Neutron capture reactions near the N = 82 shell-closure

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Neutron capture cross sections have been calculated in nuclei near the N = 82 neutron shell-closure. These nuclei are of astrophysical interest, participating in the *s*-process and the *p*-process. A semimicroscopic optical model has been used with the potential being obtained through folding the target density with the DDM3Y nucleon-nucleon interaction. Theoretical density values have been calculated using the relativistic mean-field approach. The calculated cross sections, as a function of neutron energy, agree reasonably well with experimental measurements. Maxwellian-averaged cross sections, important for astrophysical processes, have been calculated.

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I. INTRODUCTION

After the seminal work of Burbidge *et al.* [1], the method of creation of heavy elements through the slow neutron capture or *s*-process has been firmly established. A recent review that discusses our current understanding of the *s*-process may be found in Käppeler *et al.* [2]. It is now understood that a major fraction of the nuclear abundance in the mass region 90 < A < 209 is due to the main *s*-process that takes place in He shells in low-mass asymptotic giant branch stars of moderate mass.

The role of the neutron capture reaction in the s-process has been explored in many works. More accurate measurements have shown the inadequacy of the classical site-independent s-process and have paved the way to coupling with stellar models. A mass region, where the reaction cross section plays a very important role, lies near the N = 82 shell-closure. Here, the elements Cs (Z = 55) to Sm (Z = 62) have small cross sections for neutron capture reactions because of the proximity of the shell closure. Hence, they act as bottlenecks for the *s*-process reaction path. An *s*-process peak occurs at 138 Ba. There are several *s*-only nuclides such as 134,136 Ba, 142 Nd, and ^{148,150}Sm in this mass region. In the case of pairs of s-only isotopes such as 134,136 Ba, the cross sections and the abundances can be used to obtain the branching ratios of the s-process. Nuclei on the s-process path that have comparable β -decay rates and neutron capture rates act as branch points as the nucleosynthesis path bifurcates towards both the protonand neutron-rich sides while passing through them. The cross sections at the branch points and s-only isotopes can provide important clues to the physical environments where the sprocess takes place.

Although experimental measurements are available for many isotopes in the mass region, cross-section values are required for some unstable nuclei those are important in determining the branching ratios. Such nuclei include ^{134,135}Cs, ¹⁴¹Ce, ¹⁴⁷Nd, and ^{147,148}Pm. We should also remember that although the classical or canonical *s*-process calculations use the Maxwellian-averaged cross sections (MACS) at a single thermal energy (\approx 30 keV usually), recent approaches, which couple stellar models with the *s*-process network, need MACS values at different thermal energies. Measurements are not always available and extrapolation to too distant values from the measured ones may lead to errors. Theoretical calculations can supplement the experimental measurements in this regard.

There are some neutron capture reactions in this mass region whose studies are relevant for the astrophysical *p*-process. Photodissociation reactions such as (γ, n) reactions occur in extremely hot environments. Explosively burning Ne/O layer in core-collapse supernovae heated by the outgoing shock wave may provide such an environment. Cross-section values are very important as various photodissociation reactions such as (γ, n) , (γ, p) , and (γ, α) compete at high temperatures. The emitted neutrons may also be absorbed after the shock wave passes through the layer. Thus it is very important to measure the cross sections for relevant (γ, n) reactions at thermal energies. The reverse process, i.e., (n, γ) reactions, may serve the purpose. For example, Dillmann et al. [3] studied a number of (n, γ) reactions with neutrons from the ${}^{7}\text{Li}(p,n){}^{7}\text{Be}$ reaction to simulate a Maxwellian neutron distribution at 25 keV thermal energy.

In the study of the *s*-process the energy range of the neutron as a projectile is low enough so that one has to deal with the radiative thermal neutron capture cross section. Thus in the present study we calculate the σ_{γ} cross section in which the target after absorbing the neutron emits one or more γ rays. Thus, our interest in this work lies in the radiative neutron capture, i.e., (n, γ) reactions. The study includes direct capture cross sections by excited states also, though contribution of direct capture cross-sections is small in the energy region of our interest. Radiative neutron capture reactions have been studied in various methods. Older experiments usually used neutron beams of comparatively wide resolution. As the resonances in this region are narrow (less than 1 eV), one gets an average cross section in such experiments. Extremely high-resolution experiments using the neutron time-of-flight technique (TOF) have been used to study the resonances. However, we are more interested in the MACS. In such cases, the data have been compressed into coarse energy bins to obtain MACS values. In some other experiments, sources of neutrons have been used that closely simulated the thermal neutron spectrum at certain

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TABLE I. Parameter set for the FSU Gold Lagrangian density. The parameter κ and meson masses m_s , m_v , and m_ρ are in units of MeV.

m _s	m_v	$m_{ ho}$	g_s^2	g_v^2	$g_{ ho}^2$	к	λ	ζ	Λ_v
491.500	782.500	763.000	112.1996	204.5469	138.4701	1.4203	+0.023762	0.06	0.030

temperatures. They can provide direct measurement of MACS values.

