Exploring the breakup and transfer coupling effects in 9Be elastic scattering

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Two cluster structures of ⁹Be, namely, ⁵He + ⁴He and ⁸Be + n, have been considered for its breakup to describe the available data on elastic scattering for a $9Be$ projectile with ²⁸Si, ⁶⁴Zn, and ¹⁴⁴Sm targets. The results of these calculations suggest that the breakup coupling effects are significant for the 5 He + 4 He cluster model above the barrier energies, while they are dominant at relatively lower energies for the ${}^{8}Be + n$ model. The addition of a one-neutron stripping channel in the ${}^{8}Be + n$ model gives an overall good description of the elastic data for all the systems considered. The couplings generated by breakup in the ${}^{8}Be + n$ model have a behavior different from the coupling effects obtained within the ${}^{5}He + {}^{4}He$ model, the former being more prominent at lower energies and for the heavier target systems. The behavior of extracted dynamic polarization potentials generated due to breakup and one-neutron transfer coupling has been investigated.

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I. INTRODUCTION

The study of reaction dynamics for the weakly bound nuclei offer ample opportunities to understand the underlying cluster structure effects. The measurements of elastic scattering and breakup observable in the experiments involving such nuclei show that the scattering and breakup probabilities are sensitive to the internal cluster structure. The reactions induced by stable weakly bound nuclei 6.7 Li have been explained quite successfully in terms of their predominant $\alpha + d$ and $\alpha + t$ cluster structures, respectively [\[1–6\]](#page-6-0). However, the cluster structure of $9B$ e which can be thought of in terms of two α particles and a neutron is not clear. Within the three-body $\alpha + \alpha + n$ picture of ⁹Be, no two constituents alone can form a bound system, a case analogous to that observed in some loosely bound unstable nuclei such as 6 He and 11 Li, the so-called Borromean structure. The cluster structure of ⁹Be is not only of interest for studying the reaction dynamics of loosely bound nuclei but is of relevance to certain aspects of nuclear astrophysics. The nucleosynthesis via the reaction path $\alpha + \alpha + n \rightarrow$ ⁹Be followed by ⁹Be(α , *n*)¹²C [\[7\]](#page-6-0) is the most efficient path to bridge the stability gaps at $A = 5$ and $A = 8$ and knowledge of the cluster structure of ⁹Be is vital for calculating the reaction rates. While a three-body $\alpha + \alpha + n$ cluster structure picture of the $9B$ e nucleus is the more accurate one, the effective two-body $\alpha + {}^{5}He$ [$\alpha + (\alpha + n)$] [\[8,9\]](#page-6-0) or $n + {}^{8}Be$ [$n + (\alpha + \alpha)$] [\[10,11\]](#page-6-0) cluster configuration can be used successfully in the calculations to explain the reaction dynamics. Experimentally, several measurements of the ⁹Be breakup $[12-15]$ have been performed to quantify the contribution of different cluster decay components in its low-lying excitation spectrum.

There is much experimental evidence which shows that the reaction dynamics of weakly bound nuclei are quite different from the tightly bound nuclei. There is a greater

importance of the direct reactions, such as breakup or transfer, which may be enhanced owing to the low binding energies and the favorable Q values for selected transfer channels. The coupling effects due to the low-lying resonances and nonresonant continuum arising due to small breakup threshold of a weakly bound nucleus are expected to be quite dominant. In addition, the coupling effect due to transfer channels is also found to be significant. The continuum discretized coupled channel (CDCC) formalism presents an effective method to take into account the coupling effects of breakup on the elastic scattering and fusion process. In this method, the coupled channels calculations are performed including the bound states of the projectile and the continuum of its excitation which is discretized into a finite number of bins. Further, the transfer mechanism can be studied through the coupled reaction channels (CRC) formalism. The coupling effects are manifested in the behavior of the equivalent dynamic polarization potential (DPP), which may provide a qualitative idea of major couplings that have significant effect on the reaction dynamics [\[16\]](#page-6-0). The nature of DPP arising due to the couplings of the breakup and transfer processes is not clear in the case of weakly bound nuclei. In general, the breakup couplings are assumed to give repulsive behavior for the real part of DPP. However, the opposite effect is observed at low energies where the breakup couplings have the dominant dipole contribution. Similarly, the transfer couplings are expected to give attractive couplings, but in the case of positive Q -value reactions, repulsive couplings have been found $[9,17]$. In addition, it has been shown that the couplings due to breakup also change their nature as a function of energy [\[16,18\]](#page-6-0).

