Hybrid model approach for strange and multistrange hadrons in 2.76A TeV Pb + Pb collisions

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Using the VISHNU hybrid model, we calculate the multiplicity, spectra, and elliptic flow of Λ , Ξ , and Ω in 2.76A TeV Pb + Pb collisions. Comparisons between our calculations and the ALICE measurements show that the model generally describes the soft hadron data of these strange and multistrange hadrons at several centrality bins. Mass ordering of elliptic flow among π , K, p, Λ , Ξ , and Ω has also been studied and discussed. With a nice description of the particle yields, we explore chemical and thermal freeze-out of various hadrons species at the Large Hadron Collider within the framework of the VISHNU hybrid model.

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I. INTRODUCTION

Many measurements, such as jet quenching, elliptic flow, and valence quark number scaling of elliptic flow, have provided strong evidence for the creation of the quark-gluon plasma (QGP) in heavy ion collisions at the Relativistic Heavy-Ion Collider (RHIC) and the Large Hadron Collider (LHC) [1–4]. With the formation of QGP and the restoration of chiral symmetry, strange and antistrange quarks become abundant in the bulk medium above T_c , which subsequently enhances the productions of strange and multistrange hadrons in relativistic heavy ion collisions [5]. In the past decades, different aspects of strange and multistrange hadrons have been studied in theory [5-14] and in experiment [15-21]. It is generally believed that multistrange hadrons, such as Ξ and Ω , directly carry the information of the QGP phase because of their small hadronic cross sections and the associated early decouplings from the system near T_c [6]. Compared with common hadrons, their anisotropy flows are mainly developed in the QGP stage and less contaminated by the hadronic evolution.

Since the running of 2.76A TeV Pb + Pb collisions at the LHC, the flow and other soft hadron data of all charged and identified hadrons have been studied by many groups within the framework of hydrodynamics [22–31]. Using the VISHNU hybrid model [32] that connects (2+1)-dimensional viscous hydrodynamics with a hadronic afterburner, we extracted the specific QGP shear viscosity (η/s)_{QGP} from the elliptic data of all charged hadrons with Monte Carlo Kharzeev-Levin-Nardi (MC-KLN) initial conditions [24]. With the extracted value of (η/s)_{QGP}, VISHNU provides a good description of the soft hadron data for π , K, and p at the LHC [25]. Recently, the multiplicity, p_{T} -spectra and elliptic flow for Λ , Ξ , and Ω have been measured by the ALICE Collaboration [19–21]. It is thus the right time to systematically study these strange and multistrange hadrons at the LHC via the VISHNU hybrid model.

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This paper is organized as follows. In Sec. II, we briefly introduce the VISHNU hybrid model and its setup for the calculations. Section III compares our VISHNU results with the ALICE measurements in 2.76A TeV Pb + Pb collisions, including the centrality dependence of the multiplicity density, p_T spectra, and differential elliptic flow for Λ , Ξ , and Ω . Section IV studies and discusses mass ordering of elliptic flow among π , K, p, Λ , Ξ , and Ω at the LHC. Section V explores chemical and thermal freeze-out of various hadron species during the UrQMD evolution of VISHNU. Section VI summarizes our current work and presents a brief outlook for the future.

II. SETUP OF THE CALCULATION

In this section, we describe the inputs and setup for the VISHNU calculations for the soft hadron data in 2.76*A* TeV Pb+Pb collisions. The VISHNU hybrid model [32] combines (2+1)-dimensional relativistic viscous hydrodynamics (VISH2+1) [33] for the QGP fluid expansion with a microscopic hadronic transport model (UrQMD) [34] for the hadron resonance gas evolution. The transition from hydrodynamics to the hadron cascade occurs on a switching hypersurface with a constant temperature. Generally, the switching temperature T_{sw} is set to 165 MeV which is close to the QCD phase transition temperature [35–37]. For the hydrodynamic evolution above T_{sw} , we input an equation of state (EoS) constructed from recent lattice QCD data [38,39].

Following Refs. [24–26], we input MC-KLN initial conditions [40,41] and start the hydrodynamic simulations at $\tau_0 = 0.9$ fm/c. For computational efficiency, we implement single-shot simulations [24–26,32,42] using smooth initial entropy density profiles generated by the MC-KLN model through averaging over a large number of events within specific centrality bins.¹ Considering the conversion from total initial entropy to the final multiplicity of all charged hadrons, we

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¹For recent development on event-by-event VISHNU simulations, please refer to [43,44].

cut the centrality bins through the distribution of total initial entropies obtained from the event-by-event fluctuating profiles from the MC-KLN model. Such centrality classification was once used by Shen in Ref. [44], which is closer to the experimental cut from the measured multiplicity distribution. The normalization factor for the initial entropy density is fixed by the charged hadron multiplicity density in the most central collisions $(dN_{ch}/d\eta \approx 1601 \pm 60$ from ALICE [45]). The λ parameter in the MC-KLN model, which quantifies the gluon saturation scale in the initial gluon distributions [40], is tuned to 0.138 for a better fit of the centrality-dependent multiplicity density for all charged hadrons.

The QGP specific shear viscosity $(\eta/s)_{\text{QGP}}$ is set to 0.16 for MC-KLN initial conditions. Such a combined setting for VISHNU once nicely described the elliptic flow of pions, kaons and protons in 2.76*A* TeV Pb + Pb collisions [25]. Here, we continue to use it to further study the soft hadron data of strange and multistrange hadrons at the LHC. To simplify the theoretical investigations, we set the bulk viscosity to zero and neglect the net baryon density and heat conductivity for the QGP systems created at the LHC.

