

## Production of $^{26}\text{Al}$ in stellar hydrogen-burning environments: Spectroscopic properties of states in $^{27}\text{Si}$

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Model predictions of the amount of the radioisotope  $^{26}\text{Al}$  produced in hydrogen-burning environments require reliable estimates of the thermonuclear rates for the  $^{26}\text{gAl}(p,\gamma)^{27}\text{Si}$  and  $^{26}\text{mAl}(p,\gamma)^{27}\text{Si}$  reactions. These rates depend upon the spectroscopic properties of states in  $^{27}\text{Si}$  within about 1 MeV of the  $^{26}\text{gAl} + p$  threshold ( $S_p = 7463$  keV). We have studied the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction at 25 MeV using a high-resolution quadrupole-dipole-dipole magnetic spectrograph. For the first time with a transfer reaction, we have constrained  $J^\pi$  values for states in  $^{27}\text{Si}$  over  $E_x = 7.0\text{--}8.1$  MeV through angular distribution measurements. Aside from a few important cases, we generally confirm the energies and spin-parity assignments reported in a recent  $\gamma$ -ray spectroscopy study. The magnitudes of neutron spectroscopic factors determined from shell-model calculations are in reasonable agreement with our experimental values extracted using this reaction.

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### I. INTRODUCTION

Radioactive nuclei produced in various astrophysical phenomena may  $\beta$  decay to daughter nuclei in excited states, which subsequently deexcite through the emission of characteristic  $\gamma$  rays. The high penetrating power of  $\gamma$  rays permits direct translation of these observables into abundances of the mother nuclei, which can then be used to constrain and test nucleosynthesis predictions from stellar models. Obtaining absolute abundances using measurements from elsewhere in the electromagnetic spectrum generally requires additional, possibly speculative assumptions regarding the environments (e.g., stellar atmospheres) under consideration; moreover, such observations generally only provide elemental (as opposed to isotopic) abundances. Since the 1.809-MeV  $\beta$ -delayed  $\gamma$ -ray line from the decay of the ground state of  $^{26}\text{Al}$  ( $t_{1/2} = 7.2 \times 10^5$  y,  $J^\pi = 5^+$ ) is the most thoroughly examined case [1–7], its intensity and distribution within the galaxy provides one

of the most robust constraints on nucleosynthesis predictions from theoretical models. Reproducing the inferred abundance of  $^{26}\text{Al}$  in the galaxy ( $2.7 \pm 0.7 M_\odot$  [7]) with a single model (or several models accounting for different nucleosynthesis sites) could have far-reaching consequences. For example,  $^{26}\text{Al}$  is inferred to have been present in the early solar system to the level of  $^{26}\text{Al}/^{27}\text{Al} \sim 5 \times 10^{-5}$  (from meteoritic inclusions, see e.g., Ref. [8]) and the energy released by its decay was partially responsible for the melting and differentiation of planetesimals (see e.g., Refs. [9,10]), the first large bodies to form in the solar system. Planetesimals may in turn have been the source of much of Earth's water [11,12], so the habitability of our planet could be directly linked to the stellar nucleosynthesis of  $^{26}\text{Al}$ .

Radioisotopes such as  $^{26}\text{Al}$  and  $^{60}\text{Fe}$  are long-lived relative to the recurrence time scales of the events that create these isotopes. Complications in the interpretation of the  $\gamma$ -ray observations therefore arise because the detected intensities likely consist of the superposition of the emission from nuclei produced in different events, distributed in both time and space. For example, the spatial distribution of the sources must be determined to explain the observed flux. Complications in the relevant nuclear physics behind the net production of  $^{26}\text{Al}$  arise from the presence of an isomeric state in  $^{26}\text{Al}$  at  $E_x = 228$  keV ( $t_{1/2} = 6.3$  s,  $J^\pi = 0^+$ ). (Hereafter, the ground state of  $^{26}\text{Al}$  is denoted as  $^{26}\text{gAl}$ , the isomeric state as  $^{26}\text{mAl}$ , and the general nucleus as simply  $^{26}\text{Al}$ .)  $^{26}\text{gAl}$   $\beta$  decays to the  $E_x = 1.809$  and 2.938 MeV states in  $^{26}\text{Mg}$ , leading to a

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1.809-MeV  $\gamma$  ray in 99.7% of all decays. The isomer, on the other hand, decays directly (100%) to the ground state of  $^{26}\text{Mg}$  without the emission of any  $\gamma$  ray. Hence, one must distinguish between production and destruction of both  $^{26\text{g}}\text{Al}$  and  $^{26\text{m}}\text{Al}$  in astrophysical phenomena, particularly at temperatures  $T < 0.4$  GK where thermal equilibrium between the ground and isomeric states is not assured [13–16].

Stellar winds from asymptotic giant branch (AGB) and Wolf-Rayet (WR) stars and ejection through core-collapse supernova and classical nova explosions have been suggested as mechanisms through which  $^{26}\text{Al}$  may be distributed throughout the interstellar medium [4,6,16–22]. Each of these scenarios involves different characteristic temperatures over which  $^{26}\text{Al}$  is most likely to be produced or destroyed. As a result, nuclear structure information for different nuclei, and over various excitation energies in these nuclei, is required to characterize all of the relevant thermonuclear reaction rates.

