# Investigation of the thermonuclear ${}^{18}Ne(\alpha, p){}^{21}Na$ reaction rate via resonant elastic scattering of <sup>21</sup>Na + p

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The  ${}^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$  reaction is thought to be one of the key breakout reactions from the hot CNO cycles to the rp process in type I x-ray bursts. In this work, the resonant properties of the compound nucleus <sup>22</sup>Mg have been investigated by measuring the resonant elastic scattering of  ${}^{21}Na + p$ . An 89-MeV  ${}^{21}Na$  radioactive beam delivered from the CNS Radioactive Ion Beam Separator bombarded an 8.8 mg/cm<sup>2</sup> thick polyethylene (CH<sub>2</sub>)<sub>n</sub> target. The <sup>21</sup>Na beam intensity was about  $2 \times 10^5$  pps, with a purity of about 70% on target. The recoiled protons were measured at the center-of-mass scattering angles of  $\theta_{c.m.} \approx 175.2^{\circ}$ ,  $152.2^{\circ}$ , and  $150.5^{\circ}$  by three sets of  $\Delta E$ -E telescopes, respectively. The excitation function was obtained with the thick-target method over energies  $E_x$  (<sup>22</sup>Mg) = 5.5–9.2 MeV. In total, 23 states above the proton-threshold in <sup>22</sup>Mg were observed, and their resonant parameters were determined via an *R*-matrix analysis of the excitation functions. We have made several new  $J^{\pi}$  assignments and confirmed some tentative assignments made in previous work. The thermonuclear <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate has been recalculated based on our recommended spin-parity assignments. The astrophysical impact of our new rate has been investigated through one-zone postprocessing x-ray burst calculations. We find that the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate significantly affects the peak nuclear energy generation rate, reaction fluxes, and onset temperature of this breakout reaction in these astrophysical phenomena.

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# I. INTRODUCTION

Explosive hydrogen and helium burning are thought to be the main source of energy generation and nuclear trajectory to higher mass on the proton-rich side of the nuclear chart in type I x-ray bursts (XRBs) [1-5]. XRBs are characterized by a sudden increase of x-ray emission within only a few seconds to a total energy output of about  $10^{40}$  ergs, which is observed to repeat with some regularity. The recurrence time for single bursts can range from hours to days at the typical temperature of 0.4-2 GK. The bursts have been interpreted as being generated by thermonuclear runaway on the surface of a neutron star that accretes H- and He-rich material from a less evolved companion star in a close binary system. In XRBs, the hydrogen burning initially occurs via the hot CNO cycle (HCNO):

<sup>12</sup>C(
$$p,\gamma$$
)<sup>13</sup>N( $p,\gamma$ )<sup>14</sup>O( $e^+\nu$ )<sup>14</sup>N( $p,\gamma$ )<sup>15</sup>O( $e^+\nu$ )  
<sup>15</sup>N( $p,\alpha$ )<sup>12</sup>C,

while the <sup>13</sup>N( $e^+\nu$ )<sup>13</sup>C  $\beta$  decay in the CNO cycle is bypassed by the <sup>13</sup>N( $p,\gamma$ )<sup>14</sup>O reaction. The temperature of the accretion envelope increases as the compressing and exothermic nuclear reactions going on. When the temperature reaches about 0.4 GK, the second HCNO cycle becomes dominant:

<sup>12</sup>C(
$$p,\gamma$$
)<sup>13</sup>N( $p,\gamma$ )<sup>14</sup>O( $\alpha,p$ )<sup>17</sup>F( $p,\gamma$ )<sup>18</sup>Ne( $e^+\nu$ )<sup>18</sup>F( $p,\alpha$ )  
<sup>15</sup>O( $e^+\nu$ )<sup>15</sup>N( $p,\alpha$ )<sup>12</sup>C.

It was predicted [1,2] that the <sup>18</sup>Ne waiting point nucleus in the second HCNO cycle could be bypassed by the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction at  $T \approx 0.6$  GK, and subsequently, the reaction chain breaks out, eventually leading to the rp process [6–8].

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However, over stellar temperatures achieved in XRBs, this rate has not been sufficiently well determined.

The thermonuclear  ${}^{18}\text{Ne}(\alpha,p){}^{21}\text{Na}$  rate is thought to be dominated by contributions from resonances in the compound nucleus <sup>22</sup>Mg above the  $\alpha$  threshold at  $Q_{\alpha} = 8.142$  MeV [9]. As for XRBs, the temperature region of interest is about 0.4-2.0 GK, corresponding to an excitation region of  $E_x = 8.6-11.0$  MeV in <sup>22</sup>Mg. Görres *et al.* made the first estimate [10] of this rate with rather limited experimental level-structure information in <sup>22</sup>Mg. The energies for the <sup>22</sup>Mg resonances were estimated simply by shifting those of known natural-parity states in the mirror <sup>22</sup>Ne by a fixed amount (about 200 keV). The uncertainty of this first rate was mainly caused by the errors in resonant energies (or excitation energies) and resonant strengths of the excited states above the  $\alpha$  threshold in <sup>22</sup>Mg. After that, the precise locations of the excited states in <sup>22</sup>Mg were studied extensively by many transfer reaction experiments. For example, Chen et al. [11] determined the excitation energies with a typical uncertainty of 20-30 keV in a <sup>12</sup>C(<sup>16</sup>O,<sup>6</sup>He)<sup>22</sup>Mg experiment. However, the spin-parity assignments assumed and the spectroscopic  $S_{\alpha}$  factors adopted following the idea of Görres *et al.* were still uncertain. Caggiano et al. [12] and Berg et al. [13] measured the excitation energies with better precision (about 10-20 keV), but no spin-parity assignment was given. Later, Matic et al. [14] measured the excitation energies precisely by a  ${}^{24}Mg(p,t){}^{22}Mg$  experiment, with uncertainty of about 1–15 keV achieved for most states above the  $\alpha$  threshold; the spin-parity assignments were tentatively made based on the shell-model calculation or those of mirror states in <sup>22</sup>Ne. Thus, the thermonuclear  ${}^{18}\text{Ne}(\alpha, p){}^{21}\text{Na}$  rate was constrained very well in the resonant energy aspect. In a later  ${}^{24}Mg(p,t){}^{22}Mg$ measurement, Chae et al. [15] observed six excited states in <sup>22</sup>Mg above the  $\alpha$  threshold, and some spin-parity assignments were made via an angular distribution measurement. However, the insufficient resolution of their measurement at the centerof-mass (c.m.) scattering angles of  $\theta_{c.m.}$  above 20° made such  $J^{\pi}$  assignments questionable [14] (e.g., the 8.495-MeV peak was contaminated by the nearby 8.572- and 8.658-MeV states as shown in their Fig. 3). In our previous experiment of  $^{21}$ Na + p resonant elastic scattering [16,17], new spin-parity assignments were made only tentatively for the 8.547and 8.614-MeV states in <sup>22</sup>Mg due to low statistics. Those assignments gave a quite different rate for the  ${}^{18}\text{Ne}(\alpha, p){}^{21}\text{Na}$ reaction compared to the rate estimated in Chen et al. work [11]. Such tentative assignments clearly motivate further investigation.