III. MULTIPLICITY, SPECTRA, AND ELLIPTIC FLOW FOR A, $\Xi,$ AND Ω

The multiplicity, spectra, and elliptic flow of pions, kaons and protons in 2.76A TeV Pb + Pb collisions have been studied in our early paper [25]. We showed that, with MC-KLN initial conditions, $\eta/s = 0.16$, and other parameters fixed from the related data of all charged hadrons, VISHNU could nicely describe the soft hadron data of pions, kaons, and protons at the LHC. We also found that baryon-antibaryon $(B-\bar{B})$ annihilations in the UrQMD module of VISHNU could reduce the proton yields by O(30%), leading to nice fits of the proton data measured by ALICE. In this section, we extend our early VISHNU simulations to high-statistics runs to further study the soft hadron data for the strange and multistrange hadrons Λ , Ξ , and Ω in 2.76A TeV Pb + Pb collisions.²

Figure 1 shows the centrality dependence of the multiplicity density per participant pair $(dN/dy)/(N_{part}/2)$ for Λ , Ξ , and Ω in 2.76A TeV Pb + Pb collisions.³ In the inset, we plot the corresponding curves for pions, kaons, protons and for all

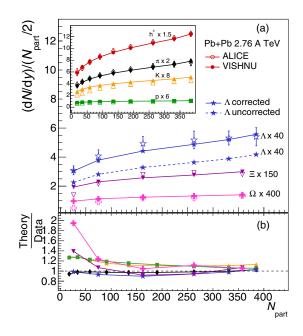


FIG. 1. (Color online) Centrality dependence of the multiplicity density per participant pair, $(dN/dy)/(N_{part}/2)$, for Λ , Ξ , and Ω in 2.76*A* TeV Pb + Pb collisions. Inset: $(dN/dy)/(N_{part}/2)$ for π , *K*, *p* and for all charged hadrons. Experimental data are from the ALICE Collaboration [19,20,45,46]. Theoretical curves are calculated with the VISHNU hybrid model, using MC-KLN initial conditions, $\eta/s = 0.16$, and $T_{sw} = 165$ MeV.

charged hadrons that were once presented in our early paper [25] for easy reference. The inputs of our current calculations are close to the ones used in [25,26], except for two points: (1) changing the λ parameter in the MC-KLN model from 0.28 to 0.138 and (2) cutting the centrality bins through initial entropy rather than the participant number N_{part} (please refer to Sec. II for details). Compared with the early setup, these two changes mainly improve the description of the centrality-dependent multiplicity for all charged hadrons and for pions, but they have small influence on other theoretical results, such as the elliptic flow of all charged and identified hadrons, etc.

One finds that VISHNU nicely describes these $(dN/dy)/(N_{\text{part}}/2)$ curves for all investigated hadrons. Like the case of protons, $B-\bar{B}$ annihilations also reduce the yields of strange and multi-strange baryons with O(30%) for Λ and O(20%) for Ξ and Ω in the most central Pb + Pb collisions (please refer to Fig. 5 in Sec. V). The lower panel of Fig. 1 shows the difference between the theoretical calculated and the experimental measured particle yields. From the most central to semiperipheral collisions, the deviations are all within 20%. For the 60–80% centrality bin, the differences increase to 40% for Ξ , and 100% for Ω . This indicates that

²The ϕ meson is another important multistrange hadron that might directly carry the QGP information due to its small hadronic cross sections. VISHNU predictions for the spectra and elliptic flow of ϕ can be found in Ref. [25]. However, later comparisons showed pretty large deviations between theory and experiment [21]. Unlike other hadrons, ϕ mesons are mainly reconstructed from the strong decay channel $\phi \rightarrow K^+K^-$, rather than being directly measured. The succeeding hadronic scatterings of kaons might contaminate the weak signals of ϕ . In this paper, we will not show and discuss the results of ϕ , but just quickly mention our early work [25] and leave the puzzle of ϕ for future study.

³We notice that the measured multiplicities of Λ from ALICE are contaminated by the feed-down decays of Σ^0 and $\Sigma(1385)$ [19]. However, the UrQMD module of VISHNU only includes strong resonance decays, without any weak decays. To partially account the effects from weak decays, e.g., $\Sigma^0 \rightarrow \Lambda + \gamma$, we directly sum the

multiplicities of Λ and Σ^0 from VISHNU to get a corrected curve of Λ (the solid blue line with star symbols). The original yields of Λ from VISHNU are also shown in Fig. 1, presented by the dashed blue line with star symbols. In our estimations, the $\Sigma^0 \rightarrow \Lambda + \gamma$ channel contributes ~30% additional Λ productions.

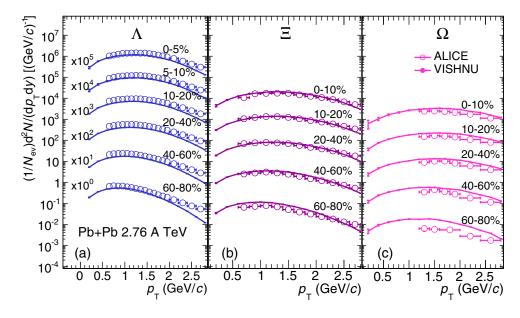


FIG. 2. (Color online) Transverse momentum spectra of Λ , Ξ , and Ω at various centralities in 2.76*A* TeV Pb + Pb collisions. Experimental data are taken from ALICE [19,20]. Theoretical curves are calculated with VISHNU with the same inputs as for Fig. 1. From top to bottom the curves correspond to 0–10% (×10⁴), 10–20% (×10³), 20–40% (×10²), 40–60% (×10¹), and 60-80% (×1) centrality, respectively, where the factors in parentheses are the multipliers applied to the spectra for clear separation. Spectra of Λ start from 0–5% (×10⁵) and 5–10% (×10⁴), instead of 0–10%.

the strangeness no longer reach chemical equilibrium in the small system created in peripheral Pb + Pb collisions.

