# Measurements of $^{152}\mathrm{Gd}(p,\gamma)^{153}\mathrm{Tb}$ and $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$ reaction cross sections for the astrophysical $\gamma$ process

R. T. Güray, <sup>1,\*</sup> N. Özkan, <sup>1</sup> C. Yalçın, <sup>1</sup> T. Rauscher, <sup>2,3</sup> Gy. Gyürky, <sup>4</sup> J. Farkas, <sup>4</sup> Zs. Fülöp, <sup>4</sup> Z. Halász, <sup>4</sup> and E. Somorjai <sup>4</sup> Department of Physics, Kocaeli University, Umuttepe 41380, Kocaeli, Turkey <sup>2</sup>Centre for Astrophysics Research, School of Physics, Astronomy and Mathematics, University of Hertfordshire, Hatfield 9AL 10AB, United Kingdom <sup>3</sup>Department of Physics, University of Basel, CH-4056 Basel, Switzerland <sup>4</sup>MTA Institute for Nuclear Research (MTA Atomki), H-4001 Debrecen, Hungary (Received 26 November 2014; published 29 May 2015)

The total cross sections for the  $^{152}\mathrm{Gd}(p,\gamma)^{153}\mathrm{Tb}$  and  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  reactions have been measured by the activation method at effective center-of-mass energies  $3.47 \leqslant E_{\mathrm{c.m.}}^{\mathrm{eff}} \leqslant 7.94$  MeV and  $4.96 \leqslant E_{\mathrm{c.m.}}^{\mathrm{eff}} \leqslant 7.94$  MeV, respectively. The targets were prepared by evaporation of 30.6% isotopically enriched  $^{152}\mathrm{Gd}$  oxide on aluminum backing foils, and bombarded with proton beams provided by a cyclotron accelerator. The cross sections were deduced from the observed  $\gamma$ -ray activity, which was detected off-line by an HPGe detector in a low background environment. The results are presented and compared with predictions of statistical model calculations. This comparison supports a modified optical proton+ $^{152}\mathrm{Gd}$  potential suggested earlier.

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#### I. INTRODUCTION

Only the lightest elements (hydrogen, helium, and traces of lithium, beryllium) originate from a hot Big Bang phase in the early stage of the universe [1-3]. All other nuclei have been produced thereafter in stars and stellar explosions. Most nuclides above the Fe group (mass numbers  $A \gtrsim 60$ ) originate from neutron captures and subsequent  $\beta$  decays and thus are called neutron-capture elements [4-6]. Two main processes have been identified, the s process [slow neutron capture process, with a main component occurring in medium mass asymptotic giant branch (AGB) stars and a weak component stemming from massive stars] and the r process (rapid neutron capture process) [7–9]. The site of the latter process is disputed but core-collapse supernova explosions and/or neutron star mergers may provide viable alternatives [10]. There are a number of proton-rich isotopes between Se and Hg which cannot be produced by either process. They are called p nuclei and further nucleosynthesis processes have to be invoked to explain their existence [11]. Among the originally 35 p nuclei [4,5], large s process contributions to <sup>164</sup>Er, <sup>152</sup>Gd, and <sup>180</sup>Ta were found in modern AGB models [12]. Also the abundances of <sup>113</sup>In and <sup>115</sup>Sn may receive contributions from the s and/or r process [13].

The currently accepted production mechanism for the bulk of p nuclei is the so-called  $\gamma$  process, synthesizing proton-rich isotopes by photodisintegration reactions [11,14]. The  $\gamma$  process occurs in the outer layers of a massive star during its core-collapse supernova explosion [15–17]. As an additional site, type Ia supernovae have been suggested, where also the required temperatures are achieved [18–21]. In both sites, quickly expanding zones of hot matter show production of p nuclei when the reached peak temperatures are in the range  $2 \leqslant T \leqslant 3.5$  GK. To produce the heavier p nuclei

it is necessary to stay at the lower end of this temperature range because they would be completely destroyed at higher temperatures. On the other hand, the higher end of the temperature range is required for the production of the light p nuclei because lighter nuclei are more strongly bound and less easily photodisintegrated [11,22,23].

The very rare  $^{138}$ La cannot be produced in a  $\gamma$  process but it was suggested to be formed through neutrino reactions on stable nuclei in core-collapse supernovae, the so-called  $\nu$  process [24,25].

