Excited states of ³⁹Ca and their significance in nova nucleosynthesis

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Background: Discrepancies exist between the observed abundances of argon and calcium in oxygen-neon nova ejecta and those predicted by nova models. An improved characterization of the ³⁸K(p, γ) ³⁹Ca reaction rate over the nova temperature regime (~0.1–0.4 GK), and thus the nuclear structure of ³⁹Ca above the proton threshold [5770.92(63) keV], is necessary to resolve these contradictions.

Purpose: The present study was performed to search for low-spin proton resonances in the 38 K + p system, and to improve the uncertainties in energies of the known astrophysically significant proton resonances in 39 Ca.

Methods: The level structure of ³⁹Ca was investigated via high-resolution charged-particle spectroscopy with an Enge split-pole spectrograph using the ⁴⁰Ca(³He, α)³⁹Ca reaction. Differential cross sections were measured over six laboratory angles at 21 MeV. Distorted-wave Born approximation calculations were performed to constrain the spin-parity assignments of observed levels with special attention to those significant in determination of the ³⁸K(p, γ)³⁹Ca reaction rate over the nova temperature regime.

Results: The resonance energies corresponding to two out of three astrophysically important states at 6154(5) and 6472.2(24) keV are measured with better precision than previous charged-particle spectroscopy measurements. A tentatively new state is discovered at 5908(3) keV. The spin-parity assignments of a few of the astrophysically important resonances are determined.

Conclusions: The present 38 K(p, γ) 39 Ca upper limit thermonuclear reaction rate at 0.1–0.4 GK is higher than that determined by Christian *et al.* [Phys. Rev. C **97**, 025802 (2018)] by at most a factor of 1.4 at 0.1 GK.

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I. INTRODUCTION

Classical novae occur in semidetached [1] close interacting binary systems consisting of a carbon-oxygen-rich (CO) or an oxygen-neon-rich (ONe) white dwarf and a main sequence star. When the white dwarf has accreted sufficient hydrogenrich material ($\sim 10^{-4} M_{\odot}$ to $10^{-6} M_{\odot}$ [2]) from its companion star, a thermonuclear runaway occurs on the surface of the white dwarf at the base of the accreted envelope (see Ref. [3] for details). Depending on the mass of the white dwarf, peak temperatures of 0.1–0.4 GK are reached within only a few hundred seconds or less [2]. The dominant nuclear reaction flow proceeds through explosive hydrogen burning via the rp process [4], where a series of (p, γ) and (p, α) reactions and β^+ decays occur on the proton-rich side of the valley of stability. An outburst follows, giving birth to a classical nova.

Relative to solar abundances, the ejecta of classical novae show significant nuclear processing [5]. Both theoretical estimations [2,6–9] and the abundance patterns inferred from observations of nova ejecta [10–17] agree that the nuclear activity in classical novae generally stops around $A \sim 40$, i.e., calcium.

Observed elemental abundances for Ar and Ca in ONe novae [10] show an enhancement with respect to the solar

abundances by up to an order of magnitude, whereas nova models [18] predict such abundances to be generally close to the solar values. A sensitivity study performed by Iliadis *et al.* [6] identified the 38 K(p, γ) 39 Ca reaction as one of the few reactions affecting the simulated nova abundances for Ar and Ca.

The 38 K(p, γ) 39 Ca reaction rate of Ref. [6] was determined solely based on Hauser-Feshbach calculations, which introduced 4 orders of magnitude uncertainty in the reaction rate. Consequently, variations of factors of ~25, 136, and 58 were found in the predicted 38 Ar, 39 K and 40 Ca final abundances, respectively [6].

Over the temperatures characteristic of explosive hydrogen burning in novae, the ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction rate is dominated by contributions from three l = 0, $J^{\pi} = 5/2^+$ states in ${}^{39}Ca$. The excitation energies of these states were reported [19] to be 6157(10), 6286(10), and 6460(10) keV based on various previous measurements. They correspond to proton resonances in the ${}^{38}K + p$ system (Q =5770.92(63) keV [20]) at $E_r = 386(10)$, 515(10), and 689(10) keV, respectively. In order to reduce the uncertainty in the ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction rate to help constrain the nova models and remove the discrepancy between simulated and observed Ar and Ca abundances in nova ejecta, the ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction was directly measured in inverse kinematics recently for the first time [21,22].

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As a result, the 689(10)-keV resonance in ³⁹Ca was observed at $E_r = 679^{+2}_{-1}(\text{stat.}) \pm 1(\text{sys.})$ keV, and its strength was measured to be $\omega\gamma = 120^{+50}_{-30}(\text{stat.})^{+20}_{-60}(\text{sys.})$ meV. The other two resonances remained unobserved [22]; however, upper limits on their strengths were determined. The ³⁸K(p, γ)³⁹Ca reaction rate was recalculated and its uncertainty was reduced to a factor of ~40 [22]. This, in turn, has reduced the uncertainty in predicted abundances of ³⁸Ar, ³⁹K, and ⁴⁰Ca to a factor of ≤ 15 [22].

Further high-resolution spectroscopic studies of ³⁹Ca were encouraged in Ref. [21] in order to search for potential unobserved low-spin proton resonances in the ³⁹K + p system.

We performed a high-resolution charged-particle spectroscopy experiment via the ${}^{40}Ca({}^{3}He, \alpha){}^{39}Ca$ reaction. We specifically aimed to explore $E_x({}^{39}Ca) \sim 6$ MeV region, where the energies of the astrophysically significant proton resonances are still ambiguous. This work presents the results.

II. EXPERIMENTAL SETUP AND DATA ANALYSIS

The experiment was performed at Triangle Universities Nuclear Laboratory (TUNL). A 21-MeV ³He²⁺ beam $(\Delta E/E \sim 3.5 \times 10^{-4})$ was delivered by the TUNL duoplasmatron ion source and 10-MV FN tandem Van de Graaff accelerator. The beam energy was analyzed using two high resolution 90° dipole magnets and focused to a spot size of 1 mm diameter on target. Typical beam intensity on target varied between 350 and 1000 *e* nA.

Three types of targets were employed: a calcium target for measuring the main reaction of interest [40 Ca(3 He, α) 39 Ca], a silicon oxide target for calibration purposes, and a carbon target for background determination. The first two targets were separately produced by thermal evaporation of natural metallic calcium and SiO₂ powder onto a 38- μ g/cm²-thick natural

carbon foil from the Arizona Carbon Foil Company [23]. A $38-\mu g/cm^2$ -thick foil was our carbon target.

Target thicknesses and stoichiometries were measured using Rutherford backscattering spectrometry (RBS) following the experiment. For the RBS, a 2-MeV ${}^{4}\text{He}^{2+}$ beam was employed using the same accelerator facility. The backscattered α particles were measured at 165° with respect to the beam axis using a single 100- μ m-thick silicon surface barrier detector with 17-keV energy resolution. A gold target with a known thickness was used to calibrate the RBS spectra. During the RBS measurement, a pulser was used to adjust the gain of the silicon detector and monitor the electronics.