In a recent study, we have thoroughly investigated [\[10\]](#page-6-0) two cluster configurations of ⁹Be, namely, the ⁵He $+$ ⁴He (breakup threshold = 2.46 MeV) and the ${}^{8}Be + n$ (breakup threshold = 1.67 MeV), through high-precision elastic scattering data at sub-Coulomb barrier energies on a 208Pb target. It was demonstrated that at these sub-Coulomb barriers only the $8Be + n$ cluster structure of ⁹Be is able to explain the data satisfactorily. Also, the effect of one-neutron transfer was

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considered in these calculations and found to be dominant even at such sub-Coulomb barrier energies. It is to be noted that in the previous study by Keeley *et al.* [\[8\]](#page-6-0), the cluster structure of 5 He + 4 He for 9 Be was used to explain the elastic scattering angular distribution data of the ${}^{9}Be + {}^{208}Pb$ system, at energies around and above the Coulomb barrier. It was also pointed out that the coupling effect of the one-neutron stripping channel plays an important role. The competing coupling effects of one-neutron transfer and the breakup channel for the 9^9 Be projectile are crucial for the proper understanding of 9^9 Be elastic scattering data for different target systems. Motivated by these investigations, we have attempted to validate the two models of ⁹Be for a few other targets $(^{28}Si$ [\[19\]](#page-6-0), ⁶⁴Zn [\[20\]](#page-6-0), and 144 Sm [\[21\]](#page-6-0)) in different mass regions, where elastic scattering data are available around Coulomb barrier energies.

II. CALCULATIONS

To study the effect of breakup and transfer couplings, we have carried out detailed coupled channels calculations. The breakup of the ⁹Be in the reactions for the ⁹Be + ²⁸Si, ⁶⁴Zn, and 144Sm systems has been taken into account by performing the CDCC calculations. In addition to breakup (BU) couplings, the effect of one-neutron transfer coupling has also been investigated through the coupled reaction channel (CRC) calculations. The code FRESCO version FRXY.li [\[22\]](#page-6-0) is used for these calculations. The CDCC calculations are performed considering ⁹Be as ⁵He + ⁴He and ⁸Be + *n* clusters. In the 5 He + 4 He cluster picture of 9 Be, the ground state of 9 Be $(3/2⁻)$ is constructed by taking the relative angular momentum $L = 0$ and 2 between the core ⁵He (3/2⁻) and the ⁴He (0⁺) cluster. The $L = 2$ component is taken in order to account for the reorientation of the highly deformed ⁹Be nucleus. The bound state and the resonances are generated by using the potential between ⁵He (3/2⁻) and ⁴He (0⁺) clusters, taken from Ref. [\[8\]](#page-6-0). The spectroscopic amplitudes 0.81 and 0.5358, obtained from a shell model calculation, are used for the two components $L = 0$ and $L = 2$ of the ground-state wave function, respectively [\[8\]](#page-6-0). Separate ground-state wave functions are obtained for the $L = 0$ and $L = 2$ components by adjusting the binding potentials of ${}^{5}He + {}^{4}He$ configuration to reproduce the experimental binding energy of 9Be. While the

TABLE II. Energy levels of residual nuclei and spectroscopic amplitudes (SA) used in the CRC calculations.

	^{29}Si			${}^{65}Zn$		$^{145}\mathrm{Sm}$				
E (MeV)	J^{π}	SA	E (MeV)	J^{π}	SA	E (MeV)	J^{π}	SA		
0.00	$1/2^+$	0.69	0.00	$5/2^{-}$	0.46	0.00	$7/2^{-}$	0.78		
1.27	$3/2^+$	0.83	0.06	$1/2^{-}$	0.58	0.89	$3/2^{-}$	0.66		
2.03	$5/2^+$	0.22	0.12	$3/2^{-}$	0.41	1.11	$13/2^{+}$	0.81		
3.62	$7/2^{-}$	0.62	0.21	$5/2^{-}$	0.33	1.43	$9/2^{-}$	0.92		
4.93	$3/2^{-}$	0.84	0.86	$1/2^{-}$	0.53	1.61	$1/2^{-}$	0.91		
5.95	$3/2^{-}$	0.37	1.04	$9/2^+$	0.79	1.66	$5/2^{-}$	0.64		
6.38	$1/2^{-}$	0.78	1.35	$5/2^+$	0.50	1.79	$9/2^{-}$	0.58		
			1.86	$1/2^+$	0.33	2.71	$13/2^{+}$	0.55		
			4.40	$1/2^+$	0.52					
			4.78	$1/2^+$	0.65					

