Effects of one valence proton on seniority and angular momentum of neutrons in neutron-rich ${}^{122-131}_{51}$ Sb isotopes

S. Biswas,^{1,*} A. Lemasson,^{1,†} M. Rejmund,¹ A. Navin,¹ Y. H. Kim,^{1,‡} C. Michelagnoli,^{1,‡} I. Stefan,² R. Banik,^{3,4} P. Bednarczyk,⁵ S. Bhattacharya,^{3,4} S. Bhattacharyya,^{3,4} E. Clément,¹ H. L. Crawford,⁶ G. de France,¹ P. Fallon,⁶ G. Frémont,¹ J. Goupil,¹ B. Jacquot,¹ H. J. Li,¹ J. Ljungvall,⁷ A. Maj,⁵ L. Ménager,¹ V. Morel,¹ R. Palit,⁸ R. M. Pérez-Vidal,⁹ J. Ropert,¹ D. Barrientos,¹⁰ G. Benzoni,¹¹ B. Birkenbach,¹² A. J. Boston,¹³ H. C. Boston,¹³ B. Cederwall,¹⁴ J. Collado,¹⁵ D. M. Cullen,¹⁶ P. Désesquelles,⁷ C. Domingo-Pardo,⁹ J. Dudouet,^{7,17} J. Eberth,¹² V. González,¹⁵ L. J. Harkness-Brennan,¹³ H. Hess,¹²
A. Jungclaus,¹⁸ W. Korten,¹⁹ M. Labiche,²⁰ A. Lefevre,¹ R. Menegazzo,²¹ D. Mengoni,^{21,22} B. Million,¹¹ D. R. Napoli,²³ A. Pullia,^{11,24} B. Quintana,²⁵ D. Ralet,^{7,26,27} F. Recchia,^{21,22} P. Reiter,¹² F. Saillant,¹ M. D. Salsac,¹⁹ E. Sanchis,¹⁵ O. Stezowski,¹⁷ Ch. Theisen,¹⁹ J. J. Valiente-Dobón,²³ and M. Zielińska¹⁹ ¹GANIL, CEA/DRF-CNRS/IN2P3, Bd Henri Becquerel, BP 55027, F-14076 Caen Cedex 5, France ²Institut de Physique Nucléaire, IN2P3-CNRS, Univ. Paris Sud, Université Paris Saclay, 91406 Orsay Cedex, France ³Variable Energy Cyclotron Centre, 1/AF Bidhan Nagar, Kolkata 700064, India ⁴Homi Bhabha National Institute, Training School Complex, Anushaktinagar, Mumbai-400094, India ⁵Institute of Nuclear Physics PAN, Kraków, Poland ⁶Nuclear Science Division, Lawrence Berkelev National Laboratory, Berkelev, California 94720, USA ⁷CSNSM, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, 91405 Orsay, France ⁸Department of Nuclear and Atomic Physics, Tata Institute of Fundamental Research, Mumbai 400005, India ⁹Instituto de Física Corpuscular, CSIC-Universitat de València, E-46980 València, Spain ¹⁰CERN, CH-1211 Geneva 23 (Switzerland) ¹¹INFN, Sezione di Milano, Milano, Italy ¹²Institut für Kernphysik, Universität zu Köln, Zülpicher Str. 77, D-50937 Köln, Germany ¹³Oliver Lodge Laboratory, The University of Liverpool, Liverpool, L69 7ZE, United Kingdom ¹⁴Department of Physics, Royal Institute of Technology, SE-10691 Stockholm, Sweden ¹⁵Departamento de Ingeniería Electrónica, Universitat de Valencia, Burjassot, Valencia, Spain ¹⁶Nuclear Physics Group, Schuster Laboratory, University of Manchester, Manchester, M13 9PL, United Kingdom ¹⁷Université de Lyon, Université Lyon-1, CNRS/IN2P3, UMR5822, IPNL, 4 Rue Enrico Fermi, F-69622 Villeurbanne Cedex, France ¹⁸Instituto de Estructura de la Materia, CSIC, Madrid, E-28006 Madrid, Spain ¹⁹IRFU, CEA/DRF, Centre CEA de Saclay, F-91191 Gif-sur-Yvette Cedex, France ²⁰STFC Daresbury Laboratory, Daresbury, Warrington, WA4 4AD, United Kingdom ²¹INFN Sezione di Padova, I-35131 Padova, Italy ²²Dipartimento di Fisica e Astronomia dell'Università di Padova, I-35131 Padova, Italy ²³INFN, Laboratori Nazionali di Legnaro, Via Romea 4, I-35020 Legnaro, Italy ²⁴Dipartimento di Fisica, Università di Milano, I-20133 Milano, Italy ²⁵Laboratorio de Radiaciones Ionizantes, Universidad de Salamanca, E-37008 Salamanca, Spain ²⁶Institut für Kernphysik, Technische Universität Darmstadt, D-64289 Darmstadt, Germany

²⁷GSI, Helmholtzzentrum für Schwerionenforschung GmbH, D-64291 Darmstadt, Germany

(Received 15 March 2019; published 3 June 2019)

Background: Levels fulfilling the seniority scheme and relevant isomers are commonly observed features in semimagic nuclei; for example, in Sn isotopes (Z = 50). Seniority isomers in Sn, with dominantly pure neutron configurations, directly probe the underlying neutron-neutron ($\nu\nu$) interaction. Furthermore, an addition of a valence proton particle or hole, through neutron-proton ($\nu\pi$) interaction, affects the neutron seniority as well as the angular momentum.

Published by the American Physical Society under the terms of the *Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI.*

^{*}biswas@ganil.fr

[†]lemasson@ganil.fr

^{*}Present address: Institut Laue-Langevin, F-38042 Grenoble Cedex, France.

Purpose: Benchmark the reproducibility of the experimental observables, like the excitation energies (E_X) and the reduced electric-quadrupole transition probabilities [B(E2)], with the results obtained from shell-model interactions for neutron-rich Sn and Sb isotopes with N < 82. Study the sensitivity of the aforementioned experimental observables to the model interaction components. Furthermore, explore from a microscopic point of view the structural similarity between the isomers in Sn and Sb, and thus the importance of the valence proton. **Methods:** The neutron-rich ^{122–131}Sb isotopes were produced as fission fragments in the reaction ⁹Be(²³⁸U, f) with 6.2 MeV/u beam energy. A unique setup, consisting of AGATA, VAMOS++, and EXOGAM detectors, was used which enabled the prompt-delayed γ -ray spectroscopy of fission fragments in the time range of 100 ns to 200 μ s.

Results: New isomers and prompt and delayed transitions were established in the even- $A^{122-130}$ Sb isotopes. In the odd- $A^{123-131}$ Sb isotopes, new prompt and delayed γ -ray transitions were identified, in addition to the confirmation of the previously known isomers. The half-lives of the isomeric states and the B(E2) transition probabilities of the observed transitions depopulating these isomers were extracted.

Conclusions: The experimental data was compared with the theoretical results obtained in the framework of large-scale shell-model (LSSM) calculations in a restricted model space. Modifications of several components of the shell-model interaction were introduced to obtain a consistent agreement with the excitation energies and the B(E2) transition probabilities in neutron-rich Sn and Sb isotopes. The isomeric configurations in Sn and Sb were found to be relatively pure. Furthermore, the calculations revealed that the presence of a single valence proton, mainly in the $g_{7/2}$ orbital in Sb isotopes, leads to significant mixing (due to the $\nu\pi$ interaction) of (i) the neutron seniorities (ν_{ν}) and (ii) the neutron angular momentum (I_{ν}). The above features have a weak impact on the excitation energies, but have an important impact on the B(E2) transition probabilities. In addition, a constancy of the relative excitation energies irrespective of neutron seniority and neutron number in Sn and Sb was observed.

DOI: 10.1103/PhysRevC.99.064302

I. INTRODUCTION

The Sn isotopes, with basically a spherical shape, span between two doubly magic nuclei, the neutron-deficient ¹⁰⁰Sn (Z = N = 50) and the neutron-rich ¹³²Sn (Z = 50, N = 82). A constant trend, as a function of neutron number, in the excitation energies (E_X) of the 2⁺ state and the parabolic shape (with a dip around N = 66) of the reduced electricquadrupole transition probabilities $[B(E2; 2^+ \rightarrow 0^+)]$, was observed for the even-A Sn isotopes [1,2]. The observed trend has recently been clarified by using state-of-the-art Monte Carlo shell-model (MCSM) calculations with a large model space, where the dip in the B(E2) was shown to correspond to a novel shape evolution from moderately deformed phase to pairing (seniority) phase around N = 66 [3]. These calculations required huge computational resources, hence only 0^+ , 2^+ , and 4^+ states were calculated for fitting purposes. Recently, the parabolic behavior of the $B(E2; 10^+ \rightarrow 8^+)$ in even-A¹¹⁶⁻¹³⁰Sn was described in the generalized seniority (v) scheme in Ref. [4], showing the necessity of the incorporation of configuration mixing of neutron $vh_{11/2}$, $vd_{3/2}$, and $vs_{1/2}$ orbitals instead of a pure $vh_{11/2}$ orbital, with generalized seniority being pure $v_{\nu} = 2$ (v_{ν} stands for neutron seniority, which refers to the number of unpaired neutrons). It is known that seniority is a good quantum number for $l_i \leq f_{7/2}$. This becomes a partial symmetry in the case of $l_i = g_{9/2}$ in ^{72,74}Ni [5]. In these isotopes, the $(6^+)_{v_{\nu}=4}$ state has a lower excitation energy than the $(6^+)_{v_v=2}$, leading to a disappearance of the seniority $(8^+)_{\nu_{\nu}=2}$ isomers. At present, there is no indication of disappearance of $(10^+)_{\nu_{\nu}=2}$ seniority isomers in the Sn isotopes $(l_i = h_{11/2})$, indicating that the 8⁺ state in Sn is still a pure $v_{\nu} = 2$ state. Recent results on the low-lying high-spin

states in even-A ^{124–128}Sb (Z = 51) and ^{122–126}In (Z = 49) suggested that there is a significant mixing of the seniorities, $v_{\nu} = 1$ and 3, due to the presence of a single valence proton particle (hole) in the $g_{7/2}$ ($g_{9/2}$) orbital [6]. It was shown in Ref. [6] that the interaction of a single proton particle (hole) in the $g_{7/2}$ ($g_{9/2}$) spin-orbit partners in Sb (In) isotopes, respectively, with the neutrons energetically favored the state with one broken pair of neutrons (breaking of the seniority) over a state with no broken pairs for the low-lying high-spin states.

The experimental study of nuclei near the shell closures serves as an important test bench for directly probing the nucleon-nucleon interaction. This acts as important input for existing shell-model interactions and allows us to improve the predictive power of such calculations. In particular, the mass $A \sim 130$ region, near shell closure, is an interesting area of research in contemporary nuclear physics, because 132 Sn is so far the heaviest neutron-rich unstable doubly magic nucleus and it is possible to access this region with the recent advent of new accelerator facilities and large detector arrays [7–10]. The excitation energies (E_X) and the transition strengths [B(E2)/B(M1)] of neighboring nuclei near 132 Sn act as a testing ground to shell-model calculations and the associated interactions [6,11–15].

