

# Experimental study of ultracold neutron production in pressurized superfluid helium

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We investigate experimentally the pressure dependence of the production of ultracold neutrons (UCNs) in superfluid helium in the range from saturated vapor pressure to 20 bar. A neutron velocity selector allows the separation of underlying single-phonon and multiphonon processes by varying the incident cold neutron (CN) wavelength in the range from 3.5 to 10 Å. The predicted pressure dependence of UCN production derived from inelastic neutron scattering data is confirmed for the single-phonon excitation. For multiphonon-based UCN production we found no significant dependence on pressure, whereas calculations from inelastic neutron scattering data predict an increase of 43(6)% at 20 bar relative to saturated vapor pressure. From our data we conclude that applying pressure to superfluid helium does not increase the overall UCN production rate at a typical CN guide.

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## I. INTRODUCTION

Ultracold neutrons (UCNs) have energies below 300 neV and can be stored for long observation times in magnetic or material bottles [1]. This peculiarity makes them attractive for high-precision measurements of fundamental properties of the neutron which are relevant for particle physics and cosmology [2]. The most prominent example is their use for searches of a neutron electric dipole moment [3–8] which would give direct evidence of *CP* violation beyond the standard model of particle physics. Other projects aim to improve the knowledge of the neutron  $\beta$ -decay lifetime, which is crucial for calculations of big-bang nucleosynthesis [9]. Together with correlation measurements in neutron decay it contributes to a more precise understanding of weak semileptonic processes in the first quark generation [10,11]. New developments might follow from observations and manipulations of quantum states of UCNs in Earth's gravitational field [12–14]. All of these endeavors greatly benefit from an increase in UCN counting statistics in their experiments.

Current projects to increase the density of UCNs for physics experiments employ neutron converters of superfluid helium (He-II) [15–20] and solid deuterium [21–26]. They exploit the concept of a superthermal source [27], where the converter temperature can be much higher than the UCN “temperature.” Upscattering of UCNs is suppressed by the Boltzmann factor if the energy of excitations in the converter is high compared to its temperature. Using liquid He as a converter was proposed in Ref. [28] and first experimentally realized in Ref. [29].

In He-II the main contribution to UCN production is due to single-phonon excitations (see [17] for a separation of UCN production in single- and multiphonon contributions), which occur at the crossing point  $\lambda^*$  of the dispersion relations of the free neutron and of He-II. At saturated vapor pressure (SVP),  $\lambda^* = 8.92(2)$  Å (derived from the data in Ref. [30]).<sup>1</sup> Application of pressure shifts  $\lambda^*$  to lower values, where the differential flux  $d\phi/d\lambda$  is higher for a typical neutron beam in a guide coupled to a liquid deuterium cold neutron (CN) source, which typically has its flux maximum around 4 Å. Combined with an increase in density of He-II with pressure one may anticipate an overall gain in UCN production.

However, a quantitative analysis based on a method described in Ref. [31] using inelastic neutron scattering data at SVP and 20 bar from [30] predicted a net decrease in single-phonon UCN production [32,33]. On the other hand, these same calculations also predicted an increase in the production from multiphonon excitations at 20 bar. We wished to test these calculations and quantify the UCN production in pressurized He-II by a direct measurement.

Independent of UCN production, another motivation for performing these studies is the higher dielectric strength of pressurized He-II [34]. This is of particular interest for searches of the neutron electric dipole moment within He-II using electrical fields of several 10 kV/cm [35].

## II. EXPERIMENTAL SETUP

The experiment took place at the CN beam facility PF1b [36] of the Institut Laue-Langevin, France. A schematic of the experimental setup is shown in Fig. 1. The setup for the He-II UCN production target and UCN extraction was similar to the one described in Refs. [18,20]: The target

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<sup>1</sup>Note that a more accurate value for SVP may be derived from the comprehensive data collection [49]. However, we wanted to base our comparisons with scattering data on one consistent data set.

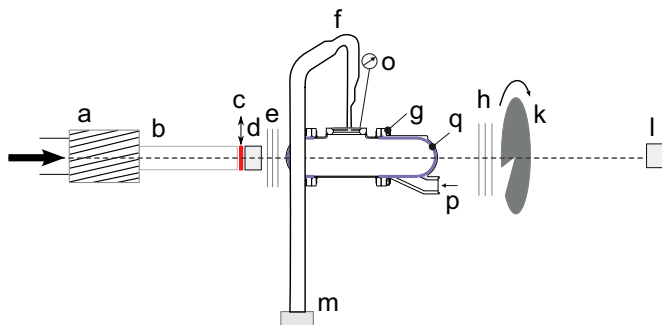


FIG. 1. (Color online) Schematic of the setup (not to scale): The CN beam passed through the velocity selector (a), a secondary CN guide (b), which could be closed off with a fast shutter (c), and a beam monitor with circular orifices (d) before it entered the cryostat through a series of thin aluminum windows (e). The He-II target was kept in the Ni-coated stainless-steel pressure container (g); CN entrance and exit sides from aluminum were covered with nickel half-spheres (q). Ultracold neutrons were guided by a polished stainless-steel tube (f), which was separated by an aluminum window from the production volume, to the  $^3\text{He}$  UCN detector (m). The CN beam exited the cryostat through aluminum windows (h) before entering a chopper (k) and TOF detector (l) for TOF spectral analysis. Pressure was applied via the filling line (p) connected to the bottom of the pressure container and measured in a static line with a gauge (o).