A  $\gamma$  process starts with  $(\gamma,n)$  reactions on stable nuclei already present in the stellar plasma. When the temperatures remain high for a sufficiently long time, proton-rich isotopes are reached for which  $(\gamma,p)$  or  $(\gamma,\alpha)$  reactions are faster than  $(\gamma,n)$ . This leads to a deflection of or branching in the nucleosynthesis path [22,23]. Because of the nuclear structure influencing the binding energies,  $(\gamma,p)$  deflections are mainly found in nuclei with neutron number N < 82, whereas  $(\gamma,\alpha)$  branchings are important in the region  $N \ge 82$  [11,22].

Stellar photodisintegration rates used in reaction network calculations are usually derived from *stellar* capture *rates* by applying the principle of detailed balance [26–30]. It should be noted that this reciprocity only applies to stellar rates, involving thermally excited nuclei in the entrance and exit channels, but not to laboratory capture cross sections and their respective photodisintegration cross sections, unless the cross sections are dominated by single transitions between initial state, compound state, and final state [26,31,32]. Reactions involving light nuclei often include only a few transitions but this is never the case in the regime of high level densities encountered in nuclei participating in the synthesis of p nuclei. Although direct  $(\gamma, n)$  measurements have been performed also for intermediate and heavy nuclei (e.g., [33–35]), it was shown that these cannot constrain stellar rates, as they only allow one to study a single  $\gamma$  transition from the ground state of the target nucleus. Its contribution to the stellar rate is less than 0.1%, contrary to capture data which allow one to constrain a

<sup>\*</sup>tguray@kocaeli.edu.tr

much larger fraction (on the order of several tens of percent, depending on plasma temperature and the nuclear level structure) of the stellar capture rate (see, e.g., [11,30,36–41]). The contribution of  $(\gamma,p)$  and  $(\gamma,\alpha)$  ground-state transitions to the stellar rate is even lower because of the shift of the Gamow window to higher compound excitation energies [40]. Interestingly, the ground-state contribution of the respective capture rates even is larger than those for  $(n,\gamma)$  at the same temperature because of Coulomb suppression of transitions with low relative energy [37,38,42]. This even applies to captures with negative reaction Q values on intermediate and heavy targets, allowing ground-state capture to always constrain a much larger fraction of the stellar rates than photodissociation measurements.

Although capture measurements still cannot completely constrain a high-temperature stellar rate, either, they can be used to test the predictions of charged particle widths. Proton and  $\alpha$  widths determine the stellar photodisintegration rates because  $\gamma$ -process temperatures, although being high even for stellar plasmas, still translate to comparatively low nuclear interaction energies, below the Coulomb barrier when involving charged particles. This results in charged particle widths being smaller than the  $\gamma$  widths and thus a dependence of the rates primarily on these charged particle widths rather than on the  $\gamma$  widths [11,40]. Experiments can probe the charged particle widths in capture reactions but the small cross sections at sub-Coulomb energies make it difficult to measure in the astrophysical energy range. Therefore, astrophysically relevant data are scarce. The few available data have shown considerable deviations from predictions, especially for reactions with  $\alpha$  particles [11,43,44]. Low-energy proton captures have been found to be predicted more reliably, although small modifications to the optical proton+nucleus potentials have been suggested [45].

Proton capture reaction cross sections for the  $\gamma$  process have been measured before, e.g., by [37,45–62]. Because  $(p,\gamma)$  above the (p,n) threshold are sensitive not only to the proton width but also to the neutron and  $\gamma$  widths, additional information is required to be able to distinguish the impact of the various widths (see also Sec. III B 1). Such information can be obtained through a simultaneous (p,n) measurement because the (p,n) cross section well above the threshold is mainly determined by the proton width. Some (p,n) measurements have been performed on s or r process seed nuclei that affect the abundances of the light p nuclei, e.g.,  $^{76}$ Ge [45],  $^{82}$ Se [47],  $^{85}$ Rb [37], and on a p nucleus  $^{120}$ Te [46].

Here, we present a simultaneous measurement of  $(p,\gamma)$  and (p,n) cross sections of <sup>152</sup>Gd. Although the  $\gamma$ -process contribution to <sup>152</sup>Gd is small and originates from  $(\gamma,n)$  reactions on other Gd isotopes, a determination of proton-induced cross sections at low energy of this proton-rich, heavy nucleus allows one to test statistical model predictions well below the Coulomb barrier. For the first time, it was also possible to determine proton capture reaction cross sections below the (p,n) threshold for this nucleus.

The  $^{152}\text{Gd}(p,\gamma)^{153}\text{Tb}$  and  $^{152}\text{Gd}(p,n)^{152}\text{Tb}$  activation measurements have been performed in an energy range between 3.47 and 7.94 MeV as a test of the statistical model predictions

over a broader energy region. The details of the experiment are given in Sec. II. The experimental cross sections are compared to predictions in the Hauser-Feshbach statistical model in Sec. III. A summary and conclusions are provided in Sec. IV.