In Fig. 2, we compare the transverse momentum spectra of Λ , Ξ , and Ω from VISHNU with the measurements from ALICE. In general, VISHNU describes the p_T spectra of these strange and multistrange hadrons from the most central to semiperipheral collisions, except for the 60–80% centrality bin. Here, the theoretical curves of Λ are plotted with the original values from VISHNU without weak decays. As a result, they are about 30% lower than the experimental measurements with weak decay contaminations. The Ω spectra from VISHNU are slightly higher than the experimental data for most centralities, but obviously above the data at the 60–80% centrality bin. Such deviations between theory and experiment are consistent with the model and data differences for the centrality-dependent multiplicity shown in Fig. 1. In spite of the normalization issues, VISHNU nicely fits the slope of the p_T spectra for Λ , Ξ , and Ω at various centralities. Together with the early nice descriptions of the p_T spectra for pions, kaons, and protons [25], it indicates that VISHNU generates a proper amount of radial flow, during its QGP and hadronic evolution, to push the spectra of various hadrons.

Figure 3 presents the differential elliptic flow of Λ , Ξ , and Ω at three chosen centralities in 2.76*A* TeV Pb + Pb collisions. The experimental data are from ALICE, which are measured with the scalar product method [21]. The theoretical lines are calculated from VISHNU with MC-KLN initial conditions and $(\eta/s)_{QGP} = 0.16$. Such inputs once nicely described the elliptic flow data of pions, kaons, and protons at the LHC [25]. In principle, the current calculations can be considered

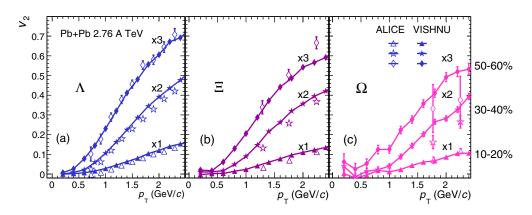


FIG. 3. (Color online) Differential elliptic flow of strange hadrons Λ and multistrange hadrons Ξ and Ω at 10–20%, 30–40% and 50–60% centralities in 2.76A TeV Pb + Pb collisions. Experimental data are from ALICE [21], theoretical curves are calculated from VISHNU with the same inputs as for Figs. 1 and 2.

as extensions of the early simulations [25]. Figure 3 shows that the elliptic flow data below 2 GeV for Λ , Ξ , and Ω are fairly well described by VISHNU within the statistical error bars. Above 2 GeV, the descriptions of the elliptic flow for Ξ at 50–60% and for Ω at 30–40% and 50–60% become worse. On the other hand, viscous corrections probably become too large in that higher p_T region, making the hydrodynamic description in VISHNU lose its predictive power.

IV. MASS ORDERING OF ELLIPTIC FLOW

Mass ordering of elliptic flow among various hadron species reflects the interaction between the radial and elliptic flows during the hadronic evolution. The radial flow tends to push the heavier particles at lower p_T to higher p_T , leading to a mass ordering of the p_T -dependent elliptic flow below 1.5–2 GeV that decreases with the increase of hadron mass. Such v_2 mass ordering has been discovered in experiments at both the RHIC and the LHC [21,47–49], and has also been studied within the framework of hydrodynamics [11,26,50–52] and the blast wave model [53,54].

In Fig. 4, we investigate mass ordering of elliptic flow among π , K, p, Λ , Ξ , and Ω in 2.76A TeV Pb + Pb collisions. For clear presentations, the ALICE data and the VISHNU results are plotted in separate panels for the two chosen centralities at 10–20% and 40–50%. Calculations in [25] and in this paper (Fig. 3) have shown that VISHNU generally describes $v_2(p_T)$ for various individual hadrons over a wide range of centralities. However, further comparisons in Fig. 4 illustrate that VISHNU could not describe the v_2 mass ordering among all hadron species. Although VISHNU nicely describes the

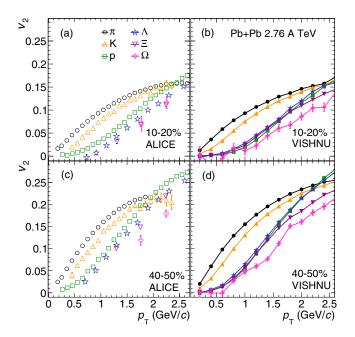


FIG. 4. (Color online) Differential elliptic flow of π , K, p, Λ , Ξ , and Ω at 10–20% and 40–50% centralities in 2.76A TeV Pb + Pb collisions. Left panels (a) and (c) are plotted with v_2 from ALICE [21], right panels (b) and (d) are plotted with v_2 from VISHNU.

mass ordering among π , K, p, and Ω , it fails to correctly describe the mass ordering among p, Λ , and Ξ . In contrast, pure viscous hydrodynamics VISH2+1 has correctly predicted the relative mass-ordering among these investigated hadrons, but it has difficulties in roughly fitting the v_2 data for these heavier hadrons such as p, Λ , and Ξ at the 10–20% centrality bin [51].

