Shears mechanism in ¹⁰⁹In

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High spin states of ¹⁰⁹In were investigated using the reaction ⁹⁶Zr(¹⁹F, 6n)¹⁰⁹In at a beam energy of 105 MeV. New level sequences have been found in this nucleus. In an earlier known band, the ordering of some of the transitions have been changed and assigned a three-quasiparticle $\pi(g_{9/2})^{-1} \otimes \nu[h_{11/2}(d_{5/2}/g_{7/2})]$ configuration. Similar three-quasiparticle bands have also been found earlier in lighter mass ¹⁰⁵In and ¹⁰⁷In nuclei. Systematics of these bands in ¹⁰⁵In, ¹⁰⁷In, and ¹⁰⁹In nuclei are discussed in the present work within the framework of the tilted axis cranking model.

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Nuclei in the mass $A \sim 110$ region have been the focus of study in recent years for the investigation of the phenomenon of magnetic rotation [1–8]. Being in close vicinity of the Z = 50shell closure, these nuclei have low deformation ($\epsilon \sim 0.1$) and therefore the observation of rotation-like structures, with $\Delta I = 1 M1$ transitions, requires an alternative interpretation. These were explained in terms of the shears mechanism within the framework of the tilted axis cranking (TAC) model [9], where spins and excitation energies in a nucleus are generated by the gradual alignment of valence neutrons \mathbf{j}_{v} and protons \mathbf{j}_{π} spin vectors toward the total angular momentum vector **I**. The bandhead state is formed by the perpendicular coupling of \mathbf{j}_{ν} and \mathbf{j}_{π} , which results in an angle θ of **I** with respect to the symmetry axis. In this mass region the configuration of these bands involve the participation of low- $\Omega h_{11/2}$ and $d_{5/2}$ or $g_{7/2}$ neutron particles that are aligned along the rotation axis and high- $\Omega g_{9/2}$ proton holes, which are aligned along the symmetry axis. Recently in ¹⁰⁷In, a $\Delta I = 1 M1$ dipole band built on a three-quasiparticle configuration (3-qp) has been identified as a magnetic rotational band [10]. The contribution from the collective rotation was found to be quite small ($\epsilon =$ 0.08 from TAC calculations). An interesting question arises as to how this contribution from collective rotation changes for the same quasiparticle configuration along an isotopic chain. This is the subject of the present work.

In this work, high spin states of ¹⁰⁹In were populated using the reaction 96 Zr(19 F, 6n) 109 In at a beam energy of 105 MeV delivered by the 15UD Pelletron Accelerator at the Inter University Accelerator Centre (IUAC), New Delhi [11]. The

 γ rays emitted in the reaction were detected by the Indian National Gamma Array (INGA) [12], which at the time of experiment was comprised of 14 Compton-suppressed Ge clover detectors with two at 32° , two at 57° , four at 90° , two at 123°, and four at 148° with respect to the beam axis. An isotopically enriched ⁹⁶Zr target of thickness 1.0 mg/cm² with 10.0-mg/cm²-thick natural Pb backing was used. The data acquisition and analysis procedure is the same as explained by the authors of Ref. [10].

The level scheme proposed for ¹⁰⁹In is shown in Fig. 1. The previous level scheme [13,14] has been modified and extended. This includes the observation of bands 2 and 5 for the first time and reordering of the placement of some of the transitions in bands 1 and 4. The properties of the transitions extracted are listed in Table I. Multipolarities of the transitions were determined using the directional correlation from oriented nuclei (DCO) measurements and the results are tabulated in Table I. The results of DCO measurements are in agreement with those found in Refs. [13,14] and therefore the \mathbf{I}^{π} assignments, except for band 4, have been adopted from these references.

Band 1 was observed earlier in the work done by Kownacki et al. [13]. They placed the 589-keV transition at the top of this band. In the present work, this transition was not found in coincidence with other transitions of band 1 (except for the 555-keV transition) above $25/2^{-}$. Rather, a new sequence of transitions of energies 589 and 555 keV (labeled as band 2) decaying via a 636-keV transition to the $25/2^{-}$ level of band 1 was observed. A linking transition of energy 396 keV $[29/2^{(-)}\rightarrow 27/2^{(-)}]$ between bands 1 and 2 was also observed. The DCO ratios of the transitions of bands 1 and 2 suggest their dipole nature (see Table I).

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FIG. 1. Level scheme of ¹⁰⁹In deduced from the present data. The width of each arrow is proportional to the intensity of transition.

