Measurement of the 65Cu(*n, γ***) cross section using the Detector for Advanced Neutron Capture Experiments at LANL**

C. J. Prokop,* A. Couture, S. Jones, S. Mosby, G. Rusev, and J. Ullmann *Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA*

M. Krtička

Charles University, V Holesšovicˇckách 2, CZ-180 00 Prague 8, Czech Republic

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Improving our understanding of the origin of the elements in the observable universe as well as the nature of the environments responsible for their production has been of paramount importance to the nuclear physics community. More than half of the isotopes of these elements are created via neutron-capture processes, and thus accurate measurements of the salient underlying nuclear physics, such as neutron-capture cross sections, masses, and β-decay half-lives are crucial. Of particular importance to the synthesis of isotopes in the mass range of $A \approx 60$ to $A \approx 90$, via the weak *s* process, are the neutron-capture cross sections of ^{63,65}Cu, where large discrepancies between measurements exist. Recent measurements have addressed these discrepancies for 63 Cu [Weigand *et al.*, [Phys. Rev. C](https://doi.org/10.1103/PhysRevC.95.015808) **[95](https://doi.org/10.1103/PhysRevC.95.015808)**, [015808](https://doi.org/10.1103/PhysRevC.95.015808) [\(2017\)](https://doi.org/10.1103/PhysRevC.95.015808)], but questions still remain for 65 Cu. In this paper we report a new measurement of the ⁶⁵Cu(n, γ) cross section performed using the Detector for Advanced Neutron Capture Experiments located at the Los Alamos Neutron Science Center of Los Alamos National Laboratory. The Maxwellian-averaged cross section (MACS) for ⁶⁵Cu(*n*, γ) at $kT = 30$ keV deduced from this work is $(37.0 \pm 0.3_{stat.} \pm 3.3_{sys.})$ mb. The impact on weak *s*-process nucleosynthesis of new MACS values, calculated over the range of $kT = 5$ to 100 keV, for ⁶⁵Cu, combined with the updated MACS for ⁶³Cu [Weigand *et al.*, [Phys. Rev. C](https://doi.org/10.1103/PhysRevC.95.015808) **[95](https://doi.org/10.1103/PhysRevC.95.015808)**, [015808](https://doi.org/10.1103/PhysRevC.95.015808) [\(2017\)](https://doi.org/10.1103/PhysRevC.95.015808)] and 63Ni [Weigand *et al.*, [Phys. Rev. C](https://doi.org/10.1103/PhysRevC.92.045810) **[92](https://doi.org/10.1103/PhysRevC.92.045810)**, [045810](https://doi.org/10.1103/PhysRevC.92.045810) [\(2015\)](https://doi.org/10.1103/PhysRevC.92.045810)], were investigated. Results of this investigation show an increase of predicted nucleosynthesis yields of elements of Zn to Zr by as much as 20% .

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I. INTRODUCTION

Improving our understanding of the origin of the elements in the observable universe is of paramount importance. Most of the isotopes of the elements heavier than iron are formed by either the slow (*s*) or rapid (*r*) neutron-capture processes. While both the timescales and nature of the host environments are different, they are both characterized by the successive capture of neutrons on seed nuclei.

The *s* process occurs in more quiescent environments with lower temperatures and neutron densities, with a path along the neutron-rich edge of the valley of β stability. It can be further subdivided into weak and main components. The former is responsible for producing several nuclei with $A \approx$ 60 to $A \approx 90$ and occurs during helium-core and carbon-shell burning of massive stars, fueled by the ${}^{13}C(\alpha, n)$ ¹⁶O and ²²Ne(α , *n*)²⁵Mg reactions. The latter is thought to occur in thermally pulsing low-mass asymptotic giant branch (AGB) stars, and creates isotopes from the $56Fe$ seed up to $209Bi$ where the process terminates [\[1\]](#page-8-0). Figure [1](#page-1-0) shows the *s*-process path in the vicinity of ⁶⁵Cu.

The relatively shorter timescales and lower neutron densities of the weak *s* process increase the impact of the input nuclear physics such as neutron-capture cross sections and β -decay half-lives. In particular the neutron-capture cross sections of ⁶³,65Cu have both a large impact on the *s* -process abundances as well as significant discrepancies between existing measurements. Measurements made at ORELA in the 1970s on $63,65$ Cu [\[2\]](#page-8-0) yielded Maxwellian-averaged cross sections (MACS) values of (94 ± 10) and (41 ± 5) mb at $kT =$ 30 keV for 63 Cu and 65 Cu, respectively. A more recent activation measurement from Karlsruhe in 2008 [\[3\]](#page-8-0) obtained MACS values of (56 ± 2.2) and (29.8 ± 1.3) mb at $kT = 30$ keV for 63 Cu and 65 Cu, respectively. The reduction of the 63,65 Cu neutron-capture cross sections reduced the nucleosynthesis yields of several isotopes between $A \approx 60$ and $A \approx 90$ at the 20% level.

