Application of isochronous mass spectrometry for the study of angular momentum population in projectile fragmentation reactions

X. L. Tu,^{1,2,3} A. Kelić-Heil,² Yu. A. Litvinov,^{1,2,3} Zs. Podolyák,⁴ Y. H. Zhang,¹ W. J. Huang,^{1,5,6} H. S. Xu,¹ K. Blaum,³ F. Bosch,² R. J. Chen,¹ X. C. Chen,^{1,2,5} C. Y. Fu,¹ B. S. Gao,^{1,2,3,5} Z. Ge,¹ Z. G. Hu,¹ D. W. Liu,¹ S. A. Litvinov,² X. W. Ma,¹ R. S. Mao,¹ B. Mei,² P. Shuai,^{1,7} B. H. Sun,⁸ Y. Sun,^{1,9} Z. Y. Sun,¹ P. M. Walker,⁴ M. Wang,¹ N. Winckler,² J. W. Xia,¹ G. Q. Xiao,¹ Y. M. Xing,¹ X. Xu,^{1,5} T. Yamaguchi,¹⁰ X. L. Yan,^{1,3,5} J. C. Yang,¹ Y. J. Yuan,¹ Q. Zeng,^{1,7} W. Zhang,^{1,5} H. W. Zhao,¹ T. C. Zhao,¹ and X. H. Zhou¹

¹Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, People's Republic of China

²GSI Helmholtzzentrum für Schwerionenforschung, Planckstraße 1, 64291 Darmstadt, Germany

³Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany

⁴Department of Physics, University of Surrey, Guildford GU2 7XH, United Kingdom

⁵Graduate University of Chinese Academy of Sciences, Beijing, 100049, People's Republic of China

⁶CSNSM, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, 91405 Orsay, France

⁷University of Science and Technology of China, Hefei 230026, China

⁸School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, People's Republic of China

⁹Department of Physics and Astronomy, Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China

¹⁰Department of Physics, Saitama University, Saitama 338-8570, Japan

(Received 2 September 2016; published 26 January 2017)

Isochronous mass spectrometry was applied to measure isomeric yield ratios of fragmentation reaction products. This approach is complementary to conventional γ -ray spectroscopy in particular for measuring yield ratios for long-lived isomeric states. Isomeric yield ratios for the high-spin $I = 19/2\hbar$ states in the mirror nuclei ⁵³Fe and ⁵³Co are measured to study angular momentum population following the projectile fragmentation of ⁷⁸Kr at energies of ~480A MeV on a beryllium target. The 19/2 state isomeric ratios of ⁵³Fe produced from different projectiles in the literature have also been extracted as a function of mass number difference between projectile and fragment (mass loss). The results are compared to ABRABLA07 model calculations. The isomeric ratios of ⁵³Fe produced using different projectiles suggest that the theory underestimates not only the previously reported dependence on the spin but also the dependence on the mass loss.

DOI: 10.1103/PhysRevC.95.014610

I. INTRODUCTION

Fragmentation nuclear reactions are often used at intermediate and high projectile energies (typically 50A-1500A MeV) to produce exotic nuclei. In the reaction process, some nucleons of the projectile are abraded at the overlapping zone between the target and projectile nuclei. As a consequence, the remaining projectile is highly excited and promptly deexcites by evaporating nucleons until a final fragment is formed with an excitation energy below the particle emission threshold [1]. The projectile fragments are characterized by relatively small angular and energy dispersion and show a very strong kinematical focusing to forward angles.

In combination with an in-flight spectrometer, which takes advantage of the reaction kinematics, one can separate nuclei of interest on very short time scales down to a few 100 ns [2]. The projectile fragmentation reaction has been proven to be an important tool for producing nuclei far from stability. It is considered to be one of the main reactions to produce even more exotic systems at the next-generation radioactive beam facilities, such as the GSI Facility for Antiproton and Ion Research (FAIR) [3] and the Heavy-Ion Advanced Research Facility (HIAF) at the Institute of Modern Physics (IMP) in China [4], where one of the goals is to investigate nuclides around the r-process path of stellar nucleosynthesis [5].

