# Discovery of low-lying E1 and M1 strengths in $^{232}$ Th

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Properties of low-energy dipole states in <sup>232</sup>Th have been investigated with the nuclear resonance fluorescence technique. The present work used monoenergetic  $\gamma$ -ray beams at energies of 2–4 MeV from the high-intensity  $\gamma$ -ray source at Triangle Universities Nuclear Laboratory. Over 40 transitions corresponding to deexcitation to the ground state and first excited state were observed for the first time. Excitation energies, integrated cross sections, decay widths, branching ratios, and transition strengths for those states in <sup>232</sup>Th were determined and compared with quasiparticle random-phase-approximation calculations. A large number of *E*1 transitions were observed for the first time in actinide nuclei with summed strength of  $3.28(69) \times 10^{-3} e^2$  fm<sup>2</sup>. The observed summed *M*1 strength of  $4.26(63)\mu_N^2$  is in good agreement with the other actinides and with the systematics of the scissors mode in deformed rare-earth nuclei.

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## I. INTRODUCTION

Investigation of low-lying electric and magnetic dipole excitations in heavy-mass nuclei is of great importance to nuclear structure physics. There have been numerous experimental and theoretical efforts to study the orbital magnetic dipole response over a wide mass region [1-4]. Following the theoretical prediction [5] of low-lying collective M1excitations known as the scissors mode in which the protons and neutrons in the nucleus undergo small-angle vibrations in a scissors-like motion with respect to each other, it has been found experimentally in deformed nuclei using electronand photon-scattering experiments [6,7]. However, most of the investigations of M1 excitations have focused on light and on deformed rare-earth nuclei [4,8] with limited experimental information on the actinides. Even less is known about E1strength below the giant dipole resonance in the actinides. Unavailability of the polarized  $\gamma$ -ray beams until recently made unambiguous identification of E1 strength very difficult.

The study of the scissors mode in the actinides is important because this region involves neutron-rich nuclei with large deformations. Previous measurements [9,10] only accounted for the scissors mode up to energies of 2.5 MeV for  $^{232}$ Th and  $^{238}$ U and 3.2 MeV for  $^{236}$ U. Observed *M*1 excitations were concentrated in the energy region of 2 to 2.5 MeV with strengths comparable to those in mid-shell rare-earth nuclei [9]. Fragmentation of this strength in rare-earth nuclei is known to spread over an energy interval of 2.4–3.7 MeV with a mean energy of 3 MeV [8].

Theoretical calculations using quasiparticle random-phase approximations (QRPA) predict the mean excitation energies,  $\bar{E}_x$ , as well as the summed B(M1) and B(E1) values in <sup>232</sup>Th, <sup>236</sup>U, and <sup>238</sup>U [11,12]. Consequently, it is desirable to obtain more experimental data on the distribution of the M1 and E1strengths in actinides. It is expected that the M1 strength will gradually decrease with increasing excitation energy and the E1 strength will increase. However,  $\gamma$  spectroscopy of the <sup>232</sup>Th nucleus above 2.3 MeV is not known.

Nuclear resonance fluorescence (NRF) is an effective spectroscopic method to investigate collective *M*1 and *E*1 excitations in nuclei [13]. In this technique, interactions of a high-energy photon with a nucleus produce an excited state, which subsequently decays to lower-lying levels by emitting  $\gamma$  ray. This paper describes NRF measurements on a <sup>232</sup>Th target performed using nearly monoenergetic and 100% linearly polarized  $\gamma$ -ray beams.

## **II. EXPERIMENT**

The experiment was carried out at the High-Intensity  $\gamma$ -ray Source (HI $\gamma$ S) facility at the Triangle Universities Nuclear Laboratory (TUNL). Energetic photon beams at HI $\gamma$ S are created by Compton backscattering of a high-intensity free-electron laser (FEL) beam with an intense electron bunch. Comprehensive information about the operation and experimental capabilities of the facility is available in Ref. [14].

