

# Neutron decays of $^{13}\text{Be}^*$ to the $0_2^+$ state of $^{12}\text{Be}$

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We suggest that an appreciable portion of the  $1/2^-$  peak in a recent  $^{13}\text{Be}^* \rightarrow ^{12}\text{Be} + n$  experiment is actually due to  $5/2^+$  decays to the excited  $0^+$  state.

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## I. INTRODUCTION

A recent paper [1] studied the reaction  $^1\text{H}(^{14}\text{Be}, ^{13}\text{Be}^*)$  and detected the outgoing  $^{13}\text{Be}^*$  as  $^{12}\text{Be} + n$  coincidences, gating on the absence of a fast  $\gamma$  ray in  $^{12}\text{Be}$  of energy  $2.1(2^+)$  or  $2.7(1^-)$  MeV. They observed a peak at a  $^{12}\text{Be} + n$  relative energy of  $E_n = 0.51$  MeV with a width of 0.45 MeV (after correcting for experimental resolution). They identify this peak as a  $1/2^-$  state expected in this region. (The history is well summarized in Ref. [1].) They quote a single-particle (sp)  $l = 1$  width of 0.55 MeV for a resonance at this energy, implying a spectroscopic factor of 0.82.

## II. THE $1/2^-$ STATE

In any reasonable model of  $^{12}\text{Be}$ , the ground state (g.s.) is written, in an obvious notation, as

$$^{12}\text{Be}(\text{g.s.}) = A [^{10}\text{Be}_{\text{CK}}(\text{g.s.}) (\text{sd})^2] + B [^{12}\text{Be}_{\text{CK}}(\text{g.s.})],$$

where the subscript CK (for Ref. [2]) is used to denote pure  $p$ -shell structures. Various models give different values of  $A$ ,  $B$ , but most would have  $A \geq B$ . Our favorite wave function [3] has  $A^2 = 0.68$ ,  $B^2 = 0.32$ . The g.s. could contain a component of  $^{10}\text{Be}_{\text{CK}}(2^+) (\text{sd})_{2^+}^2$ , but it should be small, and we ignore it here. In our model, the excited  $0^+$  state is

$$^{12}\text{Be}(0_2^+) = -B [^{10}\text{Be}_{\text{CK}}(\text{g.s.}) (\text{sd})^2] + A [^{12}\text{Be}_{\text{CK}}(\text{g.s.})].$$

The first  $1/2^-$  state of  $^{13}\text{Be}$  is mostly

$$\begin{aligned} &\gamma [^{11}\text{Be}_{\text{CK}}(1/2^-) (\text{sd})_{01}^2] + \delta [^9\text{Be}_{\text{CK}}(1/2^-) (\text{sd})_{02}^4] \\ &+ \varepsilon [^9\text{Be}_{\text{CK}}(3/2^-) (\text{sd})_{22}^4]. \end{aligned}$$

where the double subscripts denote  $JT$ , where  $T$  is isospin. We expect the last two terms to be small. The spectroscopic factor for decay of this  $1/2^-$  state to the g.s. of  $^{12}\text{Be}$  by  $n$  emission is

$$\begin{aligned} &S [^{13}\text{Be}(1/2^-) \rightarrow ^{12}\text{Be}(\text{g.s.}) + n] \\ &= A^2 \gamma^2 S [^{11}\text{Be}(1/2^-) \rightarrow ^{10}\text{Be}(\text{g.s.}) + n]. \end{aligned}$$

The latter factor has the value [2] 0.60. Even with our large value of  $A^2$ , and even if  $\gamma^2$  is near unity, the limit on the expected value of  $S$  is thus  $S \leq 0.40$ , compared to 0.82 in Ref. [1]. Furthermore, our calculated sp width, in a Woods-Saxon well with  $r_0, a = 1.25, 0.65$  fm, is  $\Gamma_{\text{sp}} = 0.40$  MeV, implying  $S = 1.1$  [1]. The authors do state that if they analyze the upper part of their energy range differently (two  $d$  states rather than one), the experimental  $1/2^-$  width changes by

0.13 MeV. Even then,  $S$  would be 0.85 (with our sp width)—still more than twice the expected value. (See Table I.) Thus we conclude that a large portion of their  $1/2^-$  peak must contain another contribution that has another origin, which we now discuss.

## III. THE $5/2^+$ STATES

The first  $5/2^+$  state of  $^{13}\text{Be}$  should be

$$\begin{aligned} ^{13}\text{Be}(5/2_1^+) &= \alpha [^{12}\text{Be}_{\text{CK}}(\text{g.s.}) \times 1d5/2] \\ &+ \beta [^{10}\text{Be}_{\text{CK}}(\text{g.s.}) (\text{sd})_{5/2}^3]. \end{aligned}$$

Another competing component is  $^{12}\text{Be}(2^+)2s1/2$ , which could be appreciable, but we omit it here because we want to keep things simple and because this component has no direct  $n$  decay to the  $0^+$  states of  $^{12}\text{Be}$ . We return to this point later. In a two-state model, the next  $5/2^+$  state would be

$$\begin{aligned} ^{13}\text{Be}(5/2_2^+) &= -\beta [^{12}\text{Be}_{\text{CK}}(\text{g.s.}) \times 1d5/2] \\ &+ \alpha [^{10}\text{Be}_{\text{CK}}(\text{g.s.}) (\text{sd})_{5/2}^3]. \end{aligned}$$

In both cases, the  $(\text{sd})^3$  configuration is primarily a combination of  $s_0^2 d$  and  $d^3$ . In the simplest two-state model for the  $0^+$  and  $2^+$  states, we would expect  $\beta^2/\alpha^2$  to be about 2 (actually near  $0.68/0.32$ ; see earlier). Mixing of the  $2^+ \times 2s1/2$  component into these two  $5/2^+$  states would reduce both  $\beta$  and  $\alpha$  but should not drastically alter the ratio.