Even-A ^{118–130}Sn isotopes possess 7⁻ and 10⁺ isomers, with dominant neutron $\nu h_{11/2}^{-1} d_{3/2}^{-1}$ and $\nu h_{11/2}^{-2}$ configurations, respectively [16–19]. Similarly, odd-A ^{119–129}Sn isotopes display 23/2⁺ and 27/2⁻ isomers with dominant $\nu h_{11/2}^{-2} d_{3/2}^{-1}$ and $\nu h_{11/2}^{-3}$ configurations, respectively [18,20,21], an additional hole in the $\nu h_{11/2}$ orbital coupled to the counterparts, 7⁻ and 10⁺ isomers in even-A Sn, respectively. The

experimental data from these nuclei, due to proton shell closure, probe the neutron-neutron $(\nu\nu)$ interaction. Odd-A $^{121-131}$ Sb isotopes have $19/2^-$ and $23/2^+$ isomers with dominant $\pi g_{7/2} \nu h_{11/2}^{-1} d_{3/2}^{-1}$ and $\pi g_{7/2} \nu h_{11/2}^{-2}$ configurations [22–26], an additional proton particle in $g_{7/2}$ coupled to the 7⁻ and 10^+ isomers in even-A Sn, respectively. The isomers in even-A ^{122–128}Sb isotopes, except for ¹³⁰Sb, were not known and are newly observed in this work. The experimental data on Sb isotopes, in addition to the information obtained for Sn, probe the neutron-proton $(\nu \pi)$ interaction. The present paper discusses the four different cases of configurational similarities between Sn and Sb:

Case I: $10^+ \to 8^+ (\nu h_{11/2}^{-2})$ in even-A Sn and $23/2^+ \to 19/2^+ (\pi g_{7/2} \nu h_{11/2}^{-2})$ in odd-A Sb. Case II: $7^- \to 5^- (\nu h_{11/2}^{-1} d_{3/2}^{-1})$ in even-A Sn and $19/2^- \to 15/2^- (\pi g_{7/2} \nu h_{11/2}^{-1} d_{3/2}^{-1})$ in odd-A Sh

Case III: $23/2^+ \rightarrow 19/2^+ (\nu h_{11/2}^{-2} d_{3/2}^{-1})$ in odd-A Sn and

 $13^+ \to 11^+ (\pi g_{7/2} \nu h_{11/2}^{-2} d_{3/2}^{-1}) \text{ in even-}A \text{ Sb.}$ Case IV: $27/2^- \to 23/2^- (\nu h_{11/2}^{-3}) \text{ in odd-}A \text{ Sn and}$ $16^- \to 14^- (\pi g_{7/2} \nu h_{11/2}^{-3}) \text{ in even-}A \text{ Sb.}$

II. EXPERIMENTAL DETAILS

The neutron-rich ¹²²⁻¹³¹Sb isotopes were produced as fission fragments via fusion- and transfer-induced fission re-actions at GANIL by using a ²³⁸U beam at an energy of 6.2 MeV/u, with typical beam intensity of 1 pnA on a ⁹Be target (1.6 and 5 μ m thick). The unambiguous isotopic identification of the fission fragments (Z, A, q) was achieved using the VAMOS++ spectrometer, placed at 20° relative to the beam axis [27–29]. The focal plane detection system of VAMOS++ was constituted of a multiwire proportional counter (MWPC), two drift chambers, and a segmented ionization chamber. The AGATA γ -ray tracking array, consisting of 32 crystals, was placed at 13.5 cm from the target position [30]. The velocity vector of the recoiling ions [measured by a dual positionsensitive MWPC (DPS-MWPC) detector [31], placed at the entrance of the VAMOS++ spectrometer], and the γ -ray emission angle (determined by using AGATA) were used to obtain the Doppler-corrected prompt γ rays (γ_P), on an eventby-event basis. Gamma-ray interaction points, determined by Pulse Shape Analysis (PSA) and GRID search algorithm techniques, were tracked by using the Orsay Forward Tracking (OFT) algorithm, as described in Ref. [32]. The delayed γ rays (γ_D) were detected by using seven EXOGAM HPGe Clover detectors [33], arranged in a wall-like configuration at the focal plane of VAMOS++. The particle identification (PID) spectra, intrinsic resolutions of the spectrometer ($\Delta Z/Z$, $\Delta A/A$, $\Delta q/q$), and additional experimental details are given in Ref. [32].

The contamination from neighboring isobars, arising from the resolution in atomic number Z, was subtracted for prompt γ -ray spectra. In addition to the background reduction for the delayed spectra as suggested in Ref. [32], the subtraction in delayed spectra for neighboring isotopes was performed for all the Sb isotopes. The $\gamma - \gamma$ matrices ($\gamma_P - \gamma_P$,

 $\gamma_D - \gamma_D$, and $\gamma_P - \gamma_D$) were generated for both the prompt (P) and delayed (D) transitions for all the Sb isotopes. The uncertainties in the energy of the prompt and delayed γ rays is ~ 1 keV. The efficiencies for the prompt and delayed γ rays were determined separately, as mentioned in Ref. [32]. The correction for the half-lives as mentioned in Ref. [32], was also taken into account. The spin-parities were assigned based on systematics and shell-model calculations. One- $(A_0e^{-t/A_1\ln 2} + A_2)$, two- $[A_0\frac{A_2}{A_1-A_2}(e^{-t/A_1\ln 2} - A_2)]$ $e^{-t/A_2 \ln 2}$) + $A_3 e^{-t/A_2 \ln 2}$ + A_4], and three-component fits, where A_i (i = 0, ..., 4) are the fitting parameters, were carried out for the estimation of half-lives of the states, wherever required. The conversion coefficients used for the estimation of the B(E2) transition probabilities were taken from BrIcc [34].

III. EXPERIMENTAL RESULTS

A summary of the level schemes for all the odd-A and even-A¹²²⁻¹³¹Sb isotopes are shown in Fig. 1. Already known γ -ray transitions are shown in black. Newly identified prompt and delayed transitions are shown by red and blue, respectively. Already known half-lives which have not been measured in this work are shown. The remeasured and newly measured half-lives have been indicated by a red line and a red box, respectively. The width of the arrows are proportional to the intensity of the transitions. The intensities of the prompt and delayed transitions have been separately measured and the lowest transition is normalized to 100 in each case. The prompt γ -ray transition emitted by the complementary fission fragment [28,29] (mainly from the fusion-fission) are observed and identified (marked by "c" in all the spectra) in the low-energy part of the γ -ray spectra. The random coincidences with x-rays emitted by ²³⁸U are also observed and are marked by an @ symbol.

A. ¹²²Sb

Previous measurements on ¹²²Sb were reported in Refs. [35,36]. The level scheme as obtained in the present work is shown in Fig. 1. Table I shows the properties of all the transitions assigned in this work.

The A- and Z-gated tracked Doppler-corrected prompt singles γ -ray (γ_P) spectrum for ¹²²Sb is shown in Fig. 2. Three new prompt transitions, 445, 657, and 1102 keV transitions, are seen and marked with an asterisk. Based on the relative intensities, the 445 keV γ ray is placed above the (8)⁻ level (a 4.2 min isomeric state observed in Ref. [35]). In addition, it follows the systematics with the higher even-A Sb isotopes. Due to low statistics, no $\gamma_P - \gamma_P$ coincidence could be carried out. However, based on the summation of gammas, the intensities, and the systematics, the 657 keV is placed above the 445 keV with the (10^{-}) level decaying by the 1102 keV to the (8)⁻ state. No A- and Z-gated delayed γ rays (γ_D) in ¹²²Sb could be identified from the present experiment.

B. ¹²³Sb

The spectroscopy of ¹²³Sb isotope was previously studied in Refs. [22,23,37,38]. The level scheme as obtained in the





064302-4



FIG. 2. A- and Z-gated γ -ray spectrum for ¹²²Sb: The tracked Doppler-corrected prompt singles γ -ray (γ_P) spectrum. The newly identified γ rays are marked with an asterisk.

present work is shown in Fig. 1. Table II shows the properties of all the transitions assigned in this work.

The A- and Z-gated γ -ray spectra for ¹²³Sb are shown in Fig. 3. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹²³Sb is shown in Fig. 3(a). Previously observed 160, 956, and 1089 keV transitions are seen in this spectrum. Two new prompt γ -ray transitions, namely 244 and 439 keV, are identified and these are marked with an asterisk. The delayed γ -ray spectrum (γ_D) for $0 < t_{decay} < 2 \mu s$ is shown in Fig. 3(b), yielding 160, 200, 382, 395, 568, 626, 1031, 1089, and 1101 keV transitions, as expected from previous works. The half-life fit (one-component) for the decay spectrum upon gating on 200 keV transition yields a value of $T_{1/2} = 222(23)$ ns for the $(19/2^{-})$ state [in agreement with the quoted value of 214(3) ns in Ref. [23]], which gives $B(E2; 19/2^- \rightarrow 15/2^-) = 6.9(7) e^2 \text{ fm}^4$. However, the weak delayed transitions, which were mentioned in Refs. [23,38]; namely, the 949, 1007, 1260, and 1656 keV transitions, are not observed owing to the low statistics in our dataset. Similarly, Fig. 3(c) shows the delayed γ -ray spectrum (γ_D) for $6 < t_{decay} < 100 \ \mu s$, leading to 128, 442, 956, and 1089 keV transitions. A half-life fit (one-component) for the decay spectrum upon gating on 128, 442, and 956 keV transitions yields a value of $T_{1/2} = 66(4) \ \mu s$ for the $23/2^+$ state [in agreement] with the value of $65(1) \ \mu s$ reported in Ref. [23]], which gives $B(E2; 23/2^+ \rightarrow 19/2^+) = 0.15(1) e^2 \text{ fm}^4$. However, the weak transitions 100, 148, 348, 375, and 1250 keV, which were mentioned in Ref. [23], are not observed owing to the low statistics in our dataset. The tracked Doppler-corrected γ_P in coincidence with any γ_D (for $6 < t_{decay} < 100 \ \mu s$) is shown in Fig. 3(d). This spectrum yields the two newly identified prompt γ -ray transitions, 244 and 439 keV transitions. To confirm these newly found prompt transitions, a gate when applied on the prompt 244 and 439 keV transitions yielded the delayed 128 keV (not shown in this figure). Thus these two new transitions are placed above the $23/2^+$ isomer. However,

TABLE I. Properties of the transitions assigned to ¹²²Sb obtained in this work.

Ξ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_f
445.2	100	$(9^-) \rightarrow (8)^-$	445	0
657.2	63(14)	$(10^{-}) \rightarrow (9^{-})$	1102	445
1102.2	29(18)	$(10^-) \rightarrow (8)^-$	1102	0



FIG. 3. *A*- and *Z*-gated γ -ray spectra for ¹²³Sb: (a) The tracked Doppler-corrected prompt γ -ray (γ_P) spectrum with the new γ -ray transitions marked with asterisk. (b), (c) The delayed γ -ray (γ_D) spectra for $0 < t_{decay} < 2 \ \mu$ s and $6 < t_{decay} < 100 \ \mu$ s, respectively. The insets in panels (b) and (c) show the decay curves along with the fits for the 200 and 128 + 442 + 956 keV transitions, respectively. (d) γ_P in coincidence with any γ_D for $6 < t_{decay} < 100 \ \mu$ s.

TABLE II. Properties of the transitions assigned to ¹²³Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Eγ	I_{γ}	$J^{\pi}_i o J^{\pi}_f$	E_i	E_f
244.1	78(16)	$(27/2^+) \rightarrow (25/2^+)$	3298	3054
439.2	100	$(25/2^+) \rightarrow 23/2^+$	3054	2615
128.2	29(16)	$23/2^+ \rightarrow 19/2^+$	2615	2487
159.8	63(36)	$5/2^+ \rightarrow 7/2^+$	160	0
200.4	108(57)	$(19/2^{-}) \rightarrow 15/2^{-}$	2239	2039
382.0	112(54)	$15/2^- \rightarrow 11/2^-$	2039	1657
395.4	44(23)	$11/2^{-} \rightarrow 9/2^{+}$	1657	1261
441.6	32(11)	$19/2^+ \rightarrow 15/2^+$	2487	2045
568.2	35(17)	$11/2^- \rightarrow 11/2^+$	1657	1089
626.0	125(56)	$11/2^- \rightarrow 9/2^+$	1657	1031
956.0	37(14)	$15/2^+ \rightarrow 11/2^+$	2045	1089
1030.5	141(64)	$9/2^+ \rightarrow 7/2^+$	1031	0
1089.0	100	$11/2^+ \rightarrow 7/2^+$	1089	0
1101.0	44(22)	$9/2^+ \to 5/2^+$	1261	160



FIG. 4. *A*- and *Z*-gated γ -ray spectra for ¹²⁴Sb: (a) The tracked Doppler-corrected prompt γ -ray (γ_P) singles spectrum. (b) The prompt γ - γ (γ_P - γ_P) spectrum with gate on 1068 keV transition. The newly identified prompt transitions are marked with an asterisk.

the tracked Doppler-corrected γ_P in coincidence with any γ_D for $0 < t_{decay} < 2 \,\mu s$, did not result in any new prompt γ rays and hence no γ ray is placed above the $(19/2^-)$ isomer.

C. ¹²⁴Sb

The γ -ray spectroscopy measurement on the high-spin states in ¹²⁴Sb was previously reported in Ref. [6]. The level scheme as obtained in the present work is shown in Fig. 1. Table III shows the properties of all the transitions assigned in this work.

The A- and Z-gated tracked Doppler-corrected prompt singles γ -ray spectrum for ¹²⁴Sb is shown in Fig. 4(a). The already identified γ rays in Ref. [6]; namely 512, 556, and 1068 keV are seen. Other than these, four new prompt 143, 338, 428, and 1012 keV γ -ray transitions are identified (marked with an asterisk). Figure 4(b) shows the A- and Z-gated tracked Doppler-corrected prompt γ - γ coincidence (γ_P - γ_P) spectrum with gate on the 1068 keV transition. This shows that the 1012 keV transition is in coincidence and hence is placed in the level scheme. The placement of 1012 keV transition in the level scheme follows the systematics with the other even-A Sb isotopes. The other prompt transitions 143, 338, and 428 keV are not placed as these are not observed in the coincidence spectrum. These γ rays probably belong to the sideband (as observed above the isomer in the case of

TABLE III. Properties of the transitions assigned to ¹²⁴Sb obtained in this work.

