Deep excursion beyond the proton dripline. I. Argon and chlorine isotope chains

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The proton-unbound argon and chlorine isotopes have been studied by measuring trajectories of their decay-in-flight products by using a tracking technique with microstrip detectors. The proton (1p) and two-proton (2p) emission processes have been detected in the measured angular correlations "heavy-fragment"+p and "heavy-fragment"+p + p, respectively. The ground states of the previously unknown isotopes 30 Cl and 28 Cl have been observed for the first time, providing the 1p-separation energies S_p of -0.48(2) and -1.60(8), MeV, respectively. The relevant systematics of 1p- and 2p-separation energies have been studied theoretically in the core + p and core + p + p cluster models. The first-time observed excited states of 31 Ar allow one to infer the 2p-separation energy S_{2p} of 6(34) keV for its ground state. The first-time observed state in 29 Ar with $S_{2p} = -5.50(18)$ MeV can be identified as either a ground state or an excited state according to different systematics.

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I. INTRODUCTION

The location of the driplines—the borderlines separating particle-stable and particle-unstable isotopes—is one of the

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fundamental questions of nuclear science. The unbound states with small decay energy can have lifetimes which are long enough to be treated as quasistationary states. Thus they may be considered as stationary states in many theoretical applications. This naturally leads us to the following question: what are the *limits of nuclear-structure existence?* In other words, how far beyond the driplines do the nuclear-structure

phenomena fade and are completely replaced by the continuum dynamics? This question represents a motivation for studies of nuclear systems far beyond the driplines.

The proton and neutron driplines have been accessed for nuclides in broad ranges of Z (number of protons) and N (number of neutrons) of the nuclear chart. However, even in these regions the information about the nearest to the dripline unbound isotopes is scarce and often missing. Thus the fundamental question about the limits of the nuclear-structure existence remains poorly investigated. For example, if we consider the proton dripline within $Z \leq 20$ (p- and sd-shell nuclei), the most extensively investigated case in that region is the fluoride isotope chain. Here our knowledge extends three mass units beyond the proton dripline: the $^{15}\mathrm{F}$ and $^{16}\mathrm{F}$ nuclides are well studied, and considerable spectroscopic information is available now for $^{14}\mathrm{F}$ [1] in addition.

This paper continues our analysis of the data on reactions with a relativistic 31 Ar beam populating particle-unstable states [2–4]. Reference [2] was focused on 30 Ar and 29 Cl isotopes which were reported for the first time. It was also found that the decay mechanism of 30 Ar is likely to belong to a transition region between true 2p-decay and sequential 2p-decay mechanisms. Such a "transition regime" exhibits strong sensitivity of observed kinematic variables to the values of parameters defining the decay mechanism: 2p-decay energy E_T , ground-state (g.s.) resonance energy in the core +p subsystem E_r , and its width Γ_r . The practical implementations of this fact, including the opportunity of a precise determination of Γ_r from the 2p correlation data, were recently elaborated in Ref. [3]. In Ref. [4] a detailed consideration of the data from Ref. [2] was given.

In the present work we report on the by-product data of the same experiment which resulted in Refs. [2–4], which include observation of 28 Cl and 30 Cl ground states and several (presumably excited) states in 29 Ar and 31 Ar. To clarify the situation with the observed states, we have performed systematic studies of separation energies in the chlorine and argon isotope chains. The depth of the performed "excursion beyond the proton dripline" in the argon and chlorine isotope chains is similar now in extent to that for the fluorine isotope chain, the best-studied case in the whole $Z \leq 20$ nuclei region.

II. EXPERIMENT

In the experiment, described in detail in Refs. [2,4], the 31 Ar beam was obtained by the fragmentation of a primary 885 AMeV 36 Ar beam at the SIS-FRS facility at GSI (Germany). The prime objective of the experiment was study of 2p decays of 30 Ar isotopes. The scheme of the measurements is shown in Fig. 1(a). We briefly repeat the general description of the experiment and the detector performance given in Ref. [4] in detail.

The GSI fragment separator (FRS) was operated with an ion-optical setting in a separator-spectrometer mode, when the first half of the FRS was set for separation and focusing of the radioactive beams on a secondary target in the middle of the FRS, and the second half of the FRS was set for detection of heavy-ion decay products. The 620 AMeV 31 Ar ions with the intensity of 50 ions s $^{-1}$ were transported by the first half

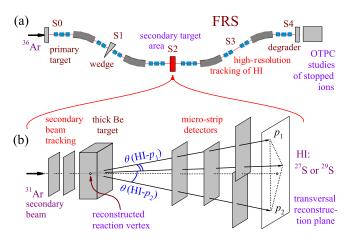


FIG. 1. Sketch of the experiment at the FRS fragment separator. (a) General layout (see details in Ref. [4]). Primary 36 Ar beam hits a target at S0, and a secondary beam of 31 Ar is selected and focused on the middle focal plane S2 by using a wedge degrader at S1. The nuclei of interest, 31 Ar* and 29 Ar, are produced in the secondary target at S2 in in-elastic scattering and two-neutron knockout reactions. The heavy-ion decay products 29,27 S are identified by their energy loss and time of flight as well as their magnetic rigidity by using the standard beam detectors at S2 and S4. At S4, the studies of stopped ions can be performed by using an optical time projection chamber (OTPC). (b) The detector setup downstream of the secondary target at S2, where the trajectories of incoming 31 Ar ions, the decay products 27,29 S, and the protons (i.e., p_1 and p_2) are measured.

of the FRS to bombard a 9Be secondary target located at the middle focal plane S2. At the first focal plane S1 of the FRS, an aluminum wedge degrader was installed to achieve an achromatic focusing of ³¹Ar at the secondary target. In the previously reported data [4] the ³⁰Ar nuclei were produced via one-neutron (-1n) knockout from the 31 Ar ions. The decay products of unbound 30Ar were tracked by a double-sided silicon microstrip detector array placed just downstream of the secondary target [see Fig. 1(b)]. The projectilelike particles, outgoing from the secondary target, were analyzed by the second half of the FRS, which was operated as a magnetic spectrometer. The magnet settings between the S2 and S4 focal planes were tuned for the transmission of the targeted heavy-ion (HI) fragments (e.g., ²⁸S) down to S4, the last focal plane. In addition to ³⁰Ar, the studies of decay properties of the stopped ³¹Ar ions were performed by using the optical time projection chamber (OTPC) detector at S4 [5].