deformation in the ground state is accounted for by taking both the $L = 0$ and $L = 2$ components explicitly, the continuum states are calculated as purely $L = 0$, 1, 2 states. This approximation which omits some terms of the full orthogonal combinations is seemingly nontrivial. However, in addition to the ground state, the 5/2[−] inelastic state at energy 2.43 MeV and the 7/2[−] resonance state at 6.38 MeV are generated using the 5 He + 4 He cluster model. The breakup calculations including these states along with the 5 He + 4 He nonresonant continuum are performed. The ${}^{5}He + {}^{4}He$ continuum model space in momentum is limited to $0 \le k \le 0.8$ fm⁻¹. The discretization scheme is suitably modified to take into account the resonances.

In the alternate cluster picture, the ${}^{8}Be + n$ cluster structure of $9Be$ is assumed. The ground-state wave function of $9Be$ is generated by coupling the valence neutron in the $1p_{3/2}$ state to the 8 Be (0⁺) core configuration. The Woods-Saxon potential parameters (radius and diffuseness) along with a spin-orbit component for the binding of the neutron in 9 Be is taken from Ref. [\[23\]](#page-6-0). The $1/2^+$ and $5/2^+$ resonance states are generated by using the radius and diffuseness parameters the same as that of the ground state while the potential depth is varied. The nonresonant continuum states are generated using the same potential as that of the resonance states. The final CDCC calculations are performed by including the

TABLE I. Optical model potentials used in the CDCC and CRC calculations. For ${}^{5}He$ + target, the same potential of ${}^{4}He$ + target was used with the diffuseness parameter increased by 0.1 fm.

System	V_0 (MeV)	r_0 (fm)	a ₀ (fm)	W_0 (MeV)	r_0 (f _m)	a ₀ (fm)	V_{s} (MeV)	r_{s} (fm)	a_{s} (fm)	W_{s} (MeV)	r_{s} (fm)	a_{s} (fm)	Ref.
${}^{8}Be + {}^{28}Si$	40.0	0.89	0.87	72.7	0.89	0.87							$[29]$
$n + {}^{28}\text{Si}$	141.5	1.29	0.60							2.1	1.29	0.60	$[27]$
4 He + 64 Zn	113.6	1.57	0.46	15.0	1.67	0.18							$[24]$
${}^{8}Be + {}^{64}Zn$	126.0	1.10	0.60	17.3	1.20	0.75							[25]
$n + {}^{64} \text{Zn}$	70.0	1.28	0.57				2.5	1.28	0.57	6.2	1.28	0.57	$[27]$
4 He + 144 Sm	50.5	1.47	0.59	18.7	1.49	0.65							$[26]$
${}^{8}Be + {}^{144}Sm$	140.0	1.06	0.71	112.0	1.06	0.71							[21]
$n + {}^{144}Sm$	70.0	1.30	0.58				2.2	1.30	0.58	5.5	1.26	0.58	$[27]$

FIG. 1. (Color online) The comparison of measured elastic scattering data for the ⁹Be + ²⁸Si system with the coupled chan-
nels calculations from two models: ⁵He + ⁴He (left column) and ${}^{8}Be + n$ (right column). The dashed, dashed-dot-dot, and solid lines are without coupling, only BU couplings, and BU-TR couplings, respectively.

nonresonant continuum and the resonance states. The cluster folding (core-target and valence-target) potentials required in CDCC calculations for constructing $9Be + target$ interaction potential are taken from Refs. [\[21,24–29\]](#page-6-0) as given in Table [I.](#page-1-0) In the final calculations, the depth of real part of optical potential for $n + {}^{144}Sm$ is normalized by a factor 0.8 at ⁹Be incident energies 37 MeV and below, which is needed to explain the data satisfactorily. The same factor is also used

for renormalizing the depth of the real part of optical potential in $n + {}^{28}\text{Si}$ at the lowest (12 MeV) energy.

