_2^0 H_{125}$ (0.01) $\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.12), $\tilde{\chi}_1^0 H_{125}$ (0.11), $\tilde{\chi}_1^\pm W^\mp$ (0.53) $\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_2^0 Z$ (0.02), $\tilde{\chi}_2^0 H_{125}$ (0.21)					
Significance at HL-LHC: WZ mediated $3l + \cancel{E}_T$: 1.5, WH_{125} mediated $3l + \cancel{E}_T$: 5.3						
Significance at HE-LHC: WZ mediated $3l + \cancel{E}_T$: 4.4, WH_{125} mediated $3l + \cancel{E}_T$: 34						

reduces except for SRA1/SRB1 type cuts, for which efficiencies are small.¹¹ We observe a dark blue colored protrusion region in the $M_2 \sim 150$ GeV region from $\mu \sim 300$ GeV to $\mu \sim 400$ GeV. The signal significance of the majority of the points in this region is marginally less than 2σ on account of the relatively smaller efficiency from SRB1.

In order to understand the underlying features, we chose two benchmark points, BP_A ($\mu \sim 717$ GeV, $M_2 \sim 1244$ GeV) and BP_B ($\mu \sim 717$ GeV, $M_2 \sim 400$ GeV), from the allowed parameter space. The masses and the composition of

¹¹Note that the scale is different in the efficiency maps of SRB1, SRC1, SRE1 and SRG1 in Fig. 10.

$\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0, \tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^{\pm 12}$ for BP_A and BP_B are shown in Table V and Table VI, respectively. Furthermore, the effective production cross section at $\sqrt{s} = 14$ TeV and 27 TeV¹³ of all viable chargino neutralino pairs which can eventually contribute to the signal yield of WZ and WH_{125} mediated $3l + \cancel{E}_T$ final state are tabulated along

¹²Note that the neutralinos in our parameter space have a negligible bino admixture.

¹³The projected discovery range and exclusion regions for direct Higgsino searches in the WZ and WH_{125} mediated $3l + \cancel{E}_T$ final state at the HE-LHC ($\sqrt{s} = 27$ TeV, $\mathcal{L} = 15$ ab⁻¹) and its translation on to the allowed parameter space has been studied in the next section (Sec. VII C).

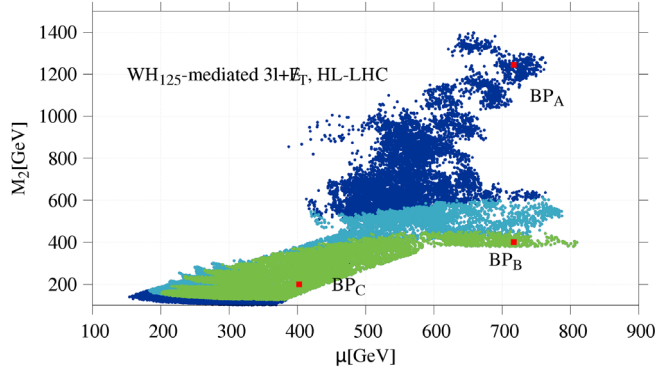


FIG. 16. The currently allowed parameter space points have been shown in the μ - M_2 plane. The pale blue and green colored points fall within the projected exclusion and discovery reach, respectively, of HL-LHC through direct Higgsino searches in the WH_{125} mediated $3l + \cancel{E}_T$ final state. The dark blue colored points remain outside HL-LHC's projected reach. The representative benchmark points: BP_A ($\mu \sim 717$ GeV, $M_2 \sim 1244$ GeV), BP_B ($\mu \sim 717$ GeV, $M_2 \sim 400$ GeV) and BP_C ($\mu \sim 403$ GeV, $M_2 \sim 200$ GeV), are also shown in this figure.

with the relevant branching fractions of the charginos and neutralinos.

In the case of BP_A , $\tilde{\chi}_1^\pm, \tilde{\chi}_2^0, \tilde{\chi}_3^0$ have a dominant Higgsino composition while $\tilde{\chi}_4^0, \tilde{\chi}_2^\pm$ are wino dominated and much heavier. The $\tilde{\chi}_1^0$, on the other hand, is singlino dominated. The $\tilde{\chi}_2^0$ and $\tilde{\chi}_3^0$ decay into $Z + \tilde{\chi}_1^0$ and $H_{125} + \tilde{\chi}_1^0$ with a branching fraction of $\sim 50\%$ and $\sim 43\%$, respectively, in each mode (shown in Table V). BP_A yields a signal significance of 3.8 in direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ searches at the HL-LHC, and falls short of the discovery reach of the HL-LHC. In case of BP_A , although $\text{Br}(\tilde{\chi}_3^0/\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 H_{125})$ is comparable with $\text{Br}(\tilde{\chi}_3^0/\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z)$, the signal significance of BP_A in the WH_{125} mediated $3l + \cancel{E}_T$ final state is $\lesssim 2$ due to the larger

cascade decay chain in the latter case which reduces the signal significance to 0.4.

In the case of BP_B , $\tilde{\chi}_2^0$ is winolike and decays dominantly into $\tilde{\chi}_1^0 H_{125}$ ($\text{Br}(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 H_{125}) \sim 82\%$) while the branching ratio into $\tilde{\chi}_1^0 Z$ is only 4%. The $\tilde{\chi}_1^\pm$ which is also winolike decays into $W^\pm \tilde{\chi}_1^0$ with 100% branching fraction. Among the six possible combinations of chargino neutralino pairs, the $\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ pair has by far the highest cross section ~ 104 fb and thereby, plays the most significant role in signal yield computation. The signal significance of BP_B in the WZ mediated $3l + \cancel{E}_T$ search channel is ~ 1.5 , and therefore, falls marginally outside the projected exclusion reach of HL-LHC. However, considering the large branching fraction of $\tilde{\chi}_2^0 \rightarrow H_2 \tilde{\chi}_1^0$, it is expected that direct searches in the WH_{125} channel will be more effective in probing BP_B . The reach of the HL-LHC for NMSSM doublet Higgsinos via the WH_{125} mediated $3l + \cancel{E}_T$ search channel is illustrated in Fig. 16, where we plot the allowed points from Fig. 1, with the same color convention as in Fig. 15. Indeed BP_B falls within the projected discovery reach of this search with a signal significance of 5.3.

Another important aspect to be noted for the BP_B benchmark point is the presence of other cascade decay modes with considerable branching ratios. For instance, $\tilde{\chi}_3^0$ decays to $Z \tilde{\chi}_2^0$ while $\tilde{\chi}_2^0$ in addition to its decay to $\tilde{\chi}_1^0 H_{125}$, also decays to $\tilde{\chi}_1^0 H_1$ with a branching ratio $\sim 14\%$. We see from Table VI that $\tilde{\chi}_3^0$ is dominantly produced in addition to $\tilde{\chi}_2^\pm$ which decays to Z or H_{125} plus $\tilde{\chi}_1^\pm$, or via W and lighter neutralinos. The final states from $\tilde{\chi}_3^0 \tilde{\chi}_2^\pm$ production can, therefore, be very rich and include $VV + \cancel{E}_T$ [131] and $V/Z/H_1 + \cancel{E}_T$ events in the final state. Unfortunately, at least for this point $\sigma(\tilde{\chi}_3^0 \tilde{\chi}_2^\pm)$ is just 2.1 fb at $\sqrt{s} = 14$ TeV and 10.2 fb at $\sqrt{s} = 27$ TeV, but see another case in Table VII where $\sigma(\tilde{\chi}_3^0 \tilde{\chi}_2^\pm)$ is much larger (24.8 fb at $\sqrt{s} = 14$ TeV and 86.5 fb at $\sqrt{s} = 27$ TeV). The search

TABLE VII. The masses, wino and Higgsino fractions of neutralinos and charginos, neutralino-chargino production cross sections, branching ratios for neutralinos and signal significance for BP_C . The input parameters of BP_C are tabulated in Appendix.

	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$	$\tilde{\chi}_1^\pm$	$\tilde{\chi}_2^\pm$
Mass [GeV]	3.0	205	415	427	206	432
Wino %	10^{-4}	0.91	7×10^{-3}	0.08	0.87	0.13
Higgsino %	10^{-4}	0.08	0.99	0.92	0.13	0.87
Singlino fraction in $\tilde{\chi}_1^0$: 0.99			$M_{H_1} = 6.6$ GeV, $M_{A_1} = 6.3$ GeV			
Cross-section (fb)	$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm$	$\tilde{\chi}_2^0 \tilde{\chi}_2^\pm$	$\tilde{\chi}_3^0 \tilde{\chi}_1^\pm$	$\tilde{\chi}_3^0 \tilde{\chi}_2^\pm$	$\tilde{\chi}_4^0 \tilde{\chi}_1^\pm$	$\tilde{\chi}_4^0 \tilde{\chi}_2^\pm$
$\sqrt{s} = 14$ TeV	1593	6.1	7.7	24.8	7.0	28.8
$\sqrt{s} = 27$ TeV	4399	19.1	23.8	86.5	21.9	100.9
Branching ratio	$\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z$ (0.04), $\tilde{\chi}_1^0 H_{125}$ (0.92), $\tilde{\chi}_1^0 H_1$ (0.03) $\tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^\pm W^\mp$ (0.68), $\tilde{\chi}_2^0 Z$ (0.29), $\tilde{\chi}_2^0 H_{125}$ (0.02) $\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_1^\pm W^\mp$ (0.72), $\tilde{\chi}_2^0 Z$ (0.04), $\tilde{\chi}_2^0 H_{125}$ (0.22)					
Significance at HL-LHC: WZ mediated $3l + \cancel{E}_T$: 1.3, WH_{125} mediated $3l + \cancel{E}_T$: 8.8						
Significance at HE-LHC: WZ mediated $3l + \cancel{E}_T$: 2.1, WH_{125} mediated $3l + \cancel{E}_T$: 48						

strategies devised to optimize the $3l + \cancel{E}_T$ searches will not be particularly efficient in the presence of these cascade decay channels and Figs. 15 and 16 may not provide the complete picture. Dedicated searches beyond the scope of this paper will be needed to explore these novel signals.

It can also be observed from Fig. 16 that future direct searches in the WH_{125} mediated $3l + \cancel{E}_T$ channel are more effective in probing the parameter space region with $M_2 \lesssim \mu$. However, below $M_2 \lesssim 125$ GeV, an on-shell H_{125} cannot be produced resulting in zero signal efficiency, and therefore this channel cannot be used. It is very striking to see the complementarity in the search power via the WZ and the WH_{125} -mediated trilepton search channels exhibited in Fig. 15 and Fig. 16, respectively. For instance, in the dark blue coloured band near $M_2 \sim 180$ GeV and $\mu \sim 300\text{--}400$ GeV in Fig. 15, the signal significance is less than 2, while in the same region in Fig. 16, the signal is above the discovery limit! Likewise, in much of the green region at large values of M_2 where the signal can be discovered via the WZ -mediated channel (Fig. 15), the signal is unobservable via the WH_{125} channel in Fig. 16. To obtain a better understanding of what is happening in the low M_2 region, we examine a representative benchmark point BP_C (see Table VII). BP_C features a winolike $\tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ and thus a large production cross section of $pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm$ (1593 fb), a large branching fraction of $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 H_2$ (92%) and $\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 W^\pm$ (100%). However, due to the small doublet Higgsino component in $\tilde{\chi}_2^0$, the branching ratio of $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z$ is only 4%. Additionally, the signal regions in Table I generate relatively lower efficiencies in the $M_{\text{NLSP}} \sim 180$ GeV region compared to the smaller and larger values of $M_{\tilde{\chi}_2^0}$, from SR1A and SR1B. Consequently, the signal significance of BP_C in the WZ channel is only ~ 1.3 and thereby falls outside the projected reach of HL-LHC. BP_C is, however, within the projected discovery reach of HL-LHC in the WH_{125} channel where the signal significance is 8.8.

An examination of Figs. 15 and 16 shows that it should be possible to discover SUSY with $>5\sigma$ confidence at the HL-LHC over almost the entire allowed parameter space (with the exception of the island at large values of M_2 and μ near the benchmark point BP_A) if it is realized as in the NMSSM scenario with $m_{\tilde{\chi}_1^0} < 62.5$ GeV.