A double-sided silicon micro-strip detector (DSSD) array consisting of four large-area DSSDs [6] was employed to measure hit coordinates of the two protons and the recoil heavy ions, resulting from the in-flight decays of the studied 2p precursors. The high-precision position measurement by DSSDs allow for reconstruction of all fragment trajectories, which let us to derive the decay vertex together with an angular HI-p and HI-p-p correlations. For example, the trajectories of measured 28 S + p + p coincidences were a basis for the analysis and the concluded spectroscopic information on 30 Ar [4].

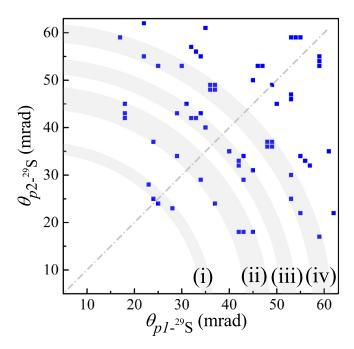


FIG. 2. Angular correlations $\theta_{p_1^{-29}\text{S}}$ - $\theta_{p_2^{-29}\text{S}}$ (in mrad) produced from the measured $^{29}\text{S}+p+p$ coincidence indicating 2p decays of ^{31}Ar excited states. The shaded arcs labeled by the lowercase Roman numerals point to four selected areas where the 2p-decay events have the same decay energies. The data symmetry respective proton permutation is illustrated by the 45° -tilted diagonal dash-dotted line.

However, a number of by-product results were obtained in a similar way from the data recorded in the same experiment. Namely, excited states of ³¹Ar were populated by various inelastic mechanisms, and the ²⁹Ar spectrum was populated in a two-neutron (-2n) knockout reaction. The unbound ³¹Ar and ²⁹Ar states were detected in triple ²⁹S + p + p and ${}^{27}S + p + p$ coincidences, respectively (see the respective angular correlation plots in Figs. 2 and 3). The relative angles there and everywhere below are presented in milliradian units (mrad). Also the states of ²⁸Cl and ³⁰Cl can be populated both in the fragmentation of ³¹Ar and as the result of proton emission from the corresponding ^{31,29}Ar isotopes. These mechanisms have lower cross sections, and the obtained results have less statistics (see the respective angular p-HI correlation plots in Figs. 9 and 6). Despite poor statistics with few events registered, we have obtained several nuclear-structure conclusions from the experimental data.

A. How nuclear-structure information can be obtained from proton-ion angular correlations

Before the data analysis presentation, we remind the reader, how nuclear-structure information concerning the nuclei involved in a 1p or 2p decay can be obtained by measuring only the trajectories of the decay products, without measuring their kinetic energies. This approach has been successfully tested in analyses of 1p and 2p decays of the known states in 19 Na and 16 Ne and has been described in detail in Ref. [7].

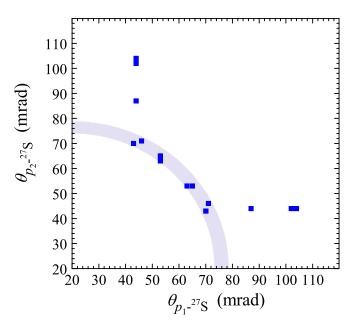


FIG. 3. Angular correlations $\theta_{p_1-2^7S}$ - $\theta_{p_2-2^7S}$ (in mrad) produced from the measured $^{27}S+p+p$ coincidence. The shaded arc where the 2p-decay events have the same decay energies indicates an ^{29}Ar state.

For the discussion of 2p decays given below, let us consider three different mechanisms. These cases are illustrated in Fig. 4. The upper panels schematically show the nuclear states involved in 2p decay of the nucleus with mass number A, and the lower panels show the corresponding momentum correlations $k_{p_1\text{-HI}}$ - $k_{p_2\text{-HI}}$, where HI corresponds to the A-2 nucleus. In the first case, Fig. 4(a), of prompt 2p decay, sequential 2p emission should be energetically forbidden. Because both emitted protons should share the 2p-decay

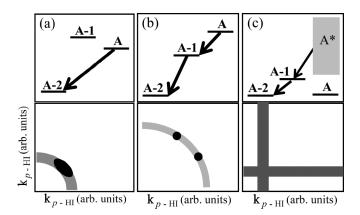


FIG. 4. Sketches of decay schemes expected for three simple mechanisms of 2p decay from a 2p- precursor with mass number A to a daughter nucleus with A-2 (illustrated in the upper panels). The respective cartoons of transverse momentum correlations $k_{p_1\text{-HI}}$ - $k_{p_2\text{-HI}}$ are shown in the lower panels: (a) prompt or direct 2p emission (three-body decay), (b) sequential emission of protons via a narrow intermediate state in nucleus A-1, and (c) deexcitation of broad continuum states in the nucleus A to a single low-lying resonance in the intermediate nucleus with A-1.

energy Q_{2p} , their energy spectra are broad and centered around the value of $Q_{2p}/2$; consequently, the 2p momentum-correlation plot should have the shape of an arc, with a radius corresponding to the Q_{2p} value and with most of the counts lying in the peak indicated by the dark spot in the lower panel of Fig. 4(a). Note that all the momentum-correlation plots in Fig. 4 are symmetric with the respect to the 45° line because the protons p_1 and p_2 are indistinguishable.

The second case, Fig. 4(b), represents the sequential emission of two protons through a narrow resonance in the intermediate nucleus with A-1. The proton energies are fixed here, and the $k_{p_1\text{-HI}}$ - $k_{p_2\text{-HI}}$ correlation plot should yield double peaks as indicated by the black dots in the lower panel of Fig. 4(b).

The third 2p-decay mechanism is 2p emission from several broad continuum parent states via a low-lying state in A-1 [see Fig. 4(c)]. This mechanism should reveal a peak in the p-HI energy with the corresponding broad distribution along the narrow "slice" as shown in the lower part of Fig. 4(c).

In the present method, we measure only total HI momentum and relative p-HI angles in the transverse direction. We register trajectories of all decay products directly downstream from the secondary-reaction target. Figure 5(b) shows the kinematics plot for the simple case of isotropic and monoenergetic single-proton emission from a high-energy heavy ion. Figure 5(c) shows the corresponding distribution of laboratory p-HI opening angles, θ_{p-HI} . The angular spectrum exhibits a sharp peak corresponding to the proton emitted almost orthogonal to the HI momentum vector. Thus the maximum value of $\theta_{p\text{-HI}}$ is directly related to the decay energy Q_p of the emitted proton. In the same way, the $k_{p_1\text{-HI}}$ - $k_{p_2\text{-HI}}$ momentum correlations for 2p decays (Fig. 5) can be replaced by the corresponding $\theta_{p_1\text{-HI}}$ - $\theta_{p_2\text{-HI}}$ correlations. If the initial and final states of p emission are narrow, the width of a peak in the angular distribution is governed mostly by the angular straggling of the proton in the secondary-reaction target. If those states are broad, the width results from a convolution of the state's width with the proton's angular straggling.