In hydrogen-burning environments, the  $^{26}\text{Al}(p,\gamma)^{27}\text{Si}$  reaction is the key pathway for the destruction of  $^{26}\text{Al}$ . The winds of AGB and WR stars are thought to eject  $^{26}\text{Al}$  produced through hydrogen burning at temperatures between roughly 30 and 100 MK. In classical novae,  $^{26}\text{Al}$  is produced only in explosions that involve an oxygen-neon white dwarf and achieve the highest temperatures, e.g.,  $T_{\text{peak}} \approx 0.2\text{--}0.4$  GK. These considerations imply the need to understand the nuclear structure of  $^{27}\text{Si}$  in the energy range between the  $^{26\text{g}}\text{Al}+p$  threshold ( $S_p = 7462.96(16)$  keV [23]) and roughly 1 MeV above this threshold to reliably evaluate the  $^{26\text{g}}\text{Al}(p,\gamma)^{27}\text{Si}$  and  $^{26\text{m}}\text{Al}(p,\gamma)^{27}\text{Si}$  rates in all of these environments. In particular, one requires the resonance energies  $E_R$  and  $(p,\gamma)$  resonance strengths for states in this energy range. Unknown resonance strengths may be estimated using indirect techniques, for example, using proton-transfer spectroscopic factors, proton- and  $\gamma$ -decay-branching ratios, and  $J^\pi$  values (see, e.g., Iliadis [24] for more details).

The  $^{26}\text{Al}(p,\gamma)^{27}\text{Si}$  reaction has been studied both directly and indirectly. Buchmann *et al.* [25] measured an excitation function using protons bombarding an  $^{26\text{g}}\text{Al}$  target and found 7 resonances within  $E_R = 270\text{--}900$  keV ( $E_x = 7.74\text{--}8.36$  MeV). They also used the thick-target method to find the strengths of these resonances. Schmalbrock *et al.* [26] used the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction to determine the energies of 58 states from  $E_x = 4.14\text{--}8.37$  MeV; 18 of these states had excitation energies greater than 7.46 MeV. These measurements were largely confirmed by Wang *et al.* [27], who studied both the  $^{27}\text{Al}(^3\text{He},t)^{27}\text{Si}$  and  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reactions. Both Schmalbrock *et al.* [26] and Wang *et al.* [27] attempted unsuccessfully to determine  $J^\pi$  values for proton-threshold states in  $^{27}\text{Si}$  through the measurement of angular distributions for the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction. Contaminant  $\alpha$  groups from ( $^3\text{He},\alpha$ ) reactions on carbon and oxygen were an issue in both studies; Wang *et al.* [27] nonetheless extracted angular distributions, but did not attempt to fit them. Vogelaar *et al.* [28] measured the  $^{26\text{g}}\text{Al}(^3\text{He},d)^{27}\text{Si}$  reaction to constrain strengths for states at  $E_x = 7.59, 7.65,$  and  $7.74$  MeV through estimates of the respective proton-transfer spectroscopic factors. Ruiz *et al.* [29], through a direct study in inverse kinematics with a high-intensity beam of  $^{26\text{g}}\text{Al}$ , measured both the energy and

strength of the key resonance for  $^{26\text{g}}\text{Al}$  destruction in classical nova explosions ( $E_R = 184$  keV,  $E_x = 7.65$  MeV). Both the resonance energy and strength, however, were in minor disagreement with the previous unpublished direct study of Vogelaar [30] (but see Sec. IV) and with the results from the transfer reaction studies of Refs. [26,27]. Deibel *et al.* [31] observed 53 states between  $E_x = 8.14$  and  $9.86$  MeV through studies of the  $^{27}\text{Al}(^3\text{He},t)^{27}\text{Si}$  and  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reactions. They also observed proton decays from excited states in  $^{27}\text{Si}$  between  $E_x = 8.14\text{--}8.98$  MeV to the ground, isomeric and second-excited states of  $^{26}\text{Al}$ , and so were able to constrain the corresponding proton-branching ratios.

Outstanding nuclear physics issues for  $^{26}\text{Al}$  destruction in AGB and WR stars and classical nova explosions included (a)  $^{26\text{g}}\text{Al}(p,\gamma)$  resonance strengths (or spectroscopic information) for states  $E_x(^{27}\text{Si}) < 7.65$  MeV; (b) the possible existence of the state at  $E_x(^{27}\text{Si}) = 7.56$  MeV (identified only in the studies of Wang *et al.* [27]); and (c) the energy of the resonance at  $E_x(^{27}\text{Si}) = 7.65$  MeV, given the  $\approx 4$  keV disagreement between the Ruiz *et al.* [29] study and the other studies [26,27,30]. Points (a) and (b) are of particular relevance for  $^{26}\text{Al}$  production in AGB and WR stars as they gave rise to uncertainties of  $\approx 4$  orders of magnitude in the  $^{26\text{g}}\text{Al}(p,\gamma)^{27}\text{Si}$  destruction rate over the temperatures involved [32], which, in turn, could affect  $^{26}\text{Al}$  production in, e.g., AGB stars by factors of  $\approx 100$  [33,34]. Point (c) is of importance to precisely quantify  $^{26}\text{Al}$  production in classical novae (expected to contribute less than 20% of the overall galactic  $^{26}\text{Al}$  abundance [22,35]). The contribution to a thermonuclear rate of a narrow, isolated resonance depends linearly on the strength of the resonance and exponentially on the resonance energy  $E_R$  through a factor  $\exp(-E_R/kT)$ , where  $T$  is the temperature of interest and  $k$  is the Boltzmann constant. An uncertainty of 4 keV in  $E_R$  leads to an uncertainty of  $\approx 20\%$  in the contribution of this resonance to the overall  $^{26\text{g}}\text{Al}(p,\gamma)^{27}\text{Si}$  rate at typical nova peak temperatures (over which this resonance dominates the reaction rate). This uncertainty is comparable to the uncertainties in measurements of the strength of this resonance [29,30]. Moreover, a reduction in the  $^{26\text{g}}\text{Al}(p,\gamma)^{27}\text{Si}$  rate by  $\approx 20\%$  led to an increase in the overall yield of  $^{26}\text{Al}$  by  $\approx 20\%$  in the nova model discussed in Ref. [29]. Finally, in addition to the above, a reliable  $^{26\text{m}}\text{Al}(p,\gamma)^{27}\text{Si}$  rate would require resonance strengths (or complete spectroscopic information) for states between  $E_x = 7.69$  MeV (i.e., the  $^{26\text{m}}\text{Al}+p$  energy threshold in  $^{27}\text{Si}$ ) and at least  $E_x = 8.14$  MeV (above which proton-branching ratios to the ground and isomeric states have been measured [31]).

