Dynamic polarization potentials and dipole polarizabilities of 11Li, 6He and 6Li compared

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Elastic scattering data for ¹¹Li, ⁶Li, and ⁶He $+$ ²⁰⁸Pb at incident energies of 29.8 MeV, 29 MeV, and 18 MeV, respectively, were analyzed by means of coupled discretized continuum channels (CDCC) calculations. Dynamic polarization potentials (DPPs) of the trivially equivalent local potential (TELP) type were derived from these calculations and compared. The dipole polarizability factor α for ¹¹Li obtained by fitting a Coulomb polarization potential to the long-range part of the real DPP is consistent with the theoretical value of 5.7 fm^3 . These results point to the dineutron model providing a very good description of 11 Li breakup coupling effects. The much larger Coulomb dipole polarizability of $¹¹Li$ suggests the persistence of large deviations from Rutherford scattering at</sup> sub-barrier energies for medium mass targets, a prediction confirmed by CDCC calculations.

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A recent measurement [\[1\]](#page-2-0) of the elastic scattering of 11 Li by a 208Pb target at incident energies below the nominal Coulomb barrier found angular distributions that deviated markedly from Rutherford scattering, in contrast to the behavior of "normal" heavy-ion scattering. Four-body coupled discretized continuum channels (CDCC) calculations were able to describe the data well and indicated that the main cause of the large deviation from Rutherford scattering was Coulomb dipole coupling, which may in turn be associated with a large Coulomb dipole polarizability of ¹¹Li. In this work we employ a two-body dineutron model of $¹¹Li$ to perform</sup> CDCC calculations for the data of Ref. [\[1\]](#page-2-0) and compare the results with calculations for ${}^{6}Li + {}^{208}Pb$ and ${}^{6}He + {}^{208}Pb$ at similar energies with respect to the Coulomb barrier (29 MeV and 18 MeV, respectively). These nuclei make excellent comparisons with $\frac{11}{11}$, since ⁶He has a large dipole polarizability (see, e.g., Parkar *et al.* [\[2\]](#page-2-0), and references therein) whereas the dipole couplings in 6 Li are negligible (identically zero in a strict $\alpha + d$ model). Dynamic polarization potentials (DPPs) of the trivially equivalent local potential (TELP) type were derived from the CDCC calculations and compared at large radii. The long range parts of the real DPPs for $\rm{^{11}Li}$ and ⁶He were well reproduced by Coulomb polarization potentials, thus enabling the dipole polarizability factors to be compared with each other and theory. This procedure [\[3\]](#page-2-0) was adopted rather than direct fitting of the elastic scattering data with a parametrized DPP (as was done in Ref. [\[2\]](#page-2-0) for example) due to the scatter in the 11 Li + 208 Pb data (see Fig. [1\)](#page-1-0) leading to a wide range of possible potentials of this type. All calculations were carried out using the code FRESCO [\[4\]](#page-2-0).

We adopted a simplified two-body model of 11 Li since it retains the essential physics of the problem while avoiding the complications of the more sophisticated three-body model used in Ref. [\[1\]](#page-2-0). Although several low-lying resonances have been identified in $\frac{11}{11}$ [\[5\]](#page-2-0) we did not include these since they have no definite spin-parity assignments as yet. To keep the size of the 11 Li calculation within reasonable bounds we set the spin of the 9Li core equal to zero. The 11Li diagonal and coupling potentials were calculated using Watanabe-type folding. The $2n + {}^{9}Li$ binding potential was of Woods-Saxon form with parameters: $R = 0.66(2^{1/3} + 9^{1/3})$ fm, $a = 0.2$ fm, the depth being adjusted to give the correct two-neutron separation energy of 0.37 MeV. The deuteron potential of Ref. [\[6\]](#page-2-0) was used for the $2n + 208$ Pb optical potential and the ⁷Li potential of Ref. [\[7\]](#page-2-0) for the ${}^{9}Li + {}^{208}Pb$ optical potential (the ${}^{9}Li$ elastic scattering at the required energy, 24.4 MeV, is very close to pure Rutherford scattering $[1]$, therefore the ¹¹Li calculation is relatively insensitive to the choice of ${}^{9}Li$ + ²⁰⁸Pb optical potential). The ² $n + {}^{9}$ Li continuum was divided into bins in momentum (k) space of width $\Delta k = 0.1$ fm⁻¹ up to a maximum value of $k_{\text{max}} = 0.7$ fm ⁻¹. Relative angular momenta $L = 0, 1, 2, 3$ were included with all couplings up to multipolarity $\lambda = 3$. The ⁶He + ²⁰⁸Pb calculations were similar to those of Ref. [\[8\]](#page-2-0) using the improved dineutron model of 6 He of Ref. [\[9\]](#page-2-0), with the exception that relative angular momentum values up to $L = 4$ and couplings up to multipolarity $\lambda = 4$ were included, although tests found that the extra bins and couplings had a negligible effect on the DPP in the radial region under discussion here. The ${}^{6}Li +{}$ 208 Pb calculations were similar to those described in Ref. [\[10\]](#page-2-0) with the continuum binning truncated at $k_{\text{max}} = 0.8 \text{ fm}^{-1}$. The $d + {}^{208}Pb$ and $\alpha + {}^{208}Pb$ optical potentials were taken from Refs. [\[6\]](#page-2-0) and [\[11\]](#page-2-0), respectively.

