# **High-spin structure of 104Pd**

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The high-spin structure of the nucleus <sup>104</sup>Pd was studied through the  ${}^{96}Zr({}^{13}C,5n)$  reaction at incident energies of 51 and 58 MeV, using the Euroball IV *γ* -ray spectrometer in conjunction with the DIAMANT charged-particle array. Several new medium- and high-spin bands were revealed. The already known positive-parity yrast and the negative-parity cascades were extended up to  $E_x \sim 13$ , ~11, and ~9 MeV with  $I^{\pi} = (26^{+})$ ,  $I^{\pi} = (23^{-})$ , and (20−), respectively. The deduced band structures were compared with Woods-Saxon total Routhian surface (TRS) calculations. In addition, non-yrast low-lying positive-parity bands were identified, which were assigned to soft *γ* -vibrational excitations.

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## **I. INTRODUCTION**

Transitional nuclei lying in the *A* ∼ 100 mass region have been in the forefront of nuclear structure research in recent decades. These investigations have revealed a large variety of interesting phenomena related to triaxial nuclear shapes, such as the occurrence of signature inversion in <sup>98</sup>*,*100–103Rh [\[1\]](#page-12-0), the appearance of chiral twin bands in  $104-106$ Rh [\[2–4\]](#page-12-0), and the identification of a quasi- $\gamma$  band in <sup>102</sup>Ru, the core nucleus of  $104$ Rh [\[5\]](#page-12-0). Recently, a study of the chiral doublet bands in <sup>103</sup>Rh has shown that the energy separation of these structures depends mainly on the core properties and, to a lesser extent, on the valence quasiparticle coupling [\[6\]](#page-12-0). However, the chiral interpretation in the  $A = 130$  region has been questioned due to lifetime measurements [\[7,8\]](#page-12-0), and it could not be confirmed by lifetime experiments in the nuclei  $^{103}$ Rh and  $^{104}$ Rh [\[9\]](#page-12-0). In this respect, it is important to understand the necessary conditions leading to the emergence of chiral geometry, one of which is the shape of the corresponding even-even core. Mapping the border of chirality in this region, the structure of  $105\,\text{Ag}$ —the even-even core of which is  $104\,\text{Pd}$ —has also been investigated. Nevertheless, no chiral sideband to the yrast band could be found [\[10\]](#page-12-0). Furthermore, the properties of the chiralcandidate doublet band structure in  $106\text{Ag}$  can be explained in terms of increased gamma softness [\[11\]](#page-12-0) compared to that observed in 104Rh. It is, therefore, interesting to investigate if

this difference is also reflected in the core nuclei <sup>104</sup>Pd and  $102$ Rh. In order to answer this question, we studied the highand medium-spin structure of  $104Pd$ .

Concerning the lowest-energy excited bands,  $^{104}$ Pd is expected to show very similar characteristics to that of its neighboring even-even isotone  $102$ Ru. In the latter nucleus several two-quasiparticle bands have been established [\[12\]](#page-12-0), and thus appearance of similar structures is expected in 104Pd.

Collective and two-quasiparticle excitations in 104Pd have been previously studied via the <sup>94</sup>Zr( $13C,3n\gamma$ ) reaction by Grau *et al.* [\[13\]](#page-12-0). High angular momentum, positive- and negativeparity states have been identified in this work using excitation function, *γ* -ray angular distribution, *γ* -ray linear polarization, and  $\gamma\gamma$ -coincidence measurements. The observed states have been interpreted with the help of a slightly deformed rotor description in terms of the interacting boson model. A more precise linear polarization measurement of *γ* rays assigned to 104Pd has been performed by Stromswold *et al.* [\[14\]](#page-12-0) using a Compton calorimeter. Their linear polarization results clearly showed the negative parity for the two major sidebands. Moreover, a high-spin rotational band has been found in this nucleus by Macchiavelli *et al.* and interpreted as arising from superdeformed shapes [\[15\]](#page-12-0).

Recently, candidate chiral structures in the rhodium isotopes around  $A \sim 104$  were studied by in-beam  $\gamma$  <span id="page-1-0"></span>spectroscopy [\[3,4\]](#page-12-0). In the performed experiment we collected a significant amount of data also on 104Pd, making it possible to extend its band structure. Section II presents the experimental techniques, data evaluation, and results, followed by the interpretation of the experimental findings in Sec. [III.](#page-6-0)

# **II. EXPERIMENTAL METHODS AND RESULTS**

High-spin states in 104Pd were populated using the  $^{96}Zr^{13}C,5n$  fusion-evaporation at beam energies of 51 and 58 MeV. The  $^{13}$ C beam, provided by the the Vivitron accelerator at IReS, Strasbourg, impinged on a stack of two targets, each of thickness 558  $\mu$ g/cm<sup>2</sup> and enriched to 86% in <sup>96</sup>Zr. The emitted  $\gamma$  rays were detected by the Euroball IV detector array [\[16\]](#page-12-0) equipped with 15 cluster [\[17\]](#page-12-0) and 26 clover [\[18\]](#page-12-0) composite Ge detectors. The cluster detectors were placed at backward angles, while the clover detectors were positioned in two rings at an averaged angle of 90◦ relative to the beam direction. The *γ* rays were measured in coincidence with light charged particles in order to eliminate the contaminants from reaction channels produced by evaporation of protons and  $\alpha$  particles from the <sup>109</sup>Pd compound nuclei. The detection of charged particles was performed by means of the highly efficient DIAMANT array, which consisted of 88 CsI detector elements [\[19\]](#page-12-0). Protons and  $\alpha$  particles were used as veto indicators.

A total of  $\sim$ 2 × 10<sup>9</sup> triple and higher-fold coincidence events were accumulated and stored onto magnetic tapes, among which  $\sim$ 4.5 × 10<sup>8</sup> belonged to the <sup>104</sup>Pd reaction channel. The data obtained from the Ge detectors were sorted offline into a three-dimensional histogram by requiring nondetection of any charged particle. For the analysis of the triple-coincidence cube, a standard gating procedure was carried out with the help of the RADWARE software package [\[20\]](#page-12-0). Sample *γ* -ray gated spectra are shown in Fig. 1.

The *γ* -ray energies and relative intensities, derived from the *γγγ* -coincidence cube, are listed in Table I. The Ge detectors were calibrated for both energy and efficiency by using a <sup>152</sup>Eu source placed at the target position. The systematic errors due to the energy and efficiency calibrations were estimated to be ∼0.2–0.3 keV and ∼5%, respectively. Altogether 104 transitions were assigned to  $104Pd$  in the present work.