# II. EXPERIMENTAL PROCEDURE

The reaction cross sections of  $^{152}\mathrm{Gd}(p,\gamma)^{153}\mathrm{Tb}$  and  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  were measured using an activation technique. The target preparation and the experiment were performed using the laboratory facilities at the Institute for Nuclear Research of the Hungarian Academy of Sciences (MTA Atomki). After the target preparation, the experiment has two stages, first the activation of the target and then the determination of the number of  $\beta$ -unstable reaction products using an off-line gamma detection system. The measurement of proton induced reactions with the activation technique is discussed in detail in Refs. [57,59].

#### A. Target preparation

The 30.6% isotopically enriched  $^{152}$ Gd oxide in powder form was provided by the company ISOFLEX USA, Certificate No. 64-02-152-1453. For the target backing, high purity thin (2.5  $\mu$ m) aluminum foils, obtained from Espi Metal, were used. The targets were prepared by vacuum evaporation.

There are two methods available in the vacuum chamber to evaporate the target material: via the resistive heating method and the use of an electron gun. Because of the high melting point ( $\approx\!2350\,^\circ\text{C})$  of gadolinium oxide  $Gd_2O_3$ , the electron gun was used for the evaporation. Before the evaporation, 40 mg  $Gd_2O_3$  powder was pressed into a pellet with 6 mm diameter. This  $Gd_2O_3$  pellet was placed in a tantalum boat and directly heated by the electron beam.

The target holder was made of aluminum with nine holes (each hole has 1.2 cm inside diameter) and Al backing foils with the size of  $1.5 \times 1.5$  cm<sup>2</sup> were placed on these holes. The target holder was placed 7 cm above the tantalum boat for Gd<sub>2</sub>O<sub>3</sub> deposition. At the same time nine targets were produced with thicknesses varying between 220  $\mu$ g/cm<sup>2</sup> and 310  $\mu$ g/cm<sup>2</sup>. After the evaporation, the targets were fixed into target frames made of aluminum with 3.8 cm outer diameter, 1.2 cm inner diameter, and 3 mm thickness. The target thickness was determined by weighing. The weight of the Al foil was measured before and after the evaporation with a precision better than 5  $\mu$ g and the Gd<sub>2</sub>O<sub>3</sub> number density could be determined from the difference. The target with the thickness of 310  $\mu$ g/cm<sup>2</sup> was also examined by the Rutherford back scattering (RBS) method with a microprobe to investigate the target homogeneity. The RBS spectra were taken at the Van de Graaff accelerator of MTA Atomki with 2.0 MeV  $\alpha$  particles using a 3 × 3  $\mu$ m<sup>2</sup> beam spot size and  $100 \times 100 \ \mu \text{m}^2$  scanning size. The largest difference in the target thickness between two points on the target was found to be 7%.

### **B.** Activation

To activate the  $^{152}{\rm Gd}$  targets, they were irradiated with a proton beam in an energy range between 3.5 and 8.0 MeV at the

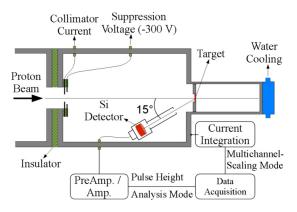


FIG. 1. (Color online) A schematic diagram of the irradiation chamber mounted at the end of the beam line at the cyclotron accelerator of MTA Atomki.

cyclotron accelerator of MTA Atomki. The proton energy was changed by 0.5 MeV steps in the laboratory frame. Figure 1 shows a schematic diagram of the irradiation chamber mounted at the end of the beam line. The beam current was measured with a current integrator using the entire chamber as a Faraday cup, after the last beam defining aperture. The beam current was kept as stable as possible at 2  $\mu$ A. The integrated current was recorded in time intervals of one minute and the changes in the beam current during the activation was taken into account in the data analysis. The activations for different proton energies lasted between 0.5 and 30 h, based on the requirement of sufficient counting statistics.

To suppress the secondary electrons from the targets, a bias voltage of -300 V was applied to the entrance of the target irradiation chamber. Backscattered protons were detected to monitor the target stability during each irradiation by using an ion implanted Si detector with a reduced entrance aperture of 0.5 mm diameter at an angle of  $165^{\circ}$  with respect to the beam direction, as shown in Fig. 1.

The target taken from the irradiation chamber after the activation was transferred to the off-line gamma detection system to determine the number of reaction products of the proton induced reactions on <sup>152</sup>Gd.