Lotay *et al.* [36] addressed some of these issues through a detailed  $\gamma$ -ray spectroscopy study of  $^{27}\text{Si}$  using the fusion-evaporation reaction  $^{12}\text{C}(^{16}\text{O},n)$ .  $J^\pi$  values were assigned for levels between the ground state and  $E_x = 8.38$  MeV. No state at 7.56 MeV was observed, and the excitation energy of the 7.65-MeV state was found to be in disagreement with the value from Ref. [29]. With this new information, a  $^{26\text{g}}\text{Al}(p,\gamma)^{27}\text{Si}$  rate was recently determined with uncertainties of less than a factor of 10 below 0.1 GK and less than  $\approx 20\%$  above 0.1 GK [37]. A reliable  $^{26\text{m}}\text{Al}(p,\gamma)^{27}\text{Si}$  rate still cannot be calculated, however, due to insufficient experimental information [16].

The structure of  $^{27}\text{Si}$  within about 1 MeV of the  $^{26}\text{gAl}+p$  threshold is of clear importance in constraining the  $^{26}\text{gAl}(p,\gamma)$  and  $^{26}\text{mAl}(p,\gamma)$  rates in hydrogen-burning environments such as AGB and WR stars and classical nova explosions. Given this, we have performed a high-resolution study of the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction to independently determine the energies and  $J^\pi$  values for relevant states in  $^{27}\text{Si}$ . We also desired to test the assertion of Wang *et al.* [27] that reliable  $J^\pi$  values could not be extracted from angular distributions of the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction at  $E \approx 22$  MeV, for states above the  $^{26}\text{gAl}+p$  energy threshold in  $^{27}\text{Si}$ .

## II. EXPERIMENT

The  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction was measured at the Maier-Leibnitz-Laboratorium (MLL) in Garching, Germany, over a total period of 3 days. A 25-MeV beam of  $^3\text{He}^{2+}$  ions ( $I \approx 550$  nA) was produced with an electron-cyclotron-resonance-like ion source [38] and an MP tandem accelerator. This beam was transported to the target position of a quadrupole-dipole-dipole-dipole (Q3D) magnetic spectrograph with superior intrinsic energy resolution  $\Delta E/E \approx 2 \times 10^{-4}$  [39]. Targets were prepared at the Technische Universität München and included the following: enriched silicon ( $20 \mu\text{g}/\text{cm}^2$ , enriched to 99.84%  $^{28}\text{Si}$ ) deposited upon a foil of enriched carbon ( $7 \mu\text{g}/\text{cm}^2$ , enriched to 99.99%  $^{12}\text{C}$ ); natural silicon dioxide (self-supporting,  $25 \mu\text{g}/\text{cm}^2$ ); enriched carbon ( $10 \mu\text{g}/\text{cm}^2$  foil, enriched to 99.99%  $^{12}\text{C}$ ); and enriched magnesium ( $20 \mu\text{g}/\text{cm}^2$ , enriched to 99.92%  $^{24}\text{Mg}$ ) deposited upon a foil of enriched carbon ( $7 \mu\text{g}/\text{cm}^2$ , enriched to 99.99%  $^{12}\text{C}$ ). The carbon and silicon dioxide targets were used primarily to characterize background due to reactions on the carbon and oxygen present in the enriched silicon target, and the magnesium target was used to help calibrate the focal plane of the spectrograph. Light reaction products entered the Q3D spectrograph through a rectangular aperture (encompassing 7.0 msr), were dispersed according to their momenta, and finally, were focused onto a multiwire gas-filled proportional counter backed by a plastic scintillator [40]. Alpha particles were clearly identified through energy loss and residual energy information from the focal-plane detection system, and  $\alpha$  spectra of the focal-plane positions were then produced. Measurements were made at spectrograph angles of  $10^\circ$ ,  $15^\circ$ ,  $20^\circ$ ,  $25^\circ$ ,  $30^\circ$ ,  $35^\circ$ ,  $40^\circ$ ,  $45^\circ$ ,  $55^\circ$ , and  $65^\circ$ ; the beam current was integrated using a Faraday cup placed at  $0^\circ$  in the target chamber.