Eγ	\mathbf{I}_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_f
512.3	30(6)	$(10^-) \rightarrow (9^-)$	1068	556
556.0	100	$(9^-) \rightarrow (8^-)$	556	0
1012.0	29(6)	$(12^{-}) \rightarrow (10^{-})$	2080	1068
1068.4	69(13)	$(10^-) \rightarrow (8^-)$	1068	0



FIG. 5. *A*- and *Z*-gated γ -ray spectra for ¹²⁵Sb: (a) The tracked Doppler-corrected prompt singles γ -ray (γ_P) spectrum with the new γ -ray transitions marked with asterisk. The inset shows the tracked Doppler-corrected prompt $\gamma_P - \gamma_P$ coincidence spectrum with gate on the newly observed 658 keV γ -ray. (b), (c) The delayed singles γ -ray (γ_D) spectra for $0 < t_{decay} < 3 \ \mu s$ and $5 < t_{decay} < 60 \ \mu s$, respectively. The insets in panels (b) and (c) shows the delayed $\gamma_D - \gamma_D$ coincidence spectra with gate on 146 and 141 keV γ rays, respectively. (d) Tracked Doppler-corrected γ_P in coincidence with $\gamma_D = 146 \ \text{keV} \ \gamma$ -ray (for $0 < t_{decay} < 3 \ \mu s$). The inset shows the decay curve along with the fit for the 146 keV transition. (e) γ_P in coincidence with the $\gamma_D = 141 \ \text{keV} \ \gamma$ -ray (for $5 < t_{decay} < 60 \ \mu s$). The inset shows the decay curve along with the fit for the 141 keV transition.

 126 Sb). No delayed γ rays could be identified for 124 Sb, using the present setup.

D. ¹²⁵Sb

Previous measurements on the γ -ray spectroscopy of highspin states in ¹²⁵Sb were reported in Refs. [22,37,39]. The level scheme as obtained in the present work is shown in Fig. 1. Table IV shows the properties of all the transitions assigned in this work.

The A- and Z-gated γ -ray spectra for ¹²⁵Sb is shown in Fig. 5. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹²⁵Sb is shown in Fig. 5(a). The previously

TABLE IV. Properties of the transitions assigned to ¹²⁵Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Ēγ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_f
345.3	45(5)	$(31/2^{-}) \rightarrow (27/2^{-})$	4138	3795
438.7	26(3)	$(35/2^{-}) \rightarrow (31/2^{-})$	4579	4138
446.5	100	$(25/2^+) \rightarrow 23/2^+$	2919	2472
453.1	17(2)	$(33/2^+) \rightarrow (31/2^+)$	4981	4528
482.0	50(3)	$(27/2^+) \rightarrow (25/2^+)$	3401	2919
538.1	13(3)	$(35/2^+) \rightarrow (33/2^+)$	5366	4934
542.7	30(2)	$(29/2^+) \rightarrow (27/2^+)$	3943	3401
584.8	23(3)	$(31/2^+) \rightarrow (29/2^+)$	4528	3943
657.8	79(6)	$(27/2^{-}) \rightarrow (23/2^{-})$	3795	3138
1025.4	100	$(23/2^-) \rightarrow 19/2^-$	3138	2112
105.1	6(4)	$17/2^- \rightarrow 19/2^-$	2217	2112
108.1	29(19)	$19/2^+ \rightarrow 17/2^-$	2326	2217
132.1	24(13)	$19/2^+ \rightarrow 15/2^+$	2326	2194
140.7	51(28)	$19/2^- \rightarrow 15/2^-$	2112	1972
146.3	52(27)	$23/2^+ \rightarrow 19/2^+$	2472	2326
213.3	5(2)	$19/2^+ \rightarrow 19/2^-$	2326	2112
245.9	19(11)	$17/2^- \rightarrow 15/2^-$	2217	1972
332.0	34(13)	$19/2^+ \rightarrow 15/2^+$	2326	1994
881.8	50(17)	$15/2^- \rightarrow 11/2^+$	1972	1090
903.8	95(32)	$15/2^- \rightarrow 9/2^+$	1972	1068
904.1	29(10)	$15/2^+ \rightarrow 11/2^+$	1994	1090
1067.7	100	$9/2^+ \rightarrow 7/2^+$	1068	0
1089.7	54(18)	$11/2^+ \rightarrow 7/2^+$	1090	0
1104.1	35(12)	$15/2^+ \rightarrow 11/2^+$	2194	1090

known 332, 446, 482, 453, 538, 543, 904, 1068, 1090, and 1104 keV transitions are observed. Seven new prompt γ ray transitions, namely 289, 345, 439, 585, 625, 658, and 1025 keV transitions are identified (marked with an asterisk). The inset shows the tracked Doppler-corrected prompt $\gamma_P - \gamma_P$ coincidence spectrum with gate on the newly identified 658 keV transition. This spectrum shows that the 345, 439, 658, and 1025 keV γ rays are in coincidence. A similar coincidence spectrum was obtained for the 446, 453, 482, 538, 543, and 585 keV transitions (not shown in this figure). No γ rays are seen in coincidence with the 289 and 625 keV transitions, hence these are not placed in the level scheme. The delayed γ -ray (γ_D) spectrum for $0 < t_{decay} < 3 \ \mu s$ is shown in Fig. 5(b) yielding 105, 108, 132, 146, 213, 246, 332, $904(15/2^+ \rightarrow 11/2^+)$, 1090, and 1104 keV transitions, as expected from the level scheme. The 213 keV is newly identified and this is marked with a hash in the spectrum. The inset of Fig. 5(b) shows the delayed $\gamma_D - \gamma_D$ coincidence spectrum with gate on 146 keV transition, yielding all the intense delayed transitions. Similarly, Fig. 5(c) shows the delayed γ -ray spectrum for $5 < t_{decay} < 60 \ \mu s$, leading to 141, 882, $904(15/2^- \rightarrow 9/2^+)$, 1068, and 1090 keV transitions. The inset of Fig. 5(c) shows the delayed $\gamma_D - \gamma_D$ coincidence spectrum with gate on 141 keV transition, yielding 904 and 1068 keV γ rays, as expected from previous works. The tracked Doppler-corrected γ_P in coincidence with $\gamma_D = 146 \text{ keV}$ (for $0 < t_{\text{decay}} < 3 \ \mu \text{s}$) is shown in Fig. 5(d). This spectrum yields the prompt γ -ray transitions, 446, 453,

482, 538, 543, and 585 keV transitions. In the previous Ref. [37], these prompt transitions, except 585 keV, were assigned negative-parities and placed above the $19/2^{-}$ isomer. Here we propose these transitions to be positive-parity states and placed above the $23/2^+$ isomer, as observed from promptdelayed coincidences. Based on the intensities, the 585 keV transition is placed above the 543 keV transition, and the 453 and 538 keV transitions are replaced. The 432 keV transition, seen in Ref. [37], is not observed in coincidence, hence it is not assigned in the present level scheme. The half-life fit (one-component) for the decay spectrum upon gating on 146 keV transition yields a value of $T_{1/2} = 278(7)$ ns for the $23/2^+$ [in agreement with the value of 272(16) ns reported in Ref. [22]], which is shown in the inset of Fig. 5(d). This leads to $B(E2; 23/2^+ \rightarrow 19/2^+) = 21.3(6) e^2 \text{ fm}^4$. The tracked Doppler-corrected γ_P in coincidence with $\gamma_D = 141$ keV for $5 < t_{decay} < 60 \ \mu s$ resulted in the observation of the newly identified 1025 keV γ ray. As seen from the inset of Fig. 5(a), the 345, 439, 658, and 1025 keV transitions are in coincidence, and hence are placed above the $19/2^{-1}$ isomer. The inset of Fig. 5(d) shows the half-life fit (twocomponent with one component fixed to 278 ns) for the decay spectrum upon gating on 141 keV transition yield a value of $T_{1/2} = 28.8(6) \ \mu s$ for the $19/2^-$ state [in agreement with the quoted value of 28.0(7) μ s in Ref. [22]], which yields $B(E2; 19/2^- \rightarrow 15/2^-) = 0.24(1) e^2 \text{ fm}^4.$

E. ¹²⁶Sb

Gamma-ray spectroscopy measurements on the high-spin states in 126 Sb was previously reported in Ref. [6]. The level scheme as obtained in the present work is shown in Fig. 1. Table V shows the properties of all the transitions assigned in this work.

The A- and Z-gated γ -ray spectra for ¹²⁶Sb are shown in Fig. 6. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹²⁶Sb is shown in Fig. 6(a). The already known γ rays from Ref. [6]; namely, 353, 374, 443, 671, 961, and 1045 keV are observed. In addition, new prompt γ rays 130, 412, 424, 491, 498, 502, and 1101 keV (marked with an asterisk) are identified. The tracked Doppler-corrected prompt $\gamma - \gamma$ coincidence ($\gamma_P - \gamma_P$) spectrum with a sum gate of 353, 443 and 961 keV prompt γ -ray transitions is shown in the inset of Fig. 6(a). This spectrum shows that the 353, 374, 412, 424, 443, 498, 671, 961, and 1045 keV transitions are in coincidence and the newly observed transitions are marked with an asterisk. Figure 6(b) shows the delayed γ -ray (γ_D) singles spectrum, with $0 < t_{decay} < 4 \mu s$. This spectrum shows the presence of two new delayed 121 and 645 keV transitions, besides the 1045 keV transition (marked with a hash). The inset in Fig. 6(b) shows the tracked Doppler-corrected prompt $\gamma - \gamma$ coincidence spectrum $(\gamma_P - \gamma_P)$ gated on the newly identified 491 keV transition. This shows that the 130, 491, and 502 keV transitions are in coincidence and these are placed above the (11^+) state in the level scheme, following the systematics with higher even-A Sb isotopes. Also in Fig. 6(a), the newly identified 1101 keV transition, is not observed in the tracked Doppler-corrected prompt $\gamma_P - \gamma_P$ spectra [insets of Fig. 6(a) and 6(b)]. Following the systematics with ¹²⁸Sb, this is placed



FIG. 6. *A*- and *Z*-gated γ -ray spectra for ¹²⁶Sb: (a) Tracked Doppler-corrected prompt γ -ray singles spectrum (γ_P). The inset shows the tracked Doppler-corrected $\gamma_P - \gamma_P$ coincidence spectrum with sum gate on $\gamma_P s$; namely, the 353, 443, and 961 keV transitions. The newly identified prompt γ rays are marked with an asterisk. (b) The delayed singles γ -ray spectrum (γ_D) for $0 < t_{decay} < 4 \ \mu s$. The newly identified delayed γ rays are marked with a hash. The inset shows the tracked Doppler-corrected $\gamma_P - \gamma_P$ coincidence spectrum with gate on the newly identified 491 keV prompt γ ray. (c), (d) The decay curve along with the fit for the delayed 121 and 645 keV transitions, respectively.

above the (13^+) state. The decay spectrum of the delayed 121 keV transition is shown in Fig. 6(c). An exponential fit (one-component) yields a value of 90(16) ns. This gives $B(E2; 13^+ \rightarrow 11^+) = 131(28) \ e^2 \text{ fm}^4$. The half-life of the 645 keV transition was also measured with $T_{1/2} = 60(20)$ ns, as shown in Fig. 6(d) (using a two-component fit with one component fixed to 90 ns).

F. ¹²⁷Sb

Previous γ -ray spectroscopy measurements on ¹²⁷Sb were reported in Refs. [24,37,40]. The level scheme as obtained in the present work is shown in Fig. 1. Table VI shows the properties of all the transitions assigned in this work.