In the present work, we have studied low-energy neutron capture cross sections of the nuclei near N = 82. In the next section, we briefly present our formalism. In Sec. III, we discuss our results for important neutron capture reactions near N = 82 shell-closure, at various neutron energies, and compare them with experimental measurements. It is then followed by calculation of the MACS values, first at 30 keV and later at different thermal energies for some selected isotopes. Finally we summarize our work.

II. CALCULATION

A. Relativistic mean-field calculation

In relativistic mean-field (RMF) theory nucleons are treated as point particles interacting via the exchange of mesons and photons. In the present work, we have chosen the Lagrangian density FSU Gold [4], which contains self-interactions for the isoscalar-scalar sigma meson (ϕ) and the isoscalar-vector omega meson (V) as well as interaction between the isovectorvector rho meson (b) and omega meson. The interaction part has the usual form,

$$\mathcal{L}_{\text{int}} = \bar{\psi} \bigg[g_s \phi - \bigg(g_v V_\mu + \frac{g_\rho}{2} \tau b_\mu + \frac{e}{2} (1 + \tau_3) A_\mu \bigg) \gamma^\mu \bigg] \psi - \frac{\kappa}{3!} (g_s \phi)^3 - \frac{\lambda}{4!} (g_s \phi)^4 + \frac{\zeta}{4!} (g_v^2 V_\mu V^\mu)^2 + \Lambda_v (g_\rho^2 \mathbf{b}_\mu \cdot \mathbf{b}^\mu) (g_v^2 V_\mu V^\mu).$$
(1)

The nucleon and the photon fields are represented by the wave functions ψ and A, respectively. The meson masses and the coupling parameters are given in Table I.

The Klein-Gordon equations for meson fields and Dirac equations for baryon fields are obtained as the usual Lagrange's equations. Pairing is incorporated in the continuum BCS approximation using a delta pairing potential $V(\mathbf{r}_1,\mathbf{r}_2) =$ $-V_0\delta(\mathbf{r_1}-\mathbf{r_2})$. The pairing strength V_0 has been chosen to be 300 MeV for both protons and neutrons. The equations are solved in co-ordinate space using spherical approximation. The equations are solved by iterative technique in a grid size of 0.1 fm. The Dirac equations are solved using a fourth order Runge-Kutta method by integrating inwards from large r as well as outwards from small r and the energy eigenvalues are varied to make the wave function continuous at some appropriate matching radius. The meson fields are solved by integrating over the appropriate Green's function using Simpson's rule. The iterations are repeated till the desired accuracy is achieved.

B. Folding model analysis and potential formation

We have used a semimicroscopic procedure to calculate the neutron capture cross sections in the present work. This method has been followed in a number of our recent works [5–10]. For example, in Chakraborty *et al.* [10], this procedure has been utilized to study proton capture reactions, important for the astrophysical *p*-process in the mass 110–125 region. In the present approach, we extend it to study neutron capture reactions near the N = 82 shell-closure.

To briefly describe our procedure, we have assumed spherical symmetry for the target nuclei. The density profiles of the nuclei have been calculated in coordinate space in the RMF approach as mentioned earlier. The charge density (ρ_{ch}) is obtained from the point proton density (ρ_p) using a standard Gaussian form factor, F(r) [11], as follows:

$$\rho_{\rm ch}(\mathbf{r}) = e \int \rho_p(\mathbf{r}') F(\mathbf{r} - \mathbf{r}') d\mathbf{r}', \qquad (2)$$

$$F(r) = (a\sqrt{\pi})^{-3} \exp(-r^2/a^2),$$
 (3)

with $a = \sqrt{2/3}a_p$, where $a_p = 0.80$ fm is the root-meansquare (rms) charge radius of the proton. The charge density thus obtained is used to calculate rms charge radii for some nuclei in and around the concerned region of shell closure to compare with experimentally available values. Comparison with measured values serves as a check on the applicability and reliability of the Lagrangian density used in the calculations. Charge density has been chosen for comparison because its experimental measurements are available from electron scattering.

