Identifying a Higgsino-like NLSP in the context of a keV-scale gravitino LSP

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I. INTRODUCTION

In the light of the 13 TeV LHC run 2 results [1,2], both experimentalists and theorists are leaving no stone unturned to interpret results of different supersymmetric (SUSY) scenarios, primarily to ensure no glaring gaps are left in the current search strategies such that the signals may slip through them. Although bounds on sparticle masses from LHC are steadily increasing, they are derived in the context of simplified scenarios. However, generic features on collider signals are helpful to investigate, if such features reflect the spectrum and the composition of the super-particle states.

The *R*-parity conserving minimal supersymmetric standard model (MSSM) ensures a stable, neutral, colorless dark matter (DM) candidate, generally the lightest neutralino $(\tilde{\chi}_1^0)$, which is the lightest SUSY particle (LSP). Depending on its composition, it could be either a democratic admixture of gaugino and Higgsino states or dominantly binolike, winolike, or Higgsino-like. The DM composition faces stringent constraints from direct search data and indirect evidence as well as from relic density measurements by Planck [3]. For example, a bino-dominated $\tilde{\chi}_1^0$ with an appropriate small admixture of Higgsinos can by and large

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be consistent with relic density as well as direct search constraints. However for a winolike LSP, SU (2)-driven annihilation channels lead to strong constraints from γ -ray [4] as well as positron data [5]. A light Higgsino-like LSP is disfavored from direct dark matter searches [6,7]. Conversely, the relic density being inversely proportional to the annihilation cross section, shows an underabundance for wino or Higgsino-like LSP, whereas a binolike LSP can lead to an overabundance unless coannihilation occurs at an adequate rate. Mixed bino-Higgsino or bino-wino dark matter scenarios could be more consistent from these standpoints [8]. The presence of a lighter particle such as a gravitino or an axino as the lightest SUSY particle relaxes these constraints on the composition of the lightest neutralino $\tilde{\chi}_1^0$, which now serves as the next-to-lightest sparticle (NLSP). Gravitinos are the LSP in models like gauge mediated supersymmetry breaking with low scale of SUSY breaking. Here, the gravitino mass scale may be lighter than the MSSM sparticle masses if the scale of SUSY breaking is light enough to allow a light gravitino mass governed by [9–11],

$$m_{\tilde{G}} = \frac{\langle F \rangle}{\sqrt{3}M_{\rm Pl}},\tag{1}$$

where $m_{\tilde{G}}$ is the mass of the gravitino, $\langle F \rangle$ is the SUSY breaking scale, and $M_{\rm Pl}$ is the Planck scale. This means that depending on the SUSY breaking scale $\langle F \rangle$, the gravitino can be as light as \mathcal{O} (keV). A light gravitino with mass of few keV is motivated to be a warm dark matter candidate [12–14]. In this work, we consider the LHC signals of a Higgsino-dominated NLSP, where one has such a light gravitino LSP.

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In this work, we aim to study signatures of a low-lying Higgsino sector in the presence of a light gravitino LSP with emphasis on determining how the NLSP nature can be convincingly identified. To do this, one would like to reconstruct the decay products of the NLSP. As the Higgsino NLSP would decay to a light Higgs or a Z boson, we may be able to observe their properties by appropriately reconstructing the Higgs boson through the b jets arising from its decay as well as the Z boson through the opposite sign dilepton pair from the gauge boson's decay, respectively. We note here a very important and interesting feature of the decay of the NLSP. It is expected that the Z boson arising from the Higgsino-like $\tilde{\chi}_1^0$ decay would be dominantly longitudinal (Goldstone boson), primarily following the equivalence theorem where, after electroweak symmetry breaking, the neutral Goldstone boson constitutes the longitudinal mode of the Z boson responsible for its mass. This property if observed in the decay of the NLSP would exclusively point towards the presence of a Higgsino-like $\tilde{\chi}_{1}^{0}$, helping us identify the nature of the NLSP. The direct production of the electroweak neutralino NLSP would be limited at the LHC as their mass becomes larger. However, the property of the NLSP could still be studied if they are produced in cascade decays of strongly interacting sparticles. We therefore study the effect of including the strong sector in exploring the compositions of the NLSP as well as from the direct production of the low-lying electroweakinos (still allowed by experiments) and propose some new kinematic observables which help identify the NLSP. Thus, the salient points of our study are as follows:

- (i) We consider a naturally compressed low-lying Higgsino sector as well as partially and/or fully compressed spectra with the strongly interacting sparticles sitting above the NLSP. The sparticles decay via cascades to the NLSP, which further decays to a Higgs and a Z boson, thereby giving rise to at least 1b jet and opposite-sign same flavor dileptons along with missing transverse energy in the final state.
- (ii) The characteristic features of a longitudinal Z boson arising from decay of the Higgsino-like $\tilde{\chi}_1^0$ are

studied by utilizing angular variables of the negatively charged lepton. In order to distinguish it from transversely polarized Z bosons coming from other sources, we compare our results with the complementary admixture of NLSP, especially gaugino-dominated neutralinos as well as the SM background.

- (iii) We observe that for a spectrum with a heavy NLSP, reflecting overall compression with respect to the strong sector leads to an increased fraction of the longitudinal mode in the *Z* boson arising from the NLSP decay.
- (iv) New observables enhancing the asymmetry in the angular distributions of the negatively charged lepton have been proposed in order to characterize a longitudinally polarized Z boson in comparison to a transversely polarized Z boson. Such observables distinctly vary, depending on the Higgsino-gaugino admixture of the NLSP, and crucially capture the effect of the equivalence theorem for a heavy NLSP.

The paper is organized as follows. In Sec. II, we discuss the current scenario with the Higgsino NLSP and gravitino LSP followed by the decay properties of the Higgsinos in Sec. III. In Sec. IV, we discuss the experimental status of a Higgsino-like NLSP with a light gravitino LSP at LHC. In Sec. V, we choose some benchmarks to study the available parameter space. We perform the collider study and discuss our results at the high luminosity run of LHC in Sec. VI. In Sec. VII, we distinguish between the features of longitudinal and transverse gauge bosons. Section VIII summarizes the main conclusions of our work.

II. HIGGSINO-DOMINATED NLSP WITH KEV LSP

In our work, we discuss light Higgsino-like NLSP as a possible consequence of a general phenomenological MSSM. Since no hint of SUSY has yet shown up at direct searches, various possible configurations of the lightest neutralino, $\tilde{\chi}_1^0$, leading to distinct signals at colliders are of interest. Such a light Higgsino-like $\tilde{\chi}_1^0$ is characterized by a low ($\leq 800 \text{ GeV}$) μ parameter and heavy bino, wino soft mass parameters, i.e., $|\mu| \ll M_1, M_2.\mu$ in the aforesaid range is also a preferred choice from the angle of naturalness [19–24]. However, $\tilde{\chi}_1^0$ may not be the LSP in many situations. In such cases, there can be several other candidates for LSP such as gravitinos, axinos, sneutrinos, etc.

The gravitino is the spin $\frac{3}{2}$ superpartner of the spin 2 graviton in local SUSY. Upon spontaneous SUSY breaking, there arises a massless Weyl fermion known as the goldstino (\tilde{G}), owing to the breaking of the fermionic generators of SUSY. After electroweak symmetry breaking, the gravitino acquires mass by absorbing the goldstino, which form the spin $\frac{1}{2}$ components of the massive gravitino. We henceforth approximate a light gravitino by the goldstino using the equivalence theorem.

The goldstino (\tilde{G}) Lagrangian is [9],

$$\mathcal{L}_{\text{goldstino}} = i \tilde{G}^{\dagger} \bar{\sigma}^{\mu} \partial_{\mu} \tilde{G} - \frac{1}{\langle F \rangle} \tilde{G} \partial_{\mu} j^{\mu} + \text{c.c.}, \qquad (2)$$

where j^{μ} refers to the supercurrent involving all other sparticles and SM particles. The couplings of the gravitino to fermion-sfermion, gauge boson-gauginos are computed in Ref. [25]. Having said this, we briefly discuss the couplings and decays of a Higgsino-like NLSP in the presence of a light \tilde{G} before moving on to our numerical analysis.

III. HIGGSINO NLSP DECAYS

A Higgsino-like $\tilde{\chi}_1^0$ is characterized by a large Higgsino fraction with suppressed wino and bino fractions, i.e., $\mu < M_1$, M_2 . In the presence of a light \tilde{G} LSP, the Higgsino-like $\tilde{\chi}_1^0$ NLSP decays to either a Higgs (*h*) or a *Z* boson and \tilde{G} . Absence of a large bino component leads to a rather suppressed photon mode unless there is substantial gaugino-bino-Higgsino admixture [16]. However, the photon mode may dominate in case of very light Higgsinos, where the decay to the Higgs or *Z* boson is phase space suppressed. As the coupling of a gravitino to other particles are inversely proportional to its mass($m_{\tilde{G}}$), a lighter gravitino has stronger couplings as compared to a heavier one. For any sparticle \tilde{X} decaying into its SM partner *X* and the gravitino, the width is given by [9]

$$\Gamma(\tilde{X} \to X\tilde{G}) = \frac{m_{\tilde{X}}^{5}}{48\pi M_{P}^{2}m_{\tilde{G}}^{2}} \left(1 - \frac{m_{X}^{2}}{m_{\tilde{X}}^{2}}\right)^{4}, \qquad (3)$$

where $m_{X(\tilde{X})}$ refers to the mass of $X(\tilde{X})$. As we are interested in the decay of the neutralino NLSP to the gravitino, the composition of the lightest neutralino becomes an essential characteristic as it would determine what the NLSP finally decays to. The neutralino mass matrix in the basis (\tilde{B} , \tilde{W}_3 , \tilde{H}_d^0 , \tilde{H}_u^0) is as follows [9]:

$$M^{n} = \begin{pmatrix} M_{1} & 0 & -M_{Z}s_{W}c_{\beta} & M_{Z}s_{W}s_{\beta} \\ 0 & M_{2} & M_{Z}c_{W}c_{\beta} & -M_{Z}c_{W}s_{\beta} \\ -M_{Z}s_{W}c_{\beta} & M_{Z}c_{W}c_{\beta} & 0 & -\mu \\ M_{Z}s_{W}s_{\beta} & -M_{Z}c_{W}s_{\beta} & -\mu & 0 \end{pmatrix}.$$
(4)

Here, $s_W = \sin \theta_W$, $c_W = \cos \theta_W$, where θ_W is the weak mixing angle, whereas $s_\beta = \sin \beta$, $c_\beta = \cos \beta$, where $\tan \beta = \frac{v_u}{v_d}$ refers to the ratio of the vacuum expectation value's of the up-type Higgs doublet (H_u) and the downtype Higgs doublet H_d . Diagonalizing the symmetric mass matrix M^n using a unitary matrix N lead to the neutralino mass eigenstates $\tilde{\chi}_i^0 (i = 1, ..., 4)$,

$$NM^{n}N^{T} = \text{diag}(m_{\tilde{\chi}_{1}^{0}}, m_{\tilde{\chi}_{2}^{0}}, m_{\tilde{\chi}_{2}^{0}}, m_{\tilde{\chi}_{4}^{0}}), \qquad (5)$$

where $m_{\tilde{\chi}_{1}^{0}} < m_{\tilde{\chi}_{2}^{0}} < m_{\tilde{\chi}_{3}^{0}} < m_{\tilde{\chi}_{4}^{0}}$.