Another modification in this work in comparison to earlier works [13,14] is the change in intensities of transitions in bands 1 and 2. It was observed that the intensities of 990and 1101-keV transitions decaying from the $19/2^{-}$ and $21/2^{-}$ level of band 1 to the $19/2^+$, 210 ms isomeric level at 2102-keV excitation energy, are significantly higher than reported in Ref. [14]. This isomeric level then decays to the $13/2^+$ level via a 674-keV transition (Ref. [14]). Whereas in Ref. [13], these transitions were not observed, instead a 990-keV transition was reported to decay to a prompt level at 2102 keV which also decays through a 674-keV transition. As a consequence, the work of the authors of Ref. [13] also does not reflect the loss in intensities of the transitions of band 1 due to its decay to the isomeric level. Although the prompt 674-keV transition was also observed in the work of Ref. [14] it was not placed in the level scheme. In the present work, band 1 is observed to decay to both the levels at 2102 keV. This is verified in the gate of the 110-keV transition (see Fig. 2), where the coincidence between the 110- and 674-keV transitions is observed, thereby suggesting the decay of band 1 to the prompt level. Whereas a relatively large intensity of the 990-keV transition in comparison to the intensity of the 674-keV transition suggest the decay to the isomeric level. Further, the observed coincidence between the 674- and 894-keV transitions corroborate the existence of prompt level (see inset of Fig. 2). These results also suggest the existence of two transitions of nearly the same energy of 990-keV decaying from the

 $19/2^{-}$ level to both the isomeric and the prompt level. The relative intensities of these transitions were then found from the 110-keV gated spectrum (see Fig. 2), where the intensity of the 674-keV transition was observed to be significantly lower (about one-fourth) than the intensity of the 990-keV transition. This suggests that the transition having higher intensity decays to the isomeric level while the one with lesser intensity decays to the prompt level. The normalized intensities of 990- and 1104-keV transitions were then obtained from 208and 110-keV gated spectra, respectively, where the intensities of 223- and 245-keV transitions were taken as a reference. Due to the feeding of the 990- and 1101-keV transitions to the isomeric level, the intensities of transitions for bands 1 and 2 cannot be calculated from the 1428-keV gate alone. Their intensities, therefore, were obtained from a sum spectrum of 1428-, 1101-, and a weighted 990-keV gate. The linear polarization of the 208- and 390-keV transitions of band 1 and the linking 245-keV transition were determined by the authors of Ref. [14]. In the present work, the multipolarities of the transitions of bands 1 and 2 have been determined to be dipole. From these results, the transitions of the bands 1 and 2 are assigned to be M1 in nature.

Band 4 was observed in the work of Ref. [13]. In the present work, based on intensity and coincidence arguments, the placement of transitions in the band has been altered. In Ref. [13], the 151- and 482-keV transitions were placed in the band. In the present work, these transitions were not observed

TABLE I. Energies, intensities, DCO ratios, and the initial and final state spins of the transitions of 109 In deduced in the present work. Q and D stand for the quadrupole and dipole natures of the gated transition.