The production cross sections σ [6], momentum distributions *P* [7], and angular momenta *J* [8] of the produced fragments are basic properties of the fragmentation reaction. Their knowledge is indispensable for the understanding of the collision process and, in turn, is essential for the design and operation of the fragment separator facilities.

Population of a particular excited state with a given angular momentum J usually cannot be measured in experiment due to its prompt deexcitation (<10 ns) [9]. However, the production cross sections and momentum distributions of the deexcited nuclei in a ground or long-lived isomeric state are routinely measured. It is well established that the isomers are produced in the projectile fragmentation reaction [10]. The promptly decaying excited states may feed an isomeric state which then survives until the measurement is performed. By assuming that all excited states with J ($J > J_m$) eventually decay to the isomeric state of interest with J_m , the measured isomeric yield ratio, which is the number of nuclei populated in an isomeric state relative to their total number, reveals the integrated population probability of the states having the excitation energies $E^* \ge E_m^*$ and angular momenta $J \ge J_m$, where E_m^* indicates the excitation energy of isomer. Thus an integral population probability of high angular momentum can be deduced from experiment.

Recently, isomeric yield ratios have been obtained from γ -ray spectroscopy investigations of angular momentum

populations of projectile fragments [9-18]. γ -ray spectroscopy is a powerful technique, which provides valuable contributions to nuclear structure investigations. However, it is typically limited to studies of excited states with half-lives between about 100 ns and several milliseconds [10,11]. The lower halflife limit is given by the time of flight through a beam line and the upper limit is determined by the need to correlate delayed γ rays with individual ions in a segmented implantation detector with a technologically limited number of pixels [11].

The latter limitation can be overcome using other experimental techniques. A nuclear isomer has the same number of protons and neutrons as the corresponding nuclear ground state but possesses an excitation energy, which is reflected in a heavier mass. The mass difference between isomeric and ground states can directly be resolved by high-resolution mass spectrometry. Recently, numerous isomers were investigated with storage-ring [19,20] and Penning-trap [21,22] mass spectrometry.

In the case of a storage ring, the experiments are performed at high energies employing highly charged ions. The revolution times T of various stored ions are related (in first order) to their mass-to-charge ratios m/q via [23]

$$\frac{\Delta T}{T} = \frac{1}{\gamma_t^2} \frac{\Delta(m/q)}{(m/q)} - \left(1 - \frac{\gamma^2}{\gamma_t^2}\right) \frac{\Delta v}{v},\tag{1}$$

where γ is the relativistic Lorentz factor and γ_t denotes the transition energy of the storage ring. To resolve and determine m/q values by the revolution times of the ions, the term containing their velocity spreads, $\Delta v/v$, needs to be made negligibly small. For this purpose, two complementary experimental techniques have been developed, namely, Schottky mass spectrometry (SMS) and isochronous mass spectrometry (IMS) [23].

In the IMS ion-optical mode, the energy of the stored ions of interest is chosen such that $\gamma \approx \gamma_t$. This leads to the situation that a faster ion of a given ion species moves on a longer orbit and a slower ion of the same ion species moves on a shorter orbit, such that the velocity difference is compensated for by the lengths of the closed orbits [23]. This means that the revolution times reflect directly the m/qratios of the stored ions independently of their $\Delta v/v$. A mass resolving power of 200 000 (FWHM) has been achieved almost over the entire spectrum with precise $B\rho$ determination at the dispersive midplane of the fragment separator (FRS) [24,25], which allows us to resolve isomers with excitation energies of several hundred keV, dependent on the charge state of the isomer.

In γ -ray spectroscopy, the produced isomers are implanted in a catcher and are thus present as neutral atoms. In a storage ring the isomeric states can be stored as fully stripped ions, thus providing the advantage that the internal conversion channel is disabled. The latter is helpful for cases where the internal conversion coefficients are experimentally unknown [15]. Owing to dedicated time-of-flight detectors, IMS has a very high detection efficiency and is sensitive to single stored ions [26]. Furthermore, an experimental cooler storage ring (CSRe) tuned into the IMS ion-optical mode can simultaneously store ions with a relative momentum acceptance $\Delta P/P$ of $\sim 0.2\%$ [27]. The latter is important in view of the wide velocity distribution of projectile fragments. These capabilities were employed to investigate properties of the projectile fragmentation reaction. For instance, relative production cross sections of the fragments were measured and a relationship of the relative odd-even staggering of yields versus the particle-emission threshold energies was established [28].