# C. Determination of the <sup>153</sup>Tb and <sup>152</sup>Tb activities

To determine the number of Tb isotopes, the  $\gamma$  radiation following their electron-capture decays was counted with a 100% relative efficiency HPGe detector in a complete  $4\pi$  low background lead shielding. After the end of each activation, the  $^{152}$ Gd target was mounted in a holder placed 10 cm from

the end of the detector cap. The  $\gamma$  spectra were taken between 2.5 and 114 h, depending on the counting statistics, and were stored regularly in every hour, thus different isotope decays could be analyzed.

The activation technique can be used to measure the reaction cross sections of  $^{152}\mathrm{Gd}(p,\gamma)^{153}\mathrm{Tb}$  and  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  because  $\beta$ -decay half-lives of the reaction products in both cases are long enough to determine their yields (Table I). For  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$ , the product  $^{152}\mathrm{Tb}$  has ground ( $^{152g}\mathrm{Tb}$ ) and isomeric states ( $^{152m}\mathrm{Tb}$ ), but  $^{152m}\mathrm{Tb}$  disintegrates 78.8% through internal transitions and 21.2% by  $\beta$  decay [63]. The contribution of  $^{152m}\mathrm{Tb}$  to the total  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  reaction cross section is negligible within uncertainties, as was verified in a calculation with the TALYS code [64].

For the analysis of the  $^{152}{\rm Gd}(p,\gamma)^{153}{\rm Tb}$  reaction data, the 212.00-keV  $\gamma$  line was used, which has an emission probability of 31.0% in electron capture of  $^{153}{\rm Tb}$  (half-life 2.34 days). In the case of the  $^{152}{\rm Gd}(p,n)^{152}{\rm Tb}$  reaction, 271.08 and 344.28 keV  $\gamma$  lines with emission probabilities of 8.6% and 65.0%, respectively, were used because they are associated with the decay of the ground state of  $^{152}{\rm Tb}$  with a half-life of 17.5 h. The  $\gamma$  transitions and decay parameters used for the data analysis are summarized in Table I. Figure 2 shows the  $\gamma$ -ray spectrum recorded for a counting time of 3.64 h after a 2.08-h activation with a 7-MeV proton beam. The  $\gamma$  transitions used in the measurements, as given in Table I, are also indicated in the figure.

The  $\gamma$ -detection system was the same as the one used in a previous  $^{130,132}$ Ba experiment and is described in detail in [65]. The absolute photopeak efficiency calibration was performed for a detector-target distance of 27 cm, where true coincidence summing effects are negligible, using the calibrated sources,  $^7$ Be,  $^{22}$ Na,  $^{54}$ Mn,  $^{57}$ Co,  $^{60}$ Co,  $^{65}$ Zn,  $^{133}$ Ba,  $^{137}$ Cs,  $^{152}$ Eu, and  $^{241}$ Am. Although the true coincidence summing effect could be expected to be small at a distance of more than 10 cm between the detector and the target, it was taken into account using the following method.

A  $^{152}$ Gd target was irradiated at a proton energy of 8.0 MeV in the laboratory frame and then the  $\gamma$  spectrum of the reaction products was measured at both 27- and 10-cm distances. Taking into account the time elapsed between the two countings, the ratio of the count rates taken at 10 cm to the one taken at 27 cm gives the ratio of the photopeak efficiency at 10 cm to one at 27 cm. In this way, an efficiency value at 27 cm can be normalized to the one at 10 cm covering the coincidence effect correction for the  $\gamma$  transition used for the analysis. The photopeak efficiencies of the  $\gamma$  transitions used to identify the products of the investigated reactions are also given in Table I.

TABLE I. Decay parameters of the  $p + {}^{152}\text{Gd}$  reaction products [63] and measured photopeak efficiencies at energies of the  $\gamma$  transitions, as used in the analysis.

Reaction	Product	Half-life	γ Energy (keV)	γ Intensity (%)	Detection efficiency (%)
$\frac{152 \text{Gd}(p, \gamma)}{152 \text{Gd}(p, n)}$	<sup>153</sup> Tb <sup>152</sup> gTb	$(2.34 \pm 0.01)$ days $(17.5 \pm 0.1)$ h	212.00 271.08 344.28	$31.0 \pm 0.2$ $8.6 \pm 0.8$ $65.0 \pm 0.1$	$1.83 \pm 0.09$ $1.53 \pm 0.08$ $1.27 \pm 0.06$

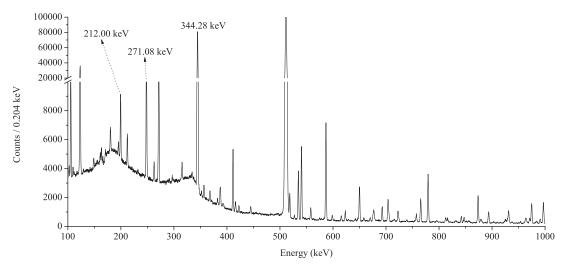


FIG. 2. The  $\gamma$ -ray spectrum recorded for a counting time of 3.64 h after 2.08 h of activation with a 7-MeV proton beam. The  $\gamma$  transitions used in the measurements are indicated by arrows.