$\overline{E_{\gamma}}$	E_x	I_{γ}	$R_{\rm DCO}(Q)$	$R_{\rm DCO}(D)$	$J^{\pi}_i ightarrow J^{\pi}_f$
(keV)	(keV)				10 - 15 -
88.9	2957.8	63.6(42)			$\frac{19}{2}^- \rightarrow \frac{17}{2}^-$
110.4	3202.4	31.2(19)		0.99(21)	$\frac{21}{2}^- \rightarrow \frac{19}{2}^-$
164.6	3122.4	54.2(25)	0.78(8)		$\frac{21}{2}^- \rightarrow \frac{19}{2}^-$
208.0	3410.4	78.2(41)	0.75(14)		$\frac{23}{2}^{-} \rightarrow \frac{21}{2}^{-}$
211.4	4686.3	19.9(12)	0.56(17)	1.15(20)	$\frac{29}{2} \rightarrow \frac{27}{2}$
223.1	3092.0	6.0(15)			$\frac{19}{2}^- \rightarrow \frac{17}{2}^-$
244.6	3202.4	35.2(17)	0.70(10)		$\frac{21}{2}^- \rightarrow \frac{19}{2}^-$
260.4	2532.3	6.6(7)			$\frac{15}{2}^- \rightarrow \frac{13}{2}^-$
288.0	3410.4	8.4(10)		1.00(28)	$\frac{23}{2}^- \rightarrow \frac{21}{2}^-$
324.4	4833.0	23.6(12)	0.73(18)		$\frac{29}{2}^{(-)} \rightarrow \frac{27}{2}^{(-)}$
336.6	2868.9	99.8(41)	0.69(4)		$\frac{17}{2}^{-} \rightarrow \frac{15}{2}^{-}$
338.4	3800.5	9.7(13)	0.56(5) ^a		$\frac{25}{2}^- \rightarrow \frac{23}{2}^-$
339.7	3800.5	33.9(38)	0.56(5) ^a		$\frac{23}{2}^{-} \rightarrow \frac{21}{2}^{-}$
354.8	5408.2	8.8(9)		1.18(37)	$\frac{2}{33} \rightarrow \frac{31}{2}$
362.5	3484.9	32.6(13)	0.63(10)		$\frac{23}{2} \rightarrow \frac{21}{2}^{-}$
367.1	5053.4	13.8(9)		1.00(28)	$\frac{\frac{2}{31}}{\frac{2}{2}} \rightarrow \frac{\frac{2}{29}}{\frac{2}{2}}$
390.1	3800.5	74.1(39)	0.61(8)		$\frac{25}{2}^{-} \rightarrow \frac{23}{2}^{-}$
396.5	4833.0	4.0(5)			$\frac{29^{(-)}}{2} \rightarrow \frac{27}{2}^{(-)}$
402.2	1428.4	26.0(18)			$\frac{13}{13}^+ \rightarrow \frac{11}{12}^+$
409.0	5242.0	16 4(10)		1 19(23)	$\frac{31}{2}^{(-)} \rightarrow \frac{29}{29}^{(-)}$
470.9	4508.6	9.9(10)		0.93(14)	$2 \xrightarrow{2}{27} (-) \xrightarrow{2}{25} -$
492.9	4308.0	22 6(13)		1.20(22)	$2 \xrightarrow{25} \rightarrow 23 \xrightarrow{23}$
497.2	3982.0	28.7(15)		1.03(16)	$\frac{2}{27} \rightarrow \frac{2}{25}$
555.4	5580.6	74(12)		$0.94(33)^{b}$	$\xrightarrow{2}{31}^{(-)} \xrightarrow{2}{29}^{(-)}$
5547	5706.7	7.1(12)		0.94(33) ^b	$2 \\ 33(-)$ $2 \\ 31(-)$
575.6	4027.7	14.8(9)		1.04(17)	$\frac{1}{2}$ $\frac{1}{25}$ $\frac{1}{23}$ $\frac{1}{23}$ $\frac{1}{23}$ $\frac{1}{23}$
581.3	5080 5	14.8(8) 8 8(9)		1.04(17) 1.11(38)	$\frac{\overline{2}}{(35)} \rightarrow \frac{\overline{2}}{33}$
500.7	5025.2	11.0(10)		1.02(46)	$\binom{2}{29^{(-)}}$ $\binom{2}{27^{(-)}}$
588.7	3023.2	11.0(10)		0.07(21)	$\overline{2} \xrightarrow{2} \overline{2} \xrightarrow{2} \overline{2}$
030.0	4430.3	20.0(13)		0.97(21)	$\frac{1}{2} \rightarrow \frac{1}{2}$
673.2 ^e	2101.6				$\frac{19}{2} \rightarrow \frac{13}{2}$
673.8	2102.2	58.6(27)	1.13(14)		$\frac{17}{2}^+ \rightarrow \frac{13}{2}$
708.1	4508.6	24.4(9)		1.28(19)	$\frac{27}{2}^{(-)} \rightarrow \frac{25}{2}^{-}$
856.2	2868.9	12.7(8)			$\frac{19}{2}^- \rightarrow \frac{19}{2}^+$
865.4	3861.3	17.1(12)			
874.0	1900.2	9.9(8)			
893.7	2995.9	18.8(15)			$\rightarrow \frac{17}{2}^+$
989.8	3092.0	9.6(11)			$\frac{19}{2}^- \rightarrow \frac{17}{2}^+$
990.4	3092.0	26.0(47)			$\frac{19}{2}^- \rightarrow \frac{19}{2}^+$
1026.2	1026.2	69.8(29)			$\frac{11}{2}^+ \rightarrow \frac{9}{2}^+$
1100.8	3202.4	16.5(8)			$\frac{21}{2}^- \rightarrow \frac{19}{2}^+$
1103.8	2532.3	100.0	0.50(5)		$\frac{15}{2}^- \rightarrow \frac{13}{2}^+$
1245.7	2271.9	8.3(8)			$\frac{\overline{13}}{2}^- \rightarrow \frac{\overline{11}}{2}^+$
1304.8	5166.1	10.6(11)			2 2
1428.4	1428.4	132.6(81)			$\frac{13}{2}^+ \rightarrow \frac{9}{2}^+$

^aDetermined for the combined 338.4- and 339.7-keV transitions.

 $^{b}\mbox{Determined}$ for the combined 554.7- and 555.4-keV transitions.

^cDelayed transition not observed in the present work.