The chargino mass matrix M^c in the basis $(\tilde{W}^+, \tilde{H}_u^+)$ is as follows [9]:

$$M^{c} = \begin{pmatrix} M_{2} & \sqrt{2}M_{W}s_{\beta} \\ \sqrt{2}M_{W}c_{\beta} & \mu \end{pmatrix}.$$
 (6)

Since, M^c is not a symmetric matrix, we need two unitary matrices U and V to diagonalize the matrix. Hence,

$$U^* M^c V^{-1} = \operatorname{diag}(m_{\tilde{\chi}^{\pm}}, m_{\tilde{\chi}^{\pm}}), \tag{7}$$

where $m_{\tilde{\chi}_1^{\pm}} < m_{\tilde{\chi}_2^{\pm}}$. In the limit where $\mu \ll M_1, M_2$, there are two nearly degenerate Higgsino-like neutralinos along with a degenerate Higgsino-like chargino, leading to a naturally compressed spectrum. The mass eigenvalues at the tree level are [26,27]

$$m_{\tilde{\chi}_{1}^{\pm}} = |\mu| \left(1 - \frac{M_{W}^{2} \sin 2\beta}{\mu M_{2}} \right) + \mathcal{O}(M_{2}^{-2})$$
$$m_{\tilde{\chi}_{1,2}^{0}} = \pm \mu - \frac{M_{Z}^{2}}{2} (1 \pm \sin 2\beta) \left(\frac{\sin^{2} \theta_{W}}{M_{1}} + \frac{\cos^{2} \theta_{W}}{M_{2}} \right).$$
(8)

In the presence of a light \tilde{G} , the following additional decay modes open up for the Higgsino-like chargino and neutralinos:

$$\begin{split} \tilde{\chi}_1^{\pm} &\to W^{\pm} \tilde{G} \\ \tilde{\chi}_2^0 &\to h \tilde{G}, Z \tilde{G} \\ \tilde{\chi}_1^0 &\to h \tilde{G}, Z \tilde{G}, \end{split}$$

where the Z boson from a neutralino decay is mostly longitudinal. The squared couplings of the Higgsino-like neutralinos and chargino, to the gravitino (\tilde{G}) LSP are [28]

$$|g_{\tilde{G}\tilde{\chi}_{1}^{0}H_{k}}|^{2} = |e_{k}N_{i3} + d_{k}N_{i4}|^{2}(M_{\text{Pl}}m_{\tilde{G}})^{-2},$$

$$|g_{\tilde{G}\tilde{\chi}_{1}^{\pm}H^{\pm}}|^{2} = (|V_{12}^{2}|\cos^{2}\beta + |U_{12}^{2}|\sin^{2}\beta)(M_{\text{Pl}}m_{\tilde{G}})^{-2}, \qquad (9)$$

TABLE I. Relevant range of the input parameters for the parameter-space scan to study the decay probabilities of the lightest neutralino is shown. We keep other parameters at fixed values which include: $M_1 = 2$ TeV, $M_2 = 2$ TeV, $M_3 = 1.917$ TeV, $M_{Q_3} = 2.8$ TeV, $M_{U_3} = 2.8$ TeV, $M_A = 2.5$ TeV, $A_t = 3$ TeV, and $m_{\tilde{G}} = 1$ keV.

Parameters	$ \mu $ (TeV)	$\operatorname{sign}(\mu)$	$\tan\beta$
Values	0.2–1.5	±1	2–45



FIG. 1. Variation of $\tilde{\chi}_1^0$ decay into a Higgs (top panel) or Z boson (bottom panel) along with the \tilde{G} LSP with μ and tan β in the colored palette. The parameters of the scan are listed in Table I.

where i = 1, 2 and k = 1, 2, 3, such that $H_k = h, H, A$, respectively. The coefficients e_k and d_k are as below,

$$e_1 = \cos \alpha, \qquad e_2 = -\sin \alpha, \qquad e_3 = -\sin \beta$$

$$d_1 = -\sin \alpha, \qquad d_2 = -\cos \alpha, \qquad d_3 = \cos \beta, \qquad (10)$$

and N_{ij} refer to the $(ij)^{\text{th}}$ entry of the neutralino mixing matrix N, α is the mixing angle between the *CP*-even Higgs bosons, h and H. In the decoupling limit, i.e., $m_A \gg m_h$, $\beta - \alpha \sim \pi/2$ (where, $0 < \beta < \pi$ and $-\pi < \alpha < 0$), the lightest *CP*-even Higgs boson (h) behaves like the SM Higgs boson [9]. The partial decay widths of the lightest neutralino $\tilde{\chi}_1^0$ are as follows [15,29]:

$$\Gamma(\tilde{\chi}_1^0 \to h\tilde{G}) \propto |N_{14}\sin\alpha - N_{13}\cos\alpha|^2 (M_{\rm Pl}m_{\tilde{G}})^{-2} \qquad (11)$$

$$\Gamma(\tilde{\chi}_1^0 \to Z\tilde{G}) \propto \left(|N_{11}\sin\theta_W - N_{12}\cos\theta_W|^2 + \frac{1}{2} |N_{14}\cos\beta - N_{13}\sin\beta|^2 \right) (M_{\rm Pl}m_{\tilde{G}})^{-2}.$$
(12)

The terms proportional to N_{14} and N_{13} denote the Goldstone couplings.¹ In the decoupling limit, $\sin \alpha = -\cos \beta$ and $\cos \alpha = \sin \beta$; thus, Eq. (11) reduces to

$$\Gamma(\tilde{\chi}^0_1 \to h\tilde{G}) \propto |N_{14}\cos\beta + N_{13}\sin\beta|^2 (M_{\rm Pl}m_{\tilde{G}})^{-2}.$$
 (13)

The interference term between the gaugino and the Higgsino vanishes [30] in the above decay mode due to the polarization states being physical states. We note that for a Higgsino-like $\tilde{\chi}_1^0$, $N_{13} \simeq -N_{14}$ for $\mu > 0$, whereas for $\mu < 0$, $N_{13} \sim N_{14}$ [15]. This leads to an increase in $\Gamma(\tilde{\chi}_1^0 \to h\tilde{G})$ as evident from Eq. (13).

A. Branching ratios

The decay branching ratios of the Higgsino-dominated $\tilde{\chi}_1^0$ NLSP are governed mainly by values of μ and $\tan \beta$. Table I summarizes the relevant parameter ranges for the scan performed using the package SPheno-v3.3.6 [31,32]. In Fig. 1, we show the regions of the parameter space, having the different branching ratios of the $\tilde{\chi}_1^0$. We discuss the salient points of the parameter space as below:

(i) The branching fractions to the Higgs and Z mode decreases with an increase in the gaugino admixture in the NLSP at higher values of μ and $\tan \beta$ (as μ gets closer to the choice of M_1 and M_2 shown in Table I). This defines a range of the parameter space with comparable branching ratios for the Higgs and Z boson decay modes of the $\tilde{\chi}_1^0$ NLSP.

(ii) For
$$|\mu| > 400$$
 GeV,

$$\mathrm{BR}(\tilde{\chi}_1^0 \to h\tilde{G}) \simeq \mathrm{BR}(\tilde{\chi}_1^0 \to Z\tilde{G}),$$

for large values of $\tan \beta$ ($\tan \beta \ge 25$) with small differences depending on $\operatorname{sign}(\mu)$. For $\operatorname{sign}(\mu) = +1$,

¹See the discussion at the beginning of Sec. VII for the decay of the Z boson and the polarization of the gauge bosons.

$$\operatorname{BR}(\tilde{\chi}_1^0 \to hG) \simeq 0.47, \qquad \operatorname{BR}(\tilde{\chi}_1^0 \to ZG) \simeq 0.53,$$

whereas for $sign(\mu) = -1$,

$$\operatorname{BR}(\tilde{\chi}_1^0 \to h\tilde{G}) \simeq 0.54, \qquad \operatorname{BR}(\tilde{\chi}_1^0 \to Z\tilde{G}) \simeq 0.46.$$

(iii) For $\mu < 400$ GeV and $\tan \beta \simeq 5$,

$$\mathrm{BR}(\tilde{\chi}^0_1 \to h \tilde{G}) \simeq 0.30, \qquad \mathrm{BR}(\tilde{\chi}^0_1 \to Z \tilde{G}) \simeq 0.70.$$

due to $N_{13} = -N_{14}$, such that the Z mode dominates over the Higgs mode. Whereas for $-\mu > 400$ GeV and $\tan \beta \simeq 5$,

$$\mathrm{BR}(\tilde{\chi}^0_1 \to h \tilde{G}) \simeq 0.67, \qquad \mathrm{BR}(\tilde{\chi}^0_1 \to Z \tilde{G}) \simeq 0.33,$$

where $N_{13} = N_{14}$ and the Higgs and Z decay modes of the $\tilde{\chi}_1^0$ NLSP dominate over the others, respectively.