Information on the multipolarities of transitions with sufficient intensity was extracted from an analysis of directional correlation of oriented nuclei (DCO) ratios [\[21\]](#page-12-0). For the DCO analysis, data obtained from the cluster detectors mounted at an average angle of 156<sup>o</sup> and the clover detectors arranged at about  $90^{\circ}$  were used. A nonsymmetric  $E_{\gamma}$ - $E_{\gamma}$  matrix, comprising of  $\gamma$  rays observed in the cluster detectors along one axis and the *γ* rays observed in the clover detectors along the other axis, was created by requiring nondetection of any charged particle. The ratios  $R_{\text{DCO}} = I_{\gamma\gamma} (156^{\circ}, 90^{\circ} \text{[gate]}) / I_{\gamma\gamma} (90^{\circ}, 156^{\circ} \text{[gate]})$  were extracted, applying corrections for the different efficiencies of the clover and the cluster detector rings. Theoretical DCO ratios have been calculated for the experimental geometry as described in Ref. [\[3\]](#page-12-0). These estimates revealed that a value of  $R_{\text{DCO}} = 1.0$  corresponds to a stretched quadrupole transition



FIG. 1. Typical background subtracted *γγγ* -coincidence spectra showing the placement of band  $3$  (a), band  $4$  (b), band  $6$  (c) and band 7 (d), respectively. Double gates are indicated on the panels.

and  $\approx 0.6$  to a stretched dipole one, when the gating transition is a stretched quadrupole  $\gamma$  ray. For the experimental geometry used, we can expect that  $R_{DCO}$  for a pure nonstretched dipole transition with  $\delta \approx 0$  multipole mixing ratio is approximately the same as for a stretched quadrupole transition. For mixed  $M1 + E2$  transitions  $R_{DCO}$  ratios can vary between 0.5 and 1.0 depending on the  $\delta$  mixing ratio of the  $\gamma$  ray [\[3\]](#page-12-0). The attenuation coefficients of incomplete alignment were fitted to strong transitions with known multipolarities in the calculations.

The DCO ratios obtained in this way for already known transitions of 104Pd are consistent with the previous assignments of Grau *et al.* [\[13\]](#page-12-0) and Stromswold *et al.* [\[14\]](#page-12-0) except for some minor differences. Grau *et al.* assigned  $\Delta I = 1$  $M1 + E2$  multipolarity to the 350 keV transition, while we propose  $\Delta I = 0$  dipole character for this  $\gamma$  ray. A stretched dipole character is obtained for the 858 keV *γ* ray from our experimental data, in contrast with the previous nonstretched M1 assignment of Grau *et al.*. The results of the DCO analysis are summarized in Table I.

The multipolarity assignments were further supported by deducing the electromagnetic character of the transitions by measuring the linear polarization of the  $\gamma$  rays. For this purpose, the four-element clover detectors placed close to 90o relative to the beam direction were used as Compton polarimeters [\[22\]](#page-12-0). Two matrices were constructed from *γγ* events detected in anticoincidence with any charged particle; single hits in any *γ* detector were placed on one axis while the

TABLE I. Energies, relative intensities, DCO ratios, linear polarizations, and deduced multipolarities of transitions assigned to 104Pd in the present work.



<span id="page-3-0"></span>

$E_{\gamma}$ (keV)	$I_{\gamma}$ (rel.)	$R_{\rm DCO}$	$\boldsymbol{P}$	Mult.	$E_i$ (keV)
762.0(3)	1.1(1)				4532
767.9(3)	92.8(43)	1.02(6)	0.54(6)	$\mathop{\mathrm{E2}}$	1324
785.9(3)	1.0(1)				1342
791.9(4)	1.9(2)				4532
794.0(4)	0.8(1)	0.96(12)		$\mathbf{D}^{\mathbf{a}}$	6227
797.3(3)	13.3(12)	1.02(6)	0.76(12)	$\mathop{\mathrm{E2}}$	5433
802.6(3)	22.1(15)	0.96(5)	0.63(8)	$\mathop{\rm E{2}}$	4024
824.5(8)	0.4(1)	0.95(20)		${\bf Q}$	3269
858.1(6)	2.5(2)	0.53(6)		${\rm D}$	2182
864.0(4)	1.1(2)	1.02(17)		${\bf Q}$	5067
879.0(3)	6.3(3)	1.08(8)	0.67(11)	$\mathop{\mathrm{E2}}$	4649
914.5(5)	1.0(2)	0.99(16)			3593
915.4(3)	10.2(8)	1.03(8)	0.46(14)	${\bf Q}$ E2	4964
926.6(3)	73.6(49)	1.05(6)	0.61(7)	$\mathop{\mathrm{E2}}$	2250
926.9(3)	8.9(6)	0.98(7)	0.69(20)	$\mathop{\rm E{2}}$	6360
					5488
955.8(7)	0.8(1)				6024
957.0(4)	1.4(2) 28.8(18)	0.94(5)	0.57(8)	E2	3222
971.2(3)				$D^a$	2298
974.5(3)	1.5(2)	1.07(18)			
990.6(7)	0.4(1)	1.02(21)		${\bf Q}$	4259
990.9(8)	0.2(1)				8099
1019.3(4)	1.6(2)	0.97(10)	0.25(18)	E2	4241
1021.9(8)	0.5(1)				7550
1026.4(5)	0.5(1)	1.03(21)		${\bf Q}$	4619
1032.9(3)	3.9(3)	1.04(8)	0.47(18)	$\mathop{\mathrm{E2}}$	5682
1040.6(6)	0.6(1)				6528
1058.7(3)	6.8(5)	0.97(7)	0.74(28)	E2	6022
1063.8(3)	6.3(5)	1.04(8)	0.76(18)	$\mathop{\rm E{2}}$	7424
1066.4(5)	0.7(1)				7090
1076.2(6)	0.3(1)				8166
1140.5(3)	2.1(2)	0.97(10)	0.74(53)	E2	6822
1147.9(5)	0.4(1)				5389
1159.1(3)	3.3(2)	0.98(7)	0.75(24)	E2	7182
1167.8(3)	13.8(8)	0.51(4)	0.42(19)	E1	2492
1172.5(4)	4.4(3)	0.99(7)	0.99(33)	E2	3422
1193.3(3)	3.3(3)	1.04(8)	0.91(39)	E2	8617
1210.5(4)	0.8(1)	1.02(23)	1.13(57)	E2	8033
1217.9(3)	1.2(2)	1.02(12)	0.65(38)	E2	8399
1256.2(3)	1.5(2)	1.02(11)	0.65(36)	E <sub>2</sub>	9873
1264.8(4)	2.1(2)	0.67(7)	$-0.40(25)$	M1	1821
1312.9(6)	0.5(1)	1.05(20)	1.20(80)	E2	9712
1342.1(7)	0.4(1)	1.08(19)	1.20(82)	E2	1342
1344.1(9)	0.2(1)	1.04(19)	0.65(52)	E2	9377
1344.4(6)	2.8(2)	0.58(6)	0.77(37)	E1	2668
1354.3(6)	1.0(2)	1.03(14)	1.21(64)	E2	2678
1365.2(4)	0.4(1)	1.01(19)		Q	11239
1385.7(7)	0.2(1)				11098
1468.4(6)	0.2(1)				12707
1527.0(3)	1.6(2)	0.93(14)	1.99(102)	E2	2083
1624.4(5)	0.8(1)				2182