The nuclear density (sum of the point proton density and the point neutron density) has then been folded with the DDM3Y nucleon-nucleon interaction to obtain the optical model potential. The interaction at distance r for density ρ and the projectile energy in the center-of-mass frame E, supplemented by a zero-range pseudopotential, is given by

$$v(r,\rho,E) = t^{\text{M3Y}}(r,E)g(\rho), \tag{4}$$

with the M3Y interaction [12,13] in MeV,

$$t^{\rm M3Y} = 7999 \frac{e^{-4r}}{4r} - 2134 \frac{e^{-2.5r}}{2.5r} - 276 \left(1 - \frac{E}{200A}\right) \delta(r).$$
(5)

Here E is given in MeV, r is in fm, and A is the mass number of the projectile. The density dependent factor is [14],

$$g(\rho) = C(1 - \beta \rho^{2/3}),$$
 (6)

with *C* and β taking the values 2.07 and 1.624 fm², respectively, obtained from nuclear matter calculation [15]. We also use an additional spin-orbit potential, $U_{n(p)}^{so}(r)$, with energy-dependent phenomenological potential depths λ_{vso} and

 $\lambda_{\rm wso}$ according to the Scheerbaum prescription [16], given by

$$U_{n(p)}^{\rm so}(r) = (\lambda_{\rm vso} + i\lambda_{\rm wso}) \frac{1}{r} \frac{d}{dr} \left(\frac{2}{3}\rho_{p(n)} + \frac{1}{3}\rho_{n(p)}\right), \quad (7)$$

with

$$\lambda_{\rm vso} = 130 \exp(-0.013E) + 40, \tag{8}$$

$$\lambda_{\rm wso} = -0.2(E - 20). \tag{9}$$

To obtain the optical potential, the target radial matter density from the RMF calculation is folded with the *NN* interaction by integrating over the entire volume in coordinate space assuming spherical symmetry:

$$V_{\text{fold}}(\mathbf{r}, E) = \int v(|\mathbf{r} - \mathbf{r}'|, \rho, E)\rho(\mathbf{r}')d\mathbf{r}'.$$
 (10)

Here ρ is the radial matter density of the target nucleus, which in this case is the sum of the point proton density and the point neutron density of the target from RMF calculation. The DDM3Y interaction provides only the real part of the potential. The imaginary part of the potential is taken to be identical to the real part. The final optical model potential is thus constructed by multiplying with normalization constants A_R and A_{Im} for real and imaginary parts, respectively as follows:

$$V_{\rm omp} = A_R V_{\rm fold} + i A_{\rm Im} V_{\rm fold}.$$
 (11)

These normalization constants have been varied to get the best agreement with experimental cross-section values. This optical model potential has been used to study the neutron capture reaction cross sections.

DDM3Y nucleon-nucleon interaction has been used in numerous works for different perspectives, for example, to study proton radioactivity [17,18] and α -decay half-lives [19], for nuclear matter calculations [20], etc. Kobos et al. [12] measured differential elastic scattering cross sections for α particles on different targets. Mohr et al. [21] obtained the real part of the optical potential via α elastic scattering using the double-folding technique with the DDM3Y interaction for astrophysically relevant energy. The DDM3Y interaction is also used to study direct neutron capture cross sections at energies below 0.3 MeV on low-mass stable targets ¹²C and ¹⁶O [22]. We have already used it to study proton reactions at low energies [5-10]. In the present work we are applying the DDM3Y interaction in the microscopic Hauser-Feshbach statistical model prescription to check its validity at very low energies of astrophysical interest (between 1 keV and 1 MeV) for radiative neutron capture reaction cross sections on nuclei relevant to the *s*-process near the N = 82 shell-closure.

C. Cross-section calculation

The computer code TALYS-1.6 [23,24] has been used for cross-section calculations.

The statistical calculation of energy-averaged cross sections are based on the well-known Hauser-Feshbach formula given

by [25]

$$\langle \sigma_{\rm re}(\alpha, \alpha') \rangle$$

$$= \frac{\pi}{k_{\alpha}^2} \sum_{J\pi} \frac{(2J+1)}{(2I_1+1)(2I_2+1)} \frac{\left[\sum_{sl} \hat{T}_l(\alpha)\right] \left[\sum_{s'l'} \hat{T}_{l'}(\alpha')\right]}{\sum_{\alpha''s''l''} \hat{T}_{l''}(\alpha'')}.$$
(12)

Here, the unprimed and primed quantities represent incident and outgoing channels, respectively. The sum over α'' runs over all channels that are energetically accessible for the decay of the compound nucleus at the total energy in the incident channel. I_1 and I_2 are the spins of the target and projectile, respectively. The quantities J, π , l, and s denote total angular momentum, parity, orbital angular momentum, and spin, respectively and are determined by the usual selection rules. The transmission coefficients $\hat{T}_l(\alpha)$ of channel α for orbital angular momentum l are obtained from optical model potential constructed as described earlier. They are determined by complex phase shifts $\delta_{\alpha l}$ as

$$\hat{T}_l(\alpha) = 1 - |e^{2i\delta_{\alpha l}}|^2$$
 (13)

In the present case of study of (n, γ) reaction cross sections, the outgoing channel involves the emission of γ rays and hence γ -transmission coefficients are necessary, especially of dominant *E*1 transitions with appropriate giant dipole resonance energies and widths. The above equation must also be supplemented by the width fluctuation correction, especially in the case of low excitation energies, because it enhances the cross section for weak reaction channels at the cost of stronger ones. It also plays a sensitive role near the threshold of new channel openings where very different channel strengths exist. A more general discussion can be found in the manual for the TALYS-1.6 code [24].