## III. DATA AND ANALYSIS

Figure 1 shows  $\alpha$  spectra measured with the enriched silicon target at spectrograph angles of  $15^\circ$  and  $20^\circ$ . Contaminant groups due to  $(^3\text{He},\alpha)$  reactions on  $^{12}\text{C}$  and  $^{16}\text{O}$  present in the target (the former primarily from the target backing) were evident, and these were unambiguously identified and characterized through both kinematic analysis at the measured angles and measurements with the enriched carbon and silicon dioxide targets. For example, contaminant groups due to  $^{16}\text{O}(^3\text{He},\alpha)$  reactions populating the 8743(6)-, 8922(2)-, and 8982.1(17)-keV states in  $^{15}\text{O}$  [41] are seen among the

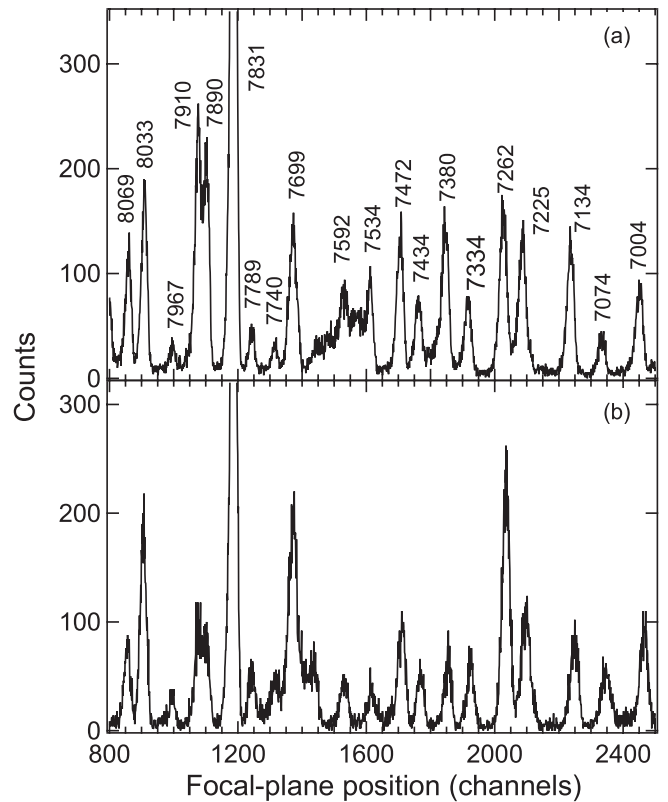


FIG. 1. Focal-plane  $\alpha$  spectra from the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction at 25 MeV,  $d\Omega = 7.0$  msr, and (a)  $\theta_{\text{lab}} = 15^\circ$  and (b)  $\theta_{\text{lab}} = 20^\circ$ . Excitation energies are labeled in keV.

7380-, 7534-, 7592-, and 7652-keV states of  $^{27}\text{Si}$  in Fig. 1(a) and among the 7534-, 7652-, 7694-, 7704-, and 7740-keV states of  $^{27}\text{Si}$  in Fig. 1(b). These spectra were analyzed using least-squares fits of multiple Gaussian or exponentially modified Gaussian functions. Consistent excitation energies were determined using each of these prescriptions. Peak widths were fixed to  $\approx 12$  keV FWHM based on fits of isolated peaks in these spectra.

At each measurement angle the focal plane was calibrated using well-resolved, known states in  $^{23}\text{Mg}$  ( $7.6 < E_x(^{23}\text{Mg}) < 8.7$  MeV and  $\Delta E_x = 1\text{--}6$  keV [42,43]) populated via the  $^{24}\text{Mg}(^3\text{He},\alpha)$  reaction with the enriched magnesium target. With this information, second-degree polynomial fits of  $\alpha$  radius of curvature  $\rho$  to focal-plane position yielded excitation energies for states in  $^{27}\text{Si}$ . Excitation energies from the present work are listed in Table I, along with uncertainties due to counting statistics, reproducibility among angles, and uncertainties in the calibration states; the slightly larger uncertainties for states with  $E_x > 7.9$  MeV arise due to the increasing reliance on calibration states with larger uncertainties. The energies from the present work are all weighted averages calculated with energies determined for at least four different angles—the exact number depends upon the precise magnetic field setting used at a particular angle (i.e., for states near the edges of the focal-plane), the presence of large contaminant peaks obscuring different states at different angles, and the requirement that a  $^{27}\text{Si}$  state lie within a region spanned entirely

TABLE I. Level structure of  $^{27}\text{Si}$  for  $E_x = 7.0\text{--}8.1$  MeV. Excitation energies are given in keV. Resonance energies from the studies of Buchmann *et al.* [25] and Ruiz *et al.* [29] have been converted to excitation energies using the  $^{26}\text{Al}+p$  energy-threshold of  $S_p = 7462.96(16)$  keV [23] in  $^{27}\text{Si}$ . One should consider a systematic uncertainty of  $\pm 2$  keV in addition to the uncertainties listed for the present work (see text).