Compared with the elliptic flow of individual hadrons, the v_2 mass-splittings between different hadron species reveal more details about the hadronic evolution. Although VISHNU could improve the description of $v_2(p_T)$ for hadron species such as p, Λ , and Ξ through its microscopic hadronic scatterings, it slightly under-predicts the proton v_2 below 2 GeV, leading to inverse v_2 mass ordering between p and Λ , and accidental overlaps of the elliptic flow for p and Ξ below 1.5 GeV. An initial flow could enhance the radial flow in the hadronic stage, which is thus expected to improve the description of v_2 mass ordering within the framework of the hybrid model. Meanwhile, the UrQMD hadronic cross sections also need to be reevaluated and improved. These have not been done currently and should be investigated in the near future.

V. CHEMICAL AND THERMAL FREEZE-OUT OF VARIOUS HADRON SPECIES

In this section, we investigate chemical and thermal freezeout of various hadron species during the UrQMD evolution within the framework of the VISHNU hybrid model.

During the QGP fireball evolution, a large number of hadrons are produced near T_c , which subsequently undergo inelastic and elastic collisions in the hadronic phase. With the termination of inelastic collisions, the yields of each hadron species no longer change. The system is considered to reach chemical freeze-out. Thermal freeze-out happens later, which is associated with the end of elastic collisions. After that, the momentum distributions of final produced hadrons are fixed.

In the statistical model, the chemical freeze-out temperature T_{ch} and the baryon chemical potential μ_b are extracted from the particle yields of various hadrons [55–58]. A systematic study of the related data at top RHIC energy gives $T_{ch} \simeq 165$ MeV [55]. This temperature could describe the yields of many identified hadrons in 2.76A TeV Pb + Pb collisions, but obviously overpredicts the protons/antiprotons data at the LHC. A good description of the p/\bar{p} data requires a lower chemical freeze-out temperature around 150 MeV. However, such a lower temperature breaks the early nice description of Ξ and Ω yields once achieved with 165 MeV [59,60].

To study the above proton puzzle from the statistical model, we systematically investigated the soft hadron data for π , K, and p at both the RHIC and the LHC with the VISHNU hybrid model [25]. We found that baryon and antibaryon annihilations influence the transport of protons/antiprotons during the hadronic evolution, leading to a largely improved description of the p/\bar{p} yields when compared with the case without $B-\bar{B}$ annihilations.⁴ Meanwhile, other soft hadron

⁴Other related work could be found in Refs. [60–62].

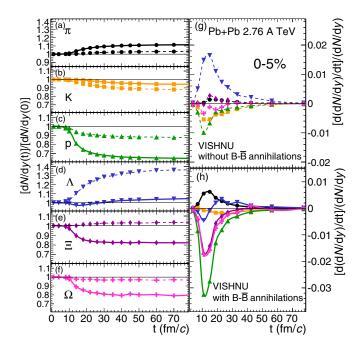


FIG. 5. (Color online) Left panels (a)–(f): time evolution of relative particle yield density $\frac{dN}{dy}(t)/\frac{dN}{dy}(0)$ for π , K, p, Λ , Ξ , and Ω during the UrQMD expansion of VISHNU. Right panels (g) and (h): time evolution of the changing rate for the corresponding particle yield density. Solid/dashed lines denote the VISHNU simulations with/without $B-\bar{B}$ annihilations in the most central 2.76A TeV Pb + Pb collisions.

data of π , *K*, and *p* are also nicely fitted in general. This paper extends the early VISHNU calculations to further study strange and multistrange hadrons at the LHC. Section III showed a nice description of the paricle yields for Λ , Ξ , and Ω , together with good fits of the spectra and elliptic flow for these hadrons.

In our calculations, the switching temperature, which connects the hydrodynamic description of the QGP expansion to the Boltzmann approach for the hadron resonance gas evolution, is set to 165 MeV at both the RHIC and the LHC. However, this temperature cannot be identified as the chemical freeze-out temperature in the statistical model, since $B-\bar{B}$ annihilations and other inelastic collisions are still frequent during the early hadronic evolution, which constantly changes the yields of various hadrons. Instead, different hadronic scatterings in UrQMD lead to a hadron-species-dependent chemical freeze-out procedure.

Figure 5 studies the time evolution of particle yield density for π , K, p, Λ , Ξ , and Ω during the UrQMD hadronic expansion. This investigation is still done within the VISHNU simulations for 2.76*A* TeV Pb + Pb collisions, but exports the UrQMD intermediate results at different evolution times. For easy comparison, the left panels (a)–(f) plot the time evolution of relative particle yield density: $\frac{dN}{dy}(t)/\frac{dN}{dy}(0)$. Here, $\frac{dN}{dy}(t)$ and $\frac{dN}{dy}(0)$ denote the particle yield density at midrapidity at later evolution time and at the starting time, respectively.

