*β***-delayed neutron and** *γ* **-ray spectroscopy of 17C utilizing spin-polarized 17B**

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(Received 31 January 2013; published 14 March 2013)

Excited states in ¹⁷C were investigated through the measurement of β -delayed neutrons and γ rays emitted in the β decay of ¹⁷B. In the measurement, three negative-parity states and two inconclusive states were identified in ¹⁷C above the neutron threshold energy, and seven $γ$ lines were identified in a $β$ -delayed multiple neutron emission of the ¹⁷B β decay. From these transitions, the β -decay scheme of ¹⁷B was determined. In particular, a de-excitation 1766-keV γ line from the first excited state of ¹⁶C was observed in coincidence with the emitted β-delayed neutrons, and this changes the previously reported β-decay scheme of $17B$ and level structure of ¹⁷C. In the present work, the β-NMR technique is combined with the β-delayed particle measurements using a fragmentation-induced spin-polarized 17B beam. This new scheme allows us to determine the spin parity of $β$ -decay feeding excited states based on the difference in the discrete $β$ -decay asymmetry parameters, provided the states are connected through the Gamow-Teller transition. In this work, $I^{\pi} = 1/2^-$, 3/2⁻, and (5/2⁻) are assigned to the observed states at $E_x = 2.71(2)$, 3.93(2), and 4.05(2) MeV in ¹⁷C, respectively.

DOI: [10.1103/PhysRevC.87.034316](http://dx.doi.org/10.1103/PhysRevC.87.034316) PACS number(s): 21.10.Hw, 23.40.−s, 27.20.+n, 29.27.Hj

I. INTRODUCTION

Neutron-rich carbon isotopes are attracting because of their anomalous level structures. It has been experimentally shown that none of the odd mass neutron-rich carbon isotopes, $15-19$ C, have the ground-state (GS) spin parities of $I^{\pi} = 5/2^{+}$, despite the $d_{5/2}$ valence neutron expected from a naive shell model. In ¹⁵C, having the neutron number $N = 9$, the inversion of single-particle levels between $d_{5/2}$ and $s_{1/2}$ is suggested from the GS spin parity of ¹⁵C, I_{GS}^{π} = 1/2⁺ [\[1,2\]](#page-15-0). Intriguingly, the further neutron-rich nucleus ¹⁷C with $N = 11$, was shown to have $I_{\text{GS}}^{\pi} = 3/2^+$. This I_{GS}^{π} assignment was performed through the study of GS properties based on the direct reaction [\[3–7\]](#page-15-0), β-delayed neutron spectroscopy of the β decay of ¹⁷C [\[8\]](#page-15-0), and magnetic moment of ${}^{17}C$ [\[9\]](#page-15-0). In the extremely neutronrich nucleus ¹⁹C with $N = 13$, the I_{GS}^{π} value again becomes $1/2^+$; this was confirmed and discussed in connection with the formation of a neutron halo $[6,10,11]$.

In these neutron-rich carbon isotopes, unlike the valence protons, which occupy the p shell, the valence neutrons occupy the sd shell, where the p -sd cross-shell interactions characteristically play an important role. To gain an understanding of these intriguing properties of p-sd neutron-rich carbon isotopes, it is important to investigate not only the GS but also the structure of the excited states, because those negative-parity states can be described such that one particle in the p shell of the low-lying positive parity states is excited to the sd shell, and thus, their energy differences from the low-lying positive-parity states are expected to reflect directly such the effective interactions.

With regard to the excited states of ^{17}C , the existence of three low-lying positive-parity states has been proposed at $E_x \sim 210$, 295, and 330 keV below the one-neutron threshold energy $S_n = 0.729(18)$ MeV [\[12\]](#page-15-0). An excited state observed at $E_x = 295(20) \text{ keV} [13]$ $E_x = 295(20) \text{ keV} [13]$ in the ⁴⁸Ca(¹⁸O, ¹⁷C)⁴⁹Ti reaction was again observed at $E_x = 295(10)$ for the same reaction, carried out at a slightly higher beam energy [\[14\]](#page-15-0). However, the 295-keV state was interpreted to be a background (BG) event during the in-beam γ -ray spectroscopy performed with a ¹⁷C beam [\[15\]](#page-15-0). Two more excited states were observed at $E_x =$ 207(15) keV and 329(5) keV in the two-step fragmentation reaction [\[16\]](#page-15-0). Two corresponding energy levels were observed, i.e., $E_x = 210(4)$ keV and 331(6) keV, in the $p(^{19}C, ^{17}C\gamma)$ reaction, for which I^{π} values were assigned as $1/2^+$ and $5/2^+$, respectively [\[17\]](#page-15-0). The same I^{π} assignments were identified in the one-neutron removal reaction of ${}^{18}C$ from a proton target, wherein a coupled-channel analysis was performed for the corresponding levels $E_x = 210$ keV and 330 keV [\[18\]](#page-16-0), and

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in the lifetime measurement, in which case the M1 transition strengths were discussed for the observed 212(8)- and 333(10) keV states [\[19\]](#page-16-0). For high-lying states, 13 positive-parity states, including the $E_x = 310(30)$ keV level, have been observed up to $E_x = 16.3$ MeV in the study of the ¹⁴C(¹²C, ⁹C)¹⁷C reaction [\[20\]](#page-16-0).

Even then, only a few studies have been conducted on the negative-parity states in ${}^{17}C$. For studying negative-parity states in ^{17}C , it is useful to perform the β -decay study of $17B$. In the light mass region of neutron-rich nuclei, the parity of sd -valence neutrons differs from that of p -shell valence protons, whereby β -decay allowed transitions feed negative-parity states [\[21\]](#page-16-0). Hence, a β -decay study is useful for studying neutron-rich nuclei located away from the stability line, owing to the large Q_β windows. Over the past several years, a number of such studies have been performed on the structure of light-mass neutron-rich nuclei through the time-of-flight (TOF) measurement of emitted β -delayed neutrons [\[8](#page-15-0)[,22–25\]](#page-16-0).

In the present work, we performed the spectroscopic study of β-delayed neutrons and γ rays in the β decay of ¹⁷B in order to investigate the level structure of ¹⁷C [hereafter, β -delayed neutron(s) and β-delayed γ ray(s) are denoted as β-n and $β$ -γ, respectively]. The $β$ -n measurement of the ¹⁷B $β$ decay has thus far been reported in Ref. [\[24\]](#page-16-0), and in this study, several β -decay transitions to the excited states in ¹⁷C above the neutron threshold energy, which were followed by neutron emission, were observed. However, in the construction of the decay scheme, all transitions observed in a one-neutron (1n) emission channel were assumed to be directly connected to the GS of ${}^{16}C$. To identify the final states in ${}^{16}C$ subsequent to the β -n emissions, we also conducted γ -ray measurements in coincidence with the β rays and neutrons. Moreover, it should be noted that this measurement was combined with a technique of fragmentation-induced spin polarization [\[26,27\]](#page-16-0). Thus, the GS of ^{17}B , as an initial state of β decay, was spin polarized. The angular distribution of the β decay through the Gamow-Teller (GT) transition from a spin-polarized nucleus is known to show anisotropy with respect to the polarization axis, and it is characterized by $A_{\beta}P$, where A_{β} denotes the asymmetry parameter of the corresponding GT transition given by the I^{π} value of the initial and final states and P denotes the polarization of the parent nucleus. Since P is common to all the transitions, the final state I^{π} can be assigned such that A_{β} becomes proportional to the experimentally determined $A_{\beta}P$ values when the initial state I^{π} is known. For the first time, by using this new method, the I^{π} values of the excited states in ${}^{15}C$ have been successfully assigned with the spin-polarized $15B$ beam [\[28\]](#page-16-0). Furthermore, by taking the advantage of highly spin-polarized Li and Na beams, the nuclear structures of 11 Be $[29]$ and ²⁸Mg $[30]$ have been studied through the spin-parity assignment of the excited states.

II. EXPERIMENTAL PROCEDURE

A. Production of spin-polarized 17B beam

A spin-polarized ^{17}B beam was produced using the same procedure as described in Ref. [\[31\]](#page-16-0), in which the fragmentation-induced spin polarization technique was

adopted $[26,27]$. A beam of ¹⁷B was obtained from the fragmentation of a ²²Ne projectile with an energy of $E/A =$ 110 MeV and a current of 90 particle-nA incident on an 93 Nb target having a thickness of 1.07 g/cm². To obtain a spin-polarized ^{17}B beam, the emission angles and outgoing momenta of the ^{17}B fragments were suitably selected [\[26,27\]](#page-16-0). Thus, fragments emitted within radial angles $\theta_L = 1.5^\circ - 5.0^\circ$ and azimuthal angles $|\phi_L| \leq 2.0^\circ$ along with the primary beam were accepted by the RIKEN projectile-fragment separator RIPS [\[32\]](#page-16-0), using a beam swinger installed upstream of the target. A range of the momentum values, i.e., $p = 7.11$ to 7.55 GeV/ c , was selected with the help of a slit at the intermediate momentum-dispersive focal plane. This momentum range corresponds to the range $1.01p_0-1.07p_0$, where $p_0 = 7.03$ GeV/c is the fragment momentum corresponding to the projectile velocity. The isotope separation was given by the combined analyses of the magnetic rigidity and the momentum loss in a wedge-shaped degrader [\[32\]](#page-16-0) with a median thickness of 1638 mg/cm² and a slope angle of 8.67 mrad.

The spin-polarized and isotope-separated $17B$ fragments were then introduced into an apparatus located at the final focus of RIPS, for the β -delayed particle measurement. They were implanted in a Pt stopper located at the center of the apparatus, which consisted of a stack of four 100 - μ m-thick Pt plates. The beam implantation was confirmed with plastic scintillators placed upstream and downstream of the Pt stopper. The upstream counter was used to distinguish the $Z > 4$ beam particles from contaminating tritons. Under the conditions described above, RIPS provided a 17B beam with a purity of ∼100%, not considering tritons, and an intensity of 17.3 particles per second (pps).