We have computed the decays of this second  $5/2^+$  state to the g.s. of  $^{12}\text{Be}$  and to the excited  $0_2^+$  state at 2.24 MeV. We find that for a wide range of values of  $\beta/\alpha$ , the decay to

TABLE I. Properties of  $1/2^-$  resonance in  $^{13}\text{Be}$  (energies and widths in MeV).

$E_n$	$\Gamma_{\text{exp}}^a$	$\Gamma_{\text{sp}}$	$S = \Gamma_{\text{exp}}/\Gamma_{\text{sp}}$
0.51	0.45	0.55 <sup>b</sup>	0.82
		0.40 <sup>c</sup>	1.1
0.49 <sup>d</sup>	0.32 <sup>d</sup>	0.38 <sup>c</sup>	0.84
Theory <sup>e</sup>			$\leq 0.41$

<sup>a</sup>Reference [1], after correcting for experimental resolution.

<sup>b</sup>Quoted in Ref. [1].

<sup>c</sup>Our value.

<sup>d</sup>Alternative analysis in Ref. [1].

<sup>e</sup> $S = A^2 \gamma^2 S [^{11}\text{Be}_{\text{CK}}(1/2^-) \rightarrow ^{10}\text{Be}_{\text{CK}} + n]$  (see text).

$0_2^+$  is highly favored, even with the limited phase space. For  $1 < \beta^2/\alpha^2 < 4$ , the BR is less than unity. We propose that this  $5/2_2^+$  state is near  $E_n = 2.8$  MeV so that decay to the  $0_2^+$  state would contribute to the 0.51 MeV peak. One of the analyses in Ref. [1] had a second  $d$  state at about 2.9 MeV. In our calculations, the sp width for  $l = 2$  is 34 keV for  $E_n = 0.51$  MeV and 1.1 MeV for  $E_n = 2.8$  MeV. Thus, from phase space, the g.s. decay branch is favored by more than a factor of 30. But the structure goes very heavily in the other direction. In Fig. 1, we plot the ratio  $S\Gamma_{sp}/S'\Gamma'_{sp}$ , where  $S$  and  $\Gamma_{sp}$  refer to the decay of the second  $5/2_2^+$  state to the g.s., and  $S'$  and  $\Gamma'_{sp}$  refer to the  $0_2^+$  state. The  $S$ 's are computed from the wave functions given earlier. Note that for a very wide variation in the wave function, the  $0_2^+$  decay is favored. Other components in the wave functions will undoubtedly fill in the minimum somewhat, but the principal feature should remain. The experimental setup in Ref. [1] could not rule out decays to  $0_2^+$  because of its long mean life; rather they argued that the 0.5 MeV peak could not be due to decays of a  $\sim 2.7$  MeV state to  $0_2^+$  because such decays should be accompanied by much stronger (on penetrability grounds) decays to the g.s.. If we are correct and the  $5/2_2^+$  states have the structure suggested here, these g.s. decays are severely inhibited, and their argument is therefore not valid.

The width of a peak arising from these proposed decays to  $0_2^+$  would be nearly all resolution width. For the proposed decays to the excited  $0^+$  state to cause a widening of the 0.5 MeV peak, their energy should be slightly different from the energy of the  $p$ -wave resonance. If so, it might be possible

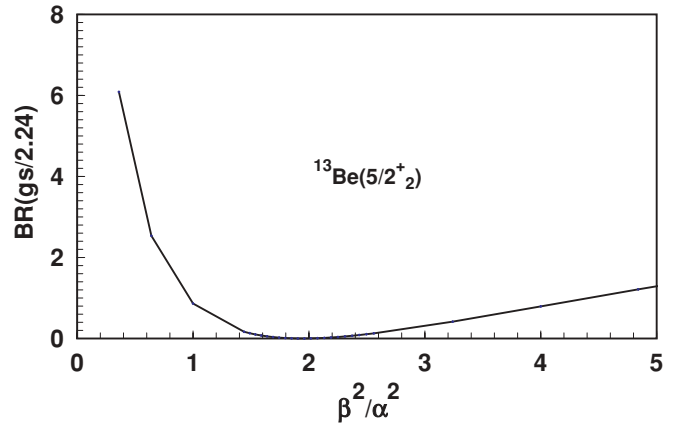


FIG. 1. For the second  $5/2_2^+$  state of  $^{13}\text{Be}$ , the ratio of widths for decay to the g.s. and excited  $0^+$  state is plotted vs  $\beta^2/\alpha^2$ , the ratio of sp to  $(sd)^3$  in the  $5/2_2^+$  state.

to observe different momentum distributions for the left and right halves of the 0.5 MeV peak in the data of Ref. [1]. The decays suggested here should have a  $d$ -wave momentum distribution.

There is also the question of forming these  $5/2_2^+$  states from  $^{14}\text{Be}$ . With a reasonable wave function of  $^{14}\text{Be}(\text{g.s.})$ , we expect that the  $5/2_2^+$  state will have about 50%–70% of the strength of  $5/2_1^+$  in the breakup of  $^{14}\text{Be}(\text{g.s.})$ .

We think it would be very interesting to look for decays of  $^{13}\text{Be}^*$  to the excited  $0^+$  state of  $^{12}\text{Be}$ .

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