

of spin 1 is the Weinberg analysis itself. It is amusing to note that if the coupling constants are defined as the coefficients of Feynman propagators, threshold factors would arise naturally so as to eliminate the contribution of $J > 1$ spin states.

Thus, for example, the g meson ($J^P = 3^-$) would contribute a term

$$M(\nu, t) = g_{g\pi\pi} g_{g\pi\pi} [(-2\nu)^3 + 6\nu t(t - 4m_\pi^2)/5] / (m_g^2 - t)$$

to $M_t^{(1)}(\nu, t)$ in the soft-pion limit. The term proportional to ν in this expression vanishes at $t=0$ and does not contribute in Eq. (5).

Insofar as this recipe differs from the constant residues prescribed in the dispersive approach, it is obviously *ad hoc*, as it allows in the residues only the threshold factors coming from the Feynman propagators, but no other t dependence.

Another point which should be emphasized is that our use of the $g_{\rho_i\pi\pi}$ obtained from the Veneziano-Lovelace formula has been for illustrative purposes only.

Indeed, in that simple model it is not true that only 1^- states contribute in Eq. (3). Thus, while the Veneziano formula can be easily made to yield the right magnitude of the $I_t=1$ scattering lengths, it does not satisfy the full restrictions of PCAC and current algebra—in particular, the requirement that only 1^- states contribute in Eq. (3).

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Baryon Spectral-Function Sum Rules*

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Necessary and sufficient conditions for baryon spectral-function sum rules are obtained under the assumptions that (1) the equal-time commutator of the axial charges $Q_s^a(x_0)$ ($a=1,2,3$) and the nucleon field $\bar{\psi}(y)$ is given by $[Q_s^a(y_0), \bar{\psi}(y)] = -r_A \bar{\psi}(y) \gamma_5 \tau^a + (\Delta I = \frac{3}{2}$ terms) and that (2) the axial-vector current $A_\mu^a(x)$ is conserved. For each of these sum rules (enumerated by $n=1,2,3\dots$), the equivalence to $\int d^3z \langle [Q_s^a(y_0), [(\partial/\partial y_0)^{2n-1} \psi(y), \bar{\psi}(z)]_+] |_{y_0=z_0} \rangle_0 = 0$ is actually shown under weaker conditions: assumption (1) and, instead of (2), $\sum_{j=0}^{2n-2} \langle [(\partial/\partial y_0)^j [\int d^3x \partial^\mu A_\mu^a(y_0 \mathbf{x}), (\partial/\partial y_0)^{2n-2-j} \psi(y)], \bar{\psi}(z)]_+ |_{y_0=z_0} \rangle_0 = 0$. Further equivalences are given. The sum rules connect the ($I = \frac{1}{2}, J = \frac{1}{2}^+$) and ($I = \frac{1}{2}, J = \frac{1}{2}^-$) baryon spectrum and include (for $n=1$) a sum rule, obtained independently by Rothleitner and (in the one-particle approximation) by Sugawara. In our derivation we make no assumptions on high-energy behavior and we use an identity of the Jacobi type. Assuming the first two sum rules to be valid, the model then predicts a $P_{11}(m > 1470 \text{ MeV})$ resonance [which may be identified as the observed $P_{11}(1750)$] from the existence of the four nucleon resonances $P_{11}(940)$, $P_{11}(1470)$, $S_{11}(1550)$, and $S_{11}(1710)$.

THE spectral-function sum rules, derived by Weinberg¹ for the chiral $SU(2) \otimes SU(2)$ currents, have been extended by several authors²⁻⁴ and various proofs have been given.¹⁻⁶ Among these, Glashow, Schnitzer, and Weinberg³ have described a derivation of the first Weinberg sum rule using the Jacobi identity, and Jackiw⁵ has used the Jacobi identity in order to derive a condition for the second Weinberg sum rule. The main difference between Weinberg's¹ original proof

of the second sum rule and the one given by Jackiw lies in the replacement of the assumption on high-energy behavior, made in Ref. 1, by the assumption that a certain vacuum expectation value of a triple commutator vanishes.

