Storage of ultracold neutrons in the magneto-gravitational trap of the UCN_{\tau} experiment

D. J. Salvat, ¹ E. R. Adamek, ¹ D. Barlow, ² J. D. Bowman, ³ L. J. Broussard, ² N. B. Callahan, ¹ S. M. Clayton, ² C. Cude-Woods, ¹ S. Currie, ² E. B. Dees, ⁴ W. Fox, ¹ P. Geltenbort, ⁵ K. P. Hickerson, ⁶ A. T. Holley, ¹ C.-Y. Liu, ¹ M. Makela, ² J. Medina, ² D. J. Morley, ² C. L. Morris, ² S. I. Penttilä, ³ J. Ramsey, ² A. Saunders, ² S. J. Seestrom, ² E. I. Sharapov, ⁷ S. K. L. Sjue, ² B. A. Slaughter, ¹ J. Vanderwerp, ¹ B. VornDick, ⁴ P. L. Walstrom, ² Z. Wang, ² T. L. Womack, ² and A. R. Young ⁴

¹ Indiana University, Bloomington, Indiana 47405, USA

² Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

³ Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

⁴ North Carolina State University, Raleigh, North Carolina 27695, USA

⁵ Institut Laue Langevin, 38042 Grenoble, France

⁶ University of California Los Angeles, Los Angeles, California 90095, USA

⁷ Joint Institute for Nuclear Research, 141980, Dubna, Russia (Received 28 October 2013; revised manuscript received 30 April 2014; published 23 May 2014)

The UCN τ experiment is designed to measure the lifetime τ_n of the free neutron by trapping ultracold neutrons (UCN) in a magneto-gravitational trap. An asymmetric bowl-shaped NdFeB magnet Halbach array confines low-field-seeking UCN within the apparatus, and a set of electromagnetic coils in a toroidal geometry provides a background "holding" field to eliminate depolarization-induced UCN loss caused by magnetic field nodes. We present a measurement of the storage time τ_{store} of the trap by storing UCN for various times and counting the survivors. The data are consistent with a single exponential decay, and we find $\tau_{\text{store}} = 860 \pm 19 \text{ s}$, within 1σ of current global averages for τ_n . The storage time with the holding field deactivated is found to be $\tau_{\text{store}} = 470 \pm 160 \text{ s}$; this decreased storage time is due to the loss of UCN, which undergo Majorana spin flips while being stored. We discuss plans to increase the statistical sensitivity of the measurement and investigate potential systematic effects.

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The decay of the free neutron $n \to p + e^- + \bar{\nu}_e$ is the simplest nuclear β decay. The mean lifetime τ_n of this decay is of importance in primordial nucleosynthesis, neutrino physics, and it is a potential probe of beyond-standard-model physics in the semileptonic weak sector at the TeV scale [1]. The ⁴He mass fraction in the early universe depends on the neutron-toproton ratio, which is determined in part by τ_n [2]. Further, the combination of the neutron lifetime with other neutron β -decay correlations overconstrains the parameters in the standard model and can test for new physics, such as the presence of tensor or scalar currents in the semileptonic charged-current Lagrangian [3–5]. However, new high-precision experiments must be developed to reduce experimental uncertainties to match the $\sim 10^{-4}$ theoretical uncertainty in the neutron decay radiative corrections and compete with limits on new interactions from collider experiments [6,7].

Most recent measurements of τ_n use ultracold neutrons (UCN), which can be bottled because their kinetic energy $E \sim 100\,\mathrm{neV}$ is comparable to the effective neutron optical potential V_F in many common materials. They can thus be confined within suitably designed experiments for times approaching the neutron lifetime. Their low velocity also allows them to be gravitationally trapped, and they are easily polarized using inhomogeneous magnetic fields [8,9]. Today, measurements of τ_n with the lowest quoted uncertainties are performed by bottling UCN in a material trap for various storage times and then emptying the trapped UCN into a counter to determine the storage time constant τ_store [10–13]. The inverse lifetime $\tau_n^{-1} = \tau_\mathrm{store}^{-1} - \tau_\mathrm{loss}^{-1}$ is then determined by varying the loss rate τ_loss of UCN from the bottle due to loss mechanisms such

as nuclear absorption and up-scattering, and extrapolating to $\tau_{\rm loss}^{-1} \to 0.$

The recent measurements and corrected values of τ_n using this technique have shifted the global average by $\sim 5\sigma$ since 2005 [14], and potential sources of these discrepancies have been widely discussed [15,16]. Among these is the failure of the often-used assumption that the UCN rapidly and uniformly occupy the phase space of the trap: This causes systematic effects due to the phase-space dependence for UCN detection efficiency, or the presence of nearly stable orbiting trajectories with $E > V_{\rm F}$ which slowly "spill" out of the trap (so-called quasibound UCN). In addition, the material bottle measurements are in disagreement with the most precise determination of τ_n using a cold neutron beam [17–19]; thus, new consistent results from both UCN and neutron beam experiments are needed to improve the precision of the current global data. This motivates new experimental techniques for the characterization of losses and phase-space-dependent effects and improved Monte Carlo studies.