For the simulations without $B-\overline{B}$ annihilations, the yields of Ξ and Ω almost do not change. This indicates that these two multistrange baryons experience early chemical freeze-

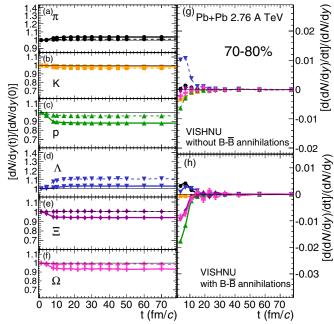


FIG. 6. (Color online) Similar to Fig. 5, but for 70–80% centrality bin.

out near the switching hypersurface of VISHNU. For other hadron species, their yields constantly change with the UrQMD evolution. By the end of the evolution, the yields of *K* and *p* respectively decrease ~5% and ~10%, and the yield of Λ increases ~40%. Meanwhile, the changing rates for the particle yield density of *K*, *p*, and Λ show wide peaks along the time axis [panel (g)], illustrating that the associated inelastic collisions are still frequent after 10–20 fm/*c*. This indicates these hadrons experience later chemical freeze-out. The yield of pions only slightly increases during the UrQMD evolution without $B-\bar{B}$ annihilations. However, this is not necessarily associated with early chemical freeze-out of pions. Instead, pions maintain relative chemical equilibrium below T_c through frequent quasielastic collisions, e.g., $\pi\pi \leftrightarrow \rho$, $\pi N \leftrightarrow \Delta$, etc. [63–66].

The $B-\bar{B}$ annihilations ($p\bar{p} \rightarrow n\pi$, etc.) mainly influence the baryon's transport in UrQMD, leading to $\sim 30\%$ reductions for the p and A yields, and $\sim 20\%$ reductions for the Ξ and Ω yields in the most central Pb + Pb collisions. Meanwhile, the yields of π and K slightly increase by ~5% through the annihilation channels. Although these two multistrange hadrons, Ξ and Ω , rarely interact with other hadrons during the UrQMD evolution, the annihilations with their own antiparticles delay their chemical freeze-out. This is presented by the wide peaks on the changing rate curves for these two multistrange baryons in panel (h). But, compared with other curves such as the proton one, Ξ and Ω still experience early chemical freeze-out. The $B-\bar{B}$ annihilations almost balance with the other inelastic collision channels on the production of Λ and K. As a result, the yields of these two hadrons only slightly change during the hadronic evolution.

Figure 5 is similar to Fig. 5, but for the 70-80% centrality bin. For the case without $B-\bar{B}$ annihilations, the particle

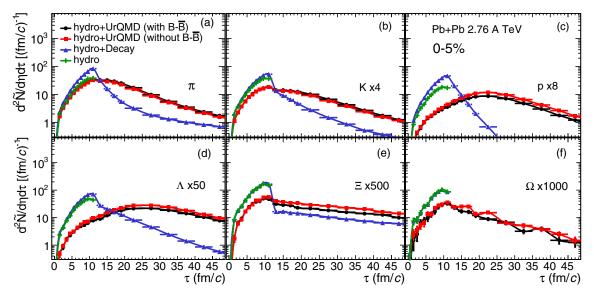


FIG. 7. (Color online) Thermal freeze-out time distributions for π , K, p, Λ , Ξ , and Ω in the most central Pb + Pb collisions, calculated from hydrodynamics (green), hydrodynamics + resonance decay (blue), and VISNU without $B-\bar{B}$ annihilations (red) and with $B-\bar{B}$ annihilations (black).

yields of various hadrons almost do not change during the UrQMD evolution. Compared with the most central Pb + Pb collisions, the number of inelastic collisions in the hadronic phase is greatly reduced. Figure 5 also showed that the $B-\bar{B}$ annihilations decrease the baryon yields for p, Λ , Ξ , and Ω by 5–8% in peripheral collisions, but most of the annihilations happen before 10 fm/c.

In short, Figs. 5 and 6 mainly show the time evolution of various hadron yields, which indirectly reflect the inelastic collisions in UrQMD. A further analysis of the space-time distributions of the last inelastic collisions will reveal direct information on chemical freeze-out, which may even help us to extract effective chemical freeze-out temperatures of various hadron species. Unfortunately, the current version of UrQMD does not record such intermediate information. We have to leave it for future study.

Besides four-momentum of final produced hadrons, UrQMD also outputs the positions (in space and time) of the last elastic collisions or resonance decays that directly reflect thermal freeze-out of the evolving system. Here we define the time distributions of the last collisions or decays for various hadrons species as the corresponding *thermal freeze-out time distributions*. On the other hand, they can also be considered as the production-time distributions of specific hadron species during the UrQMD evolution.

Figure 7 shows thermal freeze-out time distributions for π , K, p, Λ , Ξ , and Ω in the most central Pb + Pb collisions. To study the hadronic scattering effects, we set four comparison simulations: (1) viscous hydrodynamics terminated at $T_{sw} = 165$ MeV with only thermal hadron emissions, (2) viscous hydrodynamics terminated at T_{sw} with thermal hadron productions and succeeding resonance decays, (3) VISHNU without $B-\bar{B}$ annihilations, and (4) VISHNU with $B-\bar{B}$ annihilations. Here, both viscous hydrodynamics and

VISHNU simulations input the same initial conditions, EoS, and other related parameters as described in Sec. II.

The thermal freeze-out time distributions for various hadrons in case (1) all stop around 10 fm/c, because the hydrodynamic evolution terminates around that time in the most central collisions. Comparing the thermal freeze-out time distributions from hydrodynamics [case (1)] and from hydrodynamics+resonance decays [case (2)], we find that a certain portion of the resonance decays happen near the hydrodynamic freeze-out surface, which largely enhances the productions of pions and protons before 10 fm/c. Meanwhile, the long-lived resonances also contribute later hadron productions after 10 fm/c, which results in long tails for the distribution curves of π , K, p, A, and Ξ . We notice that there is no change for the Ω curves between case (1) and case (2). UrQMD only includes hadrons below 2 GeV; the associated resonance decays do not contribute to the production of this heavy multistrange baryon.