TABLE I. (*Continued.*)

<sup>a</sup>Indicates nonstretched  $\Delta I = 0$  dipole transition.

added-back double-hit scattering *γ* energies were placed on the other axis. In the first matrix the scattering events took place perpendicular to the reaction plane, while in the second matrix they occurred parallel to the reaction plane. The number of perpendicular  $(N_{\perp})$  and parallel  $(N_{\parallel})$  scatters for a given  $\gamma$  ray were obtained from spectra gated on the single-hit axis of the respective matrix by transitions in coincidence with the given *γ* ray. Assuming that each clover crystal has equal efficiency, an experimental linear polarization is defined as

$$
P = \frac{1}{Q} \frac{N_{\perp} - N_{\parallel}}{N_{\perp} + N_{\parallel}},
$$
\n(1)

where *Q* is the polarization sensitivity for the clover detectors, which is a function of the  $\gamma$ -ray energy [\[22\]](#page-12-0).  $N_{\perp}$  and  $N_{\parallel}$  denote the number of events scattered perpendicular and parallel to the reaction plane, respectively.  $P > 0$  is characteristic of stretched E1, E2 and nonstretched M1 transitions, while *P <* 0 characterizes stretched M1 and nonstretched E1 transitions. The linear polarization ratios obtained for the previously known transitions of  $104$ Pd are in agreement with the earlier assignments of Stromswold *et al.* [\[14\]](#page-12-0). The results of the linear polarization analysis are given in Table I.

During the multipolarity assignments, only dipole and electric quadrupole transitions were considered. In addition, it was assumed that, in the heavy-ion induced fusion-evaporation reactions, high-spin states are preferably populated and their decays proceed mainly via stretched transitions along the yrast line. Therefore, we assigned the maximum possible spin value allowed by the angular distribution ratios of the transitions to the states. Definite parity was proposed for a state if E1, M1, or quadrupole character could be determined for one of the transitions connecting it to a state with known parity. The multipolarities obtained are listed in Table I.

### **A. The level scheme of 104Pd**

The proposed level scheme shown in Fig. [2](#page-5-0) was constructed using the  $E_{\gamma}$ - $E_{\gamma}$ - $E_{\gamma}$  coincidence relations, energy, and intensity balances. The order of the transitions in the *γ* -ray cascades was deduced from the intensity relations when no other information was available. The placement of the known transitions is consistent with the previous works [\[13–15\]](#page-12-0) except that our coincidence data did not support the existence of the 941 keV  $\gamma$  ray assigned to <sup>104</sup>Pd by Grau *et al.* [\[13\]](#page-12-0). The already known bands (*bands 1, 3, 4*, and *8*) were extended to higher excitation energy and spin. In addition, several new bands (*bands 5, 6, 7*, and *9*) were observed and linked to the previously reported ones.

The yrast *band 1* has been previously reported up to 8  $\hbar$ [\[13–15\]](#page-12-0). In the present work it was extended up to an excitation energy  $E_x = 5.4$  MeV with two additional levels decaying by the 1019 and the 1148 keV transitions. The deduced multipolarities are in agreement with the known spin-parity values for this band, thus we adopt these values up to  $I^{\pi} = 8^{+}$ . On the basis of the DCO and linear polarization analysis, stretched E2 is assigned to the 1019 keV *γ* ray, suggesting an  $I^{\pi} = 10^{+}$  value for the state at 4241 keV. The 1148 keV  $\gamma$  ray is too weak to obtain information on its multipolarity. As this *γ* ray continues the rotational sequence, it is assumed to be a stretched E2 transition and a tentative  $I^{\pi} = (12^{+})$  spin-parity value is assigned to the state at 5389 keV.

*Band 2* has been previously observed up to  $I^{\pi} = (16^{+})$  in Ref. [\[14\]](#page-12-0),  $I^{\pi} = 18^{+}$  in Ref. [\[13\]](#page-12-0), and  $I^{\pi} = (26^{+})$  in Ref. [\[15\]](#page-12-0). Our experimental data confirmed the previous placements of the transitions assigned to this band and the spin-parity values of the levels up to  $I^{\pi} = 18^{+}$ . From the DCO and linear polarization data, stretched E2 character is deduced for

the 1193 and 1256 keV  $\gamma$  rays and quadrupole character is deduced for the 1365 keV  $\gamma$  rays, resulting in unambiguous  $I^{\pi} = 20^{+}$ ,  $22^{+}$ , and  $24^{+}$  spin parities for the states at 8617, 9873, and 11239 keV. The intensity of the 1468 keV *γ* ray is not sufficient to draw a conclusion about its multipolarity, so the spin-parity assignment of the level at 12707 keV remains tentative.

The lower part of *band 3* up to  $I^{\pi} = 15$ <sup>-</sup> has been identified in Refs. [\[13,14\]](#page-12-0). Our coincidence data support the previous placements of the transitions assigned to this band and allow the extension of the band structure by four levels up to an excitation energy  $E_x \approx 11.1$  MeV. In Fig. [1\(a\)](#page-1-0) the sum of triple *γ* -ray gate spectra shows clearly all the transitions placed in this cascade except for the gating 915 and 1159 keV *γ* lines. The extracted multipolarities are in accordance with the former spin-parity assignments of *band 3* up to  $I^{\pi} = 15^{-}$ . On the basis of the deduced stretched E2 characters of the 1159, 1218, and 1313 keV *γ* rays, we propose 17−, 19−, and 21<sup>−</sup> spin-parity values for the levels at 7182, 8399, and 9712 keV. The 1386 keV  $\gamma$  ray is too weak to determine its multipolarity. However, since this transition continues the rotational structure, a tentative  $I^{\pi} = (23^{-})$  spin-parity value is proposed for the state at 11098 keV.

*Band 4* has been reported up to  $I^{\pi} = 14^{-}$  by Grau *et al.* [\[13\]](#page-12-0) and Stromswold *et al.* [\[14\]](#page-12-0). The observed coincidence relations strengthen the positions of the 233, 410, 603, 651, 163, 251, 401, 618, 879, and 1033 keV *γ* rays. Two more linking transitions to *band 3* with energies of 718 and 600 keV were found, and *band 4* was extended by three states that decay by the 1140, 1210, and 1344 keV *γ* rays as shown in Fig. [1\(b\).](#page-1-0) The multipolarities obtained for the transitions placed in the lower part of the band are in agreement with the previous spin-parity assignments [\[13,14\]](#page-12-0). Above the  $I^{\pi} = 14^{-}$  state, the stretched E2 multipolarity of the 1140, 1210, and 1344 keV transitions yields the spin-parity assignments of the 16−, 18−, and 20<sup>−</sup> states.