A comparison of all available reaction rates of  ${}^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$  shows discrepancies of up to several orders of magnitude around  $T \sim 1$  GK [14]. So far, more than 40 levels (up to  $E_x = 13.01$  MeV) have been observed above the  $\alpha$  threshold in  ${}^{22}\text{Mg}$ . Such high level density suggests that a statistical model approach might provide a reliable estimate of the rate. However, only natural-parity states in  ${}^{22}\text{Mg}$  can be populated by the  ${}^{18}\text{Ne} + \alpha$  channel, and thus the effective level density will be considerably lower. It remains unclear whether the statistical-model calculations provide a reliable rate estimation in a wide temperature region [14]. There are still many resonances (above the  $\alpha$  threshold) without

firm spin-parity assignments, which need to be determined experimentally. As a consequence, the accuracy of the current <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction rate is mainly limited by the lack of experimental spin parities and  $\alpha$  partial widths  $\Gamma_{\alpha}$  (or spectroscopic factors  $S_{\alpha}$ ) of the resonances in <sup>22</sup>Mg above the  $\alpha$  threshold.

So far, only two direct measurements [18,19] for the <sup>18</sup>Ne $(\alpha, p)^{21}$ Na reaction were reported. The lowest energies achieved in these studies ( $E_{c.m.} = 2.0$  and 1.7 MeV) are still too high compared with the energy region  $E_{\rm c.m.} \leq$ 1.5 MeV of interest for HCNO breakout in XRBs. New results [20] have recently become available, which determined the <sup>18</sup>Ne( $\alpha$ ,  $p_0$ )<sup>21</sup>Na cross sections in the energy region of  $E_{\rm c.m.} = 1.19-2.57$  MeV by measuring those of the timereversal reaction  ${}^{21}$ Na $(p,\alpha)^{18}$ Ne in inverse kinematics. In addition, similar experiments were performed at the Argonne National Laboratory (ANL), but the results were only reported in the ANL annual reports [21]. The ANL cross-sectional data are consistent with those in Ref. [20]. Nonetheless, these results are still insufficient for a reliable rate calculation at all temperatures encountered within XRBs. Recently, a new reaction rate was recommended based on the combined analysis of all literature data [22].

In this work, the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate is determined via the measurement of the resonant elastic scattering of  ${}^{21}Na + p$ . This is an entirely new high-statistics experiment compared to the previous one [16,17]. In the resonant elastic-scattering mechanism, <sup>22</sup>Mg is formed via the fusion of  ${}^{21}Na + p$  as an excited compound nucleus, whose states promptly decay back into  ${}^{21}Na + p$ . This process interferes with Coulomb scattering resulting in a characteristic resonance pattern in the excitation function [23]. With this approach, the excitation function was obtained simultaneously in a wide range of 5.5-9.2 MeV in <sup>22</sup>Mg with a well-established thick-target method [24-26]. In total, 23 states above the proton threshold in <sup>22</sup>Mg were observed, and their resonant parameters were determined via an R-matrix analysis of the experimental data. Part of the experimental results previously reported in Ref. [27] is revisited through a more detailed analysis. The detailed experimental results presented here supersede those of Ref. [27].

#### **II. EXPERIMENT**

The experiment was carried out at the CNS Radioactive Ion Beam separator (CRIB) [28,29], installed by the Center for Nuclear Study (CNS), University of Tokyo, in the RIKEN Nishina Center. During the past decade, the radioactive ion beams (RIBs) produced at CRIB have been successfully utilized in the resonant scattering experiments with a thicktarget method [17,30–33], which proved to be a successful technique as adopted in the present study. A schematic view of CRIB and the measurement setup are shown in Fig. 1. An 8.2-MeV/nucleon primary beam of <sup>20</sup>Ne<sup>8+</sup> was accelerated by an AVF cyclotron (K = 79) at RIKEN, with an average intensity of 65 pnA. At the primary focal plane (F0), the beam bombarded a liquid-nitrogen-cooled  $D_2$  gas target (90 K) [34]. The gas was confined in a cylindrical chamber (length = 80 mm,  $\phi = 20$  mm) whose entrance and exit windows were



FIG. 1. (Color online) Schematic view of CRIB utilized for the <sup>21</sup>Na beam production. The experimental setup for measurement of the <sup>21</sup>Na + p scattering was installed in the chamber at F3.

each made of 2.5- $\mu$ m-thick Havar foils. The effective thickness of  $D_2$  gas was about 2.86 mg/cm<sup>2</sup> at a pressure of about 530 Torr. The <sup>21</sup>Na beam was produced via the <sup>20</sup>Ne(d,n)<sup>21</sup>Na reaction in inverse kinematics and separated subsequently by two dipoles. At the momentum-dispersive focal plane (F1), a slit of ±5 mm was installed to remove the contaminations from the secondary beam. This slit restricted the <sup>21</sup>Na<sup>11+</sup> particles at a mean energy of 5.9 MeV/nucleon with a momentum spread of ±0.3%. The Wien filter was operated at a high voltage of ±70 kV to further purify the <sup>21</sup>Na beam, which was about 70% on the secondary target.

The setup in a scattering chamber at the experimental focal plane (F3) consisted of two parallel-plate avalanche counters (PPACs) [35], an 8.8 mg/cm<sup>2</sup> thick polyethylene  $(CH_2)_n$  target, and three sets of  $\Delta E$ -E silicon telescopes. The PPACs measured the timing and two-dimensional position information of the incoming beam and determined the beam position on the secondary target during the measurement. The beam identification plot is shown in Fig. 2. It shows that the beam particles were clearly identified in an event-by-event mode. Here, TOF is the time of flight between PPACa and the RF signal from the cyclotron, which is equivalent to the beam flight time from F0 to F3. The beam position on the target (i.e.,  $X_{target}$  in Fig. 2) was determined by the hitting



FIG. 2. (Color online) Three-dimensional (3D) contour plot for the beam particles identification. See text for details.

positions on the two PPACs. The beam impinged on an 8.8 mg/cm<sup>2</sup> polyethylene  $(CH_2)_n$  target, which was thick enough to stop all the beam ions. Here, the energy of <sup>21</sup>Na beam was 89.4 MeV with spread of 1.95 MeV (FWHM) on the target. The beam-spot widths (FWHM) were 9.5 mm in horizontal and 4.8 mm in vertical directions. The horizontal and vertical angular spreads (FWHM) were 10 and 22 mrad, respectively. The averaged intensity of <sup>21</sup>Na beam was about  $2 \times 10^5$  pps on the target.

The recoiled light particles were detected with three  $\Delta E \cdot E$ silicon telescopes at laboratory angles of  $\theta_{Si}^{lab} \approx 0^{\circ}$  (hereafter referred to as "set 1"),  $+14^{\circ}$  ("set 2"), and  $-14^{\circ}$  ("set 3") with respect to the beam line, respectively. These silicon detectors were produced by Micron Semiconductor Inc. [36]. Each telescope subtended an opening angle of about  $10^{\circ}$  with a solid angle of about 27 msr in the laboratory frame. In the c.m. frame for elastic scattering, the averaged scattering angles of the telescopes correspond to  $\theta_{c.m.} \approx 175.2^{\circ}$  (set 1), 152.2° (set 2), and 150.5° (set 3), respectively.  $\Delta E$  is the positionsensitive double-sided-strip (16×16 strips, 3 mm width of each strip) detector, which measured the energy, position, and timing signals of the light particles. The pad E detectors (1.5 mm thick) measured their residual energies. This allowed for the clear identification of recoiled particles as shown in Fig. 3. The high-energy particles penetrating through  $\Delta E$ can be identified by the  $\Delta E - E$  method [see Fig. 3(a)]; the low-energy particles fully stopped in  $\Delta E$  can be identified by the TOF-E method [see Fig. 3(b)], where TOF is the time of flight between PPACb and  $\Delta E$ . In this work, the energy calibration for the Si detectors was carried out by using secondary proton beams produced with CRIB and a standard triple- $\alpha$  source.