#### III. RESULTS AND DISCUSSION

### A. Experimental cross sections

 $^{152}$ Gd $(p, \gamma)^{153}$ Tb of cross sections  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  have been measured at proton energies ranging from 3.5 to 8.0 MeV, in steps of 0.5 MeV. This energy range corresponds to effective center-of-mass energies between 3.47 and 7.94 MeV. The effective center-of-mass energies  $E_{\rm c.m.}^{\rm eff}$  are defined as the center-of-mass energies at which one-half of the reaction yield for the entire target thickness is obtained [31,66]. The experimental cross-section results for the  $(p,\gamma)$  and (p,n) reactions are summarized in Tables II and III, respectively, and are also shown in Fig. 3. The (p,n) channel becomes dominant very fast above its threshold energy (4.8 MeV) and its cross section becomes much higher than that of the  ${}^{152}\text{Gd}(p,\gamma){}^{153}\text{Tb}$  reaction (Fig. 3).

As mentioned in Sec. I, the product of  $^{152}\text{Gd}(p,n)$  reaction has both a ground ( $^{152g}\text{Tb}$ ) and an isomeric state ( $^{152m}\text{Tb}$ ). Based on the results of a TALYS calculation [64], the contribution of  $^{152m}\text{Tb}$  to the (p,n) reaction cross sections is less than 0.9%. This contribution can be neglected, especially because the short-lived isomer decays by high probability (78.8%) to the long-lived ground state of  $^{153}\text{Tb}$ , and is therefore included

TABLE II. Measured cross sections of the  $^{152}{\rm Gd}(p,\gamma)^{153}{\rm Tb}$  reaction.

E <sub>beam</sub> (MeV)	$E_{ m c.m.}^{ m eff}$ (MeV)	Cross section (µb)
3.500	$3.471 \pm 0.014$	$7.6 \pm 0.8$
4.000	$3.968 \pm 0.012$	$43.2 \pm 4.4$
4.500	$4.466 \pm 0.010$	$235 \pm 26$
5.000	$4.962 \pm 0.011$	$692 \pm 65$
5.500	$5.460 \pm 0.009$	$1277 \pm 133$
6.000	$5.956 \pm 0.009$	$1850 \pm 178$
7.000	$6.951 \pm 0.007$	$2796 \pm 298$
7.500	$7.447 \pm 0.006$	$3013 \pm 356$
8.000	$7.943 \pm 0.008$	$3875 \pm 887$

in the counting of the ground-state decay. For the (p,n) reaction, hence, measurements of only  $^{152}\mathrm{Gd}(p,n)^{152g}\mathrm{Tb}$  have been performed. The measured (p,n) cross sections determined from two different  $\gamma$  transitions, as explained in Sec. II C, were found to be statistically consistent with each other. As a result, the weighted averages of the  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  reaction cross sections deduced from these two  $\gamma$  transitions are presented.

The uncertainty in the final results was determined based on the propagation of partial errors: counting statistics (0.2%–21%), decay parameters (0.4%–9%), detection efficiency (5%), target thickness ( $\sim$ 7%), and beam current integration (less than 3%). The uncertainties in the effective center-of-mass energies range between 0.08% and 0.4%; they were calculated with the SRIM code [67] based on the proton energy loss in the targets.

# B. Comparison with Hauser-Feshbach statistical model predictions

# 1. Sensitivity of reaction cross sections to modifications in the predicted total widths

To gauge the dependence of the cross sections on the various ingredients of the calculation and to understand what properties can be constrained by a comparison of predictions and experiment, it is useful to first consider the sensitivities of the astrophysical reaction rates and cross sections. The

TABLE III. Measured cross sections of the  $^{152}$ Gd(p,n) $^{152}$ Tb reaction.