The UrQMD hadronic scatterings in cases (3) and (4) broaden thermal freeze-out time distributions of all hadron species, which shifts the averaged hadron production times before 10 fm/c in cases (1) and (2) to later values ranging from 10 to 40 fm/c. We also observe that the $B-\bar{B}$ annihilations further decrease the productions of p, Λ , Ξ , and Ω as shown in Fig. 5. In general, such annihilations do not change the shape of these thermal freeze-out time curves.

Figure 8 compares the thermal freeze-out time distributions from the most central collisions with the ones from peripheral collisions. Here, the results are from the VISHNU simulations with $B-\bar{B}$ annihilations. We find that the peaks of the thermal freeze-out time distributions for π , K, p, Λ , Ξ , and Ω are all shifted to much earlier time in peripheral collisions, because the created QGP fireball there has much smaller volume and shorter lifetime.

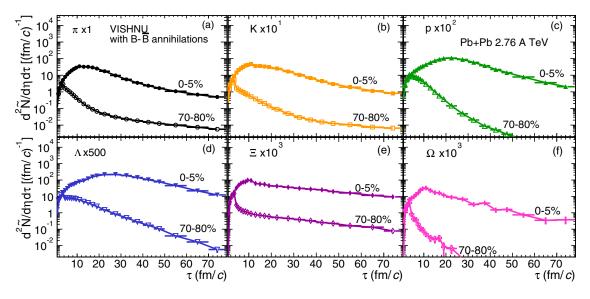


FIG. 8. (Color online) Comparisons of the thermal freeze-out time distributions for π , K, p, Λ , Ξ , and Ω between the most central and peripheral Pb + Pb collisions, calculated from VISHNU with $B-\overline{B}$ annihilations.

Figure 9 compares the thermal freeze-out time distributions for π , K, p, Λ , Ξ , and Ω in the most central Pb + Pb collisions. These curves are calculated from VISHNU with $B-\overline{B}$ annihilations, which are the same as the corresponding ones shown in different panels of Fig. 7. The peaks of the Ξ and Ω curves are both located around 10 fm/c. Compared with the curves of p and Λ , whose peaks are located around 20–30 fm/c, these two multistrange hadrons experience earlier thermal freeze-out. Although the peaks of the π and K curves are closer to the ones of Ξ and Ω , their freeze-out time distributions spread widely along the time axis. This indicates

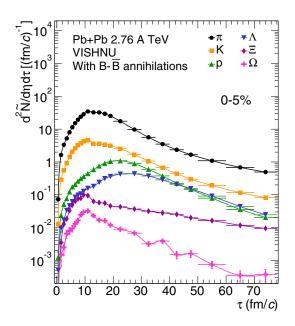


FIG. 9. (Color online) Thermal freeze-out time distributions for π , K, p, Λ , Ξ , and Ω in the most central Pb + Pb collisions, calculated from VISHNU with $B-\bar{B}$ annihilations.

that these two meson species still suffer a certain amount of hadronic scattering even during the late evolution of UrQMD. We conclude from Fig. 9 that thermal freeze-out is hadron species dependent. Compared with other hadrons, the two multistrange hadrons Ξ and Ω experience earlier thermal freeze-out, as expected, due to their much smaller hadronic cross sections.

VI. SUMMARY AND OUTLOOK

In this paper, we studied the soft hadron data of strange and multistrange hadrons at the LHC, using the VISHNU hybrid model. We found that, with MC-KLN initial conditions, $\eta/s = 0.16$, and other inputs that fit the related data of common hadrons [25], VISHNU generally describes the multiplicity, $p_{\rm T}$ spectra, and differential elliptic flow of the strange hadron Λ and the multistrange hadrons Ξ and Ω in 2.76*A* TeV Pb + Pb collisions.

Compared with the pure hydrodynamic calculations from VISH2+1 [11], VISHNU improves the descriptions of the elliptic flow for p, Λ , Ξ , and Ω with microscopic hadronic scatterings that rebalance the interactions between radial and elliptic flow. However, mass ordering of elliptic flow among various hadron species is not fully described. VISHNU slightly underpredicts the differential elliptic flow of protons, leading to inverse mass-ordering among p, Λ , and Ξ . An initial flow and improved hadronic cross sections in UrQMD may help to solve this issue. This should be investigated in the near future.

With a nice description of the particle yields for π , K, p, Λ , Ξ , and Ω , we further investigated chemical and thermal freeze-out of various hadron species within the framework of the VISHNU hybrid model. We found that, compared with other hadrons, the two multi-strange hadrons Ξ and Ω experience earlier chemical and thermal freeze-out due to their small hadronic cross sections. A study for time evolution of the hadron yields also shows that baryon-antibaryon annihilations

in UrQMD delay the chemical freeze-out of Ξ and Ω , when compared with the case without such annihilations.

We also emphasized that the switching temperature in VISHNU could not be identified as the chemical freeze-out temperature in the statistical model since inelastic collisions are still frequent during the early evolution of UrQMD. A further analysis of the space-time distributions of the last inelastic collisions could reveal more information on chemical freeze-out, which may even help us to extract effective chemical freeze-out temperatures of various hadron species. Unfortunately, such investigation could not be done with the current version of UrQMD. With an updating of UrQMD to further

record the intermediate evolution information, the chemical freeze-out procedure of the evolving hadronic system will be further studied in the future.