Experimental data with a C target  $(13.5 \text{ mg/cm}^2)$  was also acquired in a separate run to evaluate the contributions from the reactions of <sup>21</sup>Na with C nuclei. The yield ratio of these two proton spectra [with (CH<sub>2</sub>)<sub>n</sub> and C targets] was normalized by the number of beam particles and by the target thickness per unit beam energy loss in the corresponding targets [17,32].

## **III. RESULTS**

For inverse kinematics, the center-of-mass energy  $E_{c.m.}$  of the <sup>21</sup>Na + p system is related to the energy  $E_p$  of the recoiling protons detected at a laboratory angle  $\theta_{lab}$  by [32]

$$E_{\rm c.m.} = \frac{A_p + A_t}{4A_p \cos^2 \theta_{\rm lab}} E_p, \tag{1}$$

where  $A_p$  and  $A_t$  are the mass numbers of the projectile and target nuclei; this equation is valid only for an elastic scattering case. In practice,  $E_p$  was converted to  $E_{\text{c.m.}}$  by assuming the elastic scattering kinetics and considering the energy loss of particles in the target. A sample proton spectrum from the  $(CH_2)_n$  target runs obtained at the scattering of  $\theta_{\text{c.m.}} \approx 175.2^\circ$ (set 1) is shown in Fig. 4. The proton spectrum with a 13.5 mg/cm<sup>2</sup> C target (C spectrum) is also shown for comparison. The C spectra can be described using smooth curves with respect to the energy in all three telescopes. These C spectra were normalized to the corresponding proton spectra with the  $(CH_2)_n$  target using the number of beam particles and



FIG. 3. (Color online) Particle identification by (a)  $\Delta E$ -E method and (b) TOF-E method.  $\Delta E$  and E signals are measured by the silicon telescopes, and TOF is the time of flight between PPACb and  $\Delta E$ . See text for details.

the number of C atoms per unit energy loss of the beam. The normalized yield in a C spectrum was about 1/6 (at maximum) of that in the  $(CH_2)_n$  spectrum (see Fig. 4).

The laboratory differential cross section  $(d\sigma/d\Omega)$  for <sup>21</sup>Na + *p* scattering with energy  $E_p$  and angle  $\theta_{lab}$  is deduced [32] through the proton spectrum by

$$\frac{d\sigma}{d\Omega_{\rm lab}}(E_p,\theta_{\rm lab}) = \frac{N}{I_0 N_s \Delta\Omega_{\rm lab}},\tag{2}$$

where N is the number of detected protons, i.e., at energy interval of  $E_p \rightarrow E_p + \Delta E$  and scattering angle of  $\theta_{lab}$ , which are measured by a Si telescope covering a solid angle  $\Delta \Omega_{lab}$ .  $I_0$  is the total number of <sup>21</sup>Na beam particles that bombarded the (CH<sub>2</sub>)<sub>n</sub> target and is considered to be constant in the whole energy region.  $N_s$  is the number of H atoms per unit area per



FIG. 4. Reconstructed proton spectrum for the <sup>21</sup>Na + p elastic scattering taken at  $\theta_{c.m.} \approx 175.2^{\circ}$  (set 1). The abscissa is scaled to the excitation energy in <sup>22</sup>Mg. The normalized carbon background spectrum is also shown for comparison.

energy bin in the target (dx/dE) [37]. The transformation of the laboratory differential cross sections to the c.m. frame is given by

$$\frac{d\sigma}{d\Omega_{\rm c.m.}}(E_{\rm c.m.},\theta_{\rm c.m.}) = \frac{1}{4\cos\theta_{\rm lab}}\frac{d\sigma}{d\Omega_{\rm lab}}(E_p,\theta_{\rm lab}).$$
 (3)

Figure 5 shows the c.m. differential cross sections for the resonant elastic scattering of  ${}^{21}Na + p$  measured at angles of  $\theta_{c.m.} \approx 175.2^{\circ}$  (set 1), 152.2° (set 2), and 150.5° (set 3), respectively. The dead-layer region shown in sets 1 and 2 is different from that in set 3, simply because the thickness of  $\Delta E1$  and 2 (300  $\mu$ m) is different from that of  $\Delta E3$ (65  $\mu$ m). The fitting in the dead-layer region (between  $\Delta E$ and E detectors) is not reliable and removed from the figure. The abscissa is scaled by the excitation energies in <sup>22</sup>Mg, which are calculated by  $E_x = E_{c.m.} + Q_p$ . As such, a value of  $Q_p = 5.504$  MeV is adopted based on the updated masses of <sup>21</sup>Na and <sup>22</sup>Mg [9,38]. Here, the energy resolution of  $E_{c.m.}$ was determined by the resolution of the silicon detection system, the angular resolution of the scattering angle, as well as the energy width of the secondary beam and the particle straggling in the target material. Thereinto, the detector energy resolution dominates the total energy resolution of  $E_{c.m.}$  in three telescopes. Based on a Monte Carlo simulation, the overall energy resolution (FWHM) of  $E_{c.m.}$  in set 1 was estimated to be  $\sim$  30 keV, while those in sets 2 and 3 were about 30–70 keV (over  $E_{c.m.} = 0.5-4$  MeV) because of the larger scattering angle resulting in the larger kinematics shifts. The error of the deduced cross section is estimated to be 6%, which mainly arises from the statistical error of the proton yields and that of the target thickness. The deduced excitation energies in <sup>22</sup>Mg indicated on Fig. 5 are calculated by  $E_x = E_R + Q_p$ , with resonance energy  $E_R$  determined by the *R*-matrix analysis as discussed below. The present excitation energies agree with those adopted by Matic et al. within the uncertainties (see discussion below).



FIG. 5. (Color online) The c.m. differential cross sections for the resonant elastic scattering of  ${}^{21}$ Na + p measured by three sets of telescopes at different angles. The most probable *R*-matrix fitting results are shown. The data within the dead-layer region (between  $\Delta E$  and *E* detectors) were removed. See text for details.

The center-of-mass (c.m.) differential cross-sectional data have been analyzed by a multichannel *R*-matrix [39] code MULTI [40]. The overall *R*-matrix fits are shown in Fig. 5. A channel radius of  $R_n = 1.35(1 + 21^{\frac{1}{3}})$  fm [10,11] was adopted in the calculation. All possible *R*-matrix attempts were restricted to  $\ell \leq 4$ , since resonances of higher  $\ell$  transfer are invisible within the present resolution. Here, it is worth mentioning that the experimental data at sets 2 and 3 also support the  $J^{\pi}$  assignments made for set 1, although the following figures shown below are the *R*-matrix fits on the set 1 data. The parameters for the resonances in <sup>22</sup>Mg deduced from the present *R*-matrix analysis (set 1) are summarized in Table I. The excitation energies and spin parities deduced from this work are compared to the previous ones in Tables II and III. In the following *R*-matrix fitting figures, the solid

TABLE I. Resonant parameters used in the present *R*-matrix analysis.