Microscopic level densities, which are important ingredients in statistical model calculations of reaction cross sections, are taken from the calculations of Goriely *et al.* [26] included in the code. The γ -strength functions for the dominant $E1 \gamma$ transitions are taken from Goriely's hybrid model [27]. Width fluctuation corrections in compound nuclear decay are also considered. Radial densities are taken from RMF calculations. The pairing energy correction has also been included. At low incident energies, i.e., below a few MeV, mainly binary reactions occur and very often the target and the compound nuclei only are involved in the whole reaction chain. A maximum of 30 discrete levels are taken for both target and residual nuclei. Hauser-Feshbach calculations are performed with full *j*,*l* coupling. All these options are included in the TALYS code.

III. RESULTS

A. Results of RMF calculations

The most important RMF result relevant to the calculation of neutron capture in the present formalism is the density profile. Experimental results on density are available for three nuclei with N = 82, viz., ¹³⁸Ba, ¹⁴²Nd, and ¹⁴⁴Sm. In Fig. 1, we plot the charge density obtained in our calculation for these three nuclei. The experimental densities for ¹³⁸Ba and ¹⁴²Nd have been generated from the parameters for a three-parameter



FIG. 1. Charge density in several N = 82 nuclei. Solid lines denote the model values using the parameters obtained from fitting the experimental data. Dashed lines indicate our results.

Gaussian function fitted to describe the electron scattering data of Heisenberg *et al.* [28]. For ¹⁴⁴Sm, the Fourier-Bessel coefficients obtained from fitting the experimental results of Moinester *et al.* [29] have been used.

Charge radius is the first moment of the charge distribution. Hence comparison between theoretical calculations and experimental data can be done to check the success of the theoretical approach. In Table II, we compare the calculated rms charge radius values with experimental data [30]. From the comparison between experimental and calculated charge density and radius values, one can infer that the present RMF calculation can describe the nuclear density near the N = 82shell-closure very well. We now employ the theoretical density values to derive the optical model potential and extract cross sections for neutron capture.

TABLE II. Root-mean-square charge radii (r_c) of the nuclei studied in the present work. Experimental charge radii values are from the compilation of Angeli [30].

Nucleus	r_c	(fm)	Nucleus	$r_c(\mathrm{fm})$		
	Expt. Present			Expt.	Present	
¹³³ Cs	4.804	4.801	¹³⁴ Cs	4.803	4.807	
¹³⁵ Cs	4.807	4.813	¹³⁶ Cs	4.806	4.819	
¹³⁷ Cs	4.813	4.825				
¹³⁰ Ba	4.829	4.797	¹³² Ba	4.831	4.808	
¹³⁴ Ba	4.830	4.820	¹³⁵ Ba	4.827	4.826	
¹³⁶ Ba	4.833	4.832	¹³⁷ Ba	4.833	4.837	
¹³⁸ Ba	4.838	4.843				
¹³⁸ La	4.846	4.856	¹³⁹ La	4.855	4.862	
¹³⁶ Ce	4.874	4.858	¹³⁸ Ce	4.873	4.869	
¹⁴⁰ Ce	4.877	4.879	¹⁴¹ Ce		4.892	
¹⁴² Ce	4.906	4.905				
141 Pr	4.892	4.898	142 Pr		4.910	
¹⁴³ Pr		4.922				
¹⁴² Nd	4.912	4.915	¹⁴³ Nd	4.923	4.927	
¹⁴⁴ Nd	4.944	4.939	¹⁴⁵ Nd	4.958	4.953	
¹⁴⁶ Nd	4.975	4.965	¹⁴⁷ Nd	4.984	4.977	
¹⁴⁷ Pm		4.981	¹⁴⁸ Pm		4.993	
144 Sm	4.944	4.950	¹⁴⁷ Sm	4.984	4.985	
¹⁴⁸ Sm	5.001	4.998	¹⁴⁹ Sm	5.011	5.010	

B. Result of cross-section calculation

1. Elastic scattering angular distribution

We have calculated neutron differential elastic scattering cross sections for different targets near N = 82 at various energies. Our interest lies in the fact that a comparison with experiments would provide a better assessment of our optical model potential. The cross sections are compared in Fig. 2. The data for ¹⁴⁰Ce for four different energies are taken from Ref. [31]. For ¹⁴¹Pr, the data for 878 keV are taken from Cox and Dowling Cox [32] and the data for 1.2 MeV are taken from Singh and Knitter [33]. Cross sections for ¹⁴²Nd and ¹⁴⁸Sm are from Refs. [34] and [35], respectively.