$^{26}\text{Al}(p,\gamma)$ [25]	$^{28}\text{Si}(^3\text{He},\alpha)$ [26]	$^{27}\text{Al}(^3\text{He},t)$ [27]	$p(^{26}\text{Al},\gamma)$ [29]	$^{12}\text{C}(^{16}\text{O},n)$ [36]	$^{28}\text{Si}(^3\text{He},\alpha)$ Present
	7005(8)			7000.7(22) 9/2 <sup>+</sup>	7004(1) (9/2, 11/2) <sup>-</sup>
	7059(5)			7070.2(4) 9/2 <sup>-</sup>	7074(1)
	7080(3)				
	7134(5)			7129.0(2) 13/2 <sup>+</sup>	7134(2) (3/2, 5/2) <sup>+</sup>
	7223(4)			7222.4(2) 13/2 <sup>+</sup>	7225(2) (11/2, 13/2) <sup>+</sup>
	7239(4)			7245.4(5) 11/2 <sup>+</sup>	
	7260(4)			7252.5(2) 7/2 <sup>+</sup>	7262(2) (5/2, 7/2) <sup>-</sup>
	7276(3)				
	7324(4)			7325.4(18) 3/2 <sup>+</sup>	7334(2)
	7341(4)			7346.6(9) 7/2 <sup>-</sup>	
	7388(5)	7379(4)		7380.4(15) 5/2 <sup>+</sup>	7380(2) (3/2, 5/2) <sup>+</sup>
	7436(4)	7428(4)		7433.3(6) 9/2 <sup>+</sup>	7434(2)
		7436(4)			
	7465(5)	7470(4)		7468.8(8) (1/2, 5/2) <sup>+</sup> (7493.1(40)) (3/2 <sup>+</sup> )	7472(2) (3/2, 5/2) <sup>+</sup>
	7530(5)	7533(3)		7531.3(7) 5/2 <sup>+</sup>	7534(2) (3/2, 5/2) <sup>+</sup>
		(7557(3))			
	7596(4)	7589(3)		7590.1(9) 9/2 <sup>+</sup>	7592(2) (7/2, 9/2) <sup>+</sup>
	7654(5)	7651(3)	7647(1)	7651.9(6) 11/2 <sup>+</sup>	7652(2) (11/2, 13/2) <sup>+</sup>
		(7690(3))		7693.8(9) 5/2 <sup>+</sup>	7699(2)
	7703(3)	7702(3)		7704.3(2) 7/2 <sup>-</sup>	
7738.9(3) (7/2 -11/2) <sup>+</sup>	7742(3)	7741(3)		7739.3(4) 9/2 <sup>+</sup>	7740(2) (7/2, 9/2) <sup>+</sup>
	7796(4)	7789(3)		7794.8(19) 7/2 <sup>+</sup>	7789(1) (7/2, 9/2) <sup>+</sup>
7825(3) (7/2 -11/2) <sup>+</sup>		7832(3)		7831.5(5) 9/2 <sup>-</sup>	7831(1)
	7837(4)			7837.6(2) 5/2 <sup>+</sup>	
		7893(4)		7899.0(8) 5/2 <sup>+</sup>	7890(2) (3/2, 5/2) <sup>+</sup>
	7909(4)	7913(3)		7909.1(7) 3/2 <sup>+</sup>	7910(3) (1/2, 3/2) <sup>-</sup>
	7974(5)	7971(3)		7966.3(8) 5/2 <sup>+</sup>	7967(3) (3/2, 5/2) <sup>+</sup>
	8034(5)	8037(3)		8031.5(11) 5/2 <sup>+</sup>	8033(3) (7/2, 9/2) <sup>+</sup>
	8077(5)	8073(3)		8069.6(30) 3/2 <sup>-</sup>	8069(3) (3/2, 5/2) <sup>+</sup>



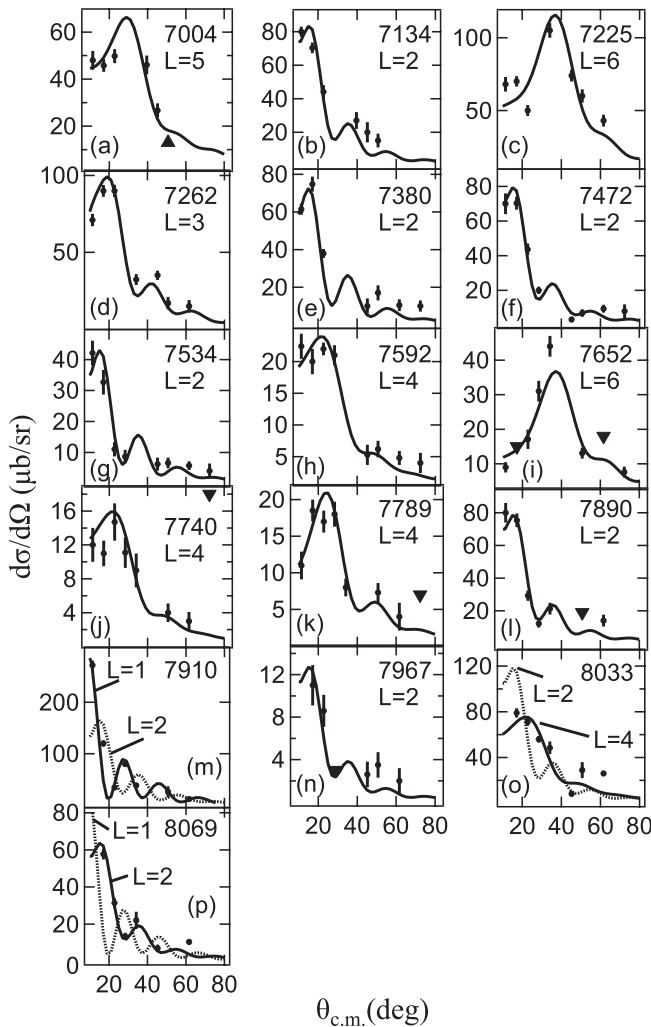


FIG. 2. Alpha angular distributions measured with the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction at 25 MeV. Curves calculated with the finite-range, coupled-reaction channels code FRESKO [45] have been fit to the data. Each panel (a–p) is labeled with the excitation energy (in keV) of the relevant state in  $^{27}\text{Si}$  and the transferred angular momentum  $L$  from the calculation that best fits the data. Panels (m), (o), and (p) also include calculations using alternative  $L$  values deduced from the spin-parity constraints of Ref. [36].