IMS can be applied to short-lived nuclides with half-lives down to $\sim 50 \ \mu s$ [29]. Furthermore, there is no upper half-life limitation. In this respect IMS is a complementary technique to γ -ray spectroscopy for the investigation of angular momentum populations. This is illustrated here with the example of the measured population of the high-spin $I = 19/2\hbar$ states in the mirror nuclei 53Fe and 53Co. The half-lives of the excited states are 2.54 m and 247 ms [30], respectively. Moreover, in the present work we investigate the relation between the isomeric ratios for a given spin and the mass loss. The question of how the isomeric yield ratio depends on the mass loss is not only related to the understanding of the origin of angular momentum, but also plays an important role in the production and application of isomeric beams [31] as well as spin-aligned beams [32]. In previous works [9–18], nuclides with the same spin had different structures and different isomer excitation energies, which masked a possible dependence of the isomeric ratios on the mass loss [11,33]. Thus, to remove the nuclear structure effects, we use the isomeric ratio values of the high-spin isomeric 19/2 state in ⁵³Fe produced using different projectiles: ⁵⁸Ni (Ref. [34]), ⁷⁸Kr (present work), ⁸⁴Kr (Refs. [35,36]), and ¹¹²Sn (Ref. [37]). We note that the same method was used to study the relation between the isomeric ratios and the mass loss in ⁴⁴Sc for the photonuclear reaction [38].

II. EXPERIMENT AND DATA ANALYSIS

The experiment was performed at the HIRFL-CSR (coolerstorage ring at the Heavy Ion Research Facility in Lanzhou) [27]. The CSRe was operated in the isochronous mode to measure masses of short-lived $T_z = -1/2$ [39] and $T_z = -3/2$ [40] nuclei. Many of these masses are decisive for the understanding of astrophysical nucleosynthesis and nuclear structure [39–42]. In this experiment, a primary 78 Kr²⁸⁺ beam at an energy of 479.4A MeV was extracted from the main storage ring (CSRm) and focused upon a ~ 2.77 g/cm² beryllium production target placed at the entrance of the radioactive beam line (RIBLL2). ⁵³Fe and ⁵³Co nuclides were produced via projectile fragmentation reactions. According to CHARGE calculations [43] at this kinetic energy more than 99.9% of Fe and Co fragments emerged from the target as fully stripped nuclei. Any contributions of other atomic charge states can be neglected in the present context. The fragments were separated in flight with RIBLL2 and then injected into the CSRe. To enable IMS, the CSRe was tuned to store ions at $\gamma_t \approx 1.4$. According to calculations with the LISE++ code [7,44], the longitudinal momenta of ⁵³Fe and ⁵³Co nuclei emerging from the target are almost identical. However, the charge state 26^+ for fully ionized ⁵³Fe is different from 27^+ for 53 Co. Thus, the magnetic rigidities of the RIBLL2 and CSRe facilities were sequentially set to 6.1994 Tm and

5.9708 Tm, respectively, to center $(dP/P_c = 0)$ the ⁵³Fe and ⁵³Co fragments, respectively. The production cross section of ⁵³Fe is sufficiently large so that the ⁵³Fe nuclei with momenta far from the central one $(dP/P_c = -3.6\%)$ could be measured in the CSRe at the magnetic rigidity of 5.9708 Tm corresponding to the central setting for ⁵³Co. The details of standard IMS measurements in the CSRe can be found in Refs. [26,45]. The revolution times of the stored ions were measured by a dedicated timing detector, see Refs. [26,46,47] for more details on the detector design and performance.

Each stored ion passed through the thin carbon foil of the timing detector at every revolution. Secondary electrons released from the foil due to the passage of each ion were guided to a set of microchannel plates thus providing timing signals. The signals from individual ions are periodic which is used to determine their revolution frequencies. The detector efficiency ranges from 20% to 70% depending on the ion species and ion number [26,47]. However, since each stored ion is recorded for ~320 turns, a detection efficiency of 100% can safely be assumed for all ions [48].