The cases sketched in Figs. 4 and 5 represent ideal cases. In reality, several proton branches may be present, representing more than one of the cases, shown schematically in Fig. 5(a), and leading to a complicated spectra with several peaks. One can, however, clean up the spectra and enhance, e.g., transitions with the small- Q_{2p} values by gating on the small angles of $\theta_{p_1\text{-HI}}$ and plotting the spectrum of $\theta_{p_2\text{-HI}}$ under this condition.

Another tool of data analysis is a kinematic variable,

$$\rho_{\theta} = \sqrt{\theta_{p_1\text{-HI}}^2 + \theta_{p_2\text{-HI}}^2},$$

describing three-body HI + p + p angular correlations. Because ρ_{θ} is related to the energy sum of both emitted protons and, therefore, to the Q_{2p} of the parent state by the relation $Q_{2p} \sim \rho_{\theta}^2$ [8], one can obtain an indication of the parent state and its 2p-decay energy by studying the distribution of ρ_{θ} . In a case of the decay from the same state, two protons share Q_{2p} , and such events should be located along a root-mean-square arc in an angular correlation plot, $\theta_{p_1\text{-HI}}$ - $\theta_{p_2\text{-HI}}$. By gating on a

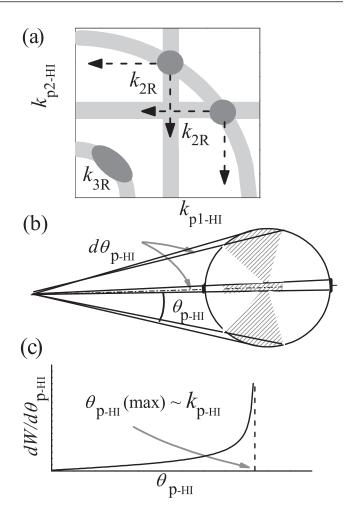


FIG. 5. (a) Cartoons of transverse momentum correlations $k_{p_1\text{-HI}}$ - $k_{p_2\text{-HI}}$ for a case of two precursor states with prompt and sequential 2p-decay mechanisms. (b) Kinematics of isotropic monoenergetic proton emission from a high-energy heavy ion, HI. (c) The corresponding angular p-HI distribution exhibiting the peak, corresponding to the Q value of the 1p decay.

particular ρ_{θ} arc, the decay events from a certain 2p precursor can be selected. The ρ_{θ} distributions are very useful in the analysis of 2p-decay data because they produce the spectra with less peaks and allow gating on a specific excitation-energy region.

In all cases, detailed Monte Carlo simulations are required to interpret the angular spectra quantitatively by taking into account the corresponding response of the experimental setup. For example, the angular correlation for fixed energy decay must first be calculated. This predicted angular correlation is then compared to the measured one. The resonance energy is obtained by the best fit where the probability that the two distributions are identical has maximum value. In the same way, limits for the width of a resonance can be obtained.

The above-described analysis procedure, where the states observed in a 2p precursor were investigated by comparing the measured angular θ and ρ_{θ} correlations with the Monte Carlo (MC) simulations of the respective detector response, has been published in Refs. [7,8]. We follow this procedure

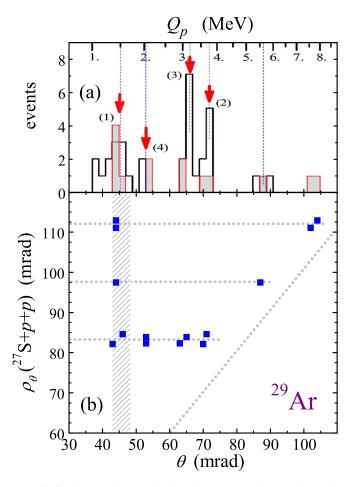


FIG. 6. The angular correlation plot θ - ρ_{θ} (angles are in mrad) for 29 Ar decay via the 27 S + p + p channel is shown in panel (b). The hatched area highlights events from the decay of a 27 S + p resonance assigned as the 28 Cl ground state. The dotted lines guide the eye for the regions corresponding to assumed 29 Ar states. Panel (a) shows the angular correlations $\theta_{p-^{27}\text{S}}$ (shaded histogram) obtained as a projection on the θ axis from the 27 S + p + p channel of panel (b). The $\theta_{p-^{27}\text{S}}$ "inclusive" angular correlations obtained from the measured p- 27 S coincident events are shown by the black hollow histogram. The arrows labeled (1)–(4) highlight the events inspected for the possible 28 Cl resonance states. The upper axis shows the corresponding 1p-decay energies Q_p . The 45° -tilted dotted line in panel (b) shows the kinematical limit.

in the present work, and the applied detector calibrations are taken from the previous ³⁰Ar analysis of the same experiment [4].

B. The data analysis: Unknown states in ²⁹Ar and ²⁸Cl

We begin from the analysis of the relatively simple case of the measured $^{27}{\rm S}+p+p$ correlations presented by the $\theta_{p_1-^{27}{\rm S}}$ - $\theta_{p_2-^{27}{\rm S}}$ and θ - ρ_{θ} plots in Figs. 3 and 6(b), respectively. These $^{29}{\rm Ar}$ -related correlations comprise just seven $^{2}{\rm P}$ -decay events, each being measured in triple $^{27}{\rm S}+p+p$ coincidence. Each detected event provides two $\theta_{p-^{27}{\rm S}}$ values and one ρ_{θ} value. Most of them are very well focused around the locations at $\theta=44$ mrad or $\rho_{\theta}=84$ mrad. These values

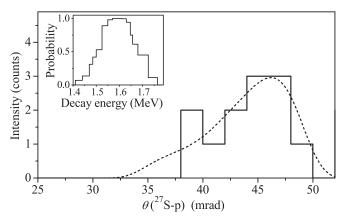


FIG. 7. Best fit of peak (1) of the θ_{p-27} s "inclusive" angular correlations from Fig. 6(b) (histogram) by simulations of the setup response to in-flight decays of ²⁸Cl with the 1*p*-decay energy of 1.60 MeV (dashed curve). The inset shows the probability that the simulated distribution matches the data as a function of the 1*p*-decay energy.

correspond to the 1p decay of the 28 Cl state with E_r of about 1.6 MeV and to the 2p decay of the 29 Ar state with Q_{2p} of about 5.5 MeV. A cross-check of this conclusion is illustrated in Fig. 6(a) where the angular correlations $\theta_{p-^{27}S}$ projected from the 27 S + p + p correlation plot [in Fig. 6(b)] are compared with the "inclusive" $\theta_{p-^{27}S}$ distribution obtained from the measured $p-^{27}$ S double-coincidence events. One may see that the "inclusive" spectrum consists of relatively enhanced peaks [peaks (1)–(3)]. Peaks (1) and (2) have the best fits at the 1p-decay energies E_r of 1.60(8) and 3.9(1) MeV, respectively. They have been assigned as the first- and second-emitted protons from the 5.5-MeV state in 29 Ar, and their sum decay energy gives the total 2p-decay energy of 5.50(18) MeV.

