

**Measurements of the branching fractions $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0)$,
 $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$ and $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0)$**

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Using the data sample of 711 fb^{-1} of $\Upsilon(4S)$ on-resonance data taken by the Belle detector at the KEKB asymmetric-energy electron-positron collider, we present the first measurements of branching fractions of the decays $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0$, $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$. The signal yields for these decays are extracted from the recoil mass spectrum of the system recoiling against $\bar{\Lambda}_c^-$ baryons in selected B^- candidates. The branching fraction of $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$ is measured to be $(1.1 \pm 0.4 \pm 0.2) \times 10^{-3}$, where the first uncertainty is statistical and the second is systematic. The 90% credibility level upper limits on $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0)$ and $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$ are determined to be 6.5×10^{-4} and 7.9×10^{-4} , respectively.

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I. INTRODUCTION

Charm physics is of high interest mainly due to the fact that the charm system provides a unique laboratory to study the subtle interplay of strong and weak interactions. Baryons with one charm quark and two light quarks are called charmed baryons. In the heavy quark symmetry (HQS) approach [1], the two light quarks are regarded as a light diquark. As chiral symmetry and HQS can provide some qualitative insights into their dynamics, the study of charmed baryons plays an important role in improving our understanding of the quark confinement mechanism. The Ξ_c charmed baryon states contain one charm quark, one strange quark, and one up or down quark. The ground state Ξ_c^0 and Ξ_c^+ baryons, which have spin-parity quantum numbers $J^P = \frac{1}{2}^+$ and no internal orbital angular momentum, are the only members of the group that decay weakly. A growing number of excited Ξ_c states have been observed in different experiments [2]. However, much is still unknown about them. Many theoretical approaches have been used to study the excitation spectrum of Ξ_c baryons and their decays. These models include quark models, heavy quark $1/m_Q$ and $1/N_c$ expansions, the coupled channel model, and QCD sum rules [3–7]. Through these QCD-inspired relativistic theories, the mass spectrum of excited Ξ_c can be predicted. Recently, the masses and intrinsic widths of isodoublets of the excited Ξ_c states Ξ_c' , $\Xi_c(2645)$, $\Xi_c(2790)$, $\Xi_c(2815)$, and $\Xi_c(2980)$ were measured more precisely by Belle by analyzing their exclusive decays [8].

The decay $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0$ proceeds via $b \rightarrow c\bar{c}s$ transition and has a relatively large branching fraction of the order of 10^{-3} [2,9]. Therefore, a B -meson factory provides an experimental research platform to investigate the Ξ_c^0 excitation spectrum exclusively through $B^- \rightarrow \bar{\Lambda}_c^- + \text{anything}$ decays. This makes it possible to search for missing excited Ξ_c^0 states. In addition, the measurement of their production rates is a good test for the theoretical calculation of $b \rightarrow c\bar{c}s$ transition processes.

In this paper, we measure the branching fractions of $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$ decays based on data collected by the Belle detector at the KEKB asymmetric-energy electron-positron collider. Here and throughout this paper, Ξ_c^{*0} represents Ξ_c^0 , $\Xi_c(2645)^0$, and $\Xi_c(2790)^0$ unless otherwise stated. We use a full hadron-reconstruction algorithm [10] to tag a B^+ signal, denoted B_{tag}^+ , and then reconstruct a $\bar{\Lambda}_c^-$ using its $\bar{p}K^+\pi^-$ and $\bar{p}K_S^0(K_S^0 \rightarrow \pi^+\pi^-)$ decay modes [11] from the remaining tracks. We search for peaks in the invariant mass spectrum of the system recoiling against the $\bar{\Lambda}_c^-$ baryons in the selected $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$ candidates, to extract Ξ_c^{*0} signal yields, from which we calculate the branching fractions of $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$.

II. DATA SAMPLE AND THE BELLE DETECTOR

This analysis utilizes a data sample of 711 fb^{-1} collected at the $\Upsilon(4S)$ on-resonance corresponding to $(772 \pm 11) \times 10^6 B\bar{B}$ pairs. All the data were collected with the Belle detector [12] operating at the KEKB asymmetric-energy e^+e^- collider [13]. The Belle detector is described in detail in Ref. [12]. It is a large solid-angle magnetic spectrometer consisting of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals located

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inside a superconducting solenoid coil that provides a 1.5T magnetic field. An iron flux return placed outside the coil is instrumented to detect K_L^0 mesons and to identify muons.