Owing to the high mass resolving power achieved in these IMS measurements of about 170 000 [45], the mass difference of \sim 3 MeV [30] between the isomeric and ground states can clearly be resolved. The revolution time spectra of the isomeric and ground states for ⁵³Fe and ⁵³Co are shown in Fig. 1.

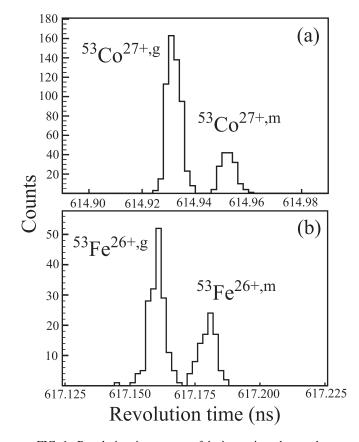


FIG. 1. Revolution time spectra of the isomeric and ground states of 53 Co and 53 Fe nuclides measured in the present work. The mass difference of \sim 3 MeV between the isomeric and ground states is reflected in a time difference of \sim 20 ps.

The ultimate efficiency of the experimental method allows the highly accurate counting of the number of stored ions in the ground and isomeric states. The experimental isomeric ratios R_{expt} are defined as the number N_{Jm} of nuclei stored in the isomeric state relative to the total number N_{all} of stored nuclei in ground and isomeric states as follows:

$$R_{\text{expt}} = \frac{N_{Jm}}{N_{\text{all}}}.$$
 (2)

The ⁵³Fe and ⁵³Co nuclides were stored as bare nuclei. The lifetimes of the isomeric and ground states are much longer than the typical measuring time of 200 μ s. Therefore, the internal conversion and β decays during the measuring time can be neglected. The relative mass difference of isomeric and ground states for ⁵³Fe and ⁵³Co is about 6 × 10⁻⁵, respectively. Thus, the transmission, injection, and storage efficiencies of isomeric and ground states are almost the same and can be neglected in the calculation of R_{expt} for one magnetic rigidity setting in CSRe.

Measured isomeric yield ratios for various dP/P_c settings are listed in Table I. The available results from the experimental storage ring (ESR) at GSI are added as well. The isomeric ratio of 9.6(4)% was obtained in 58 Ni projectile fragmentation at an energy around 370A MeV on a 4 g/cm² beryllium target [34]. For the ⁵⁸Ni experiment the ratio was measured for the central momentum by using SMS at the ESR of GSI [34]. Under the condition of the thick target, the isomeric ratios with a small mass loss are almost independent of the momentum selection [49]. By means of the fragmentation of ⁸⁴Kr projectiles at an energy of 445.3A MeV on a 2.5 g/cm² beryllium production target, an isomeric ratio of 33(4)% was measured for ⁵³Fe by IMS at the ESR with relative longitudinal momentum selection $dP/P_c = 0\%$. More experimental details can be found in Ref. [35]. A ⁵³Fe isomeric ratio of 34(2)% at relative longitudinal momentum selection $dP/P_c = -2.9\%$

TABLE I. Isomeric ratios (R_{expt}) for the 19/2 state with excitation energy of ~3 MeV in ⁵³Fe and ⁵³Co fragments (A_f) were obtained via different projectile (A_p) fragmentation reactions at IMP (this work) and GSI [34,35]. The uncertainties of ratios only include statistical errors. The relative momentum settings (dP/P_c) are listed, where P_c is the central momentum of the fragment after the target calculated by the LISE++ code, and $dP = P - P_c$ is the difference of the central momentum of the corresponding ion optical setting of the facilities.

A _p	E (MeV)	$A_f@P/P_c$	Mass loss	Spin	R _{expt} (%)	Target (g/cm ²)	Ref.
⁵⁸ Ni	$\sim 370A$	$^{53}\mathrm{Fe}\sim\!\!0\%$	5	19/2	9.6(4)	4	[34]
⁷⁸ Kr	479.4A	⁵³ Fe 0%	25	19/2	30(4)	2.77	This work
⁷⁸ Kr	479.4A	⁵³ Fe -3.6%	25	19/2	38(3)	2.77	This work
⁷⁸ Kr	486.4A	⁵³ Fe -2.1%	25	19/2	35(4)	2.77	This work
⁷⁸ Kr	482.9A	⁵³ Fe -4.6%	25	19/2	39(3) ^a	2.77	This work
	445.3A	⁵³ Fe 0%	31	19/2	33(4)	2.50	[35,36]
¹¹² Sn	395.5A	⁵³ Fe -2.9%	59	19/2	34(2)	1.85	[37]
⁷⁸ Kr	479.4A	⁵³ Co 0%	25	19/2	28(14)	2.77	This work
⁷⁸ Kr	482.9 <i>A</i>	⁵³ Co −1%	25	19/2	23(2)	2.77	This work