The data-fitting procedure is illustrated using the example of peak (1) from Fig. 6(a) at $\theta = 44$ mrad in the p^{-27} S correlation in Fig. 7. This is the same procedure described in detail in Refs. [4,7]. The best-fit simulations obtained for the in-flight decay of ²⁸Cl with the 1 p-decay energy of 1.60 MeV describe the data quantitatively, and the figure inset shows that the probability of the data matching simulations is about 1. The full width at half maximum of the probability distribution provides the evaluation of the E_r uncertainty.

There are two additional events in the decay pattern of the 5.5-MeV state in Fig. 6(b) corresponding to the inclusive peaks [peaks (3) and (4)] in Fig. 6(a). Because inclusive peak (3) is much enhanced, we may speculate that it may be evidence of the second state in 28 Cl, which is also fed by the other unspecified reaction channels, illustrated in Fig. 4(c). The best-fit 1*p*-decay energy of peak (3) is 3.20(6) MeV.

In addition, there are indications of 27 S + p + p correlations at ρ_{θ} of 97 and 112 mrad, which may correspond to the 2p decays of 29 Ar with Q_{2p} values of about 7.2 and 9.5 MeV, respectively. Both of the indicated states have the second-emitted proton energy of 1.6 MeV, which corresponds to the lowest assigned state in 28 Cl.

The derived decay scheme and levels of ²⁹Ar and ²⁸Cl are shown in Fig. 8.

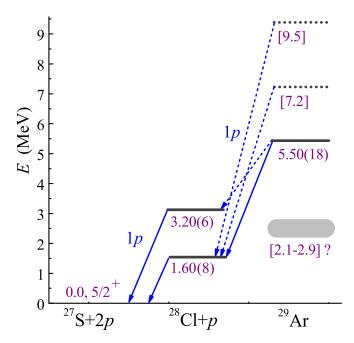


FIG. 8. The suggested decay scheme and the energy levels of 29 Ar and 28 Cl relative to the 27 S + 2p threshold. The gray-shaded region corresponds to the ground-state energy of 29 Ar predicted in this work (see the discussion in Sec. IV). The assumed and indicated 1p transitions are shown by the solid and dotted arrows, respectively. The dotted levels indicate very tentative assignments made on the basis of one or two 2p-decay events.

We argue below in Sec. III that our empirical assignments are backed by the isobaric mirror-symmetry systematics and that the most probable interpretation of the measured decay-product correlations is the observation of the ²⁸Cl ground state with $S_p = -1.60(8)$ MeV and the ²⁹Ar excited state with $S_{2p} = -5.50(18)$ MeV.

C. The data analysis: Unknown states in ³¹Ar and ³⁰Cl

The 2p-decay pattern of 31 Ar, derived from the 29 S + p+p data, is more complicated. Several separated regions with events, corresponding to the same 2p-decay energy, can be distinguished at the low angles in Fig. 2, which indicate different states in 31 Ar. The tentatively selected arcs are labeled by the lowercase Roman numerals (i)–(iv). The same event groups can be found in the angular θ - ρ_{θ} correlation plot in Fig. 9(c) derived for the assumed 31 Ar 2p decays. Its projections on the θ and ρ_{θ} axes are shown in Figs. 9(b) and 9(a), respectively. The $\theta(^{29}$ S-p) projection indicates some structures centered at the angles $\theta = \{26, 37, 43\}$ mrad, which point to possible low-energy states in 30 Cl. The ρ_{θ} projection indicates several 2p-decay patterns in 31 Ar with the center-of-gravity values at $\rho_{\theta} = \{45, 53, 61\}$ mrad.

The obtained statistics of the measured triple coincidences is low, and the nonselective projections do not allow for a quantitative analysis. Thus we have used the slice θ projections gated by the ρ_{θ} selected areas (i)–(v) in Fig. 9(a). These gated projections are shown in Fig. 10 in panels (i)–(v), respectively. Two additional projections gated at very large

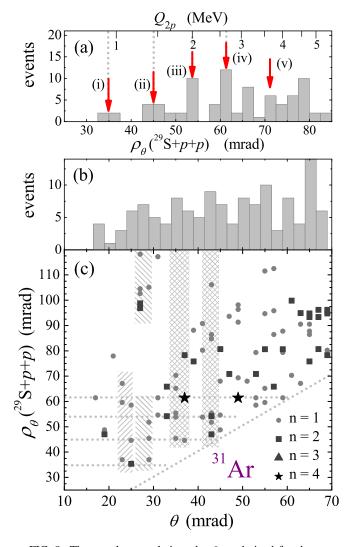


FIG. 9. The angular correlation plot θ - ρ_{θ} derived for the measured 29 S + p + p channel (c). Panels (a) and (b) show corresponding projections on the ρ_{θ} and θ axes, respectively. The hatched areas in panel (c) highlight events assumed to originate from the decay of 30 Cl resonance states. The dotted lines in panels (a) and (c) guide the eye for the regions corresponding to the assumed 31 Ar states which correspond to the events highlighted by the arcs in Fig. 2 labeled by the lowercase Roman numerals. The arrows and vertical lines in panel (a) point to the regions inspected for possible states in 31 Ar. The cases (i)–(v) correspond to the events highlighted by the arcs (i)–(v) in Fig. 2, respectively. The upper axis shows the 2p-decay energy Q_{2p} in the 29 S + p + p system. The inclined dotted line in panel (c) shows the kinematic limit for this type of plot; shape coding corresponds to multiplicity of events.