The present search for dipole excitations in <sup>232</sup>Th was performed at 10 incident  $\gamma$ -ray beam energies between 2 and 4 MeV with average energy spread of FWHM = 5%. No data were taken at a beam energy between 2.4 and 2.7 MeV due to the presence of a very strong background line at  $E_{\gamma}$  = 2.614 MeV. The energy distribution of the incident photons was measured using a large-volume HPGe detector positioned

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FIG. 1. Schematic diagram of the experimental layout showing two HPGe detectors at  $90^{\circ}$  and one at a backward angle of  $140^{\circ}$  in the horizontal plane. The other two HPGe detectors in the vertical plane are not shown. The flux monitor at  $0^{\circ}$  (8.3°) is indicated as a dashed (solid) rectangle. The figure is not drawn to scale.

into the beam. The photon flux was monitored by the same detector positioned at an angle of  $8.3^{\circ}$  relative to the beam axis. This detector measured Compton scattering of the  $\gamma$ -ray beam from a 1.1-mm-thick copper plate positioned upstream perpendicular to the beam axis 167 cm away (see Fig. 1). The absolute flux was determined using the Klein-Nishina formula [15] from the spectrum of the Compton-scattered photons, corrected for the detector response with error no greater than 7%. The Compton-scattering technique was verified against known resonance strength in <sup>11</sup>B [16].

The photon beams passed through a 30.5-cm-long lead collimator with a cylindrical hole of 2.22 cm in diameter, located at about 52.5 m from the collision point of the electrons with the FEL photons. The collimator ensures that the beam, illuminating a 0.1-cm-thick  $^{232}$ Th foil, was smaller than the surface area of the target, inclined at 61.4° relative to the incident beam. The target was enriched to 99.9%.

A schematic drawing of the experimental setup is shown in Fig. 1. The NRF  $\gamma$  rays from the target were measured with a HPGe detector array positioned about 4.8 m downstream from the collimator. The array consists of four HPGe detectors with 60% efficiency relative to a 7.62  $\times$  7.62 cm NaI scintillation detector. These detectors were positioned 10 cm away from the center of the target and  $90^{\circ}$  relative to the beam. Two of these detectors were located in the horizontal plane (called horizontal detectors) and the other two in the vertical plane (called vertical detectors). An additional HPGe detector was placed in the horizontal plane at a backward angle of 140°. This detector configuration allows for unambiguous determination of multipolarities of observed  $\gamma$ -ray transitions. The uncertainty of the detector geometry was estimated to be 4%. Part of the data was taken without one of the horizontal detectors. The detectors had passive shielding and absorbers composed of Pb and Cu. This helped to reduce the contributions from the low-energy background.

The energy calibrations came from the known decay lines of <sup>232</sup>Th and a radioactive <sup>60</sup>Co source. The detector efficiencies  $\epsilon(E_{\gamma})$  were obtained by combination of calibrated radioactive <sup>60</sup>Co and <sup>56</sup>Co source measurements with error no greater than 4%. GEANT4 simulations were used to extrapolate  $\epsilon(E_{\gamma})$  to energies above 3.6 MeV. The effects of atomic absorption of  $\gamma$  rays in the target were also accounted for in the simulations.

The signals from the detectors were processed by individual multichannel analyzers with 14-bit analog-to-digital converters, allowing the spectra to be binned to 0.27 keV/channel. The dead time of the the acquisition system was estimated from comparison of the 1.33-MeV peak area of a  $^{60}$ Co source located near the HPGe array, with and without the beam.