E <sub>beam</sub> (MeV)	$E_{ m c.m.}^{ m eff}$ (MeV)	Cross section (µb)
5.000	$4.962 \pm 0.011$	60 ± 6
5.500	$5.460 \pm 0.009$	$875 \pm 81$
6.000	$5.956 \pm 0.009$	$4530 \pm 413$
7.000	$6.951 \pm 0.007$	$25915 \pm 2365$
7.500	$7.447 \pm 0.006$	$45739 \pm 4174$
8.000	$7.943 \pm 0.008$	$101314 \pm 9241$

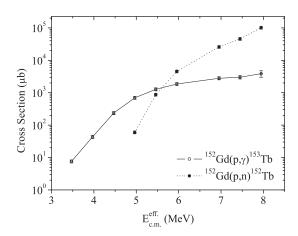


FIG. 3. Experimental cross sections of  $^{152}\text{Gd}(p,\gamma)^{153}\text{Tb}$  and  $^{152}\text{Gd}(p,n)^{152}\text{Tb}$  reactions.

sensitivity s of a cross section or rate C is extensively discussed in [40]. It is defined as

$$s = \frac{\frac{C_{\text{new}} - C_{\text{old}}}{C_{\text{old}}}}{\frac{W_{\text{new}} - W_{\text{old}}}{W_{\text{old}}}},\tag{1}$$

as is the standard in general sensitivity analysis. In the current context, the sensitivity measures by how much a rate or cross section  $\mathcal{C}$  changes when one of the averaged total widths W appearing in the Hauser-Feshbach formalism is varied. For example, if the cross section changes by the same factor by which a width is varied, the sensitivity is s=1.0, if it does not change, s=0. The sign of s provides information on whether the change in  $\mathcal{C}$  is in the same direction as the change in the width (s>0), i.e., increase with increasing width, or in opposite direction (s<0), i.e., decrease with increasing width.

Although the  $^{152}$ Gd( $p,\gamma$ ) rate is not directly important in the  $\gamma$  process, its sensitivity to a variation of the total proton,

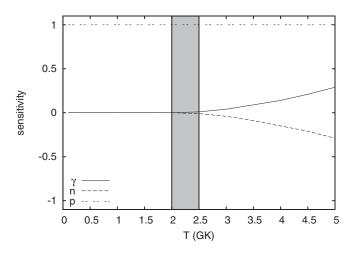


FIG. 4. Sensitivity of the astrophysical reaction rates for  $^{152}\mathrm{Gd}(p,\gamma)^{153}\mathrm{Tb}$  to a variation of total proton, neutron, and  $\gamma$  widths as a function of plasma temperature T. The temperature range relevant for the nucleosynthesis of heavy p nuclei is marked by the shaded area.

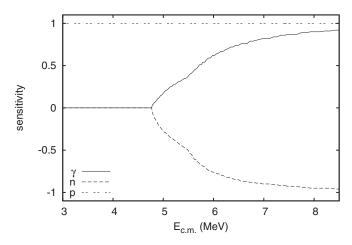


FIG. 5. Sensitivity of the cross sections of  $^{152}\text{Gd}(p,\gamma)^{153}\text{Tb}$  to a variation of total proton, neutron, and  $\gamma$  widths as function of center-of-mass energy  $E_{\text{c.m.}}$ .

neutron, and  $\gamma$  width is shown in Fig. 4. Similar results are also obtained for most  $(p,\gamma)$  reactions in the p nuclei range below N=82. Because of the Coulomb barrier, the proton widths are quickly becoming smaller than the  $\gamma$  widths and thus dominate the sensitivity. Therefore it is of astrophysical interest whether the present experimental data can confirm the predictions of proton widths. Figures 5 and 6 show the sensitivities of the reaction cross sections of  $^{152}\text{Gd}(p,\gamma)^{153}\text{Tb}$  and  $^{152}\text{Gd}(p,n)^{152}\text{Tb}$ , respectively, to variations of predicted total widths as a function of center-of-mass energy, within the same energy range as shown in Figs. 7 and 8. All cross sections are insensitive to the total  $\alpha$  width as it is too small and therefore it is not shown in the figures.

Below the (p,n) threshold, the  $(p,\gamma)$  cross section is only sensitive to the proton width, above it the importance of  $\gamma$  and neutron width quickly increase with increasing energy. The situation is reversed in the (p,n) reaction cross section which becomes less and less dependent on the  $\gamma$  and neutron widths with increasing energy. In both reactions, however, the sensitivities on the two widths act oppositely. This has to be taken into account when trying to reproduce data for

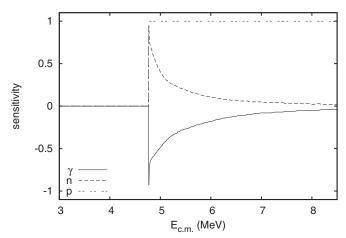


FIG. 6. Same as Fig. 5 but for  $^{152}$ Gd $(p,n)^{152}$ Tb.