 ρ values are shown in panels (vi) and (vii) of Fig. 10. In analogy to the ²⁹Ar analysis, the "inclusive" $\theta_{p^{-29}S}$ distribution obtained from the measured $p^{-29}S$ double-coincidence events is shown in the lowest panel of Fig. 10. This inclusive distribution displays the same low-energy peak [peak (1)] at around 26 mrad as well as peaks (4) and (5), though evidence on Fig. 9(c)-indicated peaks at 37 and 43 mrad [marked as (2) and (3), respectively] is weak.

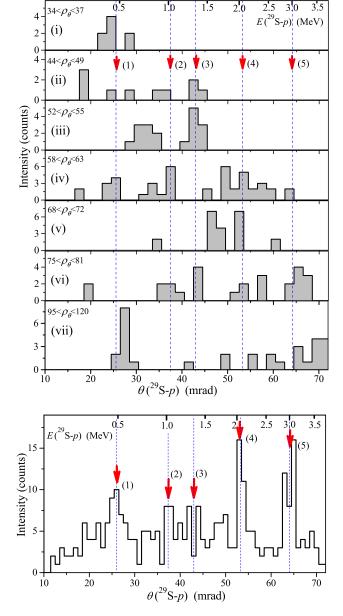


FIG. 10. The "gated" angular correlations $\theta_{p.^29\text{S}}$ derived from the measured $^{29}\text{S} + p + p$ triple-coincidence events, which are selected by choosing the gate conditions within the ρ_{θ} ranges corresponding to the highlighted arcs in Fig. 2. Panels (i)–(iv) correspond to the selection gates labeled in Fig. 2 by the same lowercase Roman numerals. The additional panels (v)–(vii) present the similar $\theta_{p.^{29}\text{S}}$ correlations selected by the larger ρ_{θ} values shown in their upper-left corners. Panel (viii) shows the "inclusive" angular $\theta_{p.^{29}\text{S}}$ correlations obtained from the measured $^{29}\text{S} + p$ double-coincident events (the hollow histogram). The upper axes show the corresponding energies in the $^{29}\text{S} + p$ system. The arrows (1)–(5) point to the events inspected for possible resonances in ^{30}Cl as well as the vertical across-panel lines.

Similar to the ²⁸Cl case, the MC simulations of the well-distinguished peaks [peaks (1), (4), and (5)] in the lowest panel of Fig. 10 by the experimental-setup response have resulted in the assigning of the unknown ³⁰Cl states with the

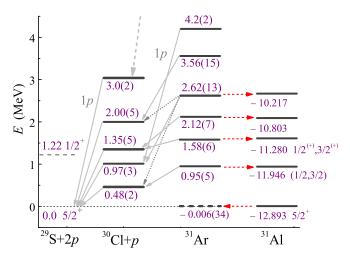


FIG. 11. The decay and level schemes for 31 Ar and 30 Cl isotopes derived from the data. The assigned 1p transitions are shown by the light-gray solid arrows. The dotted arrows show two undistinguished decay branches of the 2.62(13)-MeV state in 31 Ar, and the dashed arrow indicates 1p transitions from unidentified states in 31 Ar feeding the 3.0(2)-MeV state in 30 Cl. The vertical axis shows the energies relative to one-proton (for 30 Cl) and two-proton (for 31 Ar) breakup thresholds. The four lowest excited states of isobaric mirror partner 31 Al are aligned with corresponding observed states of 31 Ar (the correspondence of the levels is shown by red dashed arrows) and the 31 Ar g.s. energy is inferred based on isobaric symmetry assumptions. The legends for 31 Al levels show energies relative to the 2p-breakup threshold and the spin-parity J^{π} of the state.

1p-decay energies E_r of 0.48(2), 2.00(5), and 3.0(2) MeV, respectively. On the basis of the performed analysis, the 0.48(2)-MeV peak is assumed to be the ground state of 30 Cl. Such an assignment is supported by the observed 29 S + p + p correlations where one of the emitted protons has relatively large energy and another proton's energy is peaked at around 0.5 MeV [see Fig. 10(vii)]. This is a typical situation for a final-state interaction due to the 30 Cl g.s. resonance [see illustration in Fig. 4(c)].

By using the parameters of the 30 Cl g.s. one may obtain the ^{2}p -decay energy of the lowest-energy state in 31 Ar observed in the 29 S + p + p correlations [see Fig. 10(i)]. We have fitted the θ projection (i) by a sequential proton decay of 31 Ar via the g.s. of 30 Cl, and the obtained value of the ^{2}p -decay energy is 0.95(5) MeV. Though the pattern centered at ρ_{θ} = 35 mrad has low statistics, it is very important for an overall interpretation of the data, as it highly likely corresponds to the 31 Ar first-excited state. Thus we may lay the first piece into the puzzle of the 31 Ar excitation spectrum and its ^{2}p -decay scheme whose complete reconstruction is shown in Fig. 11 and which is explained in a step-by-step way below.

(a) Namely, the gated θ projections in Figs. 10(ii) and 10(iii) exhibit the same peak (3) at 43 mrad, which points to the sequential 2p decays of these 31 Ar states via the same state in 30 Cl. Peak (3) is best-fitted by assuming the 1p decay of the 30 Cl state with $E_r = 1.35(5)$ MeV. Then the 31 Ar states

corresponding to the complementary bumps in the structures (ii) and (iii) have the fitted 2p-decay energies of 1.58(6) and 2.12(7) MeV, respectively. One should note that projection (ii) provides very broad and statistically poor signal from the corresponding 31 Ar state, which makes the assignment very tentative [see Fig. 11].