#### **III. ANALYSIS AND CALCULATION**

The integrated NRF cross section  $I_s$  at deexcitation energy  $E_{\gamma}$  is given by

$$I_s = \frac{2J_x + 1}{2J_0 + 1} \left(\frac{\pi\hbar c}{E_\gamma}\right)^2 \Gamma_0 \frac{\Gamma_f}{\Gamma},\tag{1}$$

where  $J_0$  and  $J_x$  are the spins of the ground and the excited states, respectively,  $\Gamma_f$  is the decay width to the final state,  $\Gamma_0$  and  $\Gamma$  are the ground-state decay width and total width, respectively, and  $\Gamma_f / \Gamma$  is the branching ratio. In the present measurement, only deexcitations to the ground state and the first excited state of 49 keV with  $J^{\pi} = 2^+$  have been observed. Consequently, the branching ratio becomes  $\Gamma_1 / \Gamma$  and  $\Gamma = \Gamma_0$  $+ \Gamma_1$ , where  $\Gamma_1$  is the decay width to the first excited state. From the experimental observables,  $I_s$  can be deduced from

$$I_s = \frac{N}{n_t \epsilon(E_\gamma) W(\theta, \phi) \Phi},$$
(2)

where *N* is the number of counts in the peak,  $n_t$  is the number of target nuclei per unit area, and  $\Phi$  is the number of incident  $\gamma$  rays. The factor  $W(\theta, \phi)$  describes the angular distribution, where  $\theta$  is the polar angle of the outgoing radiation with respect to the linearly polarized beam and  $\phi$  is the azimuthal angle measured from the polarization plane.

In the NRF technique, a photon beam incident on a nucleus selectively populates dipole states with the highest probability. The measurement of the angular distribution of deexcitation photons  $\gamma_2$  with respect to the incoming linearly polarized photon beam  $\gamma_1$  via the sequence  $J_0 \xrightarrow{\gamma_1} J_x \xrightarrow{\gamma_2} J_0$  allows a spin assignment of the excited state in the even-even nuclei. The angular correlations calculated for the most probable spin sequences relevant to the present work are presented in Table I. The use of linearly polarized photons makes it possible to determine the parity assignment of the excited states from the measured azimuthal asymmetry. The asymmetry has maximal values of -1 and +1 for E1 and M1 transitions, respectively (for a pointlike detector).

TABLE I. Angular correlations in the detector array.

		Horizontal	Vertical	Backward
<i>M</i> 1	$0^+ \stackrel{\gamma_1}{\rightarrow} 1^+ \stackrel{\gamma_2}{\rightarrow} 0^+$	1.45	0.08	1.5
	$0^+ \stackrel{\gamma_1}{\rightarrow} 1^+ \stackrel{\gamma_2}{\rightarrow} 2^+$	1.1	0.9	1.05
E1	$0^+ \stackrel{\gamma_1}{\rightarrow} 1^- \stackrel{\gamma_2}{\rightarrow} 0^+$	0.09	1.45	0.88
	$0^+ \stackrel{\gamma_1}{\rightarrow} 1^- \stackrel{\gamma_2}{\rightarrow} 2^+$	0.9	1.1	0.96
<i>E</i> 2	$0^+ \stackrel{\gamma_1}{\rightarrow} 2^+ \stackrel{\gamma_2}{\rightarrow} 0^+$	2.5	0	1.47
	$0^+ \stackrel{\gamma_1}{\rightarrow} 2^- \stackrel{\gamma_2}{\rightarrow} 0^+$	0	2.5	0.08

For even-even nuclei, the reduced transition probabilities are related to the measured  $\Gamma_0$  by

$$B(E1) = 2.87 \times 10^{-3} \frac{\Gamma_0}{E_{\gamma}^3} [e^2 \,\mathrm{fm}^2]$$
(3)

and

$$B(M1) = 0.26 \frac{\Gamma_0}{E_{\gamma}^3} [\mu_N^2],$$
 (4)

where  $E_{\gamma}$  is in MeV and  $\Gamma_0$  is in meV.

In the deexcitation of most of the states observed in this work, branching to the first excited level  $(J^{\pi} = 2^+)$  was identified. The branching ratio is given by

$$R_{\rm exp} = \frac{B(J = 1^{\pm} \to 2^{+})}{B(J = 1^{\pm} \to 0^{+})} = \frac{\Gamma_1}{\Gamma_0} \frac{E_{\gamma 0}^3}{E_{\gamma 2}^3},$$
 (5)

where  $E_{\gamma_0}$  and  $E_{\gamma_2}$  are the transition energies to the ground state and to the 2<sup>+</sup> state, respectively.