^aGround and isomeric states were not resolved. The ratio was extracted assuming two overlapping Gaussian functions.

was measured in ¹¹²Sn projectile fragmentation [37]. The ¹¹²Sn beam from CSRm at an energy of 395.5*A* MeV impinged on a 1.85 g/cm² beryllium target placed at the entrance of RIBLL2. The ⁵³Fe ions produced were separated and injected into CSRe by RIBLL2. CSRe was set to an isochronous condition with $\gamma_t = 1.302$ and a magnetic rigidity of $B\rho = 5.306$ Tm. The revolution times for ⁵³Fe were measured by a timing detector, as in the present work described in the experiment section.

III. RESULTS AND DISCUSSION

In this section we address the dependence of the measured isomeric ratios for ⁵³Fe on the longitudinal momentum and on the mass loss.

A. Dependence of isomeric ratio on longitudinal momentum

The dependence of the isomeric ratio on the longitudinal momentum was observed for the first time by Schmidt-Ott et al. [50]. However, the dependence would be washed out for a thick target and large mass loss [33,49]. The relative momentum acceptance of the IMS at CSRe cannot cover the entire relative momentum distribution of the fragments emerging from the target. Thus, the IMS can be used to study the dependence of the isomeric ratio on the momentum. The relation between the isomeric ratios and momentum selection is also addressed in the present work. The isomeric ratios for ⁵³Fe produced by ⁷⁸Kr projectile fragmentation with the same beam energy and the same target thickness amount to 30(4)% for the central setting $(dP/P_c = 0\%)$ and 38(3)%for the setting on the tail of the longitudinal momentum distribution $(dP/P_c = -3.6\%)$. This has to be compared to the relative momentum width of $\sim 5\%$ (FWHM) for 53 Fe fragments emerging from the target. The ratios with different momentum selections and different projectile energies were also measured, see Table I. The results are plotted in Fig. 2 as a function of the relative momentum difference. The ratios of ⁵³Fe for the central settings are slightly smaller than those corresponding to the tails of the momentum distribution. As a conclusion, we see that there is a slight dependence of isomeric ratios on the momentum selection for ⁵³Fe produced via ⁷⁸Kr projectile fragmentation on a 2.77 g/cm² beryllium target.

B. Dependence of isomeric ratio on mass loss

To eliminate the effects of nuclear structure, the isomeric ratios of 53 Fe produced from different projectiles, namely, 58 Ni [34], 78 Kr [this work], 84 Kr [35,36], and 112 Sn [37], were used to study the relation between the ratios and the mass losses. The measured values of the isomeric ratios for 53 Fe are shown in Fig. 3 as a function of the mass loss, which is the difference in mass number between the considered projectile and 53 Fe. It can clearly be seen, that the value of the isomeric ratio increases rapidly with increasing mass loss and reaches an approximate flat top at the mass loss of about 25–30 mass units.

The isomeric ratios for ⁵³Fe deduced from different projectiles as a function of the mass loss have been calculated with the two-stage abrasion-ablation code ABRABLA07 [8,51,52]. Details on the deexcitation part of the ABRABLA07 code can be found in Ref. [52]. We assume that in the case of fragmentation

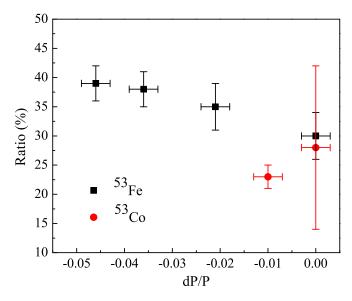


FIG. 2. Isomeric ratios measured in this work as a function of the relative longitudinal momentum selection $(dP/P = [P - P_c]/P_c)$, where *P* and *P_c* are the selected momentum and the central momentum of the fragment, respectively. Both ⁵³Fe and ⁵³Co are produced by ⁷⁸Kr projectile fragmentation on a 2.77 g/cm² beryllium target.

reactions at high projectile energies, the angular momentum removed by particle evaporation is small. Thus we calculate the spin distribution of the final fragment as a superposition of the spins of all prefragments which contribute to the production of the final fragment of interest.