Among the extensions of the Weinberg sum rules, Rothleitner⁴ has derived a sum rule for baryon spectral functions, assuming that⁷

$$\lim_{p^2 \rightarrow \infty} \lim_{q_\mu \rightarrow 0} \int d^4x d^4y e^{-iqx + ipy} \times \langle iT \{ (q_\mu + \partial_\mu) A_\mu^a(x), \psi(y), \bar{\psi}(0) \} \rangle_0 = 0, \quad (1)$$

* Supported by the DAAD through a NATO grant.

¹ S. Weinberg, Phys. Rev. Letters **18**, 507 (1967).

² T. Das, V. S. Mathur, and S. Okubo, Phys. Rev. Letters **18**, 761 (1967); P. A. Cook and G. C. Joshi, Nucl. Phys. **B10**, 253 (1969).

³ S. L. Glashow, H. J. Schnitzer, and S. Weinberg, Phys. Rev. Letters **19**, 139 (1967).

⁴ J. Rothleitner, Nucl. Phys. **B3**, 89 (1967).

⁵ R. Jackiw, Phys. Letters **27B**, 96 (1968).

⁶ W. Bierter and K. M. Bitar, Nuovo Cimento Letters **1**, 192 (1969).

⁷ Depending on how the pion mass is treated, either of the two terms vanishes trivially: For massless pions and conserved axial currents, the $[\partial^\mu A_\mu^a(x)]$ term vanishes trivially (not the q_μ term, since it has a pion pole at $q_\mu=0$). For massive pions and PCAC, there is no pion pole at $q_\mu=0$, and the $(q^\mu A_\mu^a)$ term vanishes trivially. In order to leave room for both interpretations, we will not specify Eq. (1) further.

and that

$$[A_0^a(x), \bar{\psi}(y)]|_{x_0=y_0} = -r_A \bar{\psi}(x) \gamma_5 \tau^a \delta(\mathbf{x}-\mathbf{y}) + (\Delta I = \frac{3}{2} \text{ terms}). \quad (2)$$

In the above, we have denoted (for $a=1, 2, 3$) the axial-vector current by $A_\mu^a(x)$ and the nucleon field by $\bar{\psi}(y)$. The sum rule derived in Ref. 4 from Eqs. (1) and (2) reads

$$S_1 = \int_0^\infty dm^2 m [F_+^2(m^2) - F_-^2(m^2)] = 0, \quad (3)$$

where we have defined

$$\begin{aligned} (2\pi)^{3/2} \langle 0 | \psi(0) | m^2, \epsilon; \mathbf{p}, r; \alpha \rangle \\ = w_r(\mathbf{p}) F_+^\alpha(m^2) \quad \text{for } \epsilon = 1, \\ = i\gamma_5 w_r(\mathbf{p}) F_-^\alpha(m^2) \quad \text{for } \epsilon = -1. \end{aligned} \quad (4)$$

Here, $|m^2, \epsilon; \mathbf{p}, r; \alpha\rangle$ denotes a state with the same baryon number, spin, isospin, and strangeness as the nucleon; α stands for additional quantum numbers. We have also

$$F_\pm^2(m^2) = \sum_\alpha F_\pm^\alpha(m^2)^2. \quad (5)$$

If we saturate the sum rule (3) by one-particle intermediate states, it reads

$$\sum_i \epsilon_i F_{\epsilon_i}^2(m_i^2) m_i = 0. \quad (6)$$

This is the sum rule derived by Sugawara⁸ as a consequence of his self-consistency conditions. The proof of these conditions⁸ uses, in addition to Eq. (7) below, assumptions on analyticity and high-energy behavior.

The purpose of the present paper is twofold. First, in analogy to the derivations of the Weinberg sum rules using the Jacobi identity,^{3,5} we will derive the following statement by means of an algebraic identity.

Statement 1. Let^{9,11}

$$[Q_5^a(y_0), \bar{\psi}(y)] = -r_A \bar{\psi}(y) \gamma_5 \tau^a + \bar{\Delta}^{3/2}(y) \gamma_5 \quad (7)$$

and

$$\left\langle \left[\left[\int d^3x \partial^\mu A_\mu^a(x), \psi(y) \right], \bar{\psi}(z) \right]_+ \right\rangle_0 = 0, \quad (8)$$

where $\Delta^{3/2}(y)$ denotes possible $\Delta I = \frac{3}{2}$ terms. Then we have

$$\begin{aligned} 2r_A i\tau^a \gamma_5 \int dm^2 m [F_+^2(m^2) - F_-^2(m^2)] \delta(\mathbf{y}-\mathbf{z}) \\ = \langle [Q_5^a(y_0), [\psi(y), \bar{\psi}(z)]_+]_+ \rangle_0. \end{aligned} \quad (9)$$

⁸ M. Sugawara, Phys. Rev. **172**, 1423 (1968).

