

Realistic shell-model calculations for isotopic chains “north-east” of ^{48}Ca in the (N, Z) plane

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We perform realistic shell-model calculations for nuclei with valence nucleons outside ^{48}Ca , employing two different model spaces. The matrix elements of the effective two-body interaction and electromagnetic multipole operators have been calculated within the framework of many-body perturbation theory, starting from a low-momentum potential derived from the high-precision CD-Bonn free nucleon-nucleon potential. The role played by the neutron orbital $1d_{5/2}$ has been investigated by comparing experimental data on yrast quadrupole excitations of isotopic chains north-east of ^{48}Ca with the results of calculations including or not including this single-particle state in the model space.

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I. INTRODUCTION

An interesting aspect of the physics of nuclei approaching the neutron drip line is the evolution of their shell structure. This topic is currently investigated in different mass regions, and the modern advances in the detection techniques and new experimental devices provide data that drive to a better understanding of the microscopic mechanism underlying modifications of the “magic numbers.”

In this context, in the last decade the key role played by the tensor component of the residual two-body interaction between spin-orbit partner single-particle states has been recognized [1–3]. This may give rise to a breaking of shell closures leading to the possible appearance of the so-called “island of inversion;” namely, a region of nuclei where a rapid development of collectivity is observed. The best-known example of this phenomenon is given by neutron-rich nuclei around ^{32}Mg [4].

The region of nuclei with valence protons outside doubly closed ^{48}Ca may be considered an interesting laboratory to study the shell evolution when adding neutrons, since there are long isotopic chains, such as those of iron and nickel isotopes, whose exotocity reaches an N/Z value of 1.79 in ^{78}Ni .

As a matter of fact, it can be observed that the shell closure at $N = 40$ in ^{68}Ni , corresponding to the filling of the neutron fp orbitals and of the proton $f_{7/2}$ orbital, rapidly disappears when removing protons from $f_{7/2}$, as testified by the behavior of the experimental excitation energies of the yrast $J^\pi = 2^+$ states in iron and chromium neutron-rich isotopes.

For these isotopic chains several experimental studies (see, for example, Refs. [5–9]) have found out that the disappearance of the $N = 40$ shell closure comes along with the onset of collective behavior, as indicated for instance by the observation of a rapid increase of the ratio $E_x(4_1^+)/E_x(2_1^+)$ in $^{60-64}\text{Cr}$ [10,11]. This has been related to the correlations between the quadrupole-partner neutron orbitals $0g_{9/2}$ and $1d_{5/2}$ [12–14], so, within a shell-model description of these nuclei, the inclusion of the neutron $1d_{5/2}$ orbital should be needed.

It is worth pointing out that there is a general belief [15] that shell-model effective interactions derived from realistic nucleon-nucleon (NN) potentials are defective in their monopole component, so that they are not able to provide a good description of the evolution of spectroscopic properties along the isotopic chains, unless including contributions from three-nucleon forces [16,17].

On these grounds, we have found it challenging to perform realistic shell-model calculations [18] for some isotopic chains north-east of ^{48}Ca , starting from the high-precision CD-Bonn NN potential renormalized by way of the so-called $V_{\text{low-k}}$ approach [19,20]. In particular, in order to explore the microscopic processes leading to the disappearance of the $N = 40$ shell closure and the onset of collectivity, we have derived two effective shell-model interactions for two different model spaces. The first one, which is spanned by the proton $0f_{7/2}$ and $1p_{3/2}$ orbitals and by the neutron $1p_{3/2}$, $1p_{1/2}$, $0f_{5/2}$, $0g_{9/2}$ orbitals, is able, as we show in the following, to reproduce the dropping of the $N = 40$ magic number in iron and chromium isotopes as well as many other spectroscopic properties of nuclei north-east of ^{48}Ca . The second one is spanned by the same orbitals plus the neutron $1d_{5/2}$. The calculations within the latter model space are able to reproduce the onset of collectivity in heavy iron and chromium isotopes, at the same time preserving the results obtained with the first model space.

In the following section, we outline the perturbative approach to the derivation of our shell-model Hamiltonians and effective charges of the electric quadrupole operators. In Sec. III, we present the results of our calculations for calcium, titanium, chromium, iron, and nickel isotopes. Concluding remarks are given in the last section. In the Appendix, we report the calculated two-body matrix elements (TBME) of the effective shell-model interactions, the employed single-particle (SP) energies, and the effective charges of the $E2$ operator.

II. OUTLINE OF CALCULATIONS

Within the framework of the shell model, an auxiliary one-body potential U is introduced in order to break up the

Hamiltonian for a system of A nucleons as the sum of a one-body term H_0 , which describes the independent motion of the nucleons, and a residual interaction H_1 :

$$H = \sum_{i=1}^A \frac{p_i^2}{2m} + \sum_{i<j=1}^A V_{ij}^{NN} = T + V = (T + U) + (V - U) = H_0 + H_1. \quad (1)$$

Once H_0 has been introduced, it is possible to define a reduced model space in terms of a finite subset of H_0 's eigenvectors. In this space, an effective Hamiltonian H_{eff} may be constructed and the diagonalization of the many-body Hamiltonian (1) in an infinite Hilbert space is then reduced to the solution of an eigenvalue problem in a finite space.

As mentioned in the Introduction, we derive effective shell-model Hamiltonians H_{eff} for two model spaces outside the ^{48}Ca core. The first one (I) is spanned by the two single-proton levels $0f_{7/2}$, $1p_{3/2}$ and the four single-neutron levels $1p_{3/2}$, $1p_{1/2}$, $0f_{5/2}$, $0g_{9/2}$, while the second one (II) includes also the neutron $1d_{5/2}$ orbital.

To this end, the following approach has been employed: first we derived an H_{eff} defined in a very large model space outside the ^{40}Ca closed core and spanned by six proton and neutron $pfgd$ orbitals. Then, we derive from this H_{eff} two new effective Hamiltonians, defined in the smaller model spaces (I) and (II). The above double-step procedure ensures that, when the $1d_{5/2}$ orbital is irrelevant to describe the physics of certain nuclear states, the eigenvalues obtained using model space (I) or (II) are the same or at least very close to each other.

The derivation of both H_{eff} s has been done in the framework of the time-dependent perturbation theory by way of the Kuo–Lee–Ratcliff (KLR) folded-diagram expansion [21]. More precisely, we first renormalize the high-momentum repulsive components of the CD-Bonn NN potential by way of the $V_{\text{low-}k}$ approach [19,20] with a momentum cutoff $\Lambda = 2.6 \text{ fm}^{-1}$, which provides a smooth potential preserving exactly the on-shell properties of the original NN potential. Next, we express H_{eff} in terms of the vertex function \hat{Q} -box, which is composed of irreducible valence-linked diagrams [22,23]. In the derivation of the \hat{Q} -box we have included one- and two-body Goldstone diagrams through third order in H_1 [24]. Since calculations beyond the third order in perturbation theory are computationally prohibitive, we have calculated the Padé approximant [2|1] [25,26] of the \hat{Q} -box, so as to obtain a value to which the perturbation series should converge, as suggested in Ref. [27]. The folded-diagram series is then summed up to all orders using the Lee–Suzuki iteration method [28].

The Hamiltonian H_{eff} contains one-body contributions, whose collection is the so-called \hat{S} -box [29]. In realistic shell-model calculations a subtraction procedure is commonly used, so as to retain only the TBME of H_{eff} (V_{eff}), while the SP energies are taken from experiment. This approach enables to take into account implicitly the effects of three-body forces on the SP energies.

In this work, the proton SP energy spacing is taken from the experimental one between the yrast $\frac{3}{2}^-$ state and the $\frac{7}{2}^-$ ground state in ^{49}Sc [30], which are mainly of single-particle nature [31], so that $\epsilon_{p_{3/2}} - \epsilon_{f_{7/2}} = 3.1 \text{ MeV}$. Similarly, the two neutron $\epsilon_{p_{1/2}} - \epsilon_{p_{3/2}}$, $\epsilon_{f_{5/2}} - \epsilon_{p_{3/2}}$ spacings are taken from the experimental spectrum of ^{49}Ca , considering the yrast $\frac{1}{2}^-$ and the yrare $\frac{5}{2}^-$ states [30], that have the largest observed single-particle components [32]. As regards the neutron $0g_{9/2}$ state, at present there is no experimental indication of the existence of such a state in ^{49}Ca , therefore we have fixed its energy so as to reproduce the experimental odd-even mass difference around ^{68}Ni [33]. All the observed $\frac{5}{2}^+$ states in ^{49}Ca do not exhibit a significant SP component, so we have chosen a value of the $1d_{5/2}$ energy which gives, when using model space (II), an odd-even mass difference around ^{80}Zn in a reasonable agreement with the estimated value [33]. In summary, our adopted neutron SP energy spacings for model space (I) are $\epsilon_{p_{1/2}} - \epsilon_{p_{3/2}} = 2.0 \text{ MeV}$, $\epsilon_{f_{5/2}} - \epsilon_{p_{3/2}} = 4.0 \text{ MeV}$, $\epsilon_{g_{9/2}} - \epsilon_{p_{3/2}} = 4.1 \text{ MeV}$, and for model space (II) $\epsilon_{g_{9/2}} - \epsilon_{p_{3/2}} = 3.8 \text{ MeV}$ and $\epsilon_{d_{5/2}} - \epsilon_{p_{3/2}} = 8.0 \text{ MeV}$.