RBS revealed that (i) the calcium target (see Fig. 1) is composed of 58.3 μ g/cm² Ca, 37.7 μ g/cm² O, 37.8 μ g/cm² C, and 0.9 μ g/cm² S, where the small sulfur contamination comes from residual CdS contaminations in the evaporator system; (ii) the silicon oxide target is composed of 13.6 μ g/cm² Si, 30.2 μ g/cm² O, 36.8 μ g/cm² C, and 7.5 μ g/cm² Ta, where the last contamination comes from partial melting of the Ta evaporation boat towards the end of the evaporation; and (iii) the carbon target is composed of 37.9 μ g/cm² C. The uncertainties in these thicknesses were determined to be \approx 10%. This factor comes from a conservative estimation of the uncertainty of stopping powers of helium in calcium from SRIM [24] where no experimental data are available.

The calcium target was fabricated at the beginning of the experiment and was exposed to air for less than 10 minutes when mounted into the main target chamber. Some degree of oxygen contamination was expected in the calcium target and the experiment was planned accordingly to avoid the states of interest in ³⁹Ca being obscured by the oxygen contamination. No excited states from the sulfur and tantalum contaminations in the targets were observed.

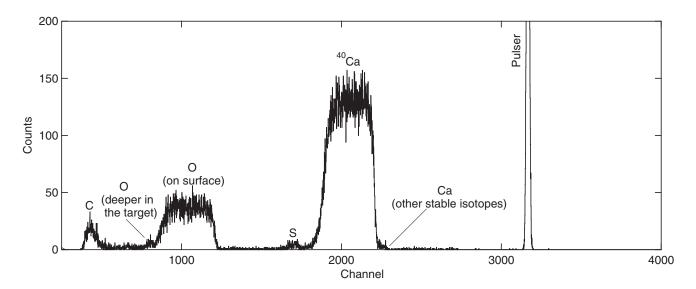


FIG. 1. The spectrum from the RBS measurement on the calcium target. The peaks corresponding to the calcium and carbon contents of this target are shown. The wide oxygen peak comes from surface oxidation of calcium due to a few minutes exposure to air. The smaller oxygen peak is deeper within the target and could possibly be caused by floating the carbon foil in water or some oxygen contamination that preexisted on the carbon backing foil. The sulfur peak comes from residual CdS contaminations in the evaporator system.

The light reaction products were accepted by the TUNL high resolution Enge split-pole magnetic spectrograph [25], whose total solid angle acceptance was set to 1 msr for this experiment. The charged particles were dispersed by the spectrograph according to their momenta and were focused onto the spectrograph's focal plane. The magnetic field of the spectrograph was varied between 8.9 and 9 kG so as to (i) kinematically exclude the elastically and inelastically scattered ³He particles and (ii) accept the α particles from the ⁴⁰Ca(³He, α) reaction whose radii of curvature lie on the focal plane between 68 and 84 cm, covered by the focal plane detector. These correspond to ³⁹Ca excited states from ground state to 7799 keV.

To obtain optimal momentum resolution with the TUNL Enge split-pole spectrograph, a high resolution position sensitive focal plane detector was deployed. The detection system is described in detail elsewhere [26]. Identification of α particles was carried out by measuring their energy losses, residual energies, and positions along the focal plane of the spectrograph. By placing software gates around the α particles, their momentum spectra were obtained at each spectrograph angle (see Fig. 2). Peaks in these spectra represent the energy levels of ³⁹Ca. The reaction products were measured at laboratory angles of 19°, 21°, 23°, 25°, 40°, and 44°. These scattering angles were particularly chosen to move the contaminant states away from the region of interest in ³⁹Ca. Scattering angles lower than 19° were not considered because the ¹⁵O state at 6176.3 keV would obscure the ³⁹Ca region of interest.

The major contaminant peaks present in the spectra were the $E_x = 0-4804$ -keV states of ¹¹C [28], populated via the ¹²C(³He, α)¹¹C reaction, and the $E_x = 0-6859$ -keV states of ¹⁵O [29], populated via the ¹⁶O(³He, α) ¹⁵O reaction (see Fig. 2).

The peaks observed in the spectra were fitted using a leastsquares multi-Gaussian fit function to determine the peak centroids, widths, and areas. The spectra were first calibrated using the known levels of ²⁷Si [30] measured using the SiO₂ target (see Fig. 3) and those of ¹⁵O [29] produced by the (³He, α) reaction on the oxygen content of the calcium target. Once the well populated low-lying states of ³⁹Ca were identified, they were used together with the strong ¹⁵O peaks and only a couple of statistically significant ²⁷Si states (780.9 and 4289.2 keV) to recalibrate each ³⁹Ca spectrum. The energies of the ³⁹Ca internal calibration points were adopted from Ref. [27] and are marked by asterisks in Table I.

Calibration of each spectrum was performed using Bayesian framework explained in Ref. [26]. A cubic polynomial fit of the form $\rho = A + Bx + Cx^2 + Dx^3$ was obtained according to this method for a set of calibration peaks at each angle. Here, ρ and x respectively correspond to the radius of curvature of an α particle traversing the spectrograph and the channel number corresponding to the centroid of the calibration peak produced on the focal plane by that α particle. Coefficients A to D are fit parameters. These fits were used to derive the excitation energies for the unknown peaks in the spectrum at that angle.

Excitation energies' uncertainties reported in Table I were computed from the statistical uncertainties in the corresponding peaks' centroids, uncertainties in the coefficients of the polynomial calibration fits, and the reproducibility of calibration peaks.

The mutually independent systematic uncertainties for the excitation energies at each angle (not included in Table I) arise from (1) $\pm 10\%$ uncertainties in the thicknesses of the calcium and SiO₂ targets affecting energy losses through these targets, (2) ± 7.3 keV uncertainty in the beam energy, and (3) the systematic uncertainties in the O values of the $({}^{3}\text{He}, \alpha)$ reactions on ${}^{16}\text{O}$, ${}^{28}\text{Si}$, and ${}^{40}\text{Ca}$ target nuclei, which are 0.49, 0.11, and 0.6 keV [20], respectively. The overall resultant systematic uncertainty in each excitation energy is 1.4 keV. This should be added in quadrature to the uncertainties quoted in Table I. To obtain the final ³⁹Ca excitation energies, a weighted average was calculated (using the V.AVELIB utility code of Ref. [38]) for each state over all the angles. The energy resolution, defined as the peak full width at half maximum (FWHM), was 22 keV at 19° and 46 keV at 44°. The loss of energy resolution at higher angles results from kinematic broadening [26.39-41] due to an increase in the energy straggling of the α particles through the target.