B. Detector apparatus

We combined the β -ray detected nuclear magnetic reso-nance (β-NMR) technique [\[33\]](#page-16-0) with the β-delayed particle emission measurement. A static magnetic field, $B_0 = 50.0$ mT, whose inhomogeneity was $\Delta B_0/B_0 \leq 10^{-2}$, was applied to the Pt stopper with a Helmholtz-type air coil to preserve the spin polarization of 17B. The effective diameter of the coil was $\phi = 250$ mm. β Rays emitted from the implanted fragments were detected with β -ray telescopes, consisting of two plastic scintillators, located above and below the Pt stopper. To exclude BG events, such as those involving cosmic muons, coincidences with signals from the other side of the $β$ -ray telescope were checked as soon as a $β$ ray was detected.

The β -n emitted from the implanted ^{17}B were measured with a high-energy neutron detector array [\[25,28\]](#page-16-0), consisting of a set of 12 plastic scintillators, whose shapes were curved in the vertical direction with a 150-cm radius, 160-cm arc length, and 40-cm latitudinal width in the median plane. The achieved electron-equivalent threshold energy, $E_{\text{th}} = 3.4(27)$ keVee, of the neutron detector array, enabled the detection of low-energy neutrons at $E_n \sim 0.5$ MeV, and an efficiency of 5.6% for ∼1 MeV neutrons was achieved as a result. A high-energy neutron detector array was placed 1.5 m away from the Pt stopper, as shown in Fig. [1,](#page-2-0) covering the solid angles $\Omega_n = 0.21 \times 4\pi$ sr. In this configuration, neutrons

FIG. 1. Arrangement of the high-energy and low-energy neutron detector arrays.

emitted vertical to the β -ray direction were detected, which minimized the neutron-energy broadening due to β -ray recoil effects. The neutron energies were determined using the TOF method, wherein the β -ray signal was used as the start pulse. The signal was read out from photomultiplier tubes (PMTs) attached at each end, and both the read-out signals were used to determine the correct TOF by calculating the mean time. Neutrons within the energy range $E_n = 0.5 \sim 10$ MeV were analyzed with this high-energy neutron detector array.

The detection efficiency of the neutron detector array was determined using ¹⁵B and ¹⁷N beams, whose β -decay branches associated with β -n emission are known [\[22,34\]](#page-16-0). Using these calibration data, the efficiency was determined as a function of the energy E_n , based on the simulation code given in Ref. [\[35\]](#page-16-0), where the reduction of photopropagation in the plastic scintillator was taken into account. Details pertaining to the high-energy neutron detector array are given in Ref. [\[28\]](#page-16-0). For the measurement of neutrons having an energy down to $E_n \geq 0.01$ MeV, a low-energy neutron detector array [\[25\]](#page-16-0) covering the solid angle $\Omega_n = 0.037 \times 4\pi$ sr was placed on a concentric circle to achieve a distance of 0.5 m from the Pt stopper, which consisted of a set of 10 45 mm \times 25 mm \times 300 mm plastic scintillators. The signal was read out from the PMTs attached at each end. The threshold energy was set to 2 keVee using the Compton edge of $137Cs$.

In addition to the neutron counters, a 50 mm^{ϕ} \times 70 mm Clover Ge detector [\[36\]](#page-16-0) and a set of four 80 mm \times 80 mm \times 152 mm NaI(Tl) detectors were placed above and below the β -ray telescope, as shown in Fig. 2. The PMTs housed in the NaI(Tl) detectors are a type of fine-mesh dynodes, which can be operated under strong magnetic fields with strengths of over 1 T [\[37\]](#page-16-0). In front of each Ge and NaI(Tl) detector, 2-mm-thick plastic scintillators were placed to distinguish γ and β rays. With the help of these plastic scintillators, NaI(Tl)

FIG. 2. Schematic layout of the setup around a Pt stopper, showing NaI(Tl) and Ge γ -ray detectors and a β -NMR system.

detectors were used to measure not only γ -ray energies but also the β-ray total energy, E_β , for up to 30 MeV, which covers a Q_{β} (¹⁷B) of 22.68(14) MeV [\[12\]](#page-15-0). The E_{β} data were calibrated for a sufficiently wide range using ¹⁷N and ¹⁵B, whose Q_β values are 8.680(15) and 19.094(22) MeV, respectively [\[12\]](#page-15-0).

C. Block diagram

The conventional block diagram for β -NMR measurements shows a beam being pulsed with a beam bombardment period of T_B . At the beginning of the beam-off period in these measurements, the oscillating magnetic field B_1 is applied for a duration of T_R , with its frequency swept over a Larmor frequency to reverse the direction of the spin polarization by means of the adiabatic fast passage (AFP) NMR method [\[38\]](#page-16-0). Then, β rays are counted during the following period, $T_{\rm C}$. This unit cycle, $T_{\rm B} + T_{\rm R} + T_{\rm C}$, is repeated many times until sufficient statistics have been accumulated. Note that the time length of the unit cycle is generally set to $2/\lambda$, where λ is the decay constant of the nuclei of interest. Through the execution of this sequence, a maximum figure of merit given by $Y_\beta \times P^2$ is achieved, where Y_β is the β -ray counting rate and P is the nuclear spin polarization. Ideally, T_B should be set by taking into account the spin-lattice relaxation time of the nuclei. The β-ray counting rate $Y_β$ is then given by

$$
Y_{\beta} = \frac{I_{\rm B}e^{-\lambda T_{\rm R}}(1 - e^{-\lambda T_{\rm B}})(1 - e^{-\lambda T_{\rm C}})}{\lambda(T_{\rm B} + T_{\rm C} + T_{\rm R})(1 - e^{-\lambda(T_{\rm R} + T_{\rm C})})},\tag{1}
$$

where I_{B} is the beam-implantation rate during the period T_{B} . In this sequence, however, ∼50% of the beam needs to be blocked, despite the low production yield of the ¹⁷B beam.

For more efficient measurements, the block diagram was improved in the present study, and it is illustrated in Fig. [3.](#page-3-0) The beam was not pulsed periodically at fixed durations. Instead, as

FIG. 3. Block diagram for the β -delayed neutron and/or γ -ray measurement combined with the AFP-NMR technique. $T_{\rm B}$, $T_{\rm R}$, and $T_{\rm C}$ are the duration of the 17 B beam bombardment; the application of the B_1 field; and the β , neutron, and γ particle detection. T_R and $T_{\rm C}$ are fixed, while $T_{\rm B}$ is not fixed and remains open until a ¹⁷B particle is implanted. The β -decay rate Y_β , as the function of the ¹⁷B implantation rate, of the new *beam-waiting* mode was compared with that of the fixed beam-on and -off cycle mode. For details, see the text.

soon as a ¹⁷B particle was identified by the beam-line counters equipped with RIPS, the beam bombardment was turned off for 19.5 ms. At the beginning of the beam-off period, the B_1 field \simeq 1.6 mT was applied for a duration of $T_R = 1.5$ ms, and in this duration, the frequency of B_1 was swept over the Larmor frequency v_0 of ¹⁷B [\[31\]](#page-16-0) in the frequency window $\Delta v/v_0$ = 2%. Then, the β rays, in addition to γ rays and neutrons, were measured during a subsequent time period of $T_C = 18$ ms. After the beam-off period, the beam bombardment was again turned on until the next ¹⁷B particle was detected. The B_1 field was applied every two beam-off cycles, to ensure that the direction of the spin polarization would change alternately; this reduced the systematic error due to differences in the efficiencies of the two β -ray telescopes and long-term beamprofile fluctuation. The Y_β yield in this *beam-waiting* mode is given by

$$
Y_{\beta} = \frac{I_{\rm B} (e^{-\lambda T_{\rm R}} - e^{-\lambda (T_{\rm R} + T_{\rm C})})}{1 + I_{\rm B} (T_{\rm R} + T_{\rm C})}.
$$
 (2)

Based on Eqs. [\(1\)](#page-2-0) and (2), the yields of ¹⁷B Y_β were calculated, for the purpose of comparison, as a function of the intensity of a 17B beam in the fixed beam-on and -off cycle mode and the *beam-waiting* mode, where $(T_{\rm B}, T_{\rm R}, T_{\rm C}) = (7.3, 1.5, 7.3)$ ms was assumed as a typical sequence in the former mode. As shown in the inset of Fig. 3, $Y_\beta = 9.6$ counts per second (cps) for the *beam-waiting* mode, and it is 2.6 times larger than $Y_\beta = 3.6$ cps, which is observed for the fixed beam-on and -off cycle mode under an actual ¹⁷B intensity of $I_B =$

17.3 pps. Factually, 12.9-pps ^{17}B particles were implanted at the intensity of $I_B = 17.3$ pps because of the dead time due to the 19.5-ms beam blocking period $T_R + T_C$. This effect is already considered in Eq. (2).

Another important advantage of the new *beam-waiting* mode is the high S:N ratio in the β -ray measurements. Given the reported multiple neutron emission probabilities in the ¹⁷B β decay [\[39\]](#page-16-0), 3.6 β rays are emitted on an average in the β-decay chain initiated by one $17B$ β decay. Since all decay-chain nuclei have significantly longer lifetimes than ¹⁷B, the BG β rays from these nuclei are assumed to be detected with the same probability inside $T_{\rm C}$ windows. For $I_{\rm B} = 17.3$ pps, the S/N ratio in the fixed beam-on and -off mode is $S(3.6 \text{cps}):N(16.8 \text{cps}) = 0.22$, whereas in the *beam-waiting* mode, the S:N ratio is 4.3 times better and has the value $S(9.6 \text{cps}):N(10.5 \text{cps}) = 0.92.$

D. Principle of the spin-parity assignment

The angular distribution function $W(\theta)$ for the β rays emitted from $17B$ with the spin polarization P is given by

$$
W(\theta) \propto 1 + (v/c)A_{\beta}P\cos\theta, \tag{3}
$$

where θ denotes the angle between the direction of the β emission and the axis of the nuclear polarization, v and c are the velocities of the β particles and light, respectively, and A_{β} is the asymmetry parameter. For simplicity, we use the approximation $v/c \approx 1$, since only a high-energy portion of the β spectrum is included in the analysis. Then, the asymmetry $A_{\beta}P$ of the β -decay transition feeding neutron emissions is given by

$$
A_{\beta}P = \frac{\sqrt{\rho} - 1}{\sqrt{\rho} + 1}.
$$
 (4)

Here, using the measured β -n spectra recorded with the identification of the signal-detected β -ray telescope, the double ratio ρ in Eq. (4) is given by

$$
\rho = \left(\frac{N_{\rm U}}{N_{\rm D}}\right) / \left(\frac{N_{\rm U}^*}{N_{\rm D}^*}\right),\tag{5}
$$

where $N_{U,D}$ are the relevant peak counting rates in the neutron TOF spectra measured in coincidence with signals from the β -ray telescopes located above (denoted by U) and below (denoted by D) the Pt stopper and $N_{\text{U,D}}^*$ are those obtained with the resonant B_1 -field application. With the obtained $A_\beta P$ values, asymmetry parameters A_β can be determined provided the polarization P is known.