The SP energies and TBME relative to ^{48}Ca used in the present calculation can be found in Tables I, II, III, and IV while the proton and neutron effective charges of the electric quadrupole operator, that have been derived consistently with H_{eff} , are in Tables V and VI. It should be pointed out that for protons the Coulomb force has been explicitly added to $V_{\text{low-}k}$ before constructing V_{eff} .

III. RESULTS

In this section, we report the results of our shell-model calculations for calcium, titanium, chromium, iron, and nickel isotopes with mass number $A > 48$ and compare them with the available experimental data. As mentioned in the Introduction, our attention is focused on the insurgence of collective behavior or shell-closure properties when adding valence neutrons.

The calculations have been performed by using the OSLO shell-model code [34].

A. Calcium isotopes

A major topic in nuclear physics is the understanding of the shell evolution towards the neutron dripline, and in this context the study of calcium isotopes provides an interesting laboratory [17,35–38].

An extensive study of the heavy calcium isotopes has been reported in Ref. [39], where we have performed a shell-model calculation using ^{40}Ca as an inert core and the full fp shell as model space. As in the present paper, the effective interaction has been obtained from a $V_{\text{low-}k}$ derived from the CD-Bonn potential with a cutoff momentum equal to 2.6 fm^{-1} . The results we obtained are in excellent agreement with the experimental data, in particular we successfully predicted the excitation energy of the yrast $J = 2^+$ in ^{54}Ca , that only recently has been measured at RIKEN [40].

Figure 1 reports the excitation energies of the yrast 2^+ states calculated with model spaces (I) and (II) as a function

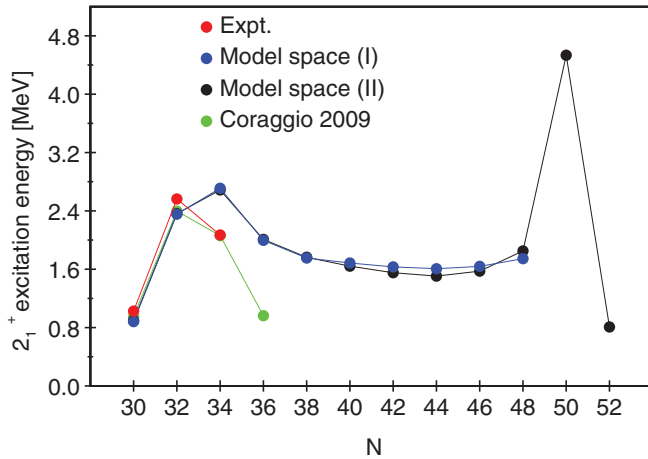


FIG. 1. (Color online) Experimental [30,40] and calculated excitation energies of the yrast $J^\pi = 2^+$ states for calcium isotopes.

of the neutron number up to $N = 52$ and compared with the available experimental data and the results obtained by our previous calculations with the full fp -shell-model space.

It can be seen that the available observed energies are well reproduced for $N = 30, 32$; the three calculations providing almost the same values. At $N = 34, 36$ the results with model spaces (I) and (II) differ from those of Ref. [39] and are almost indistinguishable up to $N = 48$. We have verified that to reproduce the observed drop in energy at $N = 34$ it is necessary, as in Ref. [39], to include explicitly the neutron $0f_{7/2}$ orbital into the model space. On the other hand, the different results obtained at $N = 36$ trace back to the presence in model spaces (I) and (II) of the $0g_{9/2}$ orbital that starts to fill just at $N = 36$. As a matter of fact, we have verified that, when blocking out this orbital, the calculated excitation energy of the yrast 2^+ state drops abruptly down at 0.7 MeV.

This suggests that to optimize the description of the calcium isotopic chain one has to adopt a model space spanned by the full fp shell plus the $0g_{9/2}$ orbital.

From the inspection of Fig. 1, it can be seen that no shell closure shows up at $N = 40$, since the $0g_{9/2}$ SP energy is very close to the pf ones, while the large energy gap between $0g_{9/2}$ and $1d_{5/2}$ orbitals is responsible for a strong shell closure at $N = 50$ and that, according to our calculations, ^{70}Ca should be the last bound calcium isotope. This picture is confirmed when looking at the behavior of the calcium effective single-particle energies (ESPEs), as reported in Fig. 2.

B. Titanium isotopes

The calculated excitation energies of the yrast 2^+ states and the $B(E2; 2^+_1 \rightarrow 0^+_1)$ transition rates for titanium isotopes are reported in Fig. 3 up to $N = 40$. It can be seen that the observed excitation energies and $B(E2)$ s are well reproduced by both calculations.

The decrease of the experimental 2^+_1 excitation energy in ^{56}Ti is linked to the lack of a $N = 34$ shell closure, as we

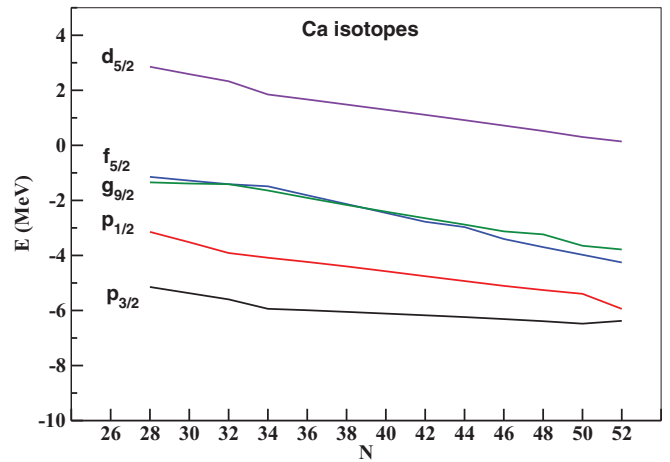


FIG. 2. (Color online) Calculated neutron effective single-particle energies for calcium isotopes from $N = 30$ to 52.

predicted in Ref. [39] and confirmed by the recent observation of the excitation energy of $J^\pi = 2^+_1$ state in ^{54}Ca [40].

From inspection of Fig. 3, it can be observed that the calculated 2^+_1 excitation energies are almost insensitive to the inclusion of the $1d_{5/2}$ orbital. This does not happen with the $B(E2)$ s, whose calculated values begin to differ substantially starting from $N = 36$ on. In particular, using model space (I) the increase of the number of valence neutrons corresponds to a rise of the proton $0f_{7/2}$ occupation number and to the decrease of the proton polarization, at variance with model space (II) where the occupation of this orbital is almost constant respect to the neutron number N (see Table VIII). This comes with a significantly larger occupation of the neutron

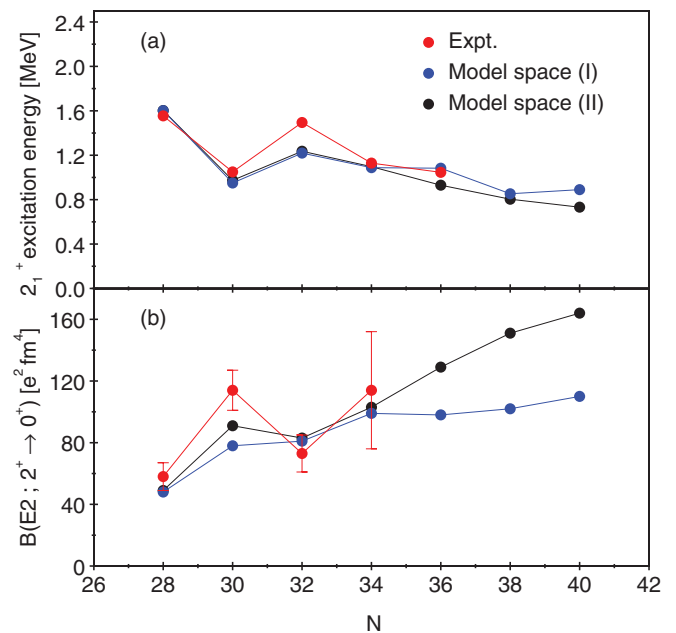


FIG. 3. (Color online) (a) Experimental [30,48] and calculated excitation energies of the yrast $J^\pi = 2^+$ states and (b) $B(E2; 2^+_1 \rightarrow 0^+_1)$ transition rates for titanium isotopes.