III. RESULTS

A. Excitation energies of ³⁹Ca

Forty-five states of ³⁹Ca with excitation energies up to 7799 keV were observed in the present work and are listed in Table I. Most of the measured energies in the present work are in agreement within 1σ – 2σ with those measured in the previous ⁴⁰Ca(³He, α)³⁹Ca experiments [32–35,42], and with the excitation energies reported in the most recent evaluation of ³⁹Ca excited states [27]. The excitation energies above 7 MeV from the present work have larger uncertainties since these states lie far from the last calibration peak used, which is the ¹⁵O state at 6176.3(17) or 6859.4(9) keV [29], depending on the angle.

Three $J^{\pi} = 5/2^+$ excited states of ³⁹Ca were identified previously [6] to dominate the ³⁸K(p, γ) ³⁹Ca reaction rate at temperatures characteristic of explosive hydrogen burning in novae. The excitation energies of these states were previously determined [19] to be $E_x = 6157(10)$, 6286(10), and 6460(10) keV. In the following, comparisons between the results of the present work with those of previous measurements will be described for these three states, as well as a few other states.

The 5537-keV level. This state is one of the very few states whose energy from the present work is inconsistent with that measured previously [37]. In the present work, the 5537-keV state is observed at four angles. At 19° and 44°, it has been obscured by the 5.183- and 5.2409-MeV states of ¹⁵O and by the ground state of ¹¹C, respectively. The only other experiment in which this state has been observed in the past is the ⁴⁰Ca(p, d) measurement performed by Matoba *et al.* [37]. They observed a state at 5588 keV, which suffered from poor statistical significance in comparison with other observed states. It may be possible that since this state was populated weakly, it would have been a peak with rather large statistical uncertainty. However, Matoba *et al.* [37] did not

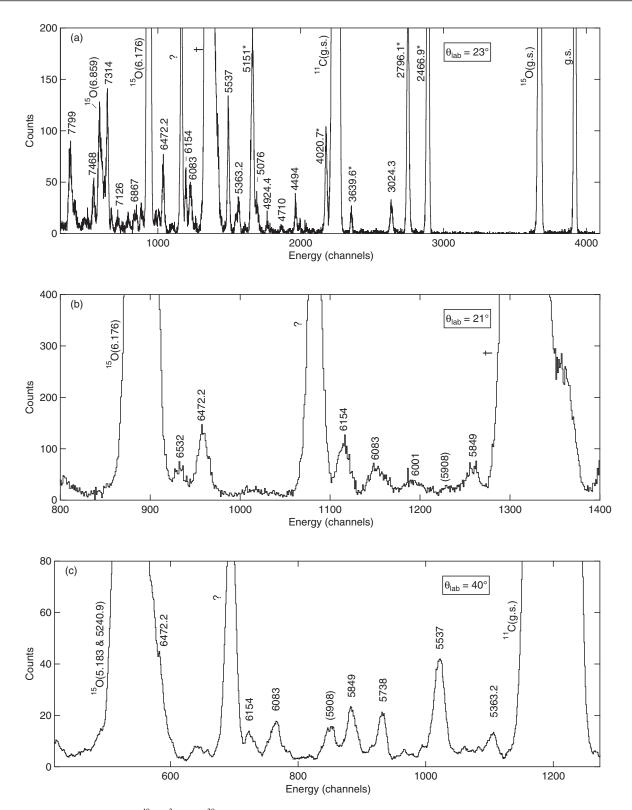


FIG. 2. The spectra from the 40 Ca(3 He, α) 39 Ca reaction at $\theta_{lab} = 23^{\circ}$ (a), 21° (b), and 40° (c). At the latter two angles, the spectra are zoomed in on the region of astrophysical significance. Peaks corresponding to 39 Ca states are labeled with energies (in keV) from the present work except those denoted by asterisks, which were used as internal calibration using energies from Ref. [27]. For clarity, not all peaks are labeled. Ground states are indicated by g.s. The main contaminant peaks are labeled with their parent nuclei and their energies (in MeV). The peak marked by \dagger consists of the 5183- and 5240.9-keV states of 15 O and the 2-MeV state of 11 C. Tentative states are in parentheses. For a discussion regarding the peak denoted by the question mark, see Sec. III A.

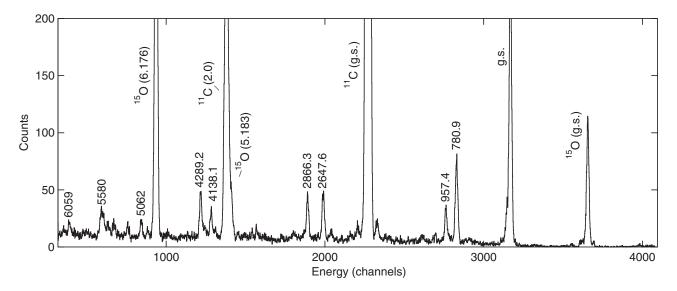


FIG. 3. The spectrum from the ²⁸Si(³He, α)²⁷Si calibration reaction measured at $\theta_{lab} = 19^{\circ}$. Selected peaks corresponding to ²⁷Si states are labeled with energies from Ref. [30] (in keV). For clarity, not all peaks are labeled. The main contaminant peaks are labeled with their parent nuclei and their energies (in MeV). g.s. indicates ground state.

assign uncertainties to their excitation energies. The 10-keV uncertainty assigned to their excitation energies in our Table I comes from the decision made by nuclear data evaluators in Refs. [19,27] to assume a 10-keV uncertainty on all their excitation energies based on their energy resolution (25–30 keV [37]).

The tentative 5908-keV level. This state is not listed as an excited state of ³⁹Ca in the most recent Evaluated Nuclear Structure Data File for ³⁹Ca [27]. The state follows expected systematics, but is weak at all three angles where it is observed [19°, 40°, and 44°; see panel (c) in Fig. 2]. Hence, we tentatively assign it to ³⁹Ca.

The 6154-keV level. The excitation energy of 6154(5) keV measured in the present work agrees very well with all of the results of the previous measurements: 6150(20) keV [35], 6158(10) keV [37,43,44], and 6160(15) keV [36].

The 6286-keV level. At all 6 angles measured in the present work, a very strong peak (denoted by a question mark in Fig. 2) is populated where the 6286-keV state, measured in Ref. [37], was expected to be observed. If it is assumed that this peak belongs to ³⁹Ca: (i) Its excitation energy is derived to be 6226(10) keV, which agrees well with the $E_x =$ 6200(50) keV measured in Ref. [45] but is inconsistent with the $E_x = 6286(10)$ keV from Ref. [37]. (ii) Its α angular distribution is in very good agreement with $J^{\pi} = 3/2^+$, $5/2^+$ [see panel (h) of Fig. 6], which is expected for the 6286-keV state [37].