$E_x$ ( <sup>22</sup> Mg)	$J^{\pi}$	S	l	$\Gamma_p$ (keV)
6.333	$1^{+}$	1	0	16
6.591	1-	2	1	36
6.615	$2^{+}$	2	0	10
6.796	$2^{-}$	1	1	62
6.885	1-	2	3	2
7.270	1-	2	1	82
7.339	$2^{+}$	2	2	18
7.369	3-	2	3	7
7.585	$2^{+}$	2	0	16
7.654	1-	2	1	114
7.802	$2^{-}$	1	1	19
7.920	$2^{+}$	2	0	3
8.005	3-	2	3	1
8.190	$2^{+}$	2	2	5
8.353	$1^{+}$	1	2	97
8.527	3-	2	1	3
8.578	$4^{+}$	2	2	5
8.677	$2^{+}$	2	2	7
8.727	$2^{+}$	2	0	12
8.827	1-	2	1	57
8.922	$2^{+}$	2	2	4
9.050	1-	2	1	105
9.158	4+	2	2	2

lines are the best fits with the parameters listed in Table I. The details of the R-matrix analysis are discussed in the following subsections.

#### 1. Levels below the $\alpha$ threshold

Four states observed at 6.333, 6.591, 6.615, and 6.796 MeV were well studied before [23] and had been assigned as  $1^+$ ,  $1^-$ ,  $2^+$ , and  $2^-$ , respectively. As shown in Fig. 5, the resonant shape of these states has been successfully reproduced by using the previous parameters determined in Ref. [23], and hence the previous  $J^{\pi}$  assignments are confirmed. Such agreement provides confidence in the present analysis.

The observed 6.885-MeV state is closest to the 6.876-MeV state in Ref. [14] and the 6.885-MeV state in Ref. [23]. Ruiz *et al.* [23] regarded it as a very weak state and excluded it from their *R*-matrix fitting. The present *R*-matrix fits for this state are shown in Fig. 6(a). This weakly populated state ( $\Gamma_p \approx 2 \text{ keV}$ ) can be fitted reasonably by 1<sup>-</sup>, 2<sup>+</sup>, and 3<sup>-</sup>, but with 1<sup>-</sup> being the most preferred assignment suggested by Matic *et al.* 

Matic *et al.* observed four states at 7.027, 7.045, 7.060, and 7.079 MeV. In the present experiment, these states are located over the dead-layer region of sets 1 and 2 in which the data are not reliable for the *R*-matrix analysis. In set 3, the energy resolution achieved is not able to resolve these four states. Therefore, these states are excluded from the present *R*-matrix analysis.

The 7.270-MeV state was tentatively assigned as  $J^{\pi} = (0^+, 1^+, 2^+)$  before [14,17]. By varying the channel spins,  $\ell$  values,

of these assignments can reproduce the experimental data well. The present *R*-matrix analysis supports a  $1^{-}$  assignment for this state [see Fig. 6(b)].

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 $(^{3}\text{He}, ^{6}\text{He})$  [12]

6.329 (4+)

 $6.771(3^{-})$ 

6.616

6.878

We have confirmed the existence of the 7.339-MeV state first identified by Matic *et al.* Figure 6(c) shows the contrast of fittings with and without this state. Thus, the tentative  $2^+$  assignment by Matic *et al.* is confirmed here

The observed 7.369-MeV state is closest to the Matic et al. 7.389-MeV (3<sup>-</sup>) state. It can be assigned as  $J^{\pi} = (3^{-}, 2^{+})$ , where  $3^{-}$  is preferred, as shown in Fig. 6(d). In addition, there is no  $2^+$  state around this region in the mirror <sup>22</sup>Ne (see Fig. 7), and hence  $J^{\pi} = 3^{-}$  is assigned to this state.

Previously there had been five states observed in the excitation energy range of 7.5-8.1 MeV, at energies of 7.601, 7.674, 7.742, 7.921, and 8.005 MeV [14]. Our data can be fitted with the resonances at corresponding energies of 7.585, 7.654, 7.802, 7.920, and 8.005 MeV, respectively. It is found that three resonances at 7.585, 7.920, and 8.005 MeV can be fitted with  $2^+$ ,  $2^+$ , and  $3^-$ , the same assignments as suggested by Matic et al., while the other two resonances at 7.654 and 7.802 MeV can be preferentially fitted by  $1^{-}$  [see Fig. 8(a)] and 2<sup>-</sup> [see Fig. 8(b)].

# 2. Levels above the $\alpha$ threshold

The <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction rate is determined by the <sup>22</sup>Mg levels above the  $\alpha$  threshold. The excitation energies of these levels were very well studied before (see Ref. [14] and references therein), but their spin parities were still poorly known. In the present experiment, ten resonances above the  $\alpha$ threshold were observed and analyzed by the *R*-matrix code. We have experimentally confirmed the  $J^{\pi}$  values tentatively assigned by Matic et al. for seven states at 8.180, 8.519, 8.572, 8.785, 8.933, 9.082, and 9.157 MeV, and assigned new  $J^{\pi}$ values for three states at 8.383, 8.658, and 8.743 MeV. The resonant parameters for calculating the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate are summarized in Table III. The present  $J^{\pi}$  assignments are discussed in detail below.

The observed 8.190-MeV state corresponds to the  $2^+$  state observed at 8.180 MeV by Matic *et al*. The  $J^{\pi} = (1^+ - 3^+)$ assignments were suggested to the 8.18-MeV state by the Rmatrix analysis of the previous  ${}^{21}Na + p$  data [17]. Here, this state is still able to be fitted by  $J^{\pi} = (1^+ - 3^+)$ . We simply adopt the  $2^+$  assignment suggested by Matic *et al.* Anyway, its contribution to the total rate is negligible (see Table IV).

The observed 8.353-MeV state was assigned as  $J^{\pi} =$  $(1^+-3^+)$  in the previous <sup>21</sup>Na + p experiment [17], where  $1^+$  was suggested to be the most probable assignment. That

Present work	Matic <i>et al.</i> ( <i>p</i> , <i>t</i> ) [14]	Caggiano <i>et al.</i> ( <sup>3</sup> He, <sup>6</sup> He) [12]	Chen <i>et al.</i> ( <sup>16</sup> O, <sup>6</sup> He) [11]	Chae <i>et al</i> . ( <i>p</i> , <i>t</i> ) [15]	Berg <i>et al.</i> ( <sup>4</sup> He, <sup>6</sup> He) [13]	He <i>et al</i> . ${}^{21}$ Na + <i>p</i> [17]
8.190 (2 <sup>+</sup> )	8.1803 (2+)	8.229	8.203		8.197	8.18 (1+-3+)
8.353 (1+)	8.383 (2+)	8.934	8.396		8.380	8.31 (1+-3+)
8.527 (3-)	8.519 (3-)	8.487	8.547 (2+)	8.495 (2+)	8.512	8.51 (3 <sup>-</sup> )
8.578 (4+)	8.572 (4+)	8.598				
$8.677(2^+)$	8.6575 (0+)		8.613 (3-)		8.644	$8.61(2^+)$
8.727 (2+)	8.743 (4+)		8.754 (4+)			
8.827 (1-)	8.7845 (1-)	8.789			8.771	
8.922 (2+)	8.9331 (2+)		8.925 (3-)		8.921	
9.050 (1-)	9.082 (1-)		9.066		9.029	
9.158 (4+)	9.157 (4+)		9.172		9.154	

TABLE III. Excitation energies and spin parities of levels above the  $\alpha$  threshold in <sup>22</sup>Mg.

He et al.

 $^{21}$ Na + *p* [17]

6.61 2+

6.81 (1+,2+) 6.93 (2+,3-)

 $7.27(2^+,1^+)$ 

7.42 (1,2+)

7.82 (2-) 7.98 (2+)

7.59 (1+,2+)

Ruiz et al.

 $^{21}$ Na + *p* [23]

6.796 (1-,2-)

6.333 1+

6.591 1-

6.615 2+

6.885

Chen et al.