In the case that the spin I_i state decays through the pure GT β^{\mp} -decay transitions associated with the spin change ΔI , the β-decay asymmetry parameter $A_β$ value is given by

$$
A_{\beta} = \begin{cases} \mp 1 & (\Delta I = -1) \\ \mp 1/(I_{i} + 1) & (\Delta I = 0) \\ \pm I_{i}/(I_{i} + 1) & (\Delta I = +1) \end{cases}
$$
 (6)

By comparing the determined A_β values to the value given in Eq. (6), the final spin-parity I_f^{π} can be determined in the case of a pure GT β decay.

To apply this method, it is necessary to know I_i^{π} and one I_f^{π} value from among the GT β -decay transitions for the determination of the spin polarization P . In the present experiment, $I_i^{\pi} = 3/2^-$ is known for the GS of ¹⁷B [\[31\]](#page-16-0), whereas none of the final state I_{f}^{π} values are known. Therefore, similar to the I^{π} assignment for ¹⁵C [\[28\]](#page-16-0), the following method was performed.

For a given set of GT transitions to the level I_f^j (j=1, 2, ..., n), there are 3^n combinations of the possible A_β values. For each allocated A_{β} value, the polarization is evaluated as $P_j =$ $(A_{\beta}P)_{i}/A_{\beta}$, where $A_{\beta}P_{i}$ is the measured asymmetry. For the proper combination of A_β values, i.e., for the correct spin assignments for all relevant final states, the evaluated P_i values need to be consistent with each other. It is therefore expected that for improper combinations of A_β values, the expected value of P will have systematic errors and the variance of P will increase. In other words, a correct assignment should reveal the least variance of P. This is the guiding principle for determining I_f^{π} values simultaneously. For the *i*th set of A_{β} values, the mean spin polarization \bar{P}_i is calculated as

$$
\bar{P}_i = \frac{\sum_j P_j w_j}{\sum_j w_j} p,\tag{7}
$$

where w_i is the statistical weight factor for each P_i value,

$$
w_j = \frac{A_{\beta}^2}{\sigma_{(A_{\beta}P)_j}^2},
$$
\n(8)

with the experimental error $\sigma_{(A_\beta P)_j}$ for $(A_\beta P)_j$. By definition, the reduced χ^2_{ν} for the *i*th set is given as

$$
\chi_{\nu}^{2}(\bar{P}_{i}) = \frac{1}{\nu} \sum_{j} (P_{j} - \bar{P}_{i})^{2} w_{j} \quad (i = 1, 2, ..., 3^{n}), \quad (9)
$$

where v denotes the degree of freedom ($\nu = n - 1$). The abovementioned guiding principle is that the most probable set of A_{β} values should yield the least χ^2_{ν} among the 3ⁿ values for all possible combinations of $A_{\beta i}$ values. In such a case, \bar{P}_i can be regarded as the statistically expected spin polarization P , whose error is defined by

$$
\sigma_{\bar{P}_i} = \frac{\sum_j (\bar{P}_i - P_j)^2 w_j}{\sum_j w_j}.
$$
\n(10)

III. ANALYSIS AND RESULTS

The ¹⁷B nucleus has the ground-state spin parity I^{π} = 3/2⁻. Its β decay, whose halflife is $t_{1/2} = 5.08(5)$ ms and Q_{β} is 22.68(14) MeV [\[12\]](#page-15-0), can be characterized by a β -delayed multiple neutron emission [\[39,40\]](#page-16-0), for which multiplicities M_n of up to four have been reported [\[39\]](#page-16-0). In the following analysis, the decay property was investigated by classifying the multiplicity of the emitted β -n.

A. 0n-decay branches

The 0n mode of the ¹⁷B β decay, i.e., a β decay not followed by β -n emission, can feed excited states in ¹⁷C below the neutron separation energy $S_n = 0.729(18)$ MeV

or the GS. Until now, the existence of three excited states has been suggested at the excitation energy values $E_x \sim$ 210 keV [\[16–](#page-15-0)[19\]](#page-16-0), 295 keV [\[13,14\]](#page-15-0), and 331 keV [\[16](#page-15-0)[–20\]](#page-16-0), below $S_n = 0.729(18)$ MeV. Investigation of these three states is a central subject for the 0n channel.

1. γ -Ray energy spectra obtained from the β-γ coincidence measurements

The observed γ -ray energy peaks below $S_n = 0.729(18)$ MeV, measured with the Ge detector in coincidence with the β ray from ¹⁷B, are summarized in Table I. For a comparison, details of γ rays observed in a BG measurement without a beam and in a detector-calibration measurement with an ¹⁷N beam are also listed in Table I. First, the γ rays observed in the BG measurement, i.e., $E_{\nu} = 77(2)$, 242(1), 352(1), and 609(2) keV, as well as the 511-keV annihilation γ ray, can be excluded from the ¹⁷B β - γ candidates. They can be assigned to KX or the γ rays from the lead parts of the experimental setup, in which some amount of the U/Th decay-chain isotopes ²¹⁴Pb and 214Bi are considered to be included. The reason that the 242(1)-keV γ ray was not observed in the ¹⁷N measurement is not clear. This may be attributable to the short measurement time. Next, the γ rays observed in the ¹⁷N β - γ measurement, i.e., $E_y = 596(5)$ and 696(8), can be also excluded. They originate from the (n, γ) or (n, n' γ) reactions, given that their shapes are broadened and skewed towards higher energy, which is a typical feature that reveals the neutron-recoil effect in Ge detectors. Here, a 67(1)-keV peak observed in both the

TABLE I. Energies of the γ -ray observed as a peak in the β - γ coincidence measurements with ^{17}B and ^{17}N beams below the ^{17}C neutron-threshold energy $S_n = 0.729(18)$ MeV, obtained using the Ge detector, together with those observed without a beam. Circles are used to indicate that they were observed in each measurement. Possible γ -ray origins are listed together in the last column, provided their energies agree with the experimental values.

E_{γ}	No	$17N$?	17 _B	Possible background		
(keV)	beam	$\beta-\gamma$	$\beta-\gamma$	Sources	(keV)	
	\times		\circ	$\text{KX}_{\alpha1}(\text{Pt})$	66.8	
67(1)		\circ		73 Ge m	66.6	
				$\text{KX}_{\alpha1}(\text{Pb})$	75.0	
77(2)	\circ	\circ	\circ	$\text{KX}_{\beta 1}(\text{Pt})$	75.7	
				$\text{KX}_{\alpha 1}(\text{Bi})$	77.1	
88(2)	\times	\times	\circ	$\text{KX}_{\beta 1}(\text{Pb})$	87.3	
217(2)	X	\times	\circ	(^{228}Ac)	(216.0)	
				^{212}Pb	238.6	
242(1)	\circ	\times	\circ	224 Ra	242.0	
				$^{214}{\rm Pb}$	241.0	
295(2)	X	\times	\circ	(^{214}Pb)	(295.2)	
331(2)	\times	\times	\circ	(^{228}Ac)	(328.0)	
352(1)	\circ	\circ	\circ	$^{214}{\rm Pb}$	351.9	
511(2)	\circ	\circ	\circ	Annihilation	511.0	
596(5)	\times	\circ	\circ	$^{73}Ge(n, \gamma)$	596.4	
				74 Ge(n, n' γ)		
609(2)	\circ	\circ	\circ	^{214}Bi	609.3	
696(8)	X	\circ	\circ	$^{72}Ge(n,n'\gamma)$	693	

¹⁷B and the ¹⁷N measurements can be assigned to the $\text{KX}_{\alpha1}$ rays originating from the Pt stopper excited by the β rays. The remaining γ -ray peaks at 295(2) and 331(2) keV, as well as a small peak at $E_{\gamma} = 217(2)$ keV, are thus the potential γ rays emitted from ${}^{17}C$ subsequent to the ${}^{17}B$ β decay.

2. Properties of the peaks at E^γ **=** *217, 295, and 331 keV*

Properties of these γ rays were then investigated in terms of the total energy of the feeding β ray, which was measured with the set of NaI(Tl) detectors and 2-mm-thick plastic scintillators described in Sec. [II B.](#page-1-0) The de-excitation γ rays from low-lying excited states of ${}^{17}C$ are associated with large β -ray energies, where the maximum β -ray energies are $E_{\beta}^{\max} \geqslant Q_{\beta} - \overline{S_n} \simeq$ 22 MeV, owing to the small S_n value. Thus, an E_γ spectrum was obtained, as shown in Fig. 5(a), by gating the E_y spectrum shown in Fig. 4(a) with the β -ray energy at $E_\beta \geq 10$ MeV. We note that the 331(2)-keV γ ray was still observed, while the 295(2)-keV peak disappeared. In addition, a minor peak at $E_v = 217(2)$ keV, as seen in Fig. 4(a), is clearly observed in Fig. $5(a)$. Although the Th decay-chain isotope ²²⁸Ac could be a possible BG event, the 217(2)-keV γ ray was observed

FIG. 4. γ -Ray energy spectra obtained with the Ge detector in coincidence with the β ray. The spectra were obtained with the counting periods T_C of (a) and (b) 18 ms and (c) 250 ms.

FIG. 5. Obtained γ -ray energy spectra measured with the Ge detector by gating with (a) β -ray energies $E_\beta > 10$ MeV, (b) neutron multiplicity $M_n \ge 1$, and (c) γ -ray energy E_γ < 400 keV measured with NaI(Tl) detectors.

in neither the BG nor $17N$ measurements, suggesting that the 217(2)-keV peak as well as 331(2)-keV peak originate from the $^{17}B \beta$ decay.