was located inside a cryostat equipped with a commercial two-stage Gifford McMahon cold head with a cooling power of 1.5 W at 4.2 K. In the cryostat, gaseous He of 99.999% purity was liquefied and cooled below the  $\lambda$  transition to superfluidity by a continuous  $^4\text{He}$  evaporation stage.  $^3\text{He}$  was removed by passing the superfluid through a superleak (for technical details on the used design, see [19]) into the UCN production volume. UCNs were extracted by an inverted U-shaped stainless-steel UCN guide to a  $^3\text{He}$  UCN detector. For further details, see [18,20,33].

In order to allow for measurements at high pressure, a dedicated He-II container was used as the converter vessel. It consisted of a stainless-steel tube (inner diameter, 66 mm; length, 193.8 mm) with two spherical end caps from aluminum (radius,  $\sim 33$  mm; wall thickness, 3 mm) for passage of the CN beam. Its total volume was  $810\text{ cm}^3$ , and the intersection volume with the neutron beam about  $180\text{ cm}^3$ . The cylinder was coated with natural nickel and the end caps had nickel half-spherical shells inserted on the inside to increase the neutron optical potential for UCN storage. The UCN flapper valve used in Ref. [18] for windowless extraction was replaced with an aluminum window (0.1-mm thickness) supported by a stainless-steel disk with an array of holes (effective hole area,  $127\text{ mm}^2$ ). The  $^3\text{He}$  evaporation stage serving to further cool the production volume had to be operated with  $^4\text{He}$  due to the higher heat load of the high-pressure volume. Therefore the target temperature reached only 1.1 K instead of the 0.7 K obtained in Ref. [18]. The temperature of the He-II was measured using a calibrated Cernox sensor (Model CX-1030-CU; Lake Shore Cryogenic, Inc.) screwed tightly to the outside of the He-II vessel. The pressure was applied from the gaseous He supply via the liquefaction chain through

the superleak and measured with a room-temperature pressure gauge calibrated for  $p < 100$  bar relative to the atmospheric pressure. The gauge was connected to the converter via a thin stainless-steel tube which could also be used for pumping to establish SVP conditions.

A neutron velocity selector [37] was used to scan the incident CN wavelength range. It had to be used in two orientations,  $-5^\circ$  and  $+5^\circ$  with respect to the incident beam, as the normal position ( $0^\circ$ ) did not give access to the entire wavelength range of interest. Hence, two scans were performed: from 3.5 to 6.5 Å and from 5.5 to 10 Å. Depending on the angular and rotational settings of the velocity selector a wavelength spread of  $\frac{\Delta\lambda(\text{FWHM})}{\lambda} \approx 0.14$  and 0.08 was obtained for  $-5^\circ$  and  $+5^\circ$ , respectively. After passage of a 2.5-m-long secondary neutron guide (cross section,  $30 \times 50\text{ mm}^2$ ) with natural nickel coating, a fast shutter in front of the beam monitor was used to open and close the beam (opening and closing time,  $< 1$  s). Before entering the beam monitor the beam's cross section was reduced to  $\varnothing = 30$  mm with two circular apertures made from  $\text{B}_4\text{C}$ . Images of the beam at various distances behind the monitor were taken before the cryostat was set up. They showed that the beam passed through the production volume without touching its cylindrical sidewall for all selected incident wavelengths. A time-of-flight (TOF) system for spectral analysis of the incident spectrum was set up behind the cryostat. It consisted of a chopper—a disk rotating at 1000 rpm with four radial rectangular slits (width, 3 mm) passing by a fixed aperture of the same dimensions—and a  $^3\text{He}$  CN-monitor with a detection efficiency proportional to  $1/v$  ( $v$  is the neutron velocity) placed 2 m downstream. The corresponding wavelength spectra for some selected velocity selector settings are displayed in Fig. 2.