- (b) Next, the gated θ projections in Figs. 10(iv) and 10(v) reveal events matching the same 2.00-MeV peak (4) in the inclusive spectrum in the lowest panel in Fig. 10. They point to the sequential 2p decays of two more states in 31 Ar via the 2.00-MeV state in 30 Cl. In particular, the fit of the peak at \sim 48 mrad which is complementary to peak (4) in projection (v) yields its energy of 1.56(10) MeV, and together they allow for the assignment of the new 31 Ar state with the 2p-decay energy of 3.56(15) MeV (see Fig. 11). Interpretation of the θ projections in Fig. 10(iv) is more complicated, because it has the additional components, and one of them matches peak (2) at 37 mrad due to a suspected state in 30 Cl.
- (c) The contribution of such a state can be spotted also in the θ projection (vi) in Fig. 10 as well as in the "inclusive" θ distribution labeled as peak (2). The corresponding fits provide the 1p-decay energy of 0.97(3) MeV assigned to the ³⁰Cl state. Then the whole structure of the θ distribution (iv) in Fig. 10 may be explained by a sequential 2p decay of one state in ³¹Ar by two branches via the intermediate 0.97- and 2.00-MeV states in ³⁰Cl. The respective fits provide two independent evaluations of the 2*p*-decay energy of the 31 Ar state of 0.97(3) + 1.65(10) = 2.62(13) MeV and 2.00(5) + 0.45(3) = 2.45(8) MeV, respectively. They agree within the statistical uncertainties. One may note that the assigned 2p-decay branch via the 2.00-MeV state in ³⁰Cl has the first-emitted proton energy of 0.45(3) MeV, which coincides with the 1p-decay energy of the g.s. of 30 Cl. Therefore the sequential 2p decay may proceed also via the g.s. of ³⁰Cl. These two assignments, indistinguishable in our experiment, are shown in Fig. 11 by the dotted arrows. Due to this uncertainty, we accept the ³¹Ar state to be at 2.62(13) MeV.
- (d) Finally, the gated θ projection in Fig. 10(vi) with the assumed peak (2) due to the 0.97-MeV state in 30 Cl allows for identification of the highest state observed in 31 Ar with the 2*p*-decay energy of 0.97(3) + 3.2(2) = 4.2(2) MeV.
- (e) The only undiscussed peak (5) at about 65 mrad in the "inclusive" θ distribution in the lowest panel of Fig. 10 is also detected in the observed ²⁹S-p-p correlations [see Fig. 9(b)]. However, energy of another emitted proton is distributed in a broad range of energy, which points to a continuum region of ³¹Ar excitations above 5 MeV. Therefore peak (5) cannot be assigned to an individual ³¹Ar state. We may speculate that it probably belongs to the 3.0(2)-MeV state in ³⁰Cl, which is strongly populated by deexcitation of the high-energy continuum in ³¹Ar.

Summarizing the above considerations, we have assigned the 30 Cl states with the decay energies E_r of 0.48(2), 0.97(3), 1.35(5), 2.00(5), and 3.0(2) MeV. There is also some indication that the structure around $\theta = 26$ mrad may consist of two substructures at about 24 and 28 mrad (corresponding to the E_r values of 0.48 and 0.55 MeV, respectively), which we discuss below. The newly prescribed states in 31 Ar have the 2p-decay energies of 0.95(5), 1.58(6), 2.12(7), 2.62(13), 3.56(15), and 4.2(2) MeV. All derived levels in 31 Ar and 30 Cl and their decay transitions are shown in Fig. 11.

III. SYSTEMATICS FOR CHLORINE ISOTOPES

As a first step in the interpretation of the data, we evaluate the energies of the states in proton-rich chlorine isotopes systematically by using the known information about their isobaric mirror partners. The obstacle here is the Thomas-Ehrman shift (TES) effect [9,10], especially pronounced in the sd-shell nuclei. The systematics of orbital size variations for s- and d-wave configurations are different when approaching the proton dripline and beyond it. This leads to a significant relative shift of the s- and d-wave dominated states distorting the expected (due to isobaric symmetry) nuclear level ordering in isotopes near the proton dripline. The core +p cluster model is a reasonable tool for consideration of this effect.

The Coulomb displacement energies in the core + p cluster model depend on two parameters: the orbital radius, which is mainly controlled by the potential radius, and the charge radius of the core. We use the potential with a Woods-Saxon form factor and with a conventional diffuseness parameter of a=0.65 fm. The radius value is provided by the standard parametrizations:

$$r_0 = 1.2(A_{\text{core}} + 1)^{1/3}$$
. (1)

The charge radii of sulfur isotopes are poorly studied [11], so we use the extrapolation shown in Fig. 12. Here we use two limits, corresponding to either the ascending trend or

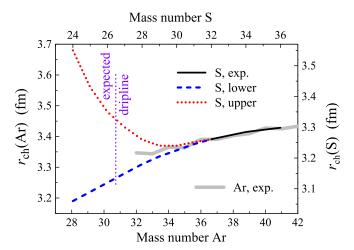


FIG. 12. Charge radii of sulfur isotopes used in the cluster core + p model for chlorine states. The dependence on sulfur isotopes is aligned with the much better studied dependence on argon isotopes to substantiate the provided extrapolation.

TABLE I. Potential parameters for the cluster two-body ${}^{A}Cl = {}^{A-1}S + p$ model. The minimum and maximum r_{sph} values correspond to the charge radii estimated from Fig. 12.

A	r_0	$r_{\rm sph}$ (min)	$r_{\rm sph}$ (max)	V_s (MeV)	V_d (MeV)
32	3.81	4.31	4.32		-46.80
31	3.77	4.29	4.31	-45.00	-45.38
30	3.73	4.26	4.31	-45.10	-44.76
29	3.69	4.23	4.33	-41.87	-41.85
28	3.64	4.20	4.38	-42.52	-42.69
27	3.60	4.16	4.45	-34.85	-39.51
26	3.56	4.12	4.55	-32.80	-38.86

the descending trend near the dripline (both trends are not excluded by the available systematics of the charge radii). One should note that the 26 S case is already uncertain. This particle-unstable nuclide (expected to be a 2p precursor [12]) has the valence-proton wave function expected to well penetrate into the subbarrier region.

Then the Coulomb potential of the charged sphere is used with the radius parameter $r_{\rm sph}$,

$$r_{\rm sph}^2 = (5/3)[r_{\rm ch}^2(A_{\rm core}) + r_{\rm ch}^2(p)],$$
 (2)

where $r_{\rm ch}(p) = 0.8$ fm. The potential parameters are collected in Table I. The results of the calculations are collected in Fig. 13. Below, we study the chain of five chlorine isotopes: $^{32-28}$ Cl.

A. 31Cl and 32Cl cases

One can see in Figs. 13(a) and 13(b) that for known isotopes 31 Cl and 32 Cl the used systematics of potential parameters given by Eqs. (1) and (2) provides level energies which are overbound a bit (by ~ 150 keV) in comparison with the data. However, the general trend is well reproduced; thus the standard set of the parameters could be a good starting point for the systematic evaluation of the whole isotope chain.