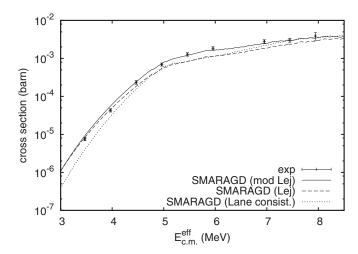


FIG. 7. Experimental cross sections (exp) of  $^{152}\text{Gd}(p,\gamma)^{153}\text{Tb}$  as a function of effective center-of-mass energy  $E_{\text{c.m.}}^{\text{eff}}$ , compared to statistical model calculations using different optical  $p+^{152}\text{Gd}$  potentials: the potentials by [71,72] (Lej), by [73] (Lane consist.), and by [37,38,45] (mod Lej).

both reactions simultaneously. Regarding the proton width, it dominates the cross-section sensitivity at the lowest measured energies in the  $(p,\gamma)$  reaction and at the highest measured energies in the (p,n) reaction.

It has to be noted that different nuclear properties enter the calculation of the widths (for details, see Sec. 5.4 in [30]). For the particle widths, most important are optical potentials required for the calculation of transmission coefficients and low-lying excited states. In the radiation width, transitions to states at higher excitation energy are important [39] and therefore this width is sensitive to the choice of  $\gamma$ -strength function and nuclear level density. The latter enters because it is used above the last included discrete excited state in a nucleus [see, e.g., Eq. (64) in [30]].

Close to stability, nuclear spectroscopic information is abundant but nevertheless it is not trivial to decide at which excitation energy to set the cutoff for inclusion of

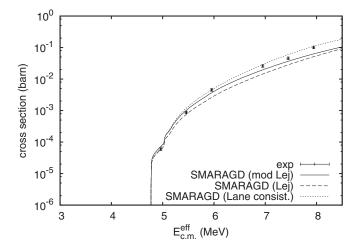


FIG. 8. Same as Fig. 7 but for  $^{152}$ Gd $(p,n)^{152}$ Tb.

experimentally determined nuclear levels in each nucleus. It is essential for the correct prediction of particle widths to use a complete level scheme. Towards higher excitation energies, more levels are missed in experimental studies and the level information given in the usual databases cannot be considered to be complete anymore. This may lead to misestimated widths in the calculation when contributing transitions are not included because of the missing excited states. In this case it is advantageous to only include the lowest experimental levels and use a theoretical level density above them, even when further levels have been identified at higher excitation energies (see, e.g., Sec. 5.4.2 in [30]). A practical example for this was discussed in [68]. This is not an issue in  $\gamma$  widths close to stability because the mainly contributing  $\gamma$  transitions involve states at high excitation energies, in the unresolved resonance region, anyway [39].

The theoretical calculations shown in Sec. 7 have been obtained with Version 0.8.4s of the nuclear reaction code SMARAGD [69], which makes use of level schemes from [70], also included in the 2010 version of NUDAT [63]. At most 40 experimental states are used for each nucleus, as long as they are found as a consecutive sequence of levels with known spin and parity assignment. A peculiar situation arises for the neutron widths in the reactions studied here: The (p,n) energy range measured here extends into a region of incomplete level information because only rotational bands with spins  $J \ge 8$  are known above 345-keV excitation energy in <sup>152</sup>Tb. Varying neutron and  $\gamma$  widths, as well as the included <sup>152</sup>Tb levels, it was found that a simultaneous reproduction of the (p,n) and  $(p,\gamma)$  data is only possible when using a theoretical nuclear level density above 345 keV. This indicates that further, unidentified low-spin levels must be present in addition to the experimentally determined rotational bands, which is not surprising as the total level density is expected to strongly increase with increasing excitation energy. No such problem was found for the proton width, indicating that the relevant excited states at low energy are already included in the experimental level scheme.

It should further be noted that the above treatment of excited states was also used to calculate the sensitivities shown in Figs. 4–6. Therefore they differ from the sensitivities given in [40], which used the default NUDAT set of experimental states.