The $E_x = 6226(10)$ keV result from the present work carries a large (relative to those of the other states) uncertainty of 10 keV because there is a rather large shift equal to 47 keV in the excitation energy of this state measured at each individual angle from 19° to 44° (see Fig. 4). Even though this kinematic shift in energy is large and seems to be correlated with angle, there are no outlying data points using the criteria described in Ref. [38]. Moreover, the present excitation energy was calculated using the bootstrap Monte Carlo method [46] because it accounts for the data exhibiting large scatter between points.

Since this peak is statistically well populated at all angles observed, it was odd that its excitation energy should differ by about 47 keV from 19° to 44°. It cannot belong to ¹¹C or ¹⁵O since the expected states of these nuclei in this region of the spectra are all accounted for. The possibility of this peak belonging to ¹²C [from the ¹³C(³He, α) reaction] or to other stable isotopes of calcium and sulfur (from contaminant isotopes in the target, see Sec. II), fluorine and nitrogen (from potential beamline contaminants), or chlorine and sodium (from potential contaminants in the water used to float the carbon backing foil of the calcium target) was examined. However, none of these cases produced an energy consistent with or even close to the known excitation energies of these nuclei. In addition, if the peak is assumed to belong to the contaminants considered above, the extracted excitation energy would exhibit a similar kinematic shift correlated with angle but of over four times more than the observed 47 keV. The shift in this state's extracted energy regardless of its assumed origin, however, means that we cannot rule out the possibility of having an unknown contaminant in our target. However, the RBS spectrum of Fig. 1 shows no evidence of a substantial amount of an unknown contaminant. Also, it seems less likely that a surface contamination of some kind which is small enough to remain undetected by the RBS measurement produces a peak which is statistically well populated at all angles. Furthermore, this peak is unlikely to be a doublet since its width is consistent with those of the known ³⁹Ca single states in the spectrum at each angle. The contaminant peaks are usually wider due to kinematic broadening caused by their different reaction kinematics. Finally, since the individual calibrations at each angle produced results for other ³⁹Ca states consistent with previously measured values, the possibility of problems with the present calibrations are confidently ruled out.

TABLE I. Weighted average (over all angles) excitation energies (in keV) of ³⁹Ca from the present work in comparison with those measured in the selected previous work. Levels measured previously but not observed in the present work are omitted from the list. Ref. [27] includes all previous experimental results for ³⁹Ca. States used in the present work for internal energy calibration are denoted by an asterisk. The uncertainties reported for the present work do not include the ± 1.4 keV systematic uncertainty in our results.

40 Ca(3 He, α) evaluation [31] ^a		40 Ca(<i>d</i> , <i>t</i>) [36]	40 Ca (p, d) [37]		³⁹ Ca Ev	valuation [27]	$({}^{3}\text{He}, \alpha)$ present work		
E_x (keV)	J^{π}	E_x (keV)	$\overline{E_x}$ (keV)	J^{π}	E_x (keV)	J^{π}	E_x (keV) J^{π}		
0 3/2+		0	0	$3/2^{+}$	0	3/2+	0	3/2+	
2473(10)		2470(15)	2463(10)	$1/2^{+}$	2466.9(5)	$1/2^{+}$	2466.9(5)*	$1/2^{+}$	
2799(10)		2790(15)	2791(10)	$7/2^{-}$	2796.1(6)	7/2-	2796.1(6)*	7/2-	
3032(10)		3030(15)	3021(10)	$3/2^{-}$	3025.1(9)	3/2-	3024.3(11)	3/2-	
3660(20)		3640(15)	3636(10)		3639.6(8)	$(9/2^{-})$	3639.6(8)*		
3840(20)		3820(15)	3820(10)		3823.6(15)	(1/2, 3/2, 5/2)	3827.1(17)		
			3886(10)		3882(2)	$(3/2^{-}, 5/2, 7/2^{+})$	3882(5)		
		3940(15)	3943(10)		3935.7(7)	$(3/2^{-})$	3936.2(22)		
4020(20)		4020(15)	4016(10)	$1/2^{+}$	4020.7(17)	$1/2^{-})$	4020.7(17)*		
4320(20)		4320(15)	4340(10)		4332(10)	$(5/2, 7/2)^{-}$	4339(3)		
4430?(20)		4460(15)	4432(10)	$5/2^{+}$	4439(10)	$3/2^+, 5/2^+$	4444(5)		
4490(20)			4487(10)	$7/2^{-}$	4488(10)	7/2-	4494(2)		
4710(20)			. ,	,	4710(20)	4710(3)			
4920(20)		4940(15)	4926(10)	$(5/2^+)$	4929(10)	$3/2^+, 5/2^+$	4924.4(24)		
5070(20)			. ,		5070(20)	$3/2^+, 5/2^+$	5076(4)		
5130(20)	$5/2^{+}$	5130(15)	5128(10)	$5/2^{+}$	5129(10)	5/2+	5116(4)		
	,			1	5151(2)	$(11/2^{-})$	5151(2)*		
			5222(10)	$5/2^{+}$	5222(10)	$3/2^+, 5/2^+$	5223(4)		
			5364(10)	1	5364(10)	1 7 1	5363.2(16)		
			5400(10)		5400(10)		5405(3)		
			5588(10)	$(5/2^+)$	5588(10)	$3/2^+, 5/2^+$	5537(6)	$3/2^+, 5/2^+$	
			5673(10)	$(5/2^+)$	5673(10)	$3/2^+, 5/2^+$	5668(3)	1 / 1	
5760(20)			5720(10)	$(7/2^{-})$	5720(10)	$(5/2^-, 7/2^-)$	5738(3)		
			5851(10)	3/2-	5851(10)	1/2-, 3/2-	5849(3) (5908(3))		
6000(20)		6010(15)	6009(10)	$(7/2^{-})$	6008(10)		6001(4)		
			6094(10)	$(1/2^+)$	6094(10)	$(1/2^{+})$	6083(7)	$(7/2^+, 9/2^+)$	
6150(20)	$5/2^{+}$	6160(15)	6158(10)	5/2+	6157(10)	5/2+	6154(5)	$3/2^+, 5/2^+$	
	- /		6286(10)	$5/2^{+}$	6286(10)	$3/2^+, 5/2^+$		- 1) - 1	
		6450(30)	6467(10)	$5/2^{+}$	6451(2)	$3/2^+, 5/2^+$	6472.2(20)	$(5/2^{-}, 7/2^{-})$	
			6514(10)	$(5/2^+)$	6514(10)	$3/2^+, 5/2^+$	6532(3)		
			6580(10)	$(7/2^{-})$	6580(10)	5/2-,7/2-	6579(7)		
			6629(10)		6629(10)	1 7 1	6645(7)		
			6794(10)	$5/2^{+}$	6794(10)	$3/2^+, 5/2^+$	6779(4)		
		6820(30)	6835(10)	,	6834(10)	$3/2^+, 5/2^+$	6867(6)		
			6954(10)		6954(10)	5/2-,7/2-	6972(3)		
			7060(10)		7060(10)	, , ,	7070(5)		
			7132(10)	$5/2^{+}$	7132(10)	$3/2^+, 5/2^+$	7126(9)		
		7210(30)	7199(10)	$5/2^{+}$	7199(10)	5/2+	7217(9)		
			7248(10)	$5/2^{+}$	7248(10)	$3/2^+, 5/2^+$	7240(9)		
			7310(10)	,	7310(10)	$(5/2^-, 7/2^-)$	7314(6)		
		7380(30)	7380(10)	$5/2^{+}$	7380(10)	5/2+	7388(5)		
			7480(10)	- , =	7480(10)	$(5/2^-, 7/2^-)$	7468(10)		
			7635(10)		7635(10)	$(5/2^-, 7/2^-)$	7610(12)		
		7700(30)	7711(10)	$5/2^{+}$	7711(10)	$3/2^+, 5/2^+$	7737(14)		
			7773(10)	-,-	7773(10)	-,-,-,-	7799(15)		