The A- and Z-gated γ -ray spectra for ¹²⁷Sb is shown in Fig. 7. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹²⁷Sb is shown in Fig. 7(a). The previously

TABLE V. Properties of the transitions assigned to ¹²⁶Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

\mathbf{E}_{γ}	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_{f}
130.1	44(4)	$(14^+) \rightarrow (13^+)$	2813	2682
352.9	72(7)	$(14^{-}) \rightarrow (12^{-})$	2359	2006
373.5	35(5)	$(10^{-}) \rightarrow (9^{-})$	1045	671
411.9	39(5)	$(16^{-}) \rightarrow (15^{-})$	3214	2802
423.5	17(2)	$(17^{-}) \rightarrow (16^{-})$	3638	3214
443.3	59(7)	$(15^{-}) \rightarrow (14^{-})$	2802	2359
491.4	78(7)	$(13^+) \to (12^+)$	2682	2191
497.6	13(2)	$(18^{-}) \rightarrow (17^{-})$	4135	3638
501.8	100	$(12^+) \to (11^+)$	2191	1689
671.2	100	$(9^-) \rightarrow (8^-)$	671	0
961.4	79(11)	$(12^{-}) \rightarrow (10^{-})$	2006	1045
1044.9	87(7)	$(10^-) \rightarrow (8^-)$	1045	0
1101.1	100	$(15^+) \to (13^+)$	2912	1811
121.3	70(43)	$(13^+) \to (11^+)$	1811	1689
644.6	76(29)	$(11^+) \to (10^-)$	1689	1045

known 161, 193, 253, 365, 387, 392, 482, 516, 613, 931, 956, 999, 1096, and 1115 keV transitions are seen. Two new prompt γ -ray transitions, namely 538 and 1052 keV transitions, are identified and these are marked with an asterisk. The inset shows the tracked Doppler-corrected prompt $\gamma_P - \gamma_P$ coincidence spectrum with sum gate on the 387, 392, 539, and 613 keV γ -ray transitions. This spectrum shows that the 253, 365, 387, 392, 482, 539, 613, 931, and 999 keV γ ravs are in coincidence. A similar coincidence spectrum is obtained for 161, 193, and 516 keV transitions (not shown in this figure). The delayed singles γ -ray (γ_D) spectrum for $0 < t_{decay} < 4 \ \mu s$ is shown in Fig. 7(b), yielding 85, 120, 131, 144, 153, 247, 852, 956, and 1096 keV transitions, as expected from the previous works. The 85, 120, and 153 keV transitions are newly identified (marked with hash). The inset shows the delayed $\gamma_D - \gamma_D$ coincidence spectrum with gate on 247 keV transition, yielding 131, 852, and 1096 keV transitions, as reported in previous measurements. The newly observed delayed transitions are placed in accordance with that of ¹²⁵Sb and summation of gammas. Similarly, Fig. 7(c) shows the singles γ_D -ray spectrum for $10 < t_{decay} < 100 \ \mu$ s, leading to 806, 825, 1096, and 1115 keV transitions. The inset shows the delayed $\gamma_D - \gamma_D$ coincidence spectrum with gate on 1115 keV transition, yielding 806 keV γ ray as expected from previous works. The γ -ray transition, 69 keV, between the (19/2⁻) and $15/2^{-}$ (similar 200 and 141 keV transitions were observed in ^{123,125}Sb isotopes, respectively) could not be observed with the present setup because it is below the energy threshold. Assuming similar structure with the other odd-A Sb isotopes, the $(19/2^{-})$ state can be assumed to be an isomeric state in ¹²⁷Sb. The tracked Doppler-corrected γ_P in coincidence with the sum gate of γ_D s; namely, 85, 120, 131, 144, 247, 852, 956, and 1096 keV transitions (for $0 < t_{decay} < 4 \mu s$) is shown in Fig. 7(d). This spectrum yields the prompt γ ray transitions, 161, 253, 365, 387, 392, 482, 539, 613, and 931 keV transitions. In the previous Ref. [37], these prompt transitions were assigned negative-parities and placed above



FIG. 7. *A*- and *Z*-gated γ -ray spectra for ¹²⁷Sb: (a) The tracked Doppler-corrected prompt singles γ -ray (γ_P) spectrum with the new γ -ray transitions marked with asterisk. The inset shows the prompt $\gamma_P \cdot \gamma_P$ coincidence spectrum with a sum gate on γ_P ; namely, 387, 392, 539, and 613 keV γ rays. (b), (c) The delayed singles γ -ray (γ_D) spectra for $0 < t_{decay} < 4 \ \mu s$ and $10 < t_{decay} < 100 \ \mu s$, respectively. The insets in panels (b) and (c) show the delayed $\gamma_D \cdot \gamma_D$ coincidence spectra with the gate on 247 and 1115 keV γ rays. (d) Tracked Doppler-corrected γ_P in coincidence with the sum gate of the γ_D ; namely, 85, 120, 131, 144, 247, 852, 956, and 1096 keV γ rays (for $0 < t_{decay} < 4 \ \mu s$). The inset shows the decay curve along with the fit for the 131 keV transition. (e) Tracked Doppler-corrected γ_P in coincidence with the fit for the 825 keV transition.

the $(19/2^{-})$ isomer. Instead, we suggest these to be positiveparity states (placed above the $23/2^{+}$ isomer), as observed from the prompt-delayed coincidences. The half-life fit (onecomponent), shown in the inset of Fig. 7(c), for the decay spectrum upon gating on 131 keV transition yields a value of $T_{1/2} = 269(5)$ ns for the $23/2^{+}$ state [close to the value of 234(12) ns reported in Ref. [24]], which has been shown in the inset. This gives $B(E2; 23/2^{+} \rightarrow 19/2^{+}) = 33.4(7) e^{2}$ fm⁴. However, the tracked Doppler-corrected γ_{P} in coincidence with $\gamma_{D} = 1115$ keV for $10 < t_{decay} < 100 \ \mu$ s, resulted in the observation of the newly identified 538 and 1052 keV γ

TABLE VI. Properties of the transitions assigned to ¹²⁷Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Ēγ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_f
161.4	38(2)	$(21/2^+) \rightarrow 23/2^+$	2486	2325
192.6	15(2)	$(23/2^+) \rightarrow (21/2^+)$	2678	2486
252.7	11(5)	$(37/2^+) \rightarrow (35/2^+)$	5354	5101
365.1	12(2)	$(35/2^+) \rightarrow (33/2^+)$	5101	4736
386.7	31(3)	$(31/2^+) \rightarrow (29/2^+)$	4255	3868
391.8	60(3)	$(27/2^+) \rightarrow (25/2^+)$	3256	2864
482.0	17(5)	$(33/2^+) \rightarrow (31/2^+)$	4736	4255
516.1	13(3)	$(25/2^+) \rightarrow (23/2^+)$	3194	2678
538.1	30(2)	$(27/2^{-}) \rightarrow (23/2^{-})$	3579	3041
539.1	100	$(25/2^+) \rightarrow 23/2^+$	2864	2325
612.8	46(3)	$(29/2^+) \rightarrow (27/2^+)$	3868	3256
930.9	32(2)	$(27/2^+) \rightarrow (23/2^+)$	3256	2325
999.0	21(3)	$(31/2^+) \rightarrow (27/2^+)$	4255	3256
1052.4	100	$(23/2^-) \rightarrow (19/2^-)$	3041	1989
84.8	11(9)	$(17/2^{-}) \rightarrow (19/2^{-})$	2074	1989
119.9	12(7)	$19/2^+ \rightarrow (17/2^-)$	2194	2074
131.1	49(28)	$23/2^+ \rightarrow 19/2^+$	2325	2194
143.5	14(7)	$19/2^+ \rightarrow 15/2^+$	2194	2051
153.1	2(1)	$(17/2^{-}) \rightarrow 15/2^{-}$	2074	1920
246.9	47(20)	$19/2^+ \rightarrow 15/2^+$	2194	1948
806.0	97(33)	$15/2^- \rightarrow 9/2^+$	1920	1115
824.8	61(21)	$15/2^- \rightarrow 11/2^+$	1920	1096
852.5	43(15)	$15/2^+ \rightarrow 11/2^+$	1948	1096
956.2	17(6)	$15/2^+ \rightarrow 11/2^+$	2051	1096
1095.8	61(20)	$11/2^- \rightarrow 7/2^+$	1096	0
1114.6	100	$9/2^+ \rightarrow 7/2^+$	1115	0

rays. These two transitions are thus placed above the $(19/2^{-})$ isomer, in accordance with the other odd-A Sb isotopes. The inset shows the half-life fit (two-component with one component fixed at 269 ns) for the decay spectrum upon gating on 825 keV transition, which yields a value of $T_{1/2} = 11.7(1) \ \mu s$ for the 15/2⁻ isomer [in agreement with the value of 11(1) μs reported in Ref. [40]].

G. ¹²⁸Sb

A previous γ -ray spectroscopy measurement on the highspin states in ¹²⁸Sb was shown in Ref. [6]. The level scheme as obtained in the present work is shown in Fig. 1. Table VII shows the properties of all the transitions assigned in this work.

The *A*- and *Z*-gated γ -ray spectra for ¹²⁸Sb is shown in Fig. 8. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹²⁸Sb is shown in Fig. 8(a). The already known γ rays, namely 288, 364, 773, 911, and 1061 keV, are seen. In addition, this spectrum shows many new prompt γ rays; namely, the 211, 245, 264, 414, 497, 541, 613, and 1195 keV transitions (marked with an asterisk). Besides, the 128 and 973 keV transitions are also seen (marked with a hash) are observed in both γ_P [Fig. 8(a)] and delayed spectrum (γ_D) [Fig. 8(b)]. The inset in Fig. 8(a) shows the prompt γ - γ coincidence spectrum (γ_P - γ_P) with a sum gate on the 264, 364 and 414 keV prompt transitions. This spectrum shows



FIG. 8. *A*- and *Z*-gated γ -ray spectra for ¹²⁸Sb: (a) Tracked Doppler-corrected Prompt singles γ -ray spectrum (γ_P). The newly identified prompt and delayed γ rays are marked with an asterisk and hash, respectively. The inset shows the γ_P - γ_P coincidence spectrum with sum gate on the γ_P 's, namely the 264, 364 and 414 keV transitions. (b) The delayed singles γ -ray spectrum (γ_D) for $0 < t_{decay} < 4 \ \mu$ s. The newly identified delayed γ rays are marked with hash. The inset shows the γ_D - γ_D coincidence spectrum with gate on the delayed 773 keV γ -ray. (c) The γ_P in coincidence with any delayed γ -ray for $0 < t_{decay} < 4 \ \mu$ s. Again, the newly identified prompt transitions are marked with an asterisk. The inset shows the γ_P - γ_P coincidence spectrum with sum gate on many γ_P 's, namely the 541 and 1195 keV transitions. Panels (d) and (e) show the decay curves along with the fits for the delayed 153 and 773 keV transitions, respectively.

that the 264, 364, 414, 497, 911, and 1061 keV transitions are in coincidence. The delayed γ -ray (γ_D) singles spectrum, with $0 < t_{decay} < 4 \ \mu s$ is shown in Fig. 8(b). This spectrum shows new delayed γ -ray transitions; namely, 128, 153, 189, 259, 360, 385, 524, 556, 697, 767, 844, 973, 1181, 1540, and 1617 keV (marked with hash), in addition to the known 773 and 1061 keV transition. The delayed γ - γ coincidence spectrum (γ_D - γ_D) with gate on the 773 keV transition is shown in the inset of Fig. 8(b). This spectrum shows that the 153, 767, and 844 keV are in coincidence with the 773 keV transition. Figure 8(c) shows the prompt spectrum (γ_P) in coincidence with any delayed γ -ray transition with $0 < t_{decay} < 4 \ \mu s$ is shown in Fig. 8(c). The inset in Fig. 8(c) shows the γ_P - γ_P

TABLE VII. Properties of the transitions assigned to ¹²⁸Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Eγ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_f
211.1	10(5)	$(18^+) \rightarrow (17^+)$	3961	3749
244.8	20(4)	$(17^+) \to (16^+)$	3749	3505
263.9	37(4)	$(16^{-}) \rightarrow (15^{-})$	3011	2748
288.4	27(3)	$(10^-) \rightarrow (9^-)$	1061	773
364.3	60(1)	$(14^{-}) \rightarrow (12^{-})$	2333	1969
413.9	52(2)	$(15^{-}) \rightarrow (14^{-})$	2748	2333
497.0	20(1)	$(17^{-}) \rightarrow (16^{-})$	3508	3011
541.3	58(3)	$(16^+) \to (15^+)$	3505	2964
612.9	100	$(12^+) \to (11^+)$	2230	1617
773.0	100	$(9^-) \rightarrow (8^-)$	773	0
910.9	76(2)	$(12^{-}) \rightarrow (10^{-})$	1969	1061
1061.4	46(2)	$(10^-) \rightarrow (8^-)$	1061	0
1195.1	100	$(15^+) \to (13^+)$	2964	1769
127.8	12(7)	$(9^+) \rightarrow (8^+)$	1540	1412
152.6	45(24)	$(13^+) \to (11^+)$	1769	1617
189.4	11(5)	$(8^+) \rightarrow (7^+)$	1412	1223
259.4	11(5)	$(7^-) \rightarrow (8^-)$	259	0
359.9	14(6)	$(7^+) \rightarrow (8^-)$	360	0
384.8	13(5)	$(11^+) \rightarrow (9^-)$	1617	1232
523.6	25(9)	$(7^+) \rightarrow (6^+)$	1223	697
556.2	42(15)	$(11^+) \to (10^-)$	1617	1061
696.9	17(6)	$(6^+) \rightarrow (8^-)$	697	0
767.0	63(22)	$(9^+) \rightarrow (9^-)$	1540	773
843.8	32(11)	$(11^+) \rightarrow (9^-)$	1617	773
973.3	20(7)	$(9^-) \rightarrow (7^-)$	1232	259
1181.2	4(2)	$(9^+) \rightarrow (7^-)$	1540	360
1540.4	43(15)	$(9^+) \rightarrow (8^-)$	1540	0
1617.2	10(3)	$(11^+) \rightarrow (8^-)$	1617	0

coincidence spectrum with gate on the newly identified 541 and 1195 keV transitions. This spectrum shows that 211, 245, 541, and 1195 keV transitions are in coincidence and placed above the (13⁺) isomer. But Fig. 8(c) shows 613 keV transition which is not present in the inset of Fig. 8(c). Hence, the 613 keV transition is placed above the (11⁺) isomer. Figures 8(d) and 8(e) show the decay curves for 153 and 773 keV transitions, respectively. An exponential fit for these curves yields values 217(7) ns (using a onecomponent fit) and 500(20) ns (using a two-component fit with one component fixed at 217 ns), respectively. This gives $B(E2; 13^+ \rightarrow 11^+) = 23.1(8) e^2 \text{ fm}^4$.