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- I. Arsene *et al.* (BRAHMS Collaboration), Nucl. Phys. A **757**, 1 (2005); B. B. Back *et al.* (PHOBOS Collaboration), *ibid.* **757**, 28 (2005); J. Adams *et al.* (STAR Collaboration), *ibid.* **757**, 102 (2005); K. Adcox *et al.* (PHENIX Collaboration), *ibid.* **757**, 184 (2005).
- [2] M. Gyulassy, in *Structure and dynamics of elementary matter*, edited by W. Greiner *et al.*, NATO Science Series II: Mathematics, Physics and Chemistry, Vol. 166 (Kluwer Academic, Dordrecht, 2004), pp. 159–182; M. Gyulassy and L. McLerran, Nucl. Phys. A **750**, 30 (2005); E. V. Shuryak, *ibid.* **750**, 64 (2005).
- [3] B. Müller and J. L. Nagle, Annu. Rev. Nucl. Part. Sci. 56, 93 (2006).
- [4] B. Müller, J. Schukraft, and B. Wyslouch, Annu. Rev. Nucl. Part. Sci. 62, 361 (2012).
- [5] J. Rafelski and B. Müller, Phys. Rev. Lett. 48, 1066 (1982); 56, 2334(E) (1986).
- [6] H. van Hecke, H. Sorge, and N. Xu, Phys. Rev. Lett. 81, 5764 (1998).
- [7] S. Hamieh, K. Redlich, and A. Tounsi, Phys. Lett. B 486, 61 (2000); K. Redlich, Nucl. Phys. A 698, 94 (2002).
- [8] J. Letessier and J. Rafelski, Int. J. Mod. Phys. E 9, 107 (2000); G. Torrieri and J. Rafelski, New J. Phys. 3, 12 (2001); J. Rafelski, J. Letessier, and G. Torrieri, Phys. Rev. C 64, 054907 (2001); 65, 069902(E) (2002).
- [9] U. W. Heinz, J. Phys. G 25, 263 (1999).
- [10] W. Broniowski and W. Florkowski, Phys. Rev. C 65, 064905 (2002).
- [11] P. Huovinen, P. F. Kolb, U. W. Heinz, P. V. Ruuskanen, and S. A. Voloshin, Phys. Lett. B 503, 58 (2001).
- [12] C. Nonaka and S. A. Bass, Phys. Rev. C 75, 014902 (2007).
- [13] M. He, R. J. Fries, and R. Rapp, Phys. Rev. C 85, 044911 (2012).
- [14] C. Blume and C. Markert, Prog. Part. Nucl. Phys. 66, 834 (2011).
- [15] J. Adams *et al.* (STAR Collaboration), Phys. Rev. Lett. 92, 182301 (2004).
- [16] J. Adams *et al.* (STAR Collaboration), Phys. Rev. Lett. 98, 062301 (2007).
- [17] B. I. Abelev *et al.* (STAR Collaboration), Phys. Rev. C 77, 044908 (2008); M. M. Aggarwal *et al.* (STAR Collaboration), *ibid.* 83, 024901 (2011); G. Agakishiev *et al.* (STAR Collaboration), Phys. Rev. Lett. 108, 072301 (2012).
- [18] J. Adams *et al.* (STAR Collaboration), Phys. Rev. Lett. 95, 122301 (2005); B. I. Abelev *et al.* (STAR Collaboration), Phys. Rev. C 77, 054901 (2008).

- [19] B. B. Abelev *et al.* (ALICE Collaboration), Phys. Rev. Lett. **111**, 222301 (2013).
- [20] B. B. Abelev *et al.* (ALICE Collaboration), Phys. Lett. B 728, 216 (2014); 734, 409(E) (2014).
- [21] B. B. Abelev et al. (ALICE Collaboration), arXiv:1405.4632.
- [22] B. Schenke, S. Jeon, and C. Gale, Phys. Lett. B 702, 59 (2011);
 Phys. Rev. C 85, 024901 (2012); C. Gale, S. Jeon, B. Schenke,
 P. Tribedy, and R. Venugopalan, Phys. Rev. Lett. 110, 012302 (2013).
- [23] Z. Qiu, C. Shen, and U. Heinz, Phys. Lett. B 707, 151 (2012).
- [24] H. Song, S. A. Bass, and U. Heinz, Phys. Rev. C 83, 054912 (2011); 87, 019902 (2013).
- [25] H. Song, S. A. Bass, and U. Heinz, Phys. Rev. C 89, 034919 (2014).
- [26] H. Song, F. Meng, X. Xin, and Y. X. Liu, J. Phys. Conf. Ser. 509, 012089 (2014).
- [27] H. Song, Nucl. Phys. A **904-905**, 114c (2013); arXiv:1401.0079.
- [28] H. Petersen, Phys. Rev. C 84, 034912 (2011).
- [29] L. Pang, Q. Wang, and X. N. Wang, Phys. Rev. C 86, 024911 (2012).
- [30] P. Bozek and I. Wyskiel-Piekarska, Phys. Rev. C 85, 064915 (2012).
- [31] J. Noronha-Hostler, G. S. Denicol, J. Noronha, R. P. G. Andrade, and F. Grassi, Phys. Rev. C 88, 044916 (2013).
- [32] H. Song, S. A. Bass, and U. Heinz, Phys. Rev. C 83, 024912 (2011); H. Song, Eur. Phys. J. A 48, 163 (2012).
- [33] H. Song and U. Heinz, Phys. Lett. B 658, 279 (2008); Phys.
 Rev. C 77, 064901 (2008); 78, 024902 (2008); H. Song,
 Ph.D. Thesis, The Ohio State University, 2009 (unpublished),
 arXiv:0908.3656.
- [34] S. A. Bass *et al.*, Prog. Part. Nucl. Phys. **41**, 255 (1998); M. Bleicher *et al.*, J. Phys. G **25**, 1859 (1999).
- [35] Y. Aoki, Z. Fodor, S. D. Katz, and K. K. Szabo, Phys. Lett. B 643, 46 (2006); Y. Aoki, S. Borsányi, S. Dürr, Z. Fodor, S. D. Katz, S. Krieg, and K. Szabo, J. High Energy Phys. 06 (2009) 088.
- [36] S. Borsányi, Z. Fodor, C. Hoelbling, S. D. Katz, S. Krieg, C. Ratti, and K. K. Szabó (Wuppertal-Budapest Collaboration), J. High Energy Phys. 09 (2010) 073; Nucl. Phys. A **904-905**, 270c (2013).
- [37] A. Bazavov et al., Phys. Rev. D 85, 054503 (2012).
- [38] P. Huovinen and P. Petreczky, Nucl. Phys. A 837, 26 (2010).
- [39] C. Shen, U. Heinz, P. Huovinen, and H. Song, Phys. Rev. C 82, 054904 (2010).