(<sup>16</sup>O,<sup>6</sup>He) [11]

6.606

6.767 (3-)

6.889 (3-)

TABLE II. Excitation energies and spin parities of levels below the  $\alpha$  threshold in <sup>22</sup>Mg.

Chae et al.

(*p*,*t*) [15]

Berg et al.

(<sup>4</sup>He,<sup>6</sup>He) [13]

6.606

6.766

Matic et al.

(*p*,*t*) [14]

6.306 (3+)

6.578 (1-)

6.602 (2+)

6.7688 (0+)

6.8760 (1-)

Present

 $^{21}$ Na + p

6.333 1+

6.591 1-

6.615 2+

6.796 2-

 $6.885(1^{-})$ 



FIG. 6. (Color online) *R*-matrix fits for states below the  $\alpha$  threshold in <sup>22</sup>Mg.

assignment was only tentative due to the poor statistics. This state is close to the 8.383-MeV state observed by Matic *et al.*, who suggested a  $2^+$  assignment by referring to the mirror state in  $^{22}$ Ne. In the present *R*-matrix fit,  $1^+$  is the best candidate as shown in Fig. 9. Furthermore, this state was only weakly populated in the transfer-reaction experiments [11,13,14], which preferentially populated the natural-parity states in  $^{22}$ Mg. This again supports our unnatural-parity  $1^+$  assignment



FIG. 7. Mirror assignments for the <sup>22</sup>Mg levels above the proton threshold. The adopted values (energies and  $J^{\pi}$ s) are mainly taken from Ref. [14]. The new  $J^{\pi}$  values assigned in this work are marked by an asterisk (\*), while those assigned in Ref. [23] and Ref. [15] are marked by the # and \$ symbols, respectively. The structure data for the mirror <sup>22</sup>Ne are adopted from Ref. [41].

for this state. Therefore, this state does not contribute to the  ${}^{18}\text{Ne}(\alpha, p){}^{21}\text{Na}$  reaction rate.

The observed 8.527-MeV state is close to the  $3^-$  state at 8.519 MeV by Matic *et al.* and at 8.51 MeV by He *et al.* [17]. It is also close to the  $2^+$  state observed at 8.547 MeV by Chen



FIG. 8. (Color online) *R*-matrix fits for states below the  $\alpha$  threshold in <sup>22</sup>Mg.

*et al.* and at 8.495 MeV by Chae *et al.* In this work, both  $3^-$  and  $2^+$  can fit the experimental data as shown in Fig. 10(a). In addition, the mirror  $2^+$  assignment made by Chen *et al.* might be questionable; Chae *et al.* could not well resolve the triplet at 8.459, 8.578, and 8.667 MeV, and hence their  $2^+$  assignment is questionable as well. Especially, there is no  $2^+$  state in the mirror  $^{22}$ Ne around this region. Here, we assign the 8.527-MeV state as  $J^{\pi} = 3^-$ .

The observed 8.578-MeV state is closest to the 8.572-MeV state of Matic *et al.* in which it was assigned as  $4^+$  based on the shell model calculation. As shown in Fig. 10(b), both  $4^+$  and  $2^+$  can fit our data very well. As such, our data support the previous  $4^+$  assignment.

The observed 8.677-MeV state corresponds to the 8.658-MeV state of Matic *et al.*, which was assigned as a  $J^{\pi} = 0^+$  based on the shell model calculation. However, such a prediction is questionable because of the high level density at such a high excitation energy region. Matic *et al.* regarded this state as the 8.613-MeV state observed by Chen *et al.*, who assumed a 3<sup>-</sup> by simply shifting the energy of the mirror 8.741-MeV state in <sup>22</sup>Ne by about 130 keV. In addition, a 2<sup>+</sup> was tentatively assigned to the 8.61-MeV state in the previous low-statistics experiment [17]. As shown in Fig. 10(c), the present experiment strongly prefers the 2<sup>+</sup> assignment.

The observed 8.727-MeV state is regarded as the 8.743-MeV state of Matic *et al.* and the 8.754-MeV state of Chen *et al.* Both of them gave a  $4^+$  assignment and considered it the mirror 8.976-MeV state in <sup>22</sup>Ne. The present *R*-matrix analysis, however, suggests a  $2^+$  for this state [see Fig. 10(d)], the mirror of the 9.045-MeV state in <sup>22</sup>Ne (see Fig. 7).

The observed 8.827-MeV state is close to the 8.785-MeV state of Matic *et al.*, who gave a tentatively  $1^-$  assignment to this state. We have tried all possible spin parities and verified very well the  $1^-$  assignment as shown in Fig. 10(e).

The spin parity for the observed 8.922-MeV state was simply assumed to be  $2^+$  by Matic *et al.* and  $3^-$  by Chen *et al.*, respectively. In this work, both  $1^+$  and  $2^+$  can reproduce the data well, as shown in Fig. 10(f), where fittings with three possible  $J^{\pi}$ s are shown. Thus, we suggest this state is a  $2^+$ .

The observed 9.050- and 9.158-MeV states correspond to the 9.082- and 9.157-MeV states of Matic *et al.*, who gave the 1<sup>-</sup>, 4<sup>+</sup> tentative assignments, respectively. The previous tentative 1<sup>-</sup> assignment for the 9.050-MeV state is confirmed as shown in Fig. 10(g). For the 9.158-MeV state, both 2<sup>+</sup> and 4<sup>+</sup> can fit the experimental data as shown in Fig. 10(h). Based on the discussion made by Matic *et al.*, 4<sup>+</sup> is thus adopted for the 9.158-MeV state.

For the states assigned the same  $J^{\pi}$  values as in Ref. [14], we have adopted the corresponding mirror assignments for the analog states in <sup>22</sup>Mg and <sup>22</sup>Ne suggested by Matic *et al.*, while for those assigned new  $J^{\pi}$  values, we made the new mirror assignments accordingly. The present mirror assignments are shown in Fig. 7.

## IV. ASTROPHYSICAL IMPLICATIONS

The thermonuclear <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate, when calculated via a full numerical integration of the energy-dependent cross section, deviates by less than 10% [22] from the rate calculated using a narrow resonance formalism [11,14]. Such deviation is negligible compared to the total uncertainty (estimated below) of the present rate. In this work, the following narrow-resonance formalism has been utilized for the rate calculations:

$$N_A \langle \sigma v \rangle_{\rm res} = 1.54 \times 10^{11} (\mu T_9)^{-3/2} \sum_i (\omega \gamma)_i \\ \times \exp\left(-\frac{11.605 E_R^i}{T_9}\right) [\rm cm^3 s^{-1} mol^{-1}], \quad (4)$$

where  $\mu$  is the reduced mass in units of amu,  $E_R^i$  and  $(\omega\gamma)_i$ (both in units of MeV) are the energy and strength of individual resonance, and  $T_9$  is the temperature in units of 10<sup>9</sup> K (i.e., GK). With the condition of  $\Gamma_{\alpha} \ll \Gamma_p \approx \Gamma_{\text{tot}}$  the resonant strength is calculated by

$$(\omega\gamma)_i = \omega \frac{\Gamma_{\alpha}\Gamma_p}{\Gamma_{\text{tot}}} \simeq (2J_i + 1)\Gamma_{\alpha},$$
 (5)

where  $J_i$  is the spin of the resonance in the compound nucleus <sup>22</sup>Mg. The  $\alpha$ -particle partial width is calculated by

$$\Gamma_{\alpha} = \frac{3\hbar^2}{\mu R_n^2} C^2 S_{\alpha} \times P_{\ell}(E_R).$$
(6)

Here, the isospin Clebsch-Gordan coefficient *C* for the <sup>18</sup>Ne +  $\alpha$  system is 1. Our rate calculation depends critically on the spectroscopic factors  $S_{\alpha}$  of the resonances, which are not known experimentally. Similar to the method used by Matic *et al.*, the corresponding  $\alpha$ -spectroscopic factors are adopted from the mirror <sup>22</sup>Ne whenever available, while for the states without known  $S_{\alpha}$  values, the average  $S_{\alpha}$ 

TABLE IV. The resonant parameters utilized for the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na (reference) rate calculation. The energies ( $E_x$  and  $E_R$ ) are exactly those adopted in Ref. [14].