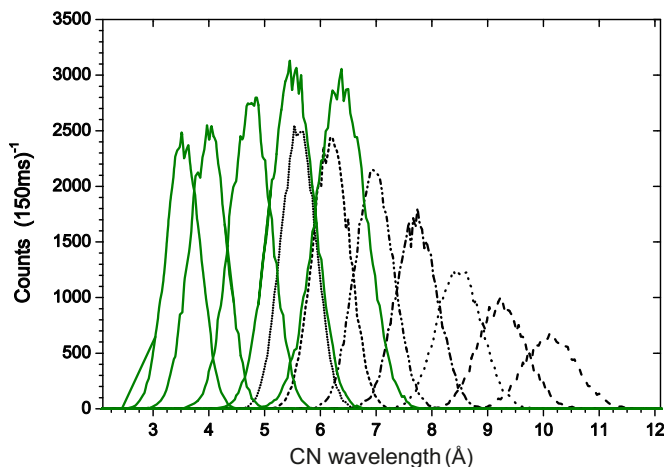


FIG. 2. (Color online) Time-of-flight spectra of the CN beam measured with an empty production volume, for various velocity selector rotation speeds at  $-5^\circ$  [solid (green) line] and  $+5^\circ$  (dashed black line) selector alignment. Each raw spectrum was normalized to area unity and then multiplied by the respective monitor count rate corrected for deadtime and  $1/v$  efficiency. The difference in integral counts for  $-5^\circ$  and  $+5^\circ$  was due to the larger transmission of the velocity selector at  $-5^\circ$ .

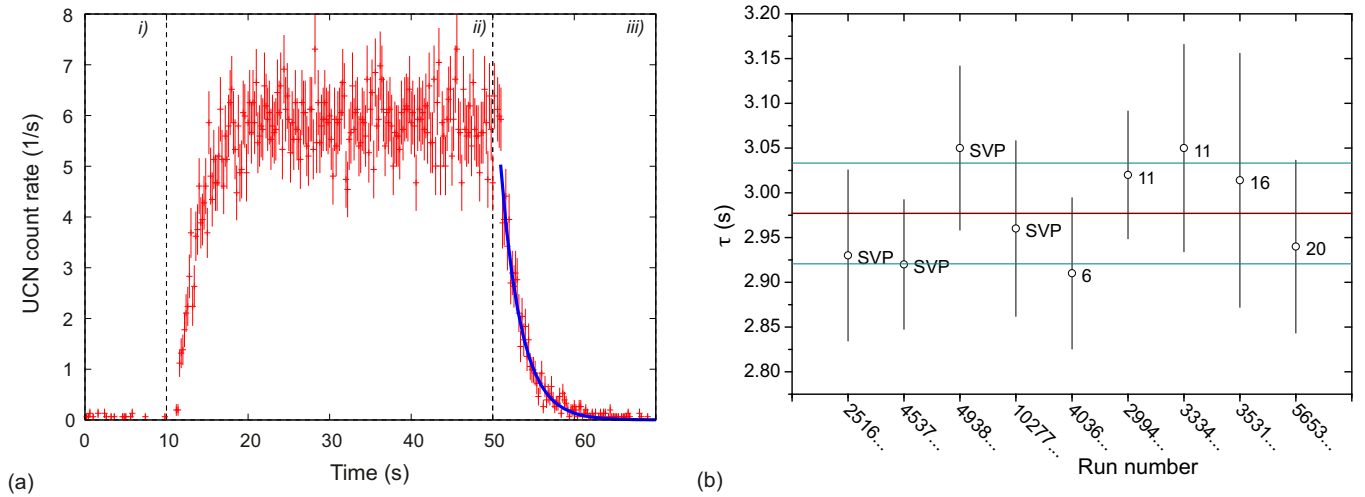


FIG. 3. (Color online) Count rate observed in the UCN detector (a). Shown is the combined data of all measurements at SVP and  $\lambda \sim 8.7$  Å (maximum of UCN production,  $\lambda_{\text{cor}} = 8.92$  Å). Vertical lines indicate the three different phases. The solid line in phase (iii) is the best fit (see text) to the data with a reduced  $\chi^2 = 1.04$ . Decay time constants  $\tau$  for different pressures were constant within the error bars (b): The red line represents the weighted mean; the blue line, the error of the weighted mean.