Recently the ⁶³Cu neutron-capture cross section was remeasured [\[4\]](#page-8-0) in a campaign via activation at the Joint Research Center (JRC) in Geel as well as by time-of-flight (TOF) at the Los Alamos Neutron Science Center (LANSCE) at Los Alamos National Laboratory (LANL) using the Detector for Advanced Neutron Capture Experiments (DANCE) [\[5\]](#page-9-0). This most recent ⁶³Cu(n, γ) measurement obtained a MACS value of (84.0 \pm 1.1_{stat.} \pm 6.7_{sys.}) mb at $kT = 30$ keV. While this value is slightly lower than what was obtained from the work of Ref. [\[2\]](#page-8-0), it is much higher than the activation measurements reported in Ref. [\[3\]](#page-8-0). The source of this discrepancy was

^{*}cprokop@lanl.gov

FIG. 1. Path of the *s* process in the vicinity of ⁶⁵Cu. Isotopes shown in black are observationally stable, isotopes shown in pink are unstable, and 65 Cu is highlighted in light blue. Blue arrows indicate neutron capture while red arrows indicate β^- decay.

determined to be primarily the influence of a 1-mm-thick natural Cu backing material not accounted for in the cross section measurements from Ref. [\[3\]](#page-8-0). The natural Cu backing absorbed neutrons and reduced the number of activated ⁶³Cu nuclei, and thus the deduced ⁶³Cu(*n*, γ) cross section. Moreover, since ⁶⁵Cu is also stable, with a ≈30% natural abundance, it is likely that a similar systematic error is also present for the ⁶⁵Cu(*n*, γ) cross section reported by Ref. [\[3\]](#page-8-0). This paper describes a new measurement of the ⁶⁵Cu(*n*, γ) cross section performed using DANCE at LANL to address these discrepancies.

II. EXPERIMENT

A. Experimental setup

DANCE is positioned on flight path 14 of the Lujan Neutron Scattering Center at LANSCE [\[6\]](#page-9-0) at a flight path length of 20.28 m. Neutrons are produced via spallation of an 800-MeV proton beam, operating at a 20-Hz repetition rate, impinged onto a pair of tungsten targets, and subsequently moderated by a room-temperature backscatter water moderator [\[7\]](#page-9-0). The resulting epithermal neutron beam ranges in energy from a few meV to a few MeV and is collimated to a 7-mm-diameter beam spot at the sample location.

DANCE [\[5\]](#page-9-0) is a 160 element close-packed BaF₂ γ -ray calorimeter with a solid angle coverage of nearly 4π . Further downstream of DANCE exists a suite of three beam monitors which utilize the ⁶Li(*n*, *t*) α , ²³⁵U(*n*, *f*), and ³He(*n*, *p*) reactions to detect neutrons. The measured yield from each beam monitor is directly proportional to the number of neutrons at the sample position.

DANCE and its associated beam monitors are read out using 16-channel CAEN VX1730 digitizers employing 14 bit 500-megasample-per-second digitizers. Each digitizer is synchronized with a common clock propagated sequentially from board to board [\[8\]](#page-9-0). All DANCE crystals and beam monitors trigger independently; however, the DANCE crystals are validated by a timing gate of fixed width starting \approx 100 μ s before the arrival of the protons on the tungsten target. The

width of this gate, typically a few milliseconds, determines the range of neutron energies recorded by the acquisition system. Data are collected continuously until a specified file size, 4 GB for the present data, is reached, at which point the run is stopped, the digitizers are reset and reprogrammed, and a new run is started. Nominal run lengths are 10 to 15 minutes.

A variety of information is recorded from DANCE and its associated beam monitors. In addition to the board and channel numbers, the leading-edge timestamp, long and short charge integrals, and partial waveforms are recorded for all channels. For each partial waveform a more precise fractional timestamp is determined offline from the location in time at which the rising edge of the detector signal crosses a threshold set by the last few samples of the partial waveform. The energy of each DANCE crystal, *ECr*, is calculated from the long integral minus the short integral to reduce the impact on linearity from overflowing of the fast component.

Based on the extracted timestamps for the DANCE crystals, a DANCE event is created by grouping all crystals identified as γ rays via pulse shape discrimination (PSD) that fired within a user-defined 5-ns coincidence window. The corresponding neutron energy, E_n , of the DANCE event is calculated from neutron TOF determined by the time difference between the first crystal of the DANCE event and the previous timing signal of the proton pulse immediately before it interacts with the tungsten spallation target. The sum of all γ -ray energies in the DANCE event is recorded as E_{Sum} and the number of crystals participating in the event is denoted as *MCr*. Beam-monitor events are treated in a similar fashion, but without coincidence requirements, as beam monitors are single, independent channels.

B. Samples

The primary sample for this experiment is a highly enriched (99.7%) 65 Cu cylinder, in metallic form, with a diameter of 4 mm and total mass of (219.2 ± 0.5) mg. Additional samples were also measured to assess backgrounds and contamination as well as normalize the neutron fluence. The ${}^{63}Cu$ sample used to characterize the $\approx 0.3\%$ ⁶³Cu contaminant was also in metallic form, enriched to 99.88% ⁶³Cu. A 4-mmdiameter 5-kÅ- thick ¹⁹⁷Au sample and a ≈100-mg ²⁰⁸Pb sample were also run for neutron fluence normalization and scattered-neutron background characterization, respectively.