C. Electroweakino searches at the HE-LHC

We have just seen that the HL-LHC will be able to probe most of the NMSSM parameter space via $3l + \cancel{E}_T$ searches via at least one or the other of the WZ or WH_{125} mediated channels. Here, we turn to the exploration of the capabilities of the proposed HE-LHC for the corresponding search. Our motivation for this is two-fold. First, it is clear that the signal might be just above the discovery limit at the HL-LHC so that a larger signal may be obtained at the proposed energy upgrade, allowing for a detailed study of the new physics. Second, we want to map out the NMSSM region

where the signal would be discoverable via both the WZ and the WH_{125} mediated channels, since observations in multiple channels would clearly help to elucidate its origin. To this end, we devise new strategies to isolate the SUSY signal from the background, and delineate the corresponding 5σ discovery reach and 2σ exclusion regions for the cases of both the WZ and the WH_{125} mediated $3l + \cancel{E}_T$ channels. We recognize that other superpartners would also be accessible, but for definiteness focus only on the golden trilepton signal from the lightest ino states.

1. WZ mediated $3l + \cancel{E}_T$ searches at the HE-LHC

We select events with exactly three isolated leptons, where lepton isolation as described in Sec. VII A 1 is used. Two isolated leptons are required to form a SFOS lepton pair with invariant mass in the range $M_Z \pm 10$ GeV. In the presence of two such SFOS lepton pairs, the one which minimizes the transverse mass of the non-SFOS lepton and \cancel{E}_T is chosen as the correct SFOS pair. In addition, a veto on b jet with $p_T > 30$ GeV and $|\eta| < 2.5$ is also applied. On-shell and off-shell WZ , VVV , $t\bar{t}V$ and ZZ are the background sources. Signal events have been generated by varying $M_{\tilde{\chi}_1^0}$ over the range of 0–1000 GeV with a step size of 30 GeV while $M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm}$ (assuming, $M_{\tilde{\chi}_3^0} = M_{\tilde{\chi}_2^0} = M_{\tilde{\chi}_1^\pm}$) has been varied from 100 GeV to 1780 GeV with a step size of 30 GeV.

As before, we have examined various distributions for several benchmark points with a diverse range of parent ino masses and mass gaps: $[M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm}, M_{\tilde{\chi}_1^0}]$ (in GeV): BPA3 [130, 30], BPB3 [250, 30], BPC3 [340, 30], BPD3 [520, 0], BPE3 [520, 390], BPF3 [1000, 0], BPG3 [1000, 480], BPH3 [1000, 780], BPI3 [1420, 0], BPJ3 [1420, 990]. Based on this analysis, we choose the ten signal regions that optimize the significance of the signal for a variety of ino and LSP masses (though, of course, for the NMSSM analysis of interest, the LSP is light). The selection cuts are listed in Table VIII.

As an illustration, we show the \cancel{E}_T and ΔR_{SFOS} distributions for the benchmark case BPH3 together with those for the main SM backgrounds (for HE-LHC) in Fig. 17. The signal event distributions are represented in a black colored shade while the distributions for WZ , VVV , $t\bar{t}V$ and ZZ backgrounds are shown in blue, orange, green and red colors, respectively. Note that BPH3 is the signal benchmark point with intermediate mass gap between the NLSP and the LSP, and was used to derive the optimized set of selection cuts corresponding to SRH3. The plots in the left panel of Fig. 17 have been obtained by imposing the requirement of three isolated leptons in the final state, presence of at least one SFOS pair of leptons with invariant mass in the range $M_Z \pm 10$ GeV, and the absence of any b jet with $p_T \geq 30$ GeV and $|\eta| < 2.5$. The distribution in the right hand panels of Fig. 17 are obtained after all the SRH3 cuts in Table VIII.

TABLE VIII. List of selection cuts corresponding to the signal regions for searches in WZ mediated $3l + \cancel{E}_T$ final state at the HE-LHC. The signal regions have been optimized through a cut-based analysis to yield maximum significance for the signal samples corresponding to the respective values of $M_{\tilde{\chi}_2^0 \tilde{\chi}_3^0 \tilde{\chi}_1^\pm}$ and $M_{\tilde{\chi}_1^0}$.

Cuts	SRA3	SRB3	SRC3	SRD3	SRE3	SRF3	SRG3	SRH3	SRI3	SRJ3
$M_{\tilde{\chi}_2^0 \tilde{\chi}_3^0 \tilde{\chi}_1^\pm}$ [GeV]	130	250	340	520	520	1000	1000	1000	1420	1420
$M_{\tilde{\chi}_1^0}$ [GeV]	30	30	30	0	390	0	480	780	0	990
$\Delta\phi_{\text{SFOS}-\cancel{E}_T}$...	[2.6: π]	[2.6: π]	[1.4: π]	[1.4: π]	[1.6: π]	[1.5: π]	[2.1: π]	[1.7: π]	[1.4: π]
ΔR_{SFOS}	[1.3:3.8]	[0.2:1.4]	[0.1:1.3]	...	[0.3:2.1]	[0.0:1.2]	[0.0:1.2]	[0.3:1.5]	≤ 1.0	[0.2:0.8]
\cancel{E}_T [GeV]	[80:160]	≥ 150	≥ 200	≥ 250	≥ 400	≥ 220	≥ 300	≥ 250	≥ 220	≥ 250
M_T^{lw} [GeV]	[100:130]	≥ 130	≥ 140	≥ 200	≥ 100	≥ 230	≥ 160	≥ 140	≥ 250	≥ 210
M_{CT}^{lw} [GeV]	[70:230]	≥ 200	≥ 200	≥ 150	≥ 100	≥ 200	≥ 200	≥ 140	≥ 250	≥ 180
$p_T^{l_1}$ [GeV]	[80:160]	≥ 90	≥ 110	≥ 170	≥ 100	≥ 220	≥ 200	≥ 130	≥ 270	≥ 200
$p_T^{l_2}$ [GeV]	≥ 50	≥ 50	≥ 70	≥ 90	≥ 50	≥ 120	≥ 120	≥ 90	≥ 130	≥ 150
$p_T^{l_3}$ [GeV]	≥ 40	≥ 40	≥ 40	≥ 50	≥ 40	≥ 70	≥ 60	≥ 50	≥ 80	≥ 50

As before, the dominant physics SM backgrounds to the hadronically quiet $3l + \cancel{E}_T$ signal is expected to come from WZ (which includes $W^{(*)}Z$ and $W^{(*)}\gamma^*$) production, $t\bar{t}V$ production, VVV production and ZZ production. The corresponding background levels obtained using MADGRAPH5_aMC@NLO are shown in Table IX after all our analysis cuts. The efficiency map of SRD3, SRE3,

SRH3 and SRJ3 are illustrated in Fig. 18 in the $M_{\tilde{\chi}_3^0 \tilde{\chi}_2^0 \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane with the color palette representing the signal efficiency. Again, we have assumed a systematic uncertainty of 5%. For this analysis, we took $\mathcal{L} = 15 \text{ ab}^{-1}$. The total background yield, B , has been computed by summing over the yields from all relevant backgrounds.

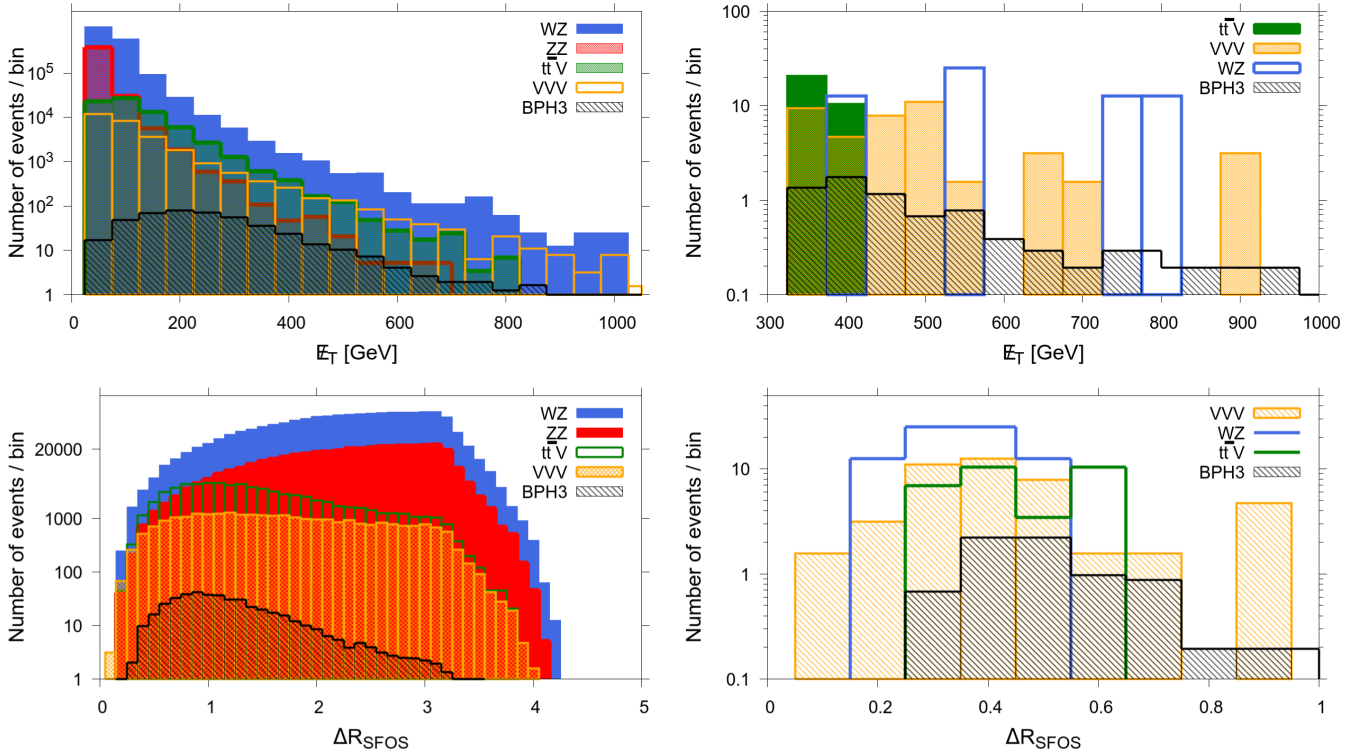


FIG. 17. The event distribution of \cancel{E}_T (top) and ΔR_{SFOS} (bottom) at the HE-LHC is shown for the signal benchmark point BPH3 ($M_{\tilde{\chi}_3^0 \tilde{\chi}_2^0 \tilde{\chi}_1^\pm} = 1000 \text{ GeV}$, $M_{\tilde{\chi}_1^0} = 780 \text{ GeV}$) in black color. The corresponding event distributions for on-shell and off-shell WZ , VVV , ZZ and $t\bar{t}V$ have been shown in blue, orange, red and green colors, respectively. The left (right) panel shows the corresponding distributions before (after) the application of SRH3 cuts.

TABLE IX. The background yields for $\sqrt{s} = 27$ TeV LHC corresponding to 15 ab^{-1} of integrated luminosity, for the 8 different signal regions considered for the cut-based analysis, are presented. The leading order (LO) cross sections generated by MADGRAPH5_aMC@NLO have also been shown. The $t\bar{t}V$ background has been specifically decayed into leptonic final states.

Background process	Cross section [LO]	Background yield (27 TeV, 15 ab^{-1})									
		SRA3	SRB3	SRC3	SRD3	SRE3	SRF3	SRG3	SRH3	SRI3	SRJ3
$t\bar{t}V$ ($V = W, Z$) ($W \rightarrow l\nu, Z \rightarrow ll$)	1385 fb	79.6	166	107	69.2	38.1	41.5	31.2	96.9	20.8	27.7
WZ	1263 fb	341	164	126	101	88.4	75.8	75.8	75.8	63.1	63.1
VVV ($V = W, Z$)	681 fb	31.4	132	99	70.7	66.0	33.0	44.0	70.7	25.1	36.1
ZZ (leptonic)	2092	0.0	0.0	0.0	10.4	5.18	0.0	0.0	5.18	0.0	0.0
Total background		452	462	333	251	198	150	151	249	109	127

We show the projected exclusion region ($S_\sigma > 2\sigma$, blue color) and the projected discovery region ($S_\sigma > 5\sigma$, grey color) obtained from doublet Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final state at the HE-LHC in Fig. 19. It can be seen from Fig. 19 that HE-LHC will be able to discover (exclude) Higgsinolike $\tilde{\chi}_3^0, \tilde{\chi}_2^0$ and $\tilde{\chi}_1^\pm$ with masses up to $\sim 1330(1660)$ GeV if the LSP is light.