### III. MEASUREMENTS

Scans of UCN count rate versus CN wavelength were performed at absolute pressures and temperatures  $(p [\text{bar}], T [\text{K}]) = (6, 1.105), (11, 1.106), (16, 1.112), (20, 1.109),$  and (SVP, 1.08), with temperature fluctuations  $\Delta T \leq 0.02$  K during individual scans. The UCN production rate was first measured in the long-wavelength range with the velocity selector angle set to  $+5^\circ$  for all pressures. Then measurement of the UCN production rate in the short-wavelength range ( $-5^\circ$ ) followed. For each pressure and angular setting, three up-down scans were performed with the same set of velocity selector frequencies, corresponding to wavelength increments of about  $0.25$  Å. During each scan the UCN production rate for a specific rotation frequency was measured five times. Each of these measurements was divided into three phases as shown in Fig. 3: (i) 10 s with the CN shutter closed to verify the absence of UCN in the converter vessel; (ii) 40 s with the CN shutter open to record the buildup and saturation of the UCN rate; and (iii) 20 s with the CN shutter closed to record the emptying of the converter vessel. The decrease in rate during phase (iii) was fitted with an exponential function (see Fig. 3),  $\dot{n}(t) = \dot{n}_0 \exp(-\frac{t}{\tau}) + r_0$ , where the fit parameter  $\tau$  is the storage lifetime of the converter [ $\tau = 2.92(7)$  s for SVP at  $T = 1.08(2)$  K]. The beam-independent background  $r_0 = 0_{-0.0}^{+3.9} \times 10^{-3} \text{ s}^{-1}$  was determined in dedicated measurements with the CN shutter closed. This parameter was kept fixed in the fits. It was found that the storage lifetime was independent of the pressure [see Fig. 3(b)]. Increasing the temperature to 1.48 K decreased  $\tau$  to 1.7(1) s. This temperature behavior combined with results from UCN Monte Carlo simulations with Geant4UCN [38] and simple gas kinetic arguments showed that the storage lifetime was dominated by UCNs escaping through the extraction holes. Hence, changes in count rate due to the small temperature fluctuations of  $\pm 0.02$  K were negligible.

In phase (ii), the background was increased by a beam-dependent component  $r_{\text{beam}}$ , causing a constant offset to the UCN buildup prompt with opening of the CN shutter. A systematic error will follow if this offset is not properly taken into account. The component  $r_{\text{beam}}$  was determined by fitting the buildup with an exponential with constant background  $r = r_0 + r_{\text{beam}}$ . It was expected to be proportional to the CN monitor count rate since the CN monitor and UCN detector both had a low efficiency, proportional to  $1/v$  for CNs. Therefore the  $r_{\text{beam}}$  was determined for four velocity selector settings (maximum of single-phonon production and three settings with a low ratio of UCN production to CN monitor count rate). A fit of the four values with  $r_{\text{beam}}(\dot{n}_{\text{CN}}) = k\dot{n}_{\text{CN}}$ , where  $\dot{n}_{\text{CN}}$  is the CN count rate of the beam monitor ( $12\,000 \text{ s}^{-1} < \dot{n}_{\text{CN}} < 17\,000 \text{ s}^{-1}$ ), yielded  $k = (5.6_{-5.6}^{+6.0}) \times 10^{-7}$ . All data for phase (ii) was corrected for both background contributions, by typically  $0.01 \text{ s}^{-1}$ .

In addition to these scans the UCN production rates across the single-phonon peak at SVP were measured several times during the entire experiment to check the reproducibility. The UCN count rate was found to decrease with time. This is suspected to be due to gas freezing out on the thin aluminum window at the extraction holes or on the surface of the extraction guide. An exponential decrease with respect to the start of the first measurement ( $t = 0$ ),  $N(t) = N_0 \exp(-\frac{t}{\mathcal{T}}) + A_0$  with a large offset  $A_0 = 1.95(10) \times N_0$  and time constant  $\mathcal{T} = 104(12)$  h, was found to describe this effect well and thus was used to correct the data. The corrected UCN counts were normalized to the particle flux as measured by the beam monitor (monitor count rate is corrected for deadtime and  $1/v$  efficiency). TOF measurements (see Fig. 2) were used to determine a central wavelength for each setting of the velocity selector. The measured TOF spectra were deconvoluted taking into account the opening function of the chopper and the finite thickness of the TOF detector. A logarithmic normal distribution was found to describe the skewed deconvoluted

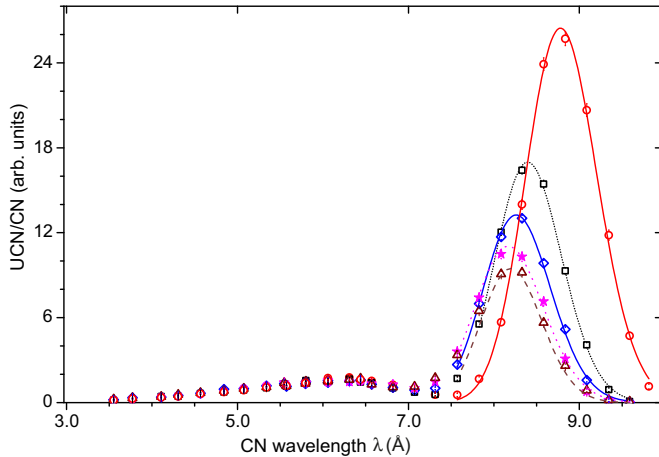


FIG. 4. (Color online) Measured wavelength-resolved UCN production rate per incident CN for  $p = \text{SVP}$  [(red) circles],  $p = 6$  bar [(black) squares],  $p = 11$  bar [(blue) diamonds],  $p = 16$  bar [(magenta) stars], and  $p = 20$  bar [(brown) triangles]. Lines are best fits of logarithmic normal distributions to the data with a reduced  $\chi^2 = 1.3, 1.2, 2.0, 1.9,$  and  $2.6$ , respectively.