In addition, as the $\tilde{\chi}_1^0$ becomes more gauginolike, the additional decay mode of $\gamma \tilde{G}$ would also open up and subsequently dominate the branching probabilities [16].

IV. EXISTING LHC LIMITS

The current bounds on the light Higgsinos as NLSP and \tilde{G} LSP are well studied at LHC for a light gravitino ($m_{\tilde{G}} = 1$ GeV [33]) assuming prompt decays.² The relevant analyses are summarized in Table II, and we list the constraints from LHC on the Higgsinos as well as on the strong sector sparticles as relevant for our study below:

$$\begin{split} \text{BR}(\tilde{\chi}_1^0 \to h\tilde{G}) &\sim 1.0 \colon m_{\tilde{\chi}_1^0} \leq 880 \text{ GeV (ATLAS)}; \\ m_{\tilde{\chi}_1^0} &\leq 760 \text{ GeV (CMS)}. \\ \text{BR}(\tilde{\chi}_1^0 \to Z\tilde{G}) &\sim 1.0 \colon m_{\tilde{\chi}_1^0} \leq 340 \text{ GeV (ATLAS)}. \end{split}$$

Combined exclusion limits on the Higgsino mass from multiple searches at CMS are as follows [17]:

$$\begin{split} & \mathrm{BR}(\tilde{\chi}^0_1 \to h\tilde{G}) \sim 1.0 \colon \ m_{\tilde{\chi}^0_1} \leq 775 \ \mathrm{GeV} \ \mathrm{(CMS)}. \\ & \mathrm{BR}(\tilde{\chi}^0_1 \to Z\tilde{G}) \sim 1.0 \colon \ m_{\tilde{\chi}^0_1} \leq 650 \ \mathrm{GeV} \ \mathrm{(CMS)}. \end{split}$$

TABLE II. List of experimental searches from LHC reinterpreted for Higgsinos relevant for our current study with \tilde{G} LSP. The rate in each final state is the sum of rates in all channels listed in the corresponding rows.

Final state	Contributing channels	ATLAS	CMS
$2/3/4b + \not \! E_T$	$ ilde{\chi}^0_1 ilde{\chi}^\pm_1, ilde{\chi}^0_2 ilde{\chi}^\pm_1, ilde{\chi}^+_1 ilde{\chi}^1, ilde{\chi}^0_1 ilde{\chi}^0_2$	[33]	[17]
$\ell^+\ell^- + \not\!\!\!E_T$	$ ilde{\chi}^0_1 ilde{\chi}^\pm_1, ilde{\chi}^0_2 ilde{\chi}^\pm_1, ilde{\chi}^\pm_1 ilde{\chi}^1, ilde{\chi}^0_1 ilde{\chi}^0_2$		[17]
$\geq 3\ell + \not\!\! E_T$	$ ilde{\chi}^0_1 ilde{\chi}^\pm_1, ilde{\chi}^0_2 ilde{\chi}^\pm_1, ilde{\chi}^\pm_1 ilde{\chi}^1, ilde{\chi}^0_1 ilde{\chi}^0_2$		[17]
$hh + \not\!\!\! E_T$	$\tilde{g}\tilde{g}$		[34]
$4\ell + \not\!\!\! E_T$	$ ilde{\chi}_1^+ ilde{\chi}_1^-, ilde{\chi}_1^\pm ilde{\chi}_2^0$	[35]	
$\geq 2j + \not \!\! E_T$	$\tilde{g}\tilde{g},\tilde{q}\tilde{q}$	[36]	
$b\bar{b} + E_T$	$ ilde{\chi}^0_2 ilde{\chi}^\pm_1$	[37]	
$1\ell + b\bar{b} + \not\!\!E_T$	${ ilde\chi}^0_2 { ilde\chi}^\pm_1$	[37]	
$3\ell + \not\!\!\! E_T$	${ ilde \chi}^0_2 { ilde \chi}^\pm_1$	[37]	
$\ell^{\pm}\ell^{\pm} + \not\!$	${ ilde\chi}^0_2 { ilde\chi}^\pm_1$	[37]	

(ii) Strong sector: Direct limits for a massless gravitino LSP scenario are placed on strong sector sparticles with G̃ LSP from opposite sign dilepton + missing energy searches in ATLAS [38], excluding m_{g̃} ≤ 1.8 TeV for m_{χ̃1}⁰ < 600 GeV. Stringent limits also arise from boosted Higgs searches [39] interpreted in terms of a simplified scenario with a light χ̃10 LSP, excluding m_{g̃} ≤ 2.2 TeV for m_{χ̃1}⁰ = 1 GeV. Other indirect searches, which constrain the above mentioned scenario, are multijets and/or multileptons + 𝔅_T searches [35,36], owing to the presence of h/Z from the NLSP decay which give rise to leptons or jets in the final state.

V. BENCHMARKS FOR OUR ANALYSIS

We choose representative benchmark points of the allowed parameter space to probe a low-lying Higgsino-like $\tilde{\chi}_1^0$ NLSP with light \tilde{G} LSP, focusing primarily on promptly decaying $\tilde{\chi}_1^0$ signals. Our choice of benchmarks is motivated by the underlying aim of uncovering the characteristics of a Higgsino-like NLSP in the presence of a light \tilde{G} LSP. Decays of the strong sector sparticles occur via the following decay modes for a keV \tilde{G} : for gluinos $(m_{\tilde{g}} < m_{\tilde{q}} \leq m_{\tilde{l}}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_4^0}, m_{\tilde{\chi}_2^\pm})$, the possible decay modes to the NLSP,

$$\tilde{g} \to t\bar{t}\tilde{\chi}^0_1, \qquad b\bar{b}\tilde{\chi}^0_1, \qquad t\bar{b}\tilde{\chi}^-_1, \qquad q\bar{q}'\tilde{\chi}^\pm_1, \qquad q\bar{q}\tilde{\chi}^0_1.$$

Among these decay modes, owing to the Higgsino-like nature of the NLSP, the interaction strengths are governed by the Yukawa couplings. Hence, the third generation squark channels dominate. For squarks $(m_{\tilde{q}} < m_{\tilde{g}} \le m_{\tilde{l}}, m_{\tilde{\chi}_{2}^{0}}, m_{\tilde{\chi}_{2}^{0}}, m_{\tilde{\chi}_{2}^{0}})$, the possible decay modes are

²Note that $m_{\tilde{G}} = 1$ GeV would correspond to a long-lived NLSP as Eq. (3) suggests. As long as the mass of the gravitino would not affect the kinematics of the process, it does not affect the analysis reported in [33].

³The third generation squarks decay would have additional decay modes, such as $\tilde{t}_1 \rightarrow \tilde{b}W^+$ and $\tilde{b}_1 \rightarrow \tilde{t}W^-$.

TABLE III. List of benchmarks chosen for our study. Mass parameters are in GeV unless specified otherwise.

Parameters	BP1	BP2	BP3	BP4	BP5
M_1	2400	800	7000	2300	2400
M_2	2400	800	7000	2300	2400
μ	800	2400	700	2250	-800
$\tan\beta$	25	25	25	25	3.8
A_t	3200	3200	100	3200	3740
m_A	2500	2500	2500	2500	3000
m_h	125.3	125.3	127.1	124.5	122.2
$m_{ ilde{g}}$	2806.4	2807.1	7271.2	2840.1	2663.3
$m_{ ilde q_L}$	2303.3	2300.2	7156.4	2313.3	2280.6
$m_{\tilde{q}_R}$	2302.2	2302.5	7155.4	2312.5	2283.7
$m_{\tilde{t}_1}$	2357.5	2184.8	7057.0	2509.1	1581.1
$m_{\tilde{t}_2}$	2340.9	2370.8	7104.0	2666.0	2271.4
$m_{\tilde{b}_1}$	2260.9	2266.4	7102.2	2583.4	2237.5
$m_{\tilde{b}_2}$	2299.0	2323.9	7129.0	2630.3	2295.6
$m_{\tilde{l}_L}$	3331.8	3326.8	7337.2	3332.6	3329.4
$m_{\tilde{l}_R}$	3335.6	3333.7	7336.3	3336.3	3334.1
$m_{\tilde{\chi}_1^0}$	810.9	797.9	718.8	2211.0	1214.8
$m_{\tilde{\chi}^0_2}$	-814.4	837.8	-723.7	-2254.8	-1217.2
$m_{\widetilde{\chi}_1^\pm}$	812.5	837.9	720.9	2223.1	1216.4
$m_{ ilde{\chi}_2^\pm}$	2415.7	2397.3	1925.9	2350.5	2420.9
$m_{\tilde{\chi}_3^0}$	2386.3	-2394.8	1923.6	2290.1	2392.2
$m_{ ilde{\chi}_4^0}$	2415.6	2397.4	1925.8	2350.5	2420.9
$m_{\tilde{G}}$ (keV)	1.0	1.0	1.0	1.0	1.0
$BR(\tilde{\chi}_1^0 \to h\tilde{G})$	0.45	0.0	0.44	0.23	0.27
$BR(\tilde{\chi}_1^0 \to Z\tilde{G})$	0.55	0.25	0.56	0.75	0.73
$\operatorname{BR}(\tilde{\chi}_1^0 \to \gamma \tilde{G})$	0	0.75	0	0.02	0
$BR(\tilde{\chi}_1^{\pm} \to W\tilde{G})$	0.024	0.0	0.003	0.0001	0.15
$\underline{\mathrm{BR}(\tilde{\chi}_1^{\pm} \to W^* \tilde{\chi}_1^0)}$	0.976	1.0	0.997	0.9999	0.85

$$\tilde{q}
ightarrow q \tilde{\chi}_1^0, \qquad q \tilde{\chi}_2^0, \qquad q' \tilde{\chi}_1^{\pm}.$$

For simplicity, $M_1 \simeq M_2 \sim 2.3-2.4$ TeV, such that their contribution to the signal region under study (directly or via cascade decays of strong sector sparticles) is negligible. Among the constraints on the parameter space, the light

Higgs mass is within the range 122–128 GeV [40,41]. In all cases, both \tilde{t}_1 and/or \tilde{t}_2 are heavy or the trilinear coupling A_t , is too large to fit the lightest *CP*-even Higgs mass [40–42]. Also, $m_{\tilde{\chi}_1^{\pm}}$ adheres to the LEP lower limit of 103.5 GeV [43]. We choose the benchmarks after passing them through the public software CheckMATE [44]. Among the searches implemented in CheckMATE, stringent constraints come from multijet searches by ATLAS [36]. The benchmark points are generated using the spectrum generator SPheno-v3.3.6 [31,32].