In addition to CDCC calculations for breakup, the CRC calculations for the one-neutron stripping channel are simultaneously performed to study its effect on elastic scattering for the ${}^{8}Be + n$ model. The CDCC wave function calculated as described previously is used in the post-form transfer transition amplitude $[30,31]$ to include coupling of the BU states to the transfer channels. The optical model potentials used in the exit channels are same as the ${}^{8}Be$ + target potential parameters as listed in Table [I](#page-1-0) in both the cases. The neutron stripping channel, viz., ²⁸Si(⁹Be, ⁸Be)²⁹Si, ⁶⁴Zn(⁹Be, ⁸Be)⁶⁵Zn, and $144\text{Sm}(^{9}\text{Be},^{8}\text{Be})^{145}\text{Sm}$, have positive Q values 6.81 MeV, 6.31 MeV, and 5.09 MeV, respectively. The excited states of the residual nucleus considered in the CRC calculations are chosen where the well-defined spectroscopic information is available in the literature [\[23,32,33\]](#page-6-0) as listed in Table [II.](#page-1-0)

FIG. 2. (Color online) Same as Fig. 1 but for the ${}^{9}Be + {}^{64}Zn$ system.

III. RESULTS AND DISCUSSION

A. Elastic scattering

The measured elastic scattering data along with the calculations for the three systems are shown in Figs. [1–](#page-2-0)3 at

FIG. 3. (Color online) Same as Fig. [1](#page-2-0) but for the ${}^{9}Be + {}^{144}Sm$ system.

a range of energies around and above the Coulomb barrier in each case. The calculations without couplings (uncoupled), only BU couplings, and full breakup plus one-neutron transfer (BU-TR) couplings are shown with dashed, dashed-dot-dot, and solid lines, respectively. The effect of the breakup and transfer on the elastic scattering is evident from the difference between the uncoupled calculations and the results obtained from including all BU couplings and subsequently also including the transfer (in the ${}^{8}Be + n$ model). As can be seen from these figures, at the above Coulomb barrier energies, the 5 He + 4 He model gives significant breakup coupling effects (left column of Figs. [1–](#page-2-0)3). However, at relatively lower energies, more dominant coupling effects are observed in calculations with the ${}^{8}Be + n$ breakup model (right column of Figs. [1–](#page-2-0)3). It is observed that the coupling of the breakup channel leads to a rise in the elastic cross sections at the backward angles for the 5 He + 4 He model. This is usually the behavior of breakup continuum couplings for nuclear systems with weakly bound projectiles. In the ${}^{8}Be + n$ model, however, the calculations show a reduction of elastic cross section from the region of the Coulomb rainbow to the backward angles. Within this model, the coupling effects of breakup are dominant for a wider range of energies for all the systems. In the test CDCC calculations we have verified that the resonances 2.43 MeV, $5/2^-$ state in the case of the ⁵He + ⁴He model and 1.78 MeV, $1/2^+$ in the case of the ${}^{8}Be + n$ model have the dominant contribution in the BU coupling.

With the inclusion of the one-neutron transfer channel, the $8Be + n$ model gives an overall good description of the data for these three systems over the entire energy range. However, the transfer couplings are found to affect the elastic cross-section not as much as the BU couplings. This observation is different from the coupling effects observed in the ${}^{9}Be + {}^{208}Pb$ system, where large coupling effects were observed at lower energy (even up to 10 MeV below the Coulomb barrier) due to one-neutron transfer. In the present systems, the transfer couplings have a general tendency to give a rise in the backward angle elastic cross section which is opposite to the effect observed in the ${}^{9}Be + {}^{208}Pb$ case [\[10\]](#page-6-0). This can be ascribed to the relatively less positive Q value for one-neutron transfer $(+ 2.27 \text{ MeV})$ which leads to better optimum Q-value matching in the latter case.

B. Dynamic polarization potential (DPP)

To understand the observation from the coupling effects in the calculations for the elastic scattering angular distribution in a better way, we have investigated the behavior of the DPP generated due to these couplings. DPP provides a useful way to simulate the influence of breakup and transfer channel coupling effects by solving the single-channel Schrödinger equation for the elastic scattering with an effective potential which comprises the bare potential and the DPP. The real and the imaginary part of the polarization potentials generated by the BU-TR couplings and only BU couplings are calculated using the prescription of Thompson *et al.* [\[22\]](#page-6-0).