## 2. The optical $p+^{152}Gd$ potential

As pointed out above, the low-energy proton width is the quantity of astrophysical interest here. As shown in Figs. 5 and 6 the cross sections are sensitive to the proton widths across all investigated energies. The additional dependence on the neutron and  $\gamma$  widths can be addressed by simultaneously comparing to the  $(p,\gamma)$  and (p,n) data which exhibit different sensitivities, as discussed above. Because the sensitivities are almost symmetric in the neutron and  $\gamma$  widths, only the ratio between the two widths can be determined. For the reactions discussed here, however, the neutron width is already well determined through the requirement of (p,n) cross-section reproduction close above the threshold, which was also used to study the excited states cutoff (Sec. III B 1). Any remaining discrepancies between theoretical and experimental cross

sections at the high end of the measured energy range of the  $(p,\gamma)$  reaction and close to the (p,n) threshold are likely from deficiencies in either the theoretical description of the proton width through an optical potential or the  $\gamma$  width, which includes two only theoretically known quantities, the  $\gamma$ -strength function and the nuclear level density. The action of the two widths can be distinguished, however, through their different impact on the  $(p,\gamma)$  and (p,n) cross sections.

We compared the measured cross sections to SMARAGD predictions using different popular optical p+nucleus potentials while keeping all other ingredients to the calculations fixed. The results are shown in Figs. 7 and 8. Essential is a simultaneous reproduction of  $(p, \gamma)$  and (p, n) data. Of special interest is the comparison with the three lowest  $(p, \gamma)$  data points which are below the (p,n) threshold, where the cross sections are only sensitive to the proton width. At all other energies, the impacts of neutron, proton, and  $\gamma$  widths have to be disentangled. The semimicroscopic optical potential of [71], including low-energy modifications for astrophysics by [72] (marked "Lej" in Figs. 7 and 8), was also used in the large-scale reaction rate calculations of [29]. It results in a different energy dependence than observed in the low-energy  $(p,\gamma)$  cross sections although the absolute magnitude is reproduced well at these energies. There is also a problem at the higher energies. Because the predicted cross sections are below the data for both reactions, it is not possible to amend this problem by changing the  $\gamma$  and/or neutron width.

Similarly to the potential by [71,72], the more recent potential by [73] (marked "Lane-consist." in the figures) is the Lane-consistent version of a potential obtained from a Brückner-Hartree-Fock model using a local density approximation but with parameters fitted to recent experimental data. Although the (p,n) cross sections at higher energy are reproduced well with this potential, the low-energy  $(p,\gamma)$  cross sections are significantly below the data. Changing the ratio of the neutron and  $\gamma$  width cannot improve the overall agreement as it mostly affects the cross sections at the highest energies in the  $(p,\gamma)$  reaction and the ones at the lowest energies in the (p,n) reaction, while the  $(p,\gamma)$  cross sections below the (p,n) threshold remain unchanged.

Finally, it was found in previous work [37,38,45] that an improved description of low-energy  $(p, \gamma)$  data is possible with a modified imaginary part of the potential by [72]. Also for the

two reactions discussed here, use of this potential (marked as "mod Lej" in the figures) yields the best overall description of the data. A further slight improvement at low (p,n) and high  $(p,\gamma)$  energies can be achieved by increasing the  $\gamma$  width by about 10% but this does not change the conclusions regarding the proton optical potential.

#### IV. SUMMARY AND CONCLUSIONS

The reaction cross sections of  $^{152}\mathrm{Gd}(p,\gamma)^{153}\mathrm{Tb}$  and  $^{152}\mathrm{Gd}(p,n)^{152}\mathrm{Tb}$  have been measured by the activation method at effective center-of-mass energies  $3.47 \leqslant E_{\mathrm{c.m.}}^{\mathrm{eff}} \leqslant 7.94~\mathrm{MeV}$  and  $4.96 \leqslant E_{\mathrm{c.m.}}^{\mathrm{eff}} \leqslant 7.94~\mathrm{MeV}$ , respectively, to extend the experimental database towards the heavier mass region for astrophysical reactions and to test the reliability of statistical model predictions. For the first time,  $(p,\gamma)$  cross sections below the (p,n) threshold of  $p+^{152}\mathrm{Gd}$  were obtained, allowing one to study the prediction of proton widths well below the Coulomb barrier.

Although the cross sections depend on a number of nuclear properties, by combining the  $(p,\gamma)$  and (p,n) data it was possible to disentangle the contributions of these ingredients and to focus on a test of the optical  $p+{}^{152}\text{Gd}$  potential. The measured cross-section values were compared to Hauser-Feshbach statistical model calculations using the nuclear code SMARAGD [69]. A good reproduction of all data across all measured energies can be obtained with the recently suggested potential by [45] which is a modification of [71,72].

Further experiments to obtain  $(p,\gamma)$  data at even lower energies than studied here would be desirable but will prove very challenging because of the tiny reaction cross sections.

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