As an alternative to material bottles, UCN in the low-field-seeking spin state can be confined by magnetic field gradients, which eliminates the need to characterize the loss of UCN on material surfaces during storage. Magnetic confinement was proposed more than 50 years ago by Vladimirskiĭ [20] and first realized by Abov *et al.* [21,22]. Since this time, only Paul *et al.* have produced a measurement of τ_n by radially confining slow neutrons using a magnetic storage ring [23]. More recently, an effort at the National Institute of Standards and Technology (NIST) has produced a preliminary storage time measurement using an Ioffe-Pritchard trap with

in situ UCN production and β -decay detection in superfluid He [24,25]. Storage in a cylindrical permanent magnet trap was subsequently achieved by Ezhov *et al.* [26]. Trapping UCN with magnetic field gradients is promising for next generation measurements of τ_n , and this has led to several ongoing experimental efforts [27–29], including the use of asymmetric magnetic traps to rapidly remove neutrons in quasibound orbits [30].

Here, we report progress toward a measurement of τ_n in the UCN τ experiment, which utilizes a magneto-gravitational permanent magnet array to confine UCN [31]. The apparatus will be used to examine the feasibility of achieving a 0.01% measurement of τ_n . To this end, the experiment is being developed to perform a 0.1% measurement of τ_{store} on a \sim day time scale. With this statistical sensitivity, the apparatus will be used to study effects such as neutron depolarization and the elimination of quasibound neutrons, and to investigate in situ UCN detection methods which can further increase statistical sensitivity and mitigate phase-space-dependent systematic effects. Reference [31] provides a detailed description of the basic trap geometry. Here we briefly review the design of the apparatus, present a preliminary measurement of the storage time of the trap, and discuss future improvements toward a more precise measurement.

The trap consists of 5310 NdFeB magnets arranged in an asymmetric bowl-shaped Halbach array with a volume of approximately 670 L. Walstrom et al. chose the present asymmetric trap shape based on their neutron-tracking studies of magneto-gravitational Halbach arrays in order to minimize the time needed to remove quasibound UCN [31]. These tracking studies were verified by the work in Ref. [32]. The asymmetry is achieved by constructing either half of the trap in the shape of an upright torus truncated at a fixed vertical height: one side with minor and major radii of 0.5 and 1 m respectively, and the other side with these values exchanged. The two sides of the bowl thus exhibit different upward slopes while being smoothly connected. The depth of the trap is 50 cm, so that UCN with energy E < 51 neV are confined from above by gravity, while those with E > 51 neV can be quasibound (see Ref. [31]). The open top of the trap provides easy access to test different detection methods and cleaning techniques.

An auxiliary "holding" field is produced by rectangular conducting coils outside of the vacuum jacket of the experiment. This field is everywhere perpendicular to the Halbach array field, which assures that field nodes (i.e., domains of $|\mathbf{B}|=0$) are not present within the trap volume, preventing neutron depolarization due to Majorana transitions. With an applied current of 300 A through each coil, the holding field strength is 64 G near the bottom of the trap and 127 G near the top (note that this is different from Ref. [31]). We show that deactivating the holding field greatly reduces τ_{store} due to the appearance of field nodes: The polarized UCN can undergo Majorana spin flips near these domains, thus ejecting them from the trap at a mean rate comparable to τ_n^{-1} [20,33].

Figure 1 shows the experimental layout used to determine τ_{store} , and a rendering of the apparatus is shown in Fig. 2. A solid-D₂-based UCN source provides a UCN density of 52 UCN/cm³ (measured at the gate valve) to several experiments in the laboratory, including the UCN τ experiment.

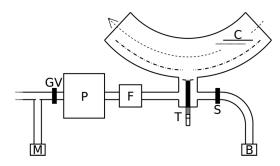


FIG. 1. A schematic of the experiment. The UCN source density is monitored through a 1-cm aperture leading to a ³He-based proportional counter (M), or detected further downstream in the ¹⁰B counter (B). The apparatus consists of a polarizing magnet (P), a spin flipper (F), and polyethylene cleaner in raised (solid) and lowered (dotted) positions (C). There is an upstream gate valve (GV) and downstream aluminum shutter (S), as well as a pneumatic piston-driven magnet plate (T) which opens the bottom of the Halbach array (dash-dot) so that UCN can be loaded. The holding field follows lines parallel to the dashed arrow.