by calibration peaks. As well, we note a systematic uncertainty of  $\pm 2$  keV due to uncertainty in the thicknesses of the enriched silicon and enriched magnesium targets (each target thickness is known to roughly 10%) and uncertainty in the relative  $Q$  value of the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  and  $^{24}\text{Mg}(^3\text{He},\alpha)^{23}\text{Mg}$  reactions (this last aspect is dominated by the 0.8-keV uncertainty in the mass of  $^{23}\text{Mg}$  [23,44]).

Angular distributions measured using the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction are plotted in Fig. 2, along with direct reaction calculations using the code FRESKO [45]. Only well-resolved singlet states clearly observed over at least five angles are included in Fig. 2. Optical model parameters for the calculations were obtained using global scaling formulas [46] for the incoming  $^{28}\text{Si} + ^3\text{He}$  channel. For the outgoing channel, parameters were taken from a study of the elastic scattering

of  $\alpha$  particles on the isobar  $^{27}\text{Al}$  at the same incident energy [47]. The shapes of the corresponding angular distribution calculations were found to be insensitive to modest variations of these optical model parameters. A further improvement was made through the consideration of inelastic excitations to the  $2_1^+$  state in  $^{28}\text{Si}$ . This improves the agreement between the calculations and the experimental data at large angles and generally reduces the amplitudes of the oscillations in the differential cross sections, but does not influence the extracted angular momentum transfers  $L$ . As in all one-particle transfer reactions, the shape of the angular distribution is insensitive to the spin  $J$  of the final state, and so only the angular momentum transfer  $L$  can be determined. This allows one to determine the parity of states populated in the reaction, making our results completely complementary to those from the  $\gamma$ -ray spectroscopy measurement of Ref. [36]. In that measurement,  $\gamma$ -ray branching ratios and angular distributions were used to determine the  $\Delta I$  of  $\gamma$ -ray transitions, which were then used to assign spins to excited states of  $^{27}\text{Si}$ ; the corresponding parities of the states were inferred largely (but not exclusively) through comparisons with states in the mirror nucleus  $^{27}\text{Al}$ .

#### IV. DISCUSSION

In Table I we compare results from the present study to previous studies of the structure of  $^{27}\text{Si}$  between  $E_x = 7.0$ – $8.1$  MeV. We include in Table I energies for peaks observed in the present work that may coincide with previously identified doublets. For example, the peak at 7.074 MeV in the present work was observed with a somewhat larger width than other, isolated states and falls between the 7.059- and 7.080-MeV states determined in the study of Schmalbrock *et al.* [26]. Similar considerations apply for the 7.334-, 7.434-, and 7.699-MeV peaks observed in the present work; note, however that the 7.074- and 7.434-MeV peaks coincide with single states observed in Ref. [36]. Attempts to analyze these peaks as unresolved doublets did not produce significant improvements over single-level fits. As well, no appreciable changes in the shapes of these peaks as a function of angle were observed.

Energies determined in the present study generally agree well with values from previous measurements. The observation of states at 7.25 MeV [36] and 7.26 MeV (present work and Ref. [26]) indicate the existence of a previously unidentified doublet. We do not observe a state at 7.49 MeV nor at 7.56 MeV (tentatively identified in Refs. [27,36], respectively). For the state at 7.65 MeV, our energy is in agreement with the values from the previous transfer-reaction and  $\gamma$ -ray spectroscopy measurements [26,27,36]. The discrepancy between this energy and that from the radiative proton-capture measurement of Ref. [29] could possibly be explained by the excitation of different members of a closely spaced doublet in  $^{27}\text{Si}$  by the different experiments. Support for this hypothesis comes from the different  $\gamma$ -decay schemes reported for this state by Lotay *et al.* [36] and in the unpublished proton-capture measurement of Vogelaar [30] (see Ref. [48] for more details). In addition, the resonance energy determined in Ref. [30] ( $E_p = 195.6(11)$  keV,  $E_x = 7651.3(11)$  keV) may need to be reduced by a few keV due to an adjustment in the

energy of a calibration state; this would improve the accord between the energies determined from the two proton-capture studies [29,30]. Measurements are in progress to explore this issue further [49]. A previously unresolved doublet of states at 7.832 and 7.838 MeV was observed for the first time by Lotay *et al.* [36]; we could not resolve these two states, but we do note that our energy for this doublet (7.831 MeV) indicates the weak relative population of the higher-energy member at all angles. Finally, the presence of a previously unknown doublet seems required by the observation of a state at 7.890(2) MeV (in the present study) and a state at 7.8990(8) MeV (in the study of Lotay *et al.* [36]).

In Table I we have listed spin-parity constraints from the present work that arise directly from our measured angular distributions—we have not appealed to any tentative mirror assignments (e.g., those suggested by Lotay *et al.* [36]). Except for the assignments to the states at 7.00, 7.13, 7.91, 8.03, and 8.07 MeV, all of our constraints are compatible with the  $J^\pi$  values assigned in Ref. [36]. Calculated angular distributions for  $L$  values corresponding to the best-fit cases as well as those values deduced from Ref. [36] are plotted in Fig. 2 for the three states above the  $^{26}\text{Al}+p$  threshold; the experimental data at low angles in particular favor our  $J^\pi$  constraints. The disagreement in assigned parity for the 7.00- and 8.07-MeV states may arise from incorrect mirror assignments in Ref. [36].