VI. LHC SIGNALS

We now discuss in detail the possible LHC signals arising in the current scenario with a Higgsino-like $\tilde{\chi}_1^0$ NLSP and keV \tilde{G} LSP. A strong sector sparticles pair produced at $\sqrt{s} = 13$ TeV LHC cascades down to the $\tilde{\chi}_1^0$ NLSP along with additional jets arising from the cascade. In situations where the strong sector is not kinematically accessible, it is worthwhile to explore signals from the direct production of the low-lying Higgsinos decaying promptly to the NLSP $\tilde{\chi}_1^0$, which then further decays to a Higgs/Z gauge boson and the \tilde{G} LSP. As discussed in Sec. III A, such a scenario would lead to hh/hZ/ZZ final states with/without extra hard jets arising from the strong sector cascade.

Motivated by the characteristics of a Higgsino NLSP spectrum, among the multifarious signatures possible, we focus on a final state consisting of a Higgs and Z boson scenario. In addition, to study the characteristic polarization of the Z boson coming from the decay of the NLSP, we require an efficient and cleaner mode of reconstruction, which can only come through the leptonic decay of the weak gauge boson. Note that for the hadronic decays of a Higgs and Z boson contributing to the signal rates, the corresponding SM hadronic background would also be significantly bigger. We therefore choose a final state that includes at least one b jet and two same-flavor opposite leptons in the final state, this is a relatively clean channel to observe at LHC as compared to an all hadronic final state. Since the LSP is a very light \tilde{G} , the ensuing h/Z from the NLSP decay and hence, the *b* jets and/or leptons have large transverse momentum (p_T) , thereby leading to a large $\not \!\!\! E_T$, where $E_T = -\vec{p}_{T_{\rm vis}}$ (balancing the net transverse momenta, $\vec{p}_{T_{vis}}$ of the visible particles). No specific criteria is imposed on the number of light jets in the scenario as will be present if the signal arises from the decay of the squarks or gluinos to the NLSP. This is because our choice of an inclusive final state signal would be able to highlight the presence of a Higgsino-like NLSP irrespective of the rest of the underlying MSSM spectrum, i.e., with/without the strong sector placed above the low-lying Higgsinos.

A. Signal, background, and event selection criteria

We consider the following SUSY production processes involving squarks as well as the low-lying Higgsinos to be pair produced when kinematically accessible:

$$pp \to \tilde{q}_i \tilde{q}_j, \tilde{q}_i \tilde{q}_j^*, \tilde{q}_i^* \tilde{q}_j^*, \tilde{q} \tilde{g}, \tilde{\chi}_1^0 \tilde{\chi}_2^0, \tilde{\chi}_1^{\pm} \tilde{\chi}_1^0, \tilde{\chi}_1^{\pm} \tilde{\chi}_2^0, \tilde{\chi}_1^{\pm} \tilde{\chi}_1^{-}.$$

Note that the gluinos are heavier compared to the squarks and Higgsinos, and their contribution to the signal is subdominant. When the signal is generated from the pair production of the strongly interacting sparticles, the final state consists of at least two hard jets in the hh/hZ/ZZ final state along with a pair of invisible gravitinos, which contribute to the large E_T . Among the possible combinations of the decay products of h and Z, we primarily focus on the $\geq 1b + \ell^+ \ell^-$ final state along with $\not\!\!E_T$. Since the Z decays leptonically, it gives a cleaner channel and better control over the SM backgrounds as compared to a hadronic final state.

We generate the signal events in MadGraph_v5 [45] using the model UFO files available from FeynRules [46]. Subsequently, parton level events are showered and hadronized using PYTHIA [47,48], and a detector simulation is performed using DELPHES [49]. Jets (including b jets) are reconstructed using the anti-kT algorithm [50], using FastJet [51] with minimum transverse momentum, $p_T > 20$ GeV within a cone $\Delta R = 0.4$. Charged leptons are reconstructed in a cone of $\Delta R = 0.2$ with a maximum energy deposit in the cone from all other particles limited to 10% of the p_T of the lepton. The significant contributions to the SM background for the given final state come from

(i)
$$t\bar{t}, (t \to bW^+, W^+ \to \ell^+ \nu)$$

(ii) hZ_+ jets $(h \to b\bar{b}, Z \to \ell^+$

(ii)
$$nZ + \text{Jets}, (n \to bb, Z \to t)$$

iii) $t\bar{t}Z \quad (Z \to \ell^+ \ell^-)$

(iii)
$$iiZ$$
, $(Z \to b\bar{b} - Z \to d\bar{b})$

(iv)
$$ZZ$$
, $(Z \to bb, Z \to \ell^+ \ell^-)$
(v) $W^{\pm}W^{\mp}Z$, $(Z \to \ell^+ \ell^-)$

$$(V) \quad W^-W^+Z, \quad (Z \to U^+)^- U^-U^-U^-$$

(vi) $l^+l^-bb + \nu\bar{\nu}$.

Although the QCD background has a large cross section, it has a negligible contribution to the signal region charachelps probe the heavy mass scale of the SUSY particles and would serve as an effective discriminator between the SUSY signal and SM background. For an SM background, we perform MLM matching [45] when needed with QCUT =20 - 30 GeV.

B. Primary selection criteria

We choose the following basic selection criteria to identify leptons (e, μ) and b jets in the signal and background:

- (i) The charged leptons are identified with $p_T >$ 10 GeV and $|\eta| < 2.5$.
- (ii) All reconstructed b jets have $p_T > 30 \text{ GeV}$ and $|\eta| < 2.5$.
- (iii) Jets and leptons are isolated with $\Delta R_{ii} > 0.4$ and $\Delta R_{\ell\ell} > 0.2$.

C. Signal analysis: At least $1b - jet + \ell^+ \ell^- + E_T$

We note that for the signal, since the NLSP-LSP mass gap is large, the transverse momenta carried by the decay products are large thereby ensuring a large amount of $\not \!\!\! E_T$ in the event. Figure 2 shows the normalized differential distribution of a few kinematic variables $(M_{\rm Eff}$ and $E_T)$ for **BP1** and **BP4** along with the background. The SUSY signal distributions for the missing transverse energy $(\not\!\!E_T)$ and effective mass $(M_{\rm Eff})$ are widely separated from the SM background for **BP4** in the presence of a heavy NLSP. However, the signal events peak at a much lower value of $M_{\rm Eff} \sim 850 {\rm ~GeV}$ for **BP1**, while significant events of the signal are found at large $M_{\rm Eff}$ values ~2.0 TeV for **BP4**. Note that for **BP4**, this is due to the high transverse momentum of the jets and leptons arising from the decay cascades of the heavy $\mathcal{O}(2)$ TeV range sparticles. However, for **BP1** with a light NLSP, there is considerable overlap of the kinematic distributions with the background while differing in the tail of the distribution. This happens because the dominant contribution to the signal comes from the direct production of the light Higgsino sector as compared to the strong production cross section. We break our analysis in two parts to study different scenarios that can present themselves at LHC. The signal from a heavy



FIG. 2. Distribution of few useful kinematic variables before application of any selection cuts.

spectrum of $\mathcal{O}(2)$ TeV, including the NLSP, that can only have a relevant signal contribution through the production of strongly interacting sparticles at the LHC is optimized using cuts in *Analysis 1*, while the signal for relatively lighter electroweakino states being directly accessible at

LHC with smaller contributions from the strong sector is analyzed in *Analysis 2*. Appropriate cuts on the relevant kinematic variables will be crucial to remove SM background in the subsequent collider analyses to study the two scenarios discussed above.

D. Analysis 1

As a crucial part of our analysis is dependent on the reconstruction of the Z boson in the events through the dilepton mode, the event rate for the signal will suffer due to the small branching fraction of the gauge boson to charged leptons. In addition, if we intend to reconstruct the light Higgs boson too using double *b*-tag jets, we will end up restricting our search sensitivity significantly. We therefore need to select events using proper cuts to be able to identify the Z boson as well as imply a Higgs like event. In order to select such a final state, we implement the following event selection criterion to retain a significant amount of signal against the SM background:

- (i) **D1**: We select a final state with two opposite sign leptons of the same flavor ($N_{\ell} = 2$ with $p_T > 20 \text{ GeV}$) and at least one *b* jet with $p_T > 30 \text{ GeV}$.
- (ii) **D2**: To reconstruct the *Z* boson, we demand that the invariant mass of a dilepton pair (opposite sign, same flavor) in the signal events is within the *Z* mass window satisfying $76 < M_{\ell^+\ell^-} < 106$ GeV.

(i) **D3**: We demand a cut on the kinematic variable $M_{T_2} > 90$ GeV to remove backgrounds from $t\bar{t}$.

The other important kinematic variable is the effective mass, $M_{\text{Eff}} = p_T(\ell^+) + p_T(\ell^-) + \not\!\!\!\!/ E_T + \sum p_{T_i}(j)$, the scalar sum of the transverse momenta of the visible jets, leptons, and $\not\!\!\!/ E_T$ in the event. M_{Eff} reflects the mass scale of the heavy SUSY particles and hence, is an efficient variable to suppress SM background. However, the choice of a strong cut on M_{Eff} would choose to retain contributions from a very heavy spectrum, and therefore, in this case, we focus on the benchmarks that contribute mainly through the production of the strong sector sparticles, viz. **BP4** and **BP5**. Note that the strong sector for **BP1** is of similar value to **BP4** and **BP5**, and therefore, the signal rates coming from the strong sector would be very similar. However, a dominant fraction of signal events would come from the light Higgsino production, and the cuts given below are not particularly optimized to study **BP1**. The **BP3** signal, on the other hand, becomes very small. We shall discuss the **BP1** and **BP3** benchmarks separately in *Analysis 2*. Additional cuts on the events are

- (i) **D4**: Since nearly all the SUSY particles excluding the LSP are heavy for **BP4** and **BP5**, a large $M_{\rm Eff}$ is expected for the signal over the SM background as shown in Fig. 2. We therefore demand a strong cut of $M_{\rm Eff} > 2$ TeV. This cut renders the signal for other benchmarks to a relatively smaller value.
- (ii) **D5**: In addition, we also put a strong cut on missing transverse energy, $\not\!\!\!E_T > 300$ GeV to further remove remaining contributions from SM background processes.