C. Energy calibrations

The $BaF₂$ crystals are temperature sensitive and have been observed to drift over time. Fortunately, the intrinsic internal activity from α decay of ²²⁶Ra, a chemical homologue of Ba, inside the the $BaF₂$ crystals provides a means for a run-by-run correction. The α -decay signals are distinguished from γ rays using PSD.

Before the start of data analysis an initial quadratic energy calibration was performed for each DANCE crystal using known lines from 22 Na, 88 Y, and PuBe sources as well as strong high-energy primary transitions from ${}^{59}Co(n, \gamma)$ measured immediately after the source runs. The combined α spectra of each crystal for the source runs, with the initial calibration applied, were saved as a template. In all subsequent, noncalibration runs the uncalibrated α spectra were fit to these templates for each crystal to extract the energy calibration for that run. However, the limited energy range of the α spectra cannot adequately constrain the quadratic fit parameters so the linear and quadratic constants were fixed to their initial values, constraining the shape of the calibration, and then scaled by a single parameter left free along with the offset parameter.

D. Time offsets and flight path corrections

The relative timing of all crystals changes slightly for each run due to the synchronization of the digitizers. All crystals were aligned with one another in time on a run-by-run basis by adjusting their time offsets such that the difference between Compton scatter events in adjacent crystals was zero for each pair of crystals.

The complicated moderation process of neutrons in the spallation target-moderator assembly introduces a moderation time (\triangle TOF) for neutrons, which is E_n dependent, that must be accounted for in the analysis. The measured time of flight $(TOF_{Measured})$ is the sum of the actual time of flight (TOF_{Actual}) of the neutron and \triangle TOF. The \triangle TOF/TOF_{Actual}, for a given flight path length, as a function of E_n leaving the face of the moderator was deduced from a simulation of the targetmoderator assembly [\[9\]](#page-9-0). The results of this simulation were then used to correct $TOF_{Measured}$ to TOF_{Actual} event by event.

The global time offset for DANCE and each beam monitor along with its precise flight path length was deduced. Each instrument displays strong absorption in the E_n spectrum at 337.3 eV, 5.906 keV, 34.765 keV, and 86.183 keV from ²⁷Al and 55Mn in beamline and moderator structural components. Resonances at 4.89 and 60.1 eV in $^{197}Au(n, \gamma)$ for DANCE and at 1.143 and 2.035 eV in ²³⁵U(*n*, *f*) for the ²³⁵U monitor were also used. The global time offset and flight path length were varied simultaneously and *En* was calculated for each combination and each resonance along with the residual sum of squares (RSS) for each combination. The combination with the smallest RSS was used as the optimum global time offset and flight path length. This procedure was carried out independently for DANCE and each beam monitor.

E. Scattered-neutron background characterization

Neutrons incident on samples in DANCE have a probability of scattering. Scattered neutrons subsequently thermalize through interactions with components inside and nearby DANCE, and can capture on the Ba in the $BaF₂$ crystals creating γ -ray signatures that are similar to the neutroncapture signal from samples of interest. This scattered-neutron background was characterized using a ²⁰⁸Pb sample. The low 3.94-MeV *Q* value of ²⁰⁸Pb(*n*, γ) coupled with a relatively low neutron-capture cross section and a relatively high neutron elastic-scattering cross section makes it the ideal sample for this purpose. Fortunately, 135 Ba has a high 9.108-MeV *Q* value, which gives a clear signature of scattered-neutron background above the *Q* values of interest for all samples run during this experiment.

FIG. 2. Beam-monitor yields, Y_{BM} , divided by the relevant beammonitor reaction cross sections, σ_{BM} , for the ⁶⁵Cu data. Below 3 keV all data are from the ⁶Li monitor, between 3 and 20 keV the data are the average of the 6 Li and 235 U monitors, and above 20 keV the data are exclusively from the 235 U monitor.

In some instances the background over an isolated resonance was characterized by selecting regions either side of the resonance instead of using the 208Pb data.

For either case, the method of obtaining the background normalization factor $\alpha_{BG}(E_n)$, for scaling the background spectrum, $C_{BG}(E_n, E_{Sum})$, to the foreground plus background spectrum, $C_{\text{FG+BG}}(E_n, E_{\text{Sum}})$, is

$$
\alpha_{\rm BG}(E_n) = \frac{\int_{8.5 \text{ MeV}}^{10.5 \text{ MeV}} C_{\rm FG+BG}(E_n, E_{\rm Sum}) dE_{\rm Sum}}{\int_{8.5 \text{ MeV}}^{10.5 \text{ MeV}} C_{\rm BG}(E_n, E_{\rm Sum}) dE_{\rm Sum}}.
$$
(1)