The source performance and characteristics are described in Ref. [34]. The UCN source density at the gate valve is continuously monitored through a 1-cm-diameter aperture, which leads to a 3 He/CF₄-filled multiwire proportional chamber [35] (M in Fig. 1). Emerging from the source, the UCN pass through a 6-T polarizing magnet (P in Fig. 1), and the polarized (high-field-seeking) neutrons then pass through a low-field adiabatic fast-passage spin flipper (F) with $B_0 \approx 140$ G, $f \approx 0.4$ MHz, converting the UCN spin to the trappable low-field-seeking state (similar to that in Ref. [36]). UCN are then guided into the trap through a pneumatically actuated door, the top of which is a 15×15 cm² plate of permanent magnets. When shut, this completes the Halbach array at the bottom of the trap.

Quasibound UCN loaded into the trap could escape on a time scale similar to τ_n , which could systematically affect the exponential decay curve and introduce an additional time constant. There are ongoing experimental and theoretical studies of this effect [37–39], which has been observed in material and magnetic traps under certain experimental

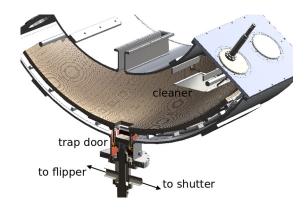


FIG. 2. (Color online) A cutaway of the apparatus. The tubular guides (7.6-cm diameter) lead to the other components shown in Fig. 1. The trap door is shown in the down position, and the cleaner is shown on the right side of the trap.

conditions [22,40]. In the current experiment, we remove the population of quasibound UCN during and after filling the trap by using a 35.5×66.0 cm² polyethylene sheet ("cleaner") suspended at the top of the trap (C in Fig. 1). The cleaner can be lowered 7 cm into the trap in order to upscatter the UCN to cold or thermal energies. These upscattered neutrons can be detected using ³He-filled drift tubes [41], which provide a measurement of the cleaning time of the trap, which will be discussed in forthcoming reports.

UCN in the guide system can also be transported past the trap door and into a ¹⁰B-coated ion chamber (B in Fig. 1) [42]. The counter is separated from the rest of the guide system by an aluminum shutter (S in Fig. 1), which transmits neutrons with an energy greater than the optical potential of aluminum (54 neV), most of which would be too high in energy to be stored if loaded into the trap. This allows the UCN flux to be monitored, while at the same time maintaining a high density of lower energy UCN in the guide system that are guided upwards into the trap. Comparing the detector count rates with the shutter open and closed is also a measure of changes in the initial UCN spectrum: Pressure and temperature fluctuations in the UCN source can change the residual gas upscattering and absorption mean free paths for UCN (which are velocity dependent), thereby changing the ratio of trappable to untrappable UCN in the apparatus.

UCN are loaded into the trap, cleaned, stored for various times, and emptied into the $^{10}\mathrm{B}$ counter to determine the storage time constant τ_{store} . A typical filling and emptying cycle of the apparatus is shown in Fig. 3. At the beginning of a cycle, all UCN valves are open, the cleaner is lowered, and the proton beam is turned on. After $t_{\mathrm{pre}} = 30$ s, the shutter is closed and filling continues for another 180 s until the time t_{fill} . Once filling is complete, the shutter is then opened to drain UCN from the guides, the proton beam is turned off,

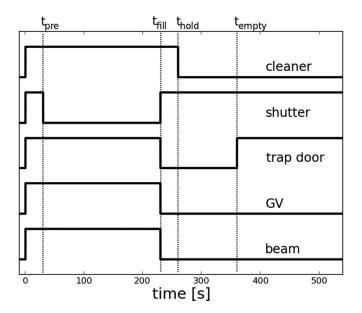


FIG. 3. The timing of components during a fill and empty cycle. The beam is on (off), valves are open (closed), and the cleaner is down (up) for a high (low) signal.