In Fig. 3 we compare the experimental results with the ABRABLA07 predictions for the isomeric ratios of the spin state 19/2 in ⁵³Fe. Qualitatively, the ABRABLA07 calculation

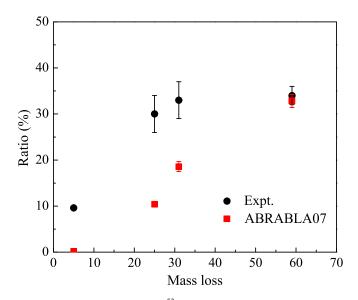


FIG. 3. Isomeric ratios for ⁵³Fe as a function of mass loss compared to the predictions of the ABRABLA07 code. The isomeric ratios rapidly increase with the projectile-fragmentation mass difference and then remain approximately constant.

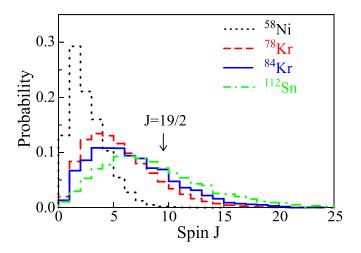


FIG. 4. Production probability of ⁵³Fe vs spin calculated with ABRABLA07 for the projectiles ⁵⁸Ni, ⁷⁸Kr, ⁸⁴Kr, and ¹¹²Sn. Spin 19/2 is indicated with an arrow.

describes the increasing trend of isomeric ratio with mass loss, which indicates that the population of angular momentum in a final fragment has a strong "memory" of the initial angular momentum population in the prefragment. However, quantitatively, except for the largest value of the mass loss, corresponding to ¹¹²Sn projectiles, the calculations underestimate the isomeric ratios: the smaller the mass loss the larger is the fractional discrepancy between the data and calculations (R_{expt}/R_{theor}) . The average square value of the angular momentum projection of a nucleon $\langle j_z^2 \rangle$ is about 2.54 for the ⁵⁶Ni region in the ABRABLA07 statistical model [8]. However, the isomer of spin state 19/2 has a three-particle configuration in the case of ⁵³Fe, each in the high angular momentum $f_{7/2}$ orbital [53]. Therefore the angular momentum per nucleon is much larger than the $\sqrt{\langle j_z^2 \rangle}$, which may explain why the ABRABLA07 prediction is so low for the ⁵⁸Ni case.

It has already been noticed, see, e.g., Ref. [18], that for high-spin states the values of isomeric ratios calculated with the ABRABLA code are lower than the measured ones. This is consistent with the present case, since the probability to produce higher spin states depends on the mass loss. Figure 4 illustrates the probabilities to produce ⁵³Fe with different spins for different projectiles calculated with the ABRABLA07 code. It can be seen that the spin 19/2 can hardly be produced for a small mass loss (⁵⁸Ni projectiles). However, it is easily produced for larger mass losses (Kr and Sn projectiles). The observation of this work suggests that the calculated underestimation (R_{expt}/R_{theor}) of the isomeric ratios depends not only on the spin [18], but also on the mass loss.

Several effects have been discussed as possible origins of the discrepancy between calculated and measured isomeric ratios for high-spin states [15,18,54]. Although a clear answer concerning the population of different spin states is still missing, data shown in Fig. 3 can serve as a benchmark for further developments in theoretical models. Fluctuations in angular momentum, mass, and nuclear charge distributions of