III. NEUTRON FLUENCE CHARACTERIZATION

In the present analysis the ${}^{6}Li$ and ${}^{235}U$ beam monitors were used for neutron fluence determination and the ³He monitor was used only for a consistency check. While ideally one would use a single beam monitor over the full range of E_n , resonances in the ²³⁵U(*n*, *f*) cross section over the 1 eV to 1 keV range for the 235 U monitor and a strong resonance at \approx 240 keV in the ⁶Li(*n*, *t*) α cross section for the ⁶Li monitor limit the feasibility of using either one exclusively. The yield, i.e., number of recorded reactions at each energy, measured in the beam monitors, Y_{BM} , divided by the relevant reaction cross section, σ_{BM} , is directly proportional to the fluence of neutrons on the sample, $\Phi(E_n)$, as

$$
\Phi(E_n) = \kappa \frac{Y_{\text{BM}}(E_n)}{\sigma_{\text{BM}}(E_n)}.
$$
\n(2)

The yield of the ⁶Li monitor divided by the ⁶Li(*n*, *t*) α cross section was normalized to the yield of the 235U monitor divided by the $^{235}U(n, f)$ cross section over the range of 3 to 20 keV. Figure 2 shows the beam-monitor yields divided by the relevant beam-monitor reaction cross sections acquired during the ⁶⁵Cu(*n*, γ) measurement. Below 3 keV all data are from the 6Li monitor, between 3 and 20 keV the data are the average of the 6 Li and 235 U monitors, and above 20 keV the data are exclusively from the 235U monitor.

The normalization of the beam-monitor response, κ from Eq. (2), was deduced from a measurement of $197Au(n, \gamma)$ on the 4-mm-diameter, 5-k-thick 197 Au sample. Prior to the

experiment, the thickness of the 197 Au sample was measured using Rutherford backscattering, placing an uncertainty on the number of ¹⁹⁷Au atoms in the sample of 4%. The measured ¹⁹⁷Au(*n*, γ) yield, $Y_{Au}(E_n)$, is related to the ¹⁹⁷Au(*n*, γ) cross section, $\sigma_{Au}(E_n)$, by

$$
Y_{\text{Au}}(E_n) = \Phi(E_n) N_{\text{Au}} \sigma_{\text{Au}}(E_n). \tag{3}
$$

Substituting Eq. [\(2\)](#page-2-0) in for $\Phi(E_n)$ in Eq. (3), one obtains

$$
Y_{\text{Au}}(E_n) = \kappa \frac{Y_{\text{BM}}(E_n)}{\sigma_{\text{BM}}(E_n)} N_{\text{Au}} \sigma_{\text{Au}}(E_n)
$$
(4)

relating the $197Au(n, \gamma)$ yield to the beam-monitor yields, allowing for extraction of the normalization factor κ .

The normalization of the beam-monitor response was performed over the 4.89-eV resonance in the $^{197}Au(n, \gamma)$ cross section. All crystal multiplicities were used and no cuts were placed on E_{Sum} .

The foreground E_{Sum} shape for neutron capture on ¹⁹⁷Au, $F_{\text{Au}}(E_{\text{Sum}})$, was determined from the 197 Au(*n*, γ) data. Background E_{Sum} spectra were taken from symmetric regions in TOF closely surrounding the 4.89-eV resonance. In this case $C_{\text{FG+BG}}(E_n, E_{\text{Sum}})$ was obtained from the data encapsulated between these two background regions. The background spectra were summed to obtain $C_{BG}(E_n, E_{Sum})$ and subsequently normalized to $C_{\text{FG+BG}}(E_n, E_{\text{Sum}})$ using Eq. [\(1\)](#page-2-0). The scaled background, $\alpha_{BG}(E_n)C_{BG}(E_n, E_{Sum})$, was then subtracted from $C_{\text{FG+BG}}(E_n, E_{\text{Sum}})$ to extract $F_{\text{Au}}(E_{\text{Sum}})$.

The background component described above taken near the 4.89-eV resonance contains too much of the $197Au(n, \gamma)$ yield to serve as the background used for the extraction of the 197 Au(*n*, γ) yield. Therefore, a different background component, $C'_{BG}(E_n, E_{Sum})$, was determined in a similar manner as before from a linear combination of symmetric regions in TOF about the 4.89-eV resonance, but this time much further away from the resonance such that minimal $\left($ <1%) foreground was present. The E_{Sum} spectrum for each E_n bin from 4 to 6 eV, shown in Fig. $3(a)$, was then fit with a combination of the scaled $F_{\text{Au}}(E_{\text{Sum}})$ and $\alpha'_{\text{BG}}(E_n)C'_{\text{BG}}(E_n, E_{\text{Sum}})$. Figure 4 shows an example fit of a E_{Sum} spectrum from a single E_n bin, shown in black. The scaled $F_{Au}(E_{Sum})$ is shown in dotted blue, and the scaled background component, $\alpha'_{BG}(E_n)C'_{BG}(E_n, E_{Sum})$, is shown in dashed red.