H. ¹²⁹Sb

References [25,41,42] reported the previous γ -ray spectroscopy measurements on ¹²⁹Sb. The level scheme as obtained in the present work is shown in Fig. 1. Table VIII shows the properties of all the transitions assigned in this work.

The *A*- and *Z*-gated γ -ray spectra for ¹²⁹Sb are shown in Fig. 9. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹²⁹Sb is shown in Fig. 9(a). The previously observed 1128 and 1161 keV transitions are seen. Many new prompt γ -ray transitions; namely, 156, 315, 471, 530, 622,



FIG. 9. *A*- and *Z*-gated γ -ray spectra for ¹²⁹Sb: (a) The tracked Doppler-corrected prompt singles γ -ray (γ_P) spectrum with the new γ -ray transitions marked with an asterisk. The inset shows the tracked Doppler-corrected prompt $\gamma_P - \gamma_P$ coincidence spectrum with gate on the newly identified 1078 keV transition. (b), (c) The delayed singles γ -ray (γ_D) spectra for $0 < t_{decay} < 4 \,\mu$ s and $5 < t_{decay} < 10 \,\mu$ s, respectively. The insets in panels (b) and (c) show the decay curves along with the fits for the 189 and 732 keV transitions, respectively. (d) Tracked Doppler-corrected γ_P in coincidence with the sum gate of the γ_D s; namely, 98, 189, 234, and 755 keV delayed transitions (for $0 < t_{decay} < 4 \,\mu$ s).

645, and 1078 keV transitions are identified (marked with an asterisk). The 755 keV (marked with a hash) is observed in both prompt (γ_P) [Fig. 9(a)] and delayed spectrum (γ_D) [Fig. 9(b)]. The 1161 keV is actually depopulating the 9/2⁺ state to the ground state [41,42], and this is not shown in the current level scheme. The inset shows the tracked Doppler-corrected prompt $\gamma_P - \gamma_P$ coincidence spectrum with gate on the newly identified 1078 keV transition. This spectrum shows that the 530 and 1078 keV transitions are in coincidence. A similar coincidence spectrum is obtained for the 315 and 622 keV transitions (not shown in this figure). However, no coincidences are seen upon gating on the 471 and 645 keV transitions, and hence these are not placed in the level scheme. The delayed singles γ -ray (γ_D) spectrum for 0 < t_{decay} < 4 μ s is shown in Fig. 9(b), yielding 98, 189,

TABLE VIII. Properties of the transitions assigned to ¹²⁹Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Eγ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_f
156.1	55(4)	$(21/2^+) \rightarrow 23/2^+$	2295	2139
314.7	44(4)	$(27/2^+) \rightarrow (25/2^+)$	3075	2761
529.7	69(10)	$(27/2^{-}) \rightarrow (23/2^{-})$	3469	2939
622.1	100	$(25/2^+) \rightarrow 23/2^+$	2761	2139
1078.6	100	$(23/2^{-}) \rightarrow 19/2^{-}$	2939	1851
98.3	38(7)	$23/2^+ \rightarrow 19/2^+$	2139	2040
189.2	71(34)	$19/2^+ \rightarrow 19/2^-$	2040	1851
234.0	35(16)	$19/2^+ \rightarrow (17/2^-)$	2040	1806
732.5	47(17)	$15/2^- \rightarrow 11/2^+$	1861	1128
755.0	37(15)	$(15/2^+) \rightarrow 11/2^+$	1883	1128
1128.5	100	$11/2^+ \rightarrow 7/2^+$	1128	0

234, 755, and 1128 keV transitions, as expected from the previous works. The 234 and 755 keV transitions are newly observed (marked with a hash). The 234 keV is placed below the $19/2^+$ state decaying to $(17/2^-)$ state, by following the systematics with the 120 keV in ¹²⁷Sb and 108 keV in ¹³¹Sb. The 755 keV on the other hand is assigned to be depopulating the $(15/2^+)$ to the $11/2^+$ state, in accordance with the 852 keV in ¹²⁷Sb and the shell-model calculations. The required 157 keV from $19/2^+$ to $(15/2^+)$, as seen in the lower odd-A Sb isotopes (442, 332, 247 keV in ^{123–127}Sb, respectively), is not seen in the delayed spectrum. The halflife fit (one-component) for the decay spectrum upon gating on 189 keV transition yields a value of $T_{1/2} = 0.89(3) \ \mu s$ [in agreement with the value of $1.1(1) \ \mu s$ reported in Ref. [25]], which gives $B(E2; 23/2^+ \rightarrow 19/2^+) = 25.3(8) e^2 \text{ fm}^4$ for the $23/2^+$ state. Similarly, Fig. 9(c) shows the γ_D -ray spectrum for 5 < t_{decay} < 10 μ s, leading to 732 and 1128 keV transitions. A half-life fit (two-component with one component fixed to 0.89 μ s) for the decay spectrum upon gating on 732 keV transition yields a value of $T_{1/2} = 2.3(3) \ \mu s$ for the $15/2^{-}$ state [in agreement with the value of 2.2(2) μ s reported in Ref. [25]]. The tracked Doppler-corrected γ_P in coincidence with the sum gate of γ_D s; namely, 98, 189, 234, and 755 keV delayed transitions ($0 < t_{decay} < 4 \mu s$) is shown in Fig. 9(d). This spectrum yields the newly identified prompt 156, 315, and 622 keV γ -ray transitions. Thus, all these transitions are placed above the $23/2^+$ isomer. Since the 156 keV transition is not observed in coincidence with 315 and 622 keV transitions (not shown in this figure), it is assigned depopulating from $(21/2^+)$ to $23/2^+$ state, in accordance with the 161 keV in ¹²⁷Sb and 206 keV in ¹³¹Sb. In addition, the γ_D in coincidence with all these newly observed prompt transitions are studied and all of these yield the 98, 189, and 1128 keV transitions (not shown in this figure). The tracked Doppler-corrected γ_P in coincidence with any γ_D for 5 < t_{decay} < 10 μ s did not result in any new prompt γ rays and hence no transitions are placed above the $15/2^{-1}$ isomer. No prompt-delayed correlations could be carried out for the $19/2^{-}$ isomer because it has a very long half-life of 17.7 min. As the inset of Fig. 9(a) shows the coincidence



FIG. 10. A- and Z-gated γ -ray spectra for ¹³⁰Sb: (a) Tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P). The newly identified prompt γ rays are marked with an asterisk. The inset shows the tracked Doppler-corrected γ_P - γ_P coincidence spectrum with gate on the newly identified 822 keV prompt γ -ray. (b) The delayed singles γ -ray spectrum (γ_D) for $0 < t_{decay} < 5 \mu$ s. The inset shows the γ_D - γ_D coincidence spectrum with gate on the delayed 365 keV γ ray. (c) The tracked Doppler-corrected γ_P in coincidence with the delayed γ rays = 365 and 1143 keV transitions, for $0 < t_{decay} < 5 \mu$ s. The newly identified prompt transitions are marked with an asterisk. The inset shows the decay curve along with the two-component fit for the delayed 365 keV transition.

of 530 and 1078 keV transitions and a similar systematics has been observed in the lower odd-A Sb isotopes, these transitions are placed above the $19/2^{-1}$ isomer.

I. ¹³⁰Sb

A previous measurement on the high-spin states using γ -ray spectroscopy in ¹³⁰Sb was reported in Ref. [43]. The level scheme as obtained in the present work is shown in Fig. 1. Table IX shows the properties of all the transitions assigned in this work.

The *A*- and *Z*-gated γ -ray spectra for ¹³⁰Sb are shown in Fig. 10. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹³⁰Sb is shown in Fig. 10(a). The already known 871 and 1143 keV γ rays are observed. In addition,

TABLE IX. Properties of the transitions assigned to ¹³⁰Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Eγ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_{f}
504.9	100	$(12^+) \to (11^+)$	2050	1545
821.8	48(8)	$(13^+) \to (12^+)$	2872	2050
84.7	11(10)	$6^- \rightarrow 8^-$	85	0
272.1	23(9)	$(10^{-}) \rightarrow (9^{-})$	1143	871
365.2	113(42)	$(11^+) \to (10^-)$	1508	1143
871.1	29(7)	$(9^-) \rightarrow 8^-$	871	0
1143.4	100	$(10^-) \rightarrow 8^-$	1143	0

three new prompt transitions; namely, 145, 505, and 822 keV transitions are observed, which are marked with an asterisk. The inset in Fig. 10(a) shows the tracked Doppler-corrected prompt $\gamma - \gamma$ coincidence spectrum $(\gamma_P - \gamma_P)$ with gate on the newly identified 822 keV transition. This shows that the 505 and 822 keV transitions are in coincidence, as shown in the level scheme. But 145 keV is not observed in coincidence and hence not placed in the level scheme. Figure 10(b) shows the delayed γ -ray (γ_D) singles spectrum with $0 < t_{decay} < 5 \ \mu s$. All the known delayed γ rays; namely, 85, 272, 365, 871, and 1143 keV transitions are observed. The delayed $\gamma - \gamma$ $(\gamma_D - \gamma_D)$ coincidence spectrum with gate on 365 keV transition is shown in the inset of Fig. 10(b). Figure 10(c) shows the tracked Doppler-corrected γ_P in coincidence with the sum gate of $\gamma_D = 365$ and 1143 keV transitions. This yields the newly identified 505 keV transition. As from the inset of Fig. 10(a), the 505 and 822 keV transitions are seen in coincidence, these two transitions are placed above the (11^+) state, following the systematics with the lower even-A Sb isotopes. The inset in Fig. 10(c) shows the decay curve for the delayed 365 keV transition. A one-component fit to this transition yielded a value shorter than 1.8(2) μ s for the (13⁺) state [43]. The discrepancy in the $T_{1/2}$ of (13⁺) state may be due to the time of flight of $\sim 2 \ \mu s$ for the setup used in Ref. [43], that bias the measurement of the half-life to higher values. Thus, the (11^+) state might also have a halflife, as observed in the lower even-A Sb isotopes. A two component fit [as shown in the lower inset in Fig. 10(c)] was carried out, which yielded a half-life of $1.25(1) \ \mu s$ for the (13⁺) state and 0.600(15) μs for the (11⁺) state. The $B(E2; 13^+ \rightarrow 11^+) = 105(6) e^2 \text{ fm}^4$ was obtained.

J. ¹³¹Sb

The high-spin γ -ray spectroscopy of ¹³¹Sb was previously reported in Refs. [26,44]. The level scheme as obtained in the present work is shown in Fig. 1. Table X shows the properties of all the transitions assigned in this work.

The *A*- and *Z*-gated γ -ray spectra for ¹³¹Sb are shown in Fig. 11. The tracked Doppler-corrected prompt singles γ -ray spectrum (γ_P) for ¹³¹Sb is shown in Fig. 11(a). The previously known 1226 keV transition is seen in this spectrum. However the other transitions; namely, 96, 344, 382, and 450 keV are not seen in Fig. 11(a) because these decay directly from long-lived isomers. In addition, many



FIG. 11. A- and Z-gated γ -ray spectra for ¹³¹Sb: The tracked Doppler-corrected prompt singles γ -ray (γ_P) spectrum with the new γ -ray transitions marked with asterisk. The inset shows the tracked Doppler-corrected prompt γ_P - γ_P coincidence spectrum with gate on the newly identified 1756 keV transition. (b), (c) The delayed singles γ -ray (γ_D) spectra for $0 < t_{decay} < 3 \ \mu$ s and $5 < t_{decay} < 150 \ \mu$ s, respectively. The insets in panels (b) and (c) show the decay curves along with the fits for the 344 and 450 keV transitions, respectively. (d) Tracked Doppler-corrected γ_P in coincidence with the sum gate of the γ_D ; namely, 96, 344, and 382 keV delayed transitions (for $0 < t_{decay} < 3 \ \mu$ s).

new prompt γ -ray transitions, namely 206, 313, 769, 776, 798, 820, and 1756 keV transitions, are identified (marked with an asterisk). The inset shows the tracked Doppler-corrected prompt γ_{P} - γ_{P} coincidence spectrum with gate on the newly identified 1756 keV transition. This spectrum shows that the 769, 820, and 1756 keV transitions are in coincidence. A similar coincidence spectrum is obtained for the 206, 313, and 776 keV transitions (not shown in this figure). However, no coincidences could be observed with a gate on the 798 keV transition, and hence this is not placed in the level scheme. The delayed singles γ -ray (γ_D) spectrum for $0 < t_{decay} < 3 \ \mu s$ is shown in Fig. 11(b), yielding 96, 344, and 382 keV transitions, as observed in previous measurements. The half-life fit (one-component) for the decay spectrum upon gating on 344 keV transition

TABLE X. Properties of the transitions assigned to ¹³¹Sb obtained in this work. The top and bottom panels, separated by a line, are for the prompt and delayed transitions, respectively.