spectra better than a symmetric Gaussian and was used to find the position of the maximum of each spectrum. Hence, each UCN production rate, which is in fact an integral UCN production rate of the specific CN spectrum of this velocity selector setting, was assigned to one wavelength  $\lambda$ . The uncertainty of the wavelength measurement was estimated as  $\frac{\Delta\lambda}{\lambda} = \pm 1\%$ .

#### IV. RESULTS

The measured wavelength-dependent UCN rates for all pressures, normalized to the incident particle flux, are shown in Fig. 4. Two regions can be distinguished for all pressures: a broad distribution for short incident wavelengths from UCN production by multiphonon processes  $R_{\text{II}}$  and a pronounced peak at long wavelengths from UCN production by single-phonon excitation  $R_{\text{I}}$  in He-II. These regions are separated by a minimum which gets less pronounced with pressure at the available wavelength resolution. Note that the wavelength

resolution was limited by the resolution of the velocity selector (the same for the range of all single-phonon peaks shown). With pressure the single-phonon peak decreases in intensity and moves towards shorter wavelengths.

The area under the peak is proportional to the UCN production rate by single-phonon excitation. The apparent peak width comes from the convolution of the incident CN spectra with the extremely narrow single-phonon scattering function (the linewidth of the roton excitation in  $^4\text{He}$  at  $\sim 1$  K is of the order of  $1 \mu\text{eV}$  (see, e.g., Ref. [39]), compared to the resolution of  $\sim 230 \mu\text{eV}$  of the velocity selector at  $8 \text{ \AA}$ ). The peak was fitted with a logarithmic normal distribution in  $q$  space. This ansatz best fit the CN spectra and was used again here since the single-phonon UCN production rate is proportional to the CN intensity at  $\lambda^*$  for each incident CN spectrum. Note that fits with logarithmic normal distributions gave, for all pressures, reduced  $\chi^2$  values closer to unity than a symmetric Gaussian distribution. The fitting range was restricted to wavelengths larger than  $7.5 \text{ \AA}$ , hence excluding contributions from multiphonon processes. The positions of the maximum of each fit function were observed for all pressures at values smaller than expected from the crossing point of the dispersion relations of He-II and the free neutron. They are listed in Table I together with the UCN production rates normalized to the rate at SVP. All single-phonon UCN production rates  $R_I$  were taken from the integrals over the fitted curves for  $\lambda > 7.5 \text{ \AA}$ .

The obtained fits were then subtracted from the data in order to extract the UCN production rates due to multiphonon processes. These are shown scaled up in Fig. 5 and found to exhibit a broad, pressure-independent maximum at approximately  $6.25 \text{ \AA}$ . For estimating the relative change in UCN production due to multiphonon excitation and multiple scattering with pressure, we used a simple sum over data points for  $\lambda < 7.5 \text{ \AA}$ , which was found to remain constant within errors in this range (see Table I).

#### V. DISCUSSION

In our experiment we observed the anticipated decrease in UCN production  $R_I$  due to single-phonon processes with pressure. This behavior can be well understood by taking a

TABLE I. Pressure dependence of measured single-phonon peak position  $\lambda^*$ , corrected values  $\lambda_{\text{cor}}^*$  (see text), and UCN production rates compared with results given in Refs. [32,33] calculated from scattering data. UCN production rates are normalized to the incident cold neutron flux. The single-phonon (s-ph) and multiphonon (m-ph) columns list the production rates at pressure  $p$  normalized to the respective SVP results. Quoted errors of  $\lambda^*$  from this experiment only include the uncertainties from the fits with the logarithmic normal distribution. Quoted errors of the measured UCN production rates are statistical uncertainties; in the single-phonon case uncertainties of the fit were increased to yield a reduced  $\chi^2$  of 1. The errors of the calculated values are the quadratic sums of all contributions.