2. WH_{125} -mediated $3l + \cancel{E}_T$ searches at the HE-LHC

As in Sec. VII A 2, we consider the signal from chargino-neutralino pair production where the neutralinos decay to H_{125} and the chargino decays to W . Dominant contributions to the $3l + \cancel{E}_T$ signal arise when W decays leptonically, and $H_{125} \rightarrow WW^* \rightarrow l\nu l'\nu$ or $H_{125} \rightarrow \tau^+\tau^-$ and the

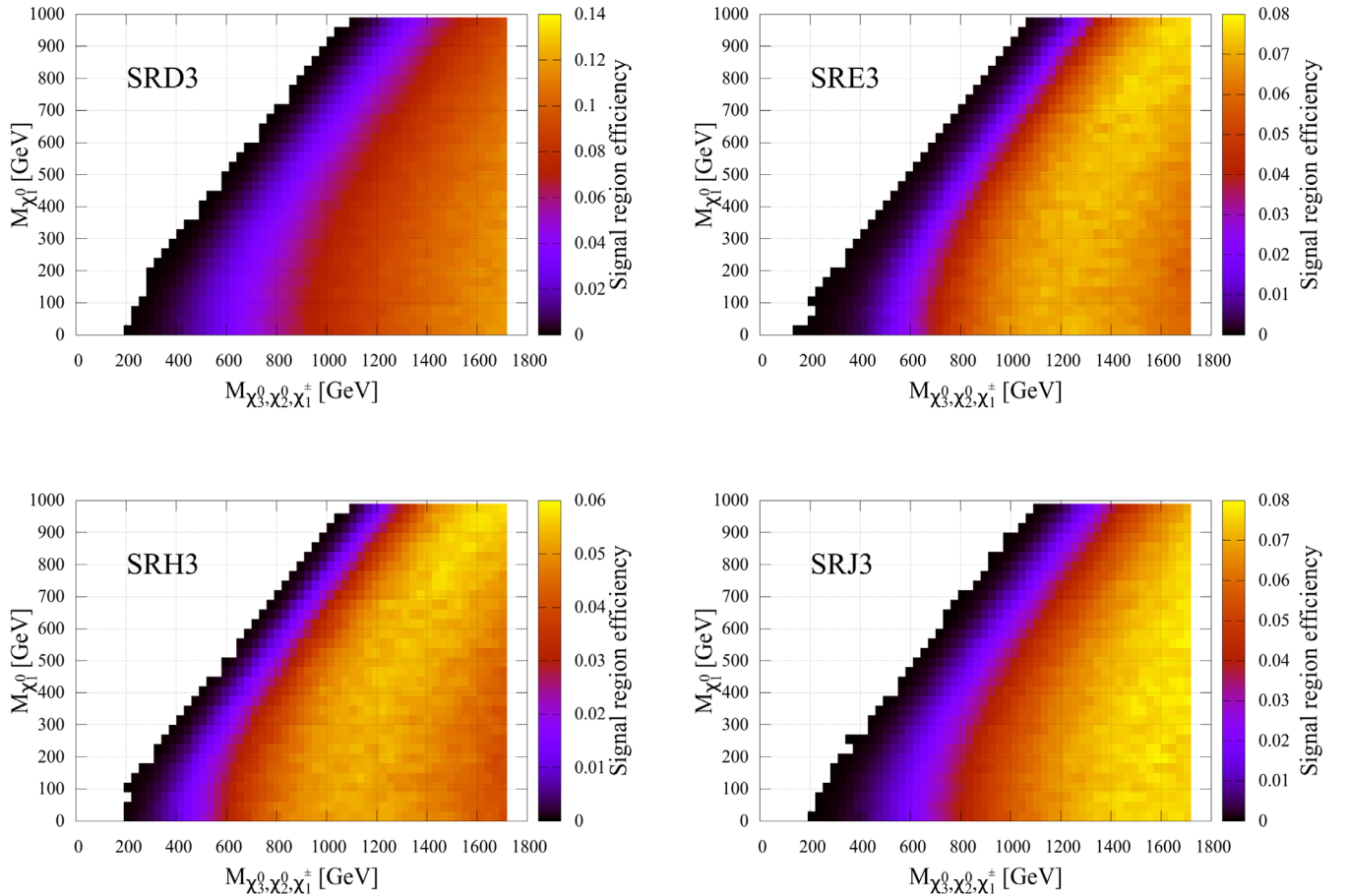


FIG. 18. The efficiency map for SRD3, SRE3, SRH3 and SRJ3 has been shown as a color palette in the $M_{\tilde{\chi}_1^0} - M_{\tilde{\chi}_2^0}$ plane. The top-left and top-right figures represent the efficiency map of SRD3 and SRE3, respectively. The bottom grid represents the efficiency map for SRH3 (left) and SRJ3 (right), respectively. Note the difference in the vertical scales in the four frames.

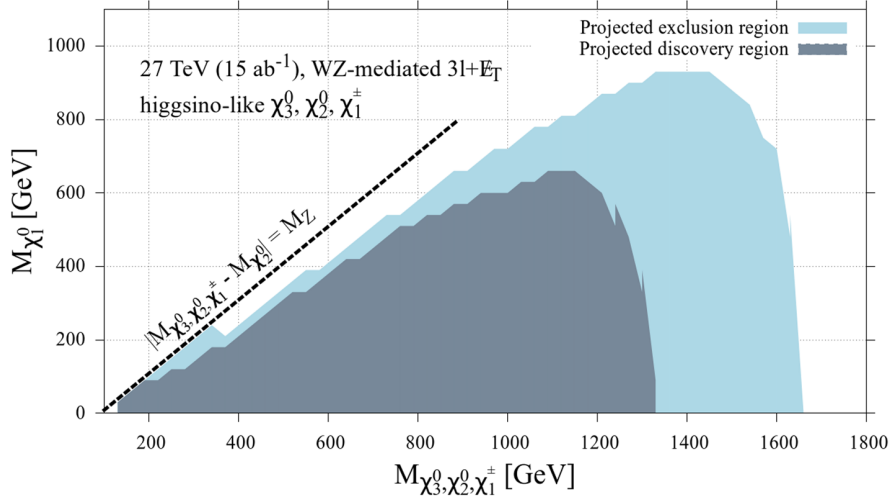


FIG. 19. The projected exclusion (blue color) and discovery regions (grey color) from searches in the WZ mediated $3l + \cancel{E}_T$ final state produced from the cascade decay of directly produced mass degenerate Higgsino-like $\tilde{\chi}_2^0\tilde{\chi}_1^\pm + \tilde{\chi}_3^0\tilde{\chi}_1^\pm$ at $\sqrt{s} = 27$ TeV LHC corresponding to an integrated luminosity of 15 ab^{-1} , are shown.

taus decay leptonically. Signal events have been generated for $M_{\tilde{\chi}_2^0\tilde{\chi}_3^0\tilde{\chi}_1^\pm}$ varying from 100 GeV to 1700 GeV, while $M_{\tilde{\chi}_1^0}$ has been varied from 0 GeV to 1000 GeV with a step size of 30 GeV. The event selection criteria prescribed in Sec. VII A 2 is followed here. Background contributions arise from WH_{125} and $WZ, VVV, t\bar{t}V$ and ZZ .

We choose 7 optimized signal regions: SRA4, SRB4, SRC4, SRD4, SRE4, SRF4 and SRG4 in order to perform the current analysis. SRA4, SRC4, SRE4 and SRG4 (SRB4, SRD4 and SRF4) have been optimized to maximize the signal significance of signal events with small (large) mass difference between the Higgsino NLSPs and the LSP. The signal regions have been obtained by optimizing the signal significances of signal processes

corresponding to the following values of $[M_{\tilde{\chi}_3^0\tilde{\chi}_2^0\tilde{\chi}_1^\pm}, M_{\tilde{\chi}_1^0}]$ (in GeV): BPA4 [160, 30], BPB4 [550, 0], BPC4 [550, 420], BPD4 [910, 0], BPE4 [910, 750], BPF4 [1240, 0] and BPG4 [1240, 900]. The kinematic variables used to design the optimized signal regions are: $p_T^{l_1}, p_T^{l_2}, M_T^{l_1}, M_T^{l_2}, M_T^{l_3}, \Delta R_{OS}^{\min}, \Delta R_{OS}^{\max}, M_{OS,\min}^{\text{inv}}$ and \cancel{E}_T . Here, ΔR_{OS}^{\min} and ΔR_{OS}^{\max} represents the ΔR between OS leptons with minimum and maximum ΔR separation, respectively, while, $M_{OS,\min}^{\text{inv}}$ represents the invariant mass of the OS lepton pair with minimum ΔR . $M_T^{l_i}$ ($i = 1, 2, 3$) corresponds to the transverse mass of the \cancel{E}_T and p_T ordered i th final state lepton. The set of optimized cuts corresponding to the signal regions are presented in Table X.

TABLE X. List of selection cuts corresponding to the signal regions for WH_{125} -mediated $3l + \cancel{E}_T$ final state. The signal regions have been optimized through a cut-based analysis to yield maximum significance for the signal samples corresponding to the respective values of $M_{\tilde{\chi}_2^0\tilde{\chi}_3^0\tilde{\chi}_1^\pm}$ and $M_{\tilde{\chi}_1^0}$.

Cuts	SRA4	SRB4	SRC4	SRD4	SRE4	SRF4	SRG4
$M_{\tilde{\chi}_2^0\tilde{\chi}_3^0\tilde{\chi}_1^\pm}$ [GeV]	160	550	550	910	910	1240	1240
$M_{\tilde{\chi}_1^0}$ [GeV]	30	0	420	0	750	0	900
$p_T^{l_1}$ [GeV]	≥ 80	≥ 120	[120:170]	≥ 200	[100:200]	≥ 200	≥ 150
$p_T^{l_2}$ [GeV]	≥ 50	≥ 80	≥ 40	≥ 100	≥ 40	≥ 120	≥ 50
$p_T^{l_3}$ [GeV]	≥ 40	≥ 40	≥ 30	≥ 50	≥ 30	≥ 50	≥ 30
$M_T^{l_1}$ [GeV]	[125:225]	≥ 235	≥ 150	≥ 250	≥ 150	≥ 350	≥ 220
$M_T^{l_2}$ [GeV]	≥ 100	≥ 150	≥ 100	≥ 170	≥ 100	≥ 150	≥ 150
$M_T^{l_3}$ [GeV]	≥ 100	≥ 120	≥ 100	≥ 120	≥ 100	≥ 120	≥ 120
ΔR_{OS}^{\min}	[0.2:0.8]	≤ 0.9	[0.2:1.2]	≤ 0.6	[0.2:0.8]	≤ 0.9	≤ 1.2
ΔR_{OS}^{\max}	[0.7-2.5]	[0.4:2.8]	[0.3:3.0]	[0.3:3.3]	[0.5:3.5]	[0.2:2.6]	[0.4:2.4]
$M_{OS,\min}^{\text{inv}}$ [GeV]	≤ 60	≤ 60	≤ 60	≤ 120	≤ 150	≤ 150	≤ 50
\cancel{E}_T [GeV]	[80:180]	≥ 150	≥ 150	≥ 150	≥ 150	≥ 200	≥ 200