^aThese are weighted averages between the results of previous ${}^{40}Ca({}^{3}He, \alpha){}^{39}Ca$ measurements of Refs. [32–35].

Considering all the evidence presented here, and to be conservative, we have claimed the peak denoted by the question mark in Fig. 2 as an unidentified peak. The 6472.2-keV level. Our measured excitation energy of 6472.2(20) keV does not agree within 2σ with $E_x = 6450(2)$ keV [21,22]. The latter measurement was carried out with three different beam energies, including 27.17 MeV.

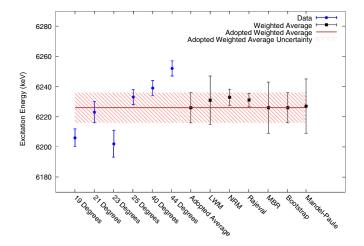


FIG. 4. The individual calibrated energies (in keV, denoted by blue circles with error bars) at indicated θ_{lab} for the peak denoted by the question mark in Fig. 2, assuming it belongs to ³⁹Ca. In the latter case, a weighted average energy of 6226(10) is adopted in the present work. The weighted average energies computed using different methods are also shown (black squares with error bars). The thick solid brown line is the adopted weighted average energy (from the bootstrap method). The red hatched band represents the uncertainty in the adopted weighted average energy.

This value was chosen by Lotay et al. to cover the centerof-mass energy range of 689 ± 13 keV across the volume of the DRAGON gas target [21], and they observed a resonance at 679(2) keV [corresponding to $E_x = 6450(2)$ keV], which was located downstream the center of the gas target. It seems unlikely for the 679-keV resonance to be the same state as the 701.3-keV resonance, which is the center-of-mass energy equivalent to the 6472.2-keV state observed in the present work. The 701.3(25)-keV¹ resonance is within the center-ofmass energy window of the measurement of Refs. [21,22]. However, there are two issues here: (a) The 701.3-keV resonance would have been placed at the very beginning of the DRAGON extended gas target, where the gas density is not homogenized or even optimized due to differential pumping system. This is clearly observed from panel (b) of Fig. 3 in Ref. [22]. (b) Even if we do not consider the dramatic drop in the gas density, and the resultant change in the stopping powers, where the 701.3-keV resonance would have been located, the DRAGON recoil acceptance is usually set for a resonance near the center of the gas target [47]. So, the measurement of Refs. [21,22] would most likely be insensitive to recoils from the 701.3-keV resonance located at the beginning of the DRAGON gas target. Therefore, it is not surprising that the 701.3-keV resonance was not observed in the measurement of Refs. [21,22]. The present result for $E_x = 6472.2(20)$ keV agrees with $E_x = 6467(10)$ keV [37] and 6450(30) keV [36].

B. Spin-parities of ³⁹Ca excited states

To determine the spin-parity values of the 39 Ca states observed in the present work, the differential cross sections in the laboratory system were obtained from the procedure presented in Ref. [48]. The measured differential cross sections in the laboratory system were converted to those in the center-of-mass system following the formalism presented in Appendix C of Ref. [49].

The theoretical angular distributions of the (³He, α) cross sections were also computed via distorted-wave Born approximation (DWBA) calculations using the one-step finite-range transfer formalism described in Ref. [50]. DWBA calculations were performed using FRESCO [51].

The distorted waves in the entrance and exit channels were calculated using global optical interaction potentials given in Table II.

Following Ref. [54], the α -particle wave functions were computed from the ³He + *n* interaction assuming a Gaussian potential of the form

$$V(r) = -V_G \exp\left(-\frac{r^2}{R_G^2}\right),\tag{1}$$

where $R_G = 2.452$ fm [54], while the potential depth V_G was varied to reproduce the $S_n({}^4\text{He}) = 20.5776$ MeV [20], where S_n is the neutron separation energy.

To describe the interaction of ${}^{\overline{39}}Ca + n \rightarrow {}^{40}Ca$, a volume Woods-Saxon potential of the form

$$V(r) = \frac{V_R}{1 + \exp\left(\frac{r - r_{0R} A_T^{1/3}}{a_R}\right)},$$
 (2)

where index *R* refers to the real part of the potential, r_{0R} was considered to be equal to 1.25 fm for the present analysis, a_R is the diffuseness parameter set equal to 0.65 fm here, and A_T is the mass of target (equal to 39 for ³⁹Ca). The real depth of the potential is described by V_R and was varied to reproduce the correct values of neutron binding energies of 15 635.0(6) keV [20] in the ⁴⁰Ca nucleus when both ³⁹Ca and ⁴⁰Ca are in their ground states, and 15 635 keV + E_x (³⁹Ca) when ³⁹Ca is in an excited state with energy E_x (in keV).

The theoretical angular distribution curves obtained from FRESCO were normalized to the center-of-mass experimental differential cross sections using linear fits with zero intercepts. Finally, DWBA calculations were performed for the first four bound states (including the ground state) of ³⁹Ca with known spin-parity to confirm the validity of the optical potential models used. The J^{π} values obtained from the present work for these cases agree with those found in Ref. [27]. We have also investigated the spin-parity of the present 5537-keV state to be more confident that we can assume it may be the same state as the 5588-keV state observed by Matoba *et al.* [37].

Figures 5 and 6 show the present α angular distribution plots for the first four ³⁹Ca bound states, the 5537-keV state, as well as those ³⁹Ca proton resonances (observed in at least five angles) which lie within the energy window important for determination of the ³⁸K(p, γ)³⁹Ca reaction rate in the nova temperature regime (see Sec. III C). In what follows, we briefly compare the spin-parities derived in the present

¹The uncertainty in the resonance energy comes from the quadratic sum of ΔE_x for the 6472.2-keV state, the uncertainty in the *Q*-value of the ³⁸K(*p*, γ) reaction, and the present ±1.4-keV systematic uncertainty in the excitation energy.