In Fig. [1](#page-1-0) we compare the calculations with the data for ¹¹Li, ⁶Li, and ⁶He $+$ ²⁰⁸Pb elastic scattering at 29.8 MeV [\[1\]](#page-2-0), 29 MeV [\[12\]](#page-2-0), and 18 MeV [\[13\]](#page-2-0).

The agreement between calculations and data validates the models used as representing the effects of breakup coupling sufficiently realistically to describe the available data. In particular, the coupling effect for 11 Li is qualitatively similar to that of Ref. [\[1\]](#page-2-0). We also show in Fig. [1](#page-1-0) the results of CDCC calculations without Coulomb couplings (but retaining the diagonal Coulomb potentials) as the dotted curves. It will be noted that while the coupling effect for 11 Li and 6 He is dominated by Coulomb coupling (cf. the solid and dotted

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FIG. 1. CDCC calculations compared to the elastic scattering data for: (a) 29.8 MeV ¹¹Li + ²⁰⁸Pb, (b) 29 MeV ⁶Li + ²⁰⁸Pb, and (c) 18 MeV 6 He + 208 Pb. The solid and dashed curves represent the results of the full CDCC and no-coupling calculations, respectively. The dotted curves denote the results of CDCC calculations with no Coulomb couplings (but retaining the diagonal Coulomb potentials). The dot-dashed curves denote the results of optical model calculations with the bare potentials $+$ DPPs, see text. Note the linear cross section scale.

curves), for 6Li the Coulomb coupling has a negligible effect, as found previously $[14,15]$ [the dotted curve on Fig. 1(b) is barely visible]. The total (Coulomb plus nuclear) coupling effect is also qualitatively different for ⁶Li, which may be ascribed to the absence of strong Coulomb dipole coupling in this nucleus.

Coupling effects may be represented by a potential term the dynamic polarization potential or DPP—added to the "bare" optical potential used as input to the coupled channels calculation. This DPP is intrinsically nonlocal and Ldependent, but local, L-independent equivalents may always be found. In this work we use one such local equivalent DPP, the so-called trivially equivalent local potential of Ref. [\[16\]](#page-2-0), as implemented in the code FRESCO [\[4\]](#page-2-0). In Fig. 2 we present the TELP-type DPPs derived from the CDCC calculations for 11 Li, ⁶He and ⁶Li at large radii. As a check on the validity of these DPPs, at least in the region where the elastic scattering is sensitive to the potential, we plot in Fig. 1 as the dot-dashed curves the angular distributions predicted by optical model calculations employing the bare potential plus the DPP. The agreement with the CDCC calculations is good (in the case of 6 Li so good that the dot-dashed curve is completely hidden) thus validating the DPPs as a representation of the coupling effects. A significant qualitative difference between the DPPs

FIG. 2. TELP-type DPPs derived from the CDCC calculations for ¹¹Li, ⁶He, and ⁶Li + ²⁰⁸Pb. The dotted curves in (a) denote the Coulomb polarization potential of Eq. (1) with values of $\alpha = 5.7$ fm³ and 1.3 fm^3 for $\frac{11}{11}$ and $\frac{6}{11}$ respectively.

for 11 Li and 6 He and that for 6 Li is immediately apparent: while the ¹¹Li and ⁶He DPPs both exhibit the long attractive and absorptive tails characteristic of strong dipole Coulomb couplings $[8,17-19]$ $[8,17-19]$, the ⁶Li DPP is essentially zero for radii $r > 20$ fm ($r > 15$ fm for the imaginary part). Given that in the $\alpha + d$ model of ⁶Li dipole couplings are identically zero this behavior is to be expected and may be adduced as further evidence that the long tails in the ¹¹Li and ⁶He DPPs do indeed result from the Coulomb dipole coupling to the continuum.