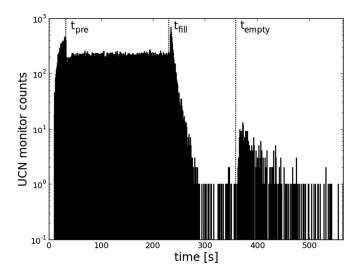


FIG. 4. The 10 B counter rate during a measurement cycle. From left to right, the vertical lines represent time $t_{\rm pre}$ when the shutter is closed, $t_{\rm fill}$ when the trap door is closed and shutter opened, and $t_{\rm empty}$ when the trap door is opened.

and the trap door and main gate valve are shut. The cleaner remains in a lowered position for an additional 30 s; it is raised at time $t_{\rm hold}$, and the UCN are stored for variable amounts of time (100 to 2000 s). The trap door is then opened at time $t_{\rm empty}$ to measure the number of surviving UCN and measure the detector background. The storage time is then given by $t_{\rm store} = t_{\rm empty} - t_{\rm hold}$. The cleaning and filling times are motivated by Monte Carlo studies of UCN in the guide system and trap.

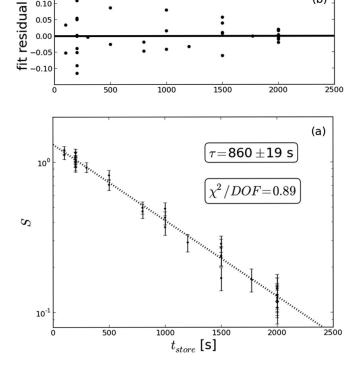
Figure 4 shows the UCN monitor rate during a typical measurement cycle. The count rate increases as the density in the guide system saturates. Once the shutter is closed at $t_{\rm pre}$, the count rate reduces due to deflecting away neutrons with $E < V_{\rm F}^{\rm (Al)}$. At the end of the filling cycle, the count rate rapidly increases due to reopening the shutter, then diminishes with time as the UCN drain from the guide system. Upon reopening the trap door at $t_{\rm empty}$, the surviving neutrons are then counted.

After filling the trap, some UCN remain in the guide system for an average time of 5–10 s before being lost or detected. For short storage times, this affects the otherwise constant background in the monitor detector. To correct for this, the counting rate from time $t_{\rm fill}$ until $t_{\rm empty}$ is fit to the function

$$B(t) = B_0 \exp(-\beta t) + B_1,$$
 (1)

where B_0 , B_1 , and β (typically $\sim 0.15 \, \mathrm{s}^{-1}$) are free parameters. As an example, for the 2000-s storage time runs, B(t) is dominated by $B_1 \approx 0.02$; the average signal to background (integrated over the signal window) for these runs was approximately 1.7. This incorporates the time-independent detector background B_1 along with the UCN draining from the guide system at time t_{hold} .

For sufficiently stable operation of the UCN source, the initial number of trapped UCN is proportional to the detector rate from time $t_{\rm pre}$ until $t_{\rm fill}$. The mean rate R during this time window is used as a normalizing factor for the emptying signal. The ratio of counts P with the shutter open to the rate R



(b)

FIG. 5. (a) The signal S vs t_{store} with statistical error bars. The storage time constant of the trap is given by τ_{store} from the exponential fit. (b) The residuals of the exponential fit vs t_{store} .

provides a coarse indication of changes in source performance, causing fluctuations in the ratio of trappable to countable UCN, as discussed above. We reject runs where P/R fluctuates by more than 20%, which serves to remove runs with abnormally high pressure in the source and runs with malfunctioning valves. This cut 9% of runs from the data, and while it does not significantly change the central value of the fit shown in Fig. 5, it does improve the goodness of fit.

The signal S is then defined to be

$$S \equiv \frac{1}{R} \frac{1}{\Delta t} \int [D(t) - B(t)] dt, \qquad (2)$$

where the limits of integration run from t_{empty} to $t_{\text{empty}} + 100 \text{ s}$, Δt is the integration bin width, and D(t) is the measured counter rate while emptying. The signal for various t_{store} is shown in Fig. 5 (with statistical error bars) for data acquired over approximately 20 h. We perform a least squares fit of $N \exp(-t/\tau_{\text{store}})$ to the data, from which τ_{store} is deduced. The measurement is repeated with the holding field deactivated, which reduces the storage time due to depolarization of the trapped UCN. We find that $\tau_{\text{store}} = 860 \pm 19 \text{ s} \ (\chi^2/\nu = 0.87)$ with the holding field activated, and $\tau_{store} = 470 \pm 160 \text{ s}$ $(\chi^2/\nu = 1.17)$ with the field deactivated. The fit value of τ_{store} with this method is consistent with a determination by computing the log ratio of the signal of long and short storage times (as was done, for example, in Refs. [10] and [11]). The observed τ_{store} is within $\sim 1\sigma$ of current global averages for τ_n [14,16], and the data are consistent with a single exponential with no additional background component.