⁹ In the case $\Delta^{3/2}(y)=0$, it has been shown in Ref. 10 that $r_A = \pm \frac{1}{2}$ follows from charge algebra, and so does the commutator of $Q^a = \int d^3x V_0^a(x)$ with $\bar{\psi}(y)$. However, our present considerations do not depend on this fact.

¹⁰ H. Genz and J. Katz, Nuovo Cimento **64A**, 291 (1969).

¹¹ In the commutators and anticommutators written below, the equal-time limit is always understood, with the exception of Eq. (23).

In the above statement, $Q_5^a(x_0)$ is defined by

$$Q_5^a(x_0) = \int d^3x A_0^a(x). \quad (10)$$

Note that Eqs. (8) and (9) have *anticommutators* for fermion operators. The statement shows that given Eqs. (7) and (8), which we discuss below, at most the non-Schwinger part of the anticommutator $[\psi(y), \bar{\psi}(z)]_+$ survives in Eq. (9). The vanishing of this expression itself is then equivalent to the sum rule (3).

As to the validity of the assumption made, Eq. (7) is a consequence of the more restrictive assumption, Eq. (2), allowing for additional arbitrary Schwinger terms. Models in which Eq. (7) holds have been investigated by several authors,^{4,8,10,12-16} and in neither case was a contradiction with Eq. (7) found. On the contrary, assuming Eq. (7) without $\Delta^{3/2}(y)$ terms, Sugawara¹⁶ has reached reasonable agreement with experiment in a number of cases. Rothleitner⁴ obtained agreement with experiment, too.¹⁷

The main advantage of Eq. (7) as compared to Eq. (2) is that Eq. (7) is more likely to hold for fermion operators introduced into a field theory of currents.¹⁸ As was shown in Ref. 15, for $\Delta^{3/2}(y)=0$, Schwinger terms are then present in the equal-time commutator of the time components of the currents with $\psi(y)$.¹⁹ As to the second assumption, Eq. (8) is [and so are the later Eqs. (13)] an obvious consequence of $\partial^\mu A_\mu^a(x)=0$. If partial conservation of axial-vector current (PCAC) holds for massive pions and the so-defined pion field and $\psi(y)$ are canonical fields, Eq. (8) follows from the canonical rule^{12,20}

$$[\partial^\mu A_\mu^a(x), \psi(y)]|_{x_0=y_0} = 0. \quad (11)$$

However, Eq. (11) does not prove the assumption in Eq. (13) of statement 2 below [as does the assumption $\partial^\mu A_\mu^a(x)=0$].

Assuming the local commutator, Eq. (2), it was shown in Ref. 4 that Eqs. (1) and (3) are equivalent, and thus

$$\langle [Q_5^a(x_0), [\psi(y), \bar{\psi}(z)]_+]_+ \rangle_0 |_{x_0=y_0=z_0} = 0, \quad (12)$$

if and only if Eq. (1) holds, under the above assumptions.

¹² M. K. Banerjee and C. A. Levinson, University of Maryland Technical Report No. 857 (unpublished).

¹³ A. M. Gleeson, Phys. Rev. **149**, 1242 (1969); H. Genz, J. Katz, and S. Wagner, Nuovo Cimento **64A**, 218 (1969).

¹⁴ H. Genz and J. Katz, Nucl. Phys. **B13**, 401 (1969).

¹⁵ H. Genz and J. Katz, Institut für Theoretische Physik der Universität Hamburg Report (unpublished).

¹⁶ For additional reference to applications of Ref. 8, see M. Sugawara, Acta Phys. Austriaca (to be published).

¹⁷ For another proposal, see S. Weinberg, Phys. Rev. **166**, 1568 (1968).

¹⁸ H. Sugawara, Phys. Rev. **170**, 1659 (1968).