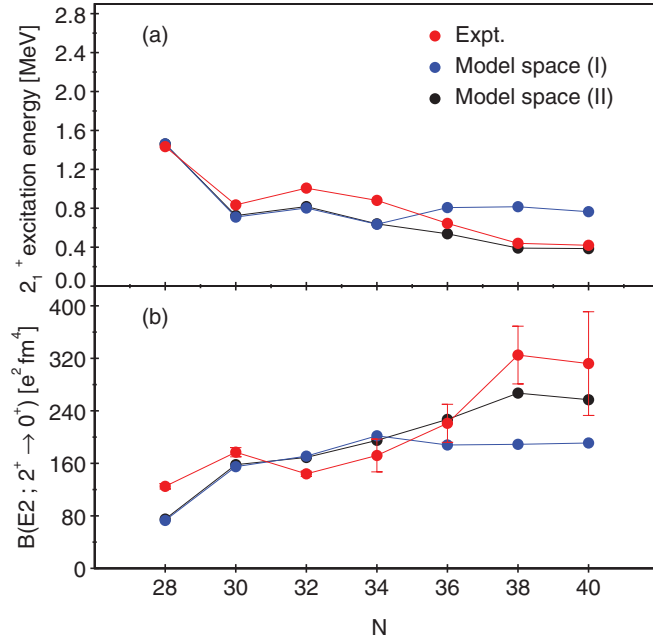


FIG. 4. (Color online) Same as in Fig. 3, but for chromium isotopes. Experimental data are taken from [30,49].

$0g_{9/2}$ orbital with model space (II) with respect to model space (I), as well as an increase of the neutron $1d_{5/2}$ -orbital occupation that provides a constant rise of the corresponding $B(E2)$ s up to $N = 40$.

C. Chromium isotopes

The excitation energies of the yrast 2^+ states and $B(E2; 2_1^+ \rightarrow 0_1^+)$ transition rates for the chromium isotopes are reported in Fig. 4 up to $N = 40$. It is worth mentioning that the observed lowering of the yrast 2^+ states starting from $N = 34$ is interpreted as a signature of the development of a pronounced collectivity towards $N = 40$ [11]. The interpretation of such a collective behavior may be framed within the quasi-SU(3) approximate symmetry owing to the interplay between the quadrupole-quadrupole component of the residual interaction and the central field in the subspace spanned by the lowest $\Delta j = 2$ orbitals of a major shell [12]. In this connection, the need to include the neutron $1d_{5/2}$ orbital in a shell-model calculation, in order to produce the onset of collectivity around $N = 40$ in chromium isotopes, has been evidenced by Caurier, Nowacki, and Poves in Ref. [13].

Our results also support the crucial role played by this orbital. In fact, from inspection of Fig. 4 it can be observed that using model space (I) from ^{58}Cr to ^{60}Cr the calculated $J^\pi = 2_1^+$ states start to rise in excitation energy, while the experimental behavior does the opposite. Actually, by employing the model space (II), there is a decrease of the 2^+ excitation energy from $N = 34$ to $N = 36$. From the inspection of Table VII, we see that the appearance of the differences between the model-space (I) and (II) results come together with an abrupt increase of the occupation number

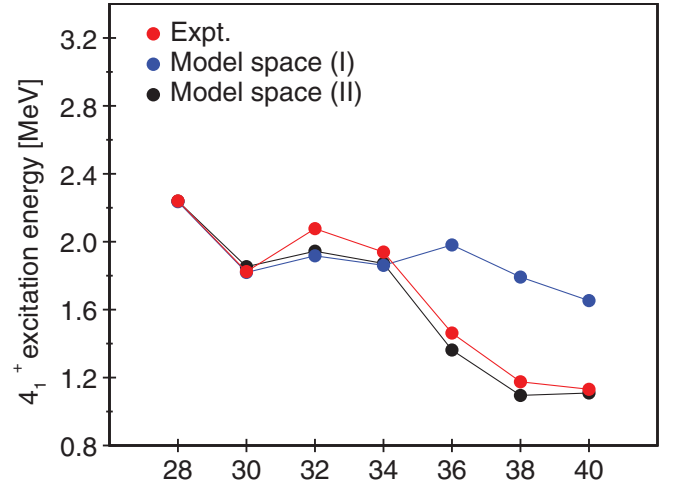


FIG. 5. (Color online) Experimental [30] and calculated excitation energies of the yrast $J^\pi = 4^+$ for Cr isotopes. See text for details.

of the neutron $1d_{5/2}, 0g_{9/2}$ orbitals and a depletion of the proton $0f_{7/2}$ one. This has to be ascribed to a reduced neutron gap between $0g_{9/2} - 0f_{5/2}$ (about 2.5 MeV) effective single-particle energies (ESPEs) with respect to the one in Ni isotopes (about 4.0 MeV), where a shell closure is found at $N = 40$ (see Sec. IV), as well as to the quadrupole-quadrupole component of the effective interaction between the $1d_{5/2}$ and the $0g_{9/2}$ orbitals.

Another feature that reveals the onset of the collectivity in chromium isotopes is the rise of the experimental $B(E2; 2_1^+ \rightarrow 0_1^+)$ transition rates from $N = 34$ to $N = 38$. This can be reproduced only by calculations with model space (II), as can be seen in Fig. 4, where the experimental data are compared with our shell-model results with both model spaces.

In Fig. 5 the calculated and experimental excitation energies of the yrast 4^+ states are also reported, evidencing that only with model space (II) it is possible to reproduce the observed increase of the ratio $E_x(4_1^+)/E_x(2_1^+)$ from ^{60}Cr to ^{62}Cr .

D. Iron isotopes

In Fig. 6 the 2_1^+ excitation energies and $B(E2; 2_1^+ \rightarrow 0_1^+)$ transition rates of even iron isotopes are shown as a function of the neutron number up to $N = 40$. It should be mentioned that experimental data are available for ^{68}Fe too [41], but they are not reported since for this nucleus calculations performed with model space (II) need a CPU time which exceeds our present computational resources.

A relevant feature that can be inferred from Fig. 6 is the abrupt enhancement of $B(E2; 2_1^+ \rightarrow 0_1^+)$ in ^{64}Fe [7,8,41] that, as in chromium isotopes, is the evidence of the onset of a quadrupole collectivity. This is at variance with the results of calculations with model space (I), which show a decrease of $B(E2; 2_1^+ \rightarrow 0_1^+)$ from ^{62}Fe to ^{64}Fe . Actually, the onset of the above-mentioned quadrupole collectivity is reproduced using model space (II), and, as in Ti and Cr

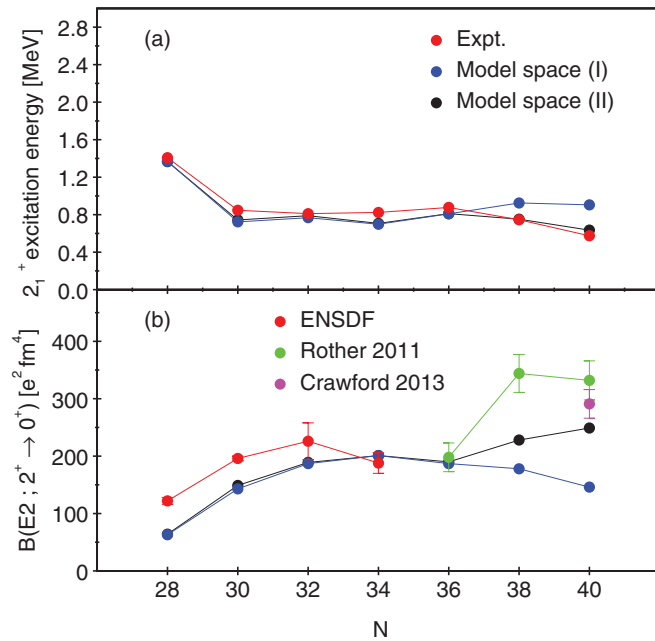


FIG. 6. (Color online) Same as in Fig. 3, but for iron isotopes. Experimental data are taken from ENSDF [30], Rother 2011 [8], and Crawford 2013 [41].

isotopes, comes with a rise of the occupation number of the neutron $0g_{9/2}$ orbital (see Table VII). It has to be pointed out, however, that the experimental datum in ^{64}Fe [8] is underestimated.

E. Nickel isotopes

The nickel isotopes represent a very interesting laboratory to study the effects of the NN interaction on the shell evolution, when increasing the number of valence neutrons. In fact, this is a very long isotopic chain with available spectroscopic data from $N = 24$ up to $N = 48$, and several efforts are at present devoted to get as much experimental information as possible on ^{78}Ni , which is a possible waiting point for r -process nucleosynthesis [42]. Figure 7 reports the experimental data and the results of our shell-model calculations with model spaces (I) and (II) for the 2_1^+ excitation energy and the $B(E2; 2_1^+ \rightarrow 0_1^+)$ systematics from $N = 28$ to $N = 50$.