## IV. RESULTS AND DISCUSSION

The spectra collected at a beam energy of 2.9 MeV are shown in Fig. 2, revealing the M1 transitions observed at this energy. The spectrum of the observed  $\gamma$  rays with the two vertical and horizontal detectors added together are shown in the upper and middle panels, respectively, while the third spectrum in this figure shows the spectrum of  $\gamma$  rays observed in the detector located at a backward angle of 140°. Similar spectra collected at a beam energy of 3.6 MeV are shown in Fig. 3, revealing the E1 transitions observed at this energy. The spectra of the observed  $\gamma$  rays with one horizontal and an average of two vertical detectors are shown in the upper and bottom panels, respectively. The transitions appearing in the horizontal (vertical) but not in the vertical (horizontal) detectors correspond to pure M1 (E1) excitations.

In the spectra shown in Fig. 2, the peak at 2885.8 keV is expected to be of equal intensity in all the detectors after correcting for efficiency, if it is truly the branching of the 2935.6-keV state. However, this was not what was observed; rather the peak was more intense in the horizontal detectors than in the vertical ones. A M1 ground-state transition coinciding with the branching transition exists, which gives more intensity in the horizontal detectors. The intensity of this M1 transition was obtained by subtracting the intensity of the branching in the vertical detectors. The data were



FIG. 2. The spectra from the  ${}^{232}\text{Th}(\vec{\gamma}, \gamma')$  reaction at photon energy of 2.9 MeV in the two vertical detectors (a), the two horizontal detectors (b), and the backward angle detector (c). The line in (a) shows the energy distribution of the photon flux,  $\Phi$ , in arbitrary units. The brackets in (b) connect the ground-state transitions from the  $J^{\pi} = 1^+$  levels with their corresponding transitions to the  $2^+$ state, separated by 49 keV, while the single arrows are ground-state transitions without detectable branching to the  $2^+$  state. The groundstate transition at 2885.8 keV coincides with the branching from the 2935.6-keV level. The same is true for the ground-state transition at 2835.7 keV and the branching transition from the 2885.8-keV state.

analyzed in this fashion in order to set an upper limit on the branching ratio for the 2935.6-keV state. The same procedure was adopted in extracting the intensity of the M1 ground state at  $E_{\gamma} = 2835.7$  keV, which coincides with the branching of the 2885.8-keV state.

A total of 20 states were identified which decay to the ground state as well as to the  $2^+$  state. The branching transitions to the  $2^+$  state were identified from the 49-keV energy differences of the observed peaks. Five levels were observed without detectable branching to the  $2^+$  state. However, an upper limit on the branching ratio has been determined for each of these five levels. The level energies deduced for all the states, the integrated cross sections, the branching ratios, the



FIG. 3. The spectra from the <sup>232</sup>Th( $\vec{\gamma}, \gamma'$ ) reaction at photon energy of 3.6 MeV in the horizontal (a) and vertical (b) detectors. The line in (a) shows the energy distribution of the photon flux,  $\Phi$ , in arbitrary units. The brackets in (b) connect the ground-state transitions from the  $J^{\pi} = 1^{-}$  levels with their corresponding transitions to the 2<sup>+</sup> state, separated by 49 keV. The peak at 3475 keV is a background line due to the activity in the target.

decay widths to the ground state, and the strengths determined for all the transitions are presented in Table II. Most of the observed transitions reported in Table II were above the  $3\sigma$ detection limit *P* defined as [17]

$$P = 3.3\sqrt{2S},\tag{6}$$

where *S* is the integral over the background with length of  $3\sigma$ , and  $\sigma$  is the dispersion of a Gaussian fit of the peaks observed at the same energy. The transitions observed with a  $2\sigma$  detection limit are also included in Table II. The detection limits were converted to the minimal detectable  $I_s$  using Eq. (2). The area *S* is calculated from the background spectrum using the dependence of FWHM on the  $\gamma$ -ray energy obtained from the calibrated radioactive source measurements. As an example, a comparison of the minimal detectable  $I_s$  at an incident beam energy of 2.9 MeV and the measured integrated cross-sections is shown in Fig. 4.