These γ rays were further investigated to determine their decay parent nuclei based on (i) the coincidence to β -n emission and (ii) the time evolution of the γ -ray peak counting rates. For determining (i), a γ -ray energy spectrum obtained with the Ge detector was plotted for β -n- γ triple coincidence events. From the resulting E_{γ} spectrum shown in Fig. 5(b), no peaks were identified within the given statistics at $E_y =$ 217(2) and 331(2) keV, indicating that these γ rays were not associated with neutron-emission channels in the ¹⁷B β decay. As described by point (ii), the time evolution of the photopeak counting rates was deduced to identify a parent nucleus. A time stamp recorded with E_{γ} was the time of a $β$ -γ coincidence event measured from the arrival time of a ¹⁷B particle, which started at T_C , as shown in Fig. [3.](#page-3-0) Thus, the time evolution in this analysis provides the β -decay lifetime of a parent nucleus feeding the relevant γ emission. The obtained time spectra for $217(2)$, $295(2)$, and $331(2)$ keV are shown in Figs. $6(a)$, $6(c)$, and $6(d)$, respectively. Dotted lines shown in

FIG. 6. Time evolution of the photopeak counts of the observed $\beta-\gamma$ lines measured with the Ge detector in the ¹⁷B β decay. The vertical bar shows the statistical error, and the horizontal bar represents the time-slice window. The dotted line curve shows the result of the χ^2 -fitting analysis using an exponential function with the known half-life of ¹⁷B, $t_{1/2} = 5.08(5)$ ms; plus a constant is used. Values R indicated in each panel show the ratio of the exponential component to the total counts. The spectrum of (a) 217(2) keV is obtained for an additional coincidence with a β ray having $E_\beta > 10$ MeV measured with the NaI(Tl) detector. Furthermore, the spectra (q) and (r) are obtained with a measurement conducted separately by expanding T_C to 250 ms for investigating components with a long lifetime.

the spectra represent the result of a least χ^2 fitting analysis with an exponential function having a known ^{17}B half-life, $t_{1/2}$ (^{17}B), plus a constant. The time spectra of 217(2) and 331(2) keV are well reproduced by $t_{1/2}$ (^{17}B), unlike the time spectrum of 295(2) keV, which is rather flat, suggesting a long lifetime of the feeding β decay. This flat spectrum is similar to the 242(1)-keV γ line in Fig. [6\(b\),](#page-6-0) which is a BG γ emission line. With regard to the two points described above, we concluded that the 217(2)- and 331(2)-keV γ rays are emitted subsequent to the ¹⁷B β decay in the 0n channel, while the 295(2)-keV γ rays is emitted by long-lifetime daughter isotopes produced in the β -decay chain from ¹⁷B. The source of the 295(2)-keV γ ray was not identified due to its long lifetime, as compared with the present value of the counting period $T_{\rm C} = 18$ ms.

Finally, an E_{γ} spectrum obtained from the $\beta-\gamma-\gamma$ triple coincidence measurement was plotted to determine whether the 217(2) and 331(2)-keV γ rays can be assigned to a direct transition to the GS or a cascade transition. The second ν -ray coincidence was detected with the set of thin plastic scintillators and NaI(Tl) detectors mentioned above, wherein the signal from the plastic scintillator was used to remove $β$ -ray events. Figure [5\(c\)](#page-5-0) shows an $E_γ$ spectrum obtained in coincidence with the second γ ray at $E_{\gamma} \le 400$ keV, measured with the NaI(Tl) detectors. This energy value was selected to investigate the cascade decay below the neutron threshold $S_n = 0.729(18)$ MeV. Since no peaks were found at the energy values $E_y = 217(2)$ and 331(2) keV in Fig. [5\(c\),](#page-5-0) we concluded that these two γ rays are emitted from the levels $E_x = 217(2)$ and 331(2) keV during the transition to the GS in ^{17}C .

3. Other γ lines

Other observed γ lines, whose sources are not clear, are plotted in Fig. [6.](#page-6-0) The time evolution of the γ lines at E_{γ} $= 743(3)$, 1767(6), 2212(10), 2322(6), and 2379(7) keV, as shown in Figs. $6(e)$, $6(1)$, $6(n)$, $6(0)$, and $6(p)$, respectively, are well reproduced by $t_{1/2}$ (¹⁷B), indicating that these γ lines were directly fed by the ^{17}B β decay, without the involvement of any daughter isotope β decays. As shown in Fig. 7, the 743(3)-keV γ line was identified as the de-excitation γ line of the $I^{\pi} = 5/2^{+}$ state at $E_x = 743(2) \text{ keV} \rightarrow 1/2^{+} \text{ GS in}$ ¹⁵C, while the γ lines at $E_{\gamma} = 1767(6)$, 2212(10), 2322(6), and 2379(7) keV were identified as the de-excitation γ lines from the $E_x = 1766(10)$, 3986(7), 4088(7), and 4142(7) keV states in ¹⁶C, respectively. The γ line at $E_{\gamma} = 4782(10) \text{ keV}$ observed in Fig. [4\(c\)](#page-5-0) agrees with the γ line of 4780(100) keV \rightarrow GS for ¹⁵C. As shown in Fig. [6\(q\),](#page-6-0) however, its time evolution is flat, suggesting that the feeding β decay is different from the ¹⁷B β (-n) decay. Its source was not identified in this study. In all $β$ -decay channels associated with $β$ -n emission, the time evolution becomes flat for the given $T_{\rm C}$ window due to the long lifetimes of the daughter nuclei. The γ lines at $E_{\gamma} = 1382(5)$ and 1855(8), shown in Figs. [6\(j\)](#page-6-0) and $6(m)$, respectively, correspond to the de-excitation γ lines at 1373.8(3) and 1849.5(3) keV in ¹⁷N, which are β - γ decays of the daughter nucleus ¹⁷C in the 0n channel of the ¹⁷B β decay. Furthermore, in the 2n channel, the γ line observed at 5290(12) keV was identified as the 5298.822(14)-keV γ line in the ¹⁵C β - γ decay. Other peaks at $E_{\gamma} = 770(2)$, 936(2),

FIG. 7. Observed γ lines in the decay chain initiated by the ¹⁷B β decay. The observed and identified γ lines are shown by open arrows.

1123(3), and 1242(5) keV were also investigated by studying their time evolution, as shown in Figs. $6(f)$, $6(g)$, $6(h)$, and $6(i)$, respectively; no direct correlation of these peaks with the ¹⁷B β decay was observed. They were likely emitted from the decay chain; however, the transitions that caused these peaks could not be identified in this study.

4. Transition strengths in the 0n channel

Strengths I_{γ} of the observed γ lines per ¹⁷B β decay were determined using the following equation:

$$
I_{\gamma} = \frac{N_{\gamma}}{N(\mathbf{1}^7 \mathbf{B}) \cdot \epsilon_{\gamma} \Omega_{\gamma} \cdot \epsilon_{\beta} \Omega_{\beta} \cdot R_{\beta}}.
$$
 (11)

Here, N_{γ} is the photopeak count, $N(^{17}B)$ are implanted ¹⁷B particles, $\epsilon_{\gamma} \Omega_{\gamma}$ and $\epsilon_{\beta} \Omega_{\beta}$ are, respectively, the overall detection efficiencies of the Ge detector and the β -ray telescopes, including their solid angles, which are evaluated based on the simulation code of GEANT [\[41\]](#page-16-0). R_β is the probability that a β decay of a parent nucleus is directly feeding a relevant β - γ -ray emission within the duration $T_{\rm C}$. The R_{β} values were obtained from a simulation based on the following equation:

$$
R_{\beta} = \sum_{i} \int_{0}^{T_{i}'} dt f(t; \lambda_{1}) F(T_{i}' + t; \lambda_{2}) (1 - F(T_{C}; \lambda_{2})),
$$

($T_{i}' = T_{i} + T_{R}$), (12)

TABLE II. Properties of $\beta-\gamma$ rays observed in the ¹⁷B β decay. This table lists the γ transition energies (E_γ), decay modes classified with the multiplicity of β -n emission, γ -ray emitter, level energies (E_x^{γ}) in the γ emitter, level energies (E_x^{γ} (17C)) in ^{17}C , γ - and β -ray intensities per ¹⁷B decay (I_y and I_β), and log ft values. For obtaining the I_β value at $E_y = 1767(6)$ keV, the intensities of the cascade decay from 2212(10), 2322(6), and 2379(7) keV were subtracted.

E_{ν} (keV)	Decay mode	γ emitter	E_x^{γ} (keV)	E_{x} (¹⁷ C) (keV)	$I_{\gamma}(\%)$	I_β (%) 2.8(11)	$\log ft$ 6.1(2)
217(2)	$\beta(0n)$	${}^{17}C$	217(2)	217(2)	2.8(11)		
331(2)	$\beta(0n)$	${}^{17}C$	331(2)	331(2)	2.1(2)	2.1(2)	6.22(5)
740(2)	$\beta(2n)$	15 C	740.0(15)	Not identified	2.6(2)	2.6(2)	
1767(6)	$\beta(1n)$	16 C	1766(10)	4050(20)	9.4(3)	7.2(4)	5.29(3)
1382(5)	$\beta(0n)$ - $\beta(^{17}C)$	^{17}N	1373.8(3)		5.9(6)		
1855(8)	$\beta(0n)$ - $\beta(^{17}C)$	^{17}N	1849.5(3)		4.5(6)		
2212(10)	$\beta(1n)$	16 C	3986(7)	Not identified	1.5(2)	1.5(2)	
2322(6)	$\beta(1n)$	${}^{16}C$	4088(7)	Not identified	0.44(9)	0.44(9)	
2379(7)	$\beta(1n)$	${}^{16}C$	4142(7)	Not identified	0.3(1)	0.3(1)	
5290(12)	$\beta(2n)$ - $\beta(^{15}C)$	15 N	5298.822(14)		7.5(11)		

where $f(t; \lambda) = \lambda \exp(-\lambda t)$ is the exponential probability density distribution with a decay constant $\lambda = 1/\tau$, $F(t; \lambda)$ is its cumulative distribution function, λ_1 is the inverse of the mean life of the ¹⁷B β decay, λ_2 is that of the daughter's β -decay constant that directly feeds a relevant γ -ray emission, and T_i is the arrival time of *i*th ¹⁷B particle at which the $T_{\rm R} + T_{\rm C}$ gate opens after the first implantation. The probability distribution of T_i is also given by $f(t; \lambda_B)$ with the average ¹⁷B beam arrival rate $\lambda_B = 17.3$ pps.