$\overline{E_x(^{22}\text{Mg}) \text{ (MeV)}}$	$E_R$ (MeV)	$J^{\pi}$	$S_{lpha}$	$\Gamma_{\alpha}$ (eV)	$\omega\gamma$ (eV)
8.1812	0.039	2 <sup>+a</sup>	$2.80 \times 10^{-1}$	$1.70 \times 10^{-65}$	$8.53 \times 10^{-65d}$
8.385	0.243	$1^{+a}$	0	0	0°
8.5193	0.377	3 <sup>-a</sup>	$4.00 \times 10^{-3}$	$7.00  imes 10^{-15}$	$4.87 \times 10^{-14}$ e
8.574	0.432	$4^{+a}$	$6.00 \times 10^{-2}$	$3.60 \times 10^{-13}$	$3.26 \times 10^{-12d}$
8.6572	0.515	$2^{+a}$	$3.20 \times 10^{-1}$	$2.10 \times 10^{-8}$	$1.03 \times 10^{-7}$ c
8.743	0.601	$2^{+a}$	$1.10 \times 10^{-1}$	$2.70 \times 10^{-7}$	$1.34 \times 10^{-6c}$
8.7832	0.642	$1^{-a}$	$1.10 \times 10^{-1}$	$4.00 \times 10^{-6}$	$1.21 \times 10^{-5d}$
8.9318	0.790	$2^{+a}$	$1.10 \times 10^{-1}$	$8.30 \times 10^{-5}$	$4.13 \times 10^{-4d}$
9.08	0.938	1 <sup>-a</sup>	$1.10 \times 10^{-1}$	$7.70 \times 10^{-3}$	$2.31 \times 10^{-2d}$
9.157	1.015	4 <sup>+a</sup>	$7.80  imes 10^{-2}$	$9.70  imes 10^{-5}$	$8.70  imes 10^{-4 \mathrm{d}}$
9.318	1.176	2 <sup>+b</sup>	$1.10 \times 10^{-1}$	$9.90 \times 10^{-2}$	$4.97  imes 10^{-1}$ d
9.482	1.342	3 <sup>-b</sup>	$1.50 \times 10^{-2}$	$1.80 \times 10^{-2}$	$1.25 \times 10^{-1}$
9.542	1.401	1 <sup>-b</sup>	$1.10 \times 10^{-1}$	$4.40 \times 10^{0}$	$1.31 \times 10^{+1d}$
9.709	1.565	$0^{+b}$	$1.50 \times 10^{-1}$	$5.20 \times 10^{+1}$	$5.18  imes 10^{+1}$ d
9.7516	1.610	2 <sup>+b</sup>	$6.20 \times 10^{-2}$	$1.61 \times 10^{+1}$	$4.82  imes 10^{+1}$ d
9.86	1.718	$0^{+b}$	$1.90 \times 10^{-2}$	$2.10 \times 10^{+1}$	$2.07 \times 10^{+1}$ d
10.085	1.944	2 <sup>+b</sup>	$5.00 \times 10^{-2}$	$4.50 \times 10^{+1}$	$2.25 \times 10^{+2d}$
10.2715	2.130	2 <sup>+b</sup>	$1.10 \times 10^{-1}$	$2.62 \times 10^{+2}$	$1.31 \times 10^{+3d}$
10.429	2.287	4 <sup>+b</sup>	$3.00 \times 10^{-2}$	$5.43 \times 10^{0}$	$4.89  imes 10^{+1}$ d
10.651	2.509	3 <sup>-b</sup>	$5.00 \times 10^{-2}$	$1.60 \times 10^{+2}$	$1.12 \times 10^{+3d}$
10.768	2.626	2 <sup>+b</sup>	$1.10 \times 10^{-1}$	$2.30 \times 10^{+3}$	$1.16 \times 10^{+4d}$
10.873	2.731	$0^{+\mathbf{b}}$	$1.10 \times 10^{-1}$	$1.19 \times 10^{+4}$	$1.19  imes 10^{+4d}$
11.001	2.859	4 <sup>+b</sup>	$3.00 \times 10^{-2}$	$6.45 \times 10^{+1}$	$5.81  imes 10^{+2d}$
11.315	3.173	4 <sup>+b</sup>	$3.00 \times 10^{-2}$	$2.00 \times 10^{+2}$	$1.83 \times 10^{+3d}$
11.499	3.357	2 <sup>+b</sup>	$1.10 \times 10^{-1}$	$1.70 \times 10^{+4}$	$8.64  imes 10^{+4}$ d
11.595	3.453	4 <sup>+b</sup>	$3.00 \times 10^{-2}$	$4.08 \times 10^{+2}$	$3.67 \times 10^{+3d}$
11.747	3.607	$0^{+b}$	$1.10 \times 10^{-1}$	$7.10 \times 10^{+4}$	$7.13 \times 10^{+4d}$
11.914	3.772	2 <sup>+b</sup>	$1.10  imes 10^{-1}$	$3.53 \times 10^{+4}$	$1.77 \times 10^{+5d}$
12.003	3.861	1 <sup>-b</sup>	$2.10 \times 10^{-1}$	$1.40 \times 10^{+5}$	$4.31 \times 10^{+5d}$
12.185	4.050	3 <sup>-b</sup>	$1.80 \times 10^{-1}$	$3.70 \times 10^{+4}$	$2.60 \times 10^{+5d}$
12.474	4.332	2 <sup>+b</sup>	$1.10 \times 10^{-1}$	$7.80  imes 10^{+4}$	$3.89 \times 10^{+5d}$
12.665	4.523	3 <sup>-b</sup>	$1.20  imes 10^{-1}$	$4.90 \times 10^{+4}$	$3.45 \times 10^{+5d}$
13.01	4.865	$0^{+b}$	$1.10 \times 10^{-1}$	$2.20\times10^{+5}$	$2.16\times10^{+5\rm d}$

<sup>a</sup>Experimentally determined spin parities in this work.

<sup>b</sup>Spin parities assumed in Ref. [22] as adopted in the present work.

<sup>c</sup>Recalculated  $\Gamma_{\alpha}$  and  $\omega\gamma$  values in this work.

<sup>d</sup>Resonant strengths in Ref. [22] as adopted in the present work.

<sup>e</sup>Resonant strength in Ref. [14] as adopted in the present work.