As already mentioned in the Introduction, it can be seen that the filling of the proton $0f_{7/2}$ orbital, corresponding to the well-known $Z = 28$ closure, produces the disappearance of the collectivity towards $N = 40$ observed in chromium and iron isotopes. The peak of the yrast 2^+ excitation energy and the fall of the corresponding $B(E2)$ in ^{68}Ni is a clear manifestation of the shell closure at $N = 40$, which is added to the ones at $N = 28$ and $N = 50$ in this long isotopic chain. As a matter of fact, it turns out that our calculated neutron ESPEs provide a large gap between the $0g_{9/2}$ and fp orbitals (see Fig. 8).

This implies a minor role played by the correlations between the quadrupole partners $0g_{9/2}, 1d_{5/2}$, as supported by the fact that the calculations with model space (I) and (II)

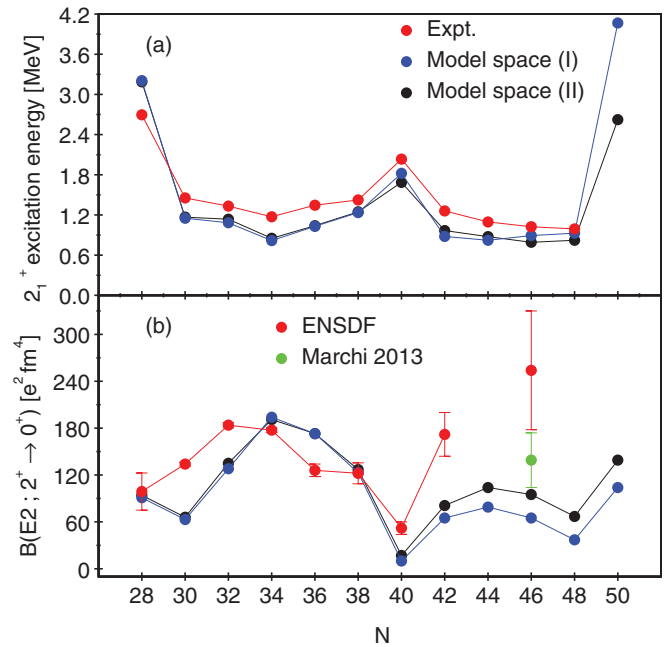


FIG. 7. (Color online) Same as in Fig. 3, but for nickel isotopes. Experimental data are taken from ENSDF [30] and Marchi 2013 [43].

give similar occupation numbers (see Table VII), as well as the same behavior for the $E_x(2_1^+)$ and the electric-quadrupole transition rates (see Fig. 7).

It is interesting to note that recently the $B(E2; 2_1^+ \rightarrow 0_1^+)$ in ^{74}Ni has been measured in a Coulomb excitation experiment [43], the obtained value being significantly smaller than the one measured indirectly via a (p, p') inelastic diffusion [44]. Our values of the $B(E2)$ s for ^{74}Ni are close to the recently measured one. They, however, do not reproduce the decrease in $B(E2)$ from $N = 42$ to $N = 46$ since the ^{70}Ni $B(E2)$ is significantly underestimated. More precisely, we predict an increase of $B(E2)$ from $N = 40$ to $N = 42$ but not as large as the observed one. This may be traced to the fact that our proton

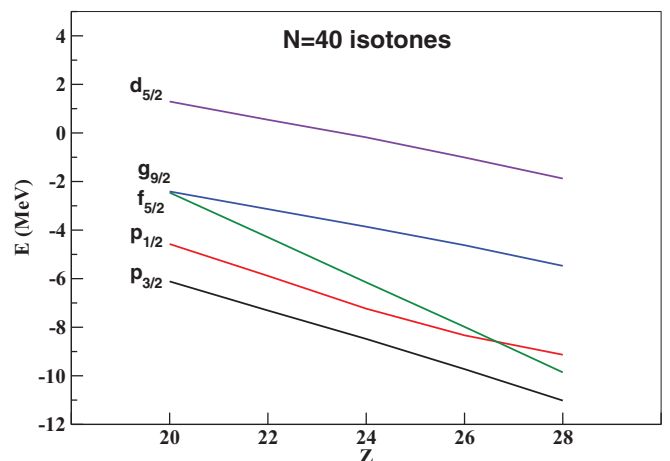


FIG. 8. (Color online) Calculated neutron effective single-particle energies for Ti, Cr, Fe, and Ni isotopes at $N = 40$.

model space leaves out the $0f_{5/2}$ orbital, which has a relevant role beyond $N = 40$ as evidenced by the behavior of the yrast $5/2^-$ states in odd-mass Cu isotopes [30]. As a matter of fact, for Ni isotopes with $N > 40$ the attraction due to the tensor force between the neutron $0g_{9/2}$ and the proton $0f_{5/2}$ orbitals may give rise to a lowering of the latter leading to a strong core polarization with a consequent increase of the $B(E2)$ s. It is worth mentioning, however, that shell-model calculations that include explicitly the proton $0f_{5/2}$ orbital show the same behavior of $B(E2)$ as ours [45].

Finally, it has to be observed that, because of the magicity at $N = 50$, the yrast $J = 2^+$ state in ^{78}Ni is built up, breaking a couple of protons in the filled $0f_{7/2}$ orbital and promoting one proton into the $1p_{3/2}$ orbital. This mechanism is then responsible of the increase of the theoretical $B(E2; 2^+ \rightarrow 0^+)$ with respect to neighboring nuclei.

IV. CONCLUDING REMARKS

We have presented here the results of an extensive shell-model study of nuclei north-east of ^{48}Ca within the framework of a microscopic approach. This means that, starting from a $V_{\text{low-k}}$ derived from the CD-Bonn NN potential, effective two-body interactions and effective electromagnetic multipole operators have been calculated by way of perturbation theory and then employed in shell-model calculations.

As mentioned in the Introduction, this region is currently the subject of many experimental and theoretical investigations, especially because of the behavior of the quadrupole collectivity at $N = 40$ versus the atomic number, as can be inferred from the inspection of Fig. 9.

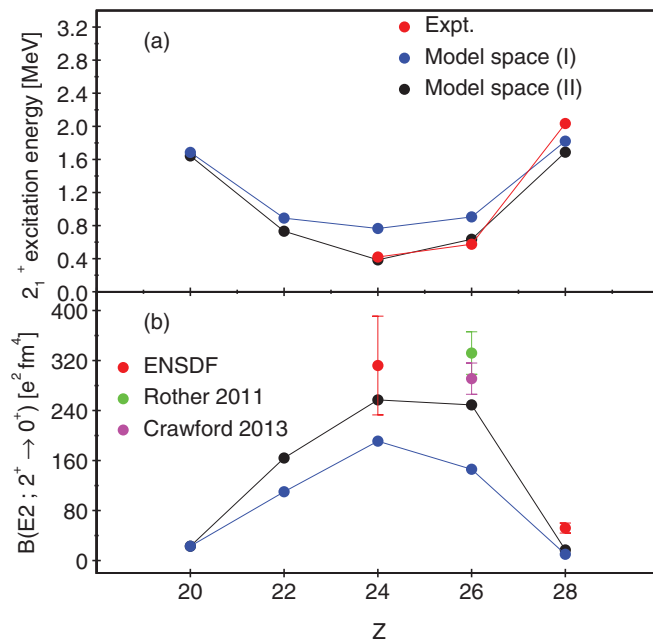


FIG. 9. (Color online) (a) Experimental (ENSDF: [30], Rother 2011: [8], Crawford 2013: [41]) and calculated excitation energies of the yrast $J^\pi = 2^+$ states and (b) $B(E2; 2^+ \rightarrow 0^+)$ transition rates for the $N = 40$ isotones.

In this context, we have focused attention on the role played by the neutron $1d_{5/2}$ orbital in the spectroscopy of the nuclei under investigation, using two different model spaces which differ only by the inclusion of this SP state.

Our results are in a better agreement with experiment when using the larger model space, in line with other large-scale shell-model calculations [14,45–47] where the TBMEs were determined empirically. This confirms the ability of realistic shell-model calculations to provide a reliable microscopic description of the shell evolution along isotopic chains, even in the presence of strong collective features. In fact, results with model spaces (I) and (II) are similar only for Ni isotopes, evidencing the relevance of including the neutron $1d_{5/2}$ orbital to describe the collective properties of Ti, Cr, and Fe isotopic chains. The role played by $1d_{5/2}$ may be explained in terms of correlations between this orbital and its quadrupole partner $0g_{9/2}$, which comes into play because of the reduction of the $0f_{5/2} - 0g_{9/2}$ gap.