In Fig. 5, the strength distributions of the M1 and E1 excitations observed in this work are presented along with previous experimental data from Heil *et al.* [9].The errors on the M1and E1 strengths reported in Table II and Fig. 5 are statistical only. The sources of systematic errors in the observed strength are listed in Table III. The overall systematic error of 9% was

TABLE II. Excited states observed in the NRF experiment on  $^{232}$ Th. Except where indicated, the detection limit of  $3\sigma$  confidence level was used.

	$E_x$	$I_s$	R <sub>exp</sub>	$\Gamma_0^2/\Gamma$	<i>B</i> ( <i>M</i> 1)		
	(keV)	(eV b)	Ĩ	(meV)	$(\mu_N^2)$		
1	2043.7(3) <sup>a</sup>	46.3(45)	0.62(9)	16.8(16)	1.34(13)		
2	2249.5(5) <sup>a,b</sup>	25.5(28)	0.48(8)	11.2(12)	0.79(9)		
3	2296.3(6) <sup>a</sup>	19.0(18)	0.89(12)	8.7(8)	0.39(4)		
4	2795.2(4)	4.4(8)	0.71(21)	3.0(5)	0.08(2)		
5	2835.0(3)	6.2(9)	0.78(17)	4.3(6)	0.15(2)		
6	2865.5(7)	3.4(5)	< 0.19(5)	2.4(4)	0.17(3)		
7	2885.8(4)	3.1(7)	< 0.26(5)	2.2(5)	0.12(3)		
8	2924.6(5)	3.5(9)	< 0.11(3)	2.6(6)	0.27(7)		
9	2935.6(3)	4.7(11)	0.44(9)	3.5(8)	0.12(3)		
10	2996.3(9) <sup>b</sup>	2.3(6)	1.37(50)	1.8(5)	0.03(1)		
11	3014.4(7)	3.0(7)	< 0.17(6)	2.4(5)	0.16(4)		
13	3115.1(5)	7.7(15)	< 0.10(3)	6.5(13)	0.61(12)		
14	3287.1(6)	1.9(4)	0.80(24)	1.8(3)	0.03(1)		
	$E_x$	$I_s$	Rexp	$\Gamma_0^2/\Gamma$	B(E1)		
	(keV)	(eV b)		(meV)	$(10^{-3} e^2 \mathrm{fm}^2)$		
1	3060.4(7)	2.1(4)	0.73(20)	1.7(3)	0.40(7)		
2	3395.8(8) <sup>b</sup>	0.9(2)	0.96(34)	0.9(2)	0.13(3)		
3	3607.9(9)	2.2(6)	0.74(18)	2.5(7)	0.36(10)		
4	3626.3(3)	1.9(3)	1.07(23)	2.1(4)	0.25(4)		
5	3639.1(6)	1.1(2)	1.29(32)	1.3(2)	0.14(3)		
6	3731.5(8)	2.0(4)	0.61(16)	2.4(4)	0.34(6)		
7	3742.6(2)	1.6(3)	0.75(23)	2.0(4)	0.26(5)		
8	3752.4(7) <sup>b</sup>	1.3(3)	1.05(36)	1.6(4)	0.17(4)		
9	3820.7(2)	1.5(3)	0.40(14)	1.8(3)	0.33(6)		
10	3920.8(6)	1.6(3)	0.47(13)	2.1(3)	0.32(5)		
11	3935.8(8)	1.1(2)	0.74(23)	1.4(3)	0.16(3)		
12	4002.2(6) <sup>b</sup>	3.0(8)	0.76(32)	4.2(11)	0.44(12)		

<sup>a</sup>Previously observed by Heil et al. [9].