Reaction channel	V _R (MeV)	<i>r_R</i> (fm)	a_R (fm)	V _I (MeV)	<i>r_I</i> (fm)	<i>a</i> _{<i>I</i>} (fm)	W _D (MeV)	<i>r</i> _D (fm)	<i>a</i> _D (fm)	V _{so} (MeV)	r _{so} (fm)	a _{so} (fm)	<i>r</i> _{0c} (fm)	$E_{beam}^{ m lab}$ (MeV)
3He + 40Caa $4He + 39Cab$	148.33 160.9	1.2 1.3421	0.72 0.6578	34.77 0	1.4 1.4259	0.88 0.5587	25.9079	1.2928	0.6359	2.5 0	1.2 1.2686	0.72 0.85	1.3 1.35	21 21

TABLE II. Global optical potential model parameters for the present DWBA analysis. The potential depths were varied to reproduce the correct binding energies corresponding to each channel. For neutron binding potential, see text.

^aAdopted from Ref. [52].

^bAdopted from Ref. [53].

work with those of the previous measurements. Considering that neither our beam nor our target was polarized, l + s and l - s transitions, where l is the orbital angular momentum and s = 1/2 is the spin of the transferred neutron, could not be differentiated.

The first four bound states. The spin-parities of these states are already known, and our angular distribution plots agree with the known assignments [see panels (a) to (d) of Fig. 5]. For the ground and first excited states of ³⁹Ca, our theoretical DWBA fits are much higher than the data at large angles [see panels (a) and (b) of Fig. 5]. This is a common feature of transfer measurements, where the DWBA approximation is known to poorly reproduce large-angle cross sections.

The 5537-keV state. Even though the energy of this state is inconsistent with that previously measured [37] (see Table I), the spin-parity assignments of $J^{\pi} = 3/2^+$, $5/2^+$ obtained in Ref. [37] agree well with our angular distribution data for this state [see panel (e) of Fig. 5].

The 6083-keV state. A tentative $J^{\pi} = (1/2^+)$ assignment is associated with this state [37]. We have obtained DWBA fits [see panel (g) of Fig. 6] for $J^{\pi} = 1/2^+$, $1/2^-$ (identical to $3/2^-$), $3/2^+$ (identical to $5/2^+$), $5/2^-$ (identical to $7/2^-$), $7/2^+$ (identical to $9/2^+$), and $9/2^-$ (identical to $11/2^-$). Out of all these assignments, the best fit is obtained for $J^{\pi} = 7/2^+$, $9/2^+$. These two identical fits give the minimum $\chi^2/\nu = 8.8$. The χ^2/ν for $J^{\pi} = 1/2^+$ is a factor of 4 larger. Thus, we have assigned a tentative $J^{\pi} = (7/2^+, 9/2^+)$ to

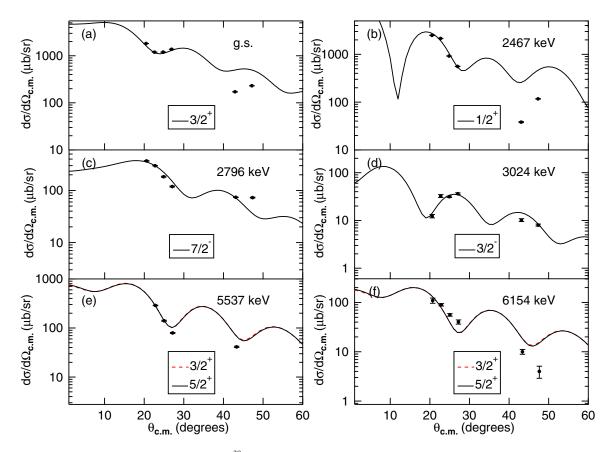


FIG. 5. α angular distributions populating states of ³⁹Ca compared with the DWBA curves (in black or red) calculated using FRESCO [51]. The filled circles with error bars are the measured differential cross sections (in the center-of-mass system) of the α particles from the ⁴⁰Ca(³He, α)³⁹Ca reaction. If not shown, the error bar is smaller than the point size.

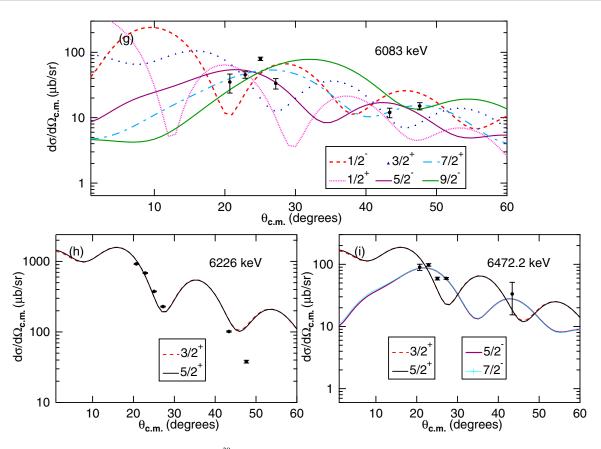


FIG. 6. α angular distributions populating states of ³⁹Ca compared with the DWBA curves (in black or color) calculated using FRESCO [51]. The filled circles with error bars are the measured differential cross sections (in the center-of-mass system) of the α particles from the ⁴⁰Ca(³He, α)³⁹Ca reaction. If not shown, the error bar is smaller than the point size. Panel (h) refers to the peak denoted by the question mark in Fig. 2 under the assumption that it belongs to ³⁹Ca.

this state. It should be noted that the uncertainties on the cross sections provided in Figs. 5 and 6 are only based on statistical uncertainties on the areas of the peaks, which are rather small. Furthermore, DWBA fits rarely pass through all the data points and they are dominated by uncertainties in the optical model; thus, it is unlikely to obtain a χ^2/ν close to one without these contributions.

The 6154-keV state. This state is known to be a $5/2^+$ state [27]. This assignment agrees well with the present α angular distribution data at lower angles [see panel (f) of Fig. 5]. However, our theoretical DWBA calculations are higher than the experimental data at larger angles. Also, we cannot distinguish between $5/2^+$ and $3/2^+$ assignments.

The 6472.2-keV state. The spin-parity assignment of this state is determined as $J^{\pi} = 3/2^+$, $5/2^+$ based on the measurements of Refs. [36,37]. These two assignments cannot be immediately rejected from the present α angular distribution data based on visual inspection of the fits; however, much better fits are obtained with $J^{\pi} = 5/2^-$, $7/2^-$ [see panel (i) of Fig. 6]. The χ^2/ν 's of our fits are $\chi^2/\nu = 100$ for $J^{\pi} = 3/2^+$, $5/2^+$ and $\chi^2/\nu = 10$ for $J^{\pi} = 5/2^-$, $7/2^-$. $J^{\pi} = 1/2^{\pm}$, $3/2^-$, $7/2^+$, $9/2^{\pm}$, and $11/2^{\pm}$ were also fitted to the present α angular distribution data. But they all resulted in having $\chi^2/\nu \gg 10$. We have therefore adopted a tentative assignment of $(5/2^-, 7/2^-)$ for this state. Considering that the present assignment differs from that assumed for the

6450(2)-keV state of Refs. [21,22], it is less likely that these two states are the same.