The transition strengths I_{γ} of the γ line, for which decay schemes were identified, were determined using Eq. [\(11\).](#page-7-0) The resulting I_{γ} values, as well as the corresponding values obtained after converting them to I_β and $\log ft$, are listed in Table II. In the derivation of the I_β value associated with the 1767(6)-keV γ line, the contributions from the cascade transitions from $E_{\gamma} = 2212(10), 2322(6),$ and 2379(7) keV were subtracted. It should be noted that the I_β values for $E_\gamma =$ 2212(10), 2322(6), and 2379(7) keV can include the sum of other $β$ -decay transitions in the 1n channel that are followed by that particular γ -ray emission, because these three γ decays could be a part of cascade γ decays from the higher E_x levels.

It is known that in the ¹⁷C β decay, $\beta-\gamma$ rays are emitted with $E_v = 1373.8(3)$ and 1849.5(3) keV with the transition strengths $I_{\nu}^{1374}(^{17}C) = 24(8)\%$ and $I_{\nu}^{1850}(^{17}C) = 22(5)\%$, re-spectively [\[42\]](#page-16-0). With the I_{γ} values obtained from the above analysis for the discussed γ lines and the two mentioned I_{γ} (¹⁷C) transition strengths, the total 0n-channel probability P_{0n} can be derived by using the equation $P_{0n} = I_{\gamma}/I_{\gamma}$ (¹⁷C). By taking the weighted average of the resulting probabilities, $P_{0n}(1382(5)$ keV $) = 25(9)\%$ and $P_{0n}(1855(8)$ keV $) = 21(5)\%$, we obtained $P_{0n} = 25(5)\%$. This probability agrees with the reported $P_{0n} = 21(2)\%$ [\[39\]](#page-16-0), within the assigned error bounds.

B. 1n-decay branches

In the one-neutron $(1n)$ decay channel, ^{17}B decays into the levels above the neutron threshold $S_n = 0.729(18)$ MeV. All of these branches are connected with the GS of ${}^{16}C$. If a transition is connected with an excited state in ${}^{16}C$, the neutron emission is further followed by the de-excitation γ -ray emission. The

subsequent β decay of ¹⁶C, whose half-life is $t_{1/2}$ (¹⁶C) = 747(8) ms [\[12\]](#page-15-0), is similarly followed by the neutron emission to ¹⁵N with ∼100% branches in all. This described decay cascade stops at the stable nucleus 15N.

Thus, the 1n-decay channel has been studied through the measurement of β -n [\[24\]](#page-16-0), in which four excited states of ¹⁷C, i.e., $E_x = 1.18, 2.25, 2.64,$ and 3.82 MeV, were identified using a TOF measurement, assuming the direct 1n-decay transition to the 16C GS for all branches. In the present measurement, the Ge and NaI(Tl) detectors were well tuned to detect and thoroughly investigate de-excitation γ rays in ¹⁶C through β -n- γ triple coincidence measurements.

1. TOF measurement of β-delayed neutrons

Figure [8](#page-9-0) shows the obtained neutron TOF spectra for the emitted neutrons from the ¹⁷B β decay; they are measured with (a) high-energy and (b) low-energy neutron detector arrays, and the multiplicity of the neutron is limited to $M_n = 1$. As clearly seen in Fig. $8(a)$, three peaks can be identified at 64, 81, and 122 ns, which correspond to the neutron kinetic energies $E_n = 3.01, 1.86,$ and 0.82 MeV, respectively. Since it is known that in the ¹⁶C β decay (t_{1/2} = 747(8) ms), β -n are emitted at $E_n = 0.82(1)$ and 1.70(1) MeV [\[24\]](#page-16-0), the observed 0.82-MeV peak can be assigned to 0.82(1) MeV. The other two peaks at $E_n = 3.01$ and 1.86 MeV can be assigned to the β -n from the $^{17}B \beta$ decay. These two major peaks were also observed at almost the same energies $E_n = 2.91(5)$ and 1.80(2) in Ref. [\[24\]](#page-16-0).

The obtained neutron TOF spectrum shown in Fig. $8(a)$ was analyzed using the response function (described later in the text) of the neutron detector array. This response function was determined so as to reproduce the well-studied β -n from the ¹⁷N β decay [\[34\]](#page-16-0). In the present analysis, the following four factors were taken into account: (a) the level width of the initial state, (b) uncertainty in the flight path of the neutrons due to the counter misalignment and a finite beam-spot size, (c) the long low-energy tail due to the scattering of emitted neutrons from materials around the Pt stopper, and (d) uncertainty in the time resolution, such as the intrinsic time resolution of the β and neutron detectors. To account for factor (a), the response

FIG. 8. TOF spectra obtained for the β -delayed neutrons emitted in the $^{17}B \beta$ decay with (a) high-energy and (b) low-energy neutron detector arrays. The solid curve shown in panel (a) is the result of a least χ^2 -fitting analysis. The decomposed components are represented by dashed curves.

function essentially assumes a Lorentzian function $H(t)$, and it includes the additional term $f(t)$ to account for factor (c), where $f(t)$ is empirically determined. The response function $\mathcal{F}(t)$ is then obtained as a Gaussian convolution of $H(t) + f(t)$ to account for factors (b) and (d). Thus, the function $\mathcal{F}(t)$ uses three parameters, the amplitude of peaks, the neutron kinetic energy E_n , and the level width Γ . The detailed description of $\mathcal{F}(t)$ is given in Ref. [\[28\]](#page-16-0).

Next, peak decomposition was conducted through the least χ^2 -fitting analysis with the obtained $\mathcal{F}(t)$ function. In this analysis, the following three types of BGs were taken into account: (i) neutrons emitted in the multineutron emission channel initiated by the ¹⁷B β decay, which was assumed to have a Gaussian shape with a wide width at the position ∼100 ns, empirically determined from a TOF spectrum of neutrons, measured with the neutron multiplicity $M \ge 2$; (ii) scattered β rays expressed by a spectral curve monotonically decreasing with t; and (iii) a constant BG. The β -n emitted from the β decay of ¹⁶C, for $E_n = 0.82(1)$ and 1.70(1) MeV, were also considered, and the reported relative intensities were fixed in this case. The result of the fitting analysis is shown in Fig. 8(a) using dashed curves. Other than the two major

peaks, which were determined to be at $E_n = 3.01(1)$ and 1.86(1), the existence of minor peaks corresponding to neutron kinetic energies $E_n = 5.04(2), 3.81(1),$ and 1.46(1) MeV was suggested. Reference [\[24\]](#page-16-0) has reported two minor transitions at $E_n = 1.43(2)$ and 0.42(1) MeV. The first E_n value listed agrees with the present $E_n = 1.46(1)$ peak, with only a small difference, although no peak corresponding to the second value was visible in the spectrum. We also investigated neutrons at a lower E_n with the low-energy neutron array. However, in the obtained spectrum shown in Fig. $8(b)$, no further peaks were identified at any E_n down to 0.01 MeV.

2. Neutron-decay branches to excited states in **¹⁶***C*

To construct the decay scheme, it is necessary to investigate connected states in ${}^{16}C$ after neutron emission. Here, we first studied a γ -ray energy spectrum obtained in a β -n- γ triple-coincidence measurement. As shown in Figs. $9(a)$ and 9(b), the de-excitation γ rays from the first exited state in ¹⁶C at $E_x = 1766(10)$ keV to the GS were clearly identified as a peak in the E_v spectrum measured using both the NaI(Tl) and Ge detectors. Another peak was also observed at $E_v = 743(2)$ keV, which corresponds to the de-excitation γ rays from the ¹⁵C excited state at $E_x = 740.0(15)$ keV to its GS following the two-neutron emission in the 2n channel of the $^{17}B \beta$ decay. To confirm the initiating β decay feeding the two corresponding E_v emissions, the time evolution of their counting rates were investigated as in the 0n-channel analysis. Both the consequently obtained time spectra, shown in Figs. [6\(e\)](#page-6-0) and 6(1), were well reproduced by $t_{1/2}$ (^{17}B), which shows that these γ emissions were directly fed by the ¹⁷B β decay. Furthermore,

FIG. 9. Obtained γ -ray energy spectra with (a) NaI(Tl) detectors and (b) the Ge detector in coincidence with β -delayed neutrons with multiplicity $M_n = 1$.

FIG. 10. TOF spectrum obtained with the neutron detector array in coincidence with a 1767(6)-keV γ peak observed with NaI(Tl) detectors.

two small peaks are observed in Fig. [4\(b\)](#page-5-0) at $E_{\gamma} = 2322(6)$ and 2379(7), which agrees with the de-excitation γ lines 2322(6) and 2379(7) keV from the 3⁽⁺⁾ state at $E_x = 4088(7)$ keV and the 4⁺ state at $E_x = 4142(7)$ keV on ¹⁶C, respectively. The time-evolution analysis described above was also performed for these two E_y lines, and the results are shown in Figs. [6\(o\)](#page-6-0) and $6(p)$, respectively. Although the statistics are not sufficient, they are reproduced by $t_{1/2}$ (¹⁷B), suggesting that the ¹⁷B β decay directly feeds these two γ emissions through β-n emissions. Although peaks should appear at $E_y = 2322(6)$ and 2379(7) in the gated E_{γ} spectrum shown in Fig. [9,](#page-9-0) they are not observed due to the limited statistics.

In the next step, β -n components connected to the $E_x =$ 1766(10) keV state in ${}^{17}C$ were investigated. Figure 10 shows a neutron TOF spectrum measured under the $β$ -n-γ coincidence condition, and in the measurement E_y energies were set as $E_{\gamma} \simeq$ (a) 1767 keV and (b) 2400 keV. To enable clear comparison, the normalized TOF spectrum without the E_{ν} window [i.e., the spectrum shown in Fig. $8(a)$] is also drawn using gray lines. In both the spectra, two major peaks at $E_n =$ 3.01(1) and 1.86(1) MeV still appear. However, this does not imply that the two peaks are connected to the 1767(6)-keV γ line. The peaks are caused by accidental coincidences owing to the following two reasons. First, the TOF spectrum obtained for $E_y = 2400$ keV, at which no Compton scattering from the $E_{\gamma} = 1767(6) \text{ keV } \gamma$ rays can interfere and no other photo peaks are observed, is analogous to the spectrum in the ungated case, as shown in Fig. $10(b)$. In addition, the obtained counting rates of the two major peaks are ∼20 times smaller than those expected on the basis of the spectrum shown in Fig. $8(a)$ and the given NaI(Tl) efficiency. If we closely

examine Fig. $10(a)$, however, a peak can be observed at ∼95 ns, which is emphasized by the $E_v = 1767(6)$ keV gate. This peak energy, $E_n = 1.51(6)$ MeV, agrees with the $E_n = 1.46(1)$ MeV obtained in the described peak decomposition analysis of the ungated E_n spectrum. In addition, the transition strength $I_\beta =$ 1.7(2)%, evaluated using the 1.51-MeV peak count based on Eq. [\(14\),](#page-11-0) which accounts for the NaI(Tl) efficiency, agrees with the value $I_\beta = 1.5(2)\%$ for the 1.46-MeV peak determined as described in Sec. [III B4.](#page-11-0) It is then natural to conclude that both the peaks are identical. No peaks are observed at $E_n = 5.04(2)$ and $3.81(1)$ MeV in Fig. $10(a)$, although peaks with statistics comparable to the $E_n = 1.46(1)$ peak should be observed if they are also connected to the $E_x = 1766(10)$ keV state.