The extracted yield as a function of E_n is represented by black squares in Fig. $3(b)$. A fit of the ENDF/B-VIII.0 197 Au(*n*, γ) cross section, adjusted for the response of the spallation target-moderator assembly, to the extracted yield is shown in red. The scale factor for the ENDF cross section to the experimentally determined yield, κN_{Au} , is 0.299 atoms per barn. To evaluate the uncertainty of κN_{Au} a bootstrap technique was employed where fifty 197 Au runs were selected at random 100 times and κN_{Au} was determined for each block of runs using the analysis techniques described in this section. The distribution of κN_{Au} was fit with a Gaussian, and a 1 σ uncertainty of 3.5% was determined. The impact on κN_{Au} from variations of the extracted foreground E_{Sum} shape due to choices of the E_n ranges selected for the various foreground and background regions was determined to be 5%.

FIG. 3. (a) E_{Sum} as a function of E_n for the ¹⁹⁷Au(*n*, γ) data. (b) Extracted yield for each E_n bin in (a) shown as black squares while a fit of the ENDF/B-VIII.0 $^{197}Au(n, \gamma)$ cross section, corrected for the response of the target-moderator assembly, to the data is shown in red.

IV. DATA ANALYSIS AND RESULTS

The analysis of ${}^{65}Cu$ proceeds following the time and energy calibrations described in Sec. [II.](#page-1-0) The raw ⁶⁵Cu(*n*, γ) data are presented in Fig. [5.](#page-4-0) E_{Sum} is on the vertical axis while E_n is on the horizontal axis. The color scale on the third axis represents the number of counts for each E_{Sum} and E_n . Crystal multiplicities of 2 through 10 are considered for this analysis. The bulk of events with $M_{Cr} = 1$ are scattered-neutron capture events inside the BaF₂ crystals, and above $M_{Cr} = 10$ there

FIG. 4. Example fit of a single E_n bin along the *x* axis of Fig. 3(a) projected onto the *y* axis. The raw data from the projection, shown in black, is a combination of foreground neutron capture, shown in dotted blue, and scattered-neutron background, shown in dashed red.

FIG. 5. Counts as a function of E_{Sum} and E_n for the ⁶⁵Cu(*n*, γ) data.

are very few events dominated by cosmic rays and pileup. A 150-keV threshold has been applied to all DANCE crystals.

The data presented in Fig. 5 contain several components that must be characterized to extract the ⁶⁵Cu(*n*, γ) cross section. The most valuable information for identifying these components in DANCE are neutron-capture *Q* values and measured E_{Sum} values. The maximum possible E_{Sum} value, barring pileup, is the sum of the neutron-capture *Q* value and E_n . When examining the data in Fig. 5 one can see several resonances in ⁶⁵Cu(*n*, γ) with E_{Sum} values peaking just below the 7.065-MeV *Q* value. There is also evidence of neutron capture on the predominant contaminant, ⁶³Cu. These events have E_{Sum} values peaking just below the 7.916-MeV $^{63}Cu(n, \gamma)$ *Q* value, and are readily observed around $E_n \approx$ 580 eV, the energy of the strongest ${}^{63}Cu(n, \gamma)$ resonance. There are strong horizontal bands around E_{Sum} of 4.7 and 9.1 MeV from the capture of thermalized, scattered neutrons on ¹³⁸Ba and ¹³⁵Ba, respectively. Contributions from the other stable Ba isotopes are also present.

A. Dead-time and pileup corrections

When a crystal of DANCE triggers a channel in the data acquisition system, the charge integral of the triggered channel is recorded for 1 μ s. The instantaneous event rate at short TOF as well as on some resonances is often high with respect to the relatively long $1-\mu s$ charge integration window. During the charge integration period a channel cannot retrigger, but the charge integral will include a fraction of any subsequent radiation that hit that crystal within 1 μ s of the first event. This is referred to as crystal pileup and results in an increase in the measured crystal energy of one or more crystals, and thus E_{Sum} , of the first event. This also gives rise to the dead time in DANCE. Since a crystal recording charge hit with subsequent radiation is unable to trigger, the observed M_{Cr} as well as the recorded E_{Sum} of the second event is reduced. A smaller effect from recording two events within the 5-ns event-building window is also observed and is referred to

as event pileup. Event- and crystal-pileup effects manifest themselves in Fig. 5 as vertical bands on strong resonances that extend in E_{Sum} beyond the neutron-capture Q value.

The characterizations of these effects and methods to correct the data for them is beyond the scope of this paper, and they are described in detail in Ref. [\[10\]](#page-9-0). The basic concept behind these methods is to use the measured event rates for all recorded multiplicities, the average number of crystals recording charge integrals at any given time, and the known event and charge integration lengths to deduce the probability of event pileup, dead time, and occurrence of crystal pileup, as well as their impacts on the recorded data. Those methods applied to the present data yield excellent results over the entire energy range relevant for calculating the Maxwellianaveraged cross section (MACS) of ⁶⁵Cu. A slight deficiency in the crystal pileup technique for the first resonance in both the $63,65$ Cu data, where instantaneous count rates vary by an order of magnitude, is still being investigated, but affects the extracted MACS at a less than 0.2% level for all energies reported in this paper.