- [40] H.-J. Drescher and Y. Nara, Phys. Rev. C 75, 034905 (2007); 76, 041903(R) (2007).
- [41] T. Hirano and Y. Nara, Phys. Rev. C 79, 064904 (2009); T. Hirano, P. Huovinen, and Y. Nara, *ibid.* 83, 021902 (2011).
- [42] H. Song, S. A. Bass, U. Heinz, T. Hirano and C. Shen, Phys. Rev. Lett. **106**, 192301 (2011); **109**, 139904(E) (2012); Phys. Rev. C **83**, 054910 (2011); **86**, 059903 (2012).
- [43] C. Shen, Z. Qiu, H. Song, J. Bernhard, S. Bass, and U. Heinz, arXiv:1409.8164.
- [44] C. Shen, Ph.D. thesis, The Ohio State University, 2014 (unpublished); Z. Qiu, Ph.D. thesis, The Ohio State University, 2013 (unpublished).
- [45] K. Aamodt *et al.* (ALICE Collaboration), Phys. Rev. Lett. **106**, 032301 (2011).
- [46] B. Abelev *et al.* (ALICE Collaboration), Phys. Rev. C 88, 044910 (2013).
- [47] J. Adams *et al.* (STAR Collaboration), Phys. Rev. C 72, 014904 (2005).
- [48] B. I. Abelev *et al.* (STAR Collaboration), Phys. Rev. C 81, 044902 (2010).
- [49] R. Snellings, arXiv:1411.7690.
- [50] T. Hirano, U. W. Heinz, D. Kharzeev, R. Lacey, and Y. Nara, Phys. Rev. C 77, 044909 (2008).
- [51] C. Shen, U. Heinz, P. Huovinen, and H. Song, Phys. Rev. C 84, 044903 (2011).
- [52] P. Bozek, Phys. Rev. C 81, 034909 (2010).

- [53] C. Adler *et al.* (STAR Collaboration), Phys. Rev. Lett. 87, 182301 (2001).
- [54] F. Retiere and M. A. Lisa, Phys. Rev. C 70, 044907 (2004).
- [55] P. Braun-Munzinger, D. Magestro, K. Redlich, and J. Stachel, Phys. Lett. B **518**, 41 (2001); A. Andronic, P. Braun-Munzinger, and J. Stachel, Nucl. Phys. A **772**, 167 (2006).
- [56] P. Braun-Munzinger, K. Redlich, and J. Stachel, in *Quark-Gluon Plasma 3*, edited by R. C. Hwa and X.-N. Wang (World Scientific, Singapore, 2004), pp. 491–599.
- [57] J. Letessier and J. Rafelski, Eur. Phys. J. A 35, 221 (2008); M. Petráň, J. Letessier, V. Petráček, and J. Rafelski, Phys. Rev. C 88, 034907 (2013).
- [58] F. Becattini, J. Manninen, and M. Gazdzicki, Phys. Rev. C 73, 044905 (2006).
- [59] J. Stachel, A. Andronic, P. Braun-Munzinger, and K. Redlich, J. Phys. Conf. Ser. **509**, 012019 (2014).
- [60] F. Becattini, M. Bleicher, T. Kollegger, T. Schuster, J. Steinheimer, and R. Stock, Phys. Rev. Lett. 111, 082302 (2013).
- [61] F. Becattini, M. Bleicher, T. Kollegger, M. Mitrovski, T. Schuster, and R. Stock, Phys. Rev. C 85, 044921 (2012).
- [62] F. Becattini, M. Bleicher, E. Grossi, J. Steinheimer, and R. Stock, Phys. Rev. C 90, 054907 (2014).
- [63] T. Hirano and K. Tsuda, Phys. Rev. C 66, 054905 (2002).
- [64] D. Teaney, arXiv:nucl-th/0204023.
- [65] P. F. Kolb and R. Rapp, Phys. Rev. C 67, 044903 (2003).
- [66] P. Huovinen, Eur. Phys. J. A 37, 121 (2008).