Eγ	I_{γ}	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i	E_{f}
206.1	56(4)	$(21/2^+) \rightarrow 23/2^+$	2372	2166
313.3	16(3)	$(25/2^+) \rightarrow (23/2^+)$	3461	3148
768.7	100	$(25/2^+) \rightarrow 23/2^+$	2935	2166
776.0	38(5)	$(23/2^+) \rightarrow (21/2^+)$	3148	2372
820.0	43(4)	$(27/2^+) \rightarrow (25/2^+)$	3755	2935
1755.7	36(5)	$(31/2^+) \rightarrow (27/2^+)$	5510	3755
96.3	11(8)	$23/2^+ \to 19/2^+$	2166	2070
343.6	30(11)	$19/2^+ \to 17/2^-$	2070	1726
382.4	16(6)	$19/2^+ \to 19/2^-$	2070	1688
450.0	61(22)	$15/2^- \rightarrow 11/2^+$	1676	1226
1226.2	100	$11/2^+ \rightarrow 7/2^+$	1226	0

yields a value of $T_{1/2} = 0.97(3) \ \mu s$ for the $23/2^+$ state [in agreement with the value of $1.1(2) \ \mu s$ given in Ref. [26]], yielding $B(E2; 23/2^+ \rightarrow 19/2^+) = 24.6(8) e^2 \text{ fm}^4$. Similarly, Fig. 11(c) shows the delayed γ -ray spectrum for $5 < t_{decay} < 150 \ \mu s$, leading to 450 and 1226 keV transitions. A half-life fit (using a three component fit with two components fixed to 0.97 μ s and 4.3 μ s) for the decay spectrum upon gating on 450 keV transition yields a value of $T_{1/2} = 64(3) \mu s$ for the $15/2^-$ state [in agreement with $65(5) \ \mu s$ quoted by Ref. [26]]. The $B(E2; 19/2^- \rightarrow 15/2^-) = 41(8) \ e^2 \ \text{fm}^4$, as given in Ref. [22]. The tracked Doppler-corrected γ_P in coincidence with the sum gate of the γ_D s; namely, 96, 344, and 382 keV delayed transitions (for $0 < t_{decay} < 3 \mu s$) is shown in Fig. 11(d). This spectrum yields almost all the newly identified prompt γ -ray transitions, that are placed above the $23/2^+$ isomer. In addition, the γ_D in coincidence with all the newly observed prompt transitions are studied and all of these yield the 96, 344, and 382 keV transitions (not shown in this figure). However, the tracked Doppler-corrected γ_P in coincidence with any γ_D for $5 < t_{decay} < 150 \ \mu s$, did not result in any new prompt γ rays and hence no transitions are placed above the $15/2^-$ isomer. Also, no transitions could be placed above the $19/2^-$ isomer.

IV. DISCUSSION

A systematic study of both odd-A and even-A ¹²²⁻¹³¹Sb isotopes was carried out in this work. The observed excited states in ¹²²⁻¹³¹Sb (Z = 51) isotopes have a close correspondence with those in ¹²¹⁻¹³⁰Sn (Z = 50) isotopes. This can be evinced from the similarities in the energy differences of the low-lying states in the even-A/odd-A Sn i.e., $E(2^+) - E(0^+) \sim E(15/2^-) - E(11/2^-)$ and odd-A/even-A Sb i.e., $E(11/2^+) - E(7/2^+) \sim E(10^-) - E(8^-)$, respectively. This is depicted in Fig. 12. Similar correspondence for selected high-spin states is presented in Fig. 13. These similarities are due to the fact that the Sb isotopes have a single valence proton particle in the $g_{7/2}$ orbital in addition to neutrons in the corresponding Sn isotopes.



FIG. 12. Evolution of the experimental (Expt.) energy differences, as a function of mass number, in Sn (open symbols) (a) $E(2^+) - E(0^+)$ (red squares), $E(15/2^-) - E(11/2^-)$ (black circle), and in Sb (shaded symbols) (b) $E(11/2^+) - E(7/2^+)$ (red squares), $E(10^-) - E(8^-)$ (black circle). The filled symbol is the newly observed state from the present experiment.

A better understanding of the aforementioned correspondence for the high-spin states in Sb and Sn isotopes was achieved by performing shell-model calculations, with the interaction used in Ref. [6] (denoted by SM1). The model space was constituted of a restricted single-particle space consisting of active particles, the neutrons in $(v) d_{3/2}, s_{1/2}, h_{11/2}$ orbits, and a proton in $(\pi) g_{7/2}$ orbit near the Fermi surface. This interaction was derived from the original jj55pn interaction [45], where the *diagonal* two-body matrix elements (TBMEs) were adjusted to account for the missing correlations in the restricted model space. The modified (original) multiplets, used in Ref. [6], were:

(i)
$$\langle d_{3/2}^2; I | \hat{\mathcal{H}} | d_{3/2}^2; I \rangle = -0.6048 \, (-0.3024),$$
 and 0.22104 (0.14814) for $I = 0$ and 2, respectively;



FIG. 13. Evolution of the experimental (Expt.) (a) 5^- (black triangle down), 6^- (green diamond), 7^- (red triangle up), 8^+ (blue circle), 10^+ (violet square), $23/2^+$ (brown x), and $19/2^+$ (orange star) states in $^{118-130}$ Sn (open symbols), and (b) $15/2^-$ (black triangle down), $17/2^-$ (green diamond), $19/2^-$ (red triangle up), $19/2^+$ (blue circle), $23/2^+$ (violet square), 13^+ (brown x), and 11^+ (orange star) states in $^{123-131}$ Sb (shaded symbols) with mass number, A. The filled symbols are the newly observed states from the present experiment.



FIG. 14. (a) Comparison of the experimental (Expt.) level schemes with that obtained from shell model calculations using the interaction in Ref. [6] (SM1 blue) and the modified interaction in the present work (SM2 red) for both positive and negative-parity states in ¹²⁷Sb. The different states with the same spin have been joined by dotted lines to show the agreement. (b) The experimental and calculated B(*E*2) values (black square) for the $23/2^+ \rightarrow 19/2^+$ in odd-A ¹²³⁻¹³¹Sb (see text).

- (ii) $\langle s_{1/2}^2; I | \hat{\mathcal{H}} | s_{1/2}^2; I \rangle = -0.959904 (-0.59994)$ for I = 0;
- (iii) $\langle h_{11/2}^2; I | \hat{\mathcal{H}} | h_{11/2}^2; I \rangle = -1.88544 (-0.94545), -0.88533 (-0.435330), 0.20683 (0.10683), 0.27145 (0.17145), and 0.33148 (0.23148) for <math>I = 0, 2, 6, 8,$ and 10, respectively;
- (iv) $\langle d_{3/2}h_{11/2}; I|\hat{\mathcal{H}}|d_{3/2}h_{11/2}; I\rangle = -0.08335 (0.016650)$ for I = 4; and
- (v) $\langle d_{3/2}s_{1/2}; I|\hat{\mathcal{H}}|d_{3/2}s_{1/2}; I\rangle = 0.05607 (-0.06399)$, for I = 2;

where $\hat{\mathcal{H}}$ represents the Hamiltonian. Effective charges of $e_{\nu} = 0.9$ and $e_{\pi} = 1.8$ were chosen to reproduce the known B(E2) values in ¹³⁰Sn $(B(E2); 10^+ \rightarrow 8^+)$ and ¹³⁴Te $(B(E2); 6^+ \rightarrow 4^+)$ isotopes. The calculations were performed by using the shell-model code, NATHAN [46]. Using SM1, the excitation energies could be well reproduced, while the binding energies and B(E2) transition probabilities were not properly reproduced. This is illustrated for ¹²⁷Sb for the level energies and for the $B(E2; 23/2^+ \rightarrow 19/2^+)$ in odd-A Sb isotopes in Fig. 14. Similar inconsistencies were observed for the other isomeric transitions (not shown in the figure).

Therefore, to improve the agreement of B(E2) values, the following parameters of the shell-model interaction were modified (denoted by SM2):

- (i) the monopole part of $\langle h_{11/2}^2 | \hat{\mathcal{H}} | h_{11/2}^2 \rangle$ was reduced by 185 keV, which led to an improved reproduction of the binding energies and the $(B(E2); 10^+ \rightarrow 8^+)$ for the even-*A* Sn isotopes;
- (ii) the monopole part of $\langle d_{3/2}^2 | \hat{\mathcal{H}} | d_{3/2}^2 \rangle$ was reduced by 450 keV, which led to a better reproduction of the $(B(E2); 23/2^+ \rightarrow 19/2^+)$ in odd-A Sb isotopes;
- (iii) the pairing term, $\langle d_{3/2}^2 | \hat{\mathcal{H}} | h_{11/2}^2 \rangle$, was increased by 260 keV, which led to the agreement of all the *B*(*E*2) values, except those for the odd-*A* Sb isotopes. Also, all the excitation energies became higher by 2 MeV;



FIG. 15. Comparison of experimental (Expt.) (shown in black) [22–26] and theoretical calculations [from shell model (SM2); shown in red] level schemes for odd- $A^{121-131}$ Sb isotopes for both positive (+ve) and negative (-ve) parities. The experimental and shell-model states of the same spin-parity have been joined with dotted lines to show the agreement.

- (iv) the pairing term, $\langle h_{11/2}^2 | \hat{\mathcal{H}} | h_{11/2}^2 \rangle$, was increased by 140 keV, to compensate for this increase in excitation energies as well as seeing to it that the *B*(*E*2)s of all the Sn and Sb do not change drastically;
- (v) the $\langle \pi g_{7/2} \nu h_{11/2}; I | \mathcal{H} | \pi g_{7/2} \nu h_{11/2}; I \rangle$ (I = 8) was reduced by 400 keV, which reproduced the B(E2)s for the odd-A Sb as well; and
- (vi) the monopole part of $\langle d_{3/2}h_{11/2}|\hat{\mathcal{H}}|d_{3/2}h_{11/2}\rangle$ was increased by 30 keV to achieve a better reproduction of B(E2) in odd-A Sn isotopes.

These modifications led to the reproduction of the binding energies (within ~2 MeV), excitation energies (within ~500 keV) and the B(E2) transition strengths (within ~50 e^2 fm⁴) for the isotopic chains of ^{119–130}Sn and ^{121–131}Sb. The energies of the excited states for ¹²⁷Sb and the improved B(E2) values for the odd-A Sb isotopes are shown in Fig. 14. The reason behind the large discrepancy in the B(E2)s between SM1 and SM2 can be understood based on the difference in the wave functions obtained in both calculations. The wave functions from SM2 are much more fragmented configuration-wise than those in SM1, leading to the dramatic reduction in the B(E2) values.

A. Excitation energies

A comparison of the experimental (black) and calculated (red) level schemes (using SM2) for both the positive (+ve) and negative (-ve) parities in odd- $A^{123-131}$ Sb isotopes is shown in Fig. 15. The data for ¹²¹Sb are taken from Ref. [23] and are also shown in this figure for comparison. The calculated order for the 9/2⁺ and 11/2⁺ states are inverted only for the odd- $A^{123-125}$ Sb isotopes. A mismatch in the ordering of the 15/2⁻, 17/2⁻, and 19/2⁻ states are observed in ¹²¹⁻¹²⁹Sb isotopes, as these states are very close in energy. Similarly, Fig. 16 shows the comparison of the experimental (black) and calculated (red) level schemes for both the positive (+ve) and negative (-ve) parities in even- $A^{122-130}$ Sb isotopes. The data for ¹²⁰Sb are taken from Ref. [47] and are also shown in this figure for comparison. This figure shows that the experimental



FIG. 16. Comparison of experimental (Expt.) (shown in black) [6,35,36,43,47] and theoretical calculations [from shell model (SM2); shown in red] level schemes for even-A ¹²²⁻¹³⁰Sb isotopes for both positive (+ve) and negative (-ve) parities. The experimental and shell-model states of the same spin-parity are joined with dotted lines to show the agreement.

energies are in reasonable agreement with the theoretical calculations.

Isomeric $15/2^-$, $19/2^-$, and $23/2^+$ were previously observed in odd-A Sb isotopes. These were interpreted as the odd $g_{7/2}$ proton coupled to the known isomeric 5⁻, 7⁻, and 10^+ states in the corresponding even-(A - 1) Sn isotopes, respectively [40]. These states along with the 6^- and 8^+ states for even-A Sn and the $17/2^-$ and $19/2^+$ states for odd-A Sb are shown in Figs. 13(a) and 13(b), respectively. In addition, the evolution of $19/2^+$ and $23/2^+$ states in odd-A Sn, and 11^+ and 13^+ states in even-A Sb are shown in these plots. The newly identified $(17/2^{-})$ and $(19/2^{-})$ states in ¹²⁷Sb; and the $(17/2^{-})$ state in ¹²⁹Sb (from the current experimental analysis) fit in the systematics. Comparison with the Sn isotopes shows that the energies of the positive-parity states in Sb follow a pattern similar to that of the Sn isotopes, with a slight dip in the case of ¹²⁹Sb. Also, the crossing of the 7^- and 5^- observed at 128 Sn is seen in the equivalent states in 129 Sb. In addition, the newly identified 11^+ and 13^+

states in even-A Sb isotopes follow a similar pattern to the corresponding $19/2^+$ and $23/2^+$ states in odd-A Sn isotopes.