We show the cut-flow result of our analysis for the signal and SM background in Table IV. As expected, the signal rates coming from a 2 TeV squark sector yields quite small numbers, even with an integrated luminosity of 3000 fb⁻¹. The overwhelmingly huge SM background is brought in control by primarily using the M_{T_2} cut and is then rendered negligibly small using the combination of M_{Eff} and $\not E_T$ cuts. We find that the sequence of cuts shown in Table IV affects the signal slightly with a suppression of the signal rate of less than 50% for **BP5**. Thus, we find a significant number of SUSY signal events surviving the event selection. Note that while a ~75% suppression of signal events happen for **BP1**, it is still quite large compared to the SM background, unlike that for **BP3**.

TABLE IV. Number of signal and background events for $\geq 1b + \ell^+ \ell^- + \not\!\!\!/ _T$ at $\sqrt{s} = 13$ TeV LHC for $\mathcal{L} = 3000$ fb⁻¹ using cuts **D1** – **D5**. Note that the total number of background events have been rounded off to the nearest integer. Cross sections for SUSY signals have been scaled using NLO K factors [53] and wherever available, NLO + NLL K factors [54]. Cross sections for SM background processes have been scaled using NLO K factors [55–59] have been used.

Signal	D1	D2	D3	D4	D5
BP1	130	104	91	39	33
BP3	98	83	74	2	2
BP4	22	17	17	16	16
BP5	62	33	30	28	26
SM background	D1	D2	D3	D4	D5
tī	365125	64968	186		
hZ	29348	28360	781	1.76	0.16
ZZ	178581	172636	2124	15	2.3
tīZ	3043.3	2111	287	6.14	0.98
$t\overline{t}W$	9121	1802	14		
WWZ	159	153	13	0.65	0.074
Total background					3

TABLE V. Required luminosities for observing the SUSY signal for the different benchmarks at $\sqrt{s} = 13$ TeV LHC run. The numbers in the parentheses include 10% systematic errors in the background.

Benchmark	\mathcal{L} (in fb ⁻¹) for 3σ excess	\mathcal{L} (in fb ⁻¹) for 5 σ excess		
BP1	240 (250)	665 (695)		
BP4	1112 (1178)	3090 (3270)		
BP5	340 (356)	943 (988)		

We compute the statistical significance (S) of the above signals using the formula in Eq. (14) and show the required integrated luminosities to observe and discover the signal in Table V,

$$S = \sqrt{2 \times \left[(s+b) \ln \left(1 + \frac{s}{b} \right) - s \right]}, \qquad (14)$$

where *s* and *b* refer to the number of signal and background events, respectively. We observe that benchmarks **BP4** and **BP5** require large integrated luminosities, whereas **BP3** with a decoupled squark sector is out of reach of LHC. Although **BP1** is observable at LHC, the large M_{Eff} cut reduces the contribution from the light Higgsino sector, which is directly accessible at LHC. Therefore, this analysis is more sensitive to the case of heavier spectra that also includes the NLSP to be quite heavy, such as **BP4** and **BP5**. However, with a light Higgsino sector and similar squark masses to **BP4**, such as in **BP1**, we are still able to get a relatively healthy number for the signal albeit after losing a large part of the signal events. A more optimized set of cuts is used in *Analysis 2* to study the scenario with lighter NLSP mass.

E. Analysis 2

We now focus on the signal contribution arising dominantly from the electroweak sector of sparticles with/ without the strong sector, as in benchmark **BP1** and **BP3**. Since the Higgsino sector is lighter, a strong cut on M_{Eff} as used in **D4** will deplete the signal significantly in this case. Therefore, we employ a different set of cuts to investigate the signal region ($\geq 1 \ b + \ell^+ \ell^- + \not E_T$) arising from the low-lying Higgsino sector. We consider the contributions from the Higgsino sector in addition to the strong sector for the benchmarks in our study when they are kinematically accessible and study the benchmarks **BP1** and **BP3**. As the final state remains unchanged, the cuts implemented on both signal and background in *Analysis 1* would still be useful for background suppression. The implemented cuts therefore remain similar except for the excluded $M_{\rm Eff}$ cut, optimized for the two benchmarks

- (i) **E1**: As in *Analysis 1*, we select a final state with two opposite sign leptons of same flavor $(N_{\ell}=2 \text{ with } p_T > 20 \text{ GeV})$ and at least one *b* jet with $p_T > 30 \text{ GeV}$.
- (ii) **E2**: To reconstruct the *Z* boson, we demand that the invariant mass of the dilepton pair in the signal events is within the *Z* mass window, satisfying $76 < M_{\ell^+\ell^-} < 106$ GeV.
- (iii) E3: As before, M_{T_2} is an efficient cut to reduce background contributions from $t\bar{t}$ to the signal region. We demand a slightly stronger cut of $M_{T_2} >$ 120 GeV in this case as it helps improve the signalto-background ratio.
- (iv) **E4**: The SUSY signal has a larger $\not\!\!\!E_T$ as compared to the SM background. Hence, $\not\!\!\!E_T > 300 \text{ GeV}$ cut

TABLE VI. Number of signal and background events for $\geq 1b + \ell^+ \ell^- + \not\!\!\!/ _T$ at $\sqrt{s} = 13$ TeV LHC for $\mathcal{L} = 3000$ fb⁻¹ using cuts **E1 – E4**. Note that the total number of background events have been rounded off to the nearest integer. Cross sections for SUSY signals have been scaled using NLO K factors [53] and wherever available, NLO + NLL K factors [54]. Cross sections for SM background processes have been scaled using NLO K factors [55–59] have been used.

BP1	E1	E2	E3	E4
$\frac{1}{\tilde{\chi}_{1}^{\pm}\tilde{\chi}_{1}^{\pm}}$	16	13	11	9
$\tilde{\chi}_1^{\pm} \tilde{\chi}_1^0$	65	54	47	36
$\tilde{\chi}^0_2 \tilde{\chi}^0_1$	16	14	12	9
$\tilde{q}\tilde{q},\tilde{q}\tilde{g}$	47	36	28	26
Total				80
BP3	E1	E2	E3	E4
$ ilde{\chi}_1^\pm ilde{\chi}_1^\pm$	33	27	24	18
$\tilde{\chi}_1^{\pm} \tilde{\chi}_{1/2}^0$	126	107	87	65
$\tilde{\chi}_2^0 \tilde{\chi}_1^0$	33	28	24	18
Total				101
SM background	E1	E2	E3	E4
tī	365125	64968		
hZ	29348	28360	298	0.67
ZZ	178581	172636	774	6.61
tīZ	3043	2111	151	8.6
$t\bar{t}W$	9121	1802	1	
WWZ	159	153	6	0.23
$l^+l^-b\bar{b}+\not\!\!\!E_T$	2933	2905	312	34.7
Total				51

TABLE VII. Required luminosities for observing the SUSY signal for the different benchmarks at $\sqrt{s} = 13$ TeV LHC run. The numbers in the parentheses include 10% systematic errors in the background.

Benchmark	\mathcal{L} (in fb ⁻¹) for 3σ excess	\mathcal{L} (in fb ⁻¹) for 5σ excess		
BP1	310 (333)	862 (924)		
BP3	208 (226)	577 (626)		

helps reduce a significant part of the remnant contributions from SM background.

The cut-flow table for the signal and SM background are as shown in Table VI. We rely on a slightly stronger cut on M_{T_2} to ensure substantial removal of the $t\bar{t}$ background while retaining the signal events. However, other background contributions, such as that from $l^+l^-b\bar{b}+\not\!\!\!E_T$, remain. This still gives a significantly large event rate for the signal as compared to Analysis 1, and thereby allowing a ~ $(8-10)\sigma$ discovery possible with $\mathcal{L} = 3000$ fb⁻¹. Since both the benchmarks have similar branching fractions into the Z and Higgs mode, the difference in the required integrated luminosity is due to the fact that the NLSP mass is heavier in **BP1** than in **BP3**. The required luminosity for observing a 3σ and 5σ significance at LHC are shown Table VII. We conclude that both **BP1** and **BP3** are well within the discovery reach of the high luminosity run of LHC.

We are now set to study the efficacy of the signal that we have analyzed to identify the nature of the NLSP and its inherent composition with respect to the gaugino-Higgsino admixture in the following section.

VII. A DISTINGUISHING FEATURE: LONGITUDINAL VS TRANSVERSE GAUGE BOSONS

We are interested in a Higgsino-like lightest neutralino $\tilde{\chi}_1^0$ for which $\tilde{\chi}_1^0 \rightarrow h\tilde{G}$ is an obvious decay channel. In addition, the Higgsino also couples to the imaginary parts of the neutral component of the two Higgs doublets. This leads to Higgsino-goldstone-gravitino interactions. The goldstone, on the other hand, approximates the longitudinal component of the *Z*, when the relevant energy scale is much larger than m_Z . Thus, for a Higgsino-like $\tilde{\chi}_1^0$ with $m_{\tilde{\chi}_1^0} \gg m_Z$, one also expects the decay $\tilde{\chi}_1^0 \rightarrow Z\tilde{G}$, when the *Z* is longitudinal.