The calculated DPPs due to BU couplings in the ${}^{5}He + {}^{4}He$ model for the ${}^{9}Be + {}^{144}Sm$ system in the vicinity of the strong absorption radii (R_{sa}) are shown in Fig. [4.](#page-4-0) It is evident from Fig. [4](#page-4-0) that the BU couplings give rise to repulsive real and

FIG. 4. (Color online) Real and imaginary parts of the DPPs around the strong absorption radius ($R_{sa} = 11.3$ fm) for the ${}^{9}Be + {}^{144}Sm$ system with the ${}^{5}He + {}^{4}He$ model. The potentials are due to the BU couplings.

attractive imaginary DPPs. Similar behavior is also observed for the ${}^{9}Be + {}^{64}Zn$ and ${}^{9}Be + {}^{28}Si$ systems (not shown here). Next, the calculated DPPs due to BU and BU-TR couplings for the ⁸Be + *n* model near the respective R_{sa} values for the 9 Be + 144 Sm, 9 Be + 64 Zn, and 9 Be + 28 Si systems are shown in Figs. 5–7, respectively. The real part of DPPs due to only BU couplings are found to be attractive at larger distances in the case of ${}^{9}Be + {}^{144}Sm$ and ${}^{9}Be + {}^{64}Zn$ systems. However, in the case of the $9Be + {}^{28}Si$ system, the real part of DPPs

FIG. 5. (Color online) Real and imaginary parts of the DPPs around the strong absorption radius ($R_{sa} = 11.3$ fm) for the ${}^{9}Be + {}^{144}Sm$ system with the ${}^{8}Be + n$ model. The potentials are due to the BU-TR couplings (left column) and BU couplings (right column).

FIG. 6. (Color online) Same as Fig. 5 but for the ${}^{9}Be + {}^{64}Zn$ system around $R_{sa} = 9.4$ fm with the ⁸Be + *n* model.

are attractive at the lowest energy (12 MeV), whereas it is repulsive at higher energies.

The attractive nature of the real part of DPP observed in the case of the ${}^{9}Be + {}^{144}Sm$ and ${}^{9}Be + {}^{64}Zn$ systems is slightly reduced due to the inclusion of transfer couplings (left part of Figs. 5 and 6). For the ${}^{9}Be + {}^{28}Si$ system, the transfer and BU couplings considered together (left part of Fig. 7) lead to an overall repulsive real DPP. The repulsive transfer coupling effect is also observed for the $9Be + 144Sm$ and $9Be + 64Zn$ systems, that leads to an overall repulsive real DPP at interior distances. The repulsive coupling effects due to transfer to positive Q-value channels have been pointed out

FIG. 7. (Color online) Same as Fig. 5 but for the ${}^{9}Be + {}^{28}Si$ system around $R_{sa} = 8.2$ fm with the ⁸Be + *n* model.

FIG. 8. Real and imaginary parts of DPPs at the respective R_{sa} due to BU-TR couplings (solid circles) and only BU couplings (empty circles) for the ⁹Be + ²⁸Si, ⁹Be + ⁶⁴Zn, and ⁹Be + ¹⁴⁴Sm systems with the ⁸Be + *n* model. The solid lines are used to guide the eye.

also by Keeley *et al.* [\[9,17\]](#page-6-0). To summarize the observations on DPP, we encounter a peculiar case where the real part of DPP is attractive due to BU couplings and it is repulsive due to transfer couplings contrary to the conventional wisdom. This observation underlines the importance of studying the detailed nature of coupling effects for each weakly bound projectile on a case to case basis, before making predictions about the gross features observed in such reactions. For example, phenomena of the fusion suppression and breakup threshold anomaly observed in many weakly bound nuclei have been often ascribed to the repulsive couplings arising due to breakup mode. However, the repulsive couplings due to the transfer processes and attractive couplings due to the breakup mode as observed here may call for a closer look on these effects before making such inferences or making any further predictions.