To optimize the signal selection criteria and to determine the signal reconstruction efficiency, Monte Carlo (MC) signal events are generated using EvtGen [14], while Ξ_c^{*0} inclusive decays are simulated using PYTHIA [15]. These events are processed by a detector simulation based on GEANT3 [16]. Inclusive MC samples of $\Upsilon(4S) \rightarrow B\bar{B}$ ($B = B^+$ or B^0) and $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) events at $\sqrt{s} = 10.58$ GeV corresponding to more than three times the integrated luminosity of the data are used to check the backgrounds.

III. COMMON EVENT SELECTION CRITERIA

To select the signal candidates, the following event selection criteria are applied. For well-reconstructed charged tracks, except those from $K_S^0 \rightarrow \pi^+\pi^-$ decays, the impact parameters perpendicular to and along the beam direction with respect to the nominal interaction point (IP) are required to be less than 1 and 4 cm, respectively, and the transverse momentum in the laboratory frame is required to be larger than 0.1 GeV/ c . For the particle identification of a well-reconstructed charged track, information from different detector subsystems, including specific ionization in the CDC, time measurement in the TOF, and the response of the ACC, is combined to form a likelihood \mathcal{L}_i [17] for particle species i , where $i = \pi, K$, or p . Tracks with $R_K = \mathcal{L}_K/(\mathcal{L}_K + \mathcal{L}_\pi) < 0.4$ are identified as pions with an efficiency of 97%, while 5% of kaons are misidentified as pions; tracks with $R_K > 0.6$ are identified as kaons with an efficiency of 95%, while 4% of pions are misidentified as kaons. A track with $\mathcal{R}_p^\pi = \mathcal{L}_p/(\mathcal{L}_p + \mathcal{L}_\pi) > 0.6$ and $\mathcal{R}_p^K = \mathcal{L}_p/(\mathcal{L}_p + \mathcal{L}_K) > 0.6$ is identified as an (anti)proton with an efficiency of about 97%; fewer than 1% of the pions and kaons are misidentified as (anti)protons. With the exception of those from K_S^0 decays, all charged tracks are required to be positively identified by the above procedure.

The K_S^0 candidates are first reconstructed from pairs of oppositely charged tracks, which are treated as pions, with a production vertex significantly separated from the average IP, then selected using a multivariate analysis using an artificial neural network [18] based on two sets of input variables [19].

Applying a full reconstruction algorithm of hadronic B -meson decays [10] which uses a multivariate analysis based on the NeuroBayes package, we reconstruct B_{tag}^+ candidates. Each B_{tag}^+ candidate has an output value O_{NN} from the multivariate analysis ranging from 0 to 1. A candidate with larger O_{NN} is more likely to be a true B meson. If multiple B_{tag}^+ candidates are found in an event, only the candidate with largest O_{NN} is selected. To improve the purity of the tagged side, we take $O_{\text{NN}} > 0.001$, $M_{\text{bc}}^{\text{tag}} > 5.27$ GeV/ c^2 ,