The above considerations are clearly illustrated by the behaviour of the ESPEs, see Fig. 8, as well as by that of the energies of the yrast 2^+ states and of the $B(E2; 2^+ \rightarrow 0^+)$ transition rates, which are reported in Fig. 9 as functions of Z for $N = 40$. From the inspection of Fig. 9, it can be clearly seen that the nature of the yrast 2^+ states changes with the filling of the proton $0f_{7/2}$ orbital, tuning the collectivity at $N = 40$.

It has to be stressed that our calculations employ only a two-body $V_{\text{low-k}}$, derived from the high-precision CD-Bonn potential, not taking into account any three-body forces. Therefore, the good quality of the agreement between theory and experiment seems to question the role of valence three-body forces in the description of the spectroscopic properties of intermediate-mass nuclei.

APPENDIX

TABLE I. Shell-model proton single-particle energies (in MeV) employed in present work (see text for details). The value of the $\epsilon_{f_{7/2}}$ is taken from the one-proton separation energy of ^{49}Sc [33].

nlj	Model space (I) and (II)
$0f_{7/2}$	−9.627
$1p_{3/2}$	−6.527

TABLE II. Shell-model neutron single-particle energies (in MeV) employed in present work (see text for details). The value of the $\epsilon_{p_{3/2}}$ is taken from the one-neutron separation energy of ^{49}Ca [33].

nlj	Model space (I)	Model space (II)
$1p_{3/2}$	−5.157	−5.157
$1p_{1/2}$	−3.157	−3.157
$0f_{5/2}$	−1.157	−1.157
$0g_{9/2}$	−1.057	−1.357
$1d_{5/2}$		2.843

TABLE III. Proton-proton, neutron-neutron, and proton-neutron matrix elements (in MeV) derived for calculations in model space (I). They are antisymmetrized and normalized by a factor $1/\sqrt{(1 + \delta_{ja_jb})(1 + \delta_{jc_jd})}$.

$n_a l_a j_a$	$n_b l_b j_b$	$n_c l_c j_c$	$n_d l_d j_d$	J	T_z	TBME
0f7/2	0f7/2	0f7/2	0f7/2	0	1	-2.021
0f7/2	0f7/2	1p3/2	1p3/2	0	1	-1.219
1p3/2	1p3/2	1p3/2	1p3/2	0	1	-0.058
0f7/2	0f7/2	0f7/2	0f7/2	2	1	-0.414
0f7/2	0f7/2	0f7/2	1p3/2	2	1	-0.704
0f7/2	0f7/2	1p3/2	1p3/2	2	1	-0.355
0f7/2	1p3/2	0f7/2	1p3/2	2	1	-0.547
0f7/2	1p3/2	1p3/2	1p3/2	2	1	-0.356
1p3/2	1p3/2	1p3/2	1p3/2	2	1	0.108
0f7/2	1p3/2	0f7/2	1p3/2	3	1	0.329
0f7/2	0f7/2	0f7/2	0f7/2	4	1	0.133
0f7/2	0f7/2	0f7/2	1p3/2	4	1	-0.408
0f7/2	1p3/2	0f7/2	1p3/2	4	1	0.059
0f7/2	1p3/2	0f7/2	1p3/2	5	1	0.497
0f7/2	0f7/2	0f7/2	0f7/2	6	1	0.406
1p3/2	1p3/2	1p3/2	1p3/2	0	-1	-0.748
1p3/2	1p3/2	1p1/2	1p1/2	0	-1	-0.903
1p3/2	1p3/2	0f5/2	0f5/2	0	-1	-0.712
1p3/2	1p3/2	0g9/2	0g9/2	0	-1	1.171
1p1/2	1p1/2	1p1/2	1p1/2	0	-1	-0.312
1p1/2	1p1/2	0f5/2	0f5/2	0	-1	-0.478
1p1/2	1p1/2	0g9/2	0g9/2	0	-1	0.884
0f5/2	0f5/2	0f5/2	0f5/2	0	-1	-0.988
0f5/2	0f5/2	0g9/2	0g9/2	0	-1	1.577
0g9/2	0g9/2	0g9/2	0g9/2	0	-1	-1.179
1p3/2	1p1/2	1p3/2	1p1/2	1	-1	0.167
1p3/2	1p1/2	1p3/2	0f5/2	1	-1	-0.054
1p3/2	0f5/2	1p3/2	0f5/2	1	-1	0.046
1p3/2	1p3/2	1p3/2	1p3/2	2	-1	-0.241
1p3/2	1p3/2	1p3/2	1p1/2	2	-1	-0.394
1p3/2	1p3/2	1p3/2	0f5/2	2	-1	-0.162
1p3/2	1p3/2	1p1/2	0f5/2	2	-1	-0.179
1p3/2	1p3/2	0f5/2	0f5/2	2	-1	-0.178
1p3/2	1p3/2	0g9/2	0g9/2	2	-1	0.441
1p3/2	1p1/2	1p3/2	1p1/2	2	-1	-0.448
1p3/2	1p1/2	1p3/2	0f5/2	2	-1	-0.176
1p3/2	1p1/2	1p1/2	0f5/2	2	-1	-0.407
1p3/2	1p1/2	0f5/2	0f5/2	2	-1	-0.292
1p3/2	1p1/2	0g9/2	0g9/2	2	-1	0.308
1p3/2	0f5/2	1p3/2	0f5/2	2	-1	0.071
1p3/2	0f5/2	1p1/2	0f5/2	2	-1	-0.280
1p3/2	0f5/2	0f5/2	0f5/2	2	-1	-0.103
1p3/2	0f5/2	0g9/2	0g9/2	2	-1	0.494
1p1/2	0f5/2	1p1/2	0f5/2	2	-1	-0.297
1p1/2	0f5/2	0f5/2	0f5/2	2	-1	-0.282
1p1/2	0f5/2	0g9/2	0g9/2	2	-1	0.572
0f5/2	0f5/2	0f5/2	0f5/2	2	-1	-0.405
0f5/2	0f5/2	0g9/2	0g9/2	2	-1	0.239
0g9/2	0g9/2	0g9/2	0g9/2	2	-1	-0.772
1p3/2	0f5/2	1p3/2	0f5/2	3	-1	0.125
1p3/2	0f5/2	1p1/2	0f5/2	3	-1	-0.005

TABLE III. (Continued.)

$n_a l_a j_a$	$n_b l_b j_b$	$n_c l_c j_c$	$n_d l_d j_d$	J	T_z	TBME
1p1/2	0f5/2	1p1/2	0f5/2	3	-1	0.169
1p3/2	0f5/2	1p3/2	0f5/2	4	-1	-0.336
1p3/2	0f5/2	0f5/2	0f5/2	4	-1	-0.247
1p3/2	0f5/2	0g9/2	0g9/2	4	-1	0.493
0f5/2	0f5/2	0f5/2	0f5/2	4	-1	-0.087
0g9/2	0g9/2	0g9/2	0g9/2	4	-1	0.115
0g9/2	0g9/2	0g9/2	0g9/2	4	-1	-0.282
0g9/2	0g9/2	0g9/2	0g9/2	6	-1	-0.108
0g9/2	0g9/2	0g9/2	0g9/2	8	-1	-0.001
0f5/2	0g9/2	0f5/2	0g9/2	2	-1	-0.404
1p3/2	0g9/2	1p3/2	0g9/2	3	-1	-0.603
1p3/2	0g9/2	0f5/2	0g9/2	3	-1	0.227
0f5/2	0g9/2	0f5/2	0g9/2	3	-1	-0.211
1p3/2	0g9/2	1p3/2	0g9/2	4	-1	0.039
1p3/2	0g9/2	1p1/2	0g9/2	4	-1	-0.105
1p3/2	0g9/2	0f5/2	0g9/2	4	-1	0.157
1p1/2	0g9/2	1p1/2	0g9/2	4	-1	0.116
1p1/2	0g9/2	0f5/2	0g9/2	4	-1	-0.007
0f5/2	0g9/2	0f5/2	0g9/2	4	-1	0.109
1p3/2	0g9/2	1p3/2	0g9/2	5	-1	-0.099
1p3/2	0g9/2	1p1/2	0g9/2	5	-1	0.361
1p3/2	0g9/2	0f5/2	0g9/2	5	-1	0.158
1p1/2	0g9/2	1p1/2	0g9/2	5	-1	-0.335
1p1/2	0g9/2	0f5/2	0g9/2	5	-1	-0.252
0f5/2	0g9/2	0f5/2	0g9/2	5	-1	-0.065
1p3/2	0g9/2	1p3/2	0g9/2	6	-1	0.260
1p3/2	0g9/2	0f5/2	0g9/2	6	-1	0.176
0f5/2	0g9/2	0f5/2	0g9/2	6	-1	0.156
0f5/2	0g9/2	0f5/2	0g9/2	7	-1	-0.730
1p3/2	1p3/2	1p3/2	1p3/2	0	0	-2.071
0f7/2	0f5/2	0f7/2	0f5/2	1	0	-1.994
0f7/2	0f5/2	1p3/2	1p3/2	1	0	0.798
0f7/2	0f5/2	1p3/2	1p1/2	1	0	-0.970
0f7/2	0f5/2	1p3/2	0f5/2	1	0	-0.684
1p3/2	1p3/2	1p3/2	1p3/2	1	0	-0.388
1p3/2	1p3/2	1p3/2	1p1/2	1	0	0.617
1p3/2	1p3/2	1p3/2	0f5/2	1	0	-0.018
1p3/2	1p1/2	1p3/2	1p1/2	1	0	-0.742
1p3/2	1p1/2	1p3/2	0f5/2	1	0	-0.428
1p3/2	1p1/2	1p3/2	0f5/2	1	0	-1.046
0f7/2	1p3/2	0f7/2	1p3/2	2	0	-0.951
0f7/2	1p3/2	0f7/2	0f5/2	2	0	-0.738
0f7/2	1p3/2	1p3/2	1p3/2	2	0	-0.432
0f7/2	1p3/2	1p3/2	1p1/2	2	0	-0.758
0f7/2	1p3/2	1p3/2	0f5/2	2	0	-0.877
0f7/2	0f5/2	0f7/2	0f5/2	2	0	-1.424
0f7/2	0f5/2	1p3/2	1p3/2	2	0	-0.109
0f7/2	0f5/2	1p3/2	1p1/2	2	0	-0.641
0f7/2	0f5/2	1p3/2	0f5/2	2	0	-0.627
1p3/2	1p3/2	1p3/2	1p3/2	2	0	-0.547
1p3/2	1p3/2	1p3/2	1p1/2	2	0	-0.688
1p3/2	1p3/2	1p3/2	0f5/2	2	0	-0.165
1p3/2	1p1/2	1p3/2	1p1/2	2	0	-1.082
1p3/2	1p1/2	1p3/2	0f5/2	2	0	-0.443