To gain further insights, the energy dependence of the DPP arising due to the BU and BU-TR couplings at R_{sa} has been studied. The real and imaginary parts of DPPs at the respective R_{sa} due to BU-TR couplings (solid circles) and only BU couplings (empty circles) for ${}^{9}Be + {}^{28}Si$, 9 Be + 64 Zn, and 9 Be + 144 Sm with the 8 Be + n model are shown in Fig. 8. These calculations have been done with the energy-independent potentials listed in Table [I](#page-1-0) without any renormalization at any energy. From these figures, it is again evident that the inclusion of transfer couplings reduces the strength of real DPPs. The real DPP for the lighter system ${}^{9}Be + {}^{28}Si$ is found to be repulsive while for the $9B + 144S$ m system it is attractive at all energies. The attractive DPP in the latter case implies that a usual threshold anomaly could be present for the $9Be + 144Sm$ system; i.e., at lower energies the real part of the total potential increases in strength (becomes more attractive), while the imaginary part decreases at energies around the Coulomb barrier. However, from Fig. 8 it is observed that the imaginary part of the potential shows an increase in strength at energies near the Coulomb barrier indicating the presence of an unusual threshold anomaly. A similar behavior in the effective potential has been observed in the optical model analysis of measured data for the ${}^{9}Be + {}^{208}Pb, {}^{209}Bi$ systems [\[34\]](#page-6-0). The additional couplings arising due to transfer lead to an effective DPP, the

real part of which is less attractive compared to that given by only BU couplings. While the real part of DPP given by the BU-TR couplings still remains attractive for the relatively heavy target system ${}^{9}Be + {}^{144}Sm$, it turns more repulsive for the light target system ${}^{9}Be + {}^{28}Si$. The ${}^{9}Be + {}^{64}Zn$ system is an intermediate case, where the real DPP at R_{sa} is slightly attractive due to only BU couplings and turns repulsive due to inclusion of transfer couplings. Therefore, it seems that there is a continuous evolution in the behavior of the real part of DPP from the attractive real for the ${}^{9}Be + {}^{144}Sm$ system, to the case of the light target system ${}^{9}Be + {}^{28}Si$, where this is repulsive. Here we would like to remark that the extent of increase in the attractive real potential may be somewhat reduced if the contributions due to continuum couplings in the 5 He + 4 He model are significant.

IV. SUMMARY

To summarize, the effects of breakup and transfer couplings have been studied on elastic scattering in the ${}^{9}Be + {}^{28}Si$, 64 Zn, and 144 Sm systems. The elastic scattering data available around the Coulomb barrier have been utilized for these investigations. Two different cluster models of 9 Be, namely, 5 He + 4 He and 8 Be + *n*, have been investigated. CDCC (breakup) calculations for both the models and CDCC-CRC calculations for the breakup plus one-neutron transfer in the $8Be + n$ model have been performed. We obtained a good agreement of the coupled channels calculations with the available data. The ${}^{8}Be + n$ model gives an overall good description of the data over the entire energy range for all the systems. The calculations for the ${}^{8}Be + n$ model show significant BU coupling effects at lower energies, whereas for the 5 He + 4 He model, large BU coupling effects are seen at energies above the barrier. Detailed investigations using the dynamic polarization potentials show that the attractive real DPP is obtained for the ${}^{8}Be + n$ breakup model for all the systems at energies below the barrier while the repulsive real DPP is obtained for the breakup via the ${}^{5}He + {}^{4}He$ model. In general, larger attractive real DPPs due to couplings of the ${}^{8}Be + n$ breakup are obtained in heavier systems which remain attractive even at energies above the barrier for these

systems. Inclusion of coupling to the single-neutron transfer channel in the ${}^{8}Be + n$ model also gives interesting effects in the present study. In the combined CDCC-CRC calculations, repulsive real DPPs are obtained due to transfer processes at all energies, while an overall attractive real DPP is generated due to the dominance of the breakup in the ${}^{8}Be + n$ model at lower energies. However, the imaginary part of the DPP shows an increasing trend towards the lower energy consistent with the phenomenon of an unusual threshold anomaly.

An extension of the present work would be the comparison of the present results with those obtained from the calculations using the three-body model of $9Be$ in a full four-body CDCC calculation. Such a calculation could provide a unified

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framework for understanding the effects due to both the ⁵He + ⁴He and ⁸Be + *n* models apart from studying the possible pure three-body effects.

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