$p$ (bar)	Experiment				$p$ (bar)	From Refs. [32,33]		
	$\lambda^*$ ( $\text{\AA}$ )	$\lambda_{\text{cor}}^*$ ( $\text{\AA}$ )	s-ph	m-ph ( $\lambda < 7.5 \text{ \AA}$ )		$\lambda^*$ ( $\text{\AA}$ )	s-ph	m-ph ( $\lambda < 7.5 \text{ \AA}$ )
SVP	8.70(1)	8.92(set)	1	1	SVP	8.92(2)	1	1
6	8.31(1)	8.52(1)	0.65(4)	0.93(4)	5	8.54(4)	0.75(11)	1.09(3)
11	8.18(1)	8.39(1)	0.54(4)	0.97(4)	10	8.39(2)	0.59(10)	1.12(3)
16	8.10(1)	8.30(1)	0.47(3)	0.97(4)	15	8.30(2)	0.47(9)	1.17(6)
20	8.09(1)	8.29(1)	0.41(3)	1.03(4)	20	8.26(2)	0.40(8)	1.43(6)



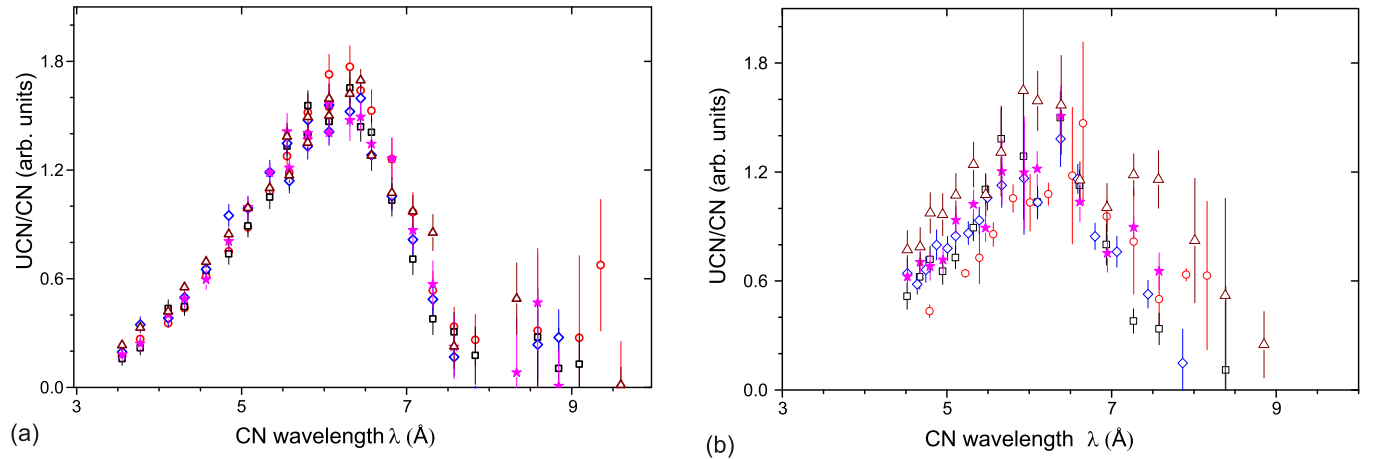


FIG. 5. (Color online) Ultracold neutron production per incident CN from multiphonon processes for  $p = \text{SVP}$  [(red) circles],  $p = 6$  bar [(black) squares],  $p = 11$  bar [(blue) diamonds],  $p = 16$  bar [(magenta) stars], and  $p = 20$  bar [(brown) triangles]. (a) Data measured after subtracting the single-phonon part (see text); (b) calculations from inelastic scattering data for  $p = \text{SVP}$  [(red) circles],  $p = 5$  bar [(black) squares],  $p = 10$  bar [(blue) diamonds],  $p = 15$  bar [(magenta) stars], and  $p = 20$  bar [(brown) triangles].

look at

$$R_I \propto N\beta\lambda^{*4} S^* \left. \frac{d\phi}{d\lambda} \right|_{\lambda^*}, \quad (1)$$

as derived in an unpublished note by Pendlebury (see also [1]), where the single-phonon scattering intensity  $S^* = S(q^*, \omega^*)$  decreases from  $S^*(\text{SVP}) = 0.118(8)$  to  $S^*(20 \text{ bar}) = 0.066(6)$  [32]. This change in the structure factor explains most of the observed decrease. Smaller contributions come from the change in  $\lambda^*$  and from the reduced overlap between the dispersion relation of He-II and that of the free neutron taken into account by the parameter  $\beta(\text{SVP}) = 1.42$  to  $\beta(20 \text{ bar}) = 1.21$  (values deduced from the scattering data [30]; see [33]). The increase in the helium number density  $N$  [ $10^{22} \text{ cm}^{-3}$ ] from  $N(\text{SVP}) = 2.1836$  to  $N(20 \text{ bar}) = 2.5349$  (calculated from the mass densities at 0.1 K from [40]) cannot compensate these effects. Note that the factor  $\left. \frac{d\phi}{d\lambda} \right|_{\lambda^*}$  does not contribute to the normalized data in Fig. 4. Its inclusion for a typical CN spectrum also does not compensate the discussed decreases. This behavior confirms the results from calculations, which agree within errors with the experimental results (see Table I and Fig. 6).