and $|\Delta E^{\text{tag}}| < 0.04$ GeV as the signal region. Here, $M_{\text{bc}}^{\text{tag}} \equiv \sqrt{E_{\text{beam}}^2 - (\sum_i \vec{p}_i^{\text{tag}})^2}$ and $\Delta E^{\text{tag}} \equiv \sum_i E_i^{\text{tag}} - E_{\text{beam}}$, where $E_{\text{beam}} \equiv \sqrt{s}/2$ is the beam energy and $(E_i^{\text{tag}}, \vec{p}_i^{\text{tag}})$ is the 4-momentum of the B_{tag}^+ daughter i in the e^+e^- center-of-mass system. After reconstructing the B_{tag}^+ candidate, the $\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-$ and $\bar{\Lambda}_c^- \rightarrow \bar{p}K_S^0$ decays are reconstructed from the remaining tracks. We perform a fit for the $\bar{\Lambda}_c^-$ decay vertex and require that $\chi_{\text{vertex}}^2/\text{n.d.f.} < 15$, where n.d.f. is the number of degrees of freedom. The multi-combination rate of $\bar{\Lambda}_c^-$ candidates is 21%. If there is more than one $\bar{\Lambda}_c^-$ candidate in an event, the candidate with the smallest $\chi_{\text{vertex}}^2/\text{n.d.f.}$ is selected. The $\bar{\Lambda}_c^-$ signal region is defined to be $|M_{\bar{\Lambda}_c^-} - m_{\bar{\Lambda}_c^-}| < 10$ MeV/ c^2 corresponding to about 3σ , where σ denotes the standard deviation. Here, $M_{\bar{\Lambda}_c^-}$ is the reconstructed and $m_{\bar{\Lambda}_c^-}$ is the nominal mass of the $\bar{\Lambda}_c^-$ [2].

IV. Ξ_c^{*0} , $\Xi_c(2645)^0$, AND $\Xi_c(2790)^0$ SIGNAL EXTRACTION

We extract the number of Ξ_c^{*0} , $\Xi_c(2645)^0$, and $\Xi_c(2790)^0$ baryons in decays of the type $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$, $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$ by fitting the recoiling mass spectrum ($M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}}$). We choose 2.5 GeV/ $c^2 < M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}} < 2.86$ GeV/ c^2 as the fit region. To improve the recoil mass resolution, we use $M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}} \equiv M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{miss}} + M_{B_{\text{tag}}^+} - m_B + M_{\bar{\Lambda}_c^-} - m_{\bar{\Lambda}_c^-}$, where $M_{B_{\text{tag}}^+}$ is the reconstructed and m_B is the nominal mass [2] of the B^+ meson and $M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{miss}}$ is the invariant mass recoiling against the $\bar{\Lambda}_c^-$ on the signal side, which is calculated using $\sqrt{(P_{\text{c.m.s.}} - P_{B_{\text{tag}}^+} - P_{\bar{\Lambda}_c^-})^2}$ with $P_{\text{c.m.s.}}$, $P_{B_{\text{tag}}^+}$, and $P_{\bar{\Lambda}_c^-}$ being 4-momenta of the initial e^+e^- system, the reconstructed B_{tag}^+ meson, and the reconstructed $\bar{\Lambda}_c^-$ baryon, respectively.

Figure 1 shows the ΔE^{tag} distribution in the Ξ_c^{*0} signal region, i.e., 2.5 GeV/ $c^2 < M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}} < 2.86$ GeV/ c^2 , after applying all of the above requirements. A double-Gaussian function is used as the signal shape, and the background shape is described by a first-order polynomial. Because of the small sample size, the parameters of the double-Gaussian function are fixed to the values obtained by fitting the signal MC distribution. The fit results are shown as curves in Fig. 1. We take $|\Delta E^{\text{tag}}| < 0.04$ GeV as the signal region.

Figure 2 shows the scatter plot of $M_{\bar{\Lambda}_c^-}$ of the signal side in the Ξ_c^{*0} signal region vs $M_{\text{bc}}^{\text{tag}}$ of the B_{tag}^+ . To check for possible peaking backgrounds, the $M_{\text{bc}}^{\text{tag}}$ and $M_{\bar{\Lambda}_c^-}$ sideband regions are selected as shown in Fig. 2. The normalized contribution from the $M_{\text{bc}}^{\text{tag}}$ and $M_{\bar{\Lambda}_c^-}$ sidebands is estimated using 50% of the number of events in the blue dashed boxes

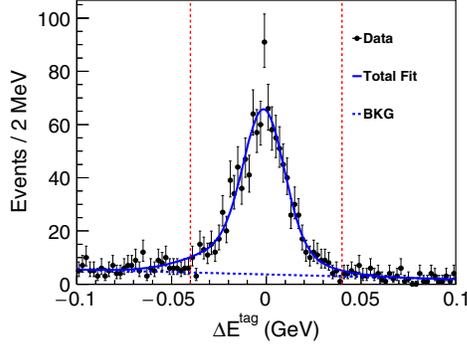


FIG. 1. ΔE^{tag} distribution summed over the two reconstructed $\bar{\Lambda}_c^-$ decay modes. The points with error bars represent the data, the solid curve is the best-fit result, and the blue dashed curve is the fitted background. The red dashed lines show the defined ΔE^{tag} signal region.