FIG. 9. (Color online) *R*-matrix fits for the 8.353-MeV state.

values [i.e.,  $S_{\alpha}(0^+) = 0.11$ ,  $S_{\alpha}(1^-) = 0.11$ ,  $S_{\alpha}(2^+) = 0.11$ ,  $S_{\alpha}(3^-) = 0.05$ , and  $S_{\alpha}(4^+) = 0.03$ ] adopted by Matic *et al.* are utilized in the present calculations. Here, the errors of these adopted factors are estimated as the standard deviation of the  $S_{\alpha}$  factors for the states with same  $J^{\pi}$ : they are  $\sigma(0^+) = 0.18$ ,  $\sigma(1^-) = 0.09$ ,  $\sigma(2^+) = 0.19$ ,  $\sigma(3^-) = 0.02$ , and  $\sigma(4^+) = 0.03$ , respectively. The Coulomb penetration factor  $P_{\ell}$  on resonance is given by

$$P_{\ell}(E_R) = \frac{kR_n}{[F_{\ell}(E)^2 + G_{\ell}(E)^2]_{|E_R;R_n}},$$
(7)

where  $k = \sqrt{2\mu E_R}/\hbar$  is the wave number and  $F_\ell$  and  $G_\ell$  are the regular and irregular Coulomb functions, respectively.

The resonant parameters for the thermonuclear  ${}^{18}\text{Ne}(\alpha, p){}^{21}\text{Na}$  rate calculations are summarized in Table IV.



FIG. 10. (Color online) *R*-matrix fits for states above the  $\alpha$  threshold.

In this calculation, all resonant energies  $E_R$  (and their errors) and most of the strengths  $\omega\gamma$  are adopted from the work of Matic *et al.* [14] and Mohr and Matic [22]. For those states assigned new  $J^{\pi}$  values by this work, the strengths are recalculated (see Table IV). As in the work of Mohr and Matic, the calculated rate is taken as the reference  $N_A \langle \sigma v \rangle_{\text{reference}}$ . The uncertainty of the calculated rate is mainly caused by the errors in the resonant strengths  $\omega\gamma$ ; the uncertainty arising from those of the resonant energies contributes less than 12% over 0.1–3 GK. This is verified by the Monte Carlo approach [42]. The two inverse measurements [20,21] gave similar rates which are about 3 times lower than the reference rate at 0.8–2.7 GK [22]. As discussed in Ref. [22], both calculations of the present work and the previous time-inverse measurement work are based on simple but reasonable arguments: If we assume the corresponding uncertainties do not exceed a factor of 2, there will be a relatively narrow overlap region between the lower limit of the present  $N_A \langle \sigma v \rangle_{\text{reference}}$  and the upper limit of the reverse reaction data. The most realistic estimate from the overlap is located around  $0.55 \times N_A \langle \sigma v \rangle_{\text{reference}}$ , and is considered as the new recommended reaction rate  $N_A \langle \sigma v \rangle_{\text{recommended}}$  [22]. Note that the factor of 0.55 has been derived from the comparison of transfer data and reverse reaction data at energies between 1



FIG. 11. (Color online) (a) Ratio between the present  ${}^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$  rate and that in Ref. [22]; (b) contribution from those dominant resonances to the total rate.

and 3 MeV, i.e., corresponding to temperatures above 1 GK where the Mohr and Matic rate is practically identical to the present calculated one [see Fig. 11(a)]. Thus, the normalization factor of 0.55 is retained since the previous work. The calculated  $N_A \langle \sigma v \rangle_{\text{recommended}}$  rate is summarized in Table V. As discussed by Mohr and Matic, the realistic lower limit of the recommended rate can be taken from the Salter *et al.* data (multiplied by a factor of 3 to take the ground-state branching into account), which is about three times lower than the reference rate [20], and a realistic upper limit is the reference rate  $N_A \langle \sigma v \rangle_{\text{reference}}$ .

The ratios between our recommended rate and the one recommended in Ref. [22] are shown in Fig. 11(a). It shows that the present rate is much smaller below 0.13 GK. This is due to the unnatural-parity  $1^+$  newly assigned to the 8.385-MeV state, which does not contribute to the rate anymore. In addition, the present rate is about 1.7 times larger around 0.2 GK, because of our new 2<sup>+</sup> assignments for the 8.657- and 8.743-MeV states. Beyond 0.55 GK, the present rate is quite similar to the previously recommended one because the same resonant parameters for the high-lying states were used. The contributions of those dominant resonances to the total rate are shown in Fig. 11(b). The resonance strength of the 8.743-MeV state increases by more than two orders of magnitude as a result of the new spin-parity assignment, which significantly enhances its contribution compared with the previous estimate of Matic et al. A comparison to other available rates was made in Ref. [27], where the deduced rate is slightly different from the present recommended one.

TABLE V. Recommended <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction rate and the lower and upper limits. All are in units of cm<sup>3</sup> s<sup>-1</sup> mol<sup>-1</sup>.

<i>T</i> 9	$N_A \langle \sigma v  angle_{ m recommended}$	Upper	Lower
0.1	$2.96 \times 10^{-27}$	$5.38 \times 10^{-27}$	$1.62 \times 10^{-27}$
0.2	$2.02 \times 10^{-15}$	$3.67 \times 10^{-15}$	$1.10 \times 10^{-15}$
0.3	$4.88 \times 10^{-11}$	$8.87  imes 10^{-11}$	$2.66 \times 10^{-11}$
0.4	$1.41 \times 10^{-8}$	$2.57 \times 10^{-8}$	$7.70  imes 10^{-9}$
0.5	$7.84 \times 10^{-7}$	$1.43 \times 10^{-6}$	$4.28  imes 10^{-7}$
0.6	$1.73 \times 10^{-5}$	$3.15 \times 10^{-5}$	$9.45 \times 10^{-6}$
0.7	$2.09 \times 10^{-4}$	$3.79 \times 10^{-4}$	$1.14  imes 10^{-4}$
0.8	$1.70 \times 10^{-3}$	$3.09 \times 10^{-3}$	$9.27  imes 10^{-4}$
0.9	$1.03 \times 10^{-2}$	$1.87 \times 10^{-2}$	$5.62 \times 10^{-3}$
1.0	$4.84 \times 10^{-2}$	$8.81  imes 10^{-2}$	$2.64  imes 10^{-2}$
1.1	$1.83 \times 10^{-1}$	$3.32 \times 10^{-1}$	$9.96  imes 10^{-2}$
1.2	$5.73 \times 10^{-1}$	$1.04 \times 10^{0}$	$3.13  imes 10^{-1}$
1.3	$1.55 \times 10^{0}$	$2.81 \times 10^{0}$	$8.44  imes 10^{-1}$
1.4	$3.70 \times 10^{0}$	$6.73 \times 10^{0}$	$2.02 \times 10^{0}$
1.5	$8.03  imes 10^{0}$	$1.46 \times 10^{+1}$	$4.38  imes 10^{0}$
1.6	$1.61 \times 10^{+1}$	$2.92 \times 10^{+1}$	$8.77  imes 10^0$
1.7	$3.02 \times 10^{+1}$	$5.49 \times 10^{+1}$	$1.65 \times 10^{+1}$
1.8	$5.37 \times 10^{+1}$	$9.76 \times 10^{+1}$	$2.93  imes 10^{+1}$
1.9	$9.14 \times 10^{+1}$	$1.66 \times 10^{+2}$	$4.99  imes 10^{+1}$
2.0	$1.50 \times 10^{+2}$	$2.73 \times 10^{+2}$	$8.18 imes10^{+1}$
2.1	$2.38 \times 10^{+2}$	$4.33 \times 10^{+2}$	$1.30  imes 10^{+2}$
2.2	$3.68 \times 10^{+2}$	$6.70 \times 10^{+2}$	$2.01 \times 10^{+2}$
2.3	$5.56 \times 10^{+2}$	$1.01 \times 10^{+3}$	$3.03  imes 10^{+2}$
2.4	$8.21 \times 10^{+2}$	$1.49 \times 10^{+3}$	$4.48  imes 10^{+2}$
2.5	$1.19 \times 10^{+3}$	$2.16 \times 10^{+3}$	$6.49  imes 10^{+2}$
2.6	$1.69 \times 10^{+3}$	$3.08 \times 10^{+3}$	$9.24  imes 10^{+2}$
2.7	$2.37 \times 10^{+3}$	$4.32 \times 10^{+3}$	$1.30  imes 10^{+3}$
2.8	$3.28  imes 10^{+3}$	$5.96  imes 10^{+3}$	$1.79  imes 10^{+3}$
2.9	$4.47 \times 10^{+3}$	$8.13 \times 10^{+3}$	$2.44 \times 10^{+3}$
3.0	$6.01 \times 10^{+3}$	$1.09 \times 10^{+4}$	$3.28\times10^{+3}$