B. Contaminant characterization

The small amount of ${}^{63}Cu$ (0.3%) is clearly visible in Fig. 5, and thus its contribution must be subtracted. Data collected on the ${}^{63}Cu$, ${}^{65}Cu$, and ${}^{208}Pb$ samples in the region around $E_n = 580$ eV, the location of the strongest resonance in ${}^{63}Cu(n, \gamma)$, was used. The scattered-neutron background was approximated by the 208 Pb data scaled using Eq. [\(1\)](#page-2-0) and subtracted from the 63 Cu and 65 Cu data. Then, the ratio of the integral of counts (${}^{65}Cu/{}^{63}Cu$) in the region between 7.5 and 8.5 MeV in E_{Sum} , which brackets the 7.916-MeV ⁶³Cu(*n*, γ) *Q* value (which is above the 7.065-MeV ⁶⁵Cu(*n*, γ) *Q* value and below the 9.108-MeV $^{135}Ba(n, \gamma)Q$ value,) is the scaling factor for the 63 Cu data. The 63 Cu data was scaled and subtracted from the ${}^{65}Cu$ data to remove the contribution of ⁶³Cu(*n*, γ) across all E_n simultaneously. The ⁶³Cu(*n*, γ) subtracted ⁶⁵Cu(*n*, γ) data corrected for event pileup, dead time, and crystal pileup are shown in Fig. [6.](#page-5-0)

FIG. 6. Counts as a function of E_{Sum} and E_n for the ⁶⁵Cu(*n*, γ) data following the corrections for event pileup, dead time, and crystal pileup. The contribution from ⁶³Cu(*n*, γ) from the ⁶³Cu contaminant has also been subtracted.

Smaller contributions from unknown contaminants at \approx 60 eV and \approx 1.2 keV are also present, but have a negligible effect on the MACS values presented herein.

C. Energy-differential cross section

For each E_n bin of the ⁶⁵Cu(*n*, γ) data in Fig. 6 a background component, $C_{\text{208Pb}}(E_n, E_{\text{Sum}})$, was taken from the ²⁰⁸Pb data, and a scaling factor, $\alpha_{208p_b}(E_n)$, was determined using Eq. [\(1\)](#page-2-0). Figure 7 presents a sample fit where the ${}^{65}Cu$ data is shown in black and the scattered-neutron background, obtained from the 208 Pb data and scaled using Eq. [\(1\)](#page-2-0), is shown in dashed red. The ⁶⁵Cu(*n*, γ) yield, $Y_{65}C_{10}(E_n)$, was determined using

$$
Y_{65_{\text{Cu}}}(E_n) = \int_{5.5 \text{ MeV}}^{7.5 \text{ MeV}} [C_{65_{\text{Cu}}}(E_n, E_{\text{Sum}}) -\alpha_{208\text{pb}}(E_n)C_{208\text{pb}}(E_n, E_{\text{Sum}})]dE_{\text{Sum}}.
$$
 (5)

FIG. 7. Demonstration of background characterization for a single E_n bin of the ⁶⁵Cu data. The ⁶⁵Cu data are shown in black, and the scattered-neutron background, obtained from the ²⁰⁸Pb data and scaled using Eq. [\(1\)](#page-2-0), is shown in dashed red.

The ⁶⁵Cu(*n*, γ) yield was then converted to the ⁶⁵Cu(*n*, γ) cross section using

$$
\sigma_{^{65}\text{Cu}}(E_n) = \frac{Y_{^{65}\text{Cu}}(E_n)}{\epsilon_{^{65}\text{Cu}}\kappa N_{^{65}\text{Cu}}}\frac{\sigma_{\text{BM}}(E_n)}{Y_{\text{BM}}(E_n)},\tag{6}
$$

where κ is the cross-section normalization factor determined in Sec. [III](#page-2-0) and ϵ_{65} is the DANCE cascade efficiency for ${}^{65}Cu(n, \gamma)$.

The value of ϵ_{65} was determined from DICEBOX [\[11\]](#page-9-0) coupled with GEANT4 [\[12\]](#page-9-0) simulations. Prior to this effort the GEANT4 model of DANCE [\[13\]](#page-9-0) was validated using a variety of radioactive check sources. Simultaneous agreement between experimental and simulated crystal multiplicities, crystal energies, and total efficiencies better than 0.5% absolute for all sources was achieved.

DICEBOX simulations were performed for all possible spins and parities, J^{π} , of capture states for both *s*-wave and *p*wave neutron capture. A back-shifted Fermi gas model was chosen for the level density with a spin cutoff parameter from Ref. [\[14\]](#page-9-0) and level density parameters from Ref. [\[15\]](#page-9-0). A standard Lorenziation shape was chosen for the *E*1 photon strength function with parameters taken from Ref. [\[16\]](#page-9-0).