<sup>b</sup> $2\sigma$  confidence limit.

obtained by adding in quadrature all contributing errors. The systematic error on the energy is estimated to be 0.5 keV. For the previously known dipole excitations below 2.5 MeV, the *M*1 strengths of 1.34(13), 0.79(9), and 0.39(4)  $\mu_N^2$  were determined for the states observed at  $E_x = 2.043$ , 2.249, and



FIG. 4. Detection limit *P* normalized to cross section  $I_s$  as a function of  $\gamma$ -ray energy at a nominal beam energy of 2.90 MeV. For comparison, experimentally determined  $I_s$  values are shown.



FIG. 5. Comparison of experimental and calculated B(M1) (upper panel) and B(E1) (lower panel) in <sup>232</sup>Th. The solid line in both panels represents QRPA calculated values [12]. The calculated E1 transition at 2.1 MeV has been scaled down by a factor of 3.

2.296 MeV, respectively. These values agree well with M1 strengths of 1.48(9), 0.56(7), and 0.31(6)  $\mu_N^2$ , respectively, reported in Ref. [9]. This comparison also serves as a test to the overall procedure in our data analysis. All the states above 2.5 MeV listed in Table II were newly observed. No *E*2 transitions were observed within the  $2\sigma$  detection limit.

Theoretical calculations of low-lying electric  $1^-$  and magnetic  $1^+$  dipole states in  $^{232}$ Th, within the QRPA approach [12] are shown as solid lines in Fig. 5. This QRPA calculation provides a simultaneous description of  $1^+$  and  $1^-$  states after the restoration of rotational, translational, and Galilean invariance by separable forces. It was used successfully in the past to describe dipole excitations in rare-earth nuclei [3] and permitted a direct comparison with NRF data.

The concentration of M1 dipole states clustered around 2.8 MeV consists of most of the newly observed M1 excitations, each with relatively small strength. A calculation of the orbit-to-spin ratio for actinides using QRPA with a deformed Woods-Saxon potential and separable residual interactions was performed by Nojarov *et al.* [11]. In this energy region, the calculated orbit-to-spin ratio for actinides shows that the

TABLE III. Systematic error budget for the observed strengths.

Sources of error	Error value (%)
Detector array efficiency	3
Detector geometry	4
Target thickness	3
Beam flux	7
Total uncertainty	9

 $1^+$  excitations have a large orbital contribution to the M1 transition matrix element. For this reason, we are assuming a scissors mode for all the newly observed M1 transitions. The M1 strength gradually decreases with increasing excitation energy as expected.

The systematics of the variation of observed summed B(M1) strength with deformation was investigated for eveneven rare-earth nuclei in Ref. [1]. The quantity

$$\xi = \sum B(M1) \left(\mu_N^2\right) A^{2/3} Z^{-2},\tag{7}$$

was found to depend linearly on the square of the deformation  $\delta$  as

$$\xi \approx 0.27\delta^2. \tag{8}$$

For <sup>232</sup>Th, using  $\delta = 0.216$ , Eq. (8) gives  $\xi = 0.013$ , which is close to the experimentally determined  $\xi = 0.02(3)$  using Eq. (7).

The distributions of M1 and E1 strengths calculated in Ref. [12] seem to follow a similar pattern with substantial E1 strength predicted between 3.3 and 3.8 MeV. The summed M1 transition strength in <sup>232</sup>Th calculated from the present data is 4.26(63)  $\mu_N^2$  with  $\bar{E}_x = 2.49(37)$  MeV, which was determined using

$$\bar{E}_x = \frac{\sum_i E_{xi} B(M1)_i}{\sum_i B(M1)_i}.$$
(9)

The contribution of the newly found M1 transitions is about 40% of the total observed strength. The mean excitation energy is in agreement with  $\bar{E}_x = 2.32$  MeV calculated using  $\bar{E}_x \approx 66\delta A^{-1/3}$  for scissors mode, where  $\delta$  is the deformation parameter and A is the mass number [1,6]. This formula successfully describes the variation of strength with deformation in a wide range of rare-earth nuclei. This observed M1 strength is presented in Table IV and the value is similar to the strengths of the scissors mode in  $^{236,238}$ U [9,10].