The study of scattering at low neutron energy is important because the astrophysical reactions are usually confined to low energies. The theory agrees fairly well for ¹⁴⁰Ce and ¹⁴¹Pr isotopes. In most of the cases the theory can reproduce the scattering cross sections in the forward direction. This trend is prominent in the cases of ¹⁴²Nd and ¹⁴⁸Sm.

2. Neutron capture cross section

TALYS-1.6 is meant for analysis of data above the resolved resonance range, which is approximately 1 keV. We have compared the neutron capture cross sections with those experimental measurements that do not show resolved resonances at low energy.

Theoretical neutron capture cross-section results for different neutron energy values have been compared with experimental results in Figs. 3–6. In general, we have considered the more recent results. Our main interest lies in the nuclei that are important for astrophysical *s*- and *p*-processes. We generally present only those results where a reasonable amount of experimental data exists for comparison. The exceptions are ¹³⁹La and ¹⁴⁰Ce because these two nuclei correspond to the N = 82 shell-closure.

For convenience, we present the results for the elements where only one isotope has been studied in Fig. 3. These include ¹³³Cs, ¹³⁹La, ¹⁴⁰Ce, and ¹⁴¹Pr. Experimental crosssection values for the ¹³³Cs(n, γ) reaction are from Refs. [36– 38]. The cross-section values are averaged over the neutron energy range because the resonances are unresolved. For example, Yamamuro *et al.* [37] used the neutron beam from a tantalum photoneutron source. They then averaged the cross sections over the appropriate energy interval. For ¹³⁹La, the data are from Refs. [38,39]. Similarly, here also the neutron energy has a 5% error and we get an average value for various energies. Harnood *et al.* [40] measured the neutron capture cross sections of ¹⁴⁰Ce and ¹⁴¹Pr using the neutron TOF technique. Voss *et al.* [41] also measured the cross section for ¹⁴¹Pr in the range 3 to 225 keV. They also calculated the MACS values from their results. Voignier *et al.* [38] also measured the capture cross section for ¹⁴¹Pr in the energy range 0.5 to 3 MeV.

In Fig. 4, we show the average neutron capture cross sections in $^{135-138}$ Ba nuclei and compare with experimental values between 1 keV and 1 MeV. Experimental cross-section values are from Refs. [42–45]. Voss *et al.* [42,43] studied the neutron capture cross sections for $^{134-137}$ Ba nuclei in the energy range from 3 to 225 keV using gold as a standard.



FIG. 2. Differential angular distribution for elastic scattering of neutrons from (a) ¹⁴⁰Ce at 1.5 MeV, (b) ¹⁴⁰Ce at 2.0 MeV, (c) ¹⁴⁰Ce at 2.5 MeV, (d) ¹⁴⁰Ce at 3.0 MeV, (e) ¹⁴¹Pr at 0.878 MeV, (f) ¹⁴¹Pr at 1.2 MeV, (g) ¹⁴²Nd at 2.5 MeV, and (h) ¹⁴⁸Sm at 2.47 MeV. Solid lines denote theoretical data and discrete points represent experimental data.

Neutron capture by the neutron closed shell nucleus ¹³⁸Ba has been studied in Refs. [44,45].

Results for neutron capture cross sections of $^{142-146}$ Nd are shown in Fig. 5. Wisshak *et al.* [46,47] studied the resonances above 3 keV in $^{142-146,148}$ Nd. The data were then compressed in coarse bins to get the average behavior. In another work, Veerapaspong *et al.* [48] studied the neutron capture cross sections for 143,145,146 Nd. Their data were put in a large energy bin of 10 keV width. Their results agree with those of Refs. [46,47] and our results, though we have not shown the data in the figure.

In Fig. 6, we plot the experimental and calculated values for $^{144,147-149}$ Sm. For 144 Sm, experimental values are from Macklin *et al.* [49], where the authors have made measurements from 0.5 eV to 500 keV and have obtained the resonance parameters up to 100 keV. Wisshak *et al.* [50] studied the neutron capture cross section of $^{147-150,152}$ Sm in the energy range 3 to 225 keV using gold as a standard. Mizumoto [51] measured the neutron capture cross sections of 147,149 Sm in the energy range 3 to 300 keV using the TOF technique. Diamet *et al.* [52] used a similar technique to study $^{147-150,152,154}$ Sm in the energy range 10 to 90 keV.

From Figs. 3–6, one can see that the theoretical calculations reproduce the experimental values in most of the cases. We also repeated the calculation for all the nuclei with the Jeukenne-Lejeune-Mahaux (JLM) interaction [53] to test the sensitivity of our approach. JLM is a semimicroscopic optical model potential derived from the Brückener-Hartree-Fock approximation based on Reid's hard core nucleon-nucleon interaction. We observe that our model reproduces the experimental values better than the JLM model in all the cases. As an example,



FIG. 3. Comparison of the results of the present calculation with experimental measurements for ¹³³Cs, ¹³⁹La, ¹⁴⁰Ce, and ¹⁴¹Pr. The solid lines indicate the theoretical results. For convenience, cross-section values for ¹⁴¹Pr have been multiplied by a factor of 100.