A future measurement of the α angular distributions from the ${}^{40}\text{Ca}({}^{3}\text{He}, \alpha)$ reaction at laboratory angles lower than 19° could help make definite conclusions on spin-parity assignments of the 6083- and 6472.2-keV states.

C. The ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction rate

Over the temperatures characteristic of explosive hydrogen burning in novae, the Gamow window [49] for the ³⁸K(p, γ)³⁹Ca reaction (Q = 5770.92(63) keV [20]) spans $E_{cm} = 140-615$ keV. Therefore, the ³⁸K(p, γ)³⁹Ca reaction rate is dominated by contributions from isolated and narrow ³⁸K + p resonances corresponding to ³⁹Ca excited states with 5911 $\leq E_x \leq 6386$ keV. In particular, the largest impact on the ³⁸K(p, γ)³⁹Ca reaction rate comes from those excited states within this energy range with $J^{\pi} = 5/2^+$ and $7/2^+$, as such states correspond to l = 0 proton captures on the ground state of ³⁸K with $J^{\pi} = 3^+$.

Table I shows that there are five states in the region $5911 \leq E_x \leq 6386$ keV. The 5908- and 6001-keV states have unknown spin-parities. The 6083-keV state has a tentative $7/2^+$, $9/2^+$ assignment, and the 6154- and 6286-keV [37] states have $J^{\pi} = 3/2^+$, $5/2^+$ assignments. These states are

	From Re	f. [22]		Present work				
E_x (keV)	E_r (keV)	$\omega\gamma$ (meV)	J^{π}	E_x (keV)	E_r (keV)	$\omega\gamma$ (meV)	J^{π}	
6157(10) ^a	386(10)	≤2.54 ^b	$5/2^{+}$	6154(5)	383(5)	≤2.6	$5/2^{+}$	
6286(10) ^a	515(10)	≼18.4 ^b	$5/2^{+}$	6286(10) ^a	515(10)	≼18.4 ^b	$5/2^{+}$	
6450(2) ^c	679(2) ^d	120(25) ^d	$5/2^+$	6472.2(24)	701.3(25)	126(39)	$(5/2^{-})$	

TABLE III. ³⁹Ca level parameters for the ³⁸K(p, γ) ³⁹Ca resonant reaction rate. The ±1.4-keV systematic uncertainty in the present work is added in quadrature to the uncertainties in E_x given in Table I.

^aAdopted from Ref. [19]. Resonance was not observed.

^bThis value is the upper limit at 90% confidence level [22].

^cDerived from the measured resonance energy [21,22].

^dSee text in Sec. III C regarding the uncertainty.

candidates for dominating the ${}^{38}K(p, \gamma){}^{39}Ca$ reaction rate over the nova temperature regime.

The existence of the 5908-keV state is tentative. Furthermore, nothing is known about the decay schemes, γ branching ratios, lifetimes, or proton spectroscopic factors of the 5908-, 6001-, and 6083-keV levels. Moreover, mirror and/or isobaric analog levels of these states are also unknown. Therefore, their proton and γ widths, and thus resonance strengths, cannot be reliably estimated. In conclusion, we do not have sufficient information to make educated guesses about the properties of these three proton unbound states in ³⁹Ca.

We have therefore followed Refs. [21,22] and have calculated the contributions of the two remaining levels (at 6154(5)keV from the present work and 6286(10) keV observed in Ref. [37]) to the ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction rate. Furthermore, to be consistent with Refs. [21,22] for reaction rate calculation, we will similarly also included the higher energy resonance corresponding to the present 6472.2(24)-keV state² in the calculation of the ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction rate even though it falls outside the range of interest in ³⁹Ca over the nova temperature regime. The resonance parameters for these states are given in Table III.

The strengths of the 383- and 701.3-keV resonances from the present work were scaled from those provided in Ref. [22]. That study has used the method of thick target yield curve to compute resonance strength from [22]:

$$\omega\gamma = \frac{2N_r\epsilon}{N_b\eta\lambda^2},\tag{3}$$

where N_r and N_b are number of recoils and beam particles, respectively; ϵ is center-of-mass stopping power; η is heavy ion detection efficiency; and λ is the center-of-mass de Broglie wavelength.

In the above formula, ϵ , η , and λ are the energy -dependent factors. Reference [22] provides stopping powers for three different beam energies in the laboratory system. These were used to obtain a linear fit between ϵ and energy. Heavy ion detection efficiency is only given for one beam energy corresponding to the only resonance observed [22]. We have thereby considered η to be a constant over the small energy difference considered here. Finally, the center-of-mass de Broglie wavelength can be calculated at each resonance energy.

The scaled resonance strengths for the 383- and 701.3-keV resonances are also given in Table III. The uncertainties in these values come from propagating the 1σ uncertainties on the $\omega\gamma$, ϵ , and E_r quantities from Ref. [22] together with those on the present E_r 's and the scaled ϵ 's. We have adopted the 515(10)-keV resonance from the excitation energy of 6286(10) keV measured in Ref. [37], and its strength is adopted from the upper limit derived in Ref. [22]. Lastly, for the $E_r = 679^{+2}_{-1}$ (stat.) ± 1 (sys.) keV and $\omega \gamma = 120 \pm$ $20(\text{stat.}) \pm 15(\text{sys.}) \text{ meV}$ values measured in Refs. [21,22], the statistical and systematic uncertainties are added together in quadrature to derive the final uncertainties in the resonance energy and strength for the 679-keV resonance.

For the 383- and 515-keV resonances in Table III, we have assumed a spin-parity of $5/2^+$ instead of $3/2^+$ because the corresponding resonance strengths given in Ref. [22] were obtained assuming the spin-parities of $5/2^+$. Also, this assignment is consistent with an l = 0 transfer in the ³⁸K + p system, whereas a $J^{\pi} = 3/2^+$ state in ³⁹Ca corresponds to an l = 2 transfer, which makes the contribution of such a resonance to the 38 K (p, γ) 39 Ca reaction rate less important. With these, the total 38 K (p, γ) 39 Ca resonant reaction rate

was calculated analytically [55]:

$$N_{A} \langle \sigma \upsilon \rangle_{r} = \frac{1.5399 \times 10^{11}}{T_{9}^{3/2}} \left(\frac{M_{0} + M_{1}}{M_{0}M_{1}}\right)^{3/2} \\ \times \sum_{i} (\omega \gamma)_{i} \exp\left(\frac{-11.605E_{i}}{T_{9}}\right), \quad (4)$$

where $N_A \langle \sigma \upsilon \rangle_r$ is the resonant reaction rate (in cm³ mol⁻¹ s⁻¹); T_9 is the temperature (in GK), M_0 and M_1 are the masses (in amu) of the proton and ³⁸K, respectively, $(\omega \gamma)_i$ is the strength of resonance *i* (in MeV), and E_i is the energy of resonance i (in MeV).