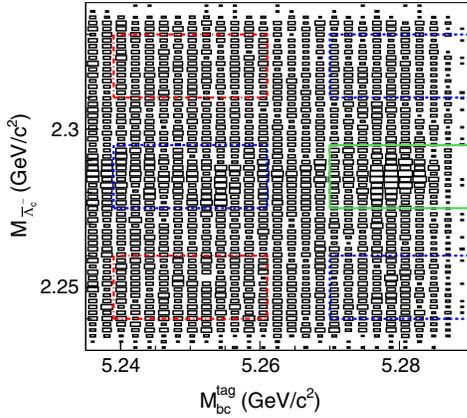


FIG. 2. Scatter plot of $M_{\bar{\Lambda}_c^-}$ of signal side vs M_{bc}^{tag} of B_{tag}^+ in the Ξ_c^{*0} signal region, i.e., $2.5 \text{ GeV}/c^2 < M_{bc}^{\text{tag}} < 2.86 \text{ GeV}/c^2$. The solid box shows the selected signal region, and the blue and red dashed boxes define the M_{bc}^{tag} and $M_{\bar{\Lambda}_c^-}$ sidebands described in the text.

minus 25% of the number of events in the red dashed boxes. Figure 3 shows the $M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}}$ distribution in the signal box (points with error bars) and in the sideband boxes (shaded histogram). No peaking background is found in the M_{bc}^{tag} and $M_{\bar{\Lambda}_c^-}$ sideband events or in the inclusive MC samples of $\Upsilon(4S) \rightarrow B\bar{B}$ and $e^+e^- \rightarrow q\bar{q}$ events.

To extract the Ξ_c^{*0} signal yields, an unbinned maximum-likelihood fit to the $M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}}$ distribution is performed. In this fit, the Ξ_c^{*0} signal shape is described by a double-Gaussian function, while the $\Xi_c(2645)^0$ and $\Xi_c(2790)^0$ signal shapes are Breit-Wigner (BW) functions convolved with double-Gaussian functions. The background is parametrized by a second-order polynomial function. Due to the limited sample size, the values of the

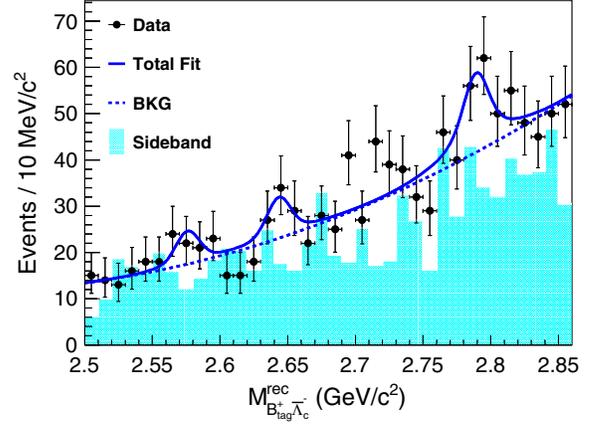


FIG. 3. $M_{B_{\text{tag}}^+ \bar{\Lambda}_c^-}^{\text{rec}}$ distribution of selected candidate events. The points with error bars represent the data, the solid blue curve is the best fit, the dashed curve is the fitted total background, and the cyan shaded histogram is the normalized distribution of the M_{bc}^{tag} and $M_{\bar{\Lambda}_c^-}$ sideband events (see Fig. 2).

parameters in double-Gaussian functions are fixed to those obtained from the fit to the corresponding signal MC distribution. For $\Xi_c(2645)^0$ and $\Xi_c(2790)^0$ signal shapes, the masses and widths of BW functions are fixed to world average values [2]. The fit result is shown in Fig. 3. The difference between the fitted background level and the normalized M_{bc}^{tag} and $M_{\bar{\Lambda}_c^-}$ sidebands is due to the contribution from other multibody B^- decay modes with a $\bar{\Lambda}_c^-$, for example, $B^- \rightarrow K^- \Lambda_c^+ \bar{\Lambda}_c^-$.