FIG. 4. Comparison of the results of the present calculation with experimental measurements for ^{135–138}Ba. The solid lines indicate the theoretical results. For convenience, cross-section values for ^{135,136}Ba have been multiplied by a factor of 10.



FIG. 5. Comparison of the results of the present calculation with experimental measurements for $^{142-146}$ Nd. The solid lines indicate the theoretical results. For convenience, cross-section values for 143,144 Nd have been multiplied by a factor of 10.

in Fig. 7 we have shown the results for 144 Sm. As can be easily seen, the JLM model differs from our measurement as well as from experimental data by a factor of order ~ 2 . For other nuclei, the trend is more or less similar. As already mentioned, we have also varied the normalization constants, particularly the imaginary part. However, we found very small changes in cross sections while varying the imaginary depth by a factor of ~ 2 . Hence we kept it at the value unity. In the next subsection, we employ our method to calculate the MACS for some astrophysically important nuclei.

C. Maxwellian-averaged cross sections

Apart from the nuclei with N = 82 in the *s*-process path, i.e., ¹³⁸Ba, ¹³⁹La, ¹⁴⁰Ce, ¹⁴¹Pr, and ¹⁴²Nd, which act as bottlenecks due to low cross sections, neutron capture reactions in some other nuclei in the neighborhood are also important for nucleosynthesis. In Fig. 8, we show the *s*-process path in the neighborhood of the shell closure at N = 82. The shaded rectangles indicate stable and extremely long-lived nuclei. The



FIG. 6. Comparison of the results of the present calculation with experimental measurements for $^{144,147-149}$ Sm. The solid lines indicate the theoretical results. For convenience, cross-section values for 148,149 Sm have been multiplied by a factor of 10.



FIG. 7. The Neutron capture cross sections on the ¹⁴⁴Sm target are shown with two different optical model potential calculations and plotted against experimental data. The solid line denotes the present formalism and the dotted line represents the JLM optical model potential.

weak branch points are indicated by rectangles with dashed lines. Similarly, weak *s*-process paths are indicated by dashed lines. One can see that there are strong branch points in the *s*-process path at ¹³⁴Cs, ¹⁴⁷Nd, and ^{147,148}Pm. Besides, there are weaker branch points at ¹³⁶Cs, ¹⁴¹Ce, and ^{147,149}Pm. As already pointed out, the nuclei ^{134,136}Ba, ¹⁴²Nd, and ^{148,150}Sm are *s*-only. There are several *p* nuclei such as ¹³⁰Ba (not shown in Fig. 8) ¹³²Ba, ¹³⁸La, ^{136,138}Ce, and ¹⁴⁴Sm, the last corresponding to the shell closure.

In Table III, we present the theoretically calculated MACS values at kT = 30 keV for a number of selected isotopes and compare with experimental measurements whenever available. Experimental values are from the KADONIS database [54], which is an updated version of the compilation of Bao *et al.* [55]. Theoretical values from MOST calculations [56], which are listed in the KADONIS online database, are also presented. MOST is a Hauser-Feshbach code that derives all nuclear inputs from global microscopic models. As one can see, agreement of our results with experiment is better than the MOST results in almost all cases. In the next part of the discussion, we comment only on the more significant results.



FIG. 8. The *s*-process path near the shell closure at N = 82. Also shown are some of the *p* nuclei. See text for more details.

TABLE III. Maxwellian-averaged cross sections at kT = 30 keV for nuclei near the N = 82 shell-closure. Experimental values are from Ref. [54]. See text for other experimental values. The nuclei with N = 82 are in bold font.