We observe a displacement of all measured single-phonon production rate peaks to wavelengths lower than anticipated from the crossing points of the free neutron dispersion curve with the He-II curve. This can be explained by an unintentional displacement of TOF monitor by 5 cm, the width of the detector. This most probably happened during the setup for the second measurement period (the only one which delivered data). For this reason we present all our results in Table I using a “corrected” wavelength scale,  $\lambda_{\text{cor}} = 1.025 \cdot \lambda$ .

In the multiphonon range we observed a discrepancy between the measured and the calculated pressure dependence of the UCN production rate (see Table I and Fig. 5). From calculations we would have expected an increase with pressure, whereas no increase could be observed. The observed pressure independence of the storage time constant does not indicate a change in the UCN extraction probability from the converter

vessel with pressure. Note that our experimental approach provides a direct relative comparison of the production rates at different pressures: For a fixed wavelength, the same incident beam was used. Pressure-dependent UCN losses (e.g., due to cracks in the coating of the storage vessel) are independent of the CN wavelength.

One explanation for the discrepancy in the multiphonon region could be a change in the dynamic structure factor  $S(q, E)$  with temperature. The calculations in Refs. [32,33] employ scattering data measured at 0.5 K, whereas our measurements were done at 1.1 K. An increasing temperature results, for example, in a broadening of the single-phonon excitation. This increase is small at low temperatures but becomes large towards the  $\lambda$  transition [30]. In Ref. [30] the temperature dependence of the single-phonon excitation linewidth for different pressures was determined from fits to the measured

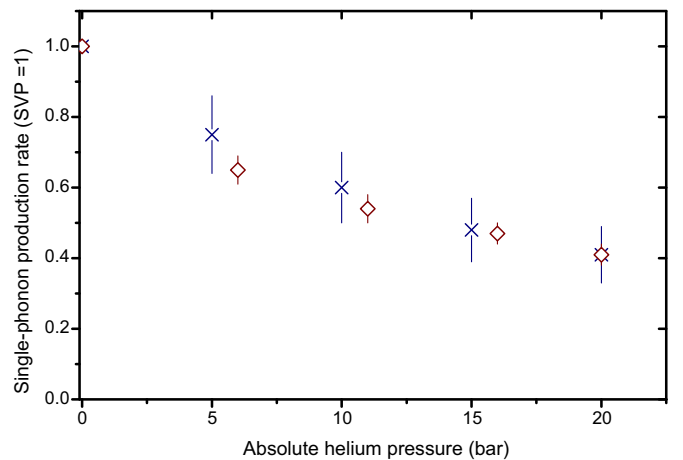


FIG. 6. (Color online) Comparison of the pressure dependence of single-phonon UCN production from this experiment [(brown) diamonds] and from calculations from scattering data [(blue) X's] [32,33]. Both dependencies have been normalized to the respective production rate at SVP.

dynamic structure factor. No significant change in these values was found below about 1.3 K. Likewise, the multiphonon scattering varies only weakly with temperature [30]. Therefore we consider the scattering data measured at 0.5 K as adequate to predict UCN production at 1.1 K. Note that the temperature also influences UCN up-scattering, but this effect cannot explain the observed discrepancy, as it is independent of the CN wavelength, and would also shift the single-phonon data from expectation.

Assuming no significant change in the dynamic structure factor between 0.5 and 1.1 K, the observed discrepancy can only be explained by an effect depending on both the CN wavelength and the He pressure, such as inelastic scattering to other than UCN energy. Inelastic scattering has two types of consequences: (i) a reduction in the beam intensity averaged over the production volume with respect to the incident one, as scattered neutrons may leave the production volume sideways; and (ii) a change in the CN energy, which may influence the probability of UCN production for the scattered neutron (multiple scattering). Neither effect is taken into account in the calculations.

In order to estimate the reduction in the beam intensity, (i), we use the wavelength- and temperature-dependent transmission of neutrons through liquid He at SVP measured by Sommers *et al.* [41]. We calculate the volume-average CN flux in the multiphonon range (from 3.5 to 7.5 Å) inside the production volume relative to the incoming flux:

$$t_{\text{m-ph}} = \int_{\text{m-ph}} \frac{d\phi}{d\lambda} t(\lambda) d\lambda \int_{\text{m-ph}} \frac{d\phi}{d\lambda} d\lambda. \quad (2)$$

Values between 3.5 and 4.52 Å were obtained from linear extrapolation of the data given there. We obtain  $t_{\text{m-ph}}(\text{SVP}) = 0.89$ . For 8.9 Å, the correction is  $t_{\text{s-ph}}(\text{SVP}) = 0.98$ . Note that for a longer production volume, the correction would be larger. We define multiphonon and single-phonon production rates,  $R_{\text{II}}$  and  $R_{\text{I}}$ , as integrals over the respective regions in the CN-normalized UCN production spectrum shown in Fig. 4. In order to compare the observed ratio  $R_{\text{II}}/R_{\text{I}}(\text{SVP}) = 0.14(1)$  with the calculations, we need to correct the prediction with the geometry specific attenuation,  $t_{\text{m-ph}}/t_{\text{s-ph}} \cdot R_{\text{II}}^{\text{calc}}/R_{\text{I}}^{\text{calc}}(\text{SVP}) = 0.11(1)$ .