¹⁹ For $\Delta^{3/2}(y)=0$, see also S. Coleman, D. Gross, and R. Jackiw, Phys. Rev. **180**, 1359 (1969).

²⁰ The author thanks M. K. Banerjee and C. A. Levinson for discussions on these points.

The other purpose of the present paper is to give conditions for additional sum rules. We will prove the following:

Statement 2. Let Eq. (7) be valid and let¹¹ for $n \geq 1$

$$0 = \sum_{j=0}^{2n-2} \left\langle \left[\left(\frac{\partial}{\partial y_0} \right)^j \int d^3x \partial^\mu A_{\mu^a}(x), \left(\frac{\partial}{\partial y_0} \right)^{2n-2-j} \psi(y) \right]_+, \bar{\psi}(z) \right\rangle_0. \quad (13)$$

Then we have

$$\begin{aligned} & \frac{1}{2} \left\langle \left[Q_5^a(x_0), \left[\left(\frac{\partial}{\partial y_0} \right)^{2n-1} \psi(y), \bar{\psi}(z) \right]_+ \right] \right\rangle_0 \\ &= i\tau^a \gamma_5 r_A \int dm^2 m [F_{+^2}(m^2) - F_{-^2}(m^2)] \\ & \quad \times \left(\frac{\partial}{\partial \mathbf{y}} \frac{\partial}{\partial \mathbf{y}} - m^2 \right)^{n-1} \delta(\mathbf{y} - \mathbf{z}) \\ &= i\tau^a \gamma_5 r_A \sum_{\nu=0}^{n-1} S_{1+2\nu} \binom{n-1}{\nu} \left(\frac{\partial}{\partial \mathbf{y}} \frac{\partial}{\partial \mathbf{y}} \right)^{n-1-\nu} \delta(\mathbf{y} - \mathbf{z}). \quad (14) \end{aligned}$$

In the above statement we have defined S_ν by

$$S_\nu = \int dm^2 m^\nu [F_{+^2}(m^2) - F_{-^2}(m^2)]. \quad (15)$$

Note again the anticommutators in Eqs. (13) and (14). Conditions under which Eq. (13) is valid have been investigated above. In Eq. (14), the highest-order Schwinger term is of order $2(n-1)$. That this term vanishes is equivalent to the sum rule (3).

The rule (for $0 \leq \nu \leq n-1$)

$$S_{2\nu+1} = 0 \quad (16)$$

is valid if and only if the Schwinger term of order $2(n-1-\nu)$ is absent in Eq. (14). Note that each $S_{2\nu+1}$ is present in all the expressions (14), for which $n \geq \nu+1$. In Eq. (14), S_{2n+1} multiplies the non-Schwinger term. These remarks establish a set of conditions for each sum rule, as well as identities between Schwinger terms in Eq. (14). These can be read off easily.

For all integers $\nu \geq 0$, Eq. (16) would imply

$$m[F_{+^2}(m^2) - F_{-^2}(m^2)] = 0. \quad (17)$$

That is, up to massless fermions, the $\frac{1}{2}^+$ and $\frac{1}{2}^-$ spectral functions are identical. Since there are no $J=I=\frac{1}{2}$ parity doublets, $\psi(y)$ would not allow any particle interpretation. Unless this is the case, the anticommutators $[(\partial/\partial y_0)^{2k-1} \psi(y), \bar{\psi}(z)]_+|_{x_0=y_0}$ are not c numbers for all integers $k \geq 1$ [and Schwinger terms are present in some of the Eqs. (14)].

Finally, from Ref. 4 and the high-energy expansion^{6,21} of the spectral representation for $\langle T(\bar{\psi}\psi) \rangle_0$, one derives that, if Eq. (2) also holds, Eq. (16) is equivalent to a vanishing of the expression in Eq. (1), like $(p^2)^{-\nu-1}$ in the limit $p^2 \rightarrow \infty$.