The lowest-lying negative-parity states at 2182, 2298, and 2492 keV have been established in Refs. [\[13,14\]](#page-12-0). Our experimental data confirm the stretched E1 multipolarity for the 1168 keV *γ* ray suggested by Stromswold *et al.* [\[14\]](#page-12-0) and, thus, the firm  $I^{\pi} = 5^-$  assignment for the 2492 keV initial state.  $I^{\pi} = 4^+$  and  $4^-$  spin-parity values have been proposed by Grau *et al.* [\[13\]](#page-12-0) for the states at 2182 and 2298 keV, respectively. The stretched E2 character obtained for the 603 keV transition, which connects the  $I^{\pi} = 6^{-}$ 2901 keV and the 2298 keV states, strengthens the  $I^{\pi} = 4^{-}$ assignment to the latter one. The 2182 keV level is fed by the 116 and 310 keV  $\gamma$  rays from the 3<sup>-</sup> and 5<sup>-</sup> states at 2298 and 2492 keV, as well as being connected by the 858 and 1624 keV transitions to the yrast  $2^+$  and  $4^+$  states. The stretched quadrupole character of the 310 keV *γ* ray deduced from our DCO data suggests a  $I^{\pi} = 3^{-}$  spin-parity for the 2182 keV state, contrary to the  $4^+$  value of Grau *et al.* [\[13\]](#page-12-0). Our assignment is supported by the stretched dipole character obtained for the 116 and 858 keV transitions.

Besides the major sideband structures, two new bands (*bands 5* and *6*) were found to decay to negative-parity states. On the basis of the coincidence relations, *band 5* is connected to *bands 3* and *4*, among others, by the M1 588 keV and

<span id="page-5-0"></span>

FIG. 2. The partial level scheme of <sup>104</sup>Pd obtained in the present work.

the E2 751 keV  $\gamma$  rays, thereby firmly establishing negative parity for *band 5*. The stretched quadrupole nature of the 751 keV transition and the stretched character of the 588 keV transition determine the  $I = 9$  spin assignment for the lowest level in the band at 3740 keV. The 762 and 792 keV *γ* rays, deexciting the next state in the band at 4532 keV, were too weak to determine their multipolarities. In order to deduce

an unambiguous spin-parity of this level, the stretched dipole assignment of the 535 keV  $\gamma$  line was used. This transition feeds the 4532 keV state from the 12<sup>−</sup> 5067 keV one; hence, an  $I^{\pi} = 11^{-}$  value is proposed for the final state. Due to the insufficient intensity of the 956, 1041, and 1022 keV *γ* rays, tentative  $I^{\pi} = (13^{-})$ ,  $(15^{-})$ , and  $(17^{-})$  values are assigned to the higher observed levels in *band 5*.

<span id="page-6-0"></span>In *band 6* Grau *et al.* have identified the lowest-lying 467, 350, and tentatively the 701 keV  $\gamma$  rays of <sup>104</sup>Pd [\[13\]](#page-12-0). Based on the coincidence relations, shown in Fig.  $1(c)$ , we assigned these transitions to a rotational structure, which was extended by four additional transitions up to an excitation energy  $E_x \approx$ 8*.*2 MeV and connected to *bands 4* and *5* by three more *γ* rays. In the case of the 467 keV transition a stretched M1 multipolarity was obtained, establishing a firm  $I^{\pi} = 6^{-}$ spin-parity for the lowest level in the band at 2959 keV. The 4203 keV state is connected by the stretched M1 463 keV *γ* ray to the 9<sup>-</sup> state in *band* 5, thus, the  $I^{\pi} = 10^{-1}$  value is assigned to this level. The  $I^{\pi} = 8^-$  spin-parity of the middle-lying 3502 keV state was determined from the stretched E2 character of the feeding 701 keV transition. This assignment is confirmed by the  $\Delta I = 0$  nonstretched dipole nature of the deexciting 350 keV  $\gamma$  line. Above the  $I^{\pi} = 10^{-1}$  state, the stretched quadrupole character of the 864 keV transition yields the spin parity of the 12<sup>−</sup> state. The intensities of the 957, 1066, and 1076 keV  $\gamma$  rays are not sufficient to draw a conclusion about their multipolarities, so the spin-parity assignments of the levels at 6024, 7090, and 8166 keV remain tentative.

In addition to the already known positive-parity bands, there appeared three other rotational-like structures, *bands 7, 8,* and *9*, connected to this part of the level scheme. The 1265 keV *γ* ray linking the lowest-lying state in *band 7* to the yrast band has been observed by Grau *et al.*, and a stretched M1 multipolarity has been assigned to it [\[13\]](#page-12-0). On the basis of our experimental data, we confirmed the position of this transition and the  $I^{\pi} = 3^+$  spin parity of its initial state at 1821 keV. Using the observed coincidence relations, shown in Fig.  $1(d)$ , a new band was built on this state up to an excitation energy  $E_x \approx 4.3$  MeV. Based on the quadrupole character of the 624, 824, and 991 keV *γ* rays, we propose 5+, 7+, and  $9^+$  spin-parity values for the levels at 2445, 3269, and 4259 keV.

The yrare  $2^+$  and  $4^+$  states have been identified by Grau *et al.* [\[13\]](#page-12-0). Our coincidence data confirm the previous placements of the 1342, 786, 741, 1527, and 759 keV transitions, and make possible extending the cascade by three levels and connecting to *band 1* and *7* by several transitions. The obtained stretched E2 and quadrupole multipolarities of the 1342, 1527, and 741 keV  $\gamma$  rays are in accordance with the spin parities of the states at 1342 and 2083 keV, thus, we adopt the  $I^{\pi} = 2^{+}$  and 4<sup>+</sup> values for them. On the basis of the DCO and linear polarization analysis, stretched E2 character is deduced for the 1354 keV transition and quadrupole character is deduced for the 914 and 1026 keV transitions, suggesting unambiguous  $I^{\pi}$ =6<sup>+</sup>, 8<sup>+</sup>, and 10<sup>+</sup> values for the states at 2678, 3593 and 4619 keV. The assignments in *band 7* and *8* are further corroborated by the  $\Delta I = 1$  (233, 361, and 666) keV  $\gamma$  rays) and the  $\Delta I = 0$  (371, 428, and 759 keV  $\gamma$  rays) dipole natures of the linking transitions.

In *band 9* mainly the linking transitions to *band 2* were observed. Unfortunately, these *γ* rays do not have enough intensity for us to get any information on their multipolarities. If we assigned stretched quadrupole character to them, these states would become yrast, which contradicts the fact that this band population is less than 10 times weaker than the yrast *band 2* at this spin region. Thus, we assume tentative

 $I^{\pi} = (14^+), (16^+), (18^+), (20^+),$  and  $(22^+)$  spin-parity values for the states at 6227, 7108, 8099, 9191, and 10468 keV, respectively.