Nucleus		MACS (mb)		Nucleus	MACS (mb)			
	Present	Expt.	MOST		Present	Expt.	MOST	
¹³³ ₅₅ Cs	685	509 ± 21	469	$^{134}_{55}$ Cs	786		805	
¹³⁵ ₅₅ Cs	147	160 ± 10	148	¹³⁶ ₅₅ Cs	90.4			
¹³⁷ ₅₅ Cs	16.1							
¹³⁰ ₅₆ Ba	625.2	746 ± 34	490	$^{132}_{56}$ Ba	393	397 ± 16	227	
¹³⁴ ₅₆ Ba	158	176.0 ± 5.6	117	¹³⁵ ₅₆ Ba	528	455 ± 15	259	
¹³⁶ ₅₆ Ba	74.6	61.2 ± 2.0	49.4	¹³⁷ ₅₆ Ba	81.8	76.3 ± 2.4	95.4	
¹³⁸ ₅₆ Ba	4.14	4.00 ± 0.20	2.79					
¹³⁸ ₅₇ La	417		337	¹³⁹ ₅₇ La	31.0	32.4 ± 3.1	45.9	
¹³⁶ ₅₈ Ce	547	328 ± 21	206	¹³⁸ ₅₈ Ce	137	179 ± 5	60.5	
¹⁴⁰ ₅₈ Ce	12.7	11.0 ± 0.4	6.71	¹⁴¹ ₅₈ Ce	198.8		58.4	
¹⁴² ₅₈ Ce	33.5	28 ± 1	16.7					
¹⁴¹ ₅₉ Pr	101	111.4 ± 1.4	130	$^{142}_{59}{\rm Pr}$	233		261	
¹⁴³ ₅₉ Pr	170		57.7					
$^{142}_{60}$ Nd	54.5	35.0 ± 0.7	22.9	$^{143}_{60}$ Nd	362.4	245 ± 3	105	
¹⁴⁴ ₆₀ Nd	82.3	81.3 ± 1.5	37.1	$^{145}_{60}$ Nd	617.9	425 ± 5	207	
¹⁴⁶ ₆₀ Nd	128.7	91.2 ± 1.0	56.8	$^{147}_{60}$ Nd	1434.4		663	
$^{147}_{61}$ Pm	1210.4	709 ± 100	452	$^{148}_{61}$ Pm	1529.7			
$_{62}^{144}$ Sm	91.0	92 ± 6	38.6	$^{147}_{62}$ Sm	1229	973 ± 10	584	
$^{148}_{62}{ m Sm}$	340	241 ± 2	130	$_{62}^{149}$ Sm	1622	1820 ± 17	1274	

The Cs isotopes that are involved in the *s*-process are 133,134,135 Cs. The nucleus 134 Cs is unstable with a half-life of 2.06 yr and no neutron capture data are yet available. However, this is important for the abundances of 134,136 Ba in view of the strong branching at 134 Cs. The compilation by Bao *et al.* [55] recommended a MACS value of 664 ± 174 mb. Our calculated value for 135 Cs is close to the experimental measurements. However, the neutron-deficient 133 Cs rate is comparatively poorly reproduced.

Dillmann *et al.* [3] have measured the MACS values for a number of nuclei relevant to the *p*-process. The measured values at kT = 25 keV for the nuclei ^{130,132}Ba are 736 ± 29 mb and 392.6 ± 14.8 mb, respectively. Our calculated values for ^{130,132}Ba at 25 keV are 675.3 mb and 424.1 mb, respectively. The neutron capture cross sections of the *s*-only nuclei ^{134,136}Ba are very important for constraining the *s*-process. The cross section for ¹³⁶Ba is also known to be an important ingredient in determining the mean neutron exposure in the main *s*-process component. As one can see, here also our results are reasonably close to experimental measurements except in the case of ¹³⁰Ba.

Käppeler *et al.* [57] measured the cross sections for stable Ce isotopes. They then constructed an optical model potential for this region and calculated the cross sections for ¹⁴¹La and ^{142,143}Pr in the Hauser-Feshbach formalism. Their calculated values for these two nuclei at 30 keV are 91 mb, 297 mb,

and 205 mb, respectively. Although their results for ^{140,142}Ce and ¹⁴¹Pr are very close to our calculations, the value for ¹⁴¹Ce is smaller by more than a factor of 2, while the values for ^{142,143}Pr are larger by more than 25% and 20%, respectively. The results for La and Pr isotopes are also close to experimental measurements. The nucleus ¹³⁸La is produced in the *p*-process. However, results for more neutron-deficient Ce isotopes do not agree well with experiments.

As one goes to heavier isotopes, agreements become poorer except in a few cases such as ¹⁴⁴Nd and ¹⁴⁴Sm, though they are still better than the MOST calculations. In general, the poor agreements may be due to the fact that, away from the closed shell, deformation effects come into the picture. However, our calculation is unable to explain the recent results for ¹⁴²Nd, a spherical nucleus with N = 82, though some of the older measurements for ¹⁴²Nd are closer to our calculation. Results for all the other nuclei with N = 82 are explained with a good accuracy.

The differences between our calculations and the MOST data can be attributed to the different choice of nucleon-nucleon interactions as well as different choices for certain inputs, especially, nuclear level densities and $E1 \gamma$ -ray strength function. The MOST calculation is based on the JLMB nucleon potential [58], a revised version of the JLM potential introduced by Jeukenne *et al.* [53]. A large contribution to uncertainty in nuclear rate calculation comes from the ambiguity in the

TABLE IV. Maxwellian-averaged neutron	capture cross	s sections of	¹³⁸ Ba,	¹³⁹ La,	¹⁴⁰ Ce,	¹⁴¹ Pr, and	142 Nd. T	The exper	imental	values
presented are from Ref. [54]. See text for more	details about	the experimer	nts and t	he avai	lable lat	est measure	ements no	ot include	d in Ref.	. [54].