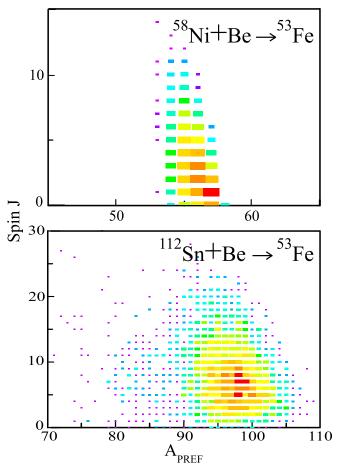


FIG. 5. Angular momentum vs mass of the prefragments leading to the observed ⁵³Fe final fragment produced in the fragmentation of ⁵⁸Ni and ¹¹²Sn calculated with the ABRABLA07 code.

prefragments produced in the fragmentation of ¹¹²Sn leading to ⁵³Fe final fragments may be large enough to properly reproduce the observed isomeric ratios. These fluctuations "overwrite" any other effect influencing angular momentum in the fragmentation reactions. However, for small mass losses these fluctuations are also small, see Fig. 5, since the number of different prefragments leading to the final fragment is rather small. These are thus the cases where additional contributions to angular momentum populations have to be investigated.

IV. SUMMARY

The isochronous mass spectrometry (IMS) method was applied to investigate angular momentum populations of highspin isomers in projectile fragmentation reactions. Isomeric ratios were measured for the spin 19/2 state in the mirror nuclei ⁵³Fe and ⁵³Co following the projectile fragmentation of ⁷⁸Kr with energies of ~480*A* MeV on a beryllium target at HIRFL-CSR. The half-lives of the excited states of ⁵³Fe and ⁵³Co are 2.54 m and 247 ms [39], respectively, in which cases the IMS can be seen as a complementary technique to γ -ray spectroscopy for the study of angular momentum populations, especially for systems with long lifetimes. The relationship of the isomeric ratio and momentum selection was studied by measured isomeric ratios of ⁵³Fe. The experimental isomeric ratios for the same spin were extracted as a function of the mass loss. Data obtained in this work and from literature show that the isomeric ratios rapidly increase with the mass loss and then saturate. This increasing behavior is approximately reproduced by the ABRABLA07 calculations. Quantitatively, the calculations can reproduce data for the 19/2 spin state in ⁵³Fe for the largest mass loss, but they considerably underestimate the corresponding data for small mass losses. Our new data point to the need for further development of the theoretical description of the fragmentation reaction process. The latter is indispensable for the planning of experiments at operating facilities as well as for the next-generation facilities like FAIR or HIAF.

ACKNOWLEDGMENTS

This work is supported in part by NSFC (Grants No. 11205205, No. 11575112, No. U1232208, No. 11135005, No.11605252, No. 11605267, and No. 11605249), by the CAS Pioneer Hundred Talents Program, by the 973 Program of China (No. 2013CB 834401), by the BMBF grant in the framework of the Internationale Zusammenarbeit in Bildung und Forschung Projekt-Nr. 01DO12012, by the Helmholtz-CAS Joint Research Group HCJRG-108, by the External Cooperation Program of the Chinese Academy Sciences Grant No. GJHZ1305, by the UK STFC, by the Max-Plank-Society, and by the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation program (Grant Agreement No 682841 "ASTRUm").