TABLE III. (Continued.)

$n_a l_a j_a$	$n_b l_b j_b$	$n_c l_c j_c$	$n_d l_d j_d$	J	T_z	TBME
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	2	0	-0.447
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	3	0	-0.348
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{1/2}	3	0	0.587
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	3	0	0.141
0f _{7/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	3	0	-0.449
0f _{7/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	3	0	0.141
0f _{7/2}	1p _{1/2}	0f _{7/2}	1p _{1/2}	3	0	-0.618
0f _{7/2}	1p _{1/2}	0f _{7/2}	0f _{5/2}	3	0	-0.275
0f _{7/2}	1p _{1/2}	1p _{3/2}	1p _{3/2}	3	0	0.528
0f _{7/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	3	0	-0.117
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	3	0	-0.524
0f _{7/2}	0f _{5/2}	1p _{3/2}	1p _{3/2}	3	0	0.436
0f _{7/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	3	0	-0.369
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	3	0	-0.811
1p _{3/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	3	0	0.227
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	3	0	-0.261
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	4	0	-0.100
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{1/2}	4	0	-0.297
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	4	0	-0.229
0f _{7/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	4	0	-0.615
0f _{7/2}	1p _{1/2}	0f _{7/2}	1p _{1/2}	4	0	-0.592
0f _{7/2}	1p _{1/2}	0f _{7/2}	0f _{5/2}	4	0	-0.590
0f _{7/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	4	0	-1.004
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	4	0	-0.848
0f _{7/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	4	0	-0.783
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	4	0	-0.753
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	5	0	-0.884
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	5	0	0.274
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	5	0	-0.179
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	6	0	-1.577
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	1	0	-0.846
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	2	0	-0.617
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	3	0	-0.176
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	3	0	-0.419
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	3	0	-0.723
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	4	0	-0.091
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	4	0	-0.419
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	4	0	-0.211
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	5	0	-0.003
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	5	0	-0.282
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	5	0	-0.043
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	6	0	-0.149
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	6	0	-0.574
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	6	0	-0.533
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	7	0	0.073
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	8	0	-1.134

TABLE IV. Proton-proton, neutron-neutron, and proton-neutron matrix elements (in MeV) derived for calculations in model space (II). They are antisymmetrized and normalized by a factor $1/\sqrt{(1+\delta_{ja_jb})(1+\delta_{jc_jd})}$.

$n_a l_a j_a$	$n_b l_b j_b$	$n_c l_c j_c$	$n_d l_d j_d$	J	T_z	TBME
0f _{7/2}	0f _{7/2}	0f _{7/2}	0f _{7/2}	0	1	-2.026
0f _{7/2}	0f _{7/2}	1p _{3/2}	1p _{3/2}	0	1	-1.225
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	0	1	-0.068
0f _{7/2}	0f _{7/2}	0f _{7/2}	0f _{7/2}	2	1	-0.416
0f _{7/2}	0f _{7/2}	0f _{7/2}	1p _{3/2}	2	1	-0.710
0f _{7/2}	0f _{7/2}	1p _{3/2}	1p _{3/2}	2	1	-0.358
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	2	1	-0.556
0f _{7/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	2	1	-0.361
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	2	1	0.104
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	3	1	0.329
0f _{7/2}	0f _{7/2}	0f _{7/2}	0f _{7/2}	4	1	0.133
0f _{7/2}	0f _{7/2}	0f _{7/2}	1p _{3/2}	4	1	-0.410
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	4	1	0.057
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	5	1	0.496
0f _{7/2}	0f _{7/2}	0f _{7/2}	0f _{7/2}	6	1	0.407
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	0	-1	-0.715
1p _{3/2}	1p _{3/2}	1p _{1/2}	1p _{1/2}	0	-1	-0.869
1p _{3/2}	1p _{3/2}	0f _{5/2}	0f _{5/2}	0	-1	-0.695
1p _{3/2}	1p _{3/2}	0g _{9/2}	0g _{9/2}	0	-1	1.026
1p _{3/2}	1p _{3/2}	1d _{5/2}	1d _{5/2}	0	-1	0.967
1p _{1/2}	1p _{1/2}	1p _{1/2}	1p _{1/2}	0	-1	-0.302
1p _{1/2}	1p _{1/2}	0f _{5/2}	0f _{5/2}	0	-1	-0.470
1p _{1/2}	1p _{1/2}	0g _{9/2}	0g _{9/2}	0	-1	0.846
1p _{1/2}	1p _{1/2}	1d _{5/2}	1d _{5/2}	0	-1	0.603
0f _{5/2}	0f _{5/2}	0f _{5/2}	0f _{5/2}	0	-1	-0.978
0f _{5/2}	0f _{5/2}	0g _{9/2}	0g _{9/2}	0	-1	1.555
0f _{5/2}	0f _{5/2}	1d _{5/2}	1d _{5/2}	0	-1	0.610
0g _{9/2}	0g _{9/2}	0g _{9/2}	0g _{9/2}	0	-1	-1.171
0g _{9/2}	0g _{9/2}	1d _{5/2}	1d _{5/2}	0	-1	-0.884
1d _{5/2}	1d _{5/2}	1d _{5/2}	1d _{5/2}	0	-1	-0.904
1p _{3/2}	1p _{1/2}	1p _{3/2}	1p _{1/2}	1	-1	0.165
1p _{3/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	1	-1	-0.053
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	1	-1	0.050
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	2	-1	-0.219
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{1/2}	2	-1	-0.372
1p _{3/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	2	-1	-0.158
1p _{3/2}	1p _{3/2}	1p _{1/2}	0f _{5/2}	2	-1	-0.163
1p _{3/2}	1p _{3/2}	0f _{5/2}	0f _{5/2}	2	-1	-0.168
1p _{3/2}	1p _{3/2}	0g _{9/2}	0g _{9/2}	2	-1	0.393
1p _{3/2}	1p _{3/2}	0g _{9/2}	1d _{5/2}	2	-1	0.340
1p _{3/2}	1p _{3/2}	1d _{5/2}	1d _{5/2}	2	-1	0.471
1p _{3/2}	1p _{1/2}	1p _{3/2}	1p _{1/2}	2	-1	-0.418
1p _{3/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	2	-1	-0.172
1p _{3/2}	1p _{1/2}	1p _{1/2}	0f _{5/2}	2	-1	-0.384
1p _{3/2}	1p _{1/2}	0f _{5/2}	0f _{5/2}	2	-1	-0.280
1p _{3/2}	1p _{1/2}	0g _{9/2}	0g _{9/2}	2	-1	0.271
1p _{3/2}	1p _{1/2}	0g _{9/2}	1d _{5/2}	2	-1	0.536
1p _{3/2}	1p _{1/2}	1d _{5/2}	1d _{5/2}	2	-1	0.207
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	2	-1	0.072
1p _{3/2}	0f _{5/2}	1p _{1/2}	0f _{5/2}	2	-1	-0.277
1p _{3/2}	0f _{5/2}	0f _{5/2}	0f _{5/2}	2	-1	-0.101
1p _{3/2}	0f _{5/2}	0g _{9/2}	0g _{9/2}	2	-1	0.475
1p _{3/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	2	-1	0.072
1p _{3/2}	0f _{5/2}	1d _{5/2}	1d _{5/2}	2	-1	0.089

TABLE IV. (Continued.)