B. 30Cl and 29Cl cases

The spectrum of ²⁹Cl was discussed in detail in Refs. [2,4] [see Fig. 13(d)]. The data on the ³⁰Cl spectrum are reported in this work for the first time. The spectra of these isotopes can be reasonably interpreted only on the bases of the strong TES effect for some states. The calculated levels shown in Fig. 13(c) present evidence that two low-lying structures in the spectrum of 30 Cl [at 0.48(2) and 0.97(3) MeV] can be associated with nearly overlapping doublets 2^+-3^+ and 1^{+} - 3^{+} . We assume that the 3^{+} g.s. in 30 Al has a d-wave structure. Then its doublet partner, the 2⁺ state, is expected to be strongly shifted down by the TES and therefore to become the ³⁰Cl g.s. There is a hint in the data shown in Figs. 9 and 10 that the "ground-state peak" in 30 Cl at $\theta = 26$ mrad actually consists of two substructures, differently populated in the decays of several ³¹Ar states. In this work, the ³⁰Cl g.s. prescription is based on the lower substructure with the corresponding proton emission energy $E_r = 0.48$ MeV.

Why is the abovementioned prescription reliable? The Thomas-Ehrman shift for the 30 Al- 30 Cl g.s. pair is about 330 keV. If we assume that the 3⁺ g.s. in 30 Al has an *s*-wave structure, then the Thomas-Ehrman shift leads to the evaluated energies $E_r = 50$ –150 keV of the 3⁺ g.s. in 30 Cl. For such low decay energies, the 30 Cl g.s. should live a sufficiently long time to "survive" the flight through the second achromatic stage of the FRS fragment separator (of \sim 150 ns). We do not report such an experimental observation. We may also assume a *d*-wave structure of the 2⁺ and second 3⁺ states. However such an assumption practically does not change the predicted S_p energy of 30 Cl, but it requires the existence of peaks that are not seen in our data.

C. ²⁸Cl case

A doublet of low-lying states can be found in the bottom of the 28 Na spectrum [see Fig. 13(e)]. Presumably, the 2^+ and 1^+ states are separated by ~ 50 keV. The 1^+ state can be only d-wave dominated, while 2^+ can be either s- or d-wave dominated. If both states have a d-wave structure, then the 28 Cl g.s. should be found at about 2.4 MeV. In contrast, the observation of decay events corresponding to $E_r = 1.60(8)$ MeV can be easily interpreted as the s-wave g.s. of 28 Cl with the predicted energy of 1.77-1.84 MeV.

IV. SYSTEMATICS LOOK ON ARGON ISOTOPES

After we have systematically investigated the behavior of 1p-separation energies for the chlorine isotopic chain, we can turn to the systematic studies of the corresponding argon isotopic chain, which is based on the obtained information. Namely, we apply the systematics of odd-even staggering (OES) energies, which were shown to be a very helpful indicator concerning the dripline systems in our previous works [2,12,13]. The OES energy is defined as

$$2E_{\text{OES}} = S_{2p} - 2S_p.$$

The systematics of $E_{\rm OES}$ is presented in Fig. 14. One can see that the systematic trends are very stable for all the considered isotopic chains. The E_{OES} is always smaller for the proton-rich systematics compared to the neutron-rich one. The difference of 0.5 MeV is practically the same value for all three cases (see the gray line in Fig. 14). The $E_{\rm OES}$ also systematically decreases with an increase of mass number, which indicates a borderline of nuclear stability. The $E_{\rm OES}$ for $^{30}{\rm Ar}$ was found to be smaller than the corresponding systematic expectation [2]. It was argued in this work that such a deviation is typical for systems beyond the dripline, which is confirmed by the examples of well-studied 2p emitters ¹²O, ¹⁶Ne, and ¹⁹Mg. The theoretical basis for such an effect is provided by the three-body mechanism of the TES [14], which was recently validated by the high-precision data and theoretical calculations in Ref. [15]. When extrapolating this trend to the nearby isotopes, one may expect that 31 Ar should reside on the E_{OES} systematics curve or slightly below, while the ²⁹Ar could be considerably below.

The excitation spectrum of ³¹Ar obtained in this work demonstrates a very high level of isobaric symmetry with

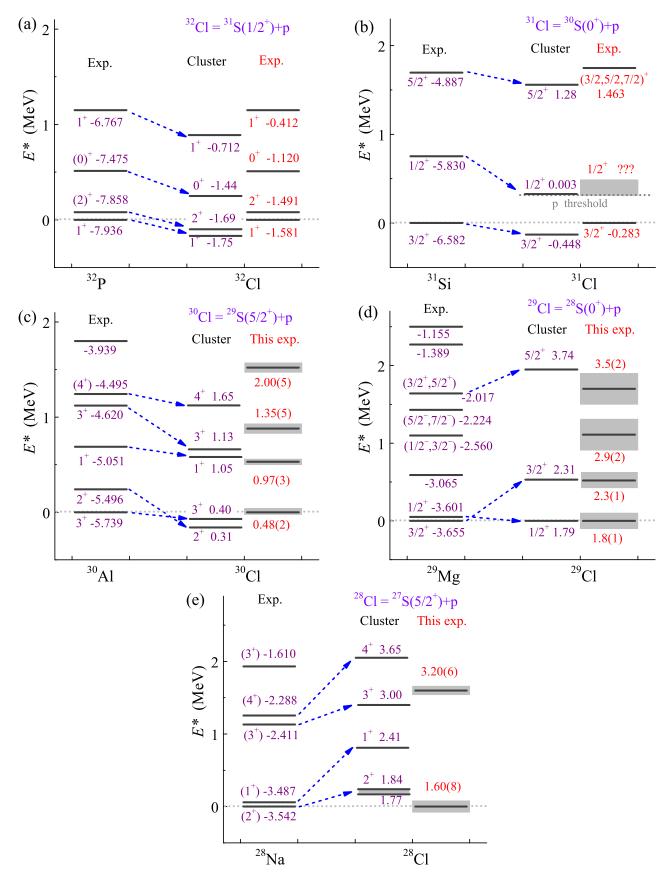


FIG. 13. Energy levels of chlorine isotopes. Vertical axes show excitation energies E^* . The level legend gives the spin-parity J^{π} and energies relative to the 1*p*-emission threshold for the chlorine chain members or to the 1*n*-emission threshold for their isobaric mirror partners.