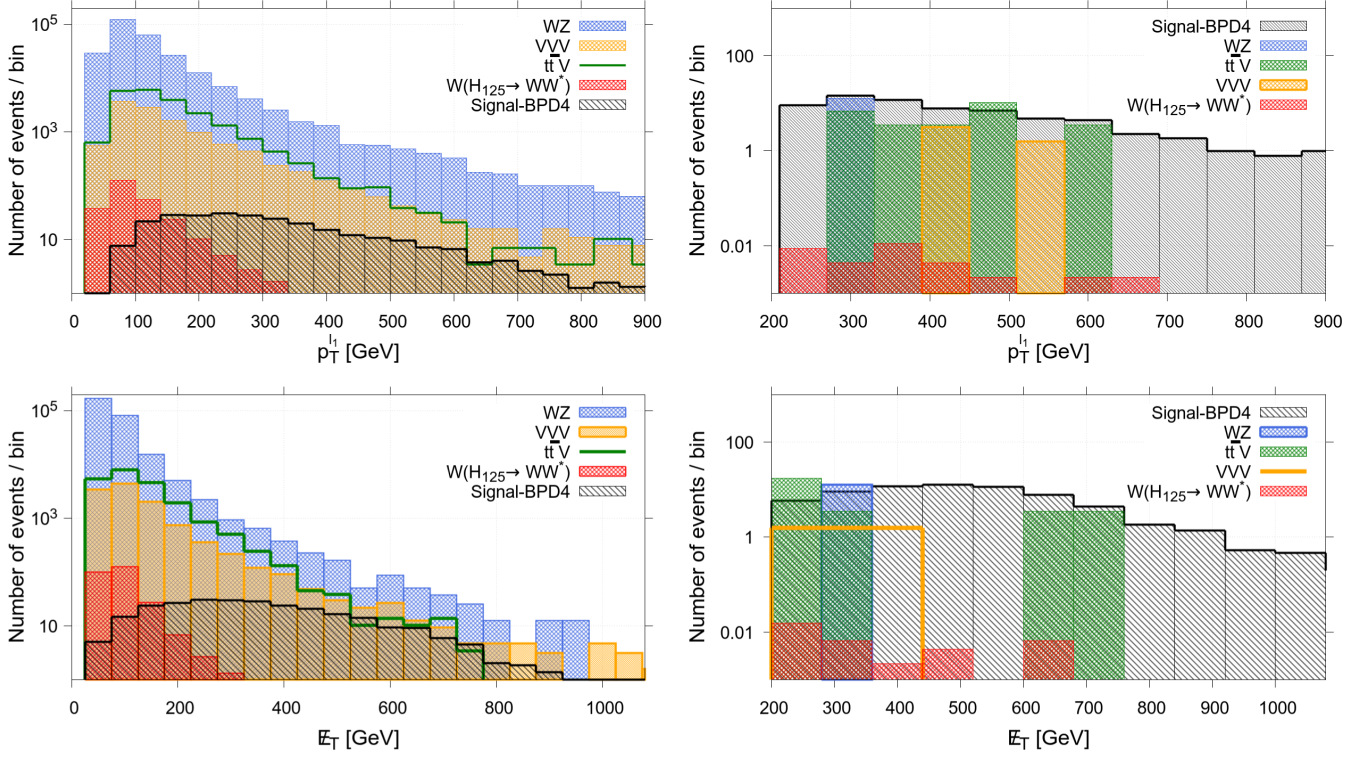


FIG. 20. Event distribution of p_T^l (top) and E_T (bottom) at the HE-LHC for BPD4 [$M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm} = 910$ GeV, $M_{\tilde{\chi}_1^0} = 0$ GeV] used to obtain the optimized signal region SRD4 (shown in black shade), and the background processes: $t\bar{t}V$ (shown in green color), WZ (shown in blue color), WH_{125} (shown in red color) and VVV (shown in orange color). The figures on the left have been obtained after demanding the presence of three isolated leptons in the final state, b jet veto and a veto on SFOS pair with invariant mass in the range $M_Z \pm 12$ GeV. The figures on the right have been obtained upon a further application of SRD4 cuts.

Although not directly germane to the NMSSM signal with a light LSP, we find it interesting to show the event distribution of p_T^l and E_T for BPD4 at the HE-LHC. The signal distribution is shown by the black-hatched region in Fig. 20 together with the distributions of the relevant background processes ($t\bar{t}V$: green color, WH_{125} : red color, VVV : orange color, and, WZ : blue color). The distributions on the left panels of Fig. 20 have been obtained by requiring the presence of exactly three isolated leptons in the final state, the absence of any SFOS lepton pair with invariant mass in the range $M_Z \pm 12$ GeV and b – jet veto. In the case of BPD4, the large mass difference between $\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ and $\tilde{\chi}_1^0$ results in the leading p_T lepton getting produced with a larger boost and therefore peaks at a higher value (around 200 GeV) and has a flatter distribution as compared to the background processes. The larger mass difference between the NLSPs and the LSP also results in a E_T distribution which extends to much larger values (>900 GeV). The E_T distribution for the background processes, on the other hand, falls down more steeply. The figures in the right panel of Fig. 21 have been obtained after passing through the SRD4 cuts.

The event distribution of p_T^l and ΔR_{OS}^{\min} at the HE-LHC for BPE4 and the relevant background processes have been shown in Fig. 21 following the color code of Fig. 20. The

left panels of Fig. 21 have been obtained by imposing the following criteria: presence of three isolated leptons, veto on SFOS pair with invariant mass $M_Z \pm 12$ GeV and b -jet veto. Due to a smaller mass difference between the $\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ and $\tilde{\chi}_1^0$ in BPE4, the leading p_T lepton is produced with a smaller boost and peaks at a slightly lower p_T (around 50 GeV) which is roughly similar to the background processes (all of which peak around 50–100 GeV). Similarly, the ΔR_{OS}^{\min} distribution for BPE4 falls off before $\lesssim 3.0$ unlike the WZ , WH_{125} , $t\bar{t}V$ and VVV backgrounds which extend up to $\gtrsim 4.0$. The plots on the right panels of Fig. 20 show the event distribution obtained upon the further imposition of SRE4 cuts.

The LO background cross sections and the background yields corresponding to the 7 signal regions are shown in Table XI. We also show the efficiency grids for SRA4, SRB4, SRC4 and SRD4 for the $H_{125} \rightarrow WW^*$ scenario in Fig. 22 in the $M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane.

The strategy prescribed in Sec. VII A 2 has been used for the computation of signal significance. The signal significance is computed for the seven signal regions, and the one which yields the highest value for a particular point is considered in deriving the projection contours. We have assumed a systematic uncertainty of 5% in the present analysis. The projected exclusion and

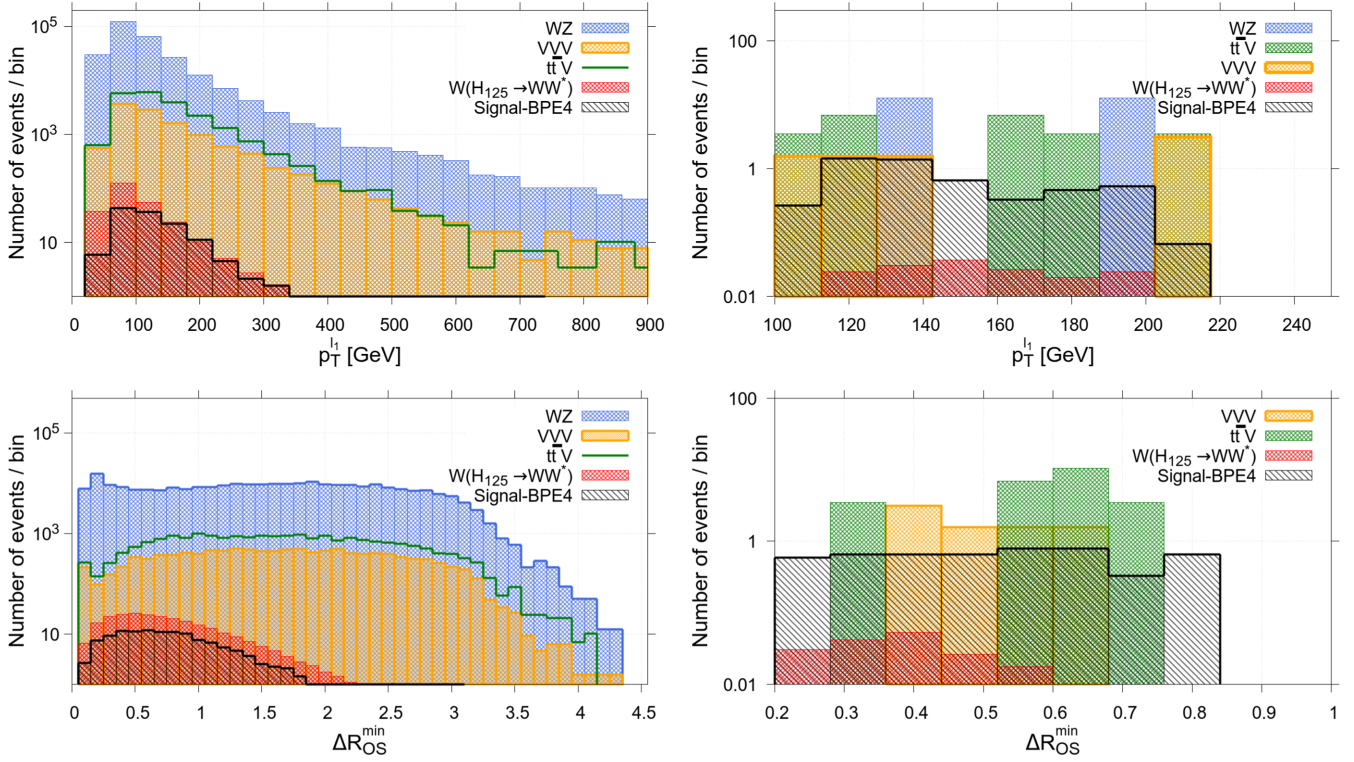


FIG. 21. Event distribution of $p_T^{l_1}$ (top) and ΔR_{OS}^{\min} (bottom) at the HE-LHC for BPE4 [$M_{\tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_1^\pm} = 910$ GeV, $M_{\tilde{\chi}_1^0} = 750$ GeV] used to obtain the optimized signal region SRE4 (shown in black shade), and the background processes: $t\bar{t}V$ (shown in green color), WZ (shown in blue color), WH_{125} (shown in red color) and VVV (shown in orange color). The figures on the left have been obtained after demanding the presence of three isolated leptons in the final state, b jet veto and a veto on SFOS pair with invariant mass in the range $M_Z \pm 12$ GeV. The figures on the right have been obtained upon a further application of SRE4 cuts.

discovery contours for direct Higgsino searches in the WH_{125} -mediated $3l + \cancel{E}_T$ channel at the HE-LHC is shown in Fig. 23. The projected discovery (exclusion) region reaches up to $M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm} \sim 1180(1500)$ GeV for a massless LSP.

D. Projected limits on NMSSM-inos at the HE-LHC

Extending the discussion and analysis prescribed in Sec. VII B, we evaluate the projected reach of doublet Higgsino searches at the HE-LHC in probing the NMSSM parameter space with light neutralinos. The direct Higgsino

TABLE XI. The background yields for $\sqrt{s} = 27$ TeV LHC corresponding to 15 ab^{-1} of integrated luminosity, for the 5 different signal regions considered for the cut-based analysis, are presented. The leading order (LO) cross sections generated by MADGRAPH5_AMC@NLO have been considered.