We estimate the trapped number of UCN (at the beginning of a storage interval) to be on the order of 10⁴ based on UCN transport simulations of the experiment. The limited statistical sensitivity is primarily due to the limited transport efficiency of the guide section that contains the trap door and loads UCN into the trap. There is also a reduced loading efficiency for lowfield-seeking UCN due to spin relaxation in the guide system prior to entering the trap. This is probably due to stainless steel components near the trap door, which are known to have a comparatively high depolarization probability per bounce, and also from field nodes in the guide system near the trap door magnet plate when it is in the lowered position. These problems will be addressed in future runs of the experiment by modifying the trap loading guides and actuator assembly to have a nondepolarizing copper lining and by increasing the travel of the trap door to improve the loading efficiency of the trap. From this we expect a significant increase in statistical sensitivity, in addition to an increase from anticipated improvements to the UCN source and guide system.

The statistical sensitivity of the measurement can also be improved by eliminating the need to transport UCN out of the trap for detection. This can be accomplished by introducing an in situ detector into the trap from above after t_{empty} , which can potentially assure a faster draining time and more uniform detection efficiency over the phase space of the trap. One such technique is currently being investigated: A vanadium foil (pure vanadium has $V_{\rm F} \approx -7$ neV) is introduced into the trap to absorb the surviving UCN and then raised into a coincident β/γ detector array to measure the activation of the foil [43]. The technique of vanadium activation has been used to measure UCN density in guide systems and the Los Alamos Neutron Science Center (LANSCE) UCN source [34,44]. Preliminary measurements using this technique indicate a substantially larger counting signal than that for the UCN monitor, and this is a subject of ongoing work. In addition, an in situ detector can be used in comparative studies with UCN monitor detectors to develop a more robust means of normalizing the initial UCN density upon filling.

Incorporating the cuts discussed above, no systematic correction due the UCN source stability is needed for these data. However, the nontrivial time structure during filling in Fig. 4 suggests that the UCN production rate and UCN spectrum may produce subtle changes in the quantity chosen for normalization of the trap density. In order to study the stability of the initial UCN density normalization for future high-precision campaigns, we have studied (in separate experiments) the stability of the UCN spectrum by comparing the instantaneous counting rates in two detectors with different potential barriers, and these studies demonstrate relative consistency at the 0.1% level. The time response of monitor detectors to fluctuations in the UCN production rate is also under study and can be directly studied by varying the pulse structure of protons on the spallation target. These studies will be used to determine the optimal monitor detector configuration to accurately determine the initial trap density to within 0.1%.

The holding-field-off storage time shows that an auxilliary field is needed to remove field nodes from the trap volume.

When the holding field is not present, ambient fields in the experimental area cancel with the small but nonzero Halbach array field far from the trap surface. Depolarization can be caused by the small but non-negligible violation of the adiabatic approximation for the UCN. Recently, Steverl et al. extended the calculation of UCN depolarization in a Halbach array found in Ref. [31]. The authors calculated the UCN velocity-averaged probability current of the high-field-seeking spin state at the surface of the array, considering trajectories with velocity components that were both normal to and parallel to the surface [45]. For a holding field strength comparable to that used here, the depolarization rate $\tau_{\rm depol}^{-1}$ is found to be approximately 10^{-6} to 10^{-5} of τ_n^{-1} . The validity of this result could be compromised near the edges of the holding field coils, the effect of which will be addressed in UCN τ by implementing a flux return for the holding field coils to assure better uniformity.

In addition, the magnetic field profile of the trap will be mapped using an automated three-axis hall probe. This will allow us to investigate possible defects in the Halbach array. These defects could cause a reduced field strength near the trap surface or a region of inadvertent cancellation between the Halbach array field and holding field. Any identified defects can be assessed and repaired to assure satisfactory magnetic field conditions.

Quasibound UCN and phase space time dependence are not expected to contribute to the uncertainty in τ_{store} at the current level of precision, but the study of these effects is

critical for future measurements of τ_n . Ongoing simulations of the experiment are being performed to estimate the severity of these effects. Future work will also provide experimental observables (e.g., the cleaning time constant) which can be used to understand the dynamics of the trap.

We have determined the storage time of the UCN τ permanent magnet trap at the LANSCE UCN source and observed a reduced storage time with no holding field, which indicates the presence of field nodes which are overcome by the activated field. The current level of statistical sensitivity of the experiment will be improved by reconfiguring the trap loading system and increasing the density of the UCN source, which will allow us to perform $\sim 0.1\%$ determinations of the storage time on an \sim day time scale, so that systematic studies and *in situ* UCN detector tests can be performed.

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