The predictions of the centroid of the scissors mode excitation energy in  $^{232}$ Th and  $^{236,238}$ U and their expected summed strengths using the sum-rule approach [8] and using QRPA calculation [12] are also shown in Table IV. The QRPA calculation predicts strength at energy above 3.3 MeV, which is not experimentally observed. Thus, it overestimates the summed *M*1 strength and the sum-rule prediction underestimates the summed *M*1 strength.

We observe a fragmentation of the M1 strengths spread from 2.0 to 3.3 MeV. This is consistent with the general trend of QRPA calculations, which predict M1 strengths distributed among 22 1<sup>+</sup> states with 16 of the predicted transitions having strength  $\leq 0.15 \ \mu_N^2$ . However, there are some differences between the data and the details of the calculations that can be most likely attributed to the fragmentation of the strength into transitions that are below the present detection limit. The spreading of M1 strength observed for  $^{232}$ Th is similar to that in the other actinides [9,10] and in the rare-earth nuclei [19,20].

The summed E1 transition strength of  $3.28(69) \times 10^{-3} e^2$  fm<sup>2</sup> is contained in 12 newly observed states with  $\bar{E}_x = 3.69(77)$  MeV. A considerable E1 strength is predicted

	Experiment				Theory						
Target	<sup>232</sup> Th <sup>a</sup>	<sup>232</sup> Th <sup>b</sup>	<sup>235</sup> U <sup>c</sup>	$^{236}\mathrm{U}^\mathrm{d}$	<sup>238</sup> U <sup>e</sup>	<sup>232</sup> Th <sup>e</sup>	<sup>236</sup> U <sup>e</sup>	<sup>238</sup> U <sup>e</sup>	<sup>232</sup> Th <sup>f</sup>	<sup>236</sup> U <sup>f</sup>	<sup>238</sup> U <sup>f</sup>
Energy range (MeV)	2–4	1.9–2.4	2.2-2.8	1.8-3.2	2-2.6	2–3		2–4			
$\bar{E}_x$ (MeV) $\sum B(M1)(\mu_N^2)$	2.5(4) 4.3(6)	2.1(2) 2.6(3)	2.5(3) 3.6(13)	2.2(2) 2.9(2)	2.3(2) 3.2(2)	2.5 2.7(5)	2.6 5.4(17)	2.6 5.0(8)	2.6 5.0	2.6 6.1	2.7 5.7

TABLE IV. Comparison of experimental and calculated B(M1) strength in actinides.

<sup>a</sup>Present work.

<sup>b</sup>Reference [9].

<sup>c</sup>Reference [18].

<sup>d</sup>Reference [10].

<sup>e</sup>Reference [8].

<sup>f</sup>Reference [12].

in the energy range from 2 to 2.5 MeV, which is not experimentally observed. In this measurement, the *E*1 transitions start to appear at about  $E_x = 3$  MeV with some gradual increase in the concentration of the observed states with increasing excitation energy. This increase may arise from the tail of the giant dipole resonance or may represent the so-called pygmy *E*1 resonance observed previously in a wide range of nuclei.

In summary, NRF experiments on  $^{232}$ Th have been performed at the HI $\gamma$ S facility using 100% linearly polarized and nearly monoenergetic beams with energies from 2 to 4 MeV. High-quality beams allowed observation of more than 20 discrete deexcitations to the ground state and the branching transitions to the first excited state were identified for most of them. Considerable *E*1 strength was identified at excitation energies between 3 and 4 MeV. A total of 12 *E*1 and 10 *M*1 excitations are newly observed in this work. The observed *M*1 strength is in agreement with other actinides and the systematics of the scissors mode observed in even-even rare-earth nuclei.

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