Background process	Cross		Background yield (27 TeV, 15 ab^{-1})					
	section [LO]	SRA4	SRB4	SRC4	SRD4	SRE4	SRF4	SRG
ZZ	2092 fb	0.0	10.4	0.0	0.0	0.0	0.0	5.18
$t\bar{t}V$ ($V = W, Z$) ($W \rightarrow l\nu, Z \rightarrow ll$)	1385 fb	10.4	10.4	6.92	27.7	24.2	17.3	6.93
WZ	1263 fb	37.9	37.9	12.6	12.6	25.3	12.6	0.00
VVV ($V = W, Z$)	681 fb	1.57	0.0	1.57	4.72	7.86	1.57	0.0
WH_{125} ($H_{125} \rightarrow \tau^+\tau^-$)	30.2 fb	0.0	0.0	0.45	0.0	0.70	0.01	0.0
WH_{125} ($H_{125} \rightarrow WW^*$) ($W \rightarrow l\nu$)	0.29 fb	0.40	0.05	0.08	0.04	0.18	0.01	0.02
Total background		50.7	58.7	21.3	45.1	57.7	31.5	12.2

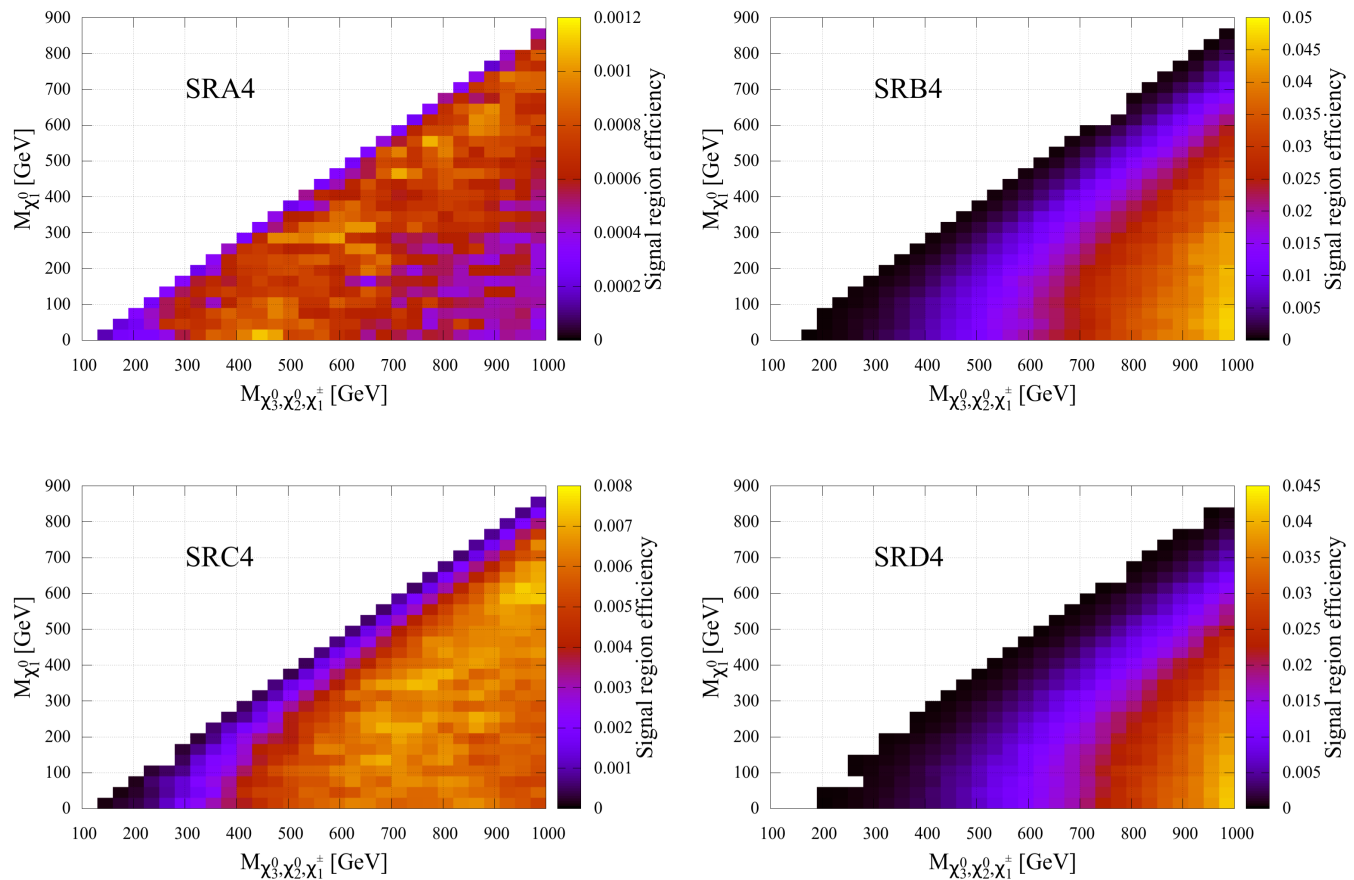


FIG. 22. Efficiency map of SRA4 (top-left), SRB4 (top-right), SRC4 (bottom-left) and SRD4 (bottom-right) is shown as a color palette in the $M_{\tilde{\chi}_3^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm} - M_{\tilde{\chi}_1^0}$ plane.

production cross sections of the relevant chargino neutralino pairs is computed at $\sqrt{s} = 27$ TeV and is then scaled with the relevant reduced couplings for each parameter space point. The signal significance values are then computed using the strategy described in Sec. VII B. The projected impact of direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final

state at the HE-LHC is shown in Fig. 24. Comparing with Fig. 15, we see that the HE-LHC provides a larger discovery opportunity than the HL-LHC for the detection of NMSSM-inos with a light LSP. Nearly all the NMSSM allowed points are within the discovery reach of the HE-LHC. The parameter space points shown in Fig. 24 correspond to the allowed

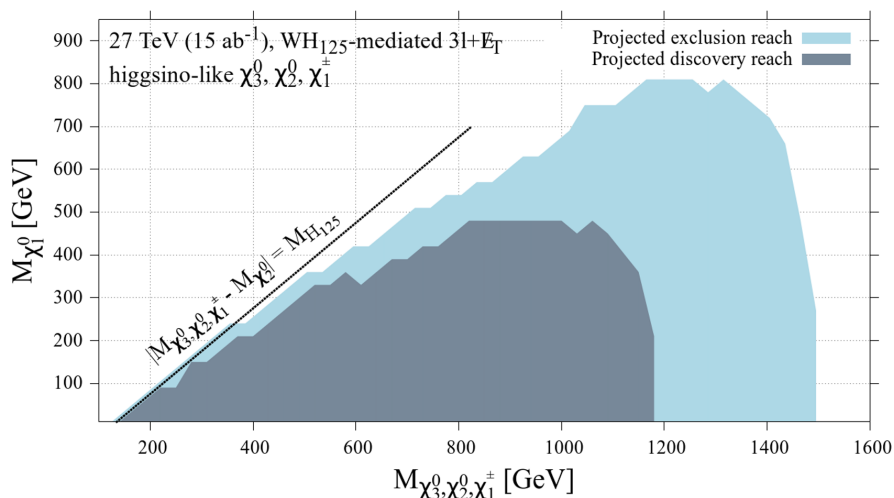


FIG. 23. The projected exclusion (blue color) and discovery regions (grey color) from searches in the WH_{125} -mediated $3l + \cancel{E}_T$ final state produced from direct Higgsino searches ($pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm + \tilde{\chi}_3^0 \tilde{\chi}_1^\pm$) at the HE-LHC, is shown.

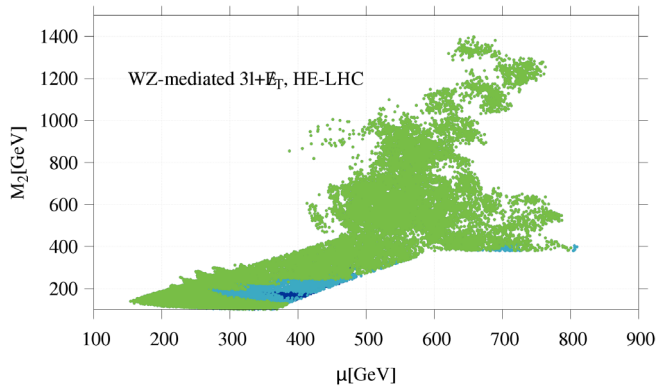


FIG. 24. The currently allowed parameter space points are shown in the $M_2 - \mu$ plane. The pale blue and green colored points fall within the projected exclusion and discovery reach, respectively, of direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ channel at the HE-LHC.

points obtained after imposing all the current constraints discussed in Sec. IV. The green colored points in Fig. 24 are within the projected discovery reach (signal significance >5), while the pale blue colored points are within the projected exclusion reach (signal significance >2) of direct Higgsino searches in the WZ mediated $3l + \cancel{E}_T$ final state at HE-LHC. The dark blue colored points, however, will be undetectable to HE-LHC, these correspond to a small band of points at $M_2 \sim 200$ GeV. We note that the signal cases, and hence the cuts, that we have chosen in Table VIII are not designed to probe the very light wino region where the lightest NLSP mass is around $M_{\text{NLSP}} \sim 180\text{--}200$ GeV resulting in reduced signal efficiency in the dark blue region. Furthermore, the lightest NLSP in the dark blue region is dominantly wino in nature resulting in small $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z$ branching rates. We have checked that even so, these points only narrowly escape the projected exclusion. We fully expect that choosing additional signal regions to optimize the signal significance around $M_{\text{NLSP}} \sim 190$ GeV will prove effective in extending the exclusion/discovery region of the HE-LHC to this region of parameter space.

Before concluding this section, we also study the future reach of direct Higgsino searches in the WH_{125} mediated $3l + \cancel{E}_T$ final state at the HE-LHC. The results are illustrated in Fig. 25 using the color code from Fig. 24. It can be seen from Fig. 25 that the projected reach of HE-LHC extends much beyond that of the HL-LHC (shown in Fig. 16) for the detection of NMSSM-inos. Here, the dark blue colored points are concentrated in the $M_2 \lesssim 125$ GeV (where the decay to H_{125} is kinematically forbidden). The projected discovery reach covers the rest of the NMSSM parameter space. We see that a combination of doublet Higgsino searches at the HE-LHC in the WH_{125} and WZ mediated $3l + \cancel{E}_T$ channels will probe the entire region of the currently allowed NMSSM parameter space with light neutralinos at the $>5\sigma$ level.

Even though discovery may be possible also at the HL-LHC, the reader may find it interesting to compare the

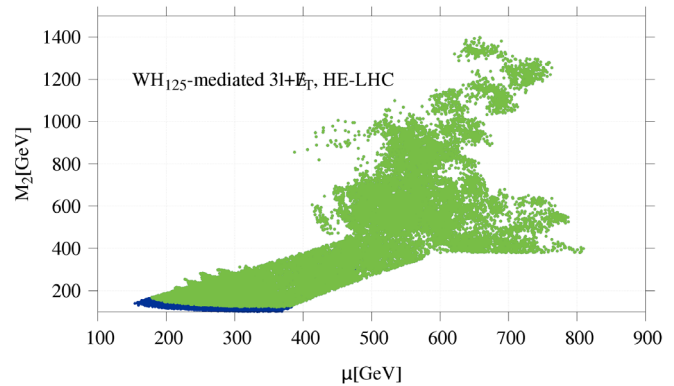


FIG. 25. The allowed parameter space points have been shown in the $M_2 - \mu$ plane. The pale blue and green colored points fall within the projected exclusion and discovery reach, respectively, of direct electroweakino searches in the WH_{125} mediated $3l + \cancel{E}_T$ channel at the HE-LHC. The dark blue colored points fall outside the HE-LHC's projected reach.

signal size after the final cuts at these facilities. We show such a comparison in Table XII for the benchmark points BP_A , BP_B and BP_C in Figs. 15 and 16, and 6 other benchmark points (BP_D , BP_E , BP_F , BP_G , BP_H and BP_I), for both the WZ and the WH_{125} mediated decays.¹⁴ The corresponding signal significance is shown in parenthesis. We see that the accumulated signal is appreciably larger at the HE-LHC. This larger data sample should enable detailed studies of event shapes and distributions, and help zero in on the origin of the new physics.

VIII. CONCLUSION

In this paper, our goal was to analyze the current status and future prospects of a light neutralino DM ($M_{\tilde{\chi}_1^0} < M_{H_{125}}/2$) within the NMSSM framework. Previous studies of light neutralinos in the MSSM have shown that such scenarios could be entirely probed at future direct detection experiments such as Xenon-nT, with potential complementary signatures in invisible Higgs decays. We therefore concentrated only on regions of the NMSSM with features clearly distinct from those of the MSSM regions explored before. In particular we focused our study on the case where a new light singlet Higgs was present (with $M_{A_1}, M_{H_1} < 122$ GeV). Such scenarios can provide a new mechanism for efficient neutralino annihilation in the early Universe via the exchange of a light scalar and/or pseudoscalar Higgs at roughly twice the mass of the neutralino DM. Thus in the NMSSM framework neutralino DM at the GeV scale can satisfy the relic density constraint.