Figure 7(a) compares the ratio of individual upper limit resonance contributions for the resonances listed in Table III (under the present work column) to the total recommended resonant rate. Under this assumption, the 383-keV resonance entirely dominates the ${}^{38}K(p, \gamma){}^{39}Ca$ reaction rate over the nova temperature regime, while the contributions of the 515- and 701.3-keV resonances to the total ${}^{38}\text{K}(p,\gamma){}^{39}\text{Ca}$

²The ± 1.4 -keV systematic uncertainty in the present work is added in quadrature to the uncertainty given in Table I.

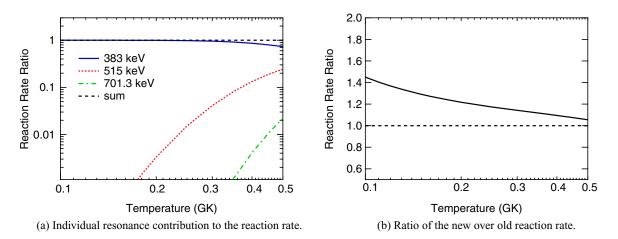


FIG. 7. Left panel: The thick solid blue, curved dotted red and curved dash-dotted green lines are the ratios of upper limit resonance contributions for the 383-, 515-, and 701.3-keV resonances, respectively (see Table III), to the sum of all three contributions. The latter (denoted by the straight dashed black line) is the total ${}^{38}K(p, \gamma) {}^{39}Ca$ resonant reaction rate, which is entirely dominated by the 383-keV resonance over the temperatures characteristic of explosive hydrogen burning in novae. Both axes are on logarithmic scale. Right panel: The thick solid black line represents the ratio of the present total resonant ${}^{38}K(p, \gamma) {}^{39}Ca$ reaction rate to that of Ref. [22]. The former is higher than the latter by up to a factor of 1.4. The *x* axis is on logarithmic scale.

resonant rate do not start until temperatures much higher than those of interest for novae.

The present total recommended ${}^{38}K(p, \gamma){}^{39}Ca$ resonant reaction rate is compared with that of Ref. [22] in Fig. 7(b). Even though the reaction rate is dominated by the 383-keV resonance over the nova temperature regime, and the energy of this resonance from the present work is only 3 keV lower than that used in Ref. [22], our recommended rate is higher in the temperature regime of interest for novae by at most a factor of 1.4 at 0.1 GK. This is because the present reaction rate is calculated based on scaled upper limit resonance strengths, and the contribution of the 515-keV resonance to the reaction rate starts to be significant (33%) compared to that of the 383-keV resonance at 0.5 GK, which is beyond the temperature range of interest for the hottest novae. Since the 383-keV resonance energy is lower compared to that used for rate calculations in Ref. [22], the present reaction rate is higher than that of Ref. [22] because the resonance energy enters Eq. (4) with a negative sign.

IV. CONCLUSIONS

In the present work, we have presented the results of a charged-particle spectroscopy experiment to study the level structure of ³⁹Ca using the ⁴⁰Ca(³He, α) ³⁹Ca reaction measured with the Enge split-pole spectrograph at TUNL.

The level structure of ³⁹Ca above the proton threshold at 5770.9 keV is important in determination of the ³⁸K(p, γ)³⁹Ca thermonuclear reaction rate at temperatures characteristic of explosive hydrogen burning in novae.

Our measured excitation energies of ³⁹Ca states agree within $1\sigma - 2\sigma$ with the results of previous measurements for most of the states. However, two of the states (at $E_x = 5537$ and 6472.2 keV) do not agree with those previously measured.

The 5537-keV state is inconsistent with the 5588(10)-keV state measured in Ref. [37]. In that work, the state was only

weakly populated and no excitation energy uncertainties were reported in the original work [37]. Its spin-parity assignment agrees well with that of the present 5537-keV state.

The excitation energy of the present 6472.2-keV state is consistent with the energies measured in Refs. [36,37] but is 22 keV higher than that measured in Refs. [21,22], assuming they are the same state.

In addition, we have observed a peak where the 6286-keV [37] state was expected to be populated with a 47-keV kinematic shift. ³⁹Ca remains the most probable origin of this peak amongst the contaminants considered. However, we conservatively label it as unidentified in our analysis. Future measurements are warranted to confirm the origin of this peak.

We have also observed a tentative weak state at 5908 keV, which may be a new state in 39 Ca. A recent charged-particle spectroscopy measurement on 39 Ca [56] with even higher energy resolution than that of the present work may shed light on these issues.

Spin-parities of a few of the proton resonances of ³⁹Ca significant for nova nucleosynthesis have been determined in the present work from DWBA calculations using FRESCO [51]. The results agree for most but not all cases with the values previously determined in other measurements [27].

Finally, the total resonant 38 K (p, γ) 39 Ca reaction rate was determined in the present work at temperatures characteristic of explosive hydrogen burning in novae using three resonances at 383-, 515- and 701.3-keV. The resultant rate is higher than that previously determined [22] by up to a factor of 1.4 due to the fact that our resonance energy for the dominant resonance is lower than that used in Ref. [22]. The strengths of the 383-, and 515-keV resonances are not measured yet. The present result for the 38 K (p, γ) 39 Ca reaction rate intrinsically depends on the upper limit resonance strengths estimated in Ref. [22].

Regarding the present 701.3-keV resonance, the measurement of Ref. [22] would not have been optimized for observing this resonance since it would have been located at the beginning of the DRAGON gas target, where the gas density is not uniform. In addition, the DRAGON's acceptance would not have been set to receive the potentially measurable recoils from this resonance due to its distance from the center of the gas target.

Finally, we would like to highlight the fact that the other low energy resonances corresponding to the tentative 5908-, 6001, and 6083-keV states could also be very important for determination of the ³⁸K(p, γ)³⁹Ca reaction rate at the nova temperature regime. They have been left out of the present rate calculation due to their unknown properties. Therefore, further high resolution study is merited to measure the spinparities and proton and γ widths of these proton resonances, and to look for potentially unobserved low spin resonances in PHYSICAL REVIEW C 98, 055804 (2018)

³⁹Ca. We furthermore suggest that an independent nova model calculation to study the effects of the ³⁸K(p, γ) ³⁹Ca reaction rate on nova abundances be postponed until these issues are resolved.

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