A reduction in CN transmission  $t_{\text{m-ph}}$  with increasing pressure could explain the observed discrepancy between the measured and the calculated pressure dependence of multiphonon UCN production. Unfortunately, a quantitative confirmation of this hypothesis is not possible, due to the lack of transmission data for higher pressures. Also, scattering data for different pressures [30] do not cover the high- $q$  range needed to calculate the transmission via total scattering.

The change in the CN energy caused by inelastic scattering, (ii), depends on the incident wavelength and the pressure. Scattering to the wavelength  $\lambda^*$  is kinematically possible and would increase the probability of UCN production by the scattered CNs; however, the width of single-phonon UCN production is very small. Multiple scattering was not taken into account in the calculations [32,33]. Its contribution to the UCN production in our setup was estimated by Monte Carlo simulations [42] based on the McStas package [43,44]. For

SVP, multiple scattered CNs were found to contribute about 6% to the UCN production rate in the multiphonon region. This fraction decreases slightly with increasing pressure, to 5% for  $p \geq 10$  bar. The weak pressure dependence of this small contribution cannot explain the discrepancy between the observed and the expected pressure dependence of multiphonon UCN production. It changes the calculated relative production rates at SVP,  $t_{\text{m-ph}}/t_{\text{s-ph}} \cdot R_{\text{II}}^{\text{calc}}/R_{\text{I}}^{\text{calc}}(\text{SVP})$ , to 0.12(1).

However, it should be noted that the accuracy of the simulations and calculations is limited by the available scattering data: Single data sets cover only a limited ( $q, \omega$ ) range or provide a limited resolution. Therefore, data sets [45–47] from different instruments and with different resolution settings had to be combined in the simulations [42]. The scattering data [30] used for the calculations [32,33] were obtained at two incident wavelengths at IN6: 4.1 Å for SVP and 4.6 Å for higher pressures. Possibly uncorrected effects may contribute to the observed discrepancies.

## VI. CONCLUSION

We have investigated CN-wavelength-dependent UCN production in pressurized He-II for pressures up to 20 bar. The single-phonon UCN production peak moves to a shorter wavelength and decreases in intensity, whereas the absolute contribution from multiphonon processes stays constant within the experimental uncertainties. We have found that predictions from calculations based on inelastic neutron scattering data [32,33] agree well with the behavior of the single-phonon UCN production rate. However, the same calculations disagree with our measurement in the multiphonon range. There is no indication of a significant change in the dynamic structure factor between 0.5 and 1.1 K that could invalidate the calculations for our experiment. However, the disagreement could be caused by a pressure- and wavelength-dependent attenuation of the CN beam in He-II. This hypothesis could not be tested due to a lack of transmission data at higher He pressures. Note that the ratio of multiphonon-to-single-phonon UCN production would decrease for longer production volumes. The calculations also did not take into account modifications of the CN spectrum by inelastic scattering inside He-II, but Monte Carlo simulations showed that the contribution of UCN production by multiple scattered CNs and its pressure dependence are too small to explain the observed disagreement.

The disagreement of the position of the single-phonon peak at SVP with earlier measurements by Yoshiki and coworkers [48] and Baker and coworkers [17] can probably be explained by an accidental displacement of the TOF detector in our experiment.

In general, the relative UCN production rate due to single-phonon and multiphonon processes depends upon the incident CN spectrum. For the spectrum in our experiment we have found that  $(30 \pm 2)\%$  of the total UCN production over all incident wavelengths is from multiphonon processes. Baker and coworkers [17] found a multiphonon contribution of  $(24 \pm 2)\%$  for a different CN beam. Note that, according to our previous discussion, also the length of the UCN production

volume (which was 326 mm in the experiment of Baker and coworkers) influences this ratio.

Using the entire spectrum of a white beam might still be advantageous for a powerful UCN source, as monochromatization by a crystal not only cuts out a narrow wavelength band around 8.92 Å but also reduces the intensity of the Bragg reflected beam substantially (by a factor of 2–5 [20,32]). In either case, monochromatic or white incident beam, the best results are obtained for He-II at SVP, without even taking into account the increase in technical complexity when going to higher pressures. For future searches of the neutron electric dipole moment it might still be beneficial to apply a pressure of a few hundred millibars to increase the dielectric strength without losing significantly in UCN production. A future

perspective to increase UCN production might be the use of solid helium as the UCN converter, which was not possible to investigate during this experimental run.

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