DICEBOX was used to generate 800 simulations, each with 100 000 capture events, for each possible J^{π} from *s*- and *p*wave neutron capture. The γ -ray cascades from these capture events were then processed through the GEANT4 model of DANCE. The resulting γ -ray energy and multiplicity spectra from these simulations were compared with the experimental data to verify agreement at a level reasonable for estimating the cascade detection efficiency. The same 150-keV *ECr* threshold and $2 \leq M_{Cr} \leq 10$ cuts applied to the data were applied to the simulation. The wide range of M_{Cr} accepted in the analysis made it possible to find an E_{Sum} range, 5.5 MeV to 7.5 in this case, where all extracted cascade efficiency values were within 5% of one another. Table [I](#page-6-0) presents a summary of $\epsilon_{65\text{Cu}}$ values obtained from these simulations. The average value of 0.45 ± 0.02 was used for ϵ_{65} in the analysis.

TABLE I. Values of ϵ_{65} obtained from DICEBOX cascades propagated through the DANCE GEANT4 model for *s*-wave and *p*-wave neutron capture. The ground state spin and parity of ${}^{65}Cu$ is 3/2⁻.

The extracted ⁶⁵Cu(*n*, γ) energy-differential cross section is shown as black squares in Fig. 8. A change between ENDF/B-VII.1 and ENDF/B-VIII.0 introduced a resonance at $E_n \approx 580$ eV that is not supported by the present measurement. However, since this energy corresponds to the location of the largest resonance in ${}^{63}Cu$, it suggests the possibility that results influencing the updated evaluation could be affected by ⁶³Cu contamination.

D. Uncertainties

There are several statistical and systematic uncertainties that must be accounted for in the analysis.

DANCE relies on the neutron TOF to deduce E_n , and thus any uncertainty in TOF must be propagated as uncertainty in *En*. There are three primary sources of TOF uncertainty. At high *En*, the largest of these is the pulse width of the proton beam responsible for producing spallation neutrons. The time profile of the beam is nominally triangular with a FWHM of 120 ns. The second source of TOF uncertainty is the modera-

TABLE II. Systematic uncertainties in the analysis. Quantities in normal-faced text are from the neutron fluence normalization and were added in quadrature to obtain the "neutron fluence normalization" uncertainty. Items in bold-faced text were added in quadrature to obtain the final systematic uncertainty.

tion time distribution of neutrons and is *En* dependent. The last TOF uncertainty comes from the response of DANCE itself. For all γ -ray energies of interest the coincidence resolving time is better than 1.5 ns.

The DANCE capture data for all measured samples for every E_n bin has an associated statistical error. The uncertainty from subtraction of the ⁶³Cu contaminant and the scatteredneutron background from the ⁶⁵Cu data was propagated into the differential cross section for each *En* bin.

Like the DANCE capture data, beam-monitor yields also have a statistical error for each E_n bin and there is an uncertainty in the relevant reaction cross sections used to obtain Y_{BM}/σ_{BM} . There is also an uncertainty from the normalization of Y_{6Li}/σ_{6Li} to Y_{235} _U/ σ_{235} _U. These uncertainties were also propagated to the differential cross section.

In addition to the uncertainties mentioned above there are a variety of systematic uncertainties provided in Table II. Items

FIG. 8. Energy differential ⁶⁵Cu(*n*, γ) cross section shown in black squares. The ENDF/B-VIII.0 ⁶⁵Cu(*n*, γ) cross section, corrected for the response of the target-moderator assembly, is shown in red.

TABLE III. Comparison of Maxwellian-averaged cross sections determined in the present work with KADoNiS v0.3.

$k_B T$ (keV)	MACS (mb) KAD _o N _i S _{v0.3}	MACS (mb) This work
5	111	132.6 ± 0.6 _{stat} ± 12 _{sys}
10	57.5	78.9 \pm 0.4 _{stat} \pm 7.0 _{sys}
15	42.2	58.2 \pm 0.4 _{stat} \pm 5.2 _{sys}
20	35.6	47.7 ± 0.4 _{stat} ± 4.2 _{sys}
25	32.0	41.3 ± 0.4 _{stat} ± 3.7 _{sys}
30	29.8 ± 1.3	37.0 ± 0.3 _{stat} ± 3.3 _{sys}
40	26.9	$31.5 \pm 0.3_{stat} \pm 2.8_{sys}$
50	24.0	28.0 ± 0.3 _{stat} ± 2.5 _{sys}
60	22.5	25.6 ± 0.3 _{stat} ± 2.3 _{sys}
80	19.6	22.0 ± 0.3 _{stat} ± 2.0 _{sys}
100	18.2	$19.7 \pm 0.2_{stat} \pm 1.7_{sys}$

in Table [II](#page-6-0) with normal-faced text originate from the neutron fluence normalization and were added in quadrature to obtain the neutron fluence normalization" uncertainty. Items in Table [II](#page-6-0) with bold-faced text were added in quadrature to obtain the final systematic uncertainty.