FIG. 2. γ -ray energy spectrum gated by the (a) 110-keV and (b) 894-keV transitions in bands 1 and 5, respectively.

in coincidence with the transitions of the band. The 211-keV transition, which was placed in an anticoincidence relationship with the 362-keV transition in Ref. [13], has been observed to be in coincidence with the 362-keV transition. The decay out 362 keV and all the other in-band transitions have been found to be of a dipole nature. A new sequence of transitions of energies 894, 865, and 1305 keV on top of the $17/2^+$ level at 2102-keV excitation energy has been observed. The sequence is labeled as band 5.

A sequence similar to band 1 was observed in ¹⁰⁷In (band 1 in Ref. [10]) and ¹⁰⁵In [13,15], where the configuration $\pi(g_{9/2})^{-1} \otimes \nu[h_{11/2}(d_{5/2}/g_{7/2})]$ has been assigned for the sequence before the alignment of pair of neutrons in $(d_{5/2}/g_{7/2})$. In the upper panel of Fig. 3, the observed spins *I* as a function of rotational frequency $\hbar \omega$ for band 1 of ¹⁰⁵In, ¹⁰⁷In, and ¹⁰⁹In are plotted. The similar behavior of the plots, especially the frequency of the band crossing at about 0.43 MeV and the alignment gain of about 4.5 \hbar at the crossing frequency, suggests similar configurations for all three bands, both before and after the alignment.

In our earlier work [10], it was established that the shears mechanism is the dominant mode of excitation in band 1 of ¹⁰⁷In. Band 1 of ¹⁰⁹In, therefore, was analyzed in light of this phenomenon. The TAC calculations have been carried out for configurations mentioned in the previous paragraph and were compared with the experimental results for this band (lower panel of Fig. 3). In these calculations, the values of the proton paring gap parameter $\Delta_{\pi} = 0.99$ MeV and the neutron pairing gap parameter $\Delta_{\nu} = 0.85$ MeV were used. These values are 0.6 and 0.8 times the odd-even mass difference, respectively. The chemical potential λ_{ν} was chosen to reproduce the particle number of N = 60. The deformation parameters ϵ_2 and γ used were obtained from the Nilsson Strutinsky's minimization procedure. These values were found to be $\epsilon_2 = 0.15$, $\gamma = 9^{\circ}$ for the states before the alignment and $\epsilon_2 = 0.08$, $\gamma = 20^{\circ}$ after the alignment. Good agreement between the calculations and experimental results is obtained. However, in Ref. [10], it was shown for the similar band in ¹⁰⁷In that the agreement between the calculations and experimental results for the states before the neutron alignment were better for the calculations



FIG. 3. (Color online) Plot of angular momentum I as a function of rotational frequency $\hbar\omega$ for band 1 in ¹⁰⁵In, ¹⁰⁷In, and ¹⁰⁹In (upper panel). In the lower panel a comparison with the TAC calculations is shown for the band in ¹⁰⁹In. 3qp stands for calculations for the three-quasiparticle configuration $\pi(g_{9/2})^{-1} \otimes \nu[h_{11/2}, (d_{7/2}/g_{7/2})]$ of the band before alignment. Similarly, 5qp stands for calculations for five-quasiparticle configuration $\pi(g_{9/2})^{-1} \otimes \nu[h_{11/2}, (d_{7/2}/g_{7/2})^3]$ of the band after the alignment. Also shown is the comparison with calculations done with the lower deformation value of $\epsilon_2 = 0.08$ for 3qp configuration.

performed with lower deformation values than the value obtained from the minimization procedure. This conclusion was also supported by the observation of a rapid decrease in B(M1) strength with increase in spin, thereby indicating a very small contribution from the core toward the angular momentum generation. Therefore, the calculations for these states in ¹⁰⁹In before the alignment were performed with a lower deformation value of $\epsilon_2 = 0.08$ obtained by reducing the strength of the coupling constant of the quadrupole-quadrupole (QQ) interaction. The result shows an improvement in the agreement. Comparing this result with the one obtained for the same configuration in ¹⁰⁷In (band 1 before the neutron alignment) indicates that there is no significant change in the deformation of the states when going from N = 58 to N = 60. In other words, there is no significant change in the contribution from the core toward the total angular momentum when going from N = 58 to N = 60. The result can be explained by the observation that the extra pair of neutrons in ¹⁰⁹In are in the $(d_{5/2}/g_{7/2})$ orbitals, which do not drive the nucleus toward strong deformation.

In the present work, we compared the relative contribution of the core and the shears mechanism for a particular set of quasiparticle configuration in ¹⁰⁷In and ¹⁰⁹In. The results indicate that this relative contribution does not significantly change when going from N = 56 to N = 60.

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