#### **III. DISCUSSION**

The  $104Pd$  nucleus with its six valence protons and eight valence neutrons lies in the upper part of the *g*9*/*<sup>2</sup> proton subshell and in the middle part of the  $d_{5/2}$ ,  $g_{7/2}$  neutron subshell, where the low- $\Omega$   $h_{11/2}$  orbitals intrude already at small deformations. According to previous studies [\[13,14\]](#page-12-0), *bands 2, 3,* and *4* correspond to two-quasiparticle bands being built on the aligned positive-parity  $v(h_{11/2})^2$  and negativeparity *νh*11*/*2*,*(*d*5*/*2*,g*7*/*2) configurations, respectively. To get a deeper insight into the structure of the observed bands, total Routhian surface (TRS) calculations based on the Woods-Saxon cranking formalism [\[23–25\]](#page-12-0) were performed and compared with Routhians (*E* ) and aligned angular momenta  $(I_x,i_x)$  [\[26\]](#page-12-0).

In  $104$ Pd at slight deformations, the neutron Fermi surface is located near the [411]3*/*2 and [413]5*/*2 positive-parity Nilsson states arising from the *d*5*/*2, *g*7*/*<sup>2</sup> subshell, as well as the [550]1*/*2 and [541]3*/*2 negative-parity Nilsson states originating from the  $h_{11/2}$  orbital. With increasing rotational frequency the high- $j$  low- $\Omega$  [550]1/2 state moves closer to the Fermi surface, and thus this orbital is presumed to contribute to the lowest-energy excited rotational bands. These assumptions are in a good agreement with the results that in both  $103Pd$  [\[27\]](#page-12-0) and <sup>105</sup>Pd [\[28\]](#page-12-0) the two lowest-lying positive-parity bands are assigned to the  $d_{5/2}$ ,  $g_{7/2}$  origin, and the negative-parity band built on the  $h_{11/2}$  configuration becomes the yrast structure above  $I^{\pi} = (11^{-})$ . Moreover, in <sup>105</sup>Pd the alignment of the  $h_{11/2}$  neutron pair appears in higher-energy positive-parity states. The proton Fermi surface lies in the middle of the unique-parity *g*9*/*<sup>2</sup> subshell, close to the [303]5*/*2 and [301]1*/*2 normal-parity Nilsson orbitals.

The  $i_x$  experimental alignments presented in Fig.  $3$ , were deduced by subtracting a reference based on a variable moment of inertia  $J_{\text{ref}} = J_0 + \omega^2 J_1$  with  $J_0 = 14 \hbar^2/\text{MeV}$  and



FIG. 3. Experimental alignments *ix* of *bands 1–6* and *9*. A frequency-dependent moment-of-inertia reference was subtracted.

<span id="page-7-0"></span> $J_1 = 15 h^4/\text{MeV}^3$ . The *K* quantum number was taken to be 0 for the ground-state band, since it corresponds to the quasiparticle vacuum configuration at low rotational frequency. *Bands 3, 4, 5,* and *6* are considered to be twoquasineutron configurations involving the [550]1*/*2 and one of the [411]3*/*2 or [413]5*/*2 Nilsson orbitals, which we assume to have  $K = 1/2$ ,  $3/2$ , and  $5/2$  values, respectively. Consequently, the possible *K* values for these bands are 1, 2, or 3, of which an average value of 2 was applied in calculating the alignments, in accordance with Ref. [\[13\]](#page-12-0). We note that at higher spins the alignment of a band is not sensitive to varying the value of *K* by one or two units.

The positive-parity *band* 2 of <sup>104</sup>Pd has been assigned to the two-quasiparticle *ν*(*h*11*/*2) <sup>2</sup> configuration [\[13,14\]](#page-12-0). According to this expectation, the alignment of a  $h_{11/2}$  neutron pair is clearly visible at frequency  $\hbar \omega \approx 0.4$  MeV in Fig. [3,](#page-6-0) with nearly the full possible alignment gain of ∼10  $\hbar$ . *Band 1* shows a small, about  $2 \hbar$ , alignment at a higher frequency of  $\sim$  0.5 MeV/h, which might be a sign of the  $\pi(g_{9/2})^2$  alignment. Such an alignment is seen also for *bands 5* and *6*, in good agreement with the corresponding TRS results. In *bands 3, 4, 5,* and *6* the *νh*11*/*<sup>2</sup> alignment seems to be blocked, as they do not show a similar alignment gain at ∼0.4 MeV*/h*¯ . This results in their configurations containing one neutron in the  $h_{11/2}$  orbit. On the basis of the alignment curves these bands are supposed to be configured by two quasiparticles. Since the parity of these bands is negative, the second quasineutron is expected to have a *g*7*/*2, *d*5*/*<sup>2</sup> origin.

According to these considerations, total Routhian surface TRS calculations were performed for the vacuum and for two-quasiparticle configurations with one quasineutron in the  $h_{11/2}$  state and another one in the four lowest-energy positiveparity states. For labeling of the lowest-energy quasineutron states, the commonly used notations, given in Table  $II$ , are adopted.

### **A. The yrast positive-parity bands**

The experimental Routhians (*E* ) and the aligned angular momenta  $(I_x)$  are compared with the results of the TRS calculations in Figs.  $4$  and  $5$ , respectively. The calculated  $E'$  curves are normalized so that the experimental and the theoretical Routhians of the yrast band overlap each other. The yrast

sequence agrees well with the vacuum configuration of the TRS calculations before the first  $h_{11/2}$  neutron pair is aligned, while *band 2* corresponds with the vacuum configuration after this alignment. The TRS calculations give a good overall description of the Routhians and the aligned angular momenta. The predicted shape for *band 1* starting from  $\hbar \omega \approx 0.3$  MeV is characterized by  $\beta_2 \approx 0.14$  and  $\gamma \approx -2^\circ$ , while the  $\nu(h_{11/2})^2$ alignment drives it to slightly larger  $\beta_2 \approx 0.19$  and  $\gamma \approx 5^\circ$ values for *band 2*.

#### **B. The negative-parity bands**

As can be seen from the experimental alignments  $i_x$ of *bands 3* and *4* in Fig. [3,](#page-6-0) and as discussed before, the structures of these bands are determined by similar two-quasineutron configurations. The lowest-energy negativeparity two-quasineutron configurations are expected to involve one quasineutron from the E  $h_{11/2}$  orbital and another quasineutron from the A or B *d*5*/*2, *g*7*/*<sup>2</sup> orbitals. Based on the good agreement between the experimental and the calculated Routhians (see Fig. [4\)](#page-8-0), we suggest that these coupled bands have a  $vh_{11/2}$ ,  $(d_{5/2}, g_{7/2})$  configuration.

The TRS calculations for aligned angular momentum predict the appearance of a proton alignment at about 0.53 MeV/ $\hbar$  in the case of *bands 3* and 4. In nuclei with  $A \sim 100$  below the  $Z = 50$  shell closure, most probably the *g*9*/*<sup>2</sup> alignment appears at this frequency. Contrary to the calculated curves, the experimental values show a more gradual change in  $I_x$  at a higher frequency of  $\sim$ 50–70 keV/ $\hbar$ , as is visible in Fig. [5.](#page-8-0) This discrepancy might be caused by larger deformations than  $\beta_2 \approx 0.15$  and  $\gamma \approx -2^\circ$  derived from the TRS calculations, as was similarly suggested in the case of  $102$ Ru [\[12\]](#page-12-0).