- D. J. Morrissey and B. M. Sherrill, Philos. Trans. R. Soc. London A 356, 1985 (1998).
- [2] H. Geissel, G. Münzenberg, and H. Weick, Nucl. Phys. A 701, 259c (2002).
- [3] W. F. Henning, Nucl. Phys. A 805, 502c (2008).
- [4] J. C. Yang et al., Nucl. Instrum. Methods B 317, 263 (2013).
- [5] E. Margaret Burbidge et al., Rev. Mod. Phys. 29, 547 (1957).
- [6] K. Sümmerer and B. Blank, Phys. Rev. C 61, 034607 (2000).
- [7] O. Tarasov, Nucl. Phys. A 734, 536 (2004).
- [8] M. de Jong, A. V. Ignatyuk, and K.-H. Schmidt, Nucl. Phys. A 613, 435 (1997).
- [9] A. M. Denis Bacelar et al., Phys. Lett. B 723, 302 (2013).
- [10] M. Pfützner et al., Phys. Rev. C 65, 064604 (2002).
- [11] K. A. Gladnishki et al., Phys. Rev. C 69, 024617 (2004).
- [12] M. Pfützner et al., Phys. Lett. B 444, 32 (1998).
- [13] S. Myalski et al., Acta Phys. Pol. B 40, 879 (2009).
- [14] S. J. Steer et al., Phys. Rev. C 84, 044313 (2011).
- [15] M. Bowry et al., Phys. Rev. C 88, 024611 (2013).
- [16] S. Myalski et al., Acta Phys. Pol. B 43, 253 (2012).
- [17] Z. Podolyák, Acta Phys. Pol. B 36, 1269 (2005).
- [18] Z. Podolyák et al., Phys. Lett. B 632, 203 (2006).
- [19] B. Sun et al., Phys. Lett. B 688, 294 (2010).
- [20] L. Chen et al., Phys. Rev. Lett. 110, 122502 (2013).
- [21] M. Block et al., Phys. Rev. Lett. 100, 132501 (2008).
- [22] J. Van Roosbroeck et al., Phys. Rev. Lett. 92, 112501 (2004).
- [23] B. Franzke, H. Geissel, and G. Münzenberg, Mass Spectrom. Rev. 27, 428 (2008).
- [24] H. Geissel et al., Hyperfine Interact. 173, 49 (2006).
- [25] B. Sun et al., Nucl. Phys. A 812, 1 (2008).
- [26] B. Mei et al., Nucl. Instrum. Methods A 624, 109 (2010).
- [27] J. W. Xia et al., Nucl. Instrum. Methods A 488, 11 (2002).
- [28] B. Mei et al., Phys. Rev. C 89, 054612 (2014).
- [29] Yu. A. Litvinov et al., Acta Phys. Pol. B 41, 511 (2010).

- [30] G. Audi et al., Chin. Phys. C 36, 1157 (2012).
- [31] P. M. Walker, Int. J. Mod. Phys. E 15, 1637 (2006).
- [32] Y. Ichikawa et al., Hyperfine Interact. 220, 47 (2013).
- [33] J. M. Daugas et al., Phys. Rev. C 63, 064609 (2001).
- [34] H. Irnich et al., Phys. Rev. Lett. 75, 4182 (1995).
- [35] M. Hausmann et al., Hyperfine Interact. 132, 291 (2001).
- [36] J. Stadlmann (private communication).
- [37] W. J. Huang (private communication).
- [38] N. V. Do et al., Nucl. Instrum. Methods B 266, 5080 (2008).
- [39] X. L. Tu et al., Phys. Rev. Lett. 106, 112501 (2011).
- [40] Y. H. Zhang et al., Phys. Rev. Lett. 109, 102501 (2012).
- [41] X. L. Tu *et al.*, J. Phys. G: Nucl. Part. Phys. **41**, 025104 (2014).
- [42] X. L. Yan et al., Astrophys. J. 766, L8 (2013).
- [43] C. Scheidenberger *et al.*, Nucl. Instrum. Methods B **142**, 441 (1998).
- [44] O. B. Tarasov and D. Bazin, Nucl. Instrum. Methods B 266, 4657 (2008).
- [45] X. L. Tu et al., Nucl. Instrum. Methods A 654, 213 (2011).
- [46] W. Zhang et al., Nucl. Instrum. Methods A 756, 1 (2014).
- [47] P. Shuai et al., Phys. Lett. B 735, 327 (2014).
- [48] X. L. Tu et al., Phys. Scr., T 166, 014009 (2015).
- [49] E. C. Simpson et al., Phys. Rev. C 80, 064608 (2009).
- [50] W.-D. Schmidt-Ott et al., Z. Phys. A 350, 215 (1994).
- [51] J.-J. Gaimard and K.-H. Schmidt, Nucl. Phys. A 531, 709 (1991).
- [52] A. Kelić, M. V. Ricciardi, and K.-H. Schmidt, in Proceedings of Joint ICTP-IAEA Advanced Workshop on Model Codes for Spallation Reactions, ICTP Trieste, Italy, 4–8 February 2008, edited by D. Filges, S. Leray, Y. Yariv, A. Mengoni, A. Stanculescu, and G. Mank, IAEA INDC(NDS)-530 (IAEA, Vienna, 2008), p. 181.
- [53] K. Eskola, Phys. Lett. 23, 471 (1966).
- [54] S. Pal and R. Palit, Phys. Lett. B 665, 164 (2008).