Although our focus is on the polarization of Z boson in the context of SUSY in this work, the polarization information of vector bosons may be extremely useful even for non-SUSY scenarios, where a polarized gauge boson is likely to be produced from the decay of a heavy particle. Thus, the features of the longitudinal Z boson, which will be discussed in detail in this work, are also applicable for other scenarios as well. For example, the presence of longitudinal gauge bosons from heavy Higgs decays have been studied in earlier works in the context of the Tevatron [60]. LHC analyses have also looked at features of longitudinal gauge bosons in the SM [61]. In case an excess over SM is observed, it is of crucial importance to extend current search strategies to characterize BSM scenarios by studying variables sensitive to the polarization information of the gauge bosons via their decay products. Although there have been several studies in the context of e^+e^- colliders focusing on studies of polarizations of the incoming electron-positron beams or polarization of the final state particles, there are few analogous studies with respect to the LHC utilizing these techniques [62]. The polarization of a Z boson has been studied briefly in [62] with respect to the LHC in a similar scenario however in displaced dilepton final states arising from the Z boson decay using the angular variable $\cos \theta^*$ discussed below. We discuss analytically some basic variables found in the literature, which distinguish longitudinal and transverse gauge bosons. The differential decay rates for the transversely polarized and longitudinally polarized Z boson in the rest frame of Z boson are [60]

$$\frac{d\Gamma_T}{d\cos\theta^*} \propto (1\pm\cos\theta^*)^2 \tag{15}$$

$$\frac{d\Gamma_L}{d\cos\theta^*} \propto \sin^2\theta^*,\tag{16}$$

where $\Gamma_T = \Gamma(\tilde{\chi}_1^0 \to Z_T \tilde{G})$ and $\Gamma_L = \Gamma(\tilde{\chi}_1^0 \to Z_L \tilde{G})$ are the partial decay widths of the $\tilde{\chi}_1^0$ to a transverse Z boson (Z_T) and longitudinal $Z(Z_L)$ boson, respectively. The angle θ^* is defined as the angle the outgoing lepton (arising from the Zboson decay) makes with the Z boson in its rest frame with the reference direction being the boost direction of the Zboson in the laboratory frame. The dependence of the decay width; i.e., $(1 \pm \cos \theta^*)^2$ corresponds to $k = \mp 1$ state and $\sin^2 \theta^*$ corresponds to k = 0 state, where k is the helicity of the Z boson. To highlight the difference, we choose the NLSP from a few of our benchmarks and generate a normalized distribution for $\cos \theta^*$, where the NLSP is decaying at rest and gives the Z boson as its decay product. The simple illustration of this reconstruction is shown in Fig. 3, where **BP1** represents a dominantly Higgsino-like NLSP, **BP2** represents a dominantly gauginolike NLSP, while **BP4** represents a comparable admixture of gauginos and Higgsinos in the NLSP.

We now go ahead and consider the full analysis for the signal $\geq 1b + \ell^+ \ell^- + \not\!\!\!\!/_T$ and focus on the negatively charged lepton. Note that we expect distributions in $\cos \theta^*$, as highlighted in Fig. 3, for the *Z* polarization to be robust against the energy smearings in the detector and the full detector simulation. To show this, we compare both parton-level analysis to the signal events obtained after detector simulations. We plot the normalized distributions



FIG. 3. Normalized distribution of $\cos \theta^*$ of the negatively charged lepton (ℓ^-) arising from the $\tilde{\chi}_1^0$ NLSP decay at rest corresponding to the benchmarks **BP1**, **BP2**, and **BP4** with the isolation variable $\Delta R > 0.2$ for the leptons.

for $\cos \theta^*$ of the negatively charged daughter lepton of the Z boson in Fig. 4 at the parton level (left) and detector level (right-panel) for our benchmarks **BP1**, **BP2**, and **BP4**, where one NLSP decays to a Z boson along with a \tilde{G} . Recall, **BP1** has a purely Higgsino-like NLSP (~99%), BP2 with purely gauginolike NLSP (~100%), and BP4 has $\sim 31\%$ gaugino admixture in the NLSP. We observe in Fig. 4 that the distributions for the negatively charged lepton (for BP1 and BP2) are largely similar at both parton and detector level simulations, to the expected distributions as shown in Fig. 3.⁴ For **BP4**, where the NLSP is a more democratic superposition of the gaugino and Higgsino states, a slightly flat and broad peak for $\cos \theta^*$ is observed. In addition, the NLSP mass is around 2 TeV, which results in a very boosted Z boson in the final state. The event selection criteria can in principle have adverse effects in this case and modify the distributions. The most notable effect for **BP4** is that the distribution starts to resemble features similar to the gauginolike NLSP (BP2) at both parton and detector-level simulations. This we find is due to the fact that when the Z boson is highly boosted, the pair of charged leptons coming from the Z boson decay get more collimated with a very small opening angle. This in turn would mean that a larger isolation requirement for the charged leptons would lead to loss of events and also affect the $\cos \theta^*$ distribution.

In our analysis, we have used the default DELPHES card using a small cone radius R = 0.2 and a maximum energy deposit in the cone being 10% of the p_T of the lepton. A lepton-lepton isolation cut on $\Delta R > 0.2$ reduces the peak of the $\cos \theta^*$ plot. To counter the consequent reduction in signal events, for **BP4**, a relatively relaxed lepton identification criterion can be useful for our purpose. To highlight this, we identify the charged leptons with a much larger cone radius of R = 0.5 for lepton identification and also demand that a large energy deposit with respect to the p_T of the lepton is allowed in the cone (~12% for electrons and 25% for muons). The distribution still retains the gauginolike behavior for an isolation of $\Delta R > 0.2$ as in the parton level but starts agreeing with the Higgsino-like feature (as in the parton-level case) when the separation between the charged leptons is chosen to be loose with $\Delta R > 0.05$ or $\Delta R > 0.1$ as can be seen in the bottom-right panel of Fig. 4.

The qualitative differences observed in the distributions of the negatively charged lepton as the gaugino admixture increases in the NLSP amongst the three cases may be effectively captured by defining asymmetry variables in $\cos \theta^*$, which could clearly discriminate between a longitudinal and transverse Z boson. Taking a cue from the features of $\cos \theta^*$, we construct a variable which highlights this difference through an asymmetry amongst the observed $\cos \theta^*$ values for the Higgsino-like and gauginolike NLSP. The asymmetry variable, C_{θ_Z} , as defined in Eq. (17), serves to enhance the features of the longitudinally polarized Z in comparison to the transversely polarized Z, such that they would be less affected if detector simulation effects smear the polarization dependence of the angular or energy observables. We define

$$C_{\theta_Z} = \frac{N_A - N_B - N_C}{N_A + N_B + N_C},$$
 (17)

where N_I 's stand for events whereas the subscript I = A, B, Crepresent the angular regions in θ^* given by $A = [\pi/3, 2\pi/3]$, $B = [0, \pi/3]$, and $C = [2\pi/3, \pi]$. The numerator focuses only on the asymmetry features while the denominator is the total number of events for $-1 < \cos \theta^* < 1$. Based on the construction of $C_{\theta_{z}}$, a positive value is indicative of a Higgsino-like NLSP whereas negative values indicate a gauginolike NLSP. Since C_{θ_7} is the normalized difference in the number of events corresponding to $|\cos \theta^*| < 0.5$ and $|\cos\theta^*| > 0.5$, a Higgsino-like NLSP gives larger events around $\cos \theta^* = 0$ as $N_A > (N_B + N_C)$, whereas for the gauginolike NLSP, the distribution peaks around $\cos \theta^* \sim$ ± 0.8 *i.e.*, $(N_B + N_C) > N_A$. Therefore, the latter shows a negative sign as compared to the former. We list the values of C_{θ_Z} for cases when the NLSP decays at rest ($C_{\theta_Z}^{\text{rest}}$) and compare this with parton-level $(C_{\theta_z}^{\text{parton}})$ results and full detector-level simulation (C_{θ_z}) of our *Analysis 1* in Table VIII of a simulation (C_{θ_z}) of our *Analysis 1* in Table VIII, for the benchmarks BP1 and BP2 (which correspond to an almost pure Higgsino and pure gaugino compositions, respectively).

Note that the values of C_{θ_z} are in good agreement with the parton level $C_{\theta_z}^{\text{parton}}$ results. For the pure Higgsino-like NLSP

⁴Similar distributions for $\cos \theta^*$ are expected for the positively charged leptons.

⁵The results in Table VIII are produced by using only squark pair production. However, the generic feature remains unchanged even when all production modes are included.



FIG. 4. Normalized distribution of $\cos \theta^*$ of the negatively charged lepton (ℓ^-) arising from the $\tilde{\chi}_1^0$ NLSP at the parton level (top left panel) and after detector simulation (top right panel) using *Analysis 1*, corresponding to the benchmarks **BP1**, **BP2**, and **BP4**. In the bottom panel, we present the plots for **BP4** at the parton level (left) and at the detector level (right) for various ΔR values as discussed in the text.

(**BP1**), $C_{\theta_{\tau}}$ is large and positive, whereas the pure gauginolike NLSP (BP2) shows a negative value. We find that the $C_{\theta_{z}}$ value starts decreasing as the gaugino admixture in the NLSP is increased when compared to BP1. Thus, with increasing gaugino admixture the asymmetry value becomes negative as shown for BP2. The most notable change is observed for the BP4 with an intermediate gaugino-Higgsino admixture. C_{θ_z} value is ~0.021 when the NLSP decays at rest with the small positive value still hinting at a larger Higgsino admixture. However, it turns negative for the analysis where the NLSP appears from cascade decays of the squark, both at the parton and the detector level owing largely to the effect of isolation cuts and detector smearing effects, which modify the $\cos \theta^*$ distribution as seen in Fig. 4 and discussed earlier. We note that the $C_{\theta_z}^{\text{parton}}$ value becomes positive giving $C_{\theta_Z}^{\text{parton}} = 0.04, 0.05$ for the loose isolation requirement and identification of the charged lepton with $\Delta R > 0.05, 0.1$ as against $C_{\theta_Z}^{\text{parton}} = -0.214$ for the tighter isolation cut of $\Delta R > 0.2$. We expect that the same would be true when the events are passed through detector simulations, which would be consistent with observations made in the lower panels of Fig. 4.