3. Neutron-decay branches to the **¹⁶***C ground state*

Because it was shown that only the 1.46(1)-MeV peak was connected to the 1767(6)-keV γ line, the two major peaks at $E_n = 3.01(1)$ and 1.86(1) MeV, as well as the minor peaks at $E_n = 5.0$ and 3.8 MeV, were assigned to the direct transition to the ${}^{16}C$ GS. As described in the following text, this assignment was verified with the $E_n = 1.86(1)$ MeV peak having the highest statistics, through the measurement of the end-point energy E_{β}^{\max} of the β decay associated with this E_n peak. Figure 11(b) shows a β-ray energy spectrum of the ¹⁷B β decay obtained with the combination of the NaI(Tl) and plastic scintillators in the β -n measurement by gating at

FIG. 11. β -Ray energy spectra (i.e., Kurie plot) measured with NaI(Tl) detectors in coincidence with (a) the 1.86(1)-MeV β -delayed neutrons in the ¹⁷B β decay and (b) 1.76-MeV β-delayed neutrons in the ¹⁵B β decay. Solid curves show the result of GEANT simulations, in which the end-point energies $E_{\beta}^{\text{max}} = 19.7(1)$ MeV and 17.9(2) MeV were deduced, respectively. For comparison with the simulation results, β -ray yields are normalized to unity at $E_\beta = 2$ MeV.

TABLE III. Levels in ¹⁷C observed in the 1n-decay channel following the β decay of ¹⁷B, which are listed along with the excitation energies E_x for ¹⁷C and the neutron-kinetic energies E_n , from which the E_x values are converted. The inconclusive levels are indicated by { }. Determined transition strengths I_β and values of log f t for the ¹⁷C levels are also listed. For details, see the text.

E_n (MeV)	E_x (MeV)	Width (MeV)	I_8 (%)	$\log ft$	B(GT)	$A_{\beta}P(\%)$	A_{β}	$2I^{\pi}$ (χ^2 Analysis)	$2I^{\pi}$ (End result)
5.04(2)	6.08(3)	2.5(7)	4(1)	5.3(1)	0.021(3)				
3.81(1)	4.78(2)	0.3(3)	0.9(1)	6.1(1)	0.003(1)				
1.46(1)	4.05(2)	0.06(6)	1.5(2)	6.0(1)	0.004(1)	$+6(23)$	$-4(15)$	$(1^-, 3^-, 5^-)$	(5^{-})
3.01(1)	3.93(2)	0.16(4)	20(3)	4.9(1)	0.05(1)	$-0.1(15)$	$+0.04(99)$	$(3^-, 5^-)$	$3-$
1.86(1)	2.71(2)	0.04(1)	33(4)	4.8(1)	0.07(1)	$+1.6(8)$	$-1.0(5)$	$1 -$	$1 -$

 $E_n = 1.86(1)$ MeV. The spectrum is expressed in the form of the Kurie plot $\sqrt{N(E)/pEF(Z, E)}$, where E and p are of the total energy and momentum of the β particle, $N(E)$ is the observed β -ray yield at E, $F(Z, E)$ is the Fermi function, and Z is the atomic number of the parent nucleus. The obtained β -ray energy spectrum was analyzed using a GEANT $[41]$ simulation, in which an arrowed β -decay transition was assumed by taking into account its $\log ft$ value 4.8(1), determined in the present work, as explained later. The obtained end-point energy $E_{\beta}^{\max} = 19.7(1)$ MeV agrees well with the 19.9(1) MeV value for the transition to the ${}^{16}C$ GS calculated using the Q_β of ¹⁷B and the neutron energy $E_n =$ 1.86(1) MeV, while it differs from $E_{\beta}^{\max} = 18.1(1)$ MeV when the β -n emission is connected to the 1767(6) keV γ emission line. The accuracy of the analysis was evaluated using the 15B β decay measured in the present work. It is known that in the ¹⁵B β decay, the transition to $E_x = 3.10$ MeV, which has the highest transition strength in the β decay, is followed by the $E_n = 1.76$ MeV β -n emission [\[22,28\]](#page-16-0). Thus, a Kurie plot was also obtained for this transition using the same experimental apparatus. As shown in Fig. $11(a)$, the end-point energy $\vec{E}_{\beta}^{\text{max}} = 15.5(1)$ MeV obtained through the same procedure again agrees with the calculated value $E_{\beta}^{\text{max}} = 16.0(1)$ MeV, with only a slight difference in values. Due to the limited statistics, this analysis cannot be carried out for the remaining minor peaks at $E_n = 5.0(3)$ and 3.8(1) MeV.

4. Transition strengths in the 1n channel

As mentioned above, the ^{17}B β decay in the 1n channel is 100%, followed by the successive β -n emission in the β decay of the daughter nucleus of ¹⁶C. Because in the ¹⁶C β decay, the strength of the transition feeding the β -n emission at $E_n = 0.82(1)$ is known to be $I_\beta = 84.4(17)\%$, the total 1n decay strength P_{1n} of the ¹⁷B β decay can be determined by

$$
P_{1n} = \frac{N_n}{N(\mathbf{1}^7 \mathbf{B}) \cdot I_\beta \cdot \epsilon_n \Omega_n \cdot \epsilon_\beta \Omega_\beta \cdot R_\beta},\tag{13}
$$

where N_n is the count of the 0.82(1)-MeV peak obtained in the described χ^2 -fitting analysis and ϵ_n and Ω_n are the efficiency and the solid angle of the neutron counter array for the 0.82(1)-MeV neutron. The values of ϵ_n were evaluated based on Ref. [\[35\]](#page-16-0), using experimental ϵ_n data obtained from the measurements separately conducted with ^{17}N and ^{15}B beams, as described in Sec. [II B.](#page-1-0) Here, the ϵ_n of the β -n at

 $E_n = 1.17$ MeV in the β decay of ¹⁷N, which is close to 0.82(1) MeV, was determined with an accuracy of $\Delta \epsilon_n = 9.4\%$. The same $\Delta \epsilon_n$ value was therefore adopted in the evaluation of ϵ_n for the 0.82(1)-MeV neutron as a systematic error. We thus obtained $P_{1n} = 67(7)\%$, which agrees with the reported value $P_{1n} = 63(1)\%$ [\[39\]](#page-16-0), within the assigned error bounds.

However, for the other E_n energies of observed β -n, the accuracies of the obtained ϵ_n reference data were not sufficiently high. Therefore, the 1n transition strengths were determined by solving for the normalization factor α in the following equation:

$$
P_{1n} = \alpha \left(\sum_{i} I'_{\beta}(i) - I'_{\beta}(1.46 \text{MeV}) \right) + 9.4\%, \quad (14)
$$

where $I'_{\beta}(i)$ is the relative transition strength obtained with a relative ϵ_n value for each transition i and 9.4% is the sum of the strengths of the 1n transitions that are finally followed by $E_{\gamma} =$ 1767(6)-keV γ -ray emissions, which were not included in the left-hand side in Eq. (14), with the exception of $I'_8(1.46 \text{MeV})$. The resultant I_β values calculated using $\alpha I'_\beta$, as well as the values obtained by converting them to $\log ft$ and $B(\text{GT})$, are summarized in Table III.

C. 2n decay and the higher-multiplicity channels

The ^{17}B β decay in the 2n-decay channel feeds states in ¹⁵C through the β -2n emission. All 2n-decay branches are then followed by the β decay of ¹⁵C ($t_{1/2} = 2.449(5)$ s [\[43\]](#page-16-0)), where the $E_{\gamma} = 5290(12)$ -keV γ ray is expected be emitted from the $I^{\pi} = 1/2^{+}$ excited state at $E_x = 5298.822(14)$ keV in ¹⁵N, with the branching ratio $I_8^{5299}(^{15}C) = 63.2(8)\%$ [\[44\]](#page-16-0). The corresponding peak was observed at $E_{\gamma} = 5290(12)$ keV in the obtained Ge spectrum, as shown in Fig. $4(c)$, for which the deduced transition strength $I_Y(^{17}B) = 7.5(11)\%$ is listed in Table [II.](#page-8-0) The total 2n-decay probability P_{2n} can then be determined as $P_{2n} = I_{\gamma}^{5290(12)}({}^{17}\text{B})/I_{\beta}^{5299}({}^{15}\text{C}) = 12(2)\%$. It should be noted that this P_{2n} value agrees well with the value $P_{2n} = 11(7)\%$ reported in Ref. [\[39\]](#page-16-0), within the assigned error bounds.

In the 2n channel, the γ ray observed at $E_{\gamma} = 743(2) \text{ keV}$ in Fig. [4\(a\)](#page-5-0) can be assigned to the de-excitation γ ray from the $I^{\pi} = 5/2^{+}$ first excited state at $E_x = 740.0(15)$ keV [\[44\]](#page-16-0) to the $I^{\pi} = 1/2^{+}$ GS of ¹⁵C. This assignment was confirmed by observing that the time evolution of the photopeak counts,

shown in Fig. $6(e)$, can be well reproduced by $t_{1/2}$ (¹⁷B). From the measured peak count, the sum of the strengths of the $^{17}B \beta$ decay transitions connected to the $E_x = 740.0(15)$ -keV state of ¹⁵C was determined to be $I_\beta = 2.6(2)\%$, as listed in Table [II.](#page-8-0) Since no γ lines of ¹⁵C, other than the one at 743(2) keV, were identified in the E_y spectrum, we concluded that the 740.0(15)-keV state is directly connected to the two-neutron emission and that the GS of ${}^{15}C$ is directly fed by the strength $P_{2n} - I_\beta = 9.4(3)\%$. To construct the decay scheme of the 2n-decay channel, it is necessary to identify the sum energy of the two emitted neutrons. However, the obtained statistics provided no clear evidence of the 2n decay.