The alignment behavior of *bands 5* and *6* seems to be similar to *bands 3* and *4*, as presented in Fig. [3.](#page-6-0) According to the TRS calculations, one quasineutron placed in the E  $h_{11/2}$  orbitals and the other one in the C or D  $d_{5/2}$ ,  $g_{7/2}$ orbitals can account for the next lowest-energy negative-parity configurations. Since the experimental  $E'$  curves are in a good agreement with the theoretical Routhians (see Fig. [4\)](#page-8-0), we propose a  $vh_{11/2}$ ,  $(d_{5/2}, g_{7/2})$  configuration for *bands* 5 and 6. For the CE and DE states the calculations predict a  $\beta_2 \approx 0.17$ deformation and a small  $\gamma \approx 7^{\circ}$  triaxiality similarly to the AE and BE  $vh_{11/2}$ ,  $(d_{5/2}, g_{7/2})$  states. It is worth mentioning that the experimental aligned angular momentum values of

TABLE II. Labels used for the quesiproton (p) and quasineutron (n) states for parity  $\pi$  and signature  $\alpha$ , with *n* denoting the *n*th such state.

	p			n	
$(\pi,\alpha)_n$	Label	Shell model	$(\pi,\alpha)_n$	Label	Shell model
$(+, +1/2)_{1}$	a	89/2	$(+, +1/2)$ <sub>1</sub>	A	$d_{5/2}, g_{7/2}$
$(+,-1/2)1$	b	89/2	$(+,-1/2)1$	B	$d_{5/2}, g_{7/2}$
$(-,-1/2)1$	$\epsilon$	$p_{1/2}$	$(+, +1/2)_{2}$	C	$d_{5/2}, g_{7/2}$
$(-, +1/2)$ <sub>1</sub>		$p_{1/2}$	$(+,-1/2)_{2}$	D	$d_{5/2}, g_{7/2}$
			$(-,-1/2)1$	E	$h_{11/2}$
			$(-, +1/2)_1$	F	$h_{11/2}$
			$(-,-1/2)_{2}$	G	$h_{11/2}$
			$(-, +1/2)_{2}$	Η	$h_{11/2}$

<span id="page-8-0"></span>

FIG. 4. Comparison of the experimental and theoretical Routhians *E'* for *bands*  $1-6$  and  $10$ .

*bands* 5 and 6 show a sharper  $\pi g_{9/2}$  alignment than those of the other two negative-parity bands. The observed alignment frequency overlaps with the ∼0.53 MeV/h calculated one, as can be seen in Fig. 5. As *band 1* shows a similar behavior at about this frequency, it is also assumed to correspond to the alignment of a *g*9*/*<sup>2</sup> quasiproton pair.

The  $B(M1)/B(E2)$  ratios within a  $\Delta I = 1$  band are sensitive to the quasiparticle configuration of the band. Thus, to corroborate the configuration assignments of the negative-parity bands, we deduced the experimental  $B(M1; I \rightarrow I-1)/B(E2; I \rightarrow I-2)$  ratios of reduced transition probabilities from the measured  $I_{\nu}(M1)/I_{\nu}(E2)$  branching ratios for *bands 3, 4,* and *6*. Since there is no observed M1 transition in *band 5* corresponding to the signature partner, reduced transition probability ratios could not be obtained for it. The  $B(M1)/B(E2)$  ratios were extracted using the



FIG. 5. Comparison of the experimental and TRS aligned angular momenta *Ix* for *bands 1-6* and *10*.

expression

$$
\frac{B(M1; I \to I - 1)}{B(E2; I \to I - 2)} = 0.697 \frac{E_{\gamma}^{5}(E2)}{E_{\gamma}^{3}(M1)} \frac{I_{\gamma}(M1)}{I_{\gamma}(E2)} \frac{1}{1 + \delta^{2}} \left(\frac{\mu_{N}}{eb}\right)^{2}, \qquad (2)
$$

where the energies of the *γ* rays are given in MeV. The branching ratios were determined by setting gates on the transitions above the decaying level. The *δ*-multipole mixing ratios of the  $\Delta I = 1$  transitions were assumed to be small, and thus *δ*<sup>2</sup> can be neglected. The experimental *B*(*M*1)*/B*(*E*2) ratios were compared to calculated values obtained, as described in detail in Ref. [\[12\]](#page-12-0).

The experimental *B*(*M*1)*/B*(*E*2) ratios for *bands 3, 4,* and *6* are plotted in Fig. [6](#page-9-0) together with the calculated values. The observed  $B(M1)/B(E2)$  ratios fall between the theoretical curves corresponding to the *νd*5*/*2*h*11*/*<sup>2</sup> and *νg*7*/*2*h*11*/*<sup>2</sup> configurations, somewhat closer to the former one, which further strengthens the proposed two-quasineutron structure of the negative-parity bands.

<span id="page-9-0"></span>

FIG. 6. Experimental and calculated *B*(*M*1)*/B*(*E*2) ratios of *bands 3, 4, 6,* and *10*.

#### **C. The low-spin negative-parity states**

In the regions of nuclei with neutron or proton number near 34, 56, and 88, strong octupole effects are expected, since the Fermi surface is between the  $g_{9/2} - p_{3/2}$ ,  $h_{11/2} - d_{5/2}$ , and  $i_{13/2}$ *f*7*/*<sup>2</sup> orbitals [\[38\]](#page-12-0), respectively. Accordingly, the appearance of octupole structures can be expected for  $\frac{104}{Pd}$ , due to it having 58 neutrons. One of the fingerprints of octupole correlation is the presence of a low-lying 3<sup>−</sup> collective state. Indeed, a 3<sup>−</sup> state is observed at 2182 keV in <sup>104</sup>Pd, the octupole character of which can be tested using a simple parametrization established by Zamfir *et al*. for the energies of  $3<sub>1</sub><sup>-</sup>$  states in all nuclei with  $A > 30$  [\[39\]](#page-12-0):

$$
E(3_1^-) = 19A^{-1/3} - 0.5\sqrt{N_p + N_n},
$$
 (3)

where  $E(3<sub>1</sub><sup>-</sup>)$  is obtained in MeV, and  $N<sub>p</sub>$  and  $N<sub>n</sub>$  are the valence-proton and -neutron numbers, respectively. Differences from the curve characterizing the normal behavior nuclei indicate octupole correlations. In Fig. 7 the energies of the first 3<sup>−</sup> states in Mo, Ru, and Pd nuclei are compared to the curves derived for the corresponding isotope chains. The valence-proton numbers  $N_p$  were counted from the  $Z = 40$ subshell closure, while the valence-neutron numbers  $N_n$  were taken from the  $N = 50$  shell closure. In the case of Mo nuclei the experimental energies fall below the calculated curve by  $~\sim$ 600–700 keV, in agreement with the presence of octupole collectivity observed in <sup>98</sup>*,*100*,*102Mo [\[40\]](#page-12-0). For Ru isotopes the deviations decrease and for Pd nuclei the experimental values lie close to the calculated curve. On the basis of this fact, the  $3<sub>1</sub><sup>-</sup>$  state in <sup>104</sup>Pd may not be connected to octupole correlations.