An additional kinematic feature that can be used to study the polarization of the Z boson, which in effect highlights the composition of the NLSP, is the charged lepton energy. Among others, the ratio of the energy carried by the charged lepton and antilepton also show a dependence on the polarization of the Z boson with an energy E, via dependence on the angle θ^* . The energy (E_{ℓ}) of the leptons in the laboratory frame [60] follows

$$E_{\ell} \propto \frac{E}{2} (1 \pm \beta \cos \theta^*). \tag{18}$$

TABLE VIII. Variation of the asymmetry variables $C_{\theta_Z}^{\text{rest}}$, $C_{\theta_Z}^{\text{parton}}$, C_{θ_Z} , and C_Z as defined in the text, at the parton level and detector level after cuts **D1** – **D5** for benchmarks **BP1** and **BP2**. The numbers for C_{θ_Z} and C_Z include both signal and background in the computation of the observables and its associated 1σ error for $\mathcal{L} = 3000 \text{ fb}^{-1}$.

Benchmark	$m_{\tilde{\chi}_1^0}$ (GeV)	Higgsino admixture (%)	Gaugino admixture (%)	$C_{\theta_Z}^{\text{rest}}$	$C_{\theta_Z}^{\text{parton}}$	$C_{ heta_Z}$	C_Z
BP1	810.9	99.83	0.17	0.38	0.33	0.35 ± 0.16	0.38 ± 0.16
BP2	797.9	0.05	99.95	-0.18	-0.08	-0.05 ± 0.21	-0.02 ± 0.21



FIG. 5. Normalized distributions of the kinematic variables Z_D and Z_R as defined in the text for distinguishing between a Higgsino and gauginolike $\tilde{\chi}_1^0$ NLSP before cuts **D1** – **D5** The variables are as defined in the text. Here, we have plotted the observables for the process $\tilde{q} \tilde{q}$ with one of the squarks decaying as: $\tilde{q} \to q\tilde{\chi}_1^0 \to qZ\tilde{G}, Z \to \ell^+\ell^-$.

Using this, we define two kinematic observables Z_D and Z_R (variations of such observables have been pointed out in earlier papers [63,64] using jet substructure to study hadronic final states),

$$Z_D = \frac{|E_{\ell^-} - E_{\ell^+}|}{E_{\ell^-} + E_{\ell^+}}; \qquad Z_R = \frac{E_{\ell^-}}{E_{\ell^-} + E_{\ell^+}}.$$
 (19)

We study the usefulness of these observables using simple cuts on kinematic variables after detector simulation effects are taken into account. For a predominantly longitudinal Z boson, there is an equal sharing of energy of the parent among its daughter particles whereas for a transverse Z boson, the energy sharing is unequal. The asymmetry is evident in Fig. 5, where the Higgsino-like NLSP peaks at $Z_D = 0.1$ as compared to $Z_D = 0.8$ for the gauginolike case. Similar effects are observed in the variable Z_R , which denotes the fraction of net leptonic energy carried away by the negatively charged lepton. The ratio peaks at $Z_R \simeq 0.5$ for **BP1** as compared to $Z_R \simeq 0.1$ and $Z_R \simeq 0.8$ for the **BP2**, since for the former case, the leptons mostly have equal energy sharing, whereas unequal energy sharing occurs for the latter case. We define an asymmetry variable similar to C_{θ_Z} , now referred to as C_Z to capture the asymmetry in the values of Z_D at the detector level,

$$C_Z = \frac{N_A - N_B}{N_A + N_B},\tag{20}$$

where N_A refers to the number of events for $Z_D < 0.5$ and N_B represents events for $Z_D > 0.5$, respectively. We list the C_Z values in Table VIII and observe that C_Z is positive for the Higgsino-like NLSP and negative for gauginolike NLSP. Note that the effect observed for the highly boosted Z boson in C_{θ_Z} also shows up for C_Z highlighting the consistency and importance of the isolation of the charged leptons. The statistical uncertainty in the observed asymmetry has been shown in Table VIII and is calculated using [65]

$$\sigma(C) = \frac{\sqrt{1 - C^2}}{\sqrt{N}},\tag{21}$$

where $C = C_{\theta_Z}$, C_Z , while *N* represents the total number of events. The uncertainty goes down as $1/\sqrt{N}$, which means that a larger luminosity would help in improving the statistical significance; therefore, we emphasize that the distribution of $\cos \theta^*$ arising from the *Z* boson decay as well as the associated asymmetry variables, C_{θ_Z} and C_Z prove quite useful in identifying the nature of the NLSP. The distinctive features of the variables discussed for distinguishing a longitudinal and transversely polarized *Z* boson are also applicable for new physics scenarios, where a polarized gauge boson is likely to be produced and therefore, can prove very important in studying BSM physics.

VIII. SUMMARY AND CONCLUSIONS

In this work, we have considered Higgsino-like NLSP in the presence of a light keV \tilde{G} LSP in the framework of phenomenological MSSM. The keV scale \tilde{G} serves as a warm dark matter candidate, significantly relaxing constraints from dark matter searches on the MSSM spectrum and thereby, allowing low μ parameter values. In addition, presence of a light \tilde{G} allows decay of the NLSP to a Higgs/Z boson and \tilde{G} leading to hard b jets and charged by the \tilde{G} . Such a scenario has been extensively explored by experiments, including the LHC, with a primary focus on the low-lying electroweak sector, leading to stringent constraints on the parameter space. The question that one ventures to answer in this study is as follows: What are the future prospects of detecting a Higgsino-like $\tilde{\chi}_1^0$ NLSP at LHC? If detected, how can we ascertain the nature of the NLSP?

an opposite sign same-flavor lepton pair from the Z boson decay besides large $\not\!\!\!E_T$. We choose a few representative benchmark points encompassing a light and heavy Higgsino sector with/without strong sector sparticles within the reach of LHC. We find that such a signal is discoverable in the upcoming runs of the high luminosity LHC after suitable cuts are applied. It is important to emphasize that such a semileptonic channel will prove crucial in identifying the nature of the NLSP, being relatively clean compared to an all hadronic final state, which may have a better discovery prospect. Thus, simultaneous use of both channels could be advocated for the purpose of discovery and identifying the nature of the NLSP. We focus on the presence of a dominantly longitudinal Z boson arising from the decay of a Higgsino-like NLSP owing to the presence of the Goldstone boson as the longitudinal mode of Z after electroweak symmetry breaking. This is quite a striking identification criteria if observable, for a Higgsinolike NLSP in sharp contrast to a dominantly gauginolike NLSP, which would dominantly decay to a transversely polarized Z. It is thus important to characterize the features of the longitudinally polarized Z boson to ascertain the composition of the parent NLSP. The effects of polarization of the Z boson are carried by its decay products, namely, the leptons through their angular distributions. We construct several kinematic variables using the negatively charged lepton as a reference and highlight its importance in observing the polarization of the parent gauge boson. We also propose new variables which utilize the observed asymmetries between the angular variables for the charged lepton coming from a parent longitudinal and transverse Z boson. We do a full detector level simulation of the events and study the asymmetries that show the characteristic features of a longitudinal Z boson and observe substantial differences between a Higgsino and gauginolike NLSP. This highlights the robustness of the constructed asymmetries. Our analysis is applicable to other BSM scenarios, which predict preferential production of longitudinally polarized gauge bosons as a consequence of the equivalence theorem.

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- [1] https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/ CombinedSummaryPlots/SUSY.
- [2] https://twiki.cern.ch/twiki/bin/view/CMSPublic/Physics ResultsSUS.
- [3] N. Aghanim *et al.*, Planck 2018 results. VI. Cosmological parameters (2018), https://inspirehep.net/literature/ 1682902.
- [4] J. Fan and M. Reece, In Wino veritas? Indirect searches shed light on neutralino dark matter, J. High Energy Phys. 10 (2013) 124.
- [5] M. Abdughani, J. Ren, and J. Zhao, Tev susy dark matter confronted with the current direct and indirect detection data, Eur. Phys. J. C 79, 146 (2019).
- [6] G. Arcadi, M. Dutra, P. Ghosh, M. Lindner, Y. Mambrini, M. Pierre, S. Profumo, and F. S. Queiroz, The waning of the wimp? A review of models, searches, and constraints, Eur. Phys. J. C 78, 203 (2018).
- [7] H. Baer, V. Barger, D. Sengupta, and X. Tata, Is natural higgsino-only dark matter excluded?, Eur. Phys. J. C 78, 838 (2018).
- [8] M. Abdughani, L. Wu, and J. M. Yang, Status and prospects of light binohiggsino dark matter in natural SUSY, Eur. Phys. J. C 78, 4 (2018).
- [9] S. P. Martin, A supersymmetry primer, Adv. Ser. Dir. High Energy Phys. **18**, 1 (1998).

- [10] M. Drees, R. Godbole, and P. Roy, Theory and Phenomenology of Sparticles: An Account of Four-Dimensional N=1 Supersymmetry in High Energy Physics (World Scientific. Singapore, 2004).
- [11] G. F. Giudice and R. Rattazzi, Theories with gauge mediated supersymmetry breaking, Phys. Rep. 322, 419 (1999).
- [12] J. Baur, N. Palanque-Delabrouille, C. Yèche, C. Magneville, and M. Viel, Lyman-alpha Forests cool warm dark matter, J. Cosmol. Astropart. Phys. 08 (2016) 012.
- [13] A. Boyarsky, J. Lesgourgues, O. Ruchayskiy, and M. Viel, Lyman-alpha constraints on warm and on warm-plus-cold dark matter models, J. Cosmol. Astropart. Phys. 05 (2009) 012.
- [14] L. Covi, Dark matter candidates: Axino and gravitino, in Proceedings, 46th Rencontres de Moriond on Electroweak Interactions and Unified Theories: La Thuile, Italy, 2011, pp. 381–388, https://indico.in2p3.fr/event/4403/session/12/ contribution/34/material/paper/0.pdf.
- [15] P. Meade, M. Reece, and D. Shih, Prompt decays of general neutralino NLSPs at the tevatron, J. High Energy Phys. 05 (2010) 105.
- [16] K. T. Matchev and S. D. Thomas, Higgs and Z boson signatures of supersymmetry, Phys. Rev. D 62, 077702 (2000).
- [17] A. M. Sirunyan *et al.*, Combined search for electroweak production of charginos and neutralinos in proton-proton collisions at $\sqrt{s} = 13$ TeV, J. High Energy Phys. 03 (2018) 160.