The numbers of fitted Ξ_c^{*0} , $\Xi_c(2645)^0$, and $\Xi_c(2790)^0$ signal events are $N_{\Xi_c^{*0}} = 17.9 \pm 10.4$, $N_{\Xi_c(2645)^0} = 24.1 \pm 13.0$, and $N_{\Xi_c(2790)^0} = 59.9 \pm 22.5$ with statistical significances of 1.7σ , 1.9σ , and 3.1σ , respectively. Here, the statistical significances are defined as $\sqrt{-2\ln(\mathcal{L}_0/\mathcal{L}_{\text{max}})}$, where \mathcal{L}_0 and \mathcal{L}_{max} are the maximized likelihoods without and with a signal component, respectively [20,21]. The $\Xi_c(2790)^0$ signal significance becomes 3.0σ when systematic uncertainties are included (see below).

Then, the branching fractions are

$$\begin{aligned} \mathcal{B}_{\bar{\Lambda}_c^- \Xi_c^{*0}} &= \frac{N_{\Xi_c^{*0}}}{2N_{B^-}(\epsilon_{\bar{p}K^+\pi^-}^{\Xi_c^{*0}} \mathcal{B}_1 + \epsilon_{\bar{p}K_s^0}^{\Xi_c^{*0}} \mathcal{B}_2)} \\ &= (3.4 \pm 2.0) \times 10^{-4}, \\ \mathcal{B}_{\bar{\Lambda}_c^- \Xi_c(2645)^0} &= \frac{N_{\Xi_c(2645)^0}}{2N_{B^-}(\epsilon_{\bar{p}K^+\pi^-}^{\Xi_c(2645)^0} \mathcal{B}_1 + \epsilon_{\bar{p}K_s^0}^{\Xi_c(2645)^0} \mathcal{B}_2)} \\ &= (4.4 \pm 2.4) \times 10^{-4}, \end{aligned}$$

and

TABLE I. The detection efficiencies $\varepsilon_{\bar{p}K^+\pi^-}^{\Xi_c^0}$ and $\varepsilon_{\bar{p}K_S^0}^{\Xi_c^0}$ including the B_{tag}^+ meson for the studied $\bar{\Lambda}_c^-$ decay modes as obtained from MC simulated $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$ processes. All the uncertainties here are statistical only.

Ξ_c^{*0} type	Ξ_c^0	$\Xi_c(2645)^0$	$\Xi_c(2790)^0$
$\varepsilon_{\bar{p}K^+\pi^-}^{\Xi_c^0}$ (%)	0.09 ± 0.003	0.09 ± 0.003	0.09 ± 0.003
$\varepsilon_{\bar{p}K_S^0}^{\Xi_c^0}$ (%)	0.13 ± 0.003	0.14 ± 0.004	0.15 ± 0.004

$$\begin{aligned} \mathcal{B}_{\bar{\Lambda}_c^- \Xi_c(2790)^0} &= \frac{N_{\Xi_c(2790)^0}}{2N_{B^-}(\varepsilon_{\bar{p}K^+\pi^-}^{\Xi_c(2790)^0} \mathcal{B}_1 + \varepsilon_{\bar{p}K_S^0}^{\Xi_c(2790)^0} \mathcal{B}_2)} \\ &= (1.1 \pm 0.4) \times 10^{-3}, \end{aligned}$$