In the interpretation of the closely spaced 3−, 4−, and 5<sup>−</sup> states at 2182, 2298, and 2492 keV, another hint can be obtained from the  $i_x$  experimental alignments (see Fig. [3\)](#page-6-0). Compared to the yrast band, *band 10* shows an alignment gain of  $\sim$ 4 *h*, so it is assumed to be configured by two quasiparticles. As more two-quasineutron structures are not expected below *bands 3, 4, 5*, and *6* belonging to the  $v h_{11/2}$ , ( $d_{5/2}$ ,  $g_{7/2}$ ) configurations, *band 10* can be built on two-quasiproton configurations. Indeed, similar structures



FIG. 7. Energies of the first 3<sup>−</sup> states in Mo, Ru, and Pd isotopes compared to the curves obtained from Eq.  $(3)$ . The data for <sup>96–108</sup>Ru and <sup>102</sup>*,*106–110Pd are taken from Refs. [\[29–37\]](#page-12-0).

have been found in  $N = 44$  isotones <sup>78</sup>Se, <sup>80</sup>Kr, <sup>82</sup>Sr, and <sup>84</sup>Zr [\[41–45\]](#page-12-0), and assigned to noncollective *νg*<sub>9</sub>*/*2,(*p*<sub>1/2</sub>, *f<sub>5/2</sub>*) configurations [\[45\]](#page-12-0). In Pd isotopes with proton number  $Z = 46$ , analogous two-quasiproton excitations can be expected.

In <sup>103</sup>Rh, the odd-Z neighbor of <sup>104</sup>Pd, bands built on the ground state and the low-lying isomer state have been observed and assigned to the  $\pi p_{1/2}$  and  $\pi g_{9/2}$  one-quasiproton configurations [\[46\]](#page-12-0), respectively. The  $5/2<sub>1</sub><sup>-</sup>$  state related to the  $\pi f_{5/2}$  configuration has been found at a higher excitation energy of 880 keV [\[46\]](#page-12-0). Accordingly, the  $\pi g_{9/2}$  and the  $\pi p_{1/2}$  orbits should be close to the Fermi surface also in  $104Pd$ , and the lowest-lying two-quasiproton excitations are expected to belong to the  $\pi g_{9/2} p_{1/2}$  configuration, while the  $\pi g_{9/2} f_{5/2}$  structures are assumed to appear at higher excitation energies of about 800 keV. Thus, we tentatively propose that the  $\pi g_{9/2} p_{1/2}$  two-quasiproton configuration belongs to these low-lying negative-parity states.

In the TRS calculations the lowest-energy negative-parity two-quasiproton configurations are predicted to be built on one quasiproton from the *a* and *b g*9*/*<sup>2</sup> orbitals and another quasiproton from the *e* and  $f$   $p_{1/2}$  orbitals. The explanation of the labeling of quasiproton states is given in Table  $II$ . The reasonable agreement between the experimental and the calculated Routhians and aligned angular momenta, presented in Figs. [4](#page-8-0) and [5,](#page-8-0) strengthens the  $\pi g_{9/2} p_{1/2}$  configuration assignment to *band 10*. For these states the calculations predict a shape with  $\beta_2 \approx 0.15$  and  $\gamma \approx -10^\circ$ .

In the case of *band 10* we could extract the experimental  $B(M1)/B(E2)$  ratio only for one excited state placed at 2492 keV. The obtained ratio is presented in Fig. [6](#page-9-0) together with the calculated curve corresponding to the  $\pi g_{9/2} p_{1/2}$ configuration. In the calculations we applied *g* factors of 0.5 and 1.1 for the  $\pi p_{1/2}$  and the  $\pi g_{9/2}$  configurations, respectively, obtained from the magnetic moments  $\mu$  of the corresponding states in  $^{103}$ Rh [\[46\]](#page-12-0). The  $\beta_2$  and  $\gamma$  shape parameters were chosen according to the TRS predictions, while the signature splitting was not taken into account in the calculations. Further details of the analysis are described above in Sec.[III B.](#page-7-0) Comparing the experimental and calculated values, the observed  $B(M1)/B(E2)$  ratio lies close to the theoretical curve of the  $\pi g_{9/2} p_{1/2}$  configuration, which further supports the proposed two-quasiproton stucture of *band 10*.

# **D. The B(E1) transition strengths**

Although the  $3<sub>1</sub><sup>-</sup>$  state in <sup>104</sup>Pd does not show the origin of permanent octupole deformation, in the case of the negativeparity bands the excitation of  $h_{11/2}$  neutrons may induce some octupole correlations. In  $^{100}$ Pd signs of octupole collectivity have been found at negative-parity higher-spin states [\[47\]](#page-12-0). In nuclei with neutron numbers above  $N = 50$ , one of the lowest-energy positive-parity orbitals is the *νd*<sub>5/2</sub>, and, hence, the excitations into the  $v h_{11/2}$  orbital are favored by coupling to the octupole phonon [\[48\]](#page-12-0). The observation of enhanced  $\Delta I = 1E1$  transitions would indicate the presence of octupole collectivity [\[49\]](#page-12-0), therefore we analyzed the relevant transitions from this perspective.

Since the *E*1 operator connects states from two different shells, they are always very hindered. In the  $A = 100$  mass region the single-proton *E*1 transitions are hindered by a factor of  $1-3 \times 10^{-6}$  in odd Ag and In isotopes, while the singleneutron transitions are hindered by a factor of  $1-2 \times 10^{-5}$  in odd Cd isotopes.

The  $B(E1)$  values for the  $E1$  linking transitions between *bands* 2 and 3 were estimated from the  $I_\nu(E1)/I_\nu(E2)$ branching ratios using the following expression:

$$
\frac{B(E1; I \to I - 1)}{B(E2; I \to I - 2)} = \frac{1}{1.3 \times 10^6} \frac{E_{\gamma}^5(E2)}{E_{\gamma}^3(E1)} \frac{I_{\gamma}(E1)}{I_{\gamma}(E2)} \text{ (fm}^{-2)}, \quad (4)
$$

where the energies of the  $\gamma$  rays are given in MeV. The  $B(E2)$ values were calculated as

$$
B(E2; I \to I - 2) = \frac{5}{16\pi} Q_0^2 |\langle J_i K 20 | J_f K \rangle|^2, \qquad (5)
$$

TABLE III. The reduced E1 transition probabilities in 104Pd estimated from branching ratios, compared to known values in <sup>100</sup>Pd and <sup>117</sup>*,*119Cd.