In order to prove the above statements, it would be sufficient to prove the second one (statement 1 is statement 2 for $n=1$). However, we would rather prove statement 1 and generalize the proof. We start with the following algebraic identity of the Jacobi type:

$$[[a, b], c]_+ + [[b, c], a]_+ - [[c, a], b]_+ = 0. \quad (18)$$

Then Eq. (7) allows us to write^{12,20}

$$\begin{aligned} & [Q_5^a(x_0), \psi(y)] \\ &= -\gamma_5 \tau^a r_A \psi(y) + \gamma_5 \Delta^{3/2}(y) - \left[\int d^3x \frac{\partial}{\partial x_0} A_0^a(x), \psi(y) \right] \\ &= -\gamma_5 \tau^a r_A \psi(y) + \gamma_5 \Delta^{3/2}(y) - \left[\int d^3x \partial^\mu A_{\mu^a}(x), \psi(y) \right]. \quad (19) \end{aligned}$$

We have used the Jacobi identity for $[Q_5^a(x_0), [H, \psi(y)]]$ and have added $-\left[\int d^3x \partial^k A_{k^a}(x), \psi(y) \right] = 0$ to the first line in Eq. (19). Then one derives

$$\begin{aligned} & \left[Q_5^a(x_0), \left(\frac{\partial}{\partial y_0} \right)^{2n-1} \psi(y) \right] \\ &= \frac{\partial}{\partial y_0} \left[Q_5^a(x_0), \left(\frac{\partial}{\partial y_0} \right)^{2n-2} \psi(y) \right] \\ & \quad - \left[\int d^3x \frac{\partial}{\partial x_0} A_0^a(x), \left(\frac{\partial}{\partial y_0} \right)^{2n-2} \psi(y) \right] \\ &= \dots = -r_A \gamma_5 \tau^a \left(\frac{\partial}{\partial y_0} \right)^{2n-1} \psi(y) + \left(\frac{\partial}{\partial y_0} \right)^{2n-1} \gamma_5 \Delta^{3/2}(y) \\ & \quad - \sum_{j=0}^{2n-2} \left(\frac{\partial}{\partial y_0} \right)^j \left[\int d^3x \partial^\mu A_{\mu^a}(x), \left(\frac{\partial}{\partial y_0} \right)^{2n-2-j} \psi(y) \right]. \quad (20) \end{aligned}$$

First we prove statement 1. We write the identity Eq. (18)¹² with $a = Q_5^a(x_0)$, $b = \psi(y)$, and $c = \bar{\psi}(z)$. Thus, from Eqs. (7) and (19) we get

$$\begin{aligned} & [r_A \gamma_5 \tau^a \psi(y), \bar{\psi}(z)]_+ + r_A [\psi(z) \gamma_5 \tau^a \psi(y)]_+ \\ & + [Q_5^a(x_0), [\psi(y), \bar{\psi}(z)]_+] = [\Delta^{3/2}(z), \bar{\psi}(z)]_+ \\ & + [\Delta^{3/2}(y), \bar{\psi}(z)]_+ - \left[\left[\int d^3x \partial^\mu A_{\mu^a}(x), \psi(y) \right], \bar{\psi}(z) \right]_+. \quad (21) \end{aligned}$$

If we take the vacuum expectation value, the right-hand side vanishes because of our assumptions, and

²¹ H. T. Nieh, Phys. Rev. **163**, 1769 (1967).

we are left with

$$-r_A \{ \gamma_5 \tau^a \langle [\psi(y), \bar{\psi}(z)]_+ |_{y_0=z_0} \rangle_0 + \langle [\psi(y), \bar{\psi}(z)]_+ |_{y_0=z_0} \rangle_0 \gamma_5 \tau^a \} = \langle [Q_5^a(x_0), [\psi(y), \bar{\psi}(z)]_+] |_{x_0=y_0=z_0} \rangle_0. \quad (22)$$

Using next the spectral representation,

$$\langle [\psi(y), \bar{\psi}(z)]_+ \rangle_0 = i \int dm^2 \left[F_+^2(m^2) \left(i \frac{\partial}{\partial y_\mu} \gamma_\mu + m \right) + F_-^2(m^2) \left(i \frac{\partial}{\partial y_\mu} \gamma_\mu - m \right) \right] \Delta(y-z; m^2), \quad (23)$$

we see that, because of the presence of γ_5 in Eq. (22), no term proportional to γ_μ contributes upon substituting Eq. (23) into Eq. (22). Finally, performing the time differentiation under the integral, we get Eq. (9) in the equal-time limit.