where $\mathcal{B}_{\bar{\Lambda}_c^- \Xi_c^0} = \mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0)$, $\mathcal{B}_{\bar{\Lambda}_c^- \Xi_c(2645)^0} = \mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$, $\mathcal{B}_{\bar{\Lambda}_c^- \Xi_c(2790)^0} = \mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0)$, $N_{B^-} = N_{\Upsilon(4S)} \mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^-)$ with $N_{\Upsilon(4S)}$ being the number of accumulated $\Upsilon(4S)$ events. We use a value of 0.514 for $\mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^-)$ [2]; $\mathcal{B}_1 = \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-)$, $\mathcal{B}_2 = \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K_S^0) \mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-)$, $\mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-)$, $\mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K_S^0)$, and $\mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-)$ are the branching fractions of $\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-$, $\bar{\Lambda}_c^- \rightarrow \bar{p}K_S^0$, and $K_S^0 \rightarrow \pi^+\pi^-$ [2], respectively. $\varepsilon_{\bar{p}K^+\pi^-}^{\Xi_c^0}$ and $\varepsilon_{\bar{p}K_S^0}^{\Xi_c^0}$ are the detection efficiencies of different $\bar{\Lambda}_c^-$ decay modes which are obtained from fits to the signal MC samples and are listed in Table I.

Since the statistical significances of Ξ_c^0 and $\Xi_c(2645)^0$ are less than 3σ , Bayesian upper limits at 90% credibility level (C.L.) [22] assuming a uniform prior probability for $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0)$ and $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$ (denoted \mathcal{B}^{up}) are determined by solving the equation

$$\int_0^{\mathcal{B}^{\text{up}}} \mathcal{L}(\mathcal{B}) d\mathcal{B} / \int_0^1 \mathcal{L}(\mathcal{B}) d\mathcal{B} = 0.9,$$

TABLE II. Summary of the fitted signal yields (N_{sig}), branching fractions (90% C.L. upper limits), and statistical signal significances (σ) for $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0$, $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$. All the uncertainties here are statistical only.

	N_{sig}	$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0})$ [Upper limit]	Significance (σ)
Ξ_c^0	17.9 ± 10.4	$(3.4 \pm 2.0) \times 10^{-4}$ [6.5×10^{-4}]	1.7
$\Xi_c(2645)^0$	24.1 ± 13.0	$(4.4 \pm 2.4) \times 10^{-4}$ [7.9×10^{-4}]	1.9
$\Xi_c(2790)^0$	59.9 ± 22.5	$(1.1 \pm 0.4) \times 10^{-3}$	3.1

TABLE III. Summary of the relative systematic uncertainties on the branching-fraction measurements (%) for $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0$, $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$.

Observable	Efficiency	Fit	$\bar{\Lambda}_c^-$ decays	B_{tag}	N_{B^\pm}	Total	Measured value
$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0)$	3.1	10.0	5.5	4.2	1.8	12.6	$(3.4 \pm 2.0 \pm 0.4) \times 10^{-4}$
$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$	3.3	8.1	5.5	4.2	1.8	11.3	$(4.4 \pm 2.4 \pm 0.5) \times 10^{-4}$
$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0)$	3.5	11.0	5.5	4.2	1.8	13.6	$(1.1 \pm 0.4 \pm 0.2) \times 10^{-3}$

where

$$\mathcal{B} = N_{\Xi_c^0} / 2N_{B^-} (\varepsilon_{\bar{p}K^+\pi^-}^{\Xi_c^0} \mathcal{B}_1 + \varepsilon_{\bar{p}K_S^0}^{\Xi_c^0} \mathcal{B}_2)$$

is the assumed branching fraction for $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0$ or $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$ and $\mathcal{L}(\mathcal{B})$ is the corresponding likelihood of the data. $N_{\Xi_c^0}$ is the fitted signal yield of Ξ_c^0 or $\Xi_c(2645)^0$. Taking into account the systematic uncertainty discussed below, the likelihoods are convolved with a Gaussian function of which the width equals the corresponding total systematic uncertainty. The 90% C.L. upper limits with systematic uncertainties included on $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0)$ and $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$ are determined to be 6.5×10^{-4} and 7.9×10^{-4} , respectively.

Table II summarizes the fitted results, branching fractions, and statistical significances for $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^0$, $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$. The uncertainties shown are statistical only.

V. SYSTEMATIC UNCERTAINTIES

There are several sources of systematic uncertainties for the branching-fraction measurements as listed in Table III, including the reconstruction efficiency-related sources, the fit uncertainty, the Λ_c decay branching fractions, the B -meson tag efficiency, and the total number of $B\bar{B}$ events.