TABLE IV. (Continued.)

$n_a l_a J_a$	$n_b l_b J_b$	$n_c l_c J_c$	$n_d l_d J_d$	J	T_z	TBME
1p _{1/2}	0f _{5/2}	1p _{1/2}	0f _{5/2}	2	-1	-0.277
1p _{1/2}	0f _{5/2}	0f _{5/2}	0f _{5/2}	2	-1	-0.273
1p _{1/2}	0f _{5/2}	0g _{9/2}	0g _{9/2}	2	-1	0.552
1p _{1/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	2	-1	0.526
1p _{1/2}	0f _{5/2}	1d _{5/2}	1d _{5/2}	2	-1	0.186
0f _{5/2}	0f _{5/2}	0f _{5/2}	0f _{5/2}	2	-1	-0.400
0f _{5/2}	0f _{5/2}	0g _{9/2}	0g _{9/2}	2	-1	0.229
0f _{5/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	2	-1	0.269
0f _{5/2}	0f _{5/2}	1d _{5/2}	1d _{5/2}	2	-1	0.138
0g _{9/2}	0g _{9/2}	0g _{9/2}	0g _{9/2}	2	-1	-0.756
0g _{9/2}	0g _{9/2}	0g _{9/2}	1d _{5/2}	2	-1	-0.377
0g _{9/2}	0g _{9/2}	1d _{5/2}	1d _{5/2}	2	-1	-0.347
0g _{9/2}	1d _{5/2}	0g _{9/2}	1d _{5/2}	2	-1	-0.774
0g _{9/2}	1d _{5/2}	1d _{5/2}	1d _{5/2}	2	-1	-0.361
1d _{5/2}	1d _{5/2}	1d _{5/2}	0f _{5/2}	2	-1	-0.275
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	3	-1	0.126
1p _{3/2}	0f _{5/2}	1p _{1/2}	0f _{5/2}	3	-1	-0.005
1p _{3/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	3	-1	0.069
1p _{1/2}	0f _{5/2}	1p _{1/2}	0f _{5/2}	3	-1	0.172
1p _{1/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	3	-1	0.125
0g _{9/2}	1d _{5/2}	0g _{9/2}	1d _{5/2}	3	-1	-0.138
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	4	-1	-0.326
1p _{3/2}	0f _{5/2}	0f _{5/2}	0f _{5/2}	4	-1	-0.244
1p _{3/2}	0f _{5/2}	0g _{9/2}	0g _{9/2}	4	-1	0.469
1p _{3/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	4	-1	0.350
1p _{3/2}	0f _{5/2}	1d _{5/2}	1d _{5/2}	4	-1	0.089
0f _{5/2}	0f _{5/2}	0f _{5/2}	0f _{5/2}	4	-1	-0.086
0f _{5/2}	0f _{5/2}	0g _{9/2}	0g _{9/2}	4	-1	0.109
0f _{5/2}	0f _{5/2}	0g _{9/2}	1d _{5/2}	4	-1	0.097
0f _{5/2}	0f _{5/2}	1d _{5/2}	1d _{5/2}	4	-1	0.089
0g _{9/2}	0g _{9/2}	0g _{9/2}	0g _{9/2}	4	-1	-0.273
0g _{9/2}	0g _{9/2}	0g _{9/2}	1d _{5/2}	4	-1	-0.357
0g _{9/2}	0g _{9/2}	1d _{5/2}	1d _{5/2}	4	-1	-0.156
0g _{9/2}	1d _{5/2}	0g _{9/2}	1d _{5/2}	4	-1	-0.229
0g _{9/2}	1d _{5/2}	1d _{5/2}	1d _{5/2}	4	-1	-0.204
1d _{5/2}	1d _{5/2}	1d _{5/2}	1d _{5/2}	4	-1	-0.072
0g _{9/2}	1d _{5/2}	0g _{9/2}	1d _{5/2}	5	-1	0.121
0g _{9/2}	0g _{9/2}	0g _{9/2}	0g _{9/2}	6	-1	-0.105
0g _{9/2}	0g _{9/2}	0g _{9/2}	1d _{5/2}	6	-1	-0.234
0g _{9/2}	1d _{5/2}	0g _{9/2}	1d _{5/2}	6	-1	-0.031
0g _{9/2}	1d _{5/2}	0g _{9/2}	1d _{5/2}	7	-1	0.127
0g _{9/2}	0g _{9/2}	0g _{9/2}	0g _{9/2}	8	-1	-0.001
0f _{5/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	0	-1	-0.497
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	1	-1	-0.765
1p _{3/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	1	-1	0.246
0f _{5/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	1	-1	-0.089
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	2	-1	-0.080
1p _{3/2}	1d _{5/2}	1p _{1/2}	1d _{5/2}	2	-1	-0.103
1p _{3/2}	1d _{5/2}	0f _{5/2}	0g _{9/2}	2	-1	-0.293
1p _{3/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	2	-1	0.032
1p _{1/2}	1d _{5/2}	1p _{1/2}	1d _{5/2}	2	-1	-0.072
1p _{1/2}	1d _{5/2}	0f _{5/2}	0g _{9/2}	2	-1	-0.348
1p _{1/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	2	-1	-0.123
0f _{5/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	2	-1	-0.382
0f _{5/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	2	-1	-0.216
0f _{5/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	2	-1	-0.057
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	3	-1	-0.497

$n_a l_a J_a$	$n_b l_b J_b$	$n_c l_c J_c$	$n_d l_d J_d$	J	T_z	TBME
1p _{3/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	3	-1	-0.337
1p _{3/2}	0g _{9/2}	1p _{1/2}	1d _{5/2}	3	-1	0.420
1p _{3/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	3	-1	0.199
1p _{3/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	3	-1	0.285
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	3	-1	-0.386
1p _{3/2}	1d _{5/2}	1p _{1/2}	1d _{5/2}	3	-1	0.315
1p _{3/2}	1d _{5/2}	0f _{5/2}	0g _{9/2}	3	-1	0.023
1p _{3/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	3	-1	0.182
1p _{1/2}	1d _{5/2}	1p _{1/2}	1d _{5/2}	3	-1	-0.416
1p _{1/2}	1d _{5/2}	0f _{5/2}	0g _{9/2}	3	-1	-0.274
1p _{1/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	3	-1	-0.240
0f _{5/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	3	-1	-0.194
0f _{5/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	3	-1	-0.300
0f _{5/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	3	-1	-0.014
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	4	-1	0.054
1p _{3/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	4	-1	-0.024
1p _{3/2}	0g _{9/2}	1p _{1/2}	0g _{9/2}	4	-1	-0.105
1p _{3/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	4	-1	0.151
1p _{3/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	4	-1	0.076
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	4	-1	0.257
1p _{3/2}	1d _{5/2}	1p _{1/2}	0g _{9/2}	4	-1	-0.035
1p _{3/2}	1d _{5/2}	0f _{5/2}	0g _{9/2}	4	-1	-0.128
1p _{3/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	4	-1	-0.018
1p _{1/2}	0g _{9/2}	1p _{1/2}	0g _{9/2}	4	-1	0.113
1p _{1/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	4	-1	-0.009
1p _{1/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	4	-1	0.022
0f _{5/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	4	-1	0.116
0f _{5/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	4	-1	-0.137
0f _{5/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	4	-1	0.027
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	5	-1	-0.075
1p _{3/2}	0g _{9/2}	1p _{1/2}	0g _{9/2}	5	-1	0.333
1p _{3/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	5	-1	0.136
1p _{3/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	5	-1	0.347
1p _{1/2}	0g _{9/2}	1p _{1/2}	0g _{9/2}	5	-1	-0.309
1p _{1/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	5	-1	-0.233
1p _{1/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	5	-1	-0.449
0f _{5/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	5	-1	-0.050
0f _{5/2}	0g _{9/2}	0f _{5/2}	1d _{5/2}	5	-1	-0.418
0f _{5/2}	1d _{5/2}	0f _{5/2}	1d _{5/2}	5	-1	-0.373
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	6	-1	0.267
1p _{3/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	6	-1	0.176
0f _{5/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	6	-1	0.158
0f _{5/2}	0g _{9/2}	0f _{5/2}	0g _{9/2}	7	-1	-0.719
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	0	0	-2.101
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	1	0	-2.000
0f _{7/2}	0f _{5/2}	1p _{3/2}	1p _{3/2}	1	0	0.804
0f _{7/2}	0f _{5/2}	1p _{3/2}	1p _{1/2}	1	0	-0.977
0f _{7/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	1	0	-0.680
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	1	0	-0.387
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{1/2}	1	0	0.618
1p _{3/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	1	0	-0.019
1p _{3/2}	1p _{1/2}	1p _{3/2}	1p _{1/2}	1	0	-0.742
1p _{3/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	1	0	-0.422
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	1	0	-1.036
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	2	0	-1.004
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	2	0	-0.748
0f _{7/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	2	0	-0.455

TABLE IV. (Continued.)