To prove statement 2, we write Eq. (18) for $a=Q_5^a(x_0)$, $b=(\partial/\partial y_0)^{2n-1}\psi(y)$, and $c=\bar{\psi}(z)$. Performing precisely the same manipulations as above but this time using Eq. (20) instead of (19), we have

$$r_A \left\{ \gamma_5 \tau^a \left\langle \left[\left(\frac{\partial}{\partial y_0} \right)^{2n-1} \psi(y), \bar{\psi}(z) \right]_+ \Big|_{y_0=z_0} \right\rangle_0 + \left\langle \left[\left(\frac{\partial}{\partial y_0} \right)^{2n-1} \psi(y), \bar{\psi}(z) \right]_+ \Big|_{y_0=z_0} \right\rangle_0 \gamma_5 \tau^a \right\} = - \left\langle \left[Q_5^a(x_0), \left[\left(\frac{\partial}{\partial y_0} \right)^{2n-1} \psi(y), \bar{\psi}(z) \right]_+ \right] \right\rangle_0. \quad (24)$$

Note that because of Eq. (13) there is no contribution from the sum in Eq. (20). We again insert the spectral representation and observe that terms proportional to γ_μ drop. Then, using

$$\frac{\partial}{\partial y_0} \left(\frac{\partial}{\partial y_0} \right)^{2n-2} \Delta(y-z; m^2) \Big|_{y_0=z_0} = - \left(\frac{\partial}{\partial y} \frac{\partial}{\partial y} - m^2 \right)^{n-1} \delta(z-y), \quad (25)$$

we reach Eq. (14), the desired result.

As to the consequences of Eq. (16), restrictions follow from the positivity

$$F_\pm^2(m^2) \geq 0. \quad (26)$$

Evidently, any of the Eqs. (16)—if saturated by one-particle intermediate states—can hold only if baryons of opposite parities exist. For $S_1=0$, this has been noted in Refs. 4 and 8.

To derive a further consequence, let us enumerate by N_1, \dots, N_4 the four nucleon resonances $P_{11}(940)$, $P_{11}(1466)$, $S_{11}(1548)$, and $S_{11}(1709)$, and let us denote $F_{\epsilon_i^2}(m_i^2)$ by F_i^2 . We assume $F_1^2 \neq 0$, and we normalize to $F_1^2=1$. The assumptions of statement 2 for $n=2$, together with assuming

$$\langle [Q_5^a(x_0), [\partial^3 \psi(y)/\partial y_0^3, \bar{\psi}(z)]_+] |_{x_0=y_0=z_0} \rangle_0 = 0, \quad (27)$$

give us the sum rules

$$S_1 = S_3 = 0. \quad (28)$$

If saturated by one-particle intermediate states, Eqs. (28) allow us to predict the existence of at least one further nucleon resonance N_5 from N_1, \dots, N_4 . Concerning its mass and parity, there are two possibilities. Either we have $m_5 < m_2$ and $\epsilon_5 = -1$, or $m_2 < m_5$ and $\epsilon_5 = +1$. Since the existence of an undiscovered resonance with a mass smaller than m_2 is very unlikely, the actual prediction is

$$m_5 > m_2, \quad \epsilon_5 = +1. \quad (29)$$

This agrees with the existence of the $P_{11}(1750)$.

In order to derive the conclusion, we write Eq. (28) as

$$m_1 + m_2 F_2^2 = m_3 F_3^2 + m_4 F_4^2 - \sum_{i=5}^R \epsilon_i m_i F_i^2, \quad (30)$$

$$m_1^3 + m_2^3 F_2^2 = m_3^3 F_3^2 + m_4^3 F_4^2 - \sum_{i=5}^R \epsilon_i m_i^3 F_i^2.$$

Thus we have

$$m_1(m_2^2 - m_1^2) = m_3(m_2^2 - m_3^2)F_3^2 + m_4(m_2^2 - m_4^2)F_4^2 - \sum_{i=5}^R \epsilon_i m_i(m_2^2 - m_i^2)F_i^2, \quad (31)$$

with R being the total number of nucleon resonances. The left-hand side is positive and the first two terms on the right-hand side are not positive. Therefore, at least one term in the sum is negative. Giving the number 5 to it, we have

$$\epsilon_5(m_2^2 - m_5^2) < 0. \quad (32)$$

This is the desired result.

The content of the paper is summarized in statements 1 and 2 and in the prediction, Eq. (29).

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