With respect to the 3n(4n)-decay branch, the β -n emission from ¹⁷B feeds states in ¹⁴C(¹³C), for which the total transition probability is reported to be $P_{3n} = 3.5(7)\%$ ($P_{4n} = 0.4(3)\%$) [\[39\]](#page-16-0). Because the half-life of ¹⁴C is $t_{1/2} = 5730$ y and ¹³C is stable, the β -decay cascade from ¹⁷B is almost stopped at the GSs. In the measurement, clear peaks were not found in the sum-energy spectra of neutrons with multiplicity $M_n = 3$ or 4 with the present statistics. Furthermore, no γ -ray peaks were found at the E_y energies associated with the de-excitation γ rays in ¹³C and ¹⁴C. Thus, both P_{3n} and P_{2n} were not determined in the present work.

D. Spin-parity assignment

After obtaining the peak counts of the β -n TOF spectra in the peak-decomposition analysis, $A_{\beta}P$ values of the transition to $E_x = 2.71(2)$, 3.93(2), and 4.05(2) MeV, for which two unassigned peaks were removed, were determined based on Eq. (4) , and the values are listed in Table [III.](#page-11-0) In order to determine I^{π} values, the least P-variance method described in Sec. [II D](#page-3-0) was applied to the obtained $A_{\beta}P$ values. For all possible $3^3 = 27$ combinations of I^{π} , χ^2_{ν} , given by Eq. [\(9\),](#page-4-0) were calculated together with the corresponding mean spin polarization \bar{P} , defined in Eq. [\(7\).](#page-4-0) The resulting χ^2_{ν} values are plotted as a function of \overline{P} in Fig. 12. The obtained χ^2_{ν}

FIG. 12. Values of χ^2_{ν} plotted as a function of the mean spin polarization calculated for all possible sets of A_β values in the ¹⁷B β-decay transition to the observed levels in ¹⁷C at $E_x = 2.71(2)$, 3.93(2), and 4.05(2) MeV. Classification according to the I^{π} for $E_n = 2.71(2)$ MeV is indicated by dotted ellipses. The dashed ellipse shows the most probable sets of the A_β allocation.

values can be divided into three groups, as indicated by the dotted ellipses in Fig. 12: $\bar{P} \simeq -2.5, -1.5,$ and $+2.4\%$. This classification is based on the I_f^{π} value of the 2.71(2)-MeV state owing to its highest statistics.

We first note that a negative spin polarization is expected for the $17B$ beam produced in the present experiment, based on the systematics observed with similar beam energies, targets, and projectile-ejectile combinations [\[9,](#page-15-0)[26,27,31,45–49\]](#page-16-0), for which the reaction proceeds through a far-side trajectory owing to the nuclear attractive force dominating the Coulomb repulsive force. Actually, the negative spin polarization of ^{15}B , $\overline{P} = -2.81(42)\%$, was observed with the same beam energies, targets, and projectile [\[28\]](#page-16-0). Thus, the possibility of assigning $5/2^-$ to the 2.71(2)-MeV state can be eliminated owing to its positive polarization $\bar{P} \simeq +2.4$. Among the remaining two I^{π} values, $1/2^-$ and $3/2^-$, the former can be assigned using the obtained minimum χ^2_ν analysis, although the possibility that 3/2[−] can be assigned is not possible to completely ignore.

After we assigned $1/2^-$ to the 2.71(2)-MeV state, the I^{π} combinations could be further divided into two groups: (i) $1/2^-$ and (ii) $3/2^-$ or $5/2^-$ assignments for the 3.93(2)-MeV state. The χ^2_{ν} values of the first group are in the range of 0.49 ~ 0.51, whereas the second group has a smaller χ^2 = $0.12 \sim 0.26$. We thus assigned $(3, 5)/2^-$ to the 3.93(2)-MeV state. However, no further I^{π} selection was performed, because the differences among the six combinations in the second group were extremely small. The I^{π} assignment completed in this analysis is listed in Table [III,](#page-11-0) together with the asymmetry parameters calculated from the expected polarization \bar{P} = 1.5(8) and given by the minimum χ^2_ν set.

IV. DISCUSSION

A. Further investigation for *I^π* **assignments**

The obtained level structure of ${}^{17}C$ was further investigated for comparison with the β decays of ¹³B and ¹⁵B. The several negative-parity states in ${}^{13}C$ (${}^{15}C$), connected with the β decay of ¹³B (¹⁵B), are illustrated in Fig. [14,](#page-14-0) where relative $B(GT)$ strengths calculated from the reported $\log ft$ values [\[44\]](#page-16-0) are indicated by the line thickness, assuming that Fermi transition strengths are negligibly small owing to the large difference between their E_{β}^{max} energies and Q_β values. In the β decay of ¹³B, the transition strength is concentrated at the β -decay branch leading to the $1/2₁^-$ GS of 13 C, whose branching ratio is 92.1%. Including the second strongest branch with the strength 7.6%, leading to the $3/2^{-}_{1/2}$ excited state at $E_x = 3684.507(19)$ keV, the sum of the ¹³B β-decay transitions exhausts ~100% of the total transition strength. Because the main GS configuration of ¹³B can be described by $|^{13}B_{GS}\rangle^{3/2^-} = |(\pi p_{3/2})_{-1} \otimes$ $(\nu p_{3/2})_4^{0^+}(\nu p_{1/2})_2^{0^+}\rangle^{3/2^-}$, given the well-established neutron magic number $N = 8$, the transition to the 1/2⁻ GS can be described by the single-particle GT transition $vp_{1/2} \rightarrow$ $\pi p_{3/2}$, under the reasonable assumption of a configuration $|^{13}C_{GS}\rangle^{1/2^-} = |(\pi p_{3/2})_4^{0^+} \otimes (\nu p_{3/2})_4^{0^+} (\nu p_{1/2})_1 \rangle^{1/2^-}$ to the $1/2_1^-$ state. Then, the concentration of the transition strength to the $1/2₁⁻$ state can be understood taking this pure single $v p_{1/2}$ particle state to the 1/2⁻ state, because the $vp_{1/2} \rightarrow \pi p_{3/2}$

GT transition can only populate this configuration from the ¹³B GS. A similar observation applies to the ¹⁵B β decay, in which the lowest negative-parity state at $E_x = 3.103$ MeV [\[44\]](#page-16-0) in ¹⁵C, which has been assigned to $I^{\pi} = 1/2^-$ [\[22,28\]](#page-16-0), is fed through the strongest GT transition. Assuming a weak coupling of the ¹³B GS with the two valence neutrons in the sd orbit, the ¹⁵B GS can be written as $1^{15}B_{GS}$ $3^{3/2^-}$ = $|^{13}$ B_{GS} $\rangle^{3/2^-}$ \otimes $|(vsd)_2\rangle^{0^+}$. Then, the observed analogous characteristics of the GT transitions in the β decays of ¹³B and ¹⁵B can be understood, provided a major contribution of the GT transition from ¹⁵B to the lowest $1/2^-$ state in ¹⁵C is largely governed by the $\nu p_{1/2} \rightarrow \pi p_{3/2}$ transition in the ¹³B GS, where the two neutrons are kept in the sd orbit to couple to form $I^{\pi} = 0^{+}$. For detailed discussions, such as those on the inversion of the $3/2₁⁻$ and $5/2₁⁻$ states in ¹⁵C, effects of the p-sd cross-shell interactions need to be taken into account. The same rule can be applied to the ¹⁷B β decay, because the main configuration of the $17B$ GS should be given by $|{}^{17}B_{GS}\rangle^{3/2^-} = |{}^{13}B_{GS}\rangle^{3/2^-} \otimes |(vsd)_4\rangle^{0^+}$. Then, the strongest GT transition can be characterized by $\nu p_{1/2} \rightarrow \pi p_{3/2}$ in the ¹³B GS, and the final state is described by $I^{\pi} = 1/2^-$, which would be the lowest negative-parity state. Factually, among the observed β-decay transitions from $17B$, the strongest transition $I_\beta = 33(4)\%$ is the branch to the $E_x = 2.71(2)$ MeV state in ¹⁷C, to which $I^{\pi} = 1/2^-$ has been assigned in the present χ^2_{ν} analysis. The relative $B(GT)$ strengths of the ¹⁷B β decay are also shown in Fig. [14](#page-14-0) in a similar manner as for 13 C and 15 C.

The decay branch to the $3/2₁⁻$ state is the second strongest transition in both the β decays of ¹³B and ¹⁵B, although the ordering of $3/2_1^-$ and $5/2_1^-$ differs for ¹³C and ¹⁵C due to the appearance of the p -sd cross-shell interactions in ¹⁵C. These transitions are considered to be related to the singleparticle GT transition $\nu p_{3/2} \rightarrow \pi p_{3/2}$, which results in the $\nu p_{3/2}$ -hole configurations in the daughter nuclei ¹³C and ¹⁵C. Similarly to the above $1/2₁⁻$ case, the $\nu p_{3/2} \rightarrow \pi p_{3/2}$ GT transition can uniquely populate the single $\nu p_{3/2}$ -hole state, suggesting its large transition strength. The same singleparticle GT transition can also occur in the ¹⁷B β decay. The gap energy between the $\nu p_{3/2}$ - and $\nu p_{1/2}$ -hole states should be comparable in both ${}^{15}C$ and ${}^{17}C$, provided the spin-orbit splitting remains relatively unchanged. From this viewpoint, $I^{\pi} = 3/2^-$ can be assigned to the 3.93(2)-MeV state in ¹⁷C, because the energy difference $\Delta E = 1.22$ MeV between the 3.93(2)-MeV state and 1/2[−] 2.71(2)-MeV state in ¹⁷C is comparable to $\Delta E = 1.55$ MeV, which is the difference between the $1/2_1^-$ and $3/2_1^-$ states in ¹⁵C, and also because the second strongest $B(GT)$ value was obtained for the transition to the 3.93(2)-MeV state. It should be noted that this I^{π} assignment agrees with the $I^{\pi} = (3, 5)/2^-$ assignment in the present χ^2_ν analysis.