The long-range tails of the 11 Li and ⁶He real DPPs may therefore be represented by the Coulomb polarization potential given by

$$
V_{\text{Pol}}(r) = -\frac{1}{2}\alpha \frac{Z_{\text{T}}^2 e^2}{r^4},\tag{1}
$$

where α is the Coulomb dipole polarizability parameter, Z_T the target atomic number, and e the charge on the electron. The 6 He real DPP is consistent with a value of $\alpha \sim 1.3$ fm³, somewhat smaller than the theoretical values of 1.88 fm³ [\[20\]](#page-3-0) or 1.99 fm³ [\[21\]](#page-3-0) but close to the value of 1.2 fm^3 obtained in Ref. [\[2\]](#page-2-0), while the ¹¹Li real DPP is consistent with the theoretical value of $\alpha = 5.7$ fm³ [\[22\]](#page-3-0). The good agreement of the "empirical" dipole polarizability with theory suggests that the dineutron model is a much better approximation for $¹¹Li$ than</sup> it is for 6He, implying a stronger correlation between the two valence neutrons in 11 Li (it will be recalled that we have used the improved dineutron model of Ref. [\[9\]](#page-2-0) for ⁶He which better matches the wave functions from more sophisticated three-body models; the "pure" dineutron model significantly overpredicts the dipole strength for 6He, as was demonstrated in Ref. [\[9\]](#page-2-0))

The long-range absorptive tail of the ¹¹Li imaginary DPP also extends to much larger radii than that for 6He, suggesting that the Coulomb breakup of $¹¹Li$ takes place further from the</sup> target. This may be explained as due to the larger size of 11 Li. However, since the difference between the rms matter radii of 11 Li and ⁶He is only of the order of 1.4 fm or so, the difference

FIG. 3. CDCC calculations for 11.6 MeV ¹¹Li + ⁵⁸Ni elastic scattering. The solid and dashed curves represent the results of the full CDCC and no-coupling calculations, respectively. The dotted curve denotes the result of a CDCC calculation with no Coulomb couplings (but retaining the diagonal Coulomb potentials). The dotdashed curve denotes the result of an optical model calculation with the bare potential $+$ DPP. Note the linear cross section scale.

in the imaginary DPPs suggests a greater extent of the neutron halo distribution for $¹¹Li$ as the probable cause of this very long</sup> range absorption. Test calculations for ${}^{11}\text{Li} + {}^{208}\text{Pb}$ where the TELP-type DPP was replaced by the forms of Eq. [\(1\)](#page-1-0) for both real and imaginary parts for $r > 24$ fm (and kept constant at the value for $r = 24$ fm for $r < 24$ fm) found that the CDCC angular distribution was well reproduced for center-of-mass

angles $\theta_{\rm c.m.} \leq 75^{\circ}$. For $\theta_{\rm c.m.} > 75^{\circ}$ the repulsive core of the real part of the TELP-type DPP seen in Fig. [2\(a\)](#page-1-0) was important.

The very much larger dipole polarizability of 11 Li compared to that of ⁶He suggests that the observed large deviations from Rutherford scattering for sub-barrier $^{11}Li + {}^{208}Pb$ elastic scattering [1] should persist for medium mass targets, unlike the situation for ⁶He which exhibits normal Fresnel scattering for such targets [\[23,24\]](#page-3-0). In Fig. 3 we show the results of CDCC calculations for 11.6 MeV ¹¹Li + ⁵⁸Ni, a roughly similar energy with respect to the nominal Coulomb barrier as the $11Li + 208Pb$ data of Ref. [1] shown in Fig. [1\(a\).](#page-1-0)

This confirms that even for medium mass targets the complete wiping out of the Coulomb rainbow, the most striking feature of the large breakup coupling effect, does indeed persist for ¹¹Li. In this respect it is similar to ¹¹Be, cf. the ¹¹Be + 64 Zn quasielastic scattering data of Ref. [\[25\]](#page-3-0). Figure 3 shows that for $¹¹$ Li the Coulomb breakup coupling remains dominant</sup> in the suppression of the Coulomb rainbow for medium mass targets.

In summary, we have shown that a two-body dineutron model of 11Li is able to describe rather well the elastic scattering data for $^{11}Li + {}^{208}Pb$ at an incident energy just below the nominal Coulomb barrier. The long-range attractive real DPP derived from this calculation is consistent with the theoretical dipole polarizability for $¹¹Li$, further supporting the</sup> suggestion that the dineutron model is more realistic for $¹¹Li$ </sup> than it is for ⁶He. The much larger dipole polarizability of $\rm^{11}Li$ compared to that of 6He suggests that the large deviations from Rutherford scattering observed for sub-barrier $^{11}Li + {}^{208}Pb$ elastic scattering should persist for medium mass targets, a prediction confirmed by CDCC calculations.

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