B. *B*(*E*2) transition probabilities

The experimental B(E2) values along with SM2 shellmodel calculations are shown in Fig. 17.

Case I: (a)
$$10^+ \rightarrow 8^+$$
 in even-A ^{118–130}Sn [16,21,48], (b)
23/2⁺ $\rightarrow 19/2^+$ in odd-A ^{123–131}Sb (see text);
Case II: (c) $7^- \rightarrow 5^-$ in even-A ^{118–126}Sn [21], (d)

- $\begin{array}{l} 19/2^{-} \rightarrow 15/2^{-} \text{ in odd-} A^{123-131} \text{Sb (see text);} \\ \text{Case III: (e) } 23/2^{+} \rightarrow 19/2^{+} \text{ in odd-} A^{119-129} \text{Sn [20,21],} \\ \text{(f) } 13^{+} \rightarrow 11^{+} \text{ states in the even-} A^{126-130} \text{Sb (see text); and} \end{array}$
- Case IV: (g) $27/2^- \rightarrow 23/2^-$ in odd-A ^{119–129}Sn isotopes [20,21,49].

The full calculations are shown by red solid lines, those restricted to one broken pair are shown by dash-dotted



FIG. 17. The experimental (Expt.) B(*E*2) values (black squares) for the (a) $10^+ \rightarrow 8^+$ in even- $A^{118-130}$ Sn [16,21,48], (b) $23/2^+ \rightarrow 19/2^+$ in odd- $A^{123-131}$ Sb (see text), (c) $7^- \rightarrow 5^-$ in even- $A^{118-126}$ Sn [21], (d) $19/2^- \rightarrow 15/2^-$ transitions in odd- $A^{123-131}$ Sb (see text), (e) $23/2^+ \rightarrow 19/2^+$ in odd- $A^{119-129}$ Sn [20,21], (f) $13^+ \rightarrow 11^+$ in the even- $A^{126-130}$ Sb (see text), and (g) $27/2^- \rightarrow 23/2^-$ in odd- $A^{119-129}$ Sn isotopes [20,21,49]. The shell-model calculations using the full interaction SM2 (red solid line), SM2 restricted to only one broken neutron pair (green dash-dotted line) and SM2 with $e_{\pi} = 0$ (purple dotted line) are also shown. The probability ratios for the (h)–(j) neutron seniority mixing [$(P(v_{\nu})/P(v_{\nu} + 2)]$ and (k)–(m) neutron angular-momentum mixing [$(P(I_{\nu})/P(I_{\nu} - 2)]$ and [$(P(I_{\nu})/P(I_{\nu} - 1)]$ are also shown.

green lines, and the full calculations with proton effective charge, $e_{\pi} = 0$, are shown by dotted violet lines. The seniority mixing, represented by the ratio of probabilities of lowest, natural (v_{ν}) , and higher $(v_{\nu} + 2)$ neutron seniorities $[P(v_{\nu})/P(v_{\nu} + 2)]$, are shown in Figs. 17(h)–17(j) for Cases I–III, respectively. The dotted black line with $P(v_{\nu})/P(v_{\nu} + 2) = 1$ represents that the mixing of seniorities, v_{ν} and $v_{\nu} + 2$, are equal. Similarly, Figs. 17(k)–17(m) for Cases I–III, respectively, denote the neutron angularmomentum mixing, represented by the ratio of probabilities of highest (I_{ν}) and lower $(I_{\nu} - 2 \text{ or } I_{\nu} - 1)$ neutron angular momenta $[P(I_{\nu})/P(I_{\nu} - 2) \text{ or } P(I_{\nu})/P(I_{\nu} - 1)]$. The dotted black line, similar to the case of neutron seniorities, denotes that the mixing of I_{ν} and $I_{\nu} - 2$ or $I_{\nu} - 1$ are equal. The present calculations agree well with the experimental values and the experimental trends are reproduced. In general, the shape of the B(E2) curves for Sn follow a parabolic behavior, as expected for seniority scheme. The full calculation and the one restricted to one broken pair, in Sn, are very similar and also the calculated neutron seniority $v_{\nu} = 2$, 3 dominates for odd-*A*, even-*A* Sn, respectively. In addition, the behavior of B(E2) for odd-*A* Sb isotopes is similar to that of the corresponding Sn, except the even-*A* Sb. The proton charge (e_{π}) does not have a considerable impact on the B(E2), except in even-*A* Sb. A detailed discussion of the four different cases, mentioned above, is given below:

Case I: From shell-model calculations, it is seen that the dominant configuration of the 10^+ and 8^+ states in



FIG. 18. (a) The states with different neutron seniorities at different excitation energies in even-A Sn (Z, N) (¹²⁴Sn), odd-A Sb (Z + 1, N) (¹²⁵Sb), odd-A Sn (Z, N + 1) (¹²⁵Sn), and even-A Sb (Z + 1, N + 1) (¹²⁶Sb) isotopes. The blue and red arrows represent the energy required to break the first pair of neutrons from seniority $v_{\nu} = n$ to $v_{\nu} = n + 2$ (n = 0, ..., 4) in even-A Sn [$E(2^+ \rightarrow 0^+)$] and other isotopes, respectively. (b) Plot of the energy differences between states with neutron seniority $v_{\nu} = n$ and $v_{\nu} = n + 2$ (n = 0, ..., 4), as shown in panel (a), for odd-A and even-A ¹¹⁹⁻¹³⁰Sn and ¹²¹⁻¹³¹Sb nuclei.

even-A Sn is $\nu h_{11/2}^{-2}$, while that of the 23/2⁺ and 19/2⁺ states in odd-A Sb is $\pi g_{7/2} \nu h_{11/2}^{-2}$. The nature of the curves in Figs. 17(a) and 17(b) is not completely identical. This is evident from the differences in the full calculations and that restricted to one broken pair in Sb. For a microscopic understanding behind this difference, a comparison of the neutron seniority for the $23/2^+$ and $19/2^+$ states was carried out. Figure 17(h) shows that the lowest neutron seniority $v_{\nu} = 2$ is mixed with $v_{\nu} = 4$ for both states. The mixing increases with the increasing number of valence neutron holes. However, for the lowest A, the number of available neutron pairs is reduced in the restricted model space, which leads to a sudden drastic decrease in seniority mixing. In addition to mixing of neutron seniorities, neutron angularmomentum mixing is also observed, as shown in Fig. 17(k). The angular-momentum mixing also increases with increase in the number of valence neutron holes. A comparison of neutron seniority and neutron angular-momentum mixing plots shows that the angular-momentum mixing is the dominant one.

Case II: Shell-model calculations show that the dominant configuration of the 7⁻ and 5⁻ states in even-*A* Sn is $\nu h_{11/2}^{-1} d_{3/2}^{-1}$, while that of the 19/2⁻ and 15/2⁻ states in odd-*A* Sb is $\pi g_{7/2} \nu h_{11/2}^{-1} d_{3/2}^{-1}$. The nature of the curves in Figs. 17(c) and 17(d) is similar. A comparison of the neutron seniority for the 19/2⁻ and 15/2⁻ states was carried out. Figure 17(i) shows that the lowest neutron seniority $\nu_{\nu} = 2$ is mixed with the $\nu_{\nu} = 4$ for both states, similar to Case I. In addition to mixing of neutron seniorities, neutron angular-momentum

mixing is also observed, as shown in Fig. 17(1), which is of similar order as the seniority mixing. The angular-momentum mixing also increases with increasing number of valence neutron holes.

Case III: The shell-model calculations show that the dominant configuration of the $23/2^+$ and $19/2^+$ states in odd-A Sn is $\nu h_{11/2}^{-2} d_{3/2}^{-1}$, while that of the 13⁺ and 11⁺ states in even-A Sb is $\pi g_{7/2} v h_{11/2}^{-2} d_{3/2}^{-1}$. The nature of the curves in Figs. 17(e) and 17(f) is significantly different. This is also evident from the differences in the full calculations and that restricted to one broken pair in Sb. The calculations with proton charge restricted to zero show that the neutrons have a considerable impact on the B(E2) in even-A Sb. For a microscopic understanding behind this difference, a comparison of the neutron seniority for the $23/2^+$ and $19/2^+$ states was carried out. Figure 17(j) shows that the lowest neutron seniority $v_{\nu} = 3$ is mixed with the $v_{\nu} = 5$ for both states. The mixing increases with increasing number of valence neutron holes. In addition to mixing of neutron seniorities, neutron angular-momentum mixing is also observed, as shown in Fig. 17(m). The angularmomentum mixing also increases with increasing number of valence neutron holes. A comparison of neutron seniority and neutron angular-momentum mixing plots show that the angular-momentum mixing is the dominant one, just as in Case I. Note that, around A = 126, as compared with the earlier two cases, both the seniority and angular-momentum mixing are significant; the higher seniority $(v_v + 2)$ and the lower angular momentum $(I_v - 2)$ dominate the 11⁺ and 13⁺ states.

Case IV: The shell-model calculations show that the dominant configuration of the $27/2^-$ and $23/2^-$ states in odd-*A* Sn is $\nu h_{11/2}^{-3}$. The corresponding isomer in even-*A* Sb with configuration $\pi g_{7/2} \nu h_{11/2}^{-3}$ is expected at $I^{\pi} = 16^-$. In the present work, the 16^- states in 126,128 Sb decay by *M*1 transitions to 15^- states, and hence no isomer was observed. In 120 Sb, in contrast, the 16^- state decays via a 148 keV transition to the 14^- state and has a half-life $T_{1/2} = 14(3)$ ns [47]. The nature of the curve in Fig. 17(g) is a parabola, similar to Fig. 17(a). The present calculations show that the dominant seniority for these states is $\nu_{\nu} = 3$, which in fact is in agreement with the calculations assuming only one broken pair.

C. Neutron pair-breaking energies

A striking feature of the constancy of the energy differences, where the increase in the number of broken neutron pairs is involved, was observed and is shown in Fig. 18. Figure 18(a) shows particular states in even-A Sn (Z, N) (¹²⁴Sn), and odd-A Sn (Z, N + 1) (¹²⁵Sn) isotopes, which involve the breaking of a pair of neutrons, leading to increase in seniority from $v_{\nu} = n$ to $v_{\nu} = n + 2$, where $n = 0, \dots, 4$ at different excitation energies. Similar states in odd-A Sb (Z + 1, N) (^{125}Sb) and even-A Sb (Z + 1, N + 1) (^{126}Sb) isotopes are also shown in the same figure. All the arrows represent the energy difference quantum with magnitude of ~ 1.1 MeV. The blue arrow represents the breaking of the first pair of neutrons in even-A Sn for the $E(2^+ \rightarrow 0^+)$. The red arrows are for all the other transitions. A plot of the energy differences in ^{119–130}Sn and ^{121–131}Sb isotopes is shown in Fig. 18(b). A subset of this figure, including only the lower spins, was shown earlier in Fig. 12. This figure shows that the average energy for the breaking of the first and second pair of neutrons is $\sim 1.1 \text{ MeV}$, and this is constant (with a deviation of $\sim 100 \text{ keV}$) for a wide range of mass numbers, irrespective of the excitation energy and mixing of neutron seniorities (v_{ν}) in the case of Sn and Sb. In addition, it follows the behaviour of even-A Sn isotopes for $E(2^+ \to 0^+)$.

V. SUMMARY AND CONCLUSIONS

The neutron-rich $^{122-131}$ Sb isotopes were produced as fission fragments in the reaction 9 Be (238 U, f) with 6.2 MeV/u beam energy. The isomers already known in the odd- $A^{123-131}$ Sb isotopes were confirmed and a number of new

prompt and delayed transitions were identified for all these isotopes. New isomers and prompt and delayed γ rays were identified in the even- $A^{122-130}$ Sb isotopes. These results could be achieved by using the unique combination of the AGATA, VAMOS++, and EXOGAM detectors, which was used for the prompt-delayed spectroscopy of fission fragments. A good agreement was achieved between the experiment and the results of the shell-model calculations in the restricted model space using an optimized interaction. Also, the level schemes were in good agreement with that of the corresponding states in the Sn isotopes. The presence of a single valence proton particle in the $g_{7/2}$ orbital leads to a neutron seniority mixing and neutron angular-momentum mixing in the Sb isotopes for all the states. The angular-momentum mixing, in general, was found to be significantly stronger than the seniority mixing. This work shows that further experimental work is required to search for new isomers in the even-A ^{122,124}Sb isotopes, which could not be observed in this work either due to low statistics, too long half-life, or too short half-life. This will give more insight into the nature of the B(E2) values, and hence the mixing of seniorities and angular momenta due to the $\nu\pi$ interaction.