The reconstruction efficiency-related uncertainties include those for tracking efficiency (0.35% per track), particle identification efficiency (1.44% per kaon, 0.86% per pion, and range from 2.13% to 3.13% per proton), as well as momentum-weighted K_S^0 selection efficiency (1.1%) [23]. Here, the systematic uncertainty due to the K_S^0 selection depends on the K_S^0 momentum and was determined using a control sample of $D^{*+} \rightarrow D^0(K_S^0)\pi^+$. For the three branching-fraction measurements, the individual reconstruction efficiency-related uncertainties from two

different $\bar{\Lambda}_c^-$ decay channels are added, linearly weighted by the product of the detection efficiency and $\bar{\Lambda}_c^-$ partial decay width. Then, those uncertainties are summed in quadrature to be the final uncertainties related to the efficiency of the reconstruction, yielding 3.1% to 3.5%, depending on the specific decay mode.

We estimate the systematic uncertainties associated with the fit by changing the order of the background polynomial, by changing the range of the fit, and by enlarging the mass resolution by 10%. The observed deviations are taken as systematic uncertainties. The masses of $\Xi_c(2790)^0$ and $\Xi_c(2815)^0$ are rather close, and no $\Xi_c(2815)^0$ signal peak can be seen. The $\Xi_c(2815)^0$ signal significance is only 0.4σ if it is added in the fit. So, we take the difference of the number of $\Xi_c(2790)^0$ signal events as the systematic uncertainty due to the possible contribution of $\Xi_c(2815)^0$ from $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2815)^0$. Finally, all the above uncertainties are summed in quadrature, and the sums are taken as the systematic uncertainties associated with the fit.

Uncertainties for the $\bar{\Lambda}_c^-$ decay branching fractions are due to $\mathcal{B}(\bar{\Lambda}_c^- \rightarrow f_i) = \Gamma_i \times \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-)$; here, $\Gamma_i = \mathcal{B}(\bar{\Lambda}_c^- \rightarrow f_i)/\mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-)$, and f_i denotes the different $\bar{\Lambda}_c^-$ decay modes. Uncertainties on $\mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-)$ and $\Gamma(\bar{\Lambda}_c^- \rightarrow \bar{p}K_s^0)/\Gamma(\bar{\Lambda}_c^- \rightarrow \bar{p}K^+\pi^-)$ are taken from Ref. [2]. The final uncertainties on the two $\bar{\Lambda}_c^-$ partial decay widths are summed in quadrature with the detection efficiency as a weighting factor. The uncertainty due to the B -meson tagging efficiency is 4.2% [24]. The uncertainty on $\mathcal{B}(\Upsilon(4S) \rightarrow B^+B^-)$ is 1.2% [2]. The systematic uncertainty on $N_{\Upsilon(4S)}$ is 1.37%. The sources of uncertainty summarized in Table III are assumed to be independent and thus are added in quadrature to obtain the total systematic uncertainty.

VI. CONCLUSION

Using the 711 fb^{-1} data sample taken at the $\Upsilon(4S)$ resonance that corresponds to $(772 \pm 11) \times 10^6 B\bar{B}$ pairs accumulated with the Belle detector at the KEKB asymmetric-energy e^+e^- collider, we present the first measurements of the branching fractions of the decays $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$, $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0$ with $\Xi_c^{*0} \rightarrow$ anything and the $\bar{\Lambda}_c^-$ candidates reconstructed via their $\bar{p}K^+\pi^-$ and $\bar{p}K_s^0$ decay modes. The branching fractions are measured to be

$$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}) = (3.4 \pm 2.0 \pm 0.4) \times 10^{-4},$$

$$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0) = (4.4 \pm 2.4 \pm 0.5) \times 10^{-4},$$

and

$$\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2790)^0) = (1.1 \pm 0.4 \pm 0.2) \times 10^{-3},$$

with statistical significances of 1.7σ , 1.9σ , and 3.1σ , respectively. Since the statistical significances are less than

3σ for $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0}$ and $B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0$, the 90% C.L. upper limits on $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c^{*0})$ and $\mathcal{B}(B^- \rightarrow \bar{\Lambda}_c^- \Xi_c(2645)^0)$ are determined to be 6.5×10^{-4} and 7.9×10^{-4} , respectively, with systematic uncertainties included.

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