After imposing relevant current constraints from collider and astrophysical experiments, the allowed parameter

¹⁴The model parameters for these benchmark points are shown in Table XIII as an Appendix.

TABLE XII. Comparison of the expected number of signal events in the WZ and WH_{125} mediated $3l + \cancel{E}_T$ channels after all cuts in the accumulated data set at the HL-LHC and the HE-LHC for the benchmark points, $BP_A, BP_B, BP_C, BP_D, BP_E, BP_F, BP_G, BP_H$ and BP_I , chosen from the allowed parameter space. BP_A, BP_B and BP_C are also shown in Figs. 15 and 16. For each case, the signal significance is shown in parenthesis. The input parameters of these benchmark points are tabulated in Appendix.

Benchmark point (M_2, μ) [in GeV]	WZ mediated		WH_{125} mediated	
	HL-LHC	HE-LHC	HL-LHC	HE-LHC
BP_A (1244, 717)	13 (3.8)	180 (14)	4 (0.4)	23 (6.6)
BP_B (400, 717)	7 (1.5)	86 (4.4)	63 (5.3)	272 (34)
BP_C (200, 403)	7 (1.3)	65 (2.1)	131 (8.8)	388 (48)
BP_D (952, 585)	20 (6.1)	231 (18)	8 (1.0)	35 (9.8)
BP_E (696, 518)	23 (7.0)	408 (20)	12 (1.2)	36 (10)
BP_F (555, 571)	28 (8.6)	418 (21)	18 (2.1)	79 (22)
BP_G (396, 515)	23 (5.2)	233 (12)	78 (5.3)	206 (27)
BP_H (204, 302)	17 (3.4)	167 (5.3)	125 (8.4)	368 (45)
BP_I (210, 262)	27 (5.3)	257 (8.1)	110 (7.4)	321 (40)

space of the model was identified. This parameter space features both a singlino- dominated LSP and a singletlike light Higgs. We showed that direct detection experiments and Higgs invisible width measurements at future colliders such at the ILC, CEPC and FCC have the potential to probe some of the model's parameter space, however two regions in particular remain out of reach. The first correspond to a neutralino with a mass below about 10 GeV where not only direct detection experiments lose their sensitivity but also where the Higgs invisible width can often be very small due to the singlino nature of the LSP. The second had a LSP mass near 62 GeV. For such a neutralino with a mass close to $M_{H_{125}}/2$, the relic density constraint can be satisfied even when the coupling of the neutralino LSP to the Higgs is strongly suppressed, thus reducing the direct detection signal as well as the Higgs invisible width. A significant fraction of the first region is also out of reach of searches for light scalars/pseudoscalars in SM-like Higgs decays at the future HL-LHC since those searches which typically involve a decay channel of a light Higgs into b-quarks lose their sensitivity when $M_{A_1, H_1} \lesssim 11$ GeV, which in our framework is linked to $M_{DM} < 5.5$ GeV. Thus a large fraction of the NMSSM parameter space with light neutralinos will remain out of reach of these future searches.

We found that these difficult-to-probe regions came with light electroweakinos, in particular with NLSP winos barely above 100 GeV or a NLSP Higgsino as light as

400 GeV, hence have the potential to be discovered at future runs of the LHC. After recasting and validating the current searches for light electroweakinos in the $3l + \cancel{E}_T$ final state from neutralino-chargino pairs in the WZ and WH_{125} channel, we investigated how these searches could probe the allowed parameter space of the model at the future high-luminosity and high-energy extension of the LHC. We showed that over a wide range of parameters, the doublet Higgsino could be probed at the HL-LHC via the WZ mediated channel, at least at the 2σ level, but for the most part even at the 5σ level. Moreover, we found that the WH_{125} mediated channel was truly complementary particularly in the wino NLSP region ($M_2 < \mu$) where the WZ channel had the least power. We found that over almost all the allowed NMSSM parameter space with a light LSP, experiments at the HL-LHC would be able to discover (5σ) SUSY via at least one of the two channels. We have limited our study to the golden $3l + \cancel{E}_T$ signal from electroweakino production. It may be worth examining other signal channels which occur at larger rates, but also have larger backgrounds.

The higher energy and luminosity available at the HE-LHC guarantees discovery via both the WZ and WH_{125} mediated trilepton channels over essentially the entire allowed parameter space. We also highlighted some regions where additional search channels, involving the decays of neutralinos into light scalar/pseudoscalar Higgses could offer distinctive probes of the NMSSM electroweakino sector. The tools developed for this analysis are not restricted to NMSSM scenarios under consideration and the recasting presented here can be applied to other prospective studies of electroweakino searches at the HL-LHC and HE-LHC where the LSP neutralinos can be heavier than 60 GeV.

ACKNOWLEDGMENTS

We thank Jason Kumar for reminding us about the CMB constraints on light dark matter. We thank Amit Adhikary, Rhitaja Sengupta and Prabhat Solanki for the helpful discussions. This work was supported in part by the CNRS LIA-THEP (Theoretical High EnergyPhysics) and the INFRE-HEPNET (IndoFrench Network on High Energy Physics) of CEFIPRA/IFCPAR (Indo-French Centre for the Promotion of Advanced Research). The work of B. B. is supported by the Department of Science and Technology, Government of India, under the Grant Agreement No. IFA13-PH-75 (INSPIRE Faculty Award). The work of D. S. is supported by the National Science Foundation under Grant No. PHY- 1915147. The work of R. M. G. is supported by the Department of Science and Technology, India under Grant No. SR/S2/JCB-64/2007. B. B., R. M. G. and R. K. B. acknowledge the hospitality at LAPTh where a part of this work was carried out. X. T. thanks the Centre for High Energy Physics, Indian Institute of Science where this work was begun for its hospitality, and also the Infosys Foundation for making this visit possible.

APPENDIX: BENCHMARK POINTS

TABLE XIII. The input parameters corresponding to the benchmark points considered in this paper.

Benchmark points	Input parameters
BP_A	$\lambda = 0.3, \kappa = 0.01, \tan\beta = 9.5, A_\lambda = 6687 \text{ GeV}, A_\kappa = 5.2 \text{ GeV},$ $\mu = 717 \text{ GeV}, M_2 = 1244 \text{ GeV}, M_3 = 2301 \text{ GeV}$
BP_B	$\lambda = 0.44, \kappa = 0.02, \tan\beta = 11.8, A_\lambda = 8894 \text{ GeV}, A_\kappa = -57 \text{ GeV},$ $\mu = 717 \text{ GeV}, M_2 = 400 \text{ GeV}, M_3 = 4323 \text{ GeV}$
BP_C	$\lambda = 0.08, \kappa = 3 \times 10^{-4}, \tan\beta = 18, A_\lambda = 6563 \text{ GeV}, A_\kappa = -7.9 \text{ GeV},$ $\mu = 403 \text{ GeV}, M_2 = 200 \text{ GeV}, M_3 = 3080 \text{ GeV}$
BP_D	$\lambda = 0.44, \kappa = 0.02, \tan\beta = 15.6, A_\lambda = 585 \text{ GeV}, A_\kappa = 9501 \text{ GeV},$ $\mu = 585 \text{ GeV}, M_2 = 952 \text{ GeV}, M_3 = 4457 \text{ GeV}$
BP_E	$\lambda = 0.27, \kappa = 0.02, \tan\beta = 11.6, A_\lambda = 5875 \text{ GeV}, A_\kappa = 12 \text{ GeV},$ $\mu = 518 \text{ GeV}, M_2 = 696 \text{ GeV}, M_3 = 3634 \text{ GeV}$
BP_F	$\lambda = 0.30, \kappa = 0.01, \tan\beta = 11.2, A_\lambda = 6319 \text{ GeV}, A_\kappa = 17 \text{ GeV},$ $\mu = 571 \text{ GeV}, M_2 = 555 \text{ GeV}, M_3 = 2687 \text{ GeV}$
BP_G	$\lambda = 0.42, \kappa = 0.02, \tan\beta = 15.9, A_\lambda = 8638 \text{ GeV}, A_\kappa = 43.4 \text{ GeV},$ $\mu = 515 \text{ GeV}, M_2 = 396 \text{ GeV}, M_3 = 2903 \text{ GeV}$
BP_H	$\lambda = 0.02, \kappa = 7 \times 10^{-5}, \tan\beta = 25.5, A_\lambda = 7348 \text{ GeV}, A_\kappa = -7.3 \text{ GeV},$ $\mu = 302 \text{ GeV}, M_2 = 204 \text{ GeV}, M_3 = 2239 \text{ GeV}$
BP_I	$\lambda = 0.02, \kappa = 6 \times 10^{-5}, \tan\beta = 27.6, A_\lambda = 6924 \text{ GeV}, A_\kappa = -5.7 \text{ GeV},$ $\mu = 262 \text{ GeV}, M_2 = 210 \text{ GeV}, M_3 = 2217 \text{ GeV}$

- [1] G. Aad *et al.*, Combined Measurement of the Higgs Boson Mass in pp Collisions at $\sqrt{s} = 7$ and 8 TeV with the ATLAS and CMS Experiments, *Phys. Rev. Lett.* **114**, 191803 (2015).
- [2] K. Kawagoe and M. M. Nojiri, Discovery of supersymmetry with degenerated mass spectrum, *Phys. Rev. D* **74**, 115011 (2006).
- [3] G. F. Giudice, T. Han, K. Wang, and L.-T. Wang, Nearly degenerate gauginos and dark matter at the LHC, *Phys. Rev. D* **81**, 115011 (2010).
- [4] T. J. LeCompte and S. P. Martin, Large Hadron Collider reach for supersymmetric models with compressed mass spectra, *Phys. Rev. D* **84**, 015004 (2011).
- [5] H. Murayama, Y. Nomura, S. Shirai, and K. Tobioka, Compact supersymmetry, *Phys. Rev. D* **86**, 115014 (2012).
- [6] H. K. Dreiner, M. Kramer, and J. Tattersall, How low can SUSY go? Matching, monojets and compressed spectra, *Europhys. Lett.* **99**, 61001 (2012).
- [7] B. Bhattacharjee and K. Ghosh, Degenerate SUSY search at the 8 TeV LHC, 2012.
- [8] K. Rolbiecki and K. Sakurai, Constraining compressed supersymmetry using leptonic signatures, *J. High Energy Phys.* **10** (2012) 071.
- [9] B. Bhattacharjee, A. Choudhury, K. Ghosh, and S. Poddar, Compressed supersymmetry at 14 TeV LHC, *Phys. Rev. D* **89**, 037702 (2014).
- [10] K. Tobioka, R. Kitano, and H. Murayama, Enhanced Higgs mass in compact supersymmetry, *J. High Energy Phys.* **04** (2016) 025.
- [11] J. Dutta, P. Konar, S. Mondal, B. Mukhopadhyaya, and S. K. Rai, A revisit to a compressed supersymmetric spectrum with 125 GeV Higgs, *J. High Energy Phys.* **01** (2016) 051.
- [12] A. Delgado, A. Martin, and N. Raj, Extending the reach of compressed gluinos at the LHC, *Phys. Rev. D* **94**, 115010 (2016).
- [13] D. Chowdhury, K. M. Patel, X. Tata, and S. K. Vempati, Indirect searches of the degenerate MSSM, *Phys. Rev. D* **95**, 075025 (2017).
- [14] N. Nagata, H. Otono, and S. Shirai, Cornering Compressed Gluino at the LHC, *J. High Energy Phys.* **03** (2017) 025.
- [15] M. Chakraborti, U. Chattopadhyay, and S. Poddar, How light a Higgsino or a wino dark matter can become in a compressed scenario of MSSM, *J. High Energy Phys.* **09** (2017) 064.
- [16] J. Dutta, P. Konar, S. Mondal, B. Mukhopadhyaya, and S. K. Rai, Search for a compressed supersymmetric spectrum with a light gravitino, *J. High Energy Phys.* **09** (2017) 026.
- [17] K. L. Chan, U. Chattopadhyay, and P. Nath, Naturalness, weak scale supersymmetry and the prospect for the