We may assign $5/2^-$ to the 4.05(2)-MeV state, which is a neighboring partner state to the $3/2₁⁻ 3.93(2)$ -MeV state, by taking into account the similarity of the level structure in this case to that of ${}^{15}C$, although we cannot disregard the fact that there are three possible candidates $I^{\pi} = (1, 3, 5)/2^{-1}$ in the χ^2_{ν} analysis. The obtained $\log ft = 6.0(1)$ value for the transition to the $4.05(2)$ -MeV state is not sufficiently small to be definitely assigned to the GT transition. However, log f t values to the corresponding $5/2₁⁻$ states at 7.547 and

FIG. 13. Decay scheme of ¹⁷B constructed in the present work. Unassigned levels $E_x = 4.78(2)$ and 6.08(3) MeV are also shown.

4.220 MeV in ¹³C and ¹⁵C are also as large as $\log ft =$ 5.33(10) [\[44\]](#page-16-0) and 5.09(9) [\[22\]](#page-16-0), respectively, indicating the similarity among their transition strengths. As investigated in the above, the GT transition $\nu p_{3/2}(\nu p_{1/2}) \rightarrow \pi p_{3/2}$ uniquely populate the $1/2^-_1(3/2^-_1)$ state having single $\nu p_{1/2}$ -particle $(vp_{3/2}$ -hole) state properties, which causes the concentration of transition strengths. However, the $5/2₁⁻$ state cannot be formed by an unpaired particle or hole in the p -sd shell unlike the $1/2₁⁻$ and $3/2₁⁻$ states. It should be a mixed configuration such as $|{}^{17}C\rangle^{5/2^-}$ = $|((\pi p_{1/2})_1(\pi p_{3/2})_{-1})^{1^+, 2^+}$ ⊗ $(vp_{3/2})_{-1}(vsd)^{0^+}_{4}$ ^{5/2-}, which prevents the concentration of the transition strength. Moreover, the GT transition $\nu p_{3/2}(\nu p_{1/2}) \rightarrow \pi p_{1/2}$, which can populate these configurations, can also populate the states up to $I^{\pi} = 7/2^{-}(5/2^{-})$, further fragments the transition strength. Thus, the $5/2^-$ assignment to the 4.05(2)-MeV state seems reasonable, although further experimental observations are necessary for a definite assignment.

Including the above-mentioned I^{π} assignment, results obtained in the present work for the ¹⁷B β decay are shown in Fig. 13 as the decay scheme.

B. Comparison with shell-model calculations

In Fig. [14,](#page-14-0) the data of the excited states of ^{17}C observed in the present study are compared with the results of shellmodel calculations [\[50\]](#page-16-0) with two different sets of effective interactions, PSDWBT [\[51\]](#page-16-0) and PSDMK [\[52\]](#page-16-0), denoted by WBT and MK, respectively.

With respect to the low-lying positive-parity states, the GS has been experimentally assigned to $I^{\pi} = 3/2^+$ [3-9], and the 210-keV and 331-keV states have been assigned to $1/2$ ⁺ and $5/2$ ⁺ [\[17](#page-15-0)[–19\]](#page-16-0). Here, we assumed that the excited

FIG. 14. Comparison of the obtained β -decay feeding excited states in 17C with shell-model calculations, with positive and negative parity states indicated by dashed and solid lines, respectively. The negative-parity states in 13 C and 15 C are also shown.

state at $E_x \sim 210 \text{ keV}$ and the observed 217(2)-keV state are identical. The shell-model calculations predict the existence of three positive-parity states, $I^{\pi} = 3/2^{+}$, $1/2^{+}$, and $5/2^{+}$, below the neutron separation energy $S_n = 0.729(18)$ MeV. However, their ordering changes, depending on the choice of effective interactions. For the I^{π} value of the GS, the MK interaction predicts the $3/2^+$ correctly, whereas the WBT interaction predicts $5/2^+$. The experimental and theoretical positive-parity states in 17C are indicated by dashed lines in Fig. 14. We note that the experimentally determined ordering of $1/2^+$ and $5/2^+$ is inverted both in the MK and WBT calculations.

Next, the observed negative-parity states were compared. As expected from the above comparison for positive-parity states, the $1/2^-$ state is predicted as the lowest negative-parity state in 17C according to both the WBT and MK interactions, which thus supports the assignment of $1/2^-$ to the $E_x =$ 2.71(2)-MeV state. The E_x energy for this state, predicted using the MK interaction, agrees well with the observation, while it is ∼1 MeV lower when determined using the WBT interaction. For the next two states at 3.93(2) and 4.05(2) MeV, $I^{\pi} = 3/2^-$ and $(5/2^-)$ were, respectively, assigned herein. The energy gap of their centroid, whose displacement is only 110 keV from the GS, is 6.0 MeV. Such a pair of neighboring states are also predicted using both the MK and WBT interactions. The MK interaction predicts the 5/2[−] and $3/2^-$ states at $E_x = 4.62$ and 4.69 MeV, respectively, for which the centroid is ∼0.7 MeV higher than in the experimental observation. In contrast, the ordering is inverted in the WBT calculation, where the $3/2^-$ and $5/2^-$ states are predicted

at $E_x = 3.09$ and 3.26 MeV, respectively. In this case, the centroid is lower by ∼0.8 MeV in the direction opposite to that observed in the MK interaction. If we calculate E_x for them using the $3/2_1^+$ state instead of the predicted $5/2_1^+$ GS, the difference is found to be ∼0.9 MeV. Thus, the WBT-interaction-based calculation systematically predicts ∼1 MeV lower E_x energies for all the low-lying negative-parity states.

In the light mass region, the phenomena of reduction in the single-particle energy of the $s_{1/2}$ state are known to occur for $N = 7$ [\[1\]](#page-15-0) and $N = 9$ [\[2\]](#page-15-0) nuclei. However, the ∼1 MeV discrepancy due to the tendency of the energies of negativeparity states in ${}^{17}C$ to be calculated as lower with the WBT interaction cannot be corrected by lowering the $s_{1/2}$ singleparticle energy. The ${}^{17}C$ energy levels calculated by reducing the original $s_{1/2}$ single-particle energy $\epsilon_{s.p.}(s_{1/2})$ to $\epsilon_{s.p.}(s_{1/2})$ – 1 MeV are also shown in Fig. 14. This modification changes the energies E_x of the positive-parity states and, in particular, the ordering of the low-lying states, while it does not affect the energies E_x of the negative-parity states. In fact, the energy displacement from the $3/2₁⁺$ state is further lowered, and hence, the discrepancy from the experimental observation is rather exacerbated.

A further investigation was performed with the WBT interaction. In this study, the WBT calculation was performed, with the $|V_{01}|$ values reduced by 30%, for the sd neutrons, and herein, $|V_{01}|$ denotes a diagonal matrix element of a two-body effective interaction in a channel with angular momentum $I = 0$ and isospin $T = 1$ for particles within the sd orbits. The diminished pairing energy is attributed to the following three reasons. First, systematic over-binding occurs for the even mass-number C isotopes ${}^{16}C$, ${}^{18}C$, and ${}^{20}C$ with the WBP interaction [\[51\]](#page-16-0), as reported in the study of binding energies for the neutron-rich C isotopes [\[11\]](#page-15-0). Second, the weakening of the coupling between excess neutrons and the core in nuclei away from the stability line causes pairing energies to be modified. A significant amount of theoretical V_{01} values of the two neutrons in the sd shell are originated from the renormalization of the two-body interaction due to the polarization of the core [\[53\]](#page-16-0). Finally, it was shown in the study of the GS magnetic-moment measurement of ^{17}B [\[31\]](#page-16-0) that the use of the pairing energy $|V_{01}|$ reduced by 30% improves agreements of the experimental and theoretical magnetic moments as well as low-lying state energies of neighboring neutron-rich nuclei. In the state structure calculated with the $0.7|V_{01}|$ values, shown in Fig. 14, the energy gap between the GS and the $1/2₁⁻$ state becomes as wide as in the experimental observation. Furthermore, the GS described by $I^{\pi} = 3/2^{+}$ was correctly reproduced. The ordering of the other low-lying positive-parity states $1/2_1^+$ and $5/2_1^+$ is, however, inverted from the experimental observation in the calculations with both WBT $(0.7|V_{01}|)$ and MK interactions.

V. SUMMARY

By virtue of the large Q_β window, excited states in ¹⁷C were effectively investigated through the measurement of β -n and γ rays emitted in the β decay of ¹⁷B. In the measurement, three negative-parity states and two inconclusive states, were

identified above the neutron threshold energy in the 1n channel of the ^{17}B β decay. Furthermore, two positive-parity states below the threshold were also observed. For the transitions, experimental I_β values were determined. We note that in the 1n-channel, the 1767(6)-keV γ ray from the first excited state of ${}^{16}C$ was observed in coincidence with the emitted β -n, which changes the reported β -decay scheme of ¹⁷B and level structure of $17C$. Apart from the 1767(6)-keV lines, several de-excitation γ lines connected after the β -n emission were identified. In the present work, the β -NMR technique was combined with the β -delayed particle measurements using a fragmentation-induced spin-polarized 17B beam. This new scheme allowed us to determine the spin parity of β -decay feeding excited states based on the difference in the β decay asymmetry parameter, which took three discrete values depending on the final state spin for a common initial spin, if the states are connected through the GT transition. As a result, $I^{\pi} = 1/2^{-}$, $3/2^{-}$, and $(5/2^{-})$ have been assigned to the

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observed states at $E_x = 2.71(2)$, 3.93(2), and 4.05(2) MeV in $17C$, respectively. The observed gap energy between low-lying positive and negative-parity states is 1∼2 MeV larger than that predicted by the shell-model calculation with the WBT interaction. This discrepancy can be reduced by assuming that the pairing energy for neutrons in the sd shell of a neutron-rich nucleus diminishes by about 30%, although it cannot be resolved by reducing the $s_{1/2}$ single-particle energy.

ACKNOWLEDGMENTS

The authors are grateful to the staffs at the RIKEN Ring Cyclotron for their support during the execution of the experiments. This work was supported in part by a Grant-in-Aid for Scientific Research from the Ministry of Education, Science, Sports and Culture. The experiment was performed at RIKEN under the Experimental Program R206n(5B).

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