The recommended rate  $N_A \langle \sigma v \rangle_{\text{recommended}}$  (in units of cm<sup>3</sup>s<sup>-1</sup>mol<sup>-1</sup>) can be well parameterized (within 2% error in 0.1–10 GK) by the following expression, e.g., Eq. (16) in Ref. [43]:

$$N_A \langle \sigma v \rangle = \exp(-2201.74 - 401.30T_9^{-1} + 5496.69T_9^{-1/3} - 2970.73T_9^{1/3} + 73.64T_9 - 2.135T_9^{5/3} + 2374.71 \ln T_9) + \exp(5493.46 - 410.12T_9^{-1} + 2889.36T_9^{-1/3} - 9603.61T_9^{1/3} + 1544.42T_9 - 286.244T_9^{5/3} + 3066.95 \ln T_9) + \exp(13426.5 - 119.86T_9^{-1} + 8781.47T_9^{-1/3} - 24789.9T_9^{1/3} + 3149.91T_9 - 452.62T_9^{5/3} + 8688.98 \ln T_9).$$

The impact of our new <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate was examined within the framework of one-zone XRB postprocessing calculations [27]. Different XRB thermodynamic histories were employed, including the K04 ( $T_{\text{peak}} = 1.4$  GK) and



FIG. 12. (Color online) Abundances during one-zone XRB calculations using the K04 thermodynamic history [44]. Results using the present rate (black solid lines) and Görres *et al.* [10] rate (red [gray] dotted lines) are indicated.

S01 ( $T_{\text{peak}} = 1.9$  GK) models from Refs. [44,45]. For each of these histories, separate postprocessing calculations were performed using the present <sup>18</sup>Ne( $\alpha, p$ )<sup>21</sup>Na rate and previous ones [10,11,14,17]; all other reaction rates in the network [44] were left unchanged.

Our previous conclusion [27] about the energy generation rate affected by this <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate still holds with the present slightly changed rate. As concluded before, our new thermonuclear <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate clearly affects predictions from our models. For example, a striking difference in the nuclear energy generation rate at early times (between 0.3 and 0.4 s, or equivalently, between 0.6 GK and 0.9 GK during the burst) has been seen when comparing XRB calculations using the present, Chae *et al.*, and Görres *et al.* rates with the K04 model. Not only does the peak energy generation rate increase by a factor of 1.4–1.8 with the present rate, but the profiles of the curves around the maxima are also rather different (see Fig. 4 in Ref. [27]).

We note that for both the K04 and S01 models, rates from Refs. [10,11,17] give lower peak nuclear energy generation rates than that from Chae et al., by about 10-30%. Furthermore, the rate of Matic et al. gives rather similar results to those using the present rate. In particular, the calculated nuclear energy generation rates agree overall to about 5% [27]. Therefore, we only discuss below the impact of the Görres et al. and present rates on the reaction flux in the K04 model. We note a change in the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction flux at the early times of the XRBs as shown in Fig. 12. For example, at 0.35 s, this reaction flux increases by a factor of 2-3 with our new rate. This contributes to the depletion of <sup>15</sup>O and <sup>18</sup>Ne at that time by a factor of 3-4 relative to abundances calculated using the Görres et al. rate. These species are effectively converted to higher mass ones. Note, however, that no significant changes (>5%) to any final abundances with mass fractions  $X > 10^{-3}$ were observed when comparing the calculations using the two rates (our recommended one and Görres et al. one).

Figure 13 shows the ratio of the recommended thermonuclear <sup>18</sup>Ne( $\alpha$ ,p)<sup>21</sup>Na rates to the  $\beta$  decay of <sup>18</sup>Ne( $e^+\nu$ )<sup>18</sup>F [46],

$$R = \rho \frac{X_{\alpha}}{m_{\alpha}} N_A \langle \sigma v \rangle / (\ln 2 / \tau_{1/2}), \qquad (8)$$



FIG. 13. (Color online) Present rate and previous ones in unit of the  $\beta$ -decay rate of  ${}^{18}\text{Ne}(e^+\nu){}^{18}\text{F}$ .

where  $X_{\alpha}$  and  $m_{\alpha}$  are the mass fraction and atomic mass of  $\alpha$  particle, respectively, and  $\tau_{1/2}$  is the  $\beta$ -decay half-life of <sup>18</sup>Ne. We assumed a typical density of 10<sup>6</sup> g/cm<sup>3</sup> and  $\alpha$  mass fraction of 0.27 for XRBs in the calculation. It shows that present <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction dominates over the  $\beta$  decay of <sup>18</sup>Ne at an onset temperature of  $T \approx 0.57$  GK. This critical temperature is noticeably lower than the temperature of  $T \approx 0.68$  GK with the rates from Refs. [10,11,15], and hence it implies that this reaction initiates the breakout earlier than previously thought. Note that the above numbers 0.57 and 0.68 were, by mistake, presented as 0.47 and 0.60 in our previous publication [27].

#### V. SUMMARY

We have studied the resonant elastic-scattering of <sup>21</sup>Na + pusing a radioactive ion beam of <sup>21</sup>Na with the thick-target method. The  $E_{c.m.}$  spectra were reconstructed from the inverse kinematics. In total, 23 resonances above the proton threshold in <sup>22</sup>Mg were observed. The relevant proton resonant parameters have been determined by the *R*-matrix analysis of the center-of-mass differential cross-sectional data at different scattering angles. The <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction rate is recalculated with the present parameters. A new recommended rate is given by combining the results from different experimental techniques, and our new rate deviates considerably from the recent recommended rate of Mohr and Matic below ~0.55 GK.

The astrophysical impact of our new rate has been investigated through one-zone postprocessing x-ray burst calculations. Compared to previous rates in Refs. [10,11,15], the new rate increases the energy production rate by factors of 1.4–1.8 at early time (between 0.3–0.4 s, or equivalently, between 0.6–0.9 GK during the burst) of the burst, and the <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na reaction flux is also enhanced about two times at that time. The breakout onset temperature for this reaction occurs at around 0.57 GK, lowered by 0.11 GK due to the increase of the reaction rate.

Despite the different  $J^{\pi}$  values adopted in the present and Matic *et al.* <sup>18</sup>Ne( $\alpha$ , p)<sup>21</sup>Na rate calculations (and the consequent differences in deduced thermonuclear rates), our models give very similar XRB nuclear energy generation rates. This suggests that  $J^{\pi}$  values for relevant states in <sup>22</sup>Mg are, for the moment, sufficiently well known for our models. Future measurements should primarily focus on measuring other quantities of interest (such as spectroscopic factors, partial widths, or the precise cross-sectional data), which can further constrain this rate.

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