kT (MeV)	MACS (mb)										
	¹³⁸ Ba		¹³⁹ La		¹⁴⁰ Ce		¹⁴¹ Pr		¹⁴² Nd		
	Present	Expt.									
0.005	10.3	13.4	118	111.2	34.0	23	353	412	146.5	98.6	
0.010	6.96	7.85	68.9	63.2	21.9	19.5	215	247	95.8	65.1	
0.015	5.68	5.93	50.8	48.1	17.6	16	161	182	76.2	51.3	
0.020	4.93	4.95	41.2	40.3	15.2	13.5	132	148	65.8	43.4	
0.025	4.46	4.38	35.2	35.7	13.8	12	114	126	58.8	38.4	
0.030	4.14	4.00	31.0	32.4	12.7	11.0	101	111	54.5	35.0	
0.040	3.61	3.49	25.4	27.7	11.2	9.5	82.8	91.5	47.9	30.7	
0.050	3.28	3.14	21.8	23.6	10.2	8.7	70.8	78.3	43.8	27.7	
0.060	3.08	2.89	19.2	22.0	9.5	8.1	62.0	69.0	41.0	25.5	
0.080	2.76	2.52	15.8	18.4	8.6	7.2	50.1	56.2	37.4	22.9	
0.100	2.58	2.23	13.7	15.2	8.0	6.6	42.4	47.6	35.5	21.0	

nuclear level density. MOST uses microscopic Hartree-Fock-BCS level densities from Ref. [59] that are treated with shell and pairing effects, deformation, and collective excitation. However we have taken the level density from Ref. [26], which is based on a microscopic combinational model explicitly taking into account the vibrational contribution of phonon excitations along with the rotational enhancement factor. This model is also coupled with suitable renormalization factors to reproduce experimental *s*- and *p*-wave neutron resonance spacings with a moderate degree of accuracy and thus reliable extrapolation at low energies is possible. The other significant input that differs from our calculation is $E1 \gamma$ -ray strength that has been taken from quasi-particle-random-phase approximation (QRPA) calculation [60] in the case of MOST calculation and from Ref. [27] in the present method.

As already pointed out, modern measurements have emphasized the importance of the MACS values at various thermal energies. Hence a number of works, apart from those already mentioned, have measured the MACS values at different temperatures. We present the MACS values at different temperatures for N = 82 isotopes in Table IV and draw attention to some important results. Heil *et al.* [61] have used neutron activation studies to measure the MACS value at 5.1 keV as 13.0 ± 0.5 mb in ¹³⁸Ba. In the present work, the MACS value for ¹³⁸Ba is calculated to be 10.2 mb at kT = 5.1 keV.

Natural lanthanum is nearly monoisotopic. It is an important element as it can be easily detected in solar spectroscopy. It is produced in both *s*- and *r*-processes and is particularly suitable for monitoring *s*-process abundances from Ba to Pb. This has led to the study of ¹³⁹La through neutron TOF spectroscopy as well as activation measurement. In Table IV, we present the MACS values for this isotope at different temperatures. O'Brien *et al.* [62] have measured the MACS values at kT = 30 keV as 31.6 ± 0.6 mb. Our calculated value of 31.0 mb agrees with the measurements. The activation technique has also been used to measure MACS at kT = 5 keV. The measured value 113.7 ± 4.0 mb [63] is in excellent agreement with our calculation. Terlizzi *et al.* have measured the resonance parameters in the energy range 0.6 to 9 eV and have recalculated the MACS values in the light of their measurements [64]. Their values also lie close to our calculated results. For example, their measurement yields a value of 106.9 ± 5.3 mb at kT = 5 keV after normalization to the value for 25 keV from Ref. [62].

Käppeler *et al.* [57] also used the ⁷Li(p,n)⁷Be reaction to study the thermal neutron capture by Ce isotopes at 25 keV. They obtained a MACS value of 12.0 ± 0.4 mb. This was extrapolated to other thermal energy values. As already mentioned, Voss *et al.* [41] have obtained the MACS values as a function of temperature for ¹⁴¹Pr.

As already mentioned, Wisshak *et al.* [46] studied the neutron capture cross sections of Nd isotopes. They have also calculated the MACS values at different energies from their data. Guber *et al.* [65] also measured the MACS values between kT = 5 and 50 keV. Both the above references have commented on the importance of the new measurements in the *s*-process.

IV. SUMMARY

To summarize, astrophysically important neutron capture reactions near the N = 82 shell-closure have been studied using a microscopic approach. Densities of relevant nuclei have been calculated in the RMF approach. The calculated charge densities and radii agree with experimental measurements, whenever available. The calculated density has been folded with the DDM3Y nucleon-nucleon interaction to obtain the optical model potential for neutron reactions. Cross sections for (n, γ) reactions have been calculated and compared with measurements. Finally MACS values, important for *s*- and *p*-processes, have been calculated.

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