- observation of supersymmetry at the Tevatron and at the CERN LHC, *Phys. Rev. D* **58**, 096004 (1998).
- [18] H. Baer, V. Barger, P. Huang, A. Mustafayev, and X. Tata, Radiative Natural Supersymmetry with a 125 GeV Higgs Boson, *Phys. Rev. Lett.* **109**, 161802 (2012).
- [19] M. Aaboud *et al.*, Search for electroweak production of supersymmetric states in scenarios with compressed mass spectra at $\sqrt{s} = 13$ TeV with the atlas detector, *Phys. Rev. D* **97**, 052010 (2018).
- [20] G. Aad *et al.*, Searches for electroweak production of supersymmetric particles with compressed mass spectra in $\sqrt{s} = 13$ TeV pp collisions with the ATLAS detector, *Phys. Rev. D* **101**, 052005 (2020).
- [21] A. M. Sirunyan *et al.*, Search for new physics in events with two soft oppositely charged leptons and missing transverse momentum in proton-proton collisions at $\sqrt{s} = 13$ TeV, *Phys. Lett. B* **782**, 440 (2018).
- [22] M. Carena, J. Osborne, N. R. Shah, and C. E. M. Wagner, Supersymmetry and LHC missing energy signals, *Phys. Rev. D* **98**, 115010 (2018).
- [23] M. Carena, J. Osborne, N. R. Shah, and C. E. M. Wagner, Return of the WIMP: Missing energy signals and the Galactic Center excess, *Phys. Rev. D* **100**, 055002 (2019).
- [24] R. K. Barman, G. Belanger, B. Bhattacharjee, R. Godbole, G. Mendiratta, and D. Sengupta, Invisible decay of the Higgs boson in the context of a thermal and nonthermal relic in MSSM, *Phys. Rev. D* **95**, 095018 (2017).
- [25] U. Ellwanger, C. Hugonie, and A. M. Teixeira, The Next-to-Minimal Supersymmetric Standard Model, *Phys. Rep.* **496**, 1 (2010).
- [26] A. Djouadi, U. Ellwanger, and A. M. Teixeira, Phenomenology of the constrained NMSSM, *J. High Energy Phys.* **04** (2009) 031.
- [27] A. Djouadi, P. Janot, J. Kalinowski, and P. M. Zerwas, SUSY decays of Higgs particles, *Phys. Lett. B* **376**, 220 (1996).
- [28] G. Belanger, F. Boudjema, A. Cottrant, R. M. Godbole, and A. Semenov, The MSSM invisible Higgs in the light of dark matter and $g-2$, *Phys. Lett. B* **519**, 93 (2001).
- [29] D. A. Vasquez, G. Belanger, R. M. Godbole, and A. Pukhov, The Higgs boson in the MSSM in light of the LHC, *Phys. Rev. D* **85**, 115013 (2012).
- [30] B. Ananthanarayan, J. Lahiri, P. N. Pandita, and M. Patra, Invisible decays of the lightest Higgs boson in supersymmetric models, *Phys. Rev. D* **87**, 115021 (2013).
- [31] D. Hooper and T. Plehn, Supersymmetric dark matter: How light can the LSP be? *Phys. Lett. B* **562**, 18 (2003).
- [32] G. Belanger, F. Boudjema, A. Cottrant, A. Pukhov, and S. Rosier-Lees, Lower limit on the neutralino mass in the general MSSM, *J. High Energy Phys.* **03** (2004) 012.
- [33] D. Feldman, Z. Liu, and P. Nath, Low mass neutralino Dark Matter in the MSSM with constraints from $B_s \rightarrow \mu^+ \mu^-$ and Higgs search limits, *Phys. Rev. D* **81**, 117701 (2010).
- [34] L. Calibbi, T. Ota, and Y. Takahashi, Light neutralino in the MSSM: A playground for dark matter, flavor physics and collider experiments, *J. High Energy Phys.* **07** (2011) 013.
- [35] C. Boehm, P. S. Bhupal Dev, A. Mazumdar, and E. Pukartas, Naturalness of light neutralino Dark Matter in pMSSM after LHC, XENON100 and Planck data, *J. High Energy Phys.* **06** (2013) 113.
- [36] G. Belanger, G. D. La Rochelle, B. Dumont, R. M. Godbole, S. Kraml, and S. Kulkarni, LHC constraints on light neutralino dark matter in the MSSM, *Phys. Lett. B* **726**, 773 (2013).
- [37] K. Hamaguchi and K. Ishikawa, Prospects for Higgs- and Z-resonant neutralino Dark Matter, *Phys. Rev. D* **93**, 055009 (2016).
- [38] D. A. Vasquez, G. Belanger, C. Boehm, A. Pukhov, and J. Silk, Can neutralinos in the MSSM and NMSSM scenarios still be light? *Phys. Rev. D* **82**, 115027 (2010).
- [39] J.-J. Cao, K.-i. Hikasa, W. Wang, J. M. Yang, K.-i. Hikasa, W.-Y. Wang, and J. M. Yang, Light dark matter in NMSSM and implication on Higgs phenomenology, *Phys. Lett. B* **703**, 292 (2011).
- [40] D. A. Vasquez, G. Belanger, and C. Boehm, Astrophysical limits on light NMSSM neutralinos, *Phys. Rev. D* **84**, 095008 (2011).
- [41] J. Kozaczkuk and S. Profumo, Light NMSSM neutralino dark matter in the wake of CDMS II and a 126 GeV Higgs boson, *Phys. Rev. D* **89**, 095012 (2014).
- [42] U. Ellwanger and C. Hugonie, The semi-constrained NMSSM satisfying bounds from the LHC, LUX and Planck, *J. High Energy Phys.* **08** (2014) 046.
- [43] D. Barducci, G. Belanger, C. Hugonie, and A. Pukhov, Status and prospects of the NMSSM after LHC Run-1, *J. High Energy Phys.* **01** (2016) 050.
- [44] U. Ellwanger and C. Hugonie, The Higgsino-singlino sector of the NMSSM: Combined constraints from dark matter and the LHC, *Eur. Phys. J. C* **78**, 735 (2018).
- [45] J. Cao, C. Han, L. Wu, P. Wu, and J. M. Yang, A light SUSY dark matter after CDMS-II, LUX and LHC Higgs data, *J. High Energy Phys.* **05** (2014) 056.
- [46] G. Belanger, F. Boudjema, C. Hugonie, A. Pukhov, and A. Semenov, Relic density of dark matter in the NMSSM, *J. Cosmol. Astropart. Phys.* **09** (2005) 001.
- [47] F. Mahmoudi, J. Rathsman, O. Stal, and L. Zeune, Light Higgs bosons in phenomenological NMSSM, *Eur. Phys. J. C* **71**, 1608 (2011).
- [48] C. Cheung, M. Papucci, D. Sanford, N. R. Shah, and K. M. Zurek, NMSSM interpretation of the galactic center excess, *Phys. Rev. D* **90**, 075011 (2014).
- [49] F. Domingo, U. Ellwanger, E. Fullana, C. Hugonie, and M.-A. Sanchis-Lozano, Radiative Upsilon decays and a light pseudoscalar Higgs in the NMSSM, *J. High Energy Phys.* **01** (2009) 061.
- [50] D. G. Cerdeno, P. Ghosh, and C. B. Park, Probing the two light Higgs scenario in the NMSSM with a low-mass pseudoscalar, *J. High Energy Phys.* **06** (2013) 031.
- [51] A. M. Sirunyan *et al.*, Search for an exotic decay of the Higgs boson to a pair of light pseudoscalars in the final state with two b quarks and two τ leptons in proton-proton collisions at $\sqrt{s} = 13$ TeV, *Phys. Lett. B* **785**, 462 (2018).
- [52] A. M. Sirunyan *et al.*, Search for an exotic decay of the Higgs boson to a pair of light pseudoscalars in the final state of two muons and two τ leptons in proton-proton collisions at $\sqrt{s} = 13$ TeV, *J. High Energy Phys.* **11** (2018) 018.

- [53] K. Wang and J. Zhu, Funnel annihilations of light dark matter and the invisible decay of the Higgs boson, *Phys. Rev. D* **101**, 095028 (2020).
- [54] M. Guchait and J. Kumar, Light Higgs Bosons in NMSSM at the LHC, *Int. J. Mod. Phys. A* **31**, 1650069 (2016).
- [55] M. Guchait and J. Kumar, Diphoton Signal of light pseudoscalar in NMSSM at the LHC, *Phys. Rev. D* **95**, 035036 (2017).
- [56] M. Guchait and A. Roy, Light singlino dark matter at the LHC, *Phys. Rev. D* **102**, 075023 (2020).
- [57] V. Khachatryan *et al.*, Search for a very light NMSSM Higgs boson produced in decays of the 125 GeV scalar boson and decaying into τ leptons in pp collisions at $\sqrt{s} = 8$ TeV, *J. High Energy Phys.* **01** (2016) 079.
- [58] V. Khachatryan *et al.*, Search for light bosons in decays of the 125 GeV Higgs boson in proton-proton collisions at $\sqrt{s} = 8$ TeV, *J. High Energy Phys.* **10** (2017) 076.
- [59] V. Khachatryan *et al.*, A search for pair production of new light bosons decaying into muons, *Phys. Lett. B* **752**, 146 (2016).
- [60] U. Ellwanger, Testing the Higgsino-Singlino sector of the NMSSM with trileptons at the LHC, *J. High Energy Phys.* **11** (2013) 108.
- [61] F. Domingo, J. S. Kim, V. Martin-Lozano, P. Martin-Ramiro, and R. Ruiz de Austri, Confronting the neutralino and chargino sector of the NMSSM to the multi-lepton searches at the LHC, 2018.
- [62] A. M. Sirunyan *et al.*, Combined search for electroweak production of charginos and neutralinos in proton-proton collisions at $\sqrt{s} = 13$ TeV, *J. High Energy Phys.* **03** (2018) 160.
- [63] E. Aprile *et al.*, Dark Matter Search Results from a One Ton-Year Exposure of XENON1T, *Phys. Rev. Lett.* **121**, 111302 (2018).
- [64] A. Albert *et al.*, Searching for Dark Matter annihilation in recently discovered Milky Way satellites with Fermi-LAT, *Astrophys. J.* **834**, 110 (2017).
- [65] M. Cepeda *et al.*, Report from Working Group 2: Higgs Physics at the HL-LHC and HE-LHC, *CERN Yellow Reports: Monographs* **7**, 221 (2019).
- [66] U. Ellwanger, C. Hugonie, and A. M. Teixeira, The next-to-minimal supersymmetric standard model, *Phys. Rep.* **496**, 1 (2010).
- [67] S. Baum, K. Freese, N. R. Shah, and B. Shakya, NMSSM Higgs boson search strategies at the LHC and the mono-Higgs signature in particular, *Phys. Rev. D* **95**, 115036 (2017).
- [68] M. Carena, H. E. Haber, I. Low, N. R. Shah, and C. E. M. Wagner, Alignment limit of the NMSSM Higgs sector, *Phys. Rev. D* **93**, 035013 (2016).
- [69] A. Djouadi, J. Kalinowski, and M. Spira, HDECAY: A program for Higgs boson decays in the standard model and its supersymmetric extension, *Comput. Phys. Commun.* **108**, 56 (1998).
- [70] U. Ellwanger, J. F. Gunion, and C. Hugonie, NMHDECAY: A Fortran code for the Higgs masses, couplings and decay widths in the NMSSM, *J. High Energy Phys.* **02** (2005) 066.
- [71] U. Ellwanger and C. Hugonie, NMHDECAY2.0: An updated program for sparticle masses, Higgs masses, couplings and decay widths in the NMSSM, *Comput. Phys. Commun.* **175**, 290 (2006).
- [72] F. Domingo and U. Ellwanger, Updated constraints from B physics on the MSSM and the NMSSM, *J. High Energy Phys.* **12** (2007) 090.
- [73] G. Degrandi and P. Slavich, On the radiative corrections to the neutral Higgs boson masses in the NMSSM, *Nucl. Phys.* **B825**, 119 (2010).
- [74] B. C. Allanach, A. Djouadi, J. L. Kneur, W. Porod, and P. Slavich, Precise determination of the neutral Higgs boson masses in the MSSM, *J. High Energy Phys.* **09** (2004) 044.
- [75] S. Heinemeyer, W. Hollik, H. Rzehak, and G. Weiglein, The Higgs sector of the complex MSSM at two-loop order: QCD contributions, *Phys. Lett. B* **652**, 300 (2007).
- [76] S. Borowka, T. Hahn, S. Heinemeyer, G. Heinrich, and W. Hollik, Renormalization scheme dependence of the two-loop QCD corrections to the neutral Higgs-boson masses in the MSSM, *Eur. Phys. J. C* **75**, 424 (2015).
- [77] G. Abbiendi *et al.*, Search for chargino and neutralino production at $s^{*}(1/2) = 192 - \text{GeV}$ to 209 GeV at LEP, *Eur. Phys. J. C* **35**, 1 (2004).
- [78] N. Aghanim *et al.*, Planck 2018 results. VI. Cosmological parameters, *Astron. Astrophys.* **641**, A6 (2018).
- [79] G. Bélanger, F. Boudjema, A. Pukhov, and A. Semenov, micrOMEGAs4.1: Two dark matter candidates, *Comput. Phys. Commun.* **192**, 322 (2015).
- [80] G. Belanger, F. Boudjema, A. Pukhov, and A. Semenov, micrOMEGAs: A program for calculating the relic density in the MSSM, *Comput. Phys. Commun.* **149**, 103 (2002).
- [81] T. Moroi and L. Randall, Wino cold dark matter from anomaly mediated SUSY breaking, *Nucl. Phys.* **B570**, 455 (2000).
- [82] G. B. Gelmini and P. Gondolo, Neutralino with the right cold dark matter abundance in (almost) any supersymmetric model, *Phys. Rev. D* **74**, 023510 (2006).
- [83] H. Baer, K.-Y. Choi, J. E. Kim, and L. Roszkowski, Dark matter production in the early Universe: Beyond the thermal WIMP paradigm, *Phys. Rep.* **555**, 1 (2015).
- [84] Y. Amhis *et al.*, Averages of b -hadron, c -hadron, and τ -lepton properties as of summer 2016, *Eur. Phys. J. C* **77**, 895 (2017).
- [85] R. Aaij *et al.*, Measurement of the $B_s^0 \rightarrow \mu^+\mu^-$ Branching Fraction and Effective Lifetime and Search for $B^0 \rightarrow \mu^+\mu^-$ Decays, *Phys. Rev. Lett.* **118**, 191801 (2017).
- [86] G. Belanger, F. Boudjema, A. Goudelis, A. Pukhov, and B. Zaldivar, micrOMEGAs5.0: Freeze-in, *Comput. Phys. Commun.* **231**, 173 (2018).
- [87] G. Belanger, F. Boudjema, A. Pukhov, and A. Semenov, micrOMEGAs: Version 1.3, *Comput. Phys. Commun.* **174**, 577 (2006).
- [88] V. Khachatryan *et al.*, Constraints on the Higgs boson width from off-shell production and decay to Z-boson pairs, *Phys. Lett. B* **736**, 64 (2014).
- [89] R. M. Godbole, M. Guchait, K. Mazumdar, S. Moretti, and D. P. Roy, Search for ‘invisible’ Higgs signals at LHC via associated production with gauge bosons, *Phys. Lett. B* **571**, 184 (2003).
- [90] D. Ghosh, R. Godbole, M. Guchait, K. Mohan, and D. Sengupta, Looking for an invisible Higgs signal at the LHC, *Phys. Lett. B* **725**, 344 (2013).