Measured angular distributions from the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction have been published previously for the 7.47-, 7.53-, 7.59-, and 7.65-MeV states by Wang *et al.* [27]. Although a similar beam energy was employed in that study, the angular range was limited to  $\theta_{\text{c.m.}}$  less than  $\approx 35^\circ$  for these four states. The authors expressed the lack of easily discernible direct reaction characteristics for their angular distributions and thus did not extract spin and parity information. In contrast, our measured angular distributions show characteristic features mainly because the angular range has been significantly extended (up to  $\theta_{\text{c.m.}} = 72^\circ$  for these states). The relative cross sections of the present study and those of Ref. [27] agree quite well, although absolute values differ by a factor of  $\approx 3$  for common angles. The source of this discrepancy is not understood—the slight increase in beam energy (22.4 MeV in Wang *et al.* [27] versus 25 MeV in the present study) does not account for such differences. The general good agreement between our  $J^\pi$  constraints and those from the  $\gamma$ -ray study of Lotay *et al.* [36] indicate that treating the neutron-removal  $^{28}\text{Si}(^3\text{He},\alpha)$  process as a direct reaction at these energies is reasonable.

Assignments between analog states in  $^{27}\text{Si}$  and  $^{27}\text{Al}$  have been extensively discussed in Lotay *et al.* [36] and were indeed exploited by necessity to extract many of their adopted parities for states in  $^{27}\text{Si}$ . To facilitate the comparison between observed states in  $^{27}\text{Si}$  and shell-model calculations, we have determined experimental neutron-removal spectroscopic factors  $S$  for the population of the  $^{27}\text{Si}$  states shown in Fig. 2, where  $S$  is the ratio between the experimental and calculated differential cross sections for a state. (Note that these neutron-removal spectroscopic factors from the  $^{28}\text{Si}(^3\text{He},\alpha)$  reaction are not of interest for calculations of the thermonuclear  $^{26}\text{Al}(p,\gamma)^{27}\text{Si}$  rate. For such applications we would require proton-transfer spectroscopic factors, which

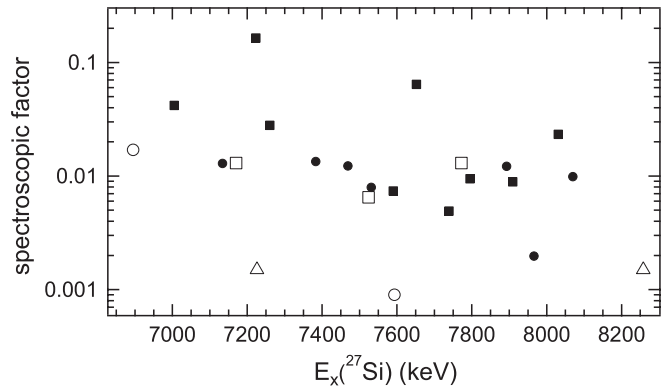


FIG. 3. Neutron spectroscopic factors for states in  $^{27}\text{Si}$  populated through the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction. Experimental values for low-spin states ( $J^\pi = \{1/2^+, 3/2^+, 5/2^+\}$ , solid circles) and higher-spin states (solid squares) are plotted with shell-model calculations for low-spin states ( $J^\pi = 1/2^+$ , open triangles;  $J^\pi = 3/2^+$ , open squares;  $J^\pi = 5/2^+$ , open circles).

could be determined through measurement of, for example, the  $^{26}\text{Al}(^3\text{He},d)^{27}\text{Si}$  reaction—see Ref. [28].) Theoretical energy levels and neutron spectroscopic factors were calculated using the code OXBASH [50]. Within the model space of the USDA interaction [51] only states with  $J^\pi = \{1/2^+, 3/2^+, 5/2^+\}$  are expected to be populated in the one-neutron removal reaction. In Fig. 3 we compare the experimental spectroscopic factors for these low-spin states to the calculated values; the experimental values are also tabulated in Table II. Over  $E_x(^{27}\text{Si}) = 6.9\text{--}8.3$  MeV, the calculated spectroscopic factors for these levels vary between about 0.001 and 0.01, as may be expected for such high-excitation energies. Given the discussion above on the disagreement between the absolute cross sections of the present measurement and those of Wang

TABLE II. Neutron spectroscopic factors  $S$  extracted from the  $^{28}\text{Si}(^3\text{He},\alpha)^{27}\text{Si}$  reaction, assuming the transferred angular momentum values  $L$  from the best-fit curves of Fig. 2.