ACKNOWLEDGMENTS

The authors would like to thank the AGATA Collaboration for the availability of the AGATA γ -ray tracking array at GANIL. We acknowledge the important technical contributions of GANIL accelerator staff. We thank C. Schmitt and A. O. Macchiavelli for help in various aspects of data collection. We also thank P. Van Isacker for his valuable discussions on the theoretical interpretation and careful reading of the paper. P.B. and A.M. acknowledge support from the Polish National Science Centre (NCN) under Contract No. 2016/22/M/ST2/00269 and the French LEA COPIGAL project. S.Bi., R.B., S.Bh., S.Bh., and R.P. acknowledge support from CEFIPRA project No. 5604-4 and the LIA France-India agreement. H.L.C. and P.F. acknowledge support from the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under Contract No. DE-AC02-05CH11231 (LBNL). R.M.P.V. acknowledge partial support by Ministry of Science, Spain, under the grants BES-2012-061407, SEV-2014-0398, FPA2017-84756-C4 and by EU FEDER funds. A.J. was supported by the Spanish Ministerio de Economía y Competitividad under contract FPA2017-84756-C4-2-P.

- R. F. Casten, Nuclear Structure from a Simple Perspective (Oxford Science Publications, Oxford, 2000).
- [2] NUDAT2, http://www.nndc.bnl.gov/nudat2/ (2019).
- [3] T. Togashi, Y. Tsunoda, T. Otsuka, N. Shimizu, and M. Honma, Phys. Rev. Lett. **121**, 062501 (2018).
- [4] B. Maheshwari and A. K. Jain, Phys. Lett. B 753, 122 (2016).
- [5] A. I. Morales, G. Benzoni, H. Watanabe, G. de Angelis, S. Nishimura, L. Coraggio, A. Gargano, N. Itaco, T. Otsuka, Y. Tsunoda, P. Van Isacker, F. Browne *et al.*, Phys. Lett. B 781, 706 (2018).
- [6] M. Rejmund, A. Navin, S. Biswas, A. Lemasson, M. Caamaño, E. Clément, O. Delaune, F. Farget, G. de France, B. Jacquot, and P. Van Isacker, Phys. Lett. B **753**, 86 (2016).
- [7] P. Bhattacharyya, P. J. Daly, C. T. Zhang, Z. W. Grabowski, S. K. Saha, R. Broda, B. Fornal, I. Ahmad, D. Seweryniak, I. Wiedenhöver, M. P. Carpenter, R. V. F. Janssens *et al.*, Phys. Rev. Lett. **87**, 062502 (2001).
- [8] P. Cottle, Nature (London) 465, 430 (2010).
- [9] K. L. Jones, A. S. Adekola, D. W. Bardayan, J. C. Blackmon, K. Y. Chae, K. A. Chipps, J. A. Cizewski, L. Erikson, C. Harlin,

R. Hatarik, R. Kapler, R. L. Kozub *et al.*, Nature (London) **465**, 454 (2010).

- [10] D. Rosiak, M. Seidlitz, P. Reiter, H. Naïdja, Y. Tsunoda, T. Togashi, F. Nowacki, T. Otsuka, G. Colò, K. Arnswald, T. Berry, A. Blazhev *et al.*, Phys. Rev. Lett. **121**, 252501 (2018).
- [11] L. Coraggio, A. Covello, A. Gargano, N. Itaco, and T. T. S. Kuo, Phys. Rev. C 91, 041301(R) (2015).
- [12] E. Teruya, N. Yoshinaga, K. Higashiyama, and A. Odahara, Phys. Rev. C 92, 034320 (2015).
- [13] S. Biswas, R. Palit, A. Navin, M. Rejmund, A. Bisoi, M. S. Sarkar, S. Sarkar, S. Bhattacharyya, D. C. Biswas, M. Caamaño, M. P. Carpenter, D. Choudhury *et al.*, Phys. Rev. C **93**, 034324 (2016).
- [14] H.-K. Wang, S. K. Ghorui, K. Kaneko, Y. Sun, and Z. H. Li, Phys. Rev. C 96, 054313 (2017).
- [15] Y. H. Kim, M. Rejmund, P. Van Isacker, and A. Lemasson, Phys. Rev. C 97, 041302(R) (2018).
- [16] B. Fogelberg, K. Heyde and J. Sau, Nucl. Phys. A 352, 157 (1981).
- [17] S. Pietri, A. Jungclaus, M. Górska, H. Grawe, M. Pfützner, L. Cáceres, P. Detistov, S. Lalkovski, V. Modamio, Z. Podolyák, P. H. Regan, D. Rudolph *et al.*, Phys. Rev. C 83, 044328 (2011).
- [18] A. Astier, M.-G. Porquet, C. Theisen, D. Verney, I. Deloncle, M. Houry, R. Lucas, F. Azaiez, G. Barreau, D. Curien, O. Dorvaux, G. Duchêne *et al.*, Phys. Rev. C 85, 054316 (2012).
- [19] W. Iskra, R. Broda, J. Wrzesinski, M. P. Carpenter, C. J. Chiara, B. Fornal, N. Hoteling, R. V. Janssens, F. G. Kondev, W. Królas, T. Lauritsen, T. Pawat *et al.*, Act. Phys. Pol. B **89**, 395 (2014).
- [20] R. L. Lozeva, G. S. Simpson, H. Grawe, G. Neyens, L. A. Atanasova, D. L. Balabanski, D. Bazzacco, F. Becker, P. Bednarczyk, G. Benzoni, N. Blasi, A. Blazhev *et al.*, Phys. Rev. C 77, 064313 (2008).
- [21] L. W. Iskra, R. Broda, R. V. F. Janssens, C. J. Chiara, M. P. Carpenter, B. Fornal, N. Hoteling, F. G. Kondev, W. Królas, T. Lauritsen, T. Pawłat, D. Seweryniak *et al.*, Phys. Rev. C 93, 014303 (2016).
- [22] D. S. Judson, A. M. Bruce, T. Kibédi, G. D. Dracoulis, A. P. Byrne, G. J. Lane, K. H. Maier, C.-B. Moon, P. Nieminen, J. N. Orce, and M. J. Taylor, Phys. Rev. C 76, 054306 (2007).
- [23] H. Watanabe, G. J. Lane, G. D. Dracoulis, T. Kibédi, A. P. Byrne, P. Nieminen, R. O. Hughes, F. G. Kondev, M. P. Carpenter, R. V. F. Janssens, T. Lauritsen, D. Seweryniak *et al.*, Phys. Rev. C **79**, 024306 (2009).
- [24] H. Watanabe, G. J. Lane, G. D. Dracoulis, a. P. Byrne, P. Nieminen, F. G. Kondev, K. Ogawa, M. P. Carpenter, R. V. F. Janssens, T. Lauritsen, D. Seweryniak, S. Zhu *et al.*, Eur. Phys. J. A **42**, 163 (2009).
- [25] J. Genevey, J. A. Pinston, H. R. Faust, R. Orlandi, A. Scherillo, G. S. Simpson, I. S. Tsekhanovich, A. Covello, A. Gargano, and W. Urban, Phys. Rev. C 67, 054312 (2003).
- [26] J. Genevey, J. A. Pinston, H. Faust, C. Foin, S. Oberstedt, and M. Rejmund, Eur. Phys. J. A 9, 191 (2000).
- [27] M. Rejmund, B. Lecornu, A. Navin, C. Schmitt, S. Damoy, O. Delaune, J. M. Enguerrand, G. Fremont, P. Gangnant, L. Gaudefroy, B. Jacquot, J. Pancin *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A **646**, 184 (2011).
- [28] A. Navin, M. Rejmund, C. Schmitt, S. Bhattacharyya, G. Lhersonneau, P. van Isacker, M. Caamaño, E. Clément, O. Delaune, F. Farget, G. de France, and B. Jacquot, Phys. Lett. B 728, 136 (2014).

- [29] A. Navin and M. Rejmund, Gamma-ray spectroscopy of neutron-rich fission fragments, in *Yearbook of Encyclopedia of Science and Technology* (McGraw-Hill, New York, 2014).
- [30] S. Akkoyun, A. Algora, B. Alikhani, F. Ameil, G. de Angelis, L. Arnold, A. Astier, A. Ataç, Y. Aubert, C. Aufranc, A. Austin, S. Aydin *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 668, 26 (2012).
- [31] M. Vandebrouck, A. Lemasson, M. Rejmund, G. Fremont, J. Pancin, A. Navin, C. Michelagnoli, J. Goupil, C. Spitaels, and B. Jacquot, Nucl. Instrum. Methods Phys. Res., Sect. A 812, 112 (2016).
- [32] Y. H. Kim, A. Lemasson, M. Rejmund, A. Navin, S. Biswas, C. Michelagnoli, I. Stefan, R. Banik, P. Bednarczyk, S. Bhattacharya, S. Bhattacharyya, E. Clément *et al.*, Eur. Phys. J. A 53, 162 (2017).
- [33] J. Simpson, F. Azaiez, G. DeFrance, J. Fouan, J. Gerl, R. Julin, W. Korten, P. Nolan, B. Nyakó, G. Sletten, and P. Walker, Act. Phys. Hung. Ser. Heavy Ion Phys. 11, 159 (2000).
- [34] T. Kibédi, T. Burrows, M. Trzhaskovskaya, P. Davidson, and C. Nestor, Nucl. Instrum. Methods Phys. Res., Sect. A 589, 202 (2008).
- [35] W. F. van Gunsteren and D. Rabenstein, Z. Phys. A: At. Nucl. (1975) 282, 55 (1977).
- [36] H. Langevin-Joliot, V. Datar, E. Gerlic, J. Van de Wiele, F. Azaiez, S. Fortier, S. Gales, J. Guillot, J. M. Maison, C. P. Massolo, G. Duhamel, and G. Perrin, Phys. Rev. C 38, 1168 (1988).
- [37] M. G. Porquet, T. Venkova, R. Lucas, A. Astier, A. Bauchet, I. Deloncle, A. Prévost, F. Azaiez, G. Barreau, A. Bogachev, N. Buforn, A. Buta *et al.*, Eur. Phys. J. A 24, 39 (2005).
- [38] G. A. Jones, S. J. Williams, P. M. Walker, Z. Podolyák, S. Zhu, M. P. Carpenter, J. J. Carroll, R. S. Chakrawarthy, P. Chowdhury, I. J. Cullen, G. D. Dracoulis, A. B. Garnsworthy *et al.*, Phys. Rev. C 77, 034311 (2008).
- [39] J. J. Ressler, J. A. Caggiano, C. J. Francy, P. N. Peplowski, J. M. Allmond, C. W. Beausang, L. A. Bernstein, D. L. Bleuel, J. T. Burke, P. Fallon, A. A. Hecht, D. V. Jordan *et al.*, Phys. Rev. C 81, 014301 (2010).
- [40] K. E. Apt and W. B. Walters, Phys. Rev. C 9, 310 (1974).
- [41] H. Huck, M. L. Pérez, and J. J. Rossi, Phys. Rev. C 26, 621 (1982).
- [42] C. A. Stone and W. B. Walters, Z. Phys. A 328, 257 (1987).
- [43] J. Genevey, J. A. Pinston, C. Foin, M. Rejmund, H. Faust, and B. Weiss, Phys. Rev. C 65, 034322 (2002).
- [44] F. Schussler, J. Blachot, J. P. Bocquet, and E. Monnand, Z. Phys. A: At. Nucl. (1975) 281, 229 (1977).
- [45] M. Hjorth-Jensen, T. T. Kuo, and E. Osnes, Phys. Rep. 261, 125 (1995).
- [46] E. Caurier, G. Martinez-Pinedo, F. Nowacki, A. Poves, J. Retamosa, and A. P. Zuker, Phys. Rev. C 59, 2033 (1999).
- [47] L. Liu, S. Y. Wang, Z. Q. Chen, C. Liu, B. Qi, D. P. Sun, S. Wang, Q. An, C. J. Xu, P. Zhang, Z. Q. Li, C. Y. Niu *et al.*, Phys. Rev. C **90**, 014313 (2014).
- [48] R. Broda, R. H. Mayer, I. G. Bearden, P. Benet, P. J. Daly, Z. W. Grabowski, M. P. Carpenter, R. V. F. Janssens, T. L. Khoo, T. Lauritsen, E. F. Moore, S. Lunardi *et al.*, Phys. Rev. Lett. 68, 1671 (1992).
- [49] R. H. Mayer, D. T. Nisius, I. G. Bearden, P. Bhattacharyya, L. Richter, M. Sferrazza, Z. W. Grabowski, P. J. Daly, R. Broda, B. Fornal, I. Ahmad, M. P. Carpenter *et al.*, Phys. Lett. B 336, 308 (1994).