E. Maxwellian-averaged cross section

The measured differential cross section shown in Fig. [8](#page-6-0) was converted to a Maxwellian-averaged cross section (MACS) using

$$
\sigma^{\text{MACS}}(kT) = \frac{2}{\sqrt{\pi}} \left(\frac{\mu}{kT}\right)^2 \sum_{E_n=10 \text{ eV}}^{1 \text{ MeV}} \sigma(E_n) E_n e^{\frac{E_n}{kT}} \delta(E_n), \quad (7)
$$

where μ is the reduced mass and $\delta(E_n)$ is the width of the bin centered on *En*.

The resulting MACS for ⁶⁵Cu(*n*, γ) for energies between 5 and 100 keV are presented in Table [III.](#page-6-0) The *En* range of 10 eV to 1 MeV in for the summation in Eq. (7) results in >99.8% of the Maxwell-Boltzmann distribution included in the calculation of the MACS, across all *kT* , and thus any associated uncertainty from truncation of the E_n range is negligible.

FIG. 9. The final composition of the models at the presupernova stage for 15, 20, and 25 M_{\odot} massive star models from [\[18,19\]](#page-9-0) computed using the KEPLER code $[20-22]$. Unstable isotopes to have been allowed to decay for 10^{16} s. The left panels show the composition relative to the solar abundance distribution while the right panels show the relative difference when the three updated (n, γ) cross sections are used.

V. ASTROPHYSICAL IMPACT

Recent experiments have improved our knowledge of the (n, γ) cross sections for ⁶³Ni [\[17\]](#page-9-0), ⁶³Cu [4], and ⁶⁵Cu (this work), all of which impact the abundances of $63,65$ Cu. The full impact of updates to these (n, y) cross sections was investigated for the complete nucleoynthesis of 15, 20, and 25 M_{\odot} massive star models from [\[18,19\]](#page-9-0) computed using the KEPLER code $[20-22]$. The method for the nucleosynthesis calculations was the following. Stellar evolution models were evolved from the main sequence through the presupernova stage. The temperature, density and diffusion coefficient¹ from stellar evolution models were saved every computational time step. We then used the NUGRID post-processing code MPPNP [\[19,23,24\]](#page-9-0), which solves the reaction equations on each grid cell and subsequently performs a diffusion solution using operator splitting on the whole domain for the mixing. This process was repeated every time step.

The reaction network used for the post-processing consisted of 1092 isotopes and approximately 14 000 reactions. A detailed description of where we take the reaction rates from can be found in Refs. [\[19,25,26\]](#page-9-0) and references therein. The time integration was performed using a fully implicit backward-Euler method with a Newton-Raphson scheme. At temperatures above 6 GK the nuclear statistical equilibrium (NSE) approximation was used to solve for the composition, which assumes that the strong reaction rates are in equilibrium. The weak reaction rates are then coupled to the NSE state using a fourth- or fifth-order Runge-Kutta type Cash-Karp time integrator [\[27\]](#page-9-0).

The final composition of the models at the presupernova stage is shown in Fig. [9,](#page-7-0) where we have allowed the unstable isotopes to decay for 10^{16} s. The left panels show the composition relative to the solar abundance distribution and the right panels show the relative difference when the three updated (n, γ) cross sections are used. We only consider the composition of the portion of the star that will be ejected in the supernova explosion, i.e., we neglect the innermost region of the core that will become the compact remnant (neutron star or black hole). We have also neglected the impact of any shock heating during the supernova explosion on the composition. This tends to destroy the *s*-process products in the carbon shell. Some *s*-process isotopes such as ⁶⁰Fe can also be produced in the carbon and helium shells during the explosion, but our tests indicate that the majority of the isotopes in Fig. [9](#page-7-0) are not significantly produced in the carbon or helium shells during the explosion.

Figure [9](#page-7-0) shows that there is approximately 20% less ⁶³Cu and 10% less 65 Cu produced when the new cross sections are adopted, and an overall increase in the weak *s*-process elements from Zn to Zr up to 20%, peaking around Kr.

VI. CONCLUSION

The ⁶⁵Cu(n, γ) cross section was measured with DANCE located at LANSCE of LANL. MACS values extracted from the data are significantly higher than the most recent measurements [3] but are in agreement with those extracted from prior measurements [2]. The impacts of this new ⁶⁵Cu(*n*, γ) cross section coupled with updated ⁶³Cu(*n*, γ) [4] and ⁶³Ni(*n*, γ) [\[17\]](#page-9-0) cross sections were investigated for the complete nucleosynthesis of 15, 20, and 25 M_{\odot} massive star models from [\[18\]](#page-9-0) and [\[19\]](#page-9-0) computed using the KEPLER code [\[20–22\]](#page-9-0). Decrease in abundances for $63,65$ Cu by 20% and 10%, respectively, were observed along with an overall increase of 20% in nucleosynthesis yield of elements from Zn to Zr. In particular these new results enhance the production of *s*-only isotopes 70Ge, 76Se, and ⁸⁰,82Kr. This impacts the *s*-process nucleosynthesis calibration for the weak component as well as abundances that must be accounted for by the proposed lighter element primary process (LEPP) [\[28\]](#page-9-0) or other novel nucleosynthesis mechanisms.

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