$E_x(^{27}\text{Si})$ (keV)	$L$	$S$
7004	5	0.042
7134	2	0.013
7225	6	0.16
7262	3	0.028
7380	2	0.013
7472	2	0.012
7534	2	0.0079
7592	4	0.0074
7652	6	0.064
7740	4	0.0049
7789	4	0.0095
7890	2	0.012
7910	1	0.0089
7967	2	0.0020
8033	4	0.023
8069	2	0.0098

*et al.* [27], one should consider a systematic uncertainty of a factor of  $\approx 3$  in the experimental values of  $S$ . Moreover, for states without a definite spin-parity assignment, or where our  $J^\pi$  constraints disagree with the assignments of Lotay *et al.* [36] (see Table I), we have adopted the calculations with the higher spins when extracting the experimental spectroscopic factors. This affects the experimental value of  $S$  by, for example, 30% when comparing  $S$  values determined with  $J^\pi = 3/2^+$  versus  $J^\pi = 5/2^+$  for the state at  $E_x = 7134$  keV. From Fig. 3, we see that although the general agreement between the magnitudes of the experimental and calculated spectroscopic factors is acceptable, the direct assignment of experimental states to shell-model states is not straightforward. This is due to the high density of observed states as well as the fact that fewer low-spin states are predicted in this energy region than have been observed (see Table I—only states that were well-resolved in the present set of measurements are included in Fig. 3). We note, however, that significant progress has been made in this regard by Lotay *et al.* [36] through concurrent  $\gamma$ -ray spectroscopy studies of  $^{27}\text{Al}$  and  $^{27}\text{Si}$ .

The structure of  $^{27}\text{Si}$  above the  $^{26}\text{gAl}+p$  threshold (7463 keV) and the  $^{26}\text{mAl}+p$  threshold (7691 keV) is required to calculate thermonuclear rates for proton capture on the ground and isomeric states of  $^{26}\text{Al}$ . We do not observe a state at 7.56 MeV, and the energy we determine for a state at 7.65 MeV is consistent with the measurements of Refs. [26,27,36] (and inconsistent with the energy from the study of Ruiz *et al.* [29]). Comparison between the constraints of the present study and Ref. [36] indicate that the 7.47-MeV state has  $J^\pi = 5/2^+$ . Given these considerations, as well as our agreement with the  $J^\pi$  values of Ref. [36] for the 7.53- and 7.59-MeV states, we propose no changes to the thermonuclear  $^{26}\text{gAl}(p,\gamma)^{27}\text{Si}$  rate determined in the recent evaluation of Iliadis *et al.* [37] over temperatures relevant to hydrogen burning in AGB and WR stars and classical nova explosions. It is still not possible to calculate a reliable experimental  $^{26}\text{mAl}(p,\gamma)^{27}\text{Si}$  rate [16] because of the lack of resonance strength (or proton spectroscopic factor) measurements for states immediately above the  $^{26}\text{mAl}+p$  threshold. The spin-parities of these states as determined in the present work and that of Lotay *et al.* [36] therefore represent critical information needed both for rate estimates and to guide future experimental investigations dedicated to improving the  $^{26}\text{mAl}(p,\gamma)$  rate. Indeed, Lotay *et al.* [36] express the importance of the 8.07 MeV state given their  $J^\pi$  assignment of  $3/2^-$  (corresponding to a  $\ell = 1$  proton-capture resonance). Our data, however, are consistent with a different assignment for both the 8.07-MeV state (i.e., corresponding to a  $\ell = 2$  resonance) and the 7.91-MeV state (i.e., corresponding to a  $\ell = 1$  resonance). This would shift the importance of the  $\ell = 1$  resonance down to lower temperatures, where it could dominate the reaction rate [36]. Without more nuclear structure information however, it is impossible at the moment to precisely quantify the contributions of individual resonances to the  $^{26}\text{mAl}(p,\gamma)$  rate at temperatures involved in AGB and WR stars and classical nova explosions. The existence of additional states beyond those in Table I should also be investigated.

## V. CONCLUSIONS

We have measured energies and angular distributions for states in  $^{27}\text{Si}$  over  $E_x = 7.0\text{--}8.1$  MeV through a study of the  $^{28}\text{Si}(^3\text{He},\alpha)$  reaction. Constraints on  $J^\pi$  values for 16 states above the  $^{26}\text{gAl}+p$  threshold have been determined for the first time using a transfer reaction; these constraints (and all energies) are generally in good agreement with the results from a recent  $\gamma$ -ray spectroscopy study [36]. A direct reaction mechanism adequately describes our experimental angular distributions, in contrast with indications from a previous measurement using the same reaction and similar beam energy [27].

In the absence of measured resonance strengths for states immediately above the  $^{26}\text{gAl}+p$  and  $^{26}\text{mAl}+p$  energy thresholds, the  $J^\pi$  values of these states represent critical nuclear structure information needed to estimate the corresponding thermonuclear proton-capture reaction rates. The present work confirms the assumptions made in the calculation of Ref. [37] for the  $^{26}\text{gAl}(p,\gamma)^{27}\text{Si}$  rate. To further reduce the uncertainties in this rate, especially over temperatures encountered in AGB and WR stars and classical nova explosions, the  $^{26}\text{Al}(^3\text{He},d)^{27}\text{Si}$  reaction should be studied to extract proton spectroscopic factors for the 7.53- and 7.59-MeV states. A vital improvement over the previous study of this reaction [28] would involve the minimization of any  $^{27}\text{Al}$  contamination in the target [52]. Measurements to better constrain the  $^{26}\text{mAl}(p,\gamma)^{27}\text{Si}$  rate could involve a study similar to that of Ref. [31], optimized to allow the detection of protons from the decay of states  $E_x(^{27}\text{Si}) < 8.1$  MeV. The reaction could also be measured directly in inverse kinematics [53]; prior identification of  $\ell = 0$  and  $\ell = 1$  resonances would help to guide this challenging study. For this reason, the  $J^\pi$  values of states above the  $^{26}\text{mAl}+p$  threshold, particularly those at 7.91 and 8.07 MeV, should be confirmed.

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