- [18] https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/Combined SummaryPlots/SUSY/ATLAS_SUSY_EWSummary_GGM/ ATLAS_ SUSY_EWSummary_GGM.png.
- [19] H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev, and X. Tata, Radiative natural supersymmetry: Reconciling electroweak fine-tuning and the Higgs boson mass, Phys. Rev. D 87, 115028 (2013).
- [20] H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev, and X. Tata, Naturalness, supersymmetry and light higgsinos: A snowmass whitepaper, in *Proceedings, Community Summer Study 2013: Snowmass on the Mississippi* (CSS2013): Minneapolis, MN, USA, 2013, https://inspirehep .net/record/1238302/files/arXiv:1306.2926.pdf.
- [21] A. Mustafayev and X. Tata, Supersymmetry, naturalness, and light higgsinos, Indian J. Phys. 88, 991 (2014).
- [22] H. Baer, V. Barger, P. Huang, A. Mustafayev, and X. Tata, Radiative Natural SUSY with a 125 GeV Higgs Boson, Phys. Rev. Lett. **109**, 161802 (2012).
- [23] H. Baer, V. Barger, M. Savoy, and X. Tata, Multichannel assault on natural supersymmetry at the high luminosity LHC, Phys. Rev. D 94, 035025 (2016).
- [24] H. Baer, V. Barger, J. S. Gainer, P. Huang, M. Savoy, D. Sengupta, and X. Tata, Gluino reach and mass extraction at the lhc in radiatively-driven natural susy, Eur. Phys. J. C 77, 499 (2017).
- [25] H. Baer and X. Tata, Weak Scale Supersymmetry: From Superfields to Scattering Events (Cambridge University Press, Cambridge, England, 2006).
- [26] M. Drees, M. M. Nojiri, D. P. Roy, and Y. Yamada, Light Higgsino dark matter, Phys. Rev. D 56, 276 (1997); Erratum, Phys. Rev. D 64, 039901 (2001).
- [27] G. F. Giudice and A. Pomarol, Mass degeneracy of the Higgsinos, Phys. Lett. B 372, 253 (1996).
- [28] A. Djouadi, The anatomy of electro-weak symmetry breaking. II. The Higgs bosons in the minimal supersymmetric model, Phys. Rep. 459, 1 (2008).
- [29] L. Covi, J. Hasenkamp, S. Pokorski, and J. Roberts, Gravitino dark matter and general neutralino NLSP, J. High Energy Phys. 11 (2009) 003.
- [30] J. Hasenkamp, General neutralino NLSP with gravitino dark matter vs. big bang nucleosynthesis, Ph.D. Thesis, Hamburg University, 2009.
- [31] W. Porod, SPheno, A program for calculating supersymmetric spectra, SUSY particle decays and SUSY particle production at e+ e- colliders, Comput. Phys. Commun. 153, 275 (2003).
- [32] W. Porod and F. Staub, SPheno 3.1: Extensions including flavour, *CP*-phases and models beyond the MSSM, Comput. Phys. Commun. **183**, 2458 (2012).
- [33] M. Aaboud *et al.*, Search for pair production of higgsinos in final states with at least three *b*-tagged jets in $\sqrt{s} = 13$ TeV *pp* collisions using the ATLAS detector, Phys. Rev. D **98**, 092002 (2018).
- [34] A. M. Sirunyan *et al.*, Search for Physics Beyond the Standard Model in Events with High-Momentum Higgs Bosons and Missing Transverse Momentum in Proton-Proton Collisions at 13 TeV, Phys. Rev. Lett. **120**, 241801 (2018).
- [35] M. Aaboud *et al.*, Search for supersymmetry in events with four or more leptons in $\sqrt{s} = 13$ TeV *pp* collisions with ATLAS, Phys. Rev. D **98**, 032009 (2018).

- [36] M. Aaboud *et al.*, Search for squarks and gluinos in final states with jets and missing transverse momentum using 36 fb⁻¹ of $\sqrt{s} = 13$ TeV pp collision data with the ATLAS detector, Phys. Rev. D **97**, 112001 (2018).
- [37] M. Aaboud *et al.* (ATLAS Collaboration), Search for chargino and neutralino production in final states with a Higgs boson and missing transverse momentum at $\sqrt{s} = 13$ TeV with the ATLAS detector, Phys. Rev. D **100**, 012006 (2019).
- [38] A. M. Sirunyan *et al.*, Search for new phenomena in final states with two opposite-charge, same-flavor leptons, jets, and missing transverse momentum in pp collisions at $\sqrt{s} = 13$ TeV, J. High Energy Phys. 03 (2018) 076.
- [39] A. M. Sirunyan *et al.* (CMS Collaboration), Search for Physics beyond the Standard Model in Events with High-Momentum Higgs Bosons and Missing Transverse Momentum in Proton-Proton Collisions at 13 tev, Phys. Rev. Lett. **120**, 241801 (2018).
- [40] A. M. Sirunyan *et al.*, Combined measurements of Higgs boson couplings in proton-proton collisions at $\sqrt{s} = 13$ TeV, Eur. Phys. J. C **79**, 421 (2019).
- [41] S. Chatrchyan *et al.*, Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC, Phys. Lett. B **716**, 30 (2012).
- [42] A. Arbey, M. Battaglia, A. Djouadi, F. Mahmoudi, and J. Quevillon, Implications of a 125 gev higgs for supersymmetric models, Phys. Lett. B 708, 162 (2012).
- [43] LEPSUSYWG et al., LEP2 SUSY Working Group, http:// lepsusy.web.cern.ch/lepsusy/.
- [44] M. Drees, H. Dreiner, D. Schmeier, J. Tattersall, and J. S. Kim, CheckMATE: Confronting your favourite new physics model with LHC data, Comput. Phys. Commun. 187, 227 (2015).
- [45] J. Alwall, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni, O. Mattelaer, H. S. Shao, T. Stelzer, P. Torrielli, and M. Zaro, The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations, J. High Energy Phys. 07 (2014) 079.
- [46] N. D. Christensen, P. de Aquino, N. Deutschmann, C. Duhr, B. Fuks, C. Garcia-Cely, O. Mattelaer, K. Mawatari, B. Oexl, and Y. Takaesu, Simulating spin-3/2 particles at colliders, Eur. Phys. J. C 73, 2580 (2013).
- [47] T. Sjostrand, S. Mrenna, and P.Z. Skands, PYTHIA6.4 physics and manual, J. High Energy Phys. 05 (2006) 026.
- [48] PYTHIA, http://home.thep.lu.se/ torbjorn/pythia81html/ Welcome.html.
- [49] J. de Favereau, C. Delaere, P. Demin, A. Giammanco, V. Lemaître, A. Mertens, and M. Selvaggi, DELPHES3, A modular framework for fast simulation of a generic collider experiment, J. High Energy Phys. 02 (2014) 057.
- [50] M. Cacciari, G. P. Salam, and Gr. Soyez, The Anti- k_t jet clustering algorithm, J. High Energy Phys. 04 (2008) 063.
- [51] M. Cacciari, G. P. Salam, and G. Soyez, FastJet user manual, Eur. Phys. J. C 72, 1896 (2012).
- [52] H.-C. Cheng and Z. Han, Minimal kinematic constraints and MT2, J. High Energy Phys. 12 (2008) 063.
- [53] W. Beenakker, R. Hopker, and M. Spira, PROSPINO: A program for the production of supersymmetric particles in next-to-leading order QCD (1996), http://www.thphys.uniheidelberg.de/~plehn/index.php?show=prospino&visible= tools.

- [54] W. Beenakker, C. Borschensky, M. Krämer, A. Kulesza, E. Laenen, S. Marzani, and J. Rojo, NLO+NLL squark and gluino production cross-sections with threshold-improved parton distributions, Eur. Phys. J. C 76, 53 (2016).
- [55] https://twiki.cern.ch/twiki/bin/view/LHCPhysics/LHCHXS WG1HELHCXsecs.
- [56] M. Grazzini, S. Kallweit, D. Rathlev, and M. Wiesemann, $W^{\pm}Z$ production at hadron colliders in NNLO QCD, Phys. Lett. B **761**, 179 (2016).
- [57] F. Cascioli, T. Gehrmann, M. Grazzini, S. Kallweit, P. Maierhöfer, A. von Manteuffel, S. Pozzorini, D. Rathlev, L. Tancredi, and E. Weihs, ZZ production at hadron colliders in NNLO QCD, Phys. Lett. B 735, 311 (2014).
- [58] M. Czakon, P. Fiedler, and A. Mitov, Total Top-Quark Pair-Production Cross Section at Hadron Colliders Through $O(\frac{4}{5})$, Phys. Rev. Lett. **110**, 252004 (2013).
- [59] LHC TTbar NNLO, https://twiki.cern.ch/twiki/bin/view/ LHCPhysics/TtbarNNLO#Top_quark_pair_cross_sections_at.
- [60] M. J. Duncan, G. L. Kane, and W. W. Repko, Ww physics at future colliders, Nucl. Phys. B272, 517 (1986).

- [61] M. Aaboud *et al.*, Measurement of $W^{\pm}Z$ production cross sections and gauge boson polarisation in *pp* collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector, Eur. Phys. J. C **79**, 535 (2019).
- [62] P. Meade, M. Reece, and D. Shih, Long-lived neutralino NLSPs, J. High Energy Phys. 10 (2010) 067.
- [63] G. Brooijmans *et al.*, Les Houches 2017: Physics at TeV colliders new physics working group report, in *10th Les Houches Workshop on Physics at TeV Colliders* (*PhysTeV 2017*) *Les Houches, France, 2017* (2018), http://lss.fnal.gov/archive/2017/conf/fermilab-conf-17-664ppd.pdf.
- [64] J. R. Andersen *et al.*, Les Houches 2017: Physics at TeV colliders Standard Model working group report, in 10th Les Houches Workshop on Physics at TeV Colliders (PhysTeV 2017) Les Houches, France, 2017 (2018), http:// lss.fnal.gov/archive/2018/conf/fermilab-conf-18-122-cd-t .pdf.
- [65] F. James, *Statistical Methods in Experimental Physics* (World Scientific, Singapore, 2006).