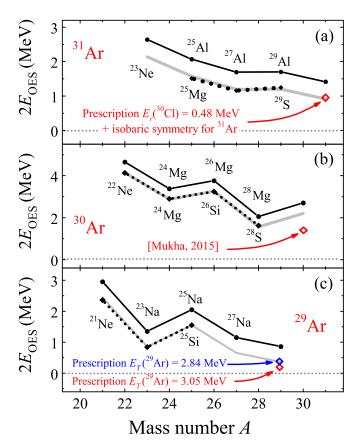


FIG. 14. Odd-even staggering (OES) energies for the isotones leading to ³¹Ar (a), ³⁰Ar (b), and ²⁹Ar (c) are shown by dashed lines. The OES energies for mirror isobar symmetry are given by solid lines. Panel (b) corresponds to Ref. [2]. The solid gray lines are provided to guide the eye. They are shifted down by the constant value of 0.5 MeV, which seems to be the very stable value for a variety of isobars and isotones.

respect to its mirror 31 Al (see Fig. 11). Based on the isobaric symmetry assumption, we can infer a very small value of the 2p threshold $S_{2p} = -3(50)$ keV for the g.s. of 31 Ar. This value is obtained by a comparison of the 2p-decay energy of 950(50) keV and the literature value of 946.7(3) keV of the excitation energy of the first-excited state in 31 Ar and its mirror 31 Al [16], respectively. The S_{2p} value of 31 Ar g.s. may be also obtained by a comparison of the aligned low-energy excited states in 31 Ar and 31 Al. Namely, the states in 31 Ar with 2p-decay energies of 1.580(60), 2.120(70), and 2.620(130) MeV match the known excited states in 31 Al [16] at excitation energies of 1.613(0.24), 2.090(11), and 2.676(28) MeV, respectively. By assuming the same energy between the g.s. and the respective excited state in both 31 Ar and 31 Al, we obtain more estimations of the g.s. of 31 Ar: at $S_{2p} = +33(60)$, -30(81), and +56(158) keV, respectively.

The weighted mean of all four pairs provides the averaged S_{2p} value of +6(34) keV, which we finally accept for the g.s. of ³¹Ar. Our evaluation agrees within the experimental uncertainties with the previously estimated S_{2p} value of -3(110) keV obtained in β -decay studies of ³¹Ar [17], and

TABLE II. Separation energies (in MeV) S_{2p} for 29 Ar and S_p for 28 Cl according to different systematics and theoretical predictions.

Work	This, expt.	This, sys.	[18]	[19]	[20]
S_{2p}	- 5.50(18)	- 2.93(25)	- 5.17(16)	- 5.17(2)	- 8.5(3.5)
S_p	-1.60(8)	-1.80(4)	-2.84(11)	-2.82(2)	

the precision of the present result is improved by a factor of 3. Our conclusion is that the ³¹Ar g.s. is bound rather than not.

With the known value $S_p(^{30}\text{Cl}) = -0.48(2)$ MeV, we can estimate the value $2E_{\text{OES}} = 0.966(74)$ MeV for 31 Ar, which is in a good agreement with the extrapolated OES energy trend in Fig. 14(a), which gives $2E_{\text{OES}} = 0.915$ MeV. This is an additional argument in favor of the isobaric symmetry (or very close to that) of the 31 Ar and 31 Al ground states.

close to that) of the 31 Ar and 31 Al ground states.

So, the 31 Ar g.s. is evaluated to be likely bound with the 2p-separation energy of less than 40 keV. Even if it is 2p unbound (which cannot be excluded by our results), its decay status is not affected: for such a small decay energy the 2p partial-lifetime of 31 Ar is incomparably longer than its β -decay lifetime. Then the g.s. of 31 Ar can still be considered as a quasistable state in many theoretical applications. An interesting issue here could be the possible existence of the 2p halo in such an extremely lousy-bound proton-rich nuclide.

Now let us turn to the ²⁹Ar system. As discussed above, we expect the chlorine isotopes to be overbound in comparison with their mirror isobars (relative to the isobaric symmetry expectations) in a region beyond the dripline because of the TES. For the argon isobars far beyond the dripline, there should be a competition of two trends. One is the overbinding because of the TES (the Coulomb displacement energy decreases because of the increase of the valence orbital size). An opposite trend is underbinding due to E_{OES} reductions (the p-p pairing energy decreases because of the increase of the valence-proton orbital size). One must note that the absolute value of extrapolated OES energy is quite low, $2E_{OES} = 0.361$ MeV [see Fig. 14(c)]. Because the negative or extremely small value of pairing energy seems to be unrealistic assumptions, we accept the following values, $\{E_{OES}, 2E_{OES}\} =$ {0.155, 0.361} MeV, as the limits of an OES energy variation. Then we obtain the value $S_{2p} = -2.93(25)$ MeV for the g.s. of ²⁹Ar by accepting $S_p = -1.60(8)$ MeV. According to this estimate, the state observed in ²⁹Ar at $S_{2p} = -5.50(18)$ MeV cannot be assigned as its ground state, and therefore it should be one of the excited states in ²⁹Ar. However, one should note that this prediction based on the OES systematics is not in accord with the other systematics and the results of theoretical calculations available in the literature (see Table II reviewing the published results on ²⁹Ar). So, further studies of the ²⁹Ar system are required to clarify the issue.

V. CONCLUSION

The new isotopes ²⁹Cl and ³⁰Ar were recently discovered [2] and the spectroscopy of these two nuclei was performed [4] with the reactions of the ³¹Ar exotic beam at 620 AMeV energy on a light target. In this work, we

investigated the additional inelastic excitation and particle knockout channels of those reactions. The main results of this work are as follows.

- (i) Two previously unknown isotopes, 28 Cl and 30 Cl, which are unbound respective to the 1p emission have been observed. The ground-state energies of 28 Cl and 30 Cl have been derived by using angular 27,29 S + p correlations. In addition, four excited states of 30 Cl have been identified as the subsystems of the previously-unknown excited states of 31 Ar. These states were populated by inelastic excitation of secondary 31 Ar beam and identified by registering 29 S + p + p correlations.
- (ii) The first-time observed excitation spectrum of 31 Ar matches very well the excitation spectrum of its isobaric partner 31 Al. The registered isobaric symmetry is used to infer the position of the 31 Ar ground state at the 2p-separation energy $S_{2p} = 0.006(34)$ MeV. The high level of isobaric symmetry of these mirror nuclei is confirmed by the systematics of OES energies. The near-zero value of S_{2p} of 31 Ar suggests speculations about the possibility of a 2p halo in this nuclide.
- (iii) First evidence of a state in the previously unobserved isotope ²⁹Ar has been obtained by detecting $^{27}S + p + p$ correlations. The state was found to be

2p unbound with $S_{2p} = -5.50(18)$ MeV. The results of the different energy systematics do not allow us to clarify the status of the observed state. It may be an excited state at $\sim 1-2$ MeV above the ground state (as estimated in this work) or it may be a ground state of 29 Ar according to Refs. [18–20]. This situation calls for further measurements.

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