- [91] A. Djouadi, O. Lebedev, Y. Mambrini, and J. Quevillon, Implications of LHC searches for Higgs–portal dark matter, *Phys. Lett. B* **709**, 65 (2012).
- [92] O. J. P. Eboli and D. Zeppenfeld, Observing an invisible Higgs boson, *Phys. Lett. B* **495**, 147 (2000).
- [93] Search for invisible Higgs boson decays with vector boson fusion signatures with the ATLAS detector using an integrated luminosity of 139 fb^{-1} , Technical Report No. ATLAS-CONF-2020-008, CERN, Geneva, 2020.
- [94] G. Aad *et al.*, Constraints on new phenomena via Higgs boson couplings and invisible decays with the ATLAS detector, *J. High Energy Phys.* **11** (2015) 206.
- [95] A. M. Sirunyan *et al.*, Search for invisible decays of a Higgs boson produced through vector boson fusion in proton-proton collisions at $\sqrt{s} = 13 \text{ TeV}$, *Phys. Lett. B* **793**, 520 (2019).
- [96] S. Dawson *et al.*, Working Group Report: Higgs Boson, in Community Summer Study 2013: Snowmass on the Mississippi (2013).
- [97] M. Aaboud *et al.*, Search for squarks and gluinos in final states with hadronically decaying τ -leptons, jets, and missing transverse momentum using pp collisions at $\sqrt{s} = 13 \text{ TeV}$ with the ATLAS detector, *Phys. Rev. D* **99**, 012009 (2019).
- [98] A. M. Sirunyan *et al.*, Search for supersymmetry in proton-proton collisions at 13 TeV in final states with jets and missing transverse momentum, *J. High Energy Phys.* **10** (2019) 244.
- [99] M. Aaboud *et al.*, Search for Higgs boson decays into a pair of light bosons in the $bb\mu\mu$ final state in pp collision at $\sqrt{s} = 13 \text{ TeV}$ with the ATLAS detector, *Phys. Lett. B* **790**, 1 (2019).
- [100] D. Alves, Simplified models for LHC new physics searches, *J. Phys. G* **39**, 105005 (2012).
- [101] Search for electroweak production of charginos and sleptons decaying in final states with two leptons and missing transverse momentum in $\sqrt{s} = 13 \text{ TeV}$ pp collisions using the ATLAS detector, Technical Report No. ATLAS-CONF-2019-008, CERN, Geneva, 2019.
- [102] E. Aprile *et al.*, Constraining the Spin-Dependent WIMP-Nucleon Cross Sections with XENON1T, *Phys. Rev. Lett.* **122**, 141301 (2019).
- [103] C. Amole *et al.*, Dark matter search results from the complete exposure of the PICO-60 C_3F_8 bubble chamber, *Phys. Rev. D* **100**, 022001 (2019).
- [104] A. Natarajan, A closer look at CMB constraints on WIMP dark matter, *Phys. Rev. D* **85**, 083517 (2012).
- [105] M. Ibe, H. Murayama, and T. T. Yanagida, Breit-Wigner enhancement of Dark Matter annihilation, *Phys. Rev. D* **79**, 095009 (2009).
- [106] E. Aprile *et al.*, Physics reach of the XENON1T dark matter experiment, *J. Cosmol. Astropart. Phys.* **04** (2016) 027.
- [107] M. Dong *et al.*, CEPC Conceptual Design Report: Volume 2—Physics & Detector, 2018.
- [108] Projected performance of Higgs analyses at the HL-LHC for ECFA 2016, Technical Report No. CMS-PAS-FTR-16-002, CERN, Geneva, 2017.
- [109] O. Cerri, M. de Gruttola, M. Pierini, A. Podo, and G. Rolandi, Study the effect of beam energy spread and detector resolution on the search for Higgs boson decays to invisible particles at a future e^+e^- circular collider, *Eur. Phys. J. C* **77**, 116 (2017).
- [110] D. M. Asner *et al.*, ILC Higgs white paper, in *Proceedings, 2013 Community Summer Study on the Future of U.S. Particle Physics: Snowmass on the Mississippi (CSS2013): Minneapolis, MN, USA, 2013* (2013).
- [111] Higgs measurements at FCC-hh, Technical Report No. CERN-ACC-2018-0045, CERN, Geneva, 2018.
- [112] J. R. Ellis, A. Ferstl, and K. A. Olive, Exploration of elastic scattering rates for supersymmetric dark matter, *Phys. Rev. D* **63**, 065016 (2001).
- [113] J. R. Ellis, A. Ferstl, and K. A. Olive, Reevaluation of the elastic scattering of supersymmetric dark matter, *Phys. Lett. B* **481**, 304 (2000).
- [114] H. Baer, A. Mustafayev, E.-K. Park, and X. Tata, Target dark matter detection rates in models with a well-tempered neutralino, *J. Cosmol. Astropart. Phys.* **01** (2007) 017.
- [115] P. Huang and C. E. M. Wagner, Blind spots for neutralino Dark Matter in the MSSM with an intermediate m_A , *Phys. Rev. D* **90**, 015018 (2014).
- [116] P. Huang, R. A. Roglans, D. D. Spiegel, Y. Sun, and C. E. M. Wagner, Constraints on supersymmetric dark matter for heavy scalar superpartners, *Phys. Rev. D* **95**, 095021 (2017).
- [117] S. Baum, M. Carena, N. R. Shah, and C. E. M. Wagner, Higgs portals for thermal Dark Matter. EFT perspectives and the NMSSM, *J. High Energy Phys.* **04** (2018) 069.
- [118] P. Cushman *et al.*, Working Group Report: WIMP Dark Matter Direct Detection, in *Community Summer Study 2013: Snowmass on the Mississippi* (2013).
- [119] E. Aprile *et al.*, Projected WIMP sensitivity of the XENONnT Dark Matter Experiment (2020).
- [120] Search for Supersymmetry at the high luminosity LHC with the ATLAS experiment, Technical Report No. ATLAS-PHYS-PUB-2014-010, CERN, Geneva, 2014.
- [121] Prospects for searches for staus, charginos and neutralinos at the high luminosity LHC with the ATLAS Detector, Technical Report No. ATLAS-PHYS-PUB-2018-048, CERN, Geneva, 2018.
- [122] T. Sjostrand, L. Lonnblad, and S. Mrenna, PYTHIA6.2: Physics and manual, [arXiv:hep-ph/0108264](https://arxiv.org/abs/hep-ph/0108264).
- [123] T. Sjostrand, S. Ask, J. R. Christiansen, R. Corke, N. Desai, P. Ilten, S. Mrenna, S. Prestel, C. O. Rasmussen, and P. Z. Skands, An Introduction to PYTHIA8.2, *Comput. Phys. Commun.* **191**, 159 (2015).
- [124] W. Beenakker, R. Hopker, M. Spira, and P. M. Zerwas, Squark Production at the Tevatron, *Phys. Rev. Lett.* **74**, 2905 (1995).
- [125] W. Beenakker, R. Hopker, M. Spira, and P. M. Zerwas, Gluino pair production at the tevatron, *Z. Phys. C* **69**, 163 (1995).
- [126] W. Beenakker, R. Hopker, and M. Spira, PROSPINO: A program for the production of supersymmetric particles in next-to-leading order QCD, 1996.
- [127] Technical Design Report for the ATLAS inner tracker strip detector, Technical Report, 2017.
- [128] J. Alwall, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni, O. Mattelaer, H. S. Shao, T. Stelzer, P. Torrielli, and M. Zaro, The automated computation of tree-level and

- next-to-leading order differential cross sections, and their matching to parton shower simulations, *J. High Energy Phys.* **07** (2014) 079.
- [129] J. de Favereau, C. Delaere, P. Demin, A. Giammanco, V. Lematre, A. Mertens, and M. Selvaggi, DELPHES3, A modular framework for fast simulation of a generic collider experiment, *J. High Energy Phys.* **02** (2014) 057.
- [130] D. R. Tovey, On measuring the masses of pair-produced semi-invisibly decaying particles at hadron colliders, *J. High Energy Phys.* **04** (2008) 034.
- [131] H. Baer, V. Barger, J. S. Gainer, M. Savoy, D. Sengupta, and X. Tata, Aspects of the same-sign diboson signature from Wino pair production with light Higgsinos at the high luminosity LHC, *Phys. Rev. D* **97**, 035012 (2018).