<b>Nucleus</b>	$E_{\nu}$ (keV)	$I_i^n \to I_f^n$	$B(E1)$ (W.u.)
104Pd	655	$10^+ \rightarrow 9^-$	$6.3(8) \times 10^{-5}$
	588	$12^+ \rightarrow 11^-$	$3.1(2) \times 10^{-5}$
	469	$14^{+} \rightarrow 13^{-}$	$3.4(8) \times 10^{-5}$
100P <sub>d</sub>	994		$1.5(3) \times 10^{-5}$
	718		$3.9(3) \times 10^{-5}$
	908		$1.4(3) \times 10^{-5}$
	591		$5.1(4) \times 10^{-5}$
	998		$1.6(4) \times 10^{-5}$
	786		$3.2(4) \times 10^{-5}$
	706		$1.2(2) \times 10^{-4}$
117 <sub>cd</sub>	205		$2.0(2) \times 10^{-5}$
	220		$9.4(9) \times 10^{-6}$
119Cd	199		$1.1(1) \times 10^{-5}$
	213		$9.4(2) \times 10^{-6}$

where values  $K = 1$  and  $Q_0 = 2$  *eb* obtained from the prediction of the TRS calculations for *band 3* were used.

It can be seen from the deduced  $B(E1)$  probabilities given in Table III that the hindrance factors are about  $3-6 \times 10^5$ . As *band 3* shows two-quasineutron character, the obtained values are to be compared to those known in Cd isotopes. On the basis of this comparision the *E*1 transitions observed in <sup>104</sup>Pd are only slightly enhanced, if they are enhanced at all. The deduced low values of enhancement mean that signs of octupole correlations were not found in 104Pd.

#### **E. The quasi-***γ* **bands 7 and 8**

Low-lying cascades built on the second  $2^+$  state have been observed in several Pd and Ru isotopes in the  $A \approx 100$  mass region. Recently, such a structure has been identified also in  $102$ Ru, and it was interpreted as a quasi- $\gamma$  band associated with *γ* -soft triaxial deformation, which might be confined in a region away from axial symmetry [\[5\]](#page-12-0). Since the nuclear structure of  $104Pd$  shows characteristics similar to that of  $102Ru$ , having only 2 protons less, the existence of a quasi-*γ* band is expected also in the studied nucleus.

The levels of the non-yrast low-lying positive-parity *bands 7* and *8* established in the present work were grouped into a *γ* band that is built on the second  $2^+$  state at 1342 keV. The band assignment is based on the observed decay pattern and on the similarities with the structure of  $102$ Ru. A distinction between excitations in a  $\gamma$ -soft and a  $\gamma$ -rigid potential can be deduced from the energy sequence in the *γ* band, and can be expressed in the odd-even spin energy staggering function

$$
S(I, I-1, I-2) = \frac{E(I) + E(I-2) - 2E(I-1)}{E(2_1^+)}.
$$
 (6)

In the case of a triaxial rigid rotor this staggering gives positive values for even spins and negative ones for odd spins. For a *γ* -soft rotor it has an opposite phase: the values fall below 0 for even spins and above 0 for odd spins.



FIG. 8. Experimentally observed odd-even spin energy staggering in *bands 7* and *8* (solid circles, solid line) compared to the values of the quasi- $\gamma$  band in <sup>102</sup>Ru (open triangles, solid line) [\[5\]](#page-12-0). The lines between the symbols are drawn to guide the eye.

The experimental odd-even spin energy staggering deduced for *bands 7* and *8* is displayed in Fig. 8 together with the values extracted for  $^{102}$ Ru [\[5\]](#page-12-0). The values obtained for  $^{104}$ Pd are the same order of magnitude as in <sup>102</sup>Ru. They vary between the negative values of −0.23 and −0.53 for even spins, and they fall between the positive values of 0.17 and 0.62 for odd spins. The resulting phase of the staggering is the same in both  $104Pd$ and 102Ru. According to the obtained odd-even spin energy



FIG. 9. Energy ratios  $E(2^+_2)/E(4^+_1)$  deduced for Pd and Ru isotopes. The data for  $96-108$ Ru and  $102,106-110$ Pd are taken from Refs. [\[29,31–37\]](#page-12-0). The lines between the symbols are drawn to guide the eye.

staggering in  $^{104}$ Pd, we can rule out the rigid triaxial rotor scenario and assign a *γ* -soft character to this nucleus. It is worth mentioning that the size of the staggering is about the same at the bottom part of the  $\gamma$  bands in both <sup>104</sup>Pd and <sup>102</sup>Ru, while it increases at higher spins in  $^{104}$ Pd, unlike  $^{102}$ Ru. This might indicate a more  $\gamma$ -soft shape at the higher-spin region in  $104$ Pd compared to  $102$ Ru.

The *γ* softness in the Pd and Ru isotopes can be compared by deducing the energy ratio  $E(2_2^+)/E(4_1^+)$ . In terms of the *γ*-fluctuating triaxial rotor model  $[45,50]$ , the *γ* softness of the potential is represented by the energy of the second  $2^+$ state relative to that of the yrast  $4^+$  state: the softer the nucleus, the lower the  $2^+_2$  state relative to the  $4^+_1$  one. The ratios  $E(2^+_2)/E(4^+_1)$  obtained for Pd and Ru isotopes between neutron numbers  $N = 52$  and 64 are presented in Fig. 9. In the case of Ru isotopes the degree of  $\gamma$  softness seems to remain about the same above  $N = 54$ . For Pd isotopes the observed curve indicates increasing *γ* softness with increasing neutron number, crossing the pattern of Ru nuclei at  $N = 58$ . Above this neutron number this feature can cause a difference in the possible formation of chiral stuctures in Ag and Rh nuclei, of which Pd and Ru isotopes serve as cores, respectively.

### **IV. SUMMARY**

High-spin states of <sup>104</sup>Pd were studied via the <sup>96</sup>Zr(<sup>13</sup>C,5*n*) reaction using the Euroball IV *γ* -ray spectrometer coupled with the DIAMANT array for the detection of charged particles. All earlier known bands were extended significantly and additional bands were identified. On the basis of the deduced  $B(M1)/B(E2)$  ratios and the comparison of the experimental Routhians and aligned angular momenta to the predictions of Woods-Saxon TRS calculations, the  $v h_{11/2}$ ,  $(d_{5/2}, g_{7/2})$  configuration was assigned to the highspin negative-parity bands. Besides these two-quasineutron structures, also two-quasiproton structures were found in this mass region, the low-spin negative-parity states were identified as belonging to the  $\pi g_{9/2} p_{1/2}$  configuration. The non-yrast low-lying positive-parity bands observed were interpreted as excitations associated with *γ* -soft deformation on the basis of their energy staggering as a function of spin.

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