$n_a l_a j_a$	$n_b l_b j_b$	$n_c l_c j_c$	$n_d l_d j_d$	J	T_z	TBME
0f _{7/2}	1p _{3/2}	1p _{3/2}	1p _{1/2}	2	0	-0.801
0f _{7/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	2	0	-0.900
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	2	0	-1.422
0f _{7/2}	0f _{5/2}	1p _{3/2}	1p _{3/2}	2	0	-0.111
0f _{7/2}	0f _{5/2}	1p _{3/2}	1p _{1/2}	2	0	-0.648
0f _{7/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	2	0	-0.631
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	2	0	-0.555
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{1/2}	2	0	-0.699
1p _{3/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	2	0	-0.176
1p _{3/2}	1p _{1/2}	1p _{3/2}	1p _{1/2}	2	0	-1.104
1p _{3/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	2	0	-0.462
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	2	0	-0.457
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	3	0	-0.370
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{1/2}	3	0	0.603
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	3	0	0.144
0f _{7/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	3	0	-0.473
0f _{7/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	3	0	0.142
0f _{7/2}	1p _{1/2}	0f _{7/2}	1p _{1/2}	3	0	-0.628
0f _{7/2}	1p _{1/2}	0f _{7/2}	0f _{5/2}	3	0	-0.279
0f _{7/2}	1p _{1/2}	1p _{3/2}	1p _{3/2}	3	0	0.544
0f _{7/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	3	0	-0.119
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	3	0	-0.525
0f _{7/2}	0f _{5/2}	1p _{3/2}	1p _{3/2}	3	0	0.439
0f _{7/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	3	0	-0.369
1p _{3/2}	1p _{3/2}	1p _{3/2}	1p _{3/2}	3	0	-0.826
1p _{3/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	3	0	0.227
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	3	0	-0.258
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	4	0	-0.106
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{1/2}	4	0	-0.302
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	4	0	-0.229
0f _{7/2}	1p _{3/2}	1p _{3/2}	0f _{5/2}	4	0	-0.620
0f _{7/2}	1p _{1/2}	0f _{7/2}	1p _{1/2}	4	0	-0.593
0f _{7/2}	1p _{1/2}	0f _{7/2}	0f _{5/2}	4	0	-0.590
0f _{7/2}	1p _{1/2}	1p _{3/2}	0f _{5/2}	4	0	-1.006
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	4	0	-0.843
0f _{7/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	4	0	-0.782
1p _{3/2}	0f _{5/2}	1p _{3/2}	0f _{5/2}	4	0	-0.756
0f _{7/2}	1p _{3/2}	0f _{7/2}	1p _{3/2}	5	0	-0.916
0f _{7/2}	1p _{3/2}	0f _{7/2}	0f _{5/2}	5	0	0.282
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	5	0	-0.184
0f _{7/2}	0f _{5/2}	0f _{7/2}	0f _{5/2}	6	0	-1.570
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	1	0	-0.843
0f _{7/2}	0g _{9/2}	0f _{7/2}	1d _{5/2}	1	0	-0.191
0f _{7/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	1	0	-0.674
0f _{7/2}	1d _{5/2}	0f _{7/2}	1d _{5/2}	1	0	-0.636
0f _{7/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	1	0	-0.248
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	1	0	-0.847
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	2	0	-0.590
0f _{7/2}	0g _{9/2}	0f _{7/2}	1d _{5/2}	2	0	-0.454
0f _{7/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	2	0	-0.405
0f _{7/2}	1d _{5/2}	0f _{7/2}	1d _{5/2}	2	0	-0.443
0f _{7/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	2	0	-0.437
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	2	0	-0.488
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	3	0	-0.179
0f _{7/2}	0g _{9/2}	0f _{7/2}	1d _{5/2}	3	0	-0.229
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	3	0	-0.436
0f _{7/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	3	0	-0.218

TABLE IV. (Continued.)

$n_a l_a j_a$	$n_b l_b j_b$	$n_c l_c j_c$	$n_d l_d j_d$	J	T_z	TBME
0f _{7/2}	1d _{5/2}	0f _{7/2}	1d _{5/2}	3	0	-0.108
0f _{7/2}	1d _{5/2}	1p _{3/2}	0g _{9/2}	3	0	-0.211
0f _{7/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	3	0	-0.213
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	3	0	-0.772
1p _{3/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	3	0	-0.378
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	3	0	-0.250
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	4	0	-0.070
0f _{7/2}	0g _{9/2}	0f _{7/2}	1d _{5/2}	4	0	-0.351
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	4	0	-0.397
0f _{7/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	4	0	-0.357
0f _{7/2}	1d _{5/2}	0f _{7/2}	1d _{5/2}	4	0	-0.254
0f _{7/2}	1d _{5/2}	1p _{3/2}	0g _{9/2}	4	0	-0.329
0f _{7/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	4	0	-0.483
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	4	0	-0.190
1p _{3/2}	0g _{9/2}	1p _{3/2}	1d _{5/2}	4	0	-0.409
1p _{3/2}	1d _{5/2}	1p _{3/2}	1d _{5/2}	4	0	-0.770
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	5	0	-0.015
0f _{7/2}	0g _{9/2}	0f _{7/2}	1d _{5/2}	5	0	-0.147
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	5	0	-0.297
0f _{7/2}	1d _{5/2}	0f _{7/2}	1d _{5/2}	5	0	-0.029
0f _{7/2}	1d _{5/2}	1p _{3/2}	0g _{9/2}	5	0	-0.134
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	5	0	-0.069
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	6	0	-0.125
0f _{7/2}	0g _{9/2}	0f _{7/2}	1d _{5/2}	6	0	-0.447
0f _{7/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	6	0	-0.538
0f _{7/2}	1d _{5/2}	0f _{7/2}	1d _{5/2}	6	0	-0.742
0f _{7/2}	1d _{5/2}	1p _{3/2}	0g _{9/2}	6	0	-0.671
1p _{3/2}	0g _{9/2}	1p _{3/2}	0g _{9/2}	6	0	-0.479
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	7	0	0.063
0f _{7/2}	0g _{9/2}	0f _{7/2}	0g _{9/2}	8	0	-1.119

TABLE V. Proton effective charges of the electric quadrupole operator $E2$ for the model spaces (I) and (II).

$n_a l_a j_a$	$n_b l_b j_b$	$\langle a e_n b \rangle$ (I)	$\langle a e_n b \rangle$ (II)
0f _{7/2}	0f _{7/2}	1.22	1.23
0f _{7/2}	1p _{3/2}	1.34	1.36
1p _{3/2}	1p _{3/2}	1.40	1.42

TABLE VI. Neutron effective charges of the electric quadrupole operator $E2$ for the model spaces (I) and (II).

$n_a l_a j_a$	$n_b l_b j_b$	$\langle a e_n b \rangle$ (I)	$\langle a e_n b \rangle$ (II)
1p _{3/2}	1p _{3/2}	0.38	0.40
1p _{3/2}	1p _{1/2}	0.39	0.42
1p _{3/2}	0f _{5/2}	0.43	0.46
1p _{1/2}	0f _{5/2}	0.41	0.45
0f _{5/2}	0f _{5/2}	0.59	0.61
0g _{9/2}	0g _{9/2}	0.39	0.40
0g _{9/2}	1d _{5/2}		0.35
1d _{5/2}	1d _{5/2}		0.36

TABLE VII. Occupation numbers of proton $0f_{7/2}$ and neutron $0g_{9/2}, 1d_{5/2}$ of $^{56-62}\text{Ti}$, $^{58-64}\text{Cr}$, $^{60-66}\text{Fe}$, and $^{62-68}\text{Ni}$ calculated with model spaces (I) and (II) (see text for details).

	N = 34		N = 36		N = 38		N = 40	
	(I)	(II)	(I)